

# INTRODUCTION TO COMPILER

Topic \_\_\_\_\_

Date 15 Sep 2021

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COMPILER:- A compiler converts high-level language into assembly language.

Step-1:- HLL → Removal of Pre-processors.

↓ pure HLL

Step-2:- Now, pure HLL will go to the compiler.

↓ Assembly lang.

Step-3:-

↓ Assembles

↓ relocatable code.

Step-4:-

↓ Linker/loader

connects secondary memory add. to primary

↓ machine code.

## PHASES OF COMPILER:-

HLL

lexical analysis

from lexical to intermediate  
- dialect is known as  
front-end of a compiler.

Syntax analysis

Semantic analysis

Symbol Table

Error

Handler

Intermediate code Generator

Code optimization

Target code generator

Assembly language

Front-end

Back-end

M/R

Source code

analysis

Synthesis

Machine code

Intermediate

Q1. LEXICAL ANALYSIS:- (Tokenization of program will happen).  
Let us have a C program.

Eg-1

int max (x, y)

int x, y;

/\* find max. of x & y \*/

{ return (x > y ? x : y); }

lexical analysis is the first phase of the compiler also known as scanner. It converts H-L input program into sequence of tokens.

→ Create tokens:-

1 2 3 4 5 6 7  
| Pnt | max | ( | x | , | y | ) |

Calculate the no. of tokens generated after lexical analysis.

8 9 10 11 12  
int | x | , | y | ;  
/\* find max. of x and y \*/; // comment  
return | ( | x | > | y | ? | x | : | y | ) | ;

25

3

Total tokens :- 25

\* Note: In C, the space is also a token.

Eg-2

1 2 3 4 5 6 7 8  
printf( " %d \n ", | x | );  
style token

\* The whole string will be treated as a single token.

Total = 8

Eg-3

⇒ (1.25) → 1 token

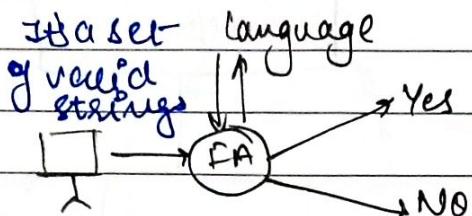
No. is replaced by 1.



\* If, while doing lexical analysis any undefined symbol is found, it shows error.

- lex is a tool used in linux for lexical analysis.
- yacc (from frontend we have this tool).
- yet another compiler compiler

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INPUT ALPHABETS:-

Eg,  $\Sigma = \{a, b\}$

$L_1 = \text{Set of all strings with length "2"}$ .

$$L_1 = \{ab, aa, bb, ba\}$$

Eg,  $\Sigma = \{a-b, A-B, 0-9, \text{special characters?}\}$

Input Alphabets inc.

length  $\rightarrow \Sigma^1 = \{a, b\}$

$\Sigma^2 = \Sigma^1 \text{ contact } \Sigma^1 \Rightarrow \{a, b\} \cup \{a, b\} \cup \dots \text{ etc on.}$

$\Sigma^0 = \{\epsilon\}$

$\Sigma^\infty \rightarrow$  Kleen closure

$\Sigma^\infty = \Sigma^0 \cup \Sigma^1 \cup \Sigma^2 \dots$

contact operation.

$\Sigma^+ = \Sigma^1 \cup \Sigma^2 \cup \dots$

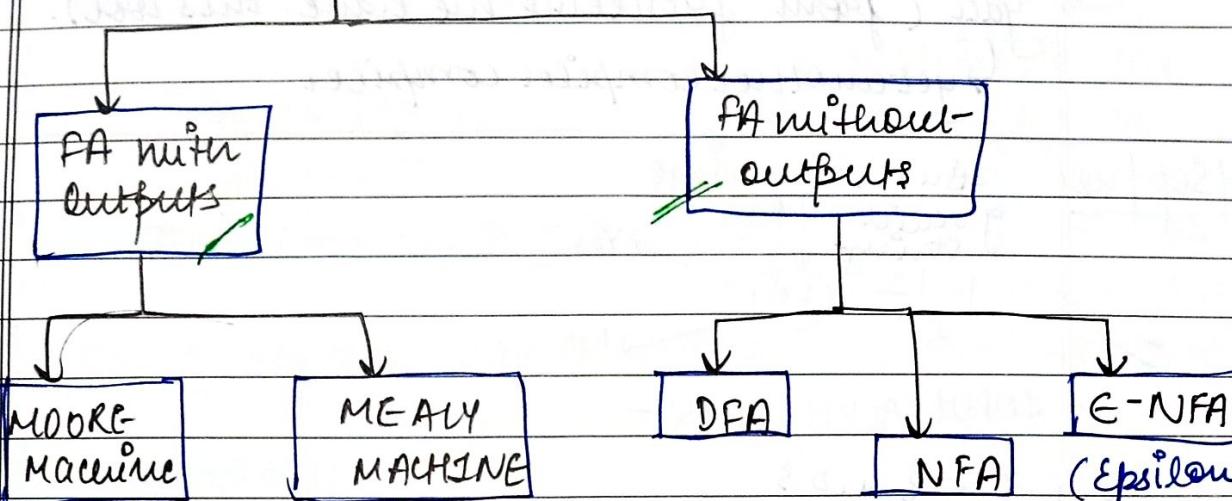
$\Sigma^+ = \Sigma^1 \cup \Sigma^2 \cup \dots$  (we don't have  $\Sigma^0$ )

if any unknown symbol Input alphabet is detected, then it will throw an error.

FINITE AUTOMATA:-

- It is an abstract machine, which is useful to check valid strings from our program.  
(H.I.L)

## \* CLASSIFICATION OF FA :-



\* DFA :- (in this we have only one path)

(Epsilon non-deterministic finite automata)

→ Associated tuples :- parameters or Attributes

5-TUPLES

- ① Q
- ② Σ
- ③ F
- ④ q₀
- ⑤ δ

- ① Q : (Set of all states)
- ② Σ : (Input Alphabet)
- ③ F : (Set of final states)
- ④ q₀ : (Initial State)
- ⑤ δ : (Transition from one state to another).

" $Q \rightarrow \Sigma \Rightarrow Q'$ "

$\downarrow$  one state  $\searrow$  read input  $\nearrow$  another state

PROBLEM :-

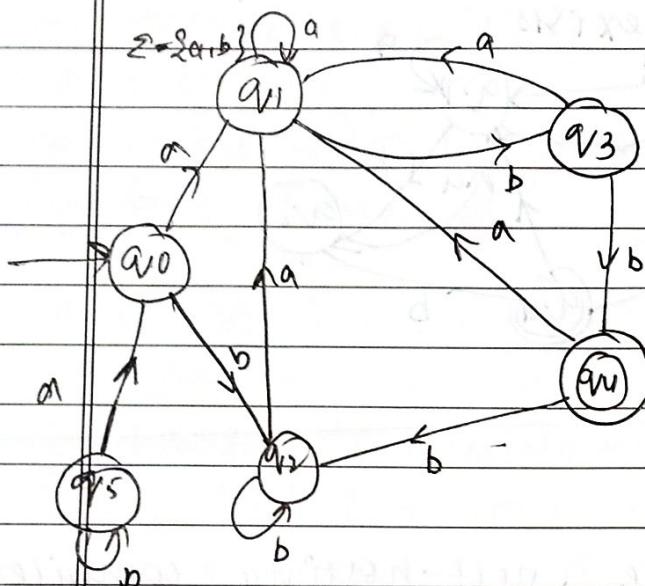
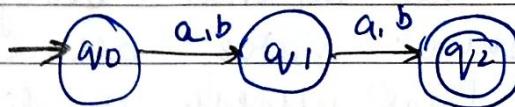
Create a DFA which accepts all strings over the Input Alphabet ( $\Sigma$ )  $\Sigma = \{a, b\}$  with length "2".

SOLUTION :-

Given :-  $\Sigma = \{a, b\}$

$$L = \{aa, bb, ab, ba\}$$





**DFA MINIMIZATION**  
(10marks)

**Step-1** :- Try to find all unreachable states in DFA & remove (delete) them & all its corresponding transitions. i.e.  $\cancel{q_5}$

**Step-2** :- Draw state transition diagram<sup>(STD)</sup> of the given DFA.

	a	b
$q_0$	$q_0, q_1$	$q_1$
$q_1$	$q_1$	$q_1, q_3$
$q_2$	$q_1$	$q_1, q_2$
$q_3$	$q_1, q_2$	$q_1, q_4$
$q_4$	$q_1$	$q_1, q_2$

	a	b
$q_1$	$q_1, q_2$	$q_2$
$q_2$	$q_2$	$q_2, q_3$
$q_3$	$q_2, q_3$	$q_3$
$q_4$	$q_2$	$q_2$
$q_5$	$q_2$	$q_2$
$q_6$	$q_2$	$q_2$
$q_7$	$q_2$	$q_2$

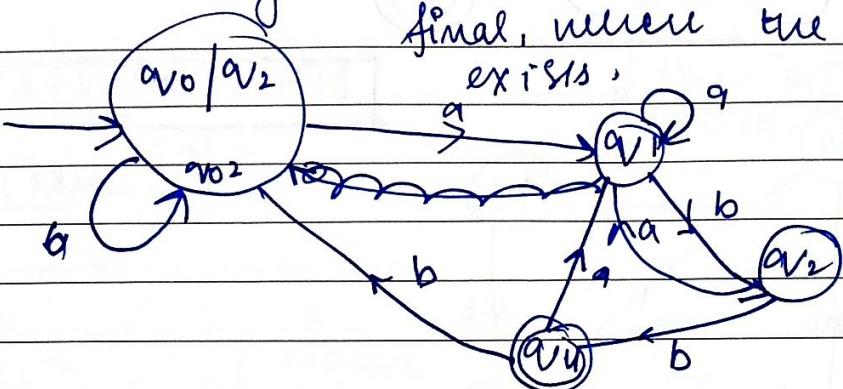
**Step-3** :- write all the states in a form of 2 set of all non-final states? 3 set of final states?

$$\Rightarrow \{q_0, q_1, q_2, q_3\} \cup \{q_4\} \quad (\text{0-equivalent})$$

marking  
marking

$$\begin{aligned} &\{q_0, q_1, q_2\} \cup \{q_3\} \cup \{q_4\} \quad (\text{1-equivalent}) \\ &\{q_0, q_2\} \cup \{q_4\} \cup \{q_3\} \quad (\text{2-equivalent}) \end{aligned}$$

Step-4 :- we make all separate set of states as a single state. make all the states as final, unless the final state exists.

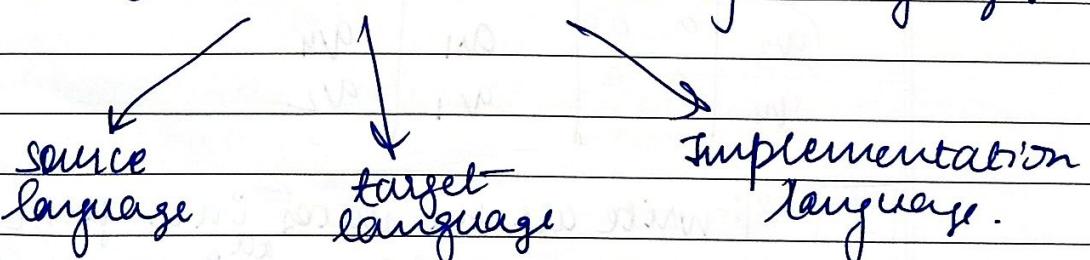


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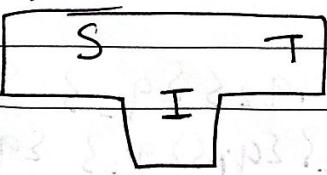
### BOOTSTRAPPING:-

- It is used to produce a self-hosting compiler. Self-hosting compiler is a type of compiler that can compile its own source code.
- Bootstrap compiler is used to compile the compiler & then you can use this compiled compiler to compile everything else as well as further version of itself.

A compiler can be characterized by 3 languages.

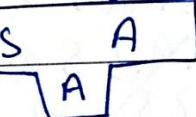


The T-diagram shows a compiler  $S \xrightarrow{T} I$  for source S, Target T, implemented in I.



(1)

Create a compiler  ${}^S C_A^A$  for subsets,  $S$  of the desired lang. L using language "A" and that compiler runs on machine A.



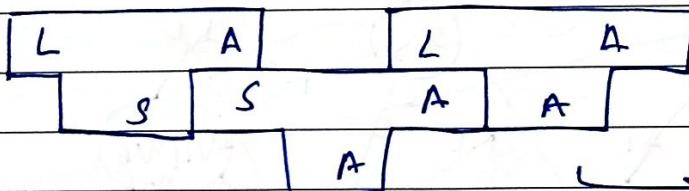
(2)

Create a compiler  ${}^L C_S^A$  for language L written in a subset of S.



(3)

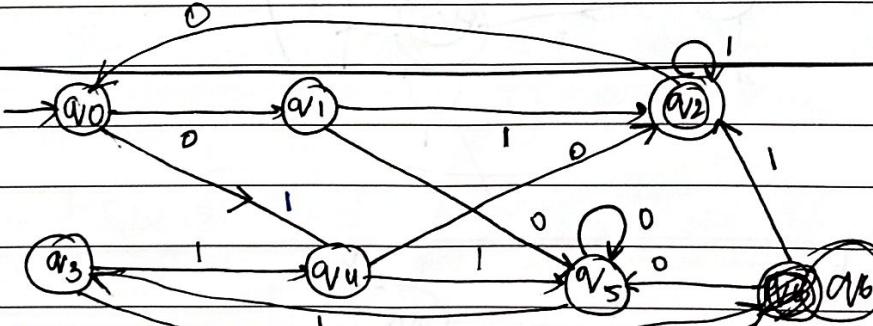
Compile  ${}^L C_S^A$  using the compiler  ${}^S C_A^A$  to obtain  ${}^L C_A^A$ .  ${}^L C_A^A$  is a compiler of language L, which runs a machine A and produces code for machine A.



Bootstrapping.

22/sep/2021

Mimic the DFA.



DFA	$q_0$	$q_1$	$q_4$
$q_0$			
$q_1$			
$q_2$			
$q_3$			
$q_4$			
$q_5$			
$q_6$			

$\rightarrow$  Non-final set  $\Sigma$  final set?

$$= \Sigma q_0, q_1, q_3, q_4, q_5, q_6 \Sigma q_2$$

$$= \Sigma q_0, q_3, q_4, q_5, q_6 \Sigma q_2$$

$$= \Sigma q_3, q_4, q_5, q_6 \Sigma q_0 \Sigma q_1 \Sigma q_2$$

$$= \Sigma q_3, q_5, q_6 \Sigma q_0 \Sigma q_1 \Sigma q_2$$

$$= \Sigma q_3, q_5, q_6 \Sigma q_0 \Sigma q_1 \Sigma q_2$$

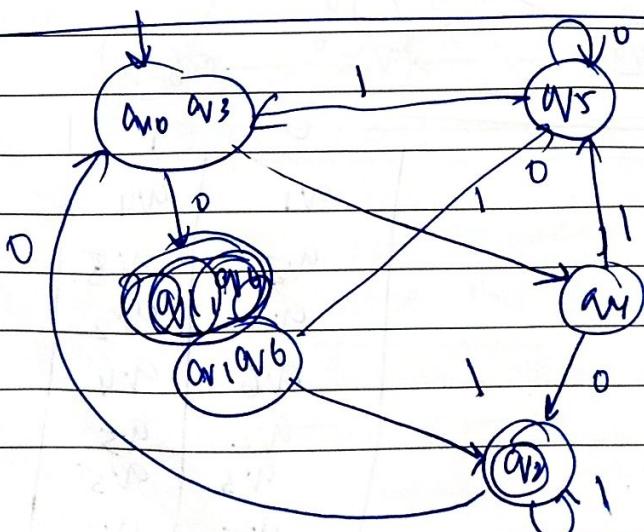
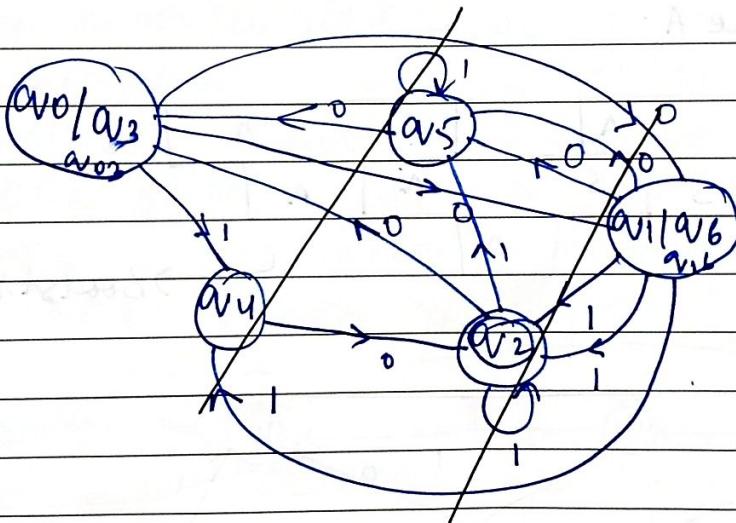
$$= \Sigma q_6 \Sigma q_3, q_5 \Sigma q_4$$

$$= \Sigma q_0, q_3, q_5 \Sigma q_1, q_6 \Sigma q_4 \Sigma q_3 \Sigma q_2$$

$$\Rightarrow \Sigma q_0, q_3 \Sigma q_5 \Sigma q_1, q_6 \\ \Sigma q_4 \Sigma q_3 \Sigma q_2$$

$q_0$	a	q
$q_1$	a	b
$q_3$	a	a
$q_4$	b	a
$q_5$	a	a
$q_6$	a	b

$q_0$	b	c
$q_3$	b	c
$q_5$	a	a



GRAMMERS:-

↓  
language

Input Symbols (Strings)

e.g. - ~~start  $\rightarrow$  AA~~  
 $\checkmark A \rightarrow a \mid b$  → production  
 $\Sigma = \{a, b\}$

$L = \{ \text{set of all strings of length } 2^k \}$   
 $L = \{aa, bb, ab, ba\}$

→ 4 types

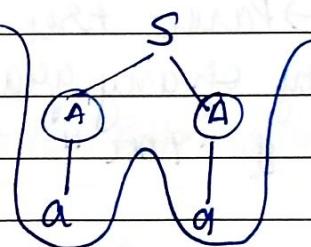
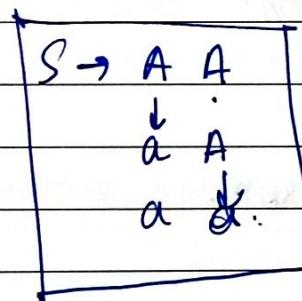
↓

→ Variables → V

→ Terminals → T

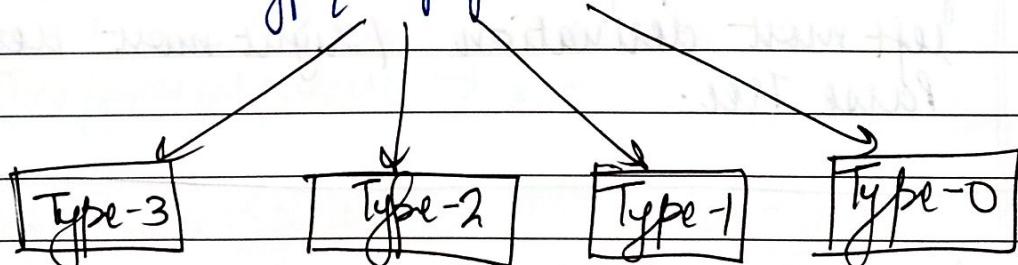
→ Production → P

→ Start Symbol → S



CLASSIFICATION OF GRAMMERS:-

There are 4 types of grammars:-

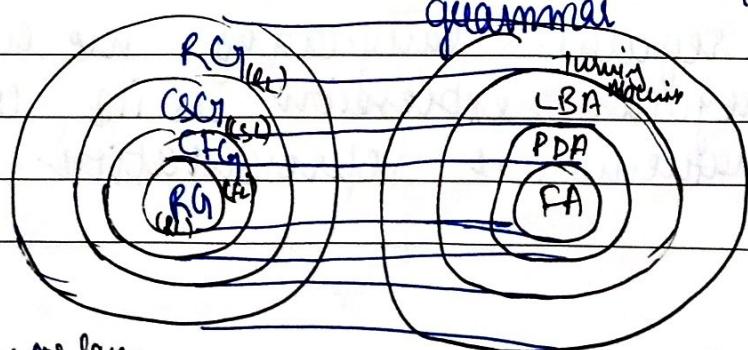


regular  
grammar

Context free  
grammar.

Context  
sensitive  
grammar

Recursive  
grammar.



SL → Regular lang.

OBG → Linear  
Bounded  
PDA. Justification  
Automata

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## UNIT-1 SUMMARY

- (1) Introduction to compiler / compiler overview.
- (2) Compiler Phases (From : lexical to target code generation)
- (3) Bootstrapping (concept)
- (4) Finite Automata (including it's classification)
- (5) Formal Grammar
- (6) Minimization of DFA.
- (7) Context free Grammar.
- (8) String Derivation
  - left most derivation.
  - right most derivation.
  - Parse tree.
- (9) Ambiguity of any grammar.
- (10) "LEX" & "YACC" Tool Jutor.

### NOTE

:- In order to derive a string from a given grammar , if we have more than one left most derivation / right most derivation / Parse Tree .

\* Regular Expressions:- ~~forget~~ It's a mathematical representation of a given language

→ for regular languages we have this regular expression as its corresponding mathematical representation.

\* Basic Operations on Regular expressions:-

- (1) Union (+)
- (2) Concat (-)
- (3) Kleen Closure (\*)
- (4) Positive closure (+)

\* Basic primitives of regular expressions:-

Let's assume it is represented by ' $\lambda$ ', then:-

- (i)  $\lambda = \emptyset = \{\}$
- (ii)  $\lambda = \epsilon$
- (iii)  $a \in \Sigma, \Sigma = \{a, b\}$

\* Operations applied on regular expression:-

If we 2 regular exp. of  $\lambda_1, \lambda_2$ , then:-

- (i) union  $\rightarrow \lambda_1 + \lambda_2$
- (ii) concat  $\rightarrow \lambda_1 \cdot \lambda_2$
- (iii) Kleen Closure  $\rightarrow \lambda_1^*$
- (iv) positive closure  $\rightarrow \lambda_1^+$

\* Regular Expression

$\emptyset$   
 $\epsilon$   
 $a$   
 $a^*$   
 $a^+ | a \cdot a^+$

Language

$\Sigma^3$   
 $\Sigma^{\epsilon}$   
 $\Sigma a^3$   
 $\Sigma \epsilon, a, aa, aaa \dots$   
 $\Sigma a, aa \dots$



at least one should be true.

$\Sigma \epsilon, a, b, ab, ba, \dots$

$$b(a)^* = \{ b, ba, baa, baaa \dots \}$$

$$(ab+ba)^* = \{ ab, ba, abba, baab \dots \}$$

Ques  $\Rightarrow$  Represent this lang. to a regular expression:-  
 Set of all strings of length exactly 2  
 on input symbols  $\Sigma = \{a, b\}$ .

$$\Rightarrow L = \{ aa, bb, ab, ba \}$$

$$a^2 + b^2 + ab + ba$$

$$a(a+b) + b(a+b)$$

$$(a+b)(a+b)$$

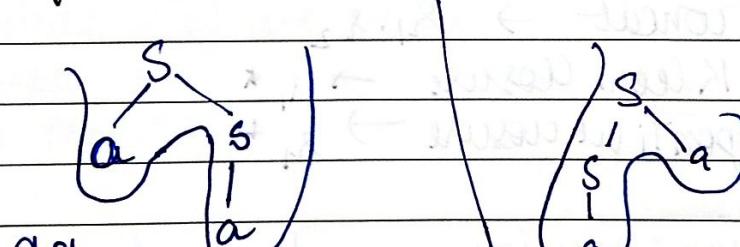
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### EXAMPLES OF UNIT-1

(i) Questions on ambiguity.

$\Rightarrow$  i)  $S \rightarrow aS | Sa | a$  - find out whether this grammar is ambiguous or not:

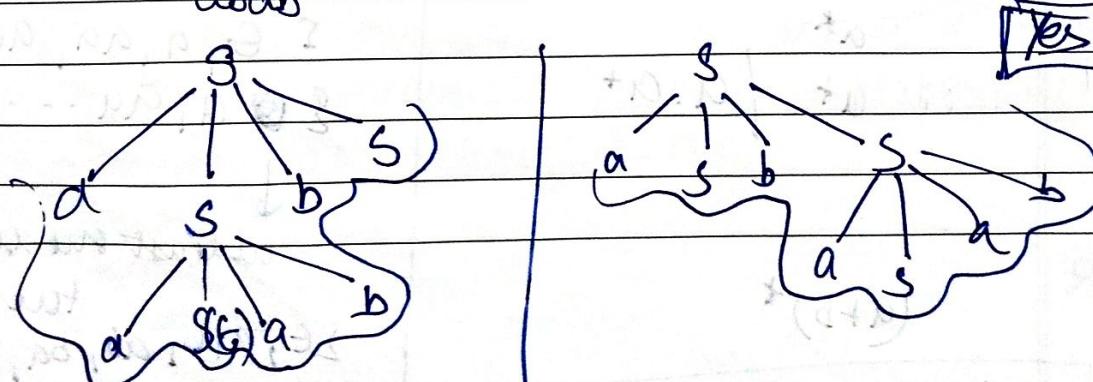
$\Rightarrow$



Yes

(ii.)  $\bullet S \rightarrow aSbS | bSaS | \epsilon$

abab



Yes

(iii)  $R \rightarrow R + R \mid RR \mid R^* \mid a \mid b \mid c$   
 $a+bc$

[Yes]

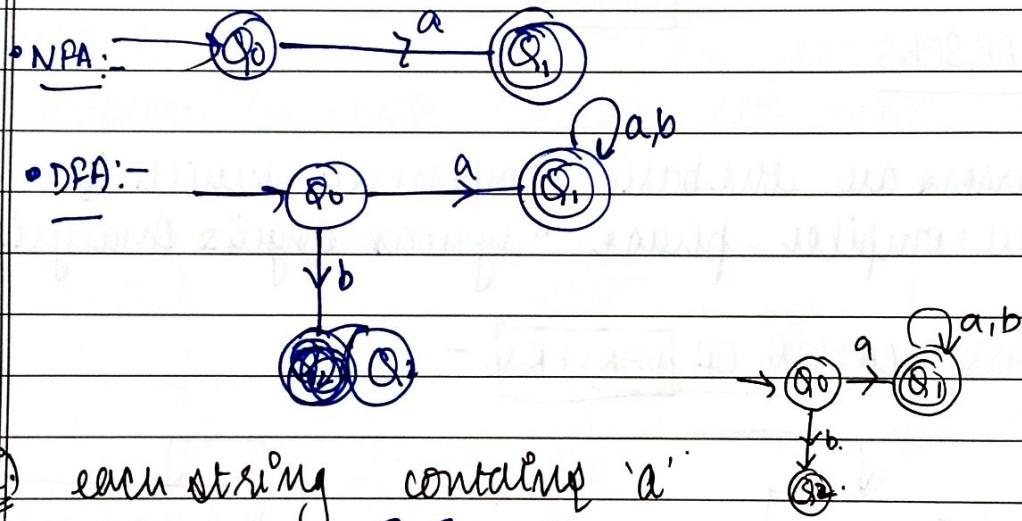
d. Questions on constructing a DFA.

i. construct a minimal DFA, which accept set of all strings over input alphabet  $a, b$ , where each string starts with small  $a$ .

$\Rightarrow$

$$\Sigma = \{a, b\}$$

$$L = \{a, ab, abb, \dots\}$$



(ii) each string containing 'a'

$$\Sigma = \{a, b\}$$

$$L = \{a, ab, ba, aab, \dots\}$$

(iii) ending with small  $a$ .

(iv) starts with  $ab$ .

~~(iv) starts with a & ends with b.~~

(v) starts with a & ends with b.  
 $a(a+b)^*b$ .

(vi) starts & end with diff. symbol.  
 $a(a+b)^*b + b(a+b)^*a$

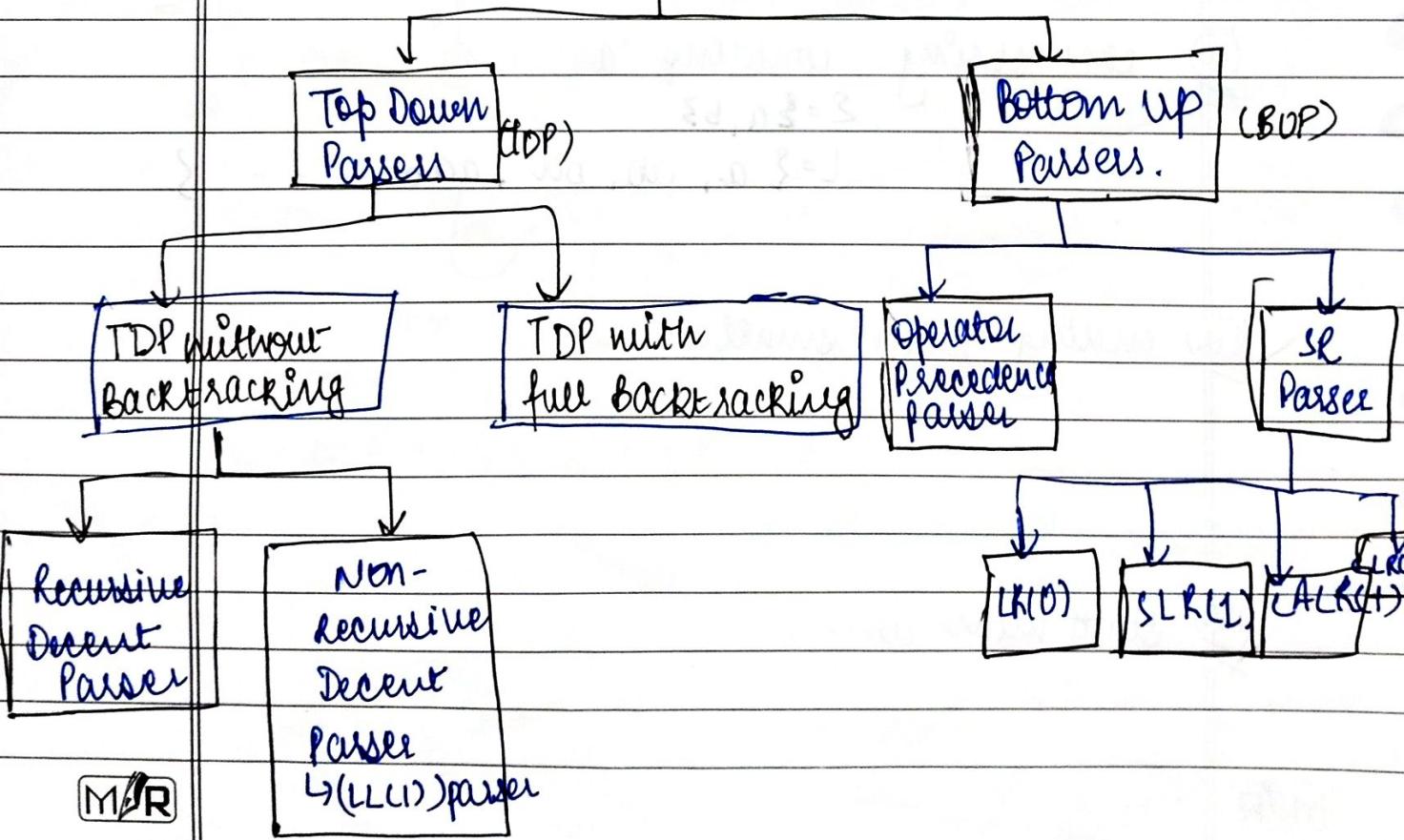
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## UNIT-2

### PARSERS

PARSERS are the basic component which is used in the compiler phase "syntax analysis".

#### CLASSIFICATION OF PARSERS:-



**[NOTE]**

- In all top-down parsers we follow leftmost derivation. ("It follows "what to use" approach).
- On other hand bottom-up parser follows rightmost derivation in reverse order. (It follows "when to reduce" approach).

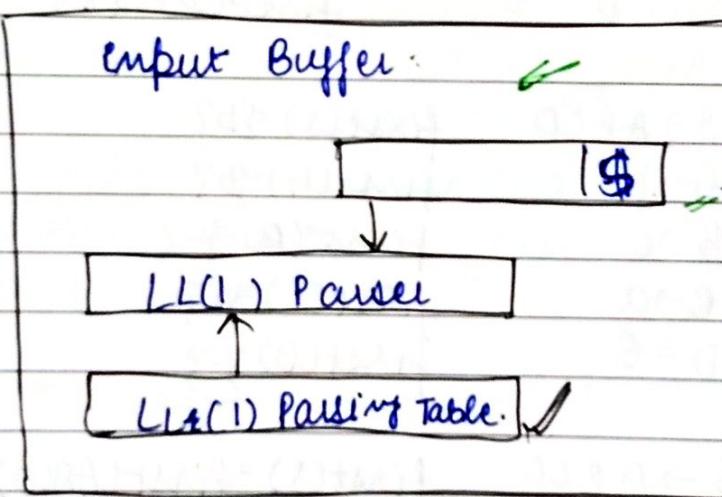
\*

**LL(1) PARSER:-**

• L: left to right.

• L: left most derivation

• (1): no. of alphabets to be scanned. It is also known as look ahead symbol.



- Input buffer: - string to be scanned.
- Stack: - The data structure, which is used by LL(1) parser to create its parsing table.
- \$: - end of string or top of the stack.
- In order to create LL(1) parsing table we need to know the concept of:  $\text{First}( )$  /  $\text{Follow}( )$

→ CONCEPT OF FIRST() & FOLLOW():-

(1) If we have a variable in our grammar from the variable, if we try to derive all strings, then whatever is coming at the first place is known as FIRST() of that variable.

(2) Eg-1  $S \rightarrow aABC D$ .  $\text{first}(S) = \text{first}(aABC D) = \text{first}(a) = \{a\}$   
 $A \rightarrow b$ .  $\text{first}(A) = \{b\}$   
 $B \rightarrow c$ .  $\text{first}(B) = \{c\}$   
 $C \rightarrow d$ .  $\text{first}(C) = \{d\}$   
 $D \rightarrow e$ .  $\text{first}(D) = \{e\}$

(3) Eg-2  $S \rightarrow ABCD$   $\text{first}(S) = \{b\}$   
 $A \rightarrow b$   $\text{first}(A) = \{b\}$   
 $B \rightarrow c$   $\text{first}(B) = \{c\}$   
 $C \rightarrow d$   $\text{first}(C) = \{d\}$   
 $D \rightarrow e$   $\text{first}(D) = \{e\}$

(4) Eg-3  $S \rightarrow A B C D$   $\text{first}(S) = \text{first}(A B C D) = \text{first}(A) \cup \text{first}(B) \cup \text{first}(C) \cup \text{first}(D) = \{b, c, d\}$   
 $A \rightarrow b \mid \epsilon$   $\text{first}(A) = \{b, \epsilon\}$   
 $B \rightarrow C$   $\text{first}(B) = \{c\}$   
 $C \rightarrow d$   $\text{first}(C) = \{d\}$   
 $D \rightarrow e$   $\text{first}(D) = \{e\}$

→  $\text{first}(ABC D) / \text{first}(BC D)$

if  $B \rightarrow C \mid \epsilon$

$C \rightarrow d \mid \epsilon \rightarrow \text{first}(S) = \{b, c, d, e, \{ \epsilon \}\}$   
 $D \rightarrow e \mid \epsilon$

→ CONCEPT OF FOLLOW( ): -

- String is always in the format of  $S\$$  where ' $S$ ' is string ' $\$$ ' is end string.
- Imp: follow() never contains ' $\epsilon$ ', bcoz if nothing is followed by variable, then it must be ' $\$$ ' at the end.
- STEPS TO FIND OUT FOLLOW:-

- (1) Follow() of start symbol(s) always consists atleast  $\$$ .
- (2) Look other variables including start symbol to the R.H.S of the production.
- (3) Evaluate follow() of each variable by finding the first fun. of the upcoming string.
- (4) If variable is in the end, then follow() of that variable will be the follow() of the L.H.S.

$$G \rightarrow S \rightarrow \underline{ABCD}$$

$$\underline{A} \rightarrow A \underline{B} \mid E$$

$$B \rightarrow C$$

$$C \rightarrow d \mid e$$

$$D \rightarrow e \mid \epsilon$$

$$\Rightarrow \text{follow}(S) = \{ \$ \}$$

$$\text{follow}(A) = \text{first}(B \cup D) \Rightarrow \text{first}(B) = \{ C \}$$

$$\text{follow}(B) = \text{first}(C \cup D) \Rightarrow \text{first}(C) = \{ d \}$$

$$\text{follow}(C) = \text{first}(D) = \{ e \}$$

$$\text{follow}(D) =$$

$$\text{follow}(S)$$

Q →

$$S \rightarrow ABCDE$$

$$A \rightarrow a/\epsilon$$

$$B \rightarrow b/\epsilon$$

$$C \rightarrow c\}$$

$$D \rightarrow d/\epsilon$$

$$E \rightarrow e/\epsilon$$

$$\text{first}(A) =$$

$$\text{first}(A) = \{a, \epsilon\}$$

$$\text{first}(B) = \{b, \epsilon\}$$

$$\text{first}(C) =$$

find First & Follow.

→

~~Scared~~

### \* EXAMPLES ON FIRST() & FOLLOW():-

①

$$S \rightarrow \underline{ABCDE}$$

$$A \rightarrow a/\epsilon$$

$$B \rightarrow b/\epsilon$$

$$C \rightarrow c\}$$

$$D \rightarrow d/\epsilon$$

$$E \rightarrow e/\epsilon$$

$$\Rightarrow \text{first}(S) = \text{first}(ABCDE) = \text{first}(A) = \{a, \epsilon\}$$

$$\text{first}(A) = \{a, \epsilon\} \quad \text{So } a, \text{ first}(B) \text{ is } \{\epsilon\}$$

$$\text{first}(B) = \{b, \epsilon\}$$

$$\text{first}(C) = \{c\}$$

$$\text{first}(D) =$$

$$\text{first}(E) =$$

$$\text{first}(ABC)$$

$$(BC)$$

$\text{first}(S) = \text{first}(ABCDE) = \text{first}(A) = \{a, b, c\}$   
 $\text{first}(A) = \text{first}(aBCDE), \text{first}(BCDE) = \{a, B, C\}$   
 $\text{first}(B) = \text{first}(B CDE), \text{first}(CDE) = \{b, E\}$   
 $\text{first}(C) = \text{first}(CDE) = \{c, D, E\}$   
 $\text{first}(D) = \text{first}(d CDE), \text{first}(E) = \{d, \emptyset, E\}$   
 $\text{first}(E) = \text{first}(E BCDE), \text{first}(E) = \{e, E\}$

$\text{follow}(S) = \$$

$\text{follow}(A) = \{b, c\}$

$\text{follow}(B) = \{c\}$

$\text{follow}(C) = \{d, e, \$\}$

$\text{follow}(D) = \{e\}$

$\text{follow}(E) = \{\$\}$

(2)

$S \rightarrow BB|Cd$

$B \rightarrow aB|E$

$C \rightarrow cC|e$

$\text{first}(S) = \text{first}(BB), \text{first}(BB) = \{a, B, E\} \{a, B, E\}$

$\text{first}(B) = \text{first}(aB), \text{first}(aB) = \{a, E\}$

$\text{first}(C) = \text{first}(cC), \text{first}(cC) = \{c, E\}$

$\text{follow}(S) = \$$

$\text{follow}(B) = \$, B$

$\text{follow}(C) = \$, B$

?

$\hookrightarrow (\text{follow}(C) \text{ & } \text{follow}(E))$

$\Rightarrow E \rightarrow TE'$   
 $E \rightarrow +TE'|e$   
 $T \rightarrow FT'$   
 $T' \rightarrow *FT'|e$   
 $F \rightarrow id$

{ Starting symbol }

$\Rightarrow first(E) = first(TE') = first(T) \cup first(E) \cup \{id, C\} \quad \checkmark$   
 $first(E') = first(+TE') \mid first(E) = \{+, e\} \quad \checkmark$   
 $first(T) = first(FT') = first(F) = \{id, C\} \quad \checkmark$   
 $first(T') = first(*FT') \mid first(E) = \{* , e\} \quad \checkmark$   
 $first(F) = first(id) \mid first(E) = \{id, C\} \quad \checkmark$

$follow(E) = \{ \$, \$, \$, \}, \text{ follows}$   
 $follow(E') = \{ \$, \$, \$, \$, \}, \{ \$, \}$   
 $follow(T) = \{ \$, \$, \$, \$, \$, \$, \}, \{ +, \$, \}$   
 $follow(T') = \{ \$, \$, \$, \$, \$, \$, \$, \}, \{ +, \$, \}$   
 $follow(F) = \{ \$, \$, \$, \$, \$, \$, \$, \$, \}, \{ *, +, \$, \}$

## \* LL(1) PARSER & ITS CORRESPONDING PARSING TREE

We will explain this concept through an example.

(10)

$$\begin{array}{l} E \rightarrow TE' \\ E' \rightarrow +TE' | E \\ T \rightarrow FT' \\ T' \rightarrow *FT' | E \\ F \rightarrow id | (E) \end{array}$$

first(T)

first

first(T') - (\*, E)

first(F) - (id, ( ))

Find out whether the above given grammar is LL(1) or not.

⇒ Step-1:- Firstly we need to calculate first() & follow() of the given grammar.

<u>Production</u>	<u>first()</u>	<u>follow()</u>
$E \rightarrow TE'$	{id, (}	{\$, )}
$E' \rightarrow TE'   E$	{+, E}	{\$, )}
$T \rightarrow FT'$	{id, (}	{+, \$, )}
$T' \rightarrow *FT'   E$	{*, E}	{+, \$, )}
$F \rightarrow id   (E)$	{id, (}	{*, +, \$, )}

• Step-2:- After calculating first() & follow() now we'll draw (LL) parsing table.

	+	*	id	(	)	\$
E			$E \rightarrow TE'$	$E \rightarrow TE'$		
E'	$E' \rightarrow TE'$				$E \rightarrow E$	$E' \rightarrow E$
T			$T \rightarrow FT'$	$T \rightarrow FT'$		
T'	$T' \rightarrow *FT'$	$T' \rightarrow *FT'$			$T' \rightarrow E$	$T \rightarrow E$
F			$F \rightarrow id$	$F \rightarrow (E)$		

- In case of normal production we take first(). But in case of E we check for follow().
- for adding the values in table we check the corresponding first() or follow() (in case of E) values & add the production there.
- Since, bcoz we only have single entry in whole LL(1) parsing tree, ~~there~~ ∴ this grammar is LL(1) grammar.

(20) Find out whether this grammar is LL(1) or not.  
 $S \rightarrow aSbS \mid bS aS \mid E$

⇒ Step-1:-

$S \rightarrow aSbS \mid bS aS \mid E$	first()	follow()
	{a, b, E}	{b, a, \$}

Step 2:-

S	a $S \rightarrow aSbS$ $S \rightarrow E$	b $S \rightarrow bS aS$ $S \rightarrow E$	\$ $S \rightarrow E$

\* FIND OUT WHETHER THE GIVEN GRAMARS ARE LR(0) OR NOT

$$\textcircled{1} \quad S \rightarrow aABb \\ A \rightarrow c/e \\ B \rightarrow d/e$$

$$\textcircled{2} \quad S \rightarrow A/a \\ A \rightarrow a$$

$$\textcircled{3} \quad S \rightarrow aB/e \\ \textcircled{4} \quad S \rightarrow aB/e$$

$$\textcircled{5} \quad C \rightarrow CS/e$$

$$\textcircled{6} \quad S \rightarrow AB \\ A \rightarrow a/e \\ B \rightarrow b/e$$

$$\textcircled{7} \quad S \rightarrow aSA/e \\ \cancel{A \rightarrow c/e}$$

	first()			follow()	
	a	b	c	d	\$
$\textcircled{1}$	$S \rightarrow a.ABb$	$\Sigma a \beta$		$\Sigma b, d \beta$	$\Sigma \$ \beta$
	$A \rightarrow c/e$	$\Sigma c, e \beta$		<del><math>\Sigma d, e \beta</math></del>	<del><math>\Sigma \\$ \beta</math></del>
	$B \rightarrow d/e$	$\Sigma d, e \beta$		$\Sigma b \beta$	$\Sigma b \beta$
	a	b	c	d	\$
S	$S \rightarrow aABb$				
A		$A \rightarrow c/e$	$A \rightarrow c$	$A \rightarrow e$	
B		$B \rightarrow e$		$B \rightarrow d$	

	first()		follow()	
	a	\$	\$	\$
$\textcircled{2}$	$S \rightarrow A/a$	$\Sigma a \beta$	$\Sigma \$ \beta$	$\Sigma \$ \beta$
	$A \rightarrow a$	$\Sigma a \beta$	$\Sigma \$ \beta$	$\Sigma \$ \beta$
	a	\$		
S	$S \rightarrow A/a$			
A	$A \rightarrow a$			

	first()		follow()	
	b	c	\$	\$
$\textcircled{3}$	$S \rightarrow aB/e$	$\Sigma a, e \beta$	$\Sigma c, \$ \beta$	$\Sigma \$ \beta$
	$B \rightarrow bC/e$	$\Sigma b, e \beta$	$\Sigma \$ \beta$	$\Sigma \$ \beta$
	$C \rightarrow CS/e$	$\Sigma c, e \beta$	<del><math>\Sigma b, c \beta</math></del>	<del><math>\Sigma b, c \beta</math></del>
	b	c	\$	\$
S	$S \rightarrow aB$			
B	$B \rightarrow bC$	$B \rightarrow c$	$B \rightarrow e$	
C	$C \rightarrow C$	$C \rightarrow C$	$C \rightarrow C$	

Topic	$\text{first}()$	$\text{follow}()$	
4.	$S \rightarrow AB$ $A \rightarrow a/E$ $B \rightarrow D/E$	$\{a, \emptyset\}$ $\{a, E\}$ $\{b, E\}$	$\{\$\}$ $\{b, \$\}$ $\{\$\}$
	$S \mid a$ $A \mid S \rightarrow AB$ $A \mid A \rightarrow a$ $b \mid B \rightarrow b$	$b$ $S \rightarrow AB$ $A \rightarrow E$ $B \rightarrow E$	$\emptyset$ $A \rightarrow E$ $B \rightarrow E$
			<u>Yes</u>
5.	$S \rightarrow aS_A A \mid E$ $A \rightarrow C/E$	$\{a\}, E?$ $\{C, E\}$	$\{ \$, \emptyset \}$ $\{\$\}$
	$S \mid a$ $A \mid S \rightarrow aS_A$ $A \mid \emptyset$	$C$ $S \rightarrow G$ $A \rightarrow C$	$\emptyset$ $S \rightarrow E$ $A \rightarrow \emptyset E$

8/10/2021

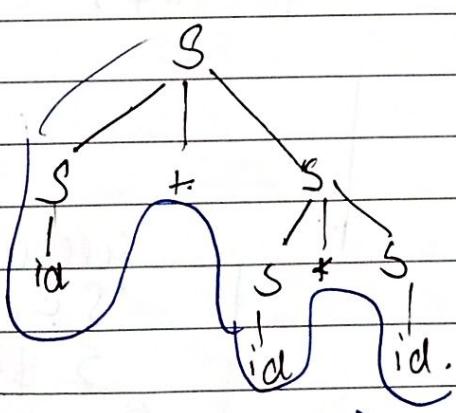
### Ambiguous Grammar

$$S \rightarrow S + S I$$

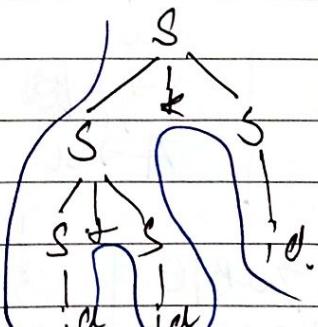
$$S * S I$$

id

$$\Rightarrow (\underline{id} + \underline{id} * \underline{id})$$



$$id + (id + id)$$



$$(id + id)^*, id$$



Here, the answer  
is correct.

This gives a wrong  
answer

The reason is :-

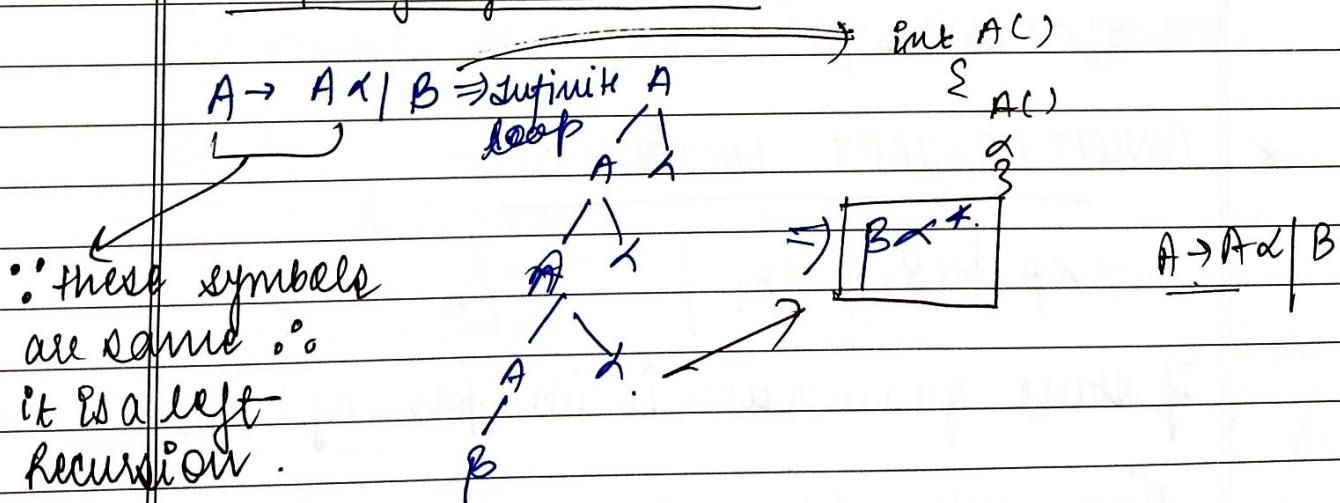
- whenever we calculating an expression we must check for priority of the operators.
- But if the priorities are same, then we need to look for the associativity.

\* How to convert ambiguous grammar to non-ambiguous grammar :-

$$S \rightarrow S+S \mid S * S \mid id.$$

$$\begin{aligned} & \xrightarrow{} S \rightarrow S+S \mid A \\ & A \rightarrow S * S \mid B \xrightarrow{} UA \\ & B \rightarrow id. \end{aligned}$$

\* Concept of left Recursion :-



\* Solution to convert left recursive grammar into its equivalent right recursive grammar.

Let's assume the given grammar is in a form of :-

$$A \rightarrow A\alpha \mid B$$

Then its corresponding equivalent LR grammar will be :-

$$\begin{array}{l} A \rightarrow BA' \\ A' \rightarrow \alpha A' | E \end{array}$$

\* Examples:-

(1) "  $E \rightarrow E + T | T$ "

$$\begin{array}{c} \overline{E} \rightarrow \overline{E} + \overline{T} | \overline{T} \\ \overline{A} \rightarrow \overline{A} \quad \overline{\alpha} \quad \overline{\beta} \end{array}$$

$$\begin{array}{c} \rightarrow \overline{E} \rightarrow T E' \\ E' \rightarrow + T E' | E \end{array}$$

$$E \rightarrow T E'$$

$$E' \rightarrow + T E' | G$$

(2)  $S \rightarrow S O S I S | O I$

$$S \rightarrow O I S'$$

$$S' \rightarrow O S I S | S' | E$$

\* CONCEPT OF LEFT FACTORIZATION:-

$$A \rightarrow \alpha \beta_1 | \alpha \beta_2 | \alpha \beta_3 | \dots | \alpha \beta_n$$

If some grammar is in form of :-

Then such type of grammar are known as non-deterministic!

\* Conversion of non-deterministic grammar into deterministic grammar :-

If  $A \rightarrow \alpha \beta_1 | \alpha \beta_2 | \alpha \beta_3 | \dots | \alpha \beta_n$ .

Then non-d. will be:-

$$A \rightarrow \alpha A'$$

$$A' \rightarrow \beta_1 | \beta_2 | \beta_3 | \dots | \beta_n.$$

→ example:-  $S \rightarrow a S S b S | a S a S b | a b b$ .

$$\Rightarrow S \rightarrow a$$

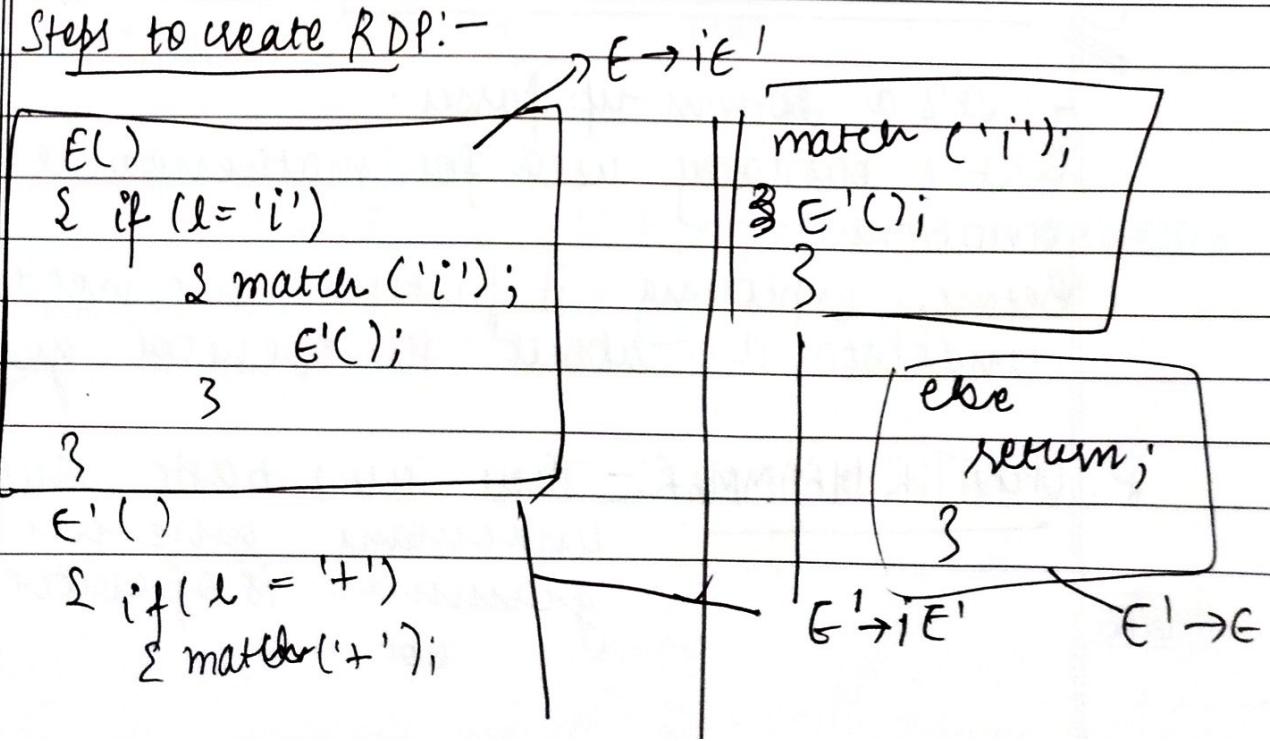
21 Oct 2021

→ RECURSIVE DESCENT PARSER:-

To create RDP, create methods for each left hand side of the production, in C program.

Ex:-  $E \rightarrow iE'$   
 $E' \rightarrow +iE' | E$

\*. Steps to create RDP:-



```
match (char t)
```

```
( if ( l == t )
```

```
    l = getchar();
```

```
else
```

```
    printf ("error");
```

```
?
```

$\therefore l = \text{look ahead symbol}$

```
main()
```

```
{
```

```
E()
```

```
if (l == $)
```

```
printf ("parsing success");
```

```
}
```

main  
function

**NOTE:-** The data structure stack is used in this KDP  
is recursive stack.

→ BOTTOM-UP PARSER

(1) OPERATOR PRECEDENCE PARSER:-

① It's a bottom-up parser.

② It is basically used for mathematical operations.

Before, exploring it further we need to understand about the operator grammar.

\* OPERATOR GRAMMAR:- There are 2 basic rules to

understand whether the grammar is operator or not.

• Rule-1 In operator grammars " no 2 consecutive variables can appear in a production".

Eg:- 1.  $E \rightarrow AB \text{ or } E$  X  $\because$  it has 2 variable A & B.

~~A  $\rightarrow a$~~   
~~B  $\rightarrow b$~~

2.  $E \rightarrow a \text{ Ba } | E$  ✓ There are no such products in which 2 variables are present hence, satisfies Rule-1.

$B \rightarrow b$

• Rule-2 :-

In operator grammars no null productions are allowed; i.e. no ' $\epsilon$ ' production are allowed.

NOTE: - Operator precedence parser is the only parser which can pass an ambiguous grammar.

~~operator~~

EXAMPLES: -

(1)  $E \rightarrow E + E \text{ or } E * E | id$  (Yes)

(2)  $E \rightarrow E AE | id$  (NO)  
 $A \rightarrow + \text{ or } *$   $\because$  2 consecutive variables

→ correction:  $E \rightarrow E + E \text{ or } E * E | id$ .

→ HOW TO CONSTRUCT OPERATOR RELATION TABLE:-

$$E \rightarrow E + E \mid E * E \mid id.$$

(Steps to create table for this operator grammar)

	id	+	*	\$
id	error	>	>	>
+	<	>	<	>
*	<	>	error	>
\$	<	<	<	error.

In order to fill the ~~above~~ mentioned table we need to apply few rules:-

Rule-1 :-

Identifiers are the highest priority / higher precedence as compared to any other operator.

Rule-2 :-

\$ is having the least precedence as compared to any other operand.

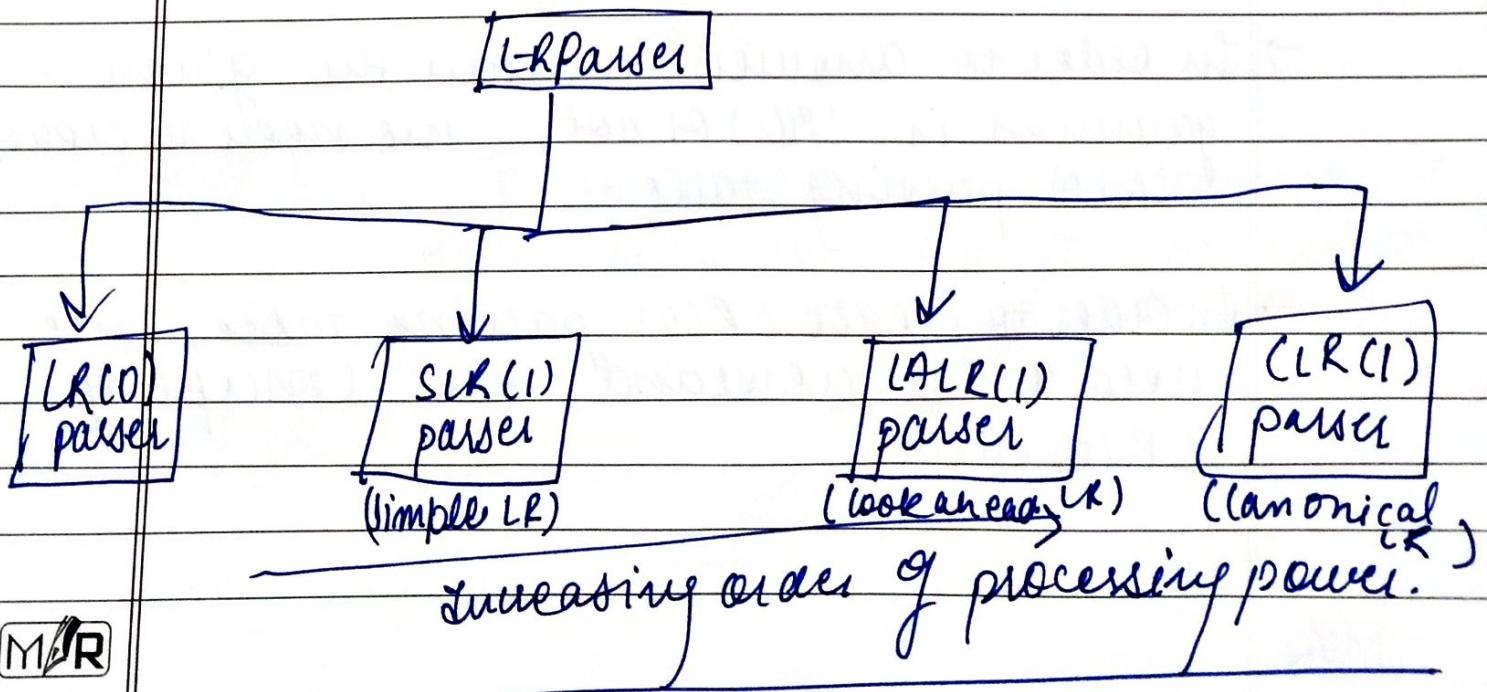
## How parsing works? :-

- ① We use stack for the scanning.
- ② Initially stack is having dollar '\$' at top of it.
- ③ When precedence is less than the next character, then perform operation = 'PUSH'.
- ④ When precedence is higher than the next character, then perform operation = 'POP'.

**NOTE:-** If we have 'n' operators, then the size of table is order of  $\Rightarrow O(n^2)$ .

\* L-R PARSERS:-

These are the bottom-up parsers.



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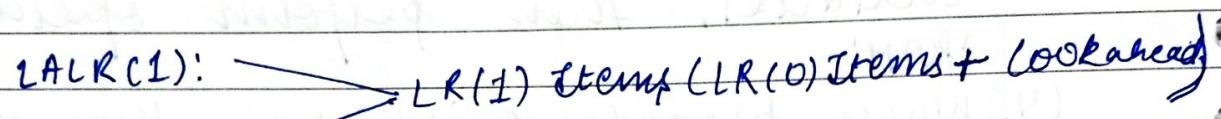
\* Their corresponding Parsing Table:-  
Concept:-

LR(0):



SLR(1):

LALR(1):



CLR(1):

- In regards to LR Parsers, the main question is whether the grammar is : LR(0) / SLR(1) / LALR(1) / CLR(1) ?
- In order to answer such question, we need to create their corresponding parsing table.

\* LR(0) PARSERS:-

- In order to answer whether the given grammar is LR(0) or not, we need to create LR(0) parsing table.
- In order to create LR(0) parsing table, we need to understand the concept of LR(0) Items.

- STEPS TO FIND L-R(0) ITEMS :-

Grammar = "  $S \rightarrow A \cdot A$   
 $A \rightarrow a \cdot A / b$ "

~~Find items~~

→ Step-1 :- In the given grammar, we need to add a dummy production, named as "Augmented Production" and it basically produces the start symbol and denoted as " $S'$ ", if the start symbol is " $S$ ".

$$\begin{aligned} S' &\rightarrow S \\ S &\rightarrow A \cdot A \\ A &\rightarrow a \cdot A / b \end{aligned}$$

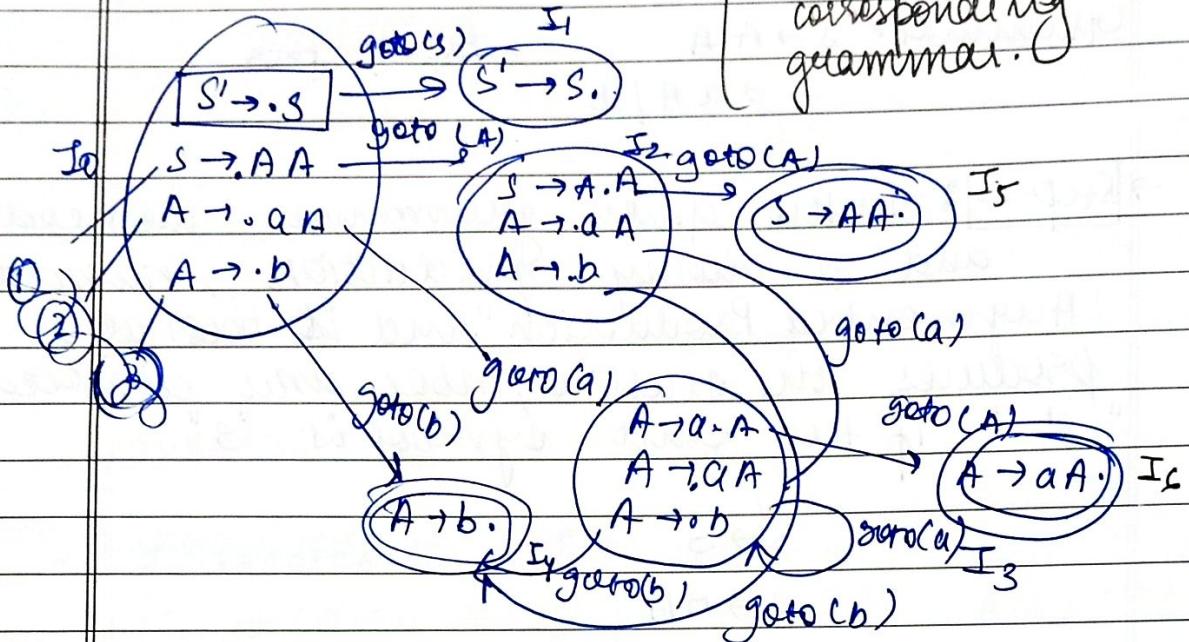
→ Step-2 :- Now we need to start with the augmented production and place a LR(0) item sign as ~~...~~ '•'

$$\begin{aligned} S' &\rightarrow \cdot S \\ S &\rightarrow A \cdot A \\ A &\rightarrow a \cdot A / b \end{aligned}$$

→ Step-3 :- To understand the functionality of LR(0) items sign all specific operation "closure & goto" needs to be understand.

- CLOSURE & GOTO :-

⑦ CLOSURE OPERATION



goto & closure will work ~~perfectly~~ / / by ,  
first we will take out the closure .  
then we will take out goto , & the  
process will continue till the final  
state is not reached .

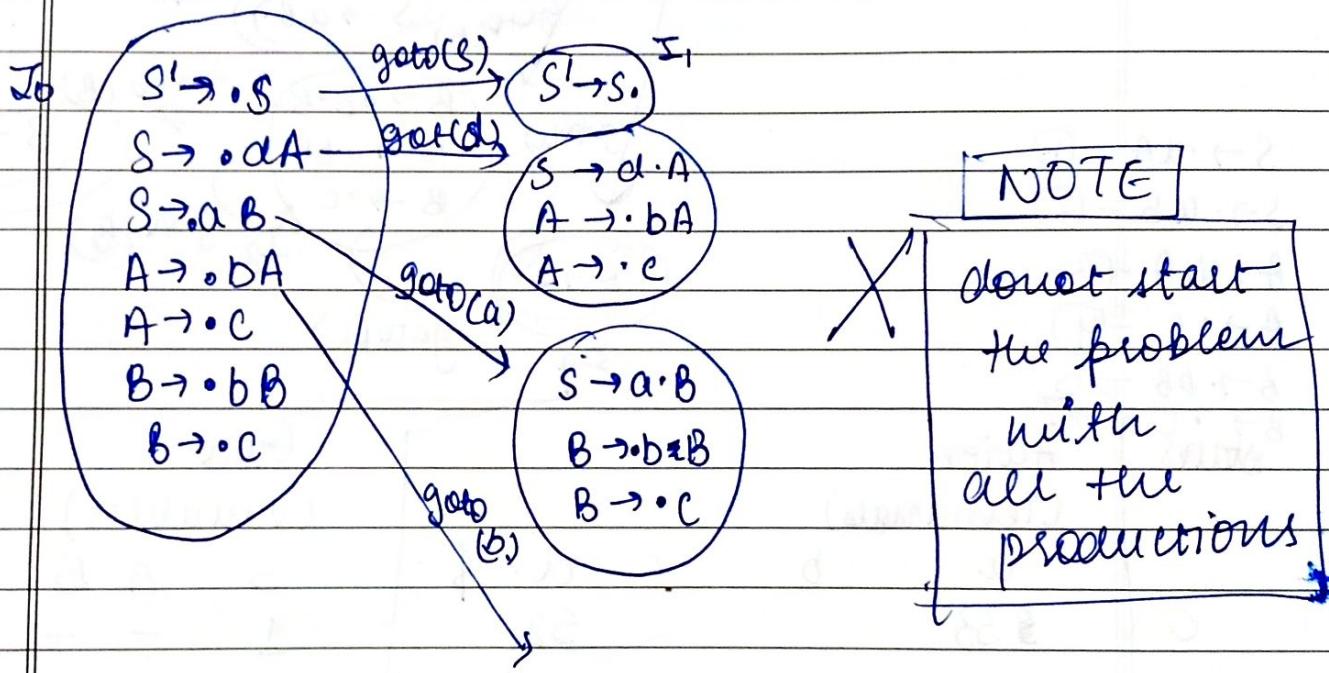
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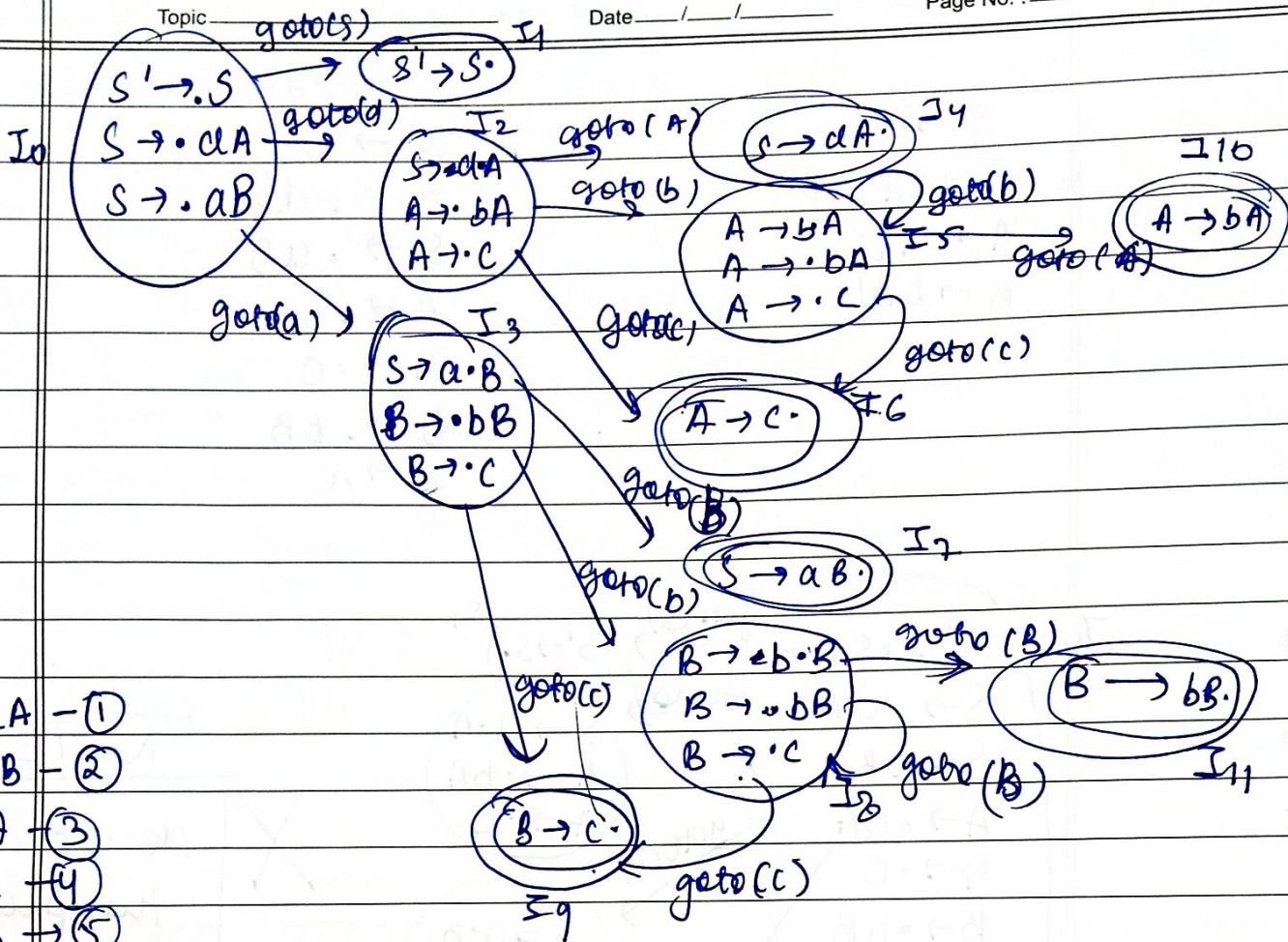
$$\begin{aligned} S &\rightarrow aA | aB \\ A &\rightarrow bA | c \\ B &\rightarrow bB | c \end{aligned}$$

②  $S' \rightarrow S$   
 $S \rightarrow aA | aB$   
 $A \rightarrow bA | c$   
 $B \rightarrow bB | c$

$\Rightarrow$   $S' \rightarrow .S$   
 $S \rightarrow aA | aB$   
 $A \rightarrow bA | c$   
 $B \rightarrow bB | c$

$$\begin{array}{l}
 S' \rightarrow S \\
 S \rightarrow dA | aB \\
 A \rightarrow bA | c \\
 B \rightarrow bB | c
 \end{array} \rightarrow
 \begin{array}{l}
 S' \rightarrow \cdot S \\
 S \rightarrow \cdot dA \\
 S \rightarrow \cdot aB \\
 A \rightarrow \cdot bA \\
 A \rightarrow \cdot c \\
 B \rightarrow \cdot bB \\
 B \rightarrow \cdot c
 \end{array}$$





States	Action (Terminals)				Goto (Variables)			
	a	b	c	d.	\$	S	A	B
0	\$ \$ \$				\$2	1	-	-
1						"accept"		
2	S5	S6				2	4	
3	S8	S9					7	
4	x1	x1	x1	x1	x1			
5	S5	S6					10	
6	x4	x4	x4	x4	x4			
7	x2	x2	x2	x2	x2			
8	S8	S9						11
9	x6	x6	x6	x6	x6			
10	x3	x3	x3	x3	x3			
	x5	x5	x5	x5	x5			

\* Shift & Reduce Moves:-

① Shift Move:-

$$(i) A \rightarrow \cdot a A \quad \checkmark$$

because  $\cdot$  is before a variable which is not acceptable.

$$(ii) A \rightarrow a \cdot A \quad X$$

because LR(0) item sign ( $\cdot$ ) is at the end of the production.

$$(iv) A \rightarrow a B \cdot c D \quad \checkmark$$

$$(v) C \rightarrow a B \cdot \quad X$$

$$(vi) S \rightarrow S \cdot s a b \quad X$$

$$(vii) S \rightarrow G$$

$\hookrightarrow$  represents  $S \rightarrow \cdot$  means at the end of production  
 $\Rightarrow \cdot$  it is not a shift move.

② Reduce Move:-

LR(0) item symbol ( $\cdot$ ) at the end of the production, in case of reducing

e.g:-

$$(i) S \rightarrow a A B \cdot \quad \checkmark$$

$$(ii) S \rightarrow \cdot \quad \checkmark$$

$$(iii) A \rightarrow a A \cdot \quad \cancel{\checkmark}$$

$$(iv) A \rightarrow a \cdot A \quad X$$

After the creation of LR(0) items it may be the possibility that we have various shift & reduce moves in all the existing stacks ( $I_0, I_1, I_2, \dots$ )

Now we need to identify the conflicts of shift & reduce moves.

$\xrightarrow{\text{shift}}$

\* Conflicts of SR  $\rightarrow$  Reduce.

There are 2 types of conflicts in the internal states of LR(0) items:-

- (1) Shift - Reduce conflict (S-R conflict)
- (2) Reduce - Reduce conflict (R-R conflict)

(i.)  $S \rightarrow S. \rightarrow R$   $\rightarrow$  because LR(0) item sign is at the end.

$S \rightarrow a.A \times$

$A \rightarrow a. \rightarrow S$

$\rightarrow$  neither shift nor conflict.

$\rightarrow$  because LR(0) item sign is at the beginning.

(ii.)  $S \rightarrow S. \rightarrow R$   
 $S \rightarrow a.A \times \rightarrow$  There is [no conflict].

(iii.)  ~~$S \rightarrow S. \rightarrow R$~~   $S \rightarrow a.A. \rightarrow R \rightarrow$   $R-R$   
 ~~$S \rightarrow a.A \times$~~   $A \rightarrow a. \rightarrow R$  conflict

→ Step-5: Now create LR(0) Parsing Table.

zero se shift  
u me ja hain: ↗  
check the goto  
variables of A  
from every state

		Action (Terminals)			GOTO (variables)	
		a	b	\$	S	A
0	S3	S4			1	2
1				"accept"		
2	S3	S4				5
3	S3	S4				6
4	R3	R3		R3		
5	R1	R1		R1		
6	R2	R2		R2		

$$\begin{array}{l}
 S \rightarrow AA \quad \textcircled{1} \\
 A \rightarrow aA \quad \textcircled{2} \\
 A \rightarrow b \quad \textcircled{3}
 \end{array}$$

① entry of variables.

② We need to make an entry of "accept" under '\$' within the state where we get our augmented production.  
(In our eg. it is state 1)

③ Now, we need to make the entries for shift more.

④ ~~entry~~ for reduce now, in which need to look the final states & make their final entries in the parsing table as per the production no.

**Step-6** :- • In order to answer whether the given grammar is LR(0) or not, we need to observe LR(0) Parsing Table.

- The given grammar is not LR(0) if it follows the below 2 conditions:-

- ① There should not be any ~~S-R~~ S-R conflict in any of the cell of given parsing table.
- ② There should not be any L-R conflict in any of the cell of given parsing table.

Now, in the above LR(0) parsing Table, there's no conflict of SR and RR. Hence, this grammar is LR(0) grammar.

\* A SHORTCUT TO FIND WHETHER THE GRAMMAR IS LR(0) OR NOT :-

- In order to answer quickly whether the grammar is LR(0) or not  $\rightarrow$  we only need to follow from step-1 to 3 till the point of creating LR(0) items.
- Now just observe each & every internal state of LR(0) items and try to find out any of the conflict of SR or R-R. If you find any of these conflicts in any of the states, then declare that this is not LR(0) grammar.

But this method is not recommended.

### \* SLR(1) :-

- After the discussion of LR(0), we can simply proceed for SLR(1). Now, again we have a question whether the grammar is SLR(1) or not?
- In order to answer if grammar is SLR(1) we need to remember these 2 rules:-
  - Rule-1:- If a grammar is LR(0), then it will definitely be SLR(1) grammar. In other words, if there is no conflict of S-R or R-R in LR(0) parsing table, then obviously the grammar will be LR(0) & as well as SLR(1).
  - Rule-2:- If a grammar is not LR(0), then obviously we have some conflict in corresponding LR(0) parsing table. In that case now we manually need to check, whether the grammar is SLR(1) or not.

### \* HOW TO CHECK WHETHER THE GRAMMAR IS SLR(0) OR NOT:-

- The parsing table for SLR(1) is same as LR(0) parsing table. but the only difference is the placement of reduce row.

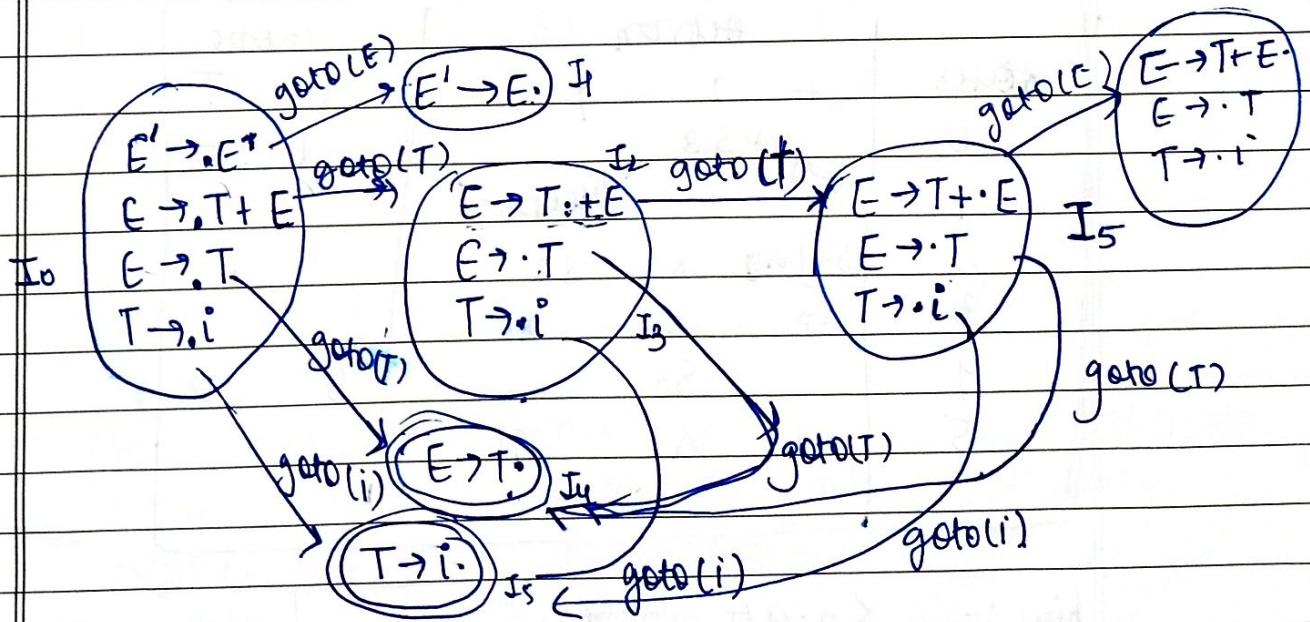
→ In case of SLR(1) we don't write the reduce move entry in all rows like LR(0). In SLR(1) we only place the reduce moves in the follow( $i$ ) of corresponding variable.

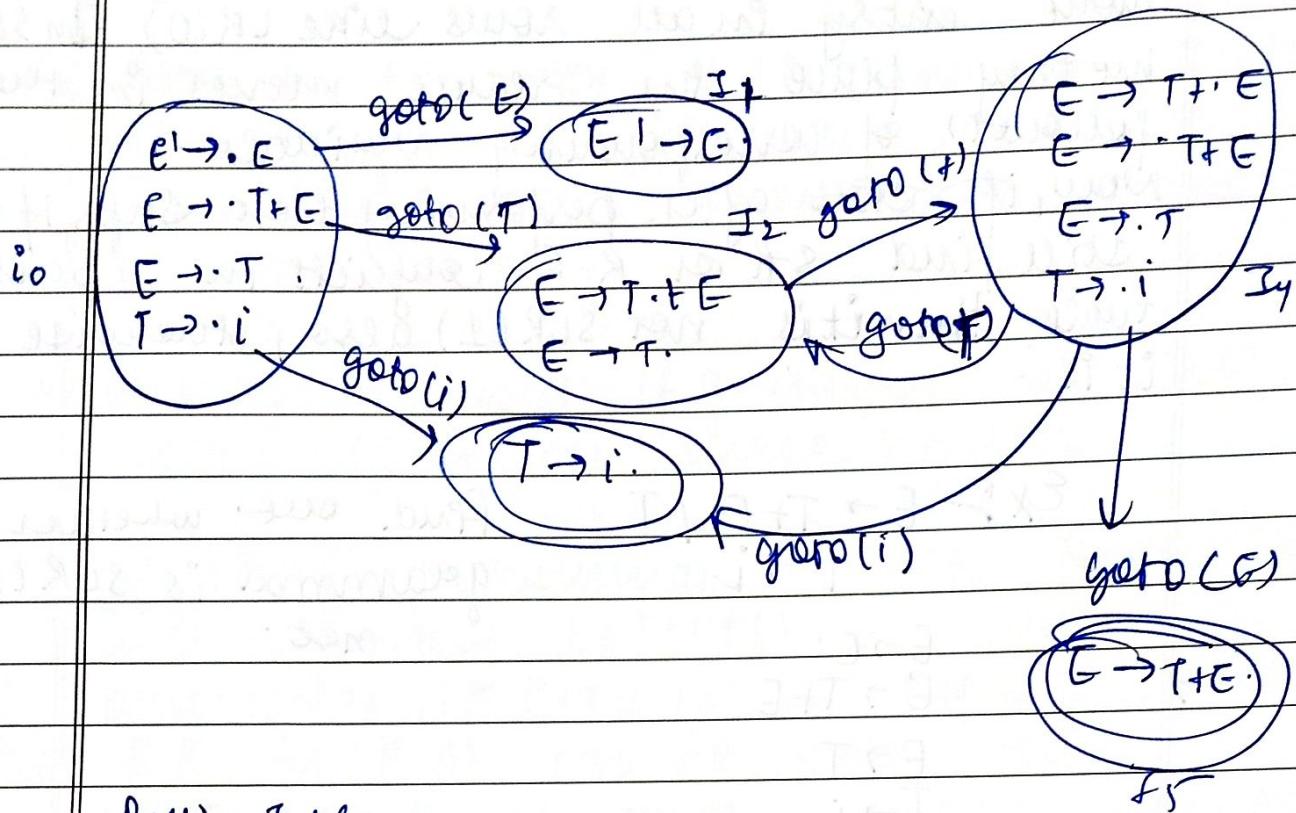
Now, if still after performing these steps if we still find S-R or R-R conflicts in parsing table, then it is not SLR(1) also, otherwise it is.

$$\text{Ex: } E \rightarrow T+E \mid T \\ T \rightarrow i.$$

Find out whether grammar is SLR(1) or not.

$$\Rightarrow \begin{array}{l} E \rightarrow E' \\ E \rightarrow T+E \\ \\ E \rightarrow T \\ T \rightarrow i \end{array}$$

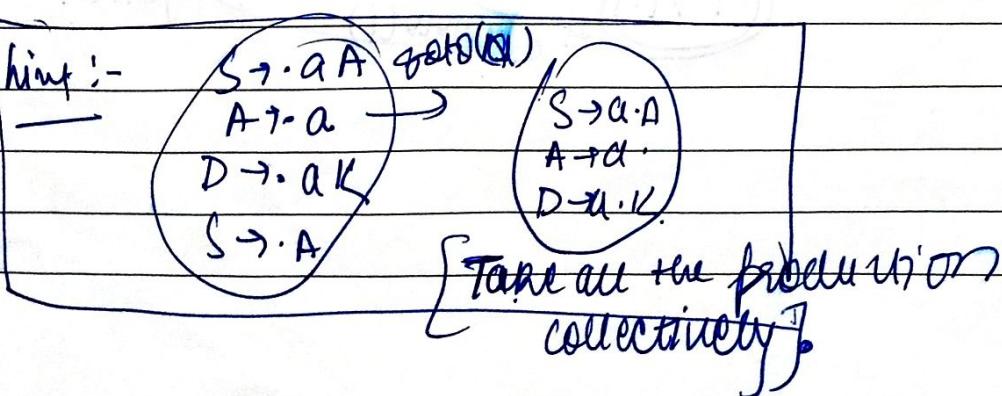




### \* Raising Table

States	Action	Items
0	+ i \$	t T
1	Accept	1 2
2	S1 a	82 82
3	λ3	λ3 83
4	λ3	5 2
5	λ1	81

Hint :-



\* This grammar is not LR(0) grammar because we have a conflict of SR in the 3<sup>rd</sup> row.

\* Now we need to follow the Rule-2 & need to check whether this grammar SLR(0) manually by calculating the follow of the reduced move in no conflicting cell.

State	Action			Output
	$\lambda$	$S_3$	$\lambda^2$	
0				T
1				2
2	$S_4$		$\lambda^2$	
3	$\lambda^3$	$\lambda^3$	$\lambda^3$	
4		$S_3$		2
5	$\lambda^1$	$\lambda^1$	$\lambda^1$	

Since required move is corresponding production is  $S \rightarrow T$ ; whose follow() is \$ so we only make the entry of reduce under \$.

If we follow rule 2 we find conflicts in parsing table, then grammar is not SLR(1).

## \* CONCEPT OF ~~LALR~~<sup>M/R</sup>(1) & CLR(1)

- In LALR(1) & CLR(1) the ultimate goal is still creating the corresponding parsing tables.  
We need to create LALR(1) parsing table & CLR(1) P.T for grammar, and declare whether the grammar is LALR(1) or CLR(1).
- ~~In LALR(1) &~~ To create parsing table of LALR(1) & CLR(1) we need to create LR(1) items, which is combination of LR(0) items + lookahead symbols.

Firstly, we need to create parsing table of CLR(1) & then we move to LALR(1) parsing table.

Ques: Create CLR(1) parsing table of the given grammar & find out whether its CLR(1) or not.

$$S \rightarrow AA$$

$$A \rightarrow aAb$$

Sol:- In order to solve such problems, we need to create CLR(1) parsing table.

## \* STEPS TO CREATE CLR(1) Parsing Table: -

Rule-1:- Look-ahead symbol of the augmented production will always be dollar \$.

$$S' \rightarrow \cdot S, \$$$

$\rightarrow$  look-ahead symbol.

### Rule-2

- Simplify follow (R(0)) items creation but while closure operation look-ahead will be the first of next whole string.

$$\text{eg} \rightarrow S \rightarrow AA$$

$$A \rightarrow aA/b$$

on applying closure on augmented producer

$$S' \rightarrow \cdot S$$

$$S \rightarrow \cdot A(A, \$)$$

$$A \rightarrow \cdot aA, a/b$$

$$A \rightarrow \cdot b, a/b$$

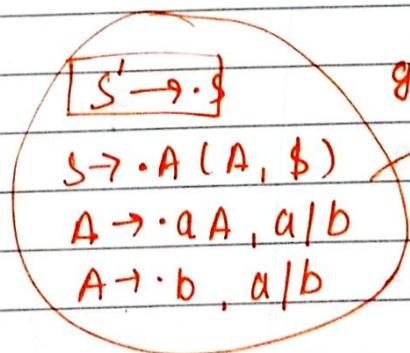
due to this, this production will be added.

will be the first

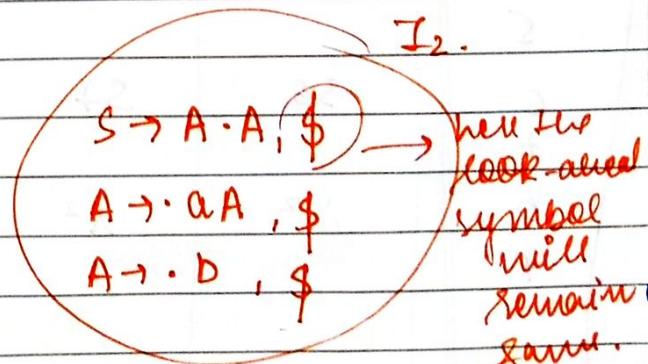
I<sub>0</sub>

### Rule-3

- During the goto operation look-ahead symbol doesn't change.

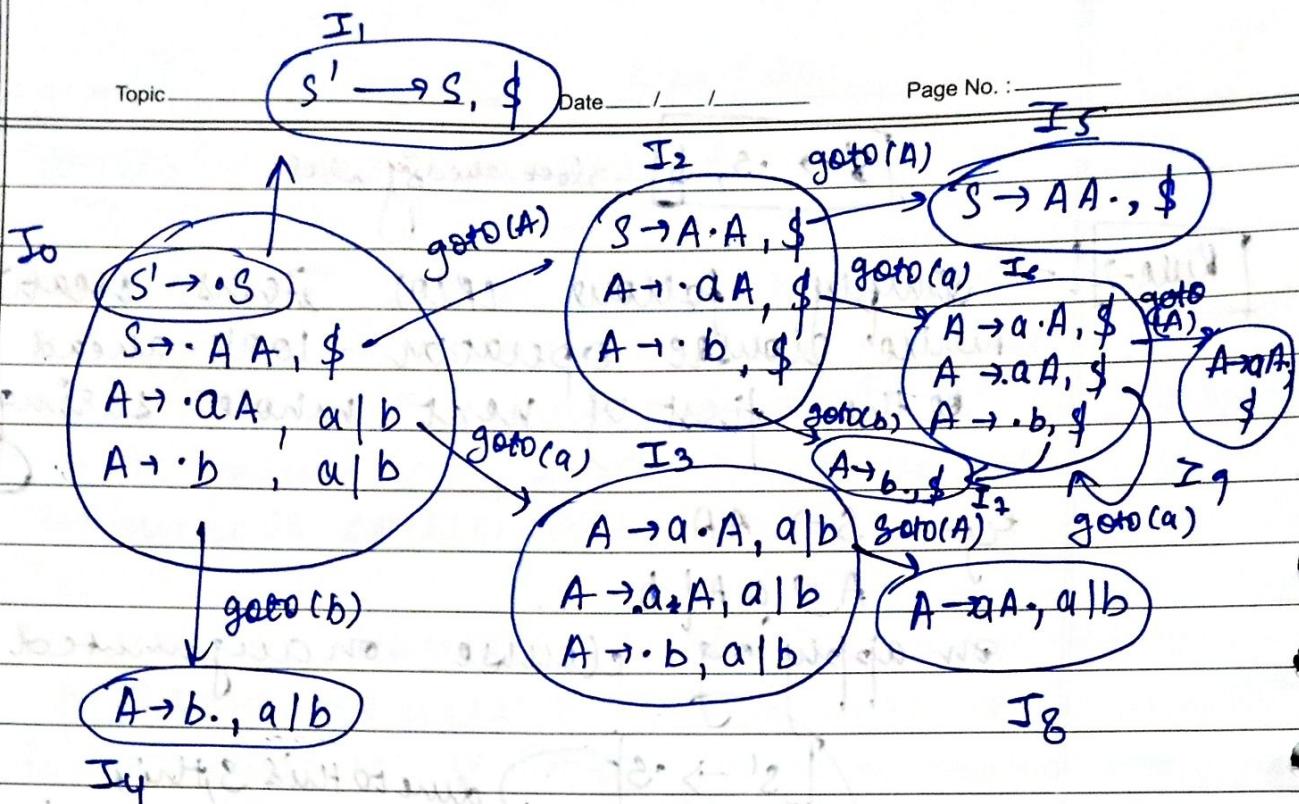


goto (A)



### Rule-4

- In LR(0) parsing table reduce moves are placed under look-ahead symbols.

StatesActionOutput

	a	b	\$	A	S
0	$s_3$	$s_4$			2
1			"accept"		
2	$s_6$	$s_7$			5
3	$s_3$	$s_4$			8
4	$\lambda^3$	$\lambda^3$			
5			$\lambda^1$		
6	$s_6$	$s_7$			9
7			$\lambda^3$		
8	$\lambda^2$	$\lambda^2$			
9			$\lambda^2$		

## MAJOR PROBLEM

Date \_\_\_\_\_ / \_\_\_\_\_ / \_\_\_\_\_

Page No. \_\_\_\_\_

Ques  $S \rightarrow AaAb \mid BbBa$

$A \rightarrow E$

$B \rightarrow E$

Find out the given grammar is LL(0), LR(0), SLR(1), CLR(1).

⇒ I Checking for LL(0) :-

Step 1:- we calculate first & follow.

<u>Production.</u>	<u>first()</u>	<u>follow()</u>
$S \rightarrow AaAb \mid BbBa$	$\{a, b\}$	$\{\$\}$
$A \rightarrow E$	$\{E\}$	$\{a, b\}$
$B \rightarrow E$	$\{E\}$	$\{a, b\}$

Step 2: Parsing table:-

	a	b	\$
S	$S \rightarrow AaAb$	$S \rightarrow BbBa$	
A	$A \rightarrow E$	$A \rightarrow E$	
B	$B \rightarrow E$	$B \rightarrow E$	

Since, we have only single entry in whole LL(0) parsing tree,

∴ This grammar is LL(0) grammar.

II Checking for LR(0) :-

Step-1 :-  $S \rightarrow S$

$$S \rightarrow AaAb \mid BbBa$$

$$A \rightarrow \epsilon \quad E$$

$$B \rightarrow \epsilon \quad E$$

Step-2 :-  $S' \rightarrow \cdot S$

$$S \rightarrow AaAb \mid BbBa$$

$$A \rightarrow \epsilon \quad E$$

$$B \rightarrow \epsilon \quad E$$

Step-3 :-

$$S' \rightarrow \cdot S$$

$$S \rightarrow \cdot AaAb \mid BbBa$$

$$A \rightarrow \cdot E$$

$$B \rightarrow \cdot E$$

I<sub>0</sub>

$$S' \rightarrow \cdot S$$

$$S \rightarrow \cdot AaAb$$

$$S \rightarrow \cdot BbBa$$

I<sub>1</sub>

$$A \rightarrow \cdot \epsilon$$

I<sub>2</sub>

$$B \rightarrow \cdot \epsilon$$

goto(A)

goto(B)

goto(B)

goto(B)

$$S' \rightarrow \cdot S$$

$$S \rightarrow A \cdot aAb$$

$$A \rightarrow \cdot E$$

$$S \rightarrow B \cdot bBa$$

$$B \rightarrow \cdot E$$

I<sub>2</sub> goto(A)

I<sub>3</sub> goto(B)

I<sub>4</sub> goto(B)

I<sub>5</sub> goto(B)

I<sub>6</sub> goto(B)

I<sub>7</sub> goto(B)

I<sub>8</sub> goto(B)

I<sub>9</sub> goto(B)

Parsing Table.

state.	a	b	\$	s	A	B
0	$R_3, R_4$	$R_3, R_4$	$R_3, R_4$	1	2	3
1						
2	$S_4$					
3		$S_5$				
4	$R_3$	$R_3$	$R_3$		6	
5	$R_4$	$R_4$	$R_4$			7
6		$S_8$				
7	$S_9$					
8	$R_1$	$R_1$	$R_1$			
9	$R_2$	$R_2$	$R_2$			

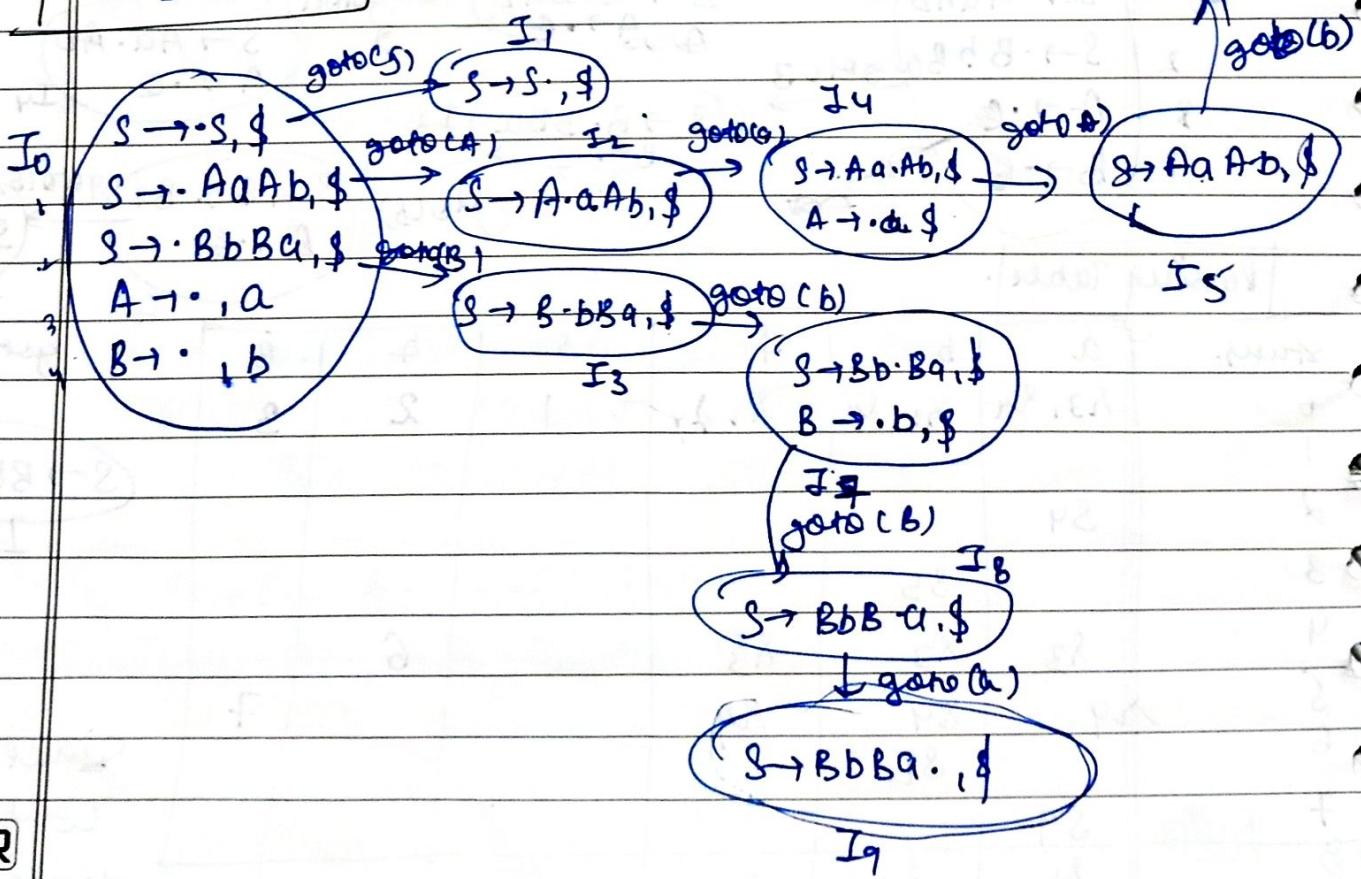
MAR

Since, R-R  
conflict  
hence, not  
LR(0).

III for SCR(1) :-

status	a	b	c	B	A	B
0						
1						
2						
3						
4						
5						
6						
7						
8						
9						

IV for CLR(1) :-

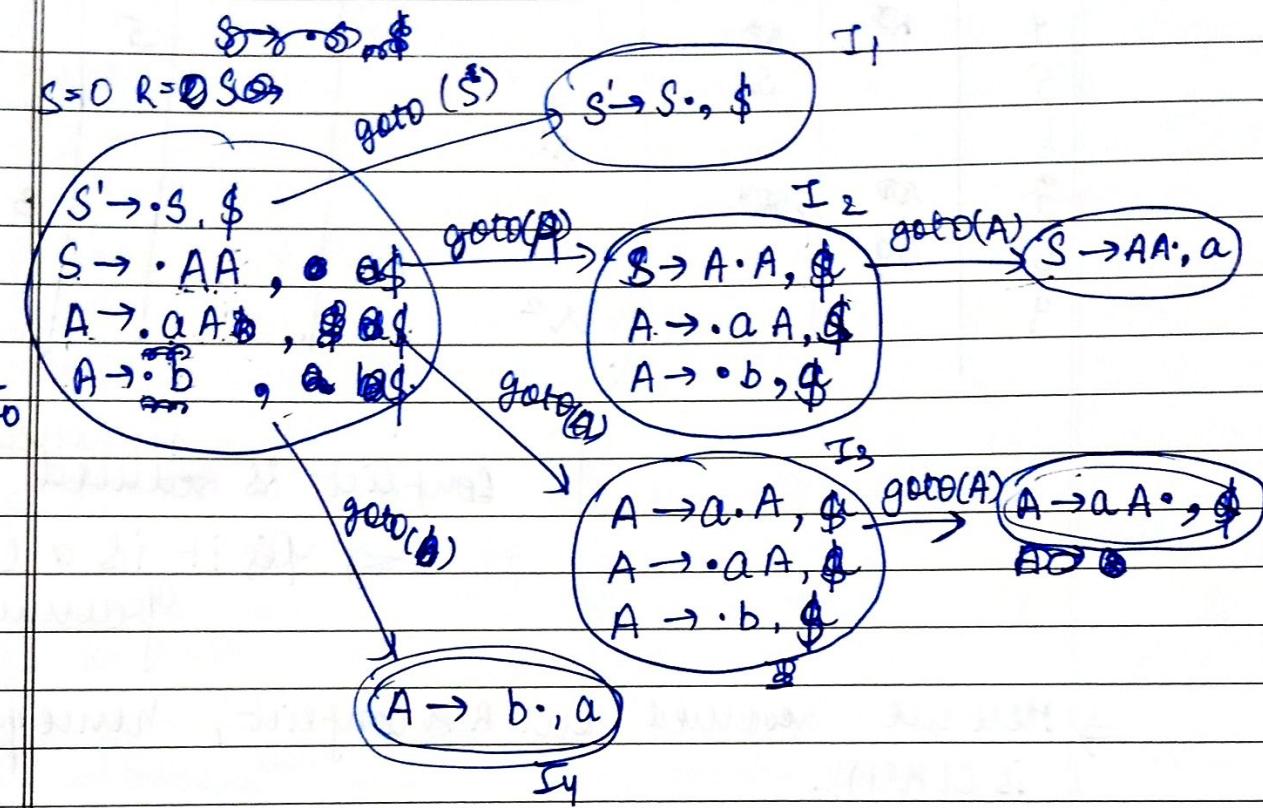


Status	Topic	Action.		Date	S	(proto)		
		a	b				A	B
0		00					1	2
1					"accept"			3
2		S4						
3			S7					
4		50	50-					5
5			S6					
6				x1				
7		50	50.					B
8		S9						
9				x2				.

conflict is removed.  
→ Yes it is a CLR(1) grammar

→ Here we resolved our R-R conflict, hence grammar is CLR(1).

Ques.  $S \rightarrow A A$   
 $A \rightarrow a A/b$



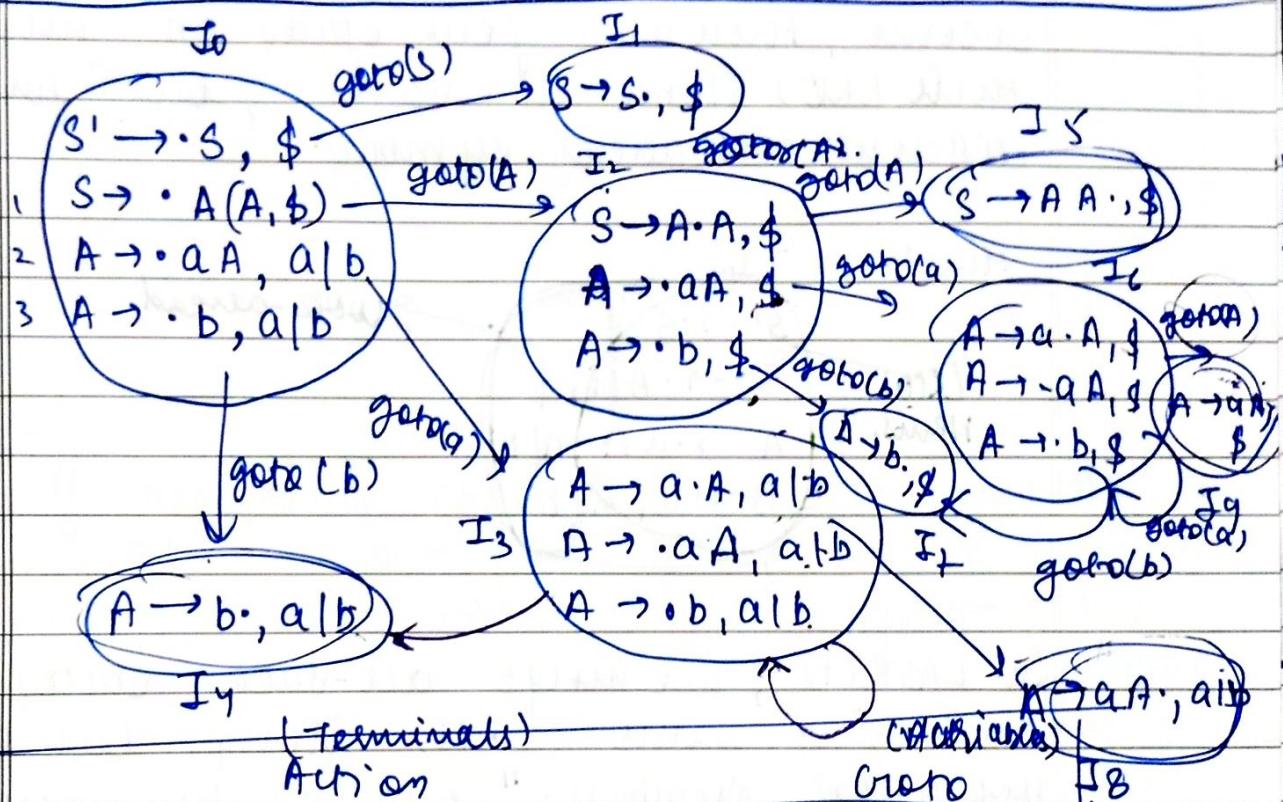
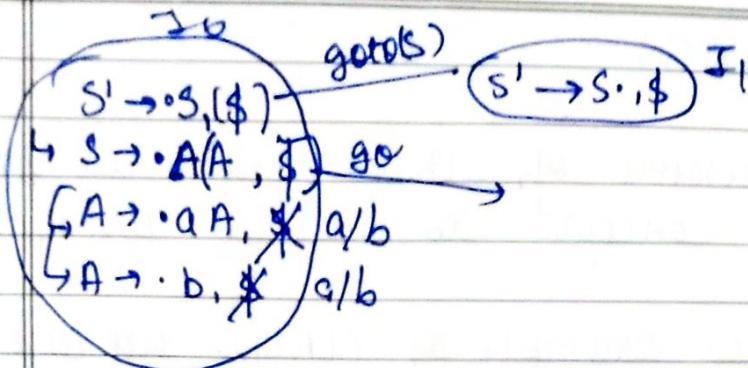
a.  
 $\cdot a \cdot b$

first(A\$)

Topic \_\_\_\_\_

Date / /

Page No. \_\_\_\_\_



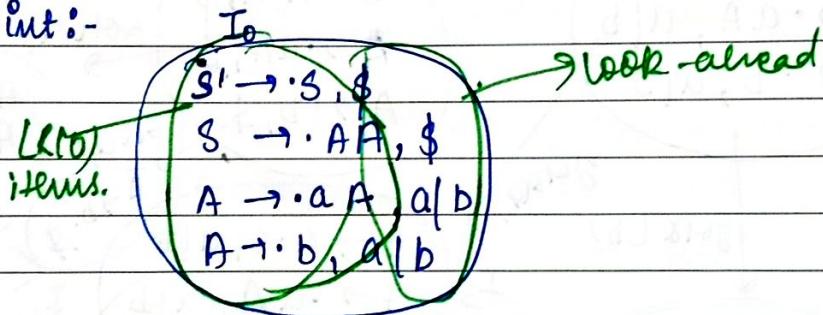
State	a	b	\$	Action	Creates
0	$S_3$	$S_4$			
1				"accept"	
2	$S_6$	$S_7$			
3	$S_3$	$S_4$			
4	$\lambda^3$	$\lambda^3$			
5					
6	$S_6$	$S_7$			
7					
8	$\lambda^2$	$\lambda^2$	*		
9					
M/R					

→ LALR(1) PARSER :-

After the discussion of CLR(1), now we partially modify CLR(1) concept to achieve LALR(1) parser.

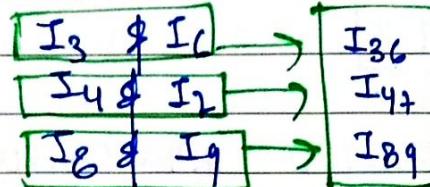
In the previous example of CLR(1) we can observe, there are few states in which their LR(0) items are same, but having different look-ahead symbol.

Hint:-



"In LALR(1), we merge all such states which are having same LR(0) items but different look-ahead symbols." And in the parsing table of CLR(1), we simply delete such rows which follow this property & keep only one row along with their shift move merge.

→ In the previous example, following are the pair of states which are having same LR(0) items but different look-ahead symbol.



Corresponding LALR(1)  
Parsing table is : 2

States	ACTION			GO TO	
	a	b	\$	A	S
0	S36	S47		2	
1			"accept"		
2	S36	S47		5	
36	S36	S47		8	
847	R3	R3	R3		
5			R1		
89	R2	R2	R2	9	

**NOTE :-**

If grammar is not CLR(1), then it must not be LALR(1), but if the grammar is LALR(1), then we manually need to check whether the grammar is LALRL(1) or not, bcoz it might be a chance, that during the merge operation in LALR(1), we must face S-R or R-R conflicts.

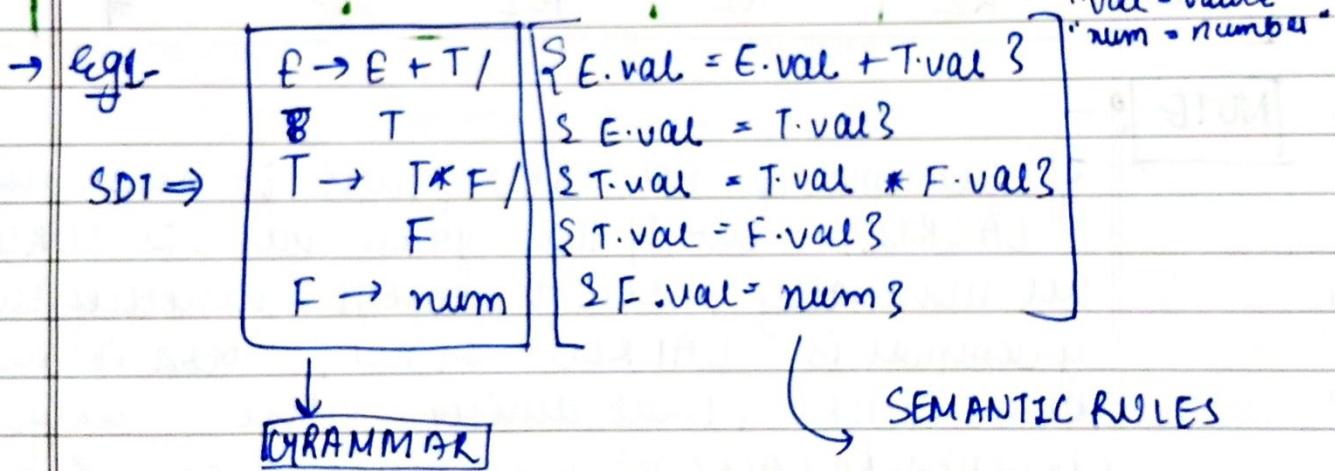
UNJ1-3

## SYNTAX DIRECTED TRANSLATION

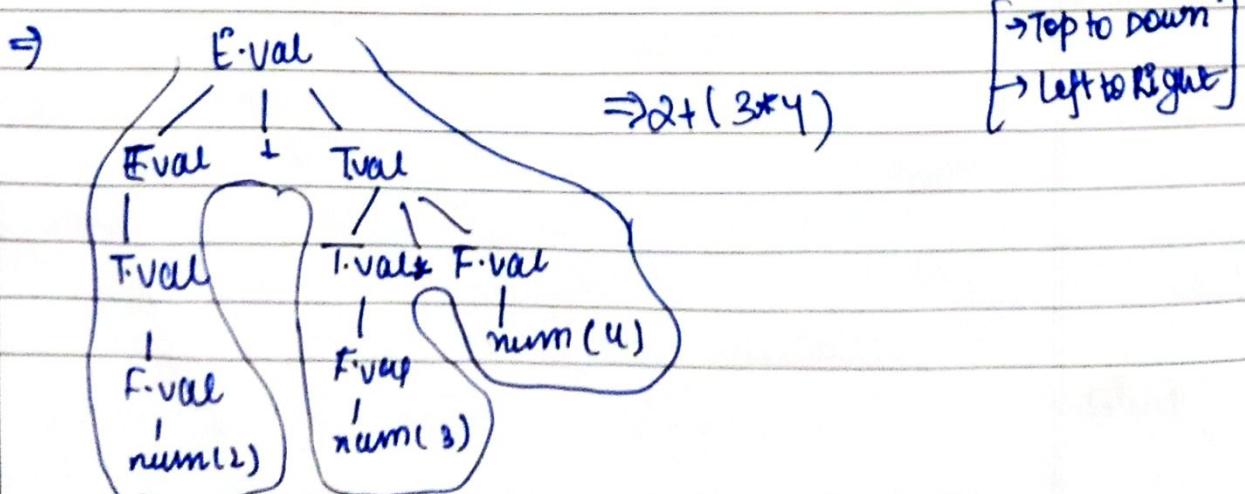
(GRAMMAR + SEMANTIC RULES)

### \* SEMANTIC RULES :-

→ Informal notation. Semantic rules are the meaningful rules that are helpful for a compiler, as well as intermediate code generator of expression evaluation.



Now, evaluate the expression "2+3\*4" using the given SDT (Syntax Directed Translation).



These are the few points regarding the above soln.:-

- ① num = token & 2, 3, 4 represents the actual values or lexical values.
- ② Traverse the parse tree :- (i) Top to down  
(ii) left to right
- ③ whenever you find any reduction, the corresponding semantic rule will be activated.

[Hint: F-val

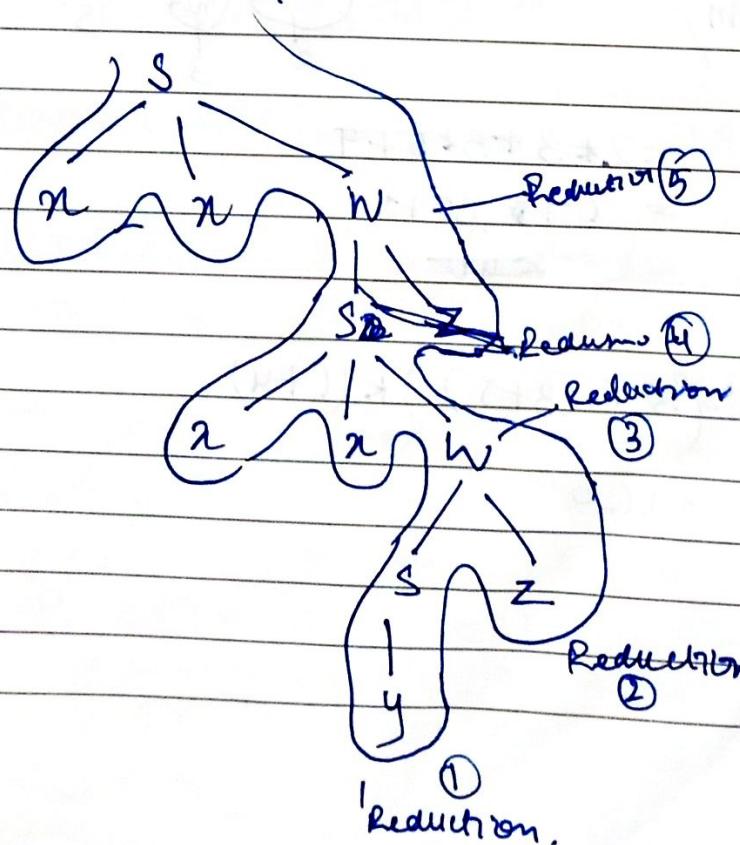
num(2) ↑ Reduction]

The corresponding semantic rule  
i.e. F-val = num gets activated

**NOTE:** - SDT can be implemented using both Top-down parser & Bottom-up parser.

Ex-2:  $S \rightarrow n n w \mid 2 \text{ point}("1"); 3$   
 $y \quad \quad \quad S \text{ point}("2"); 3$   
 $w \rightarrow S z \quad S \text{ point}("3"); 3$

What is the output  
of this SDT while  
generating the string:  
"nnnxyzz"



⇒ 23131

Eg-3

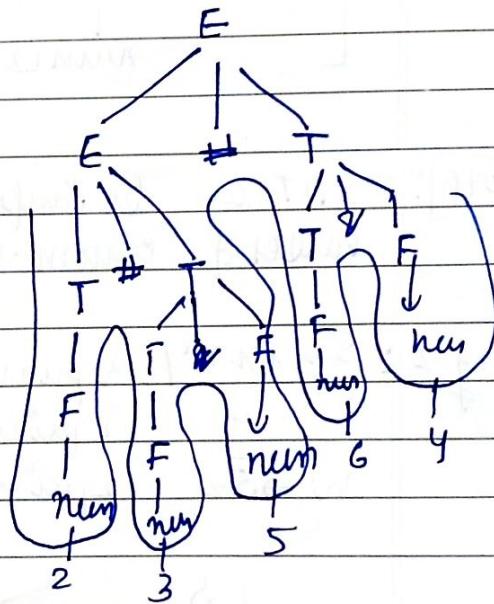
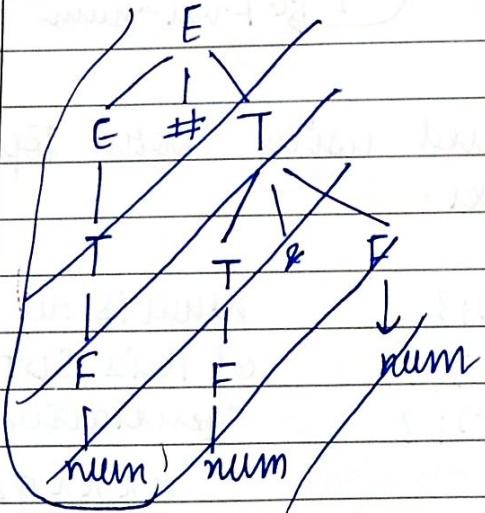
$$\begin{array}{l} E \rightarrow E \# T \mid \\ \quad T \qquad \left\{ \begin{array}{l} E \cdot \text{val} = E \cdot \text{val} * T \cdot \text{val} \\ E \cdot \text{val} = T \cdot \text{val} \end{array} \right. \\ T \rightarrow T \& F \mid \\ \quad F \qquad \left\{ \begin{array}{l} T \cdot \text{val} = T \cdot \text{val} + F \cdot \text{val} \\ T \cdot \text{val} = F \cdot \text{val} \end{array} \right. \\ F \rightarrow \text{num} \qquad \left\{ \begin{array}{l} F \cdot \text{val} = \text{num} \\ \text{val} = \text{num} \end{array} \right. \end{array}$$

(160)

Evaluate the following using acc. to the given SDF.

$2 \# 3 \& 5 \# 6 \& 4$

$\Rightarrow$



$$= 2 * 3 + 5 * 6 + 4$$

$$= 6 + 30 + 4$$

$$= 40$$

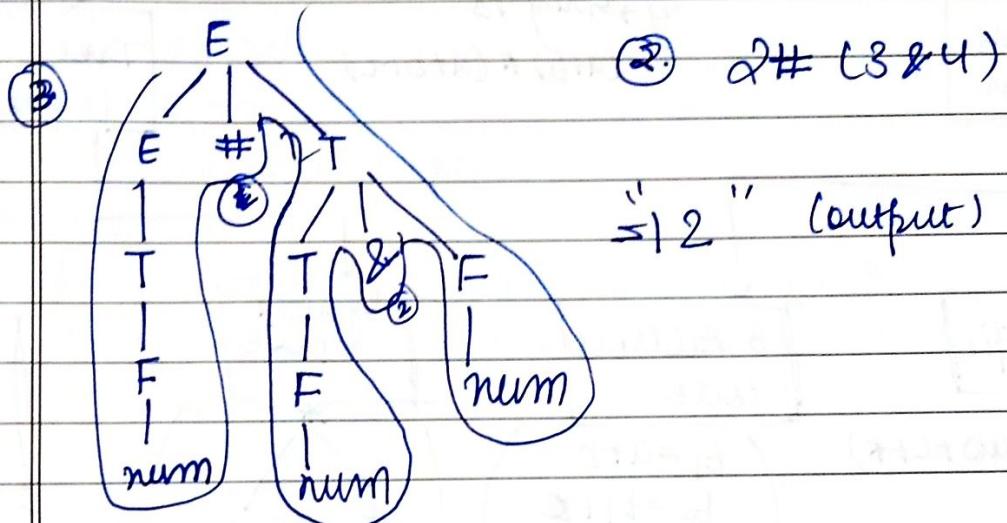
$$= (2 * (3 + 5)) + (6 + 4)$$

$$= 160$$

\* Special Example:-

(1)  $E \rightarrow E \# \& \text{ print} ("1") \{ T \mid T$   
 $T \rightarrow T \& \text{ print} ("2") \{ F \mid F$   
 $F \rightarrow \text{num} \}$   $F . \text{val} = \text{num} \}$

semantic rule can  
also arise in b/w  
production.



But if the ~~last~~ semantic rule was after the grammar, then we must write geo the output as "21".

\* INTERMEDIATE CODE GENERATION:-

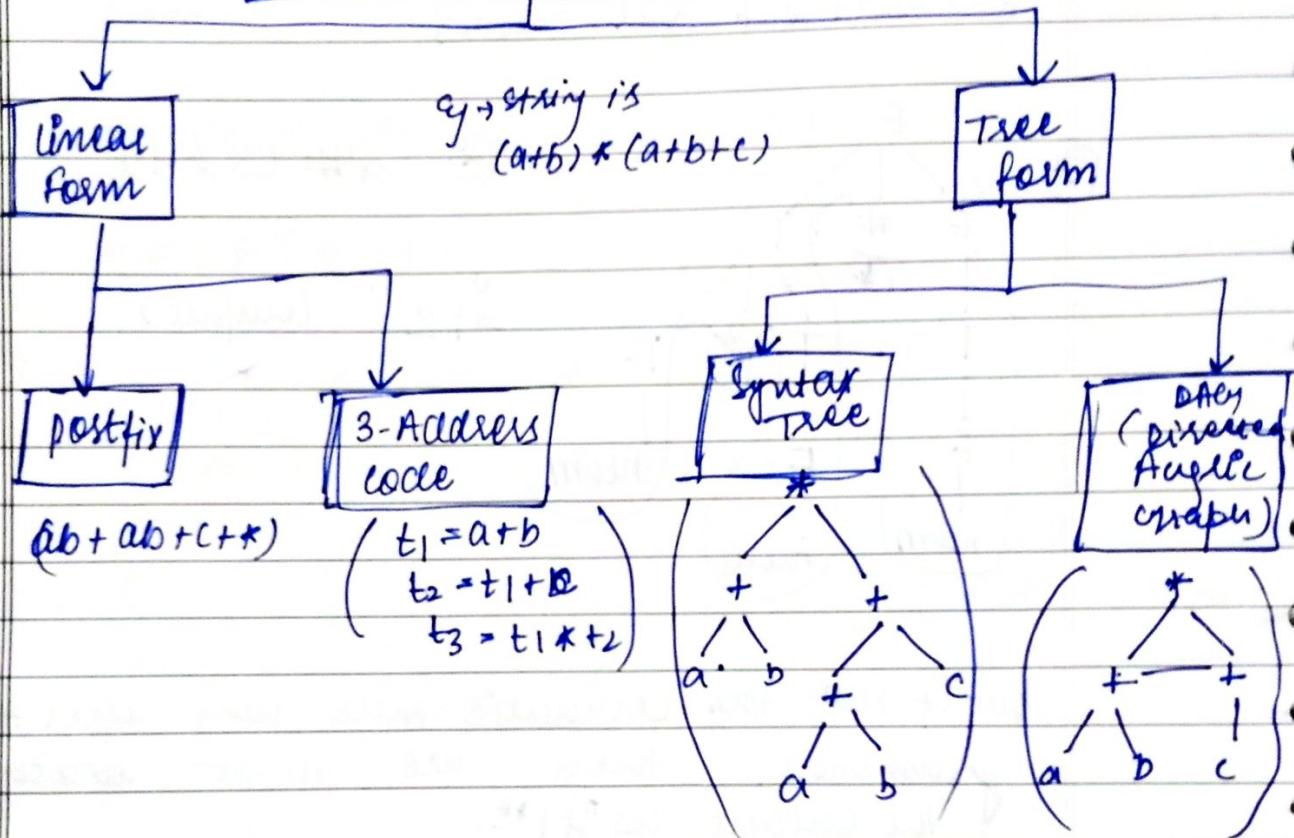
It works as a middle-ware in between source lang. & machine lang. / assembly lang.

We cannot directly convert the source lang. directly into machine lang. because for this reason we require native compiler for each individual machine with different configuration. (like different O.S)

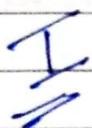
ICG helps to generate an intermediate code which is native for each & every individual machine.

\* Types:-

### Intermediate Code Generation (ICG)



\* TYPES OF ICG:-



### POSTFIX NOTATION:-

① Eg:-  $(a+b)* (a+b+c) \rightarrow (ab + ab + c + *)$

$$\begin{aligned} ab &\rightarrow ab \\ a+b*c &\rightarrow abc*+ \end{aligned}$$

II

## 3-ADDRESS CODE:-

This is the most frequent & famous 3 address code representation. There are 3 basic types of 3-Address code:-

- (1) Quadruples
- (2) Triple
- (3) Indirect Triple.

15/Nov/2021

Eg:-  ~~$a+b+c$~~  -  $(a+b)*(c+d)+(a+b+c)$

The general representation of ICFG through a 3-Address code is like :-

- (1)  $t_1 = a + b$
- (2)  $t_2 = -t_1$
- (3)  $t_3 = c + d$
- (4)  $t_4 = t_2 * t_3$
- (5)  $t_5 = a + b + c$
- (6)  $t_6 = t_5 + c$
- (7)  $t_7 = t_4 + t_6$

After writing the general representation we will proceed for quadruples, triples, indirect triple representation of the expression.

- (1) Quadruple representation:-

operator	operand (1)	operand (2)	Result
1. +	a	b	
2. -	t <sub>1</sub>		
3. +	c	d	
4. *	t <sub>2</sub>	t <sub>3</sub>	
5. +	a	b	
6. +	t <sub>5</sub>	c	
7. +	t <sub>4</sub>	t <sub>6</sub>	

→ Advantage:- Statement can be move around.

→ Disadvantage:- Too much space is wasted.

### (2) Triple Representation:-

operator	operand (1)	operand (2)
1 (i) +	a	b
2 (ii) -	t <sub>1</sub> (i)	
3 (iii) *	c	d
4 (iv) +	t <sub>2</sub> (ii)	t <sub>3</sub> (iii)
5 (v) +	a	b
6 (vi) +	t <sub>4</sub> (v)	c
7 (vii) +	t <sub>5</sub> (iv)	t <sub>6</sub> (vi)

→ Advantage:- Space is not wasted.

→ Disadvantage:- Statement cannot move around.

### (5) Indirect Triple representation:-

1. (I.)
2. (ii.)
3. (iii.)
4. (IV.)
5. (V.)
6. (VI.)
7. (Vii.)

In indirect triple, each instruction is not need to put into main memory only keep your instruction no. (pointer) in main memory & let the instructions to be in secondary memory

→ disadvantage - at least 2 memory access required

→ advantage - statements can be moved around.

→ BACK PATCHING :-  
(conversion to 3-Address code)

e.g.:  $\begin{cases} \text{if } (a < b) \text{ then } \\ \quad \text{else } t = 0 \end{cases}$  → here we have 4-Address  
( $a, b, t=0, t=1$ ) so we  
need to convert it into 3-Add.

(i.) if ( $a < b$ ) goto ( $i+3$ ) code.

( $i+1$ ) ( $i+1$ )  $t=0$

( $i+2$ ) goto ( $i+1$ )

( $i+3$ )  $t=1$

( $i+4$ )

**NOTE:-** During the conversion of statements into 3 Address code, leaving the ~~some~~ boxes of levels as empty and filling them latter is called backpatching.

e.g.:

$a < b \text{ and } c < d \text{ or } e < f$

100) if ( $a < b$ ) goto —

101)  $t_1 = 0$

102) goto —

103)  $t_1 = 1$

104) if ( $c < d$ ) goto —

105)  $t_2 = 0$

106) goto —

107)  $t_2 = 1$

108) if ( $e < f$ ) goto —

109)  $t_3 = 0$

110) goto —

111)  $t_3 = 1$

112)  $t_4 = t_1 \text{ and } t_3$

113)  $t_5 = t_4 \& t_3$

Note:  $[t_1 \ a < b \mid t_2 = c < d \mid t_3 = e < f]$