No. of times loop is running be k

$$SK = 1 + 3 + 6 + 10 \cdot t ... + TK$$
 $SK-1=$ 

Subtracting both

 $SK - SK-1 = 1 + 2 + 3 + 4 + ... + (K-1)$ 
 $T_{K} = \frac{(K-1) K}{2}$ 

Given that kth term is n.

$$\frac{T_{k} = n}{k(k-1)} = n = \frac{k^{2}}{2} - \frac{k}{2} = n$$

$$\Rightarrow k^{2} = n$$

$$\Rightarrow k = \sqrt{n}$$

$$\Rightarrow \left[ \frac{T(n)}{2} = O(\sqrt{n}) \right]$$

2. 
$$T(n) = T(n-1) + T(n-2) + O(1)$$
  
For recursive dibonacci

Recursion Tree: n-1 n-2 n-3 n-3 n-4 n-4 n-5 n-6 n-6

No. of times teep function ix running will be sum of the series:  $2 = 1 + 2 + 4 + \dots + 2^n$   $= \frac{2^{n+1} - 1}{2 - 1}$ Time Complexity:

$$O(\log(\log n))$$
: for (int i=2; i <= n; i= pow (i,3))

$$i = pow(i,3)$$

$$i = pow(i,3)$$

$$i = pow(i,3)$$

\* Here n can be any positive integer.

4. 
$$T(n) = T\left(\frac{n}{4}\right) + T\left(\frac{n}{2}\right) + cn^2$$

Ignoring lower order terms:
$$T(n) = T(\frac{n}{2}) + Cn^{2}$$

$$\alpha = 1$$
,  $6 = 20$ ,  $f(n) = n^2$ 

$$C = loj_b a = loj_z 1 = 0$$

$$\Rightarrow |\tau(n) = \theta(n^2)|$$

$$g = \frac{n}{1} + \frac{n}{2} + \frac{n}{3} + \cdots$$

$$\frac{n}{2}$$

$$\frac{1}{3} \frac{n}{3} = \sum_{i=1}^{n} \left(\frac{n}{i}\right)$$

Complexity = 
$$n \times \sum_{i=1}^{n} \left(\frac{n}{i}\right)$$

$$|T(n)| = n \log n$$

sequence:

=> 
$$2^{k^{1}}$$
 = n

$$K^{2}$$
 log  $2 = log \pi$ 
 $K^{2}$  log  $2 = log \pi$ 

[Ignoring constant (log 2)]

 $K^{2}$ 

(
$$\lambda$$
-1)  $loj k = koj(koj n)$ 

$$|\lambda = loj(loj n)|$$
(19 noring constant terms)

$$< log(n!) < n^{2} < log n < log n < log n < 2(log n)$$
 $< log n < log n < log n! < n^{2} < log n < log n! < n^{2} < n!$ 
 $< n < n log n < 2n < 4n < log (n!) < n^{2} < n!$ 
 $< 2^{2^{n}}$ 

(c) 
$$96 < \log_8 n < \log_2 n < 5n < n(\log_6 n) < n(\log_2 n) < \log_2 n < 3n^3 < n! < 8^{2n}$$

$$\log(n!) < 8n^2 < 7n^3 < n! < 8^{2n}$$