

## Home assignment № 2

Solutions should be sent to [fdr.strok@yandex.ru](mailto:fdr.strok@yandex.ru)

Deadline is 08:59 20/10/2018

Template for the title: [Posets & DM] - %Name Surname% - 2,

example, [Posets & DM] – Fedor Strok – 2

Allowed formats: .doc, .pdf. You can use either Latex or Word. Scans of pictures (if necessary) are accepted.

### Task 1

Compute all formal concepts for the following formal context K (use the definition).

A formal concept – is a pair  $(A, B)$ , such that:  $A \in 2^G, B \in 2^M, A' = B, B' = A$

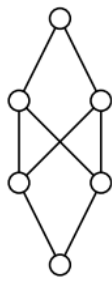
Where  $A' = \{m \in M | (g, m) \in I \text{ for all } g \text{ in } A\}$

|                             | Latin America | Europe | Canada | Asia Pacific | Middle East | Africa | Mexico | Caribbean | United States |
|-----------------------------|---------------|--------|--------|--------------|-------------|--------|--------|-----------|---------------|
| Air Canada                  | X             | X      | X      | X            | X           |        | X      | X         | X             |
| Air New Zealand             |               | X      |        | X            |             |        |        |           | X             |
| All Nippon Airways          |               | X      |        | X            |             |        |        |           | X             |
| Ansett Australia            |               |        |        | X            |             |        |        |           |               |
| The Austrian Airlines Group |               | X      | X      | X            | X           | X      |        |           | X             |
| British Midland             |               | X      |        |              |             |        |        |           |               |
| Lufthansa                   | X             | X      | X      | X            | X           | X      | X      |           | X             |
| Mexicana                    | X             |        | X      |              |             |        | X      | X         | X             |
| Scandinavian Airlines       | X             | X      |        | X            |             | X      |        |           | X             |
| Singapore Airlines          |               | X      | X      | X            | X           | X      |        |           | X             |
| Thai Airways International  | X             | X      |        | X            |             |        |        | X         | X             |
| United Airlines             | X             | X      | X      | X            |             |        | X      | X         | X             |
| VARIG                       | X             | X      |        | X            |             | X      | X      |           | X             |

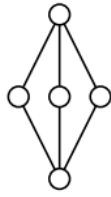
### Task 2

Which of the following figures represent a lattice? Why?

Are there any complete lattices?



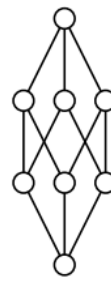
(i)



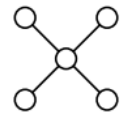
(ii)



(iii)



(iv)



(v)

### Task 3

Let  $(L, \leq)$  be a lattice with infimum and supremum defined as usual.

Prove that for any  $x, y \in L$

- $x \vee x = x$
- $x \vee (x \wedge y) = x$
- $x \vee y = y \vee x$