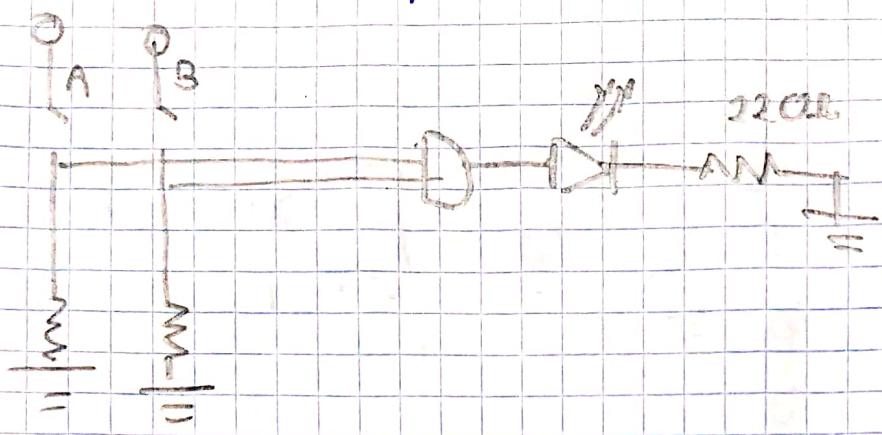
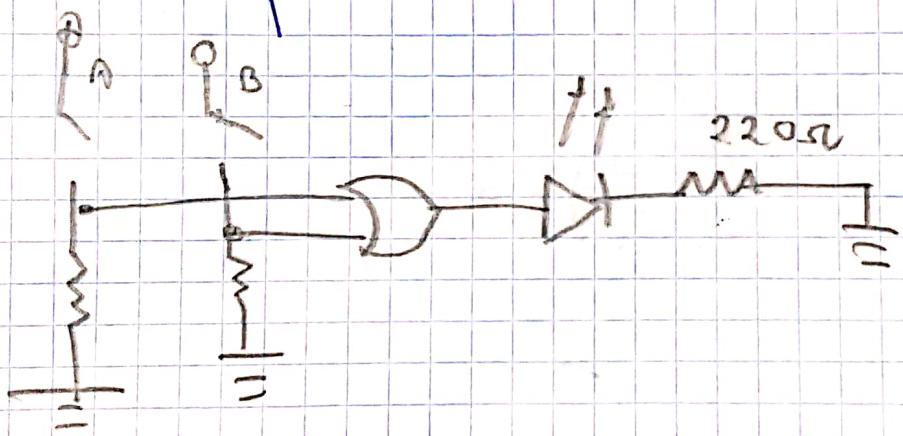


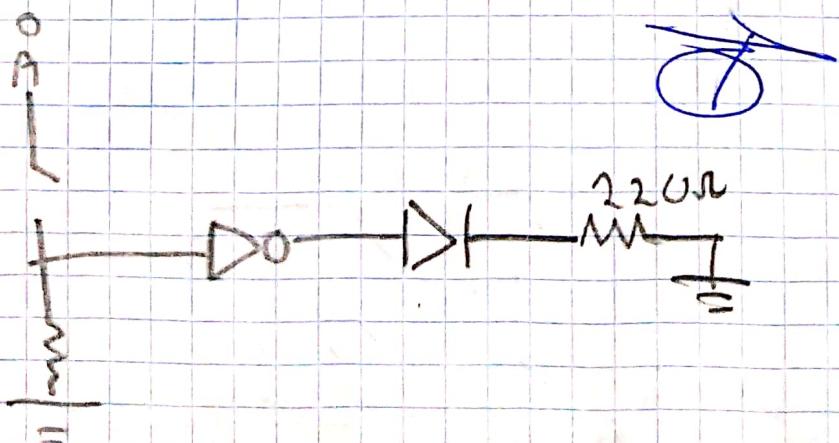
AND ~~N~~



OR ~~N~~

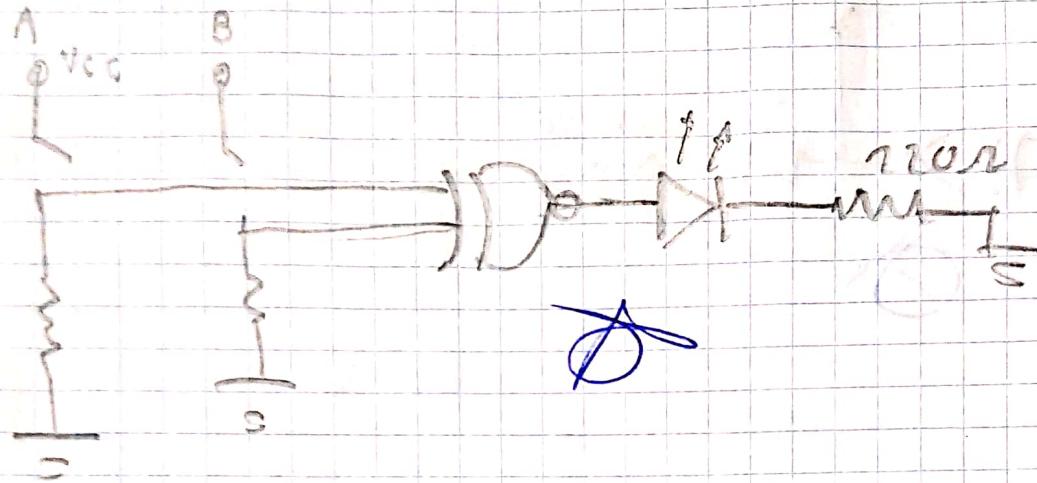


NOT

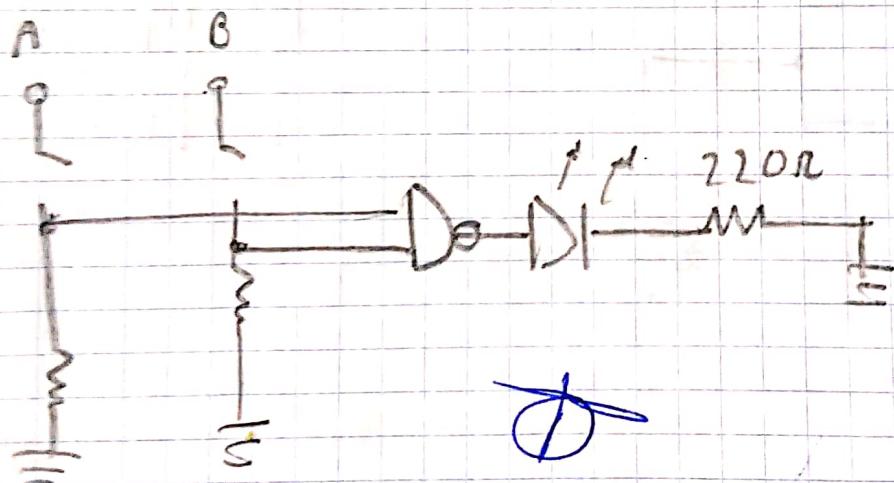


NOR NAND

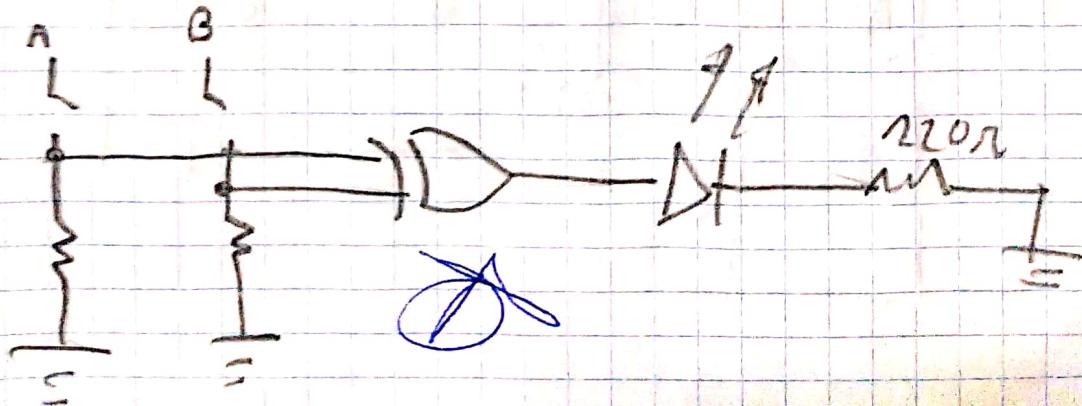
NOR

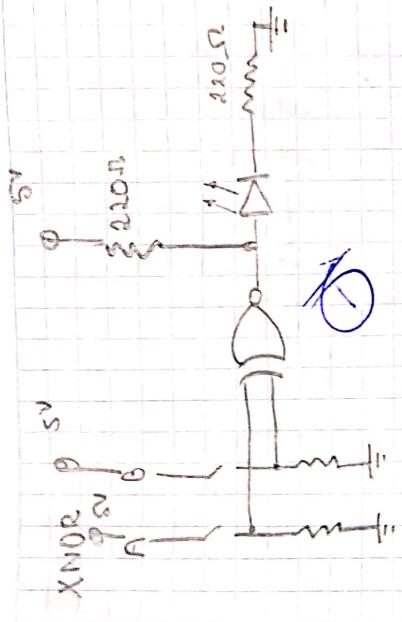


NAND

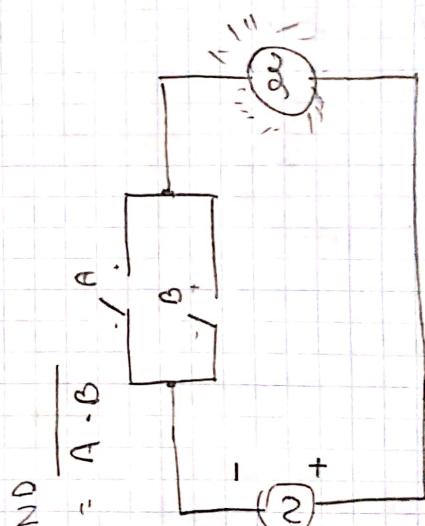


XOR

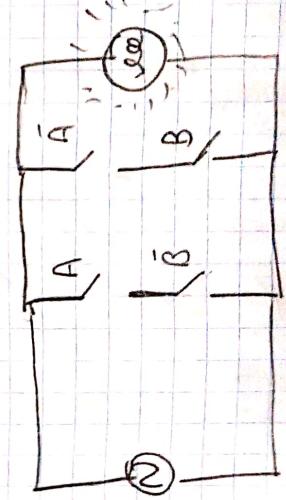




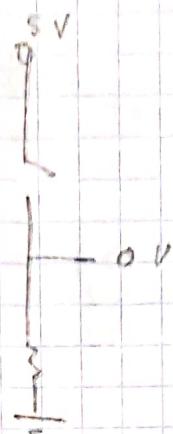
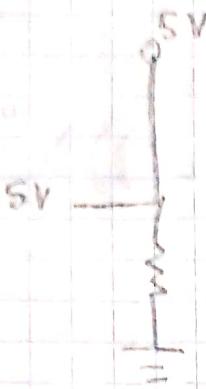
	S	-	-	0
A	0	-	0	-
B	0	0	-	-



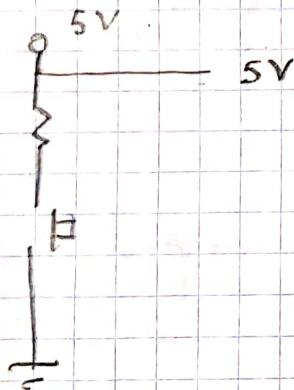
A	B	S	-	0	0	-
0	0	-	-	0	0	-
0	0	-	-	0	0	-



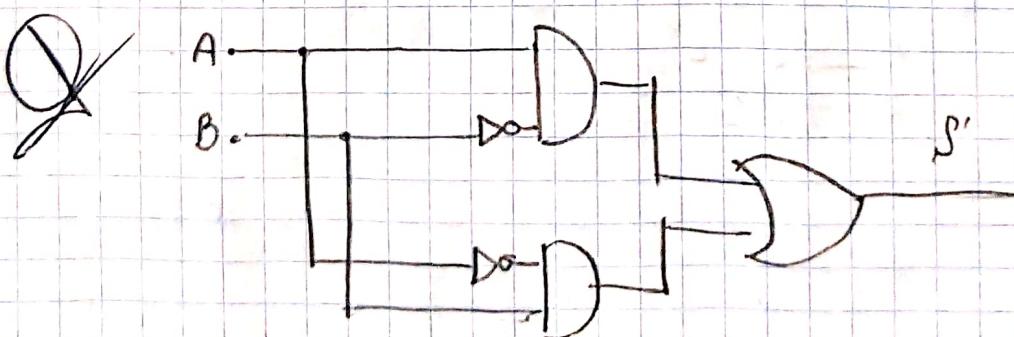
Lógica Positiva



Lógica Negativa



$$\text{XOR} = A\bar{B} + \bar{A}B$$

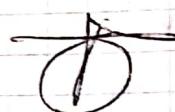
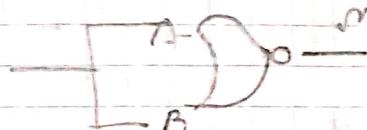


NOR

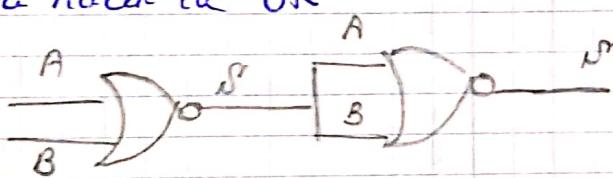
A	B	S
0	0	1
0	1	0
1	0	0
1	1	0



Para hacer la NOT

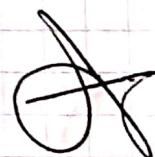


Para hacer la OR



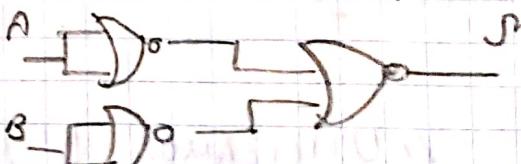
Para hacer la AND

$$\overline{A+B} = \overline{A} \cdot \overline{B}$$



Por Teorema D' Morgan

$$\overline{A+B} = \overline{A} \cdot \overline{B} =$$



$$\overline{A \cdot B} = \overline{A} + \overline{B}$$

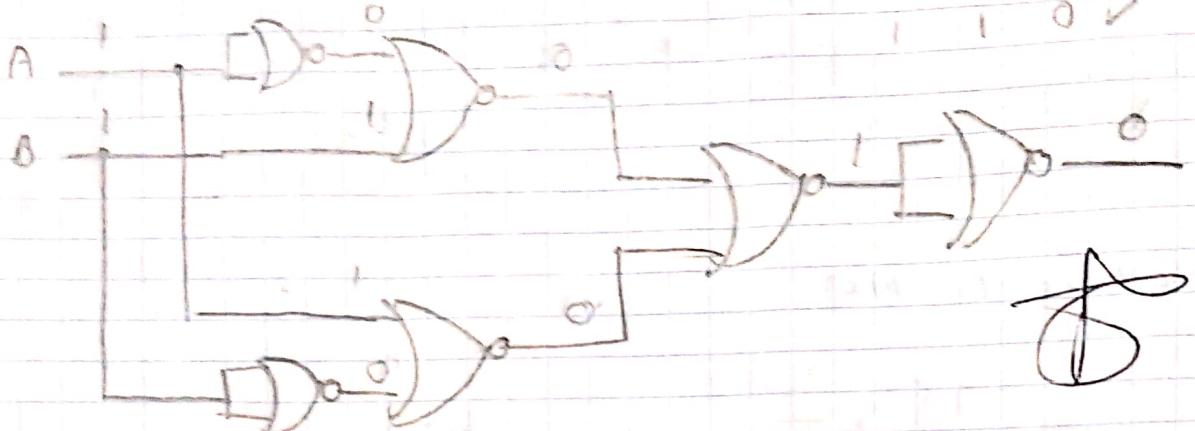
Comprobamos

AND

A	B	S
0	0	0
0	1	0
1	0	0
1	1	1



XOR

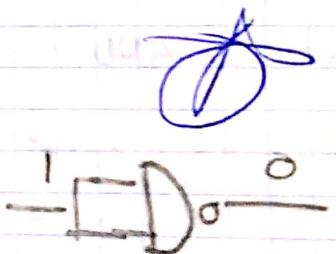


II Construcción de compuertas con la NAND



A	B	S
0	0	1
0	1	1
1	0	1
1	1	0

NOT



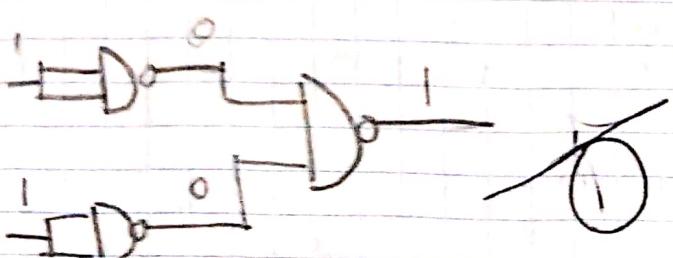
OR // UTILIZAMOS D' MORGAN

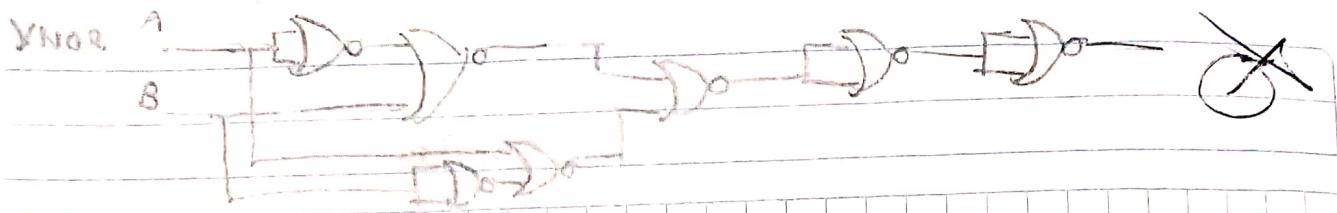
$$\overline{A+B} = \overline{A} \cdot \overline{B}$$

$$\overline{A \cdot B} = \overline{A} + \overline{B}$$

OR

A	B	S
0	0	0
0	1	1
1	0	1
1	1	1





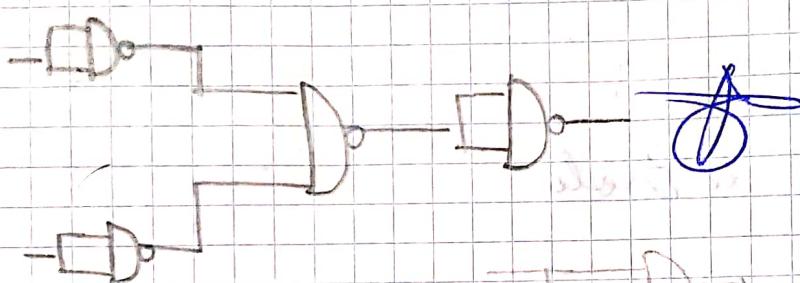
AND



~~NOT~~ AND

A	B	S
0	0	0
0	1	0
1	0	0
1	1	1

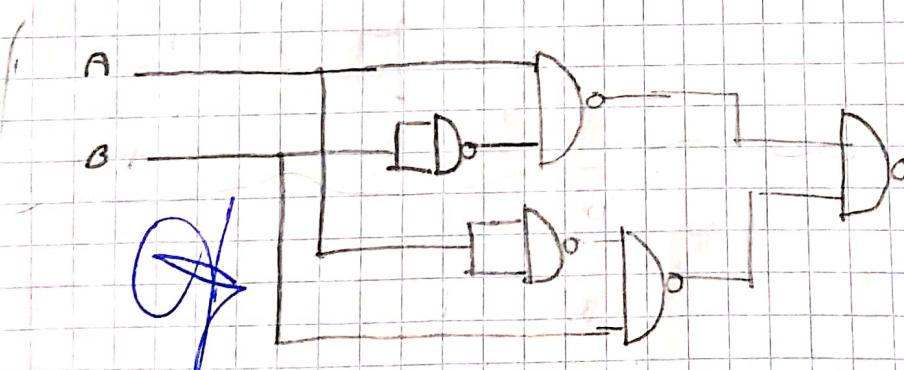
NOE



A	B	S
0	0	1
0	1	0
1	0	0
1	1	0

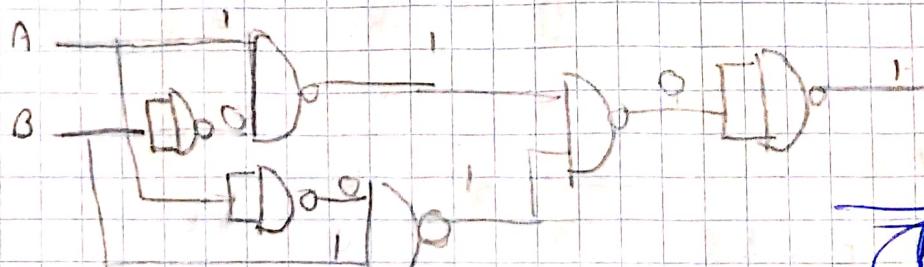
XOR

$$A \bar{B} + \bar{A} B$$



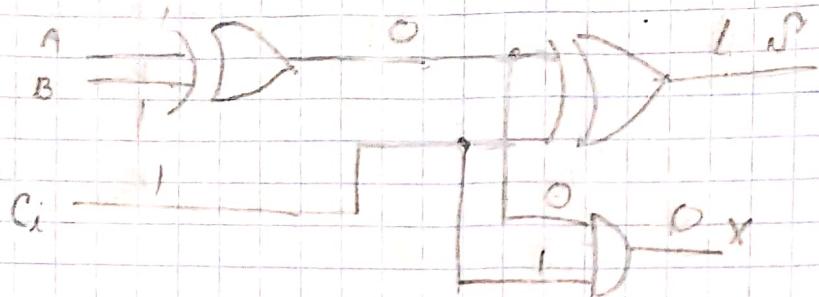
A	B	S
0	0	0
0	1	1
1	0	1
1	1	0

XNOR



A	B	S
0	0	1
0	1	0
1	0	0
1	1	1

* Hacer con NOR y NAND



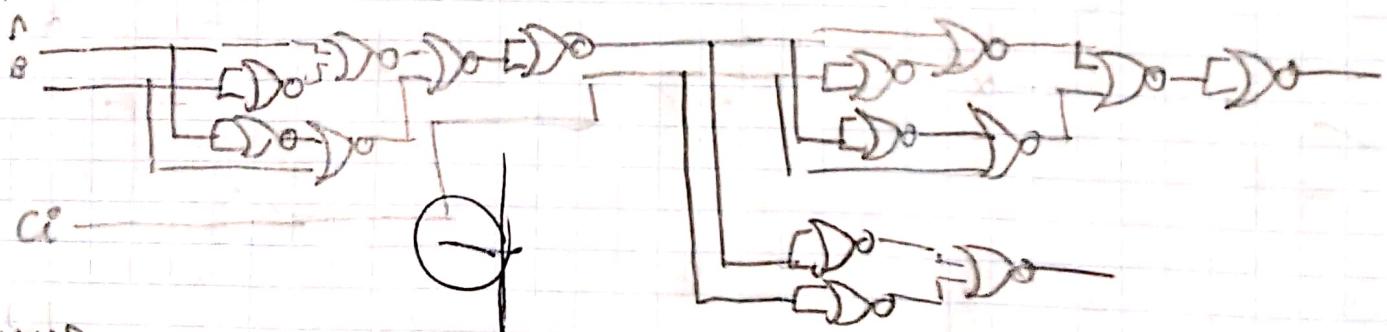
A	B	S
0	0	0
0	1	1
1	0	1
1	1	0

A	B	S
0	0	0
0	1	0
1	0	0
1	1	1

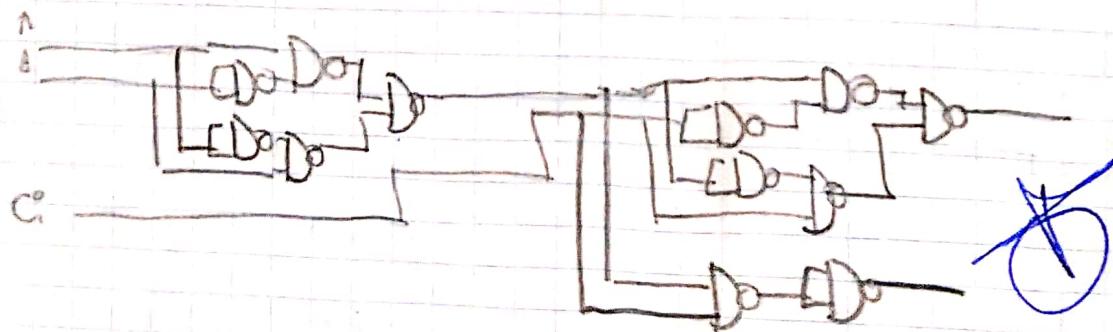
$$\bar{A}B + \bar{A}\bar{B}$$

C°	B	A	S.	X
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	0
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	0

NOR



NAND



Sumar

A	B	suma	Acarreo de Salida
0	0	0	0
0	1	1	0
1	0	0	0
1	1	0	1

{ XOR

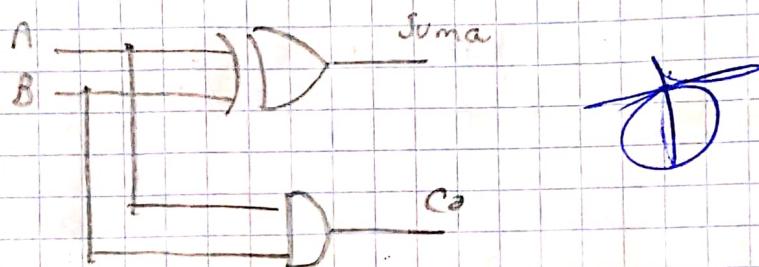
← AND

$$\bar{A}B + \bar{A}B + AB = AB$$

$$\bar{A}(B \oplus B) + \bar{A}(C \oplus B)$$

$$\bar{A} + \bar{A} = \bar{A}$$

Medio Sumador



$$\begin{array}{r}
 + 0 \\
 + 0 \\
 \hline
 0
 \end{array}
 \quad
 \begin{array}{r}
 + 0 \\
 + 1 \\
 \hline
 1
 \end{array}
 \quad
 \begin{array}{r}
 + 1 \\
 + 0 \\
 \hline
 1
 \end{array}
 \quad
 \begin{array}{r}
 + 1 \\
 + 1 \\
 \hline
 0
 \end{array}$$

$Co = 1$

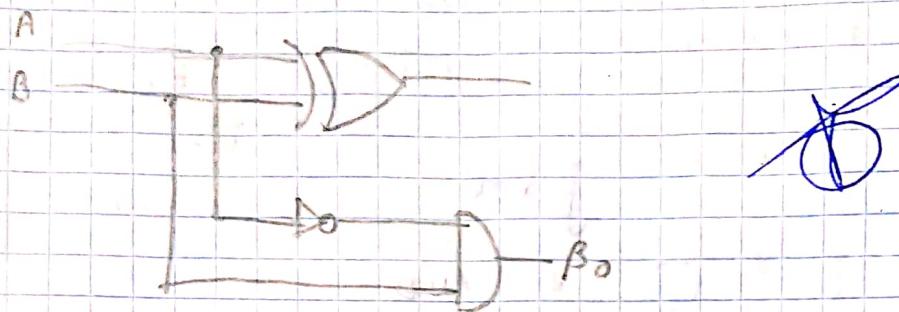
A	B	Resta	Préstamo	β
0	0	0	0	0
0	1	1	1	1
1	0	1	0	0
1	1	0	0	0

← NOT

$$\begin{array}{r}
 0 \quad 0 \\
 - 0 \quad - 1 \\
 \hline
 0 \quad 1
 \end{array}
 \quad
 \begin{array}{r}
 1 \quad 0 \\
 - 0 \\
 \hline
 1
 \end{array}
 \quad
 \begin{array}{r}
 1 \\
 - 1 \\
 \hline
 0
 \end{array}$$

$\beta = 0 \quad \beta = 1 \quad \beta = 0 \quad \beta = 0$

Medio Restador



Hacer el medio sumador y el medio restador con NOR y NOR

* NOR	OR	A	B	S	NOR	A	B	S	$\neg D_o$
		0	0	0		0	0	1	
		0	1	1		0	1	0	
		1	0	1		1	0	0	
		1	1	1		1	1	0	

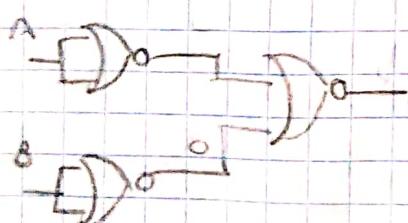
OR



NOT

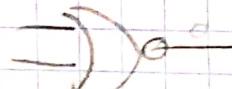


AND

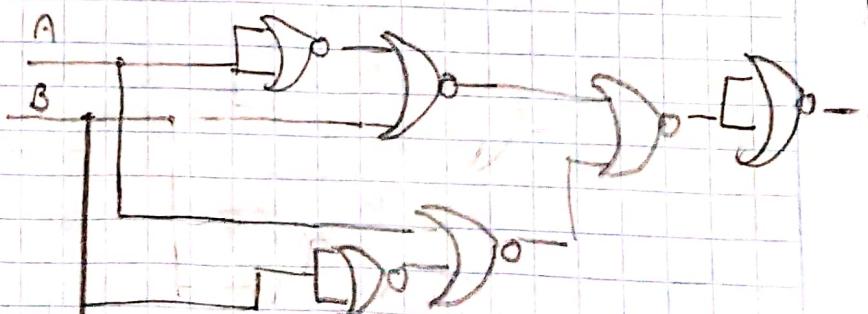


AND

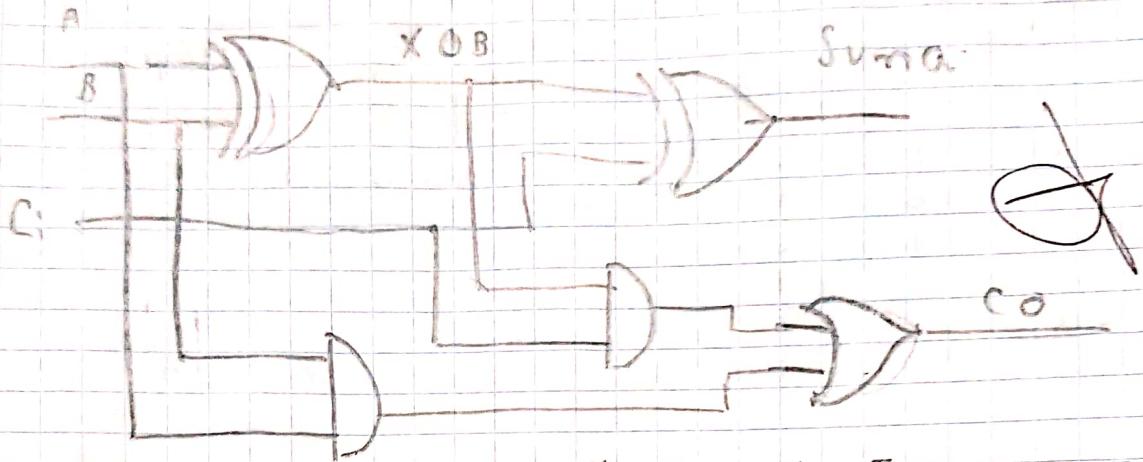
A	B	S
0	0	0
0	1	0
1	0	0
1	1	1



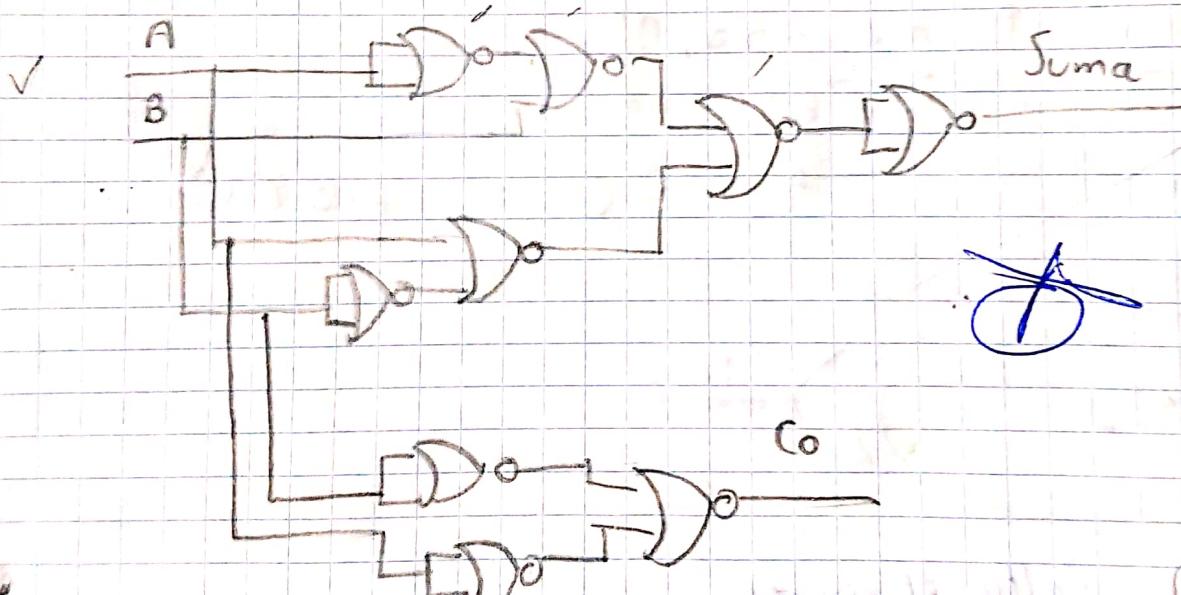
XOR $\bar{A}B + A\bar{B}$



Sumador Completo con acarreo



Medio Sumador con NOR

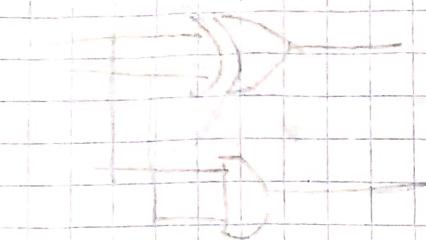


0	0	0
0	1	1
1	0	1
1	1	1

$$\begin{array}{r} 1 \\ + 1 \\ \hline 11 \end{array}$$

Hacer ejercicios de Algebra de Boole.

Medio Sumador con NAND



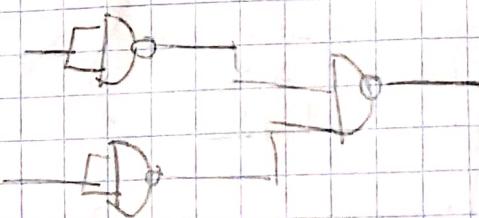
NOT

AND

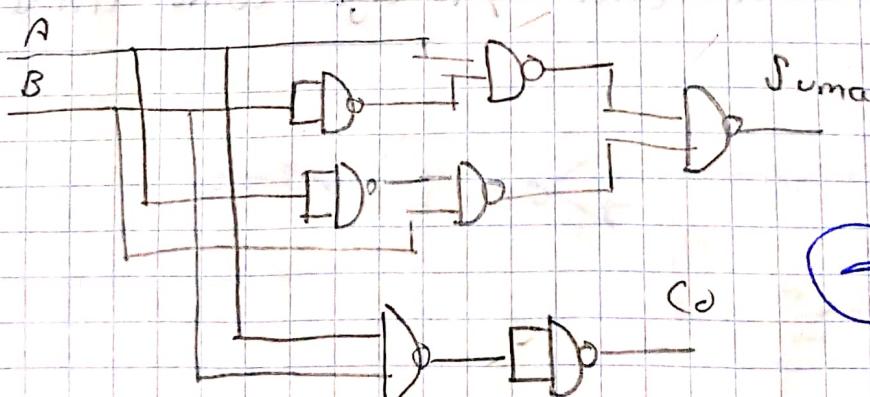
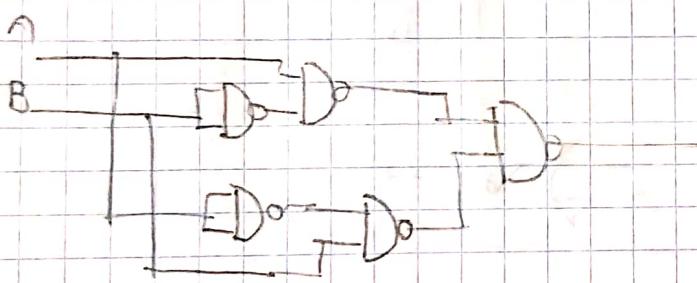
A	B	S
0	0	1
0	1	0
1	0	0
1	1	0



OR

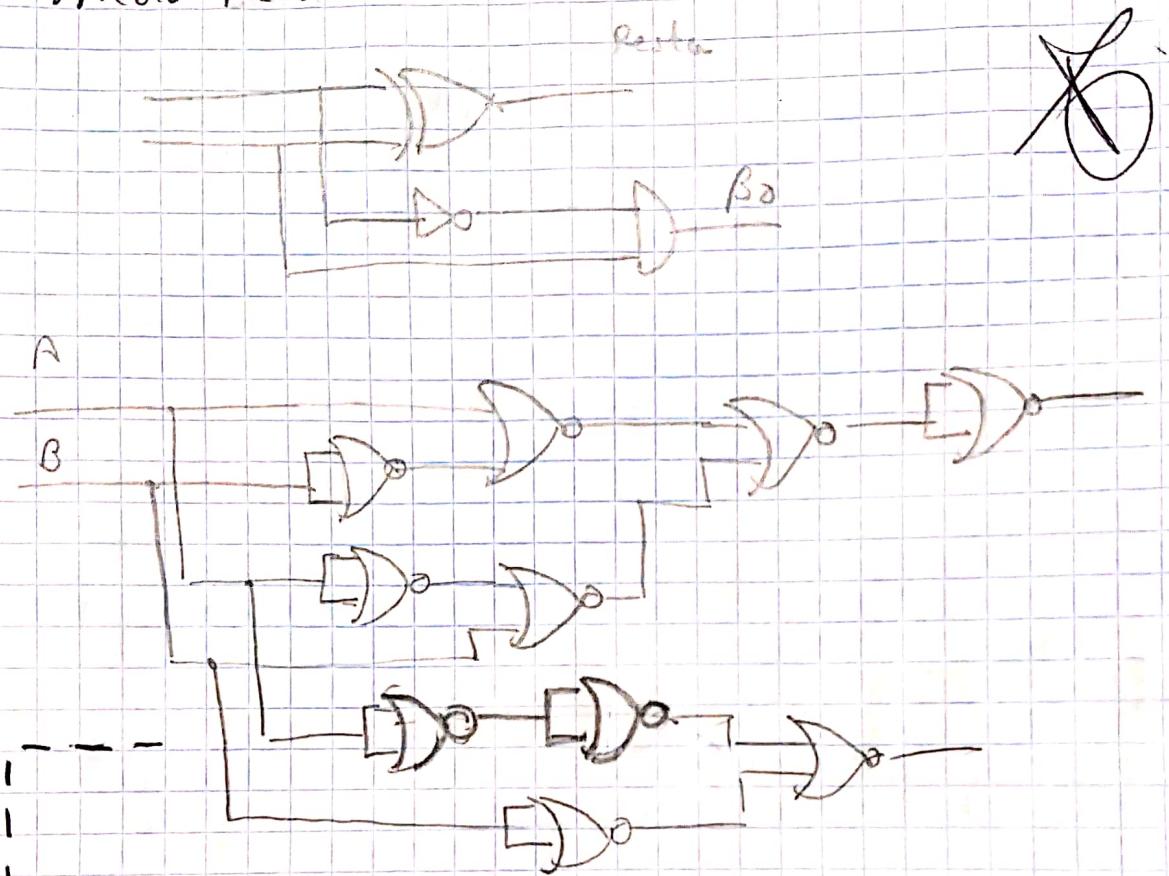


$$A\bar{B} + \bar{A}B$$

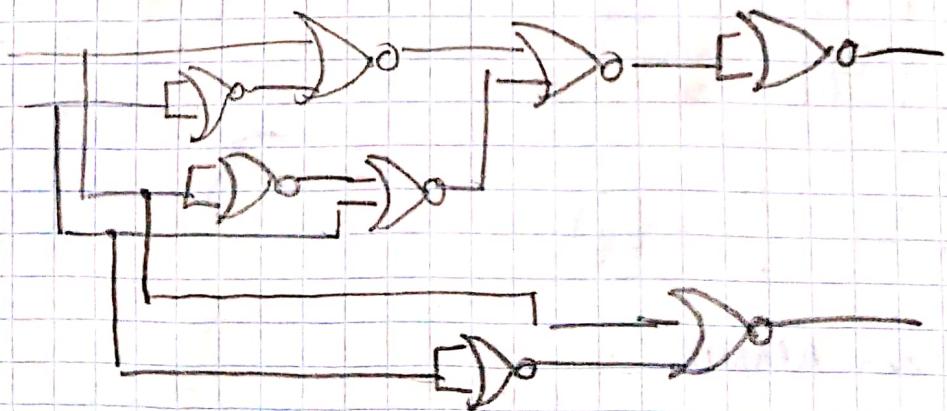


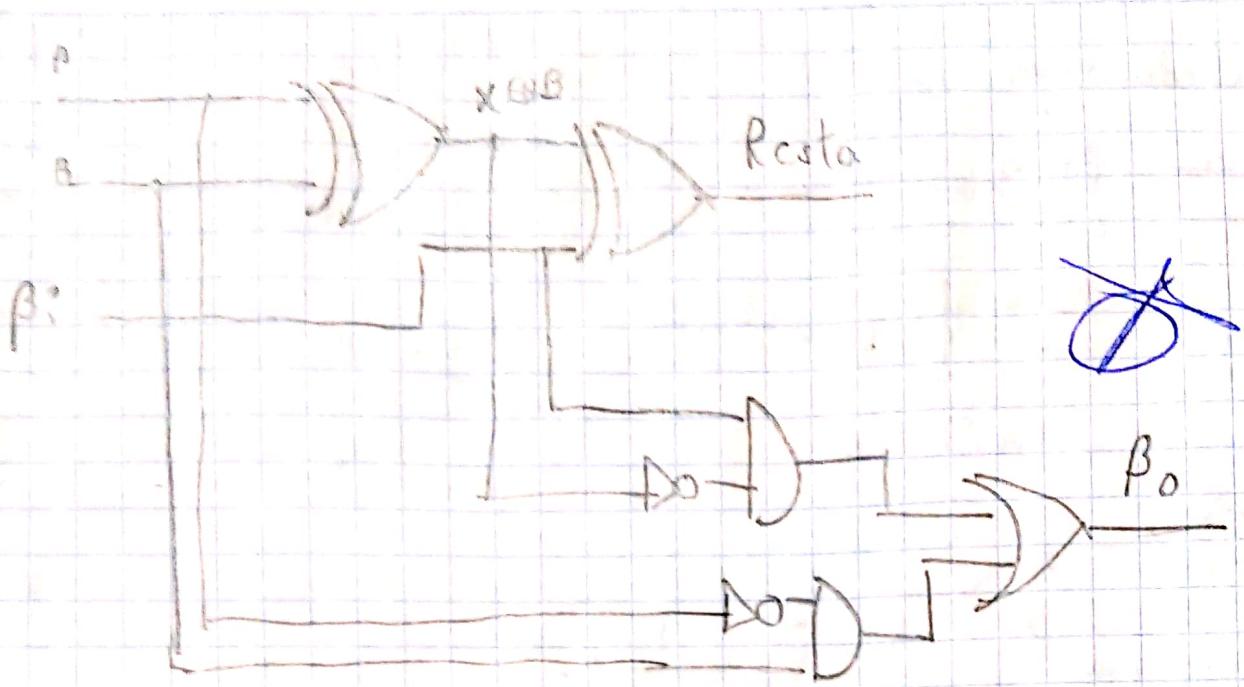
Medio Sumador con NAND

Medio Restador con NOR

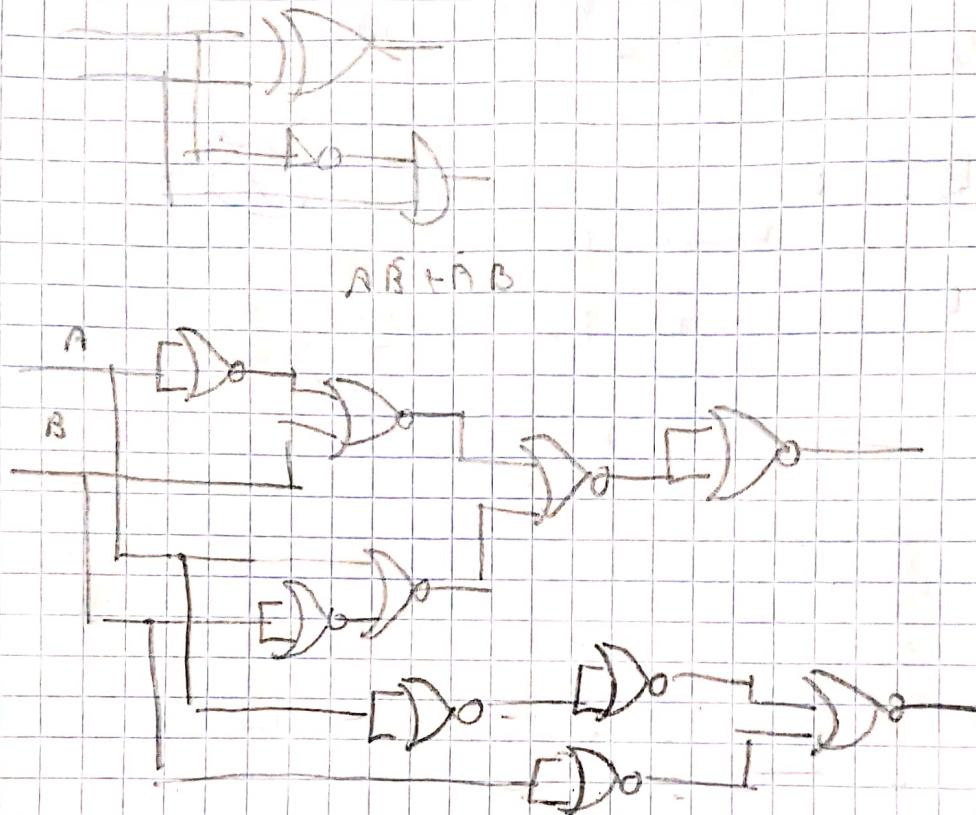


↓
Cuando hay 2 NOT se cancelan y se deja como linea. ~~bás~~

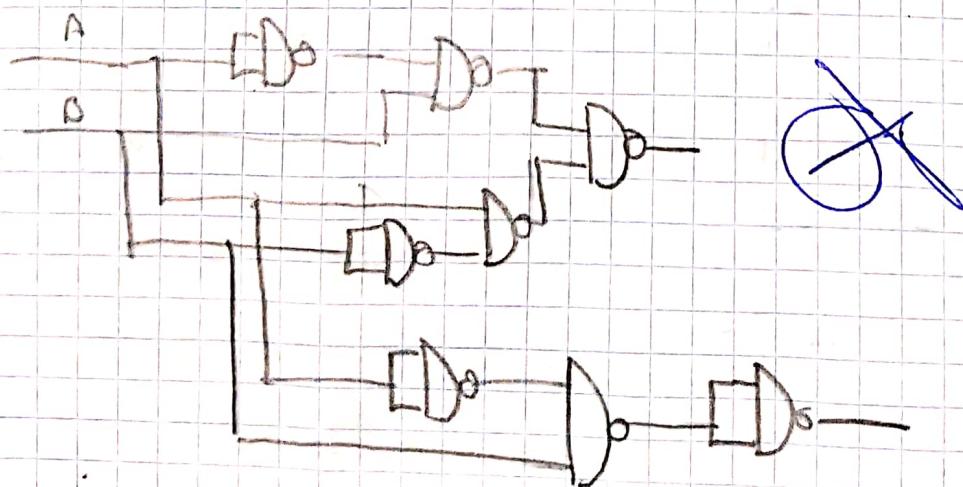




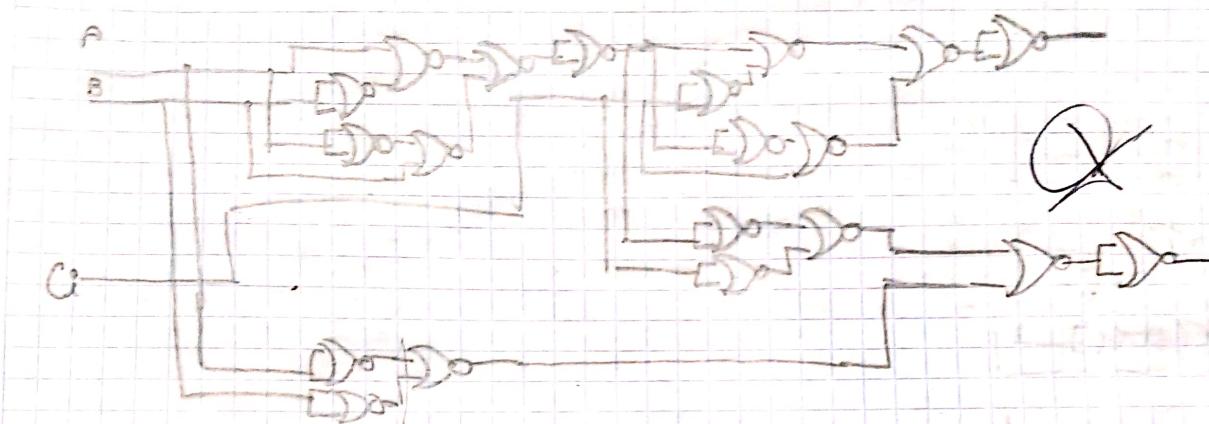
Medio rectificador con NOR



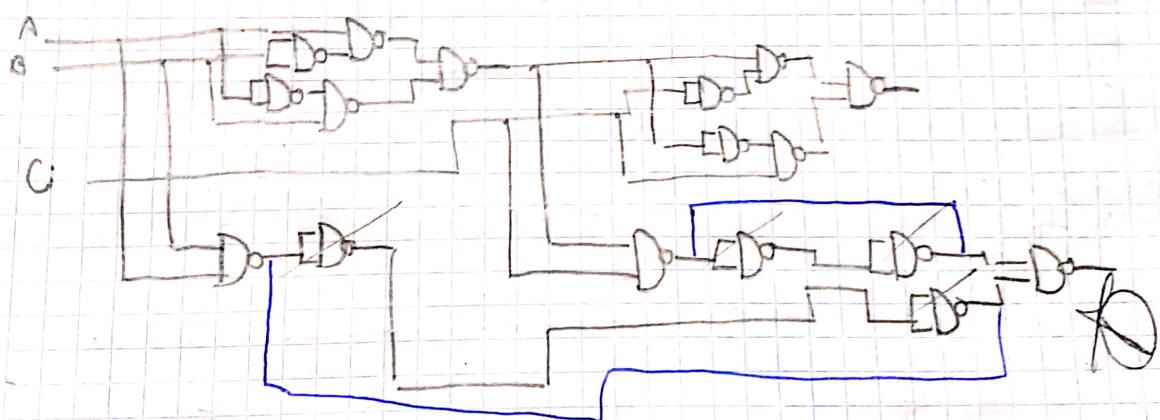
Medio Rectificador con NAND



Sumador completo con NOR



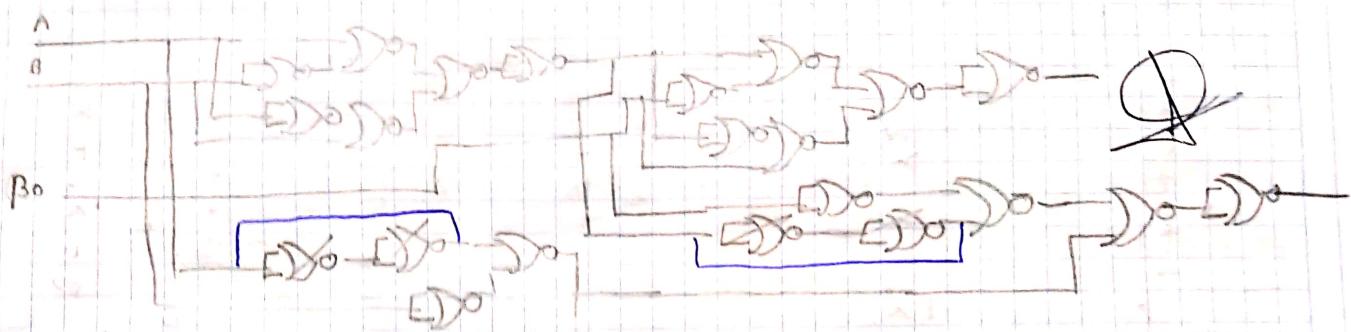
Sumador completo con NAND



Restador Completo con NOR

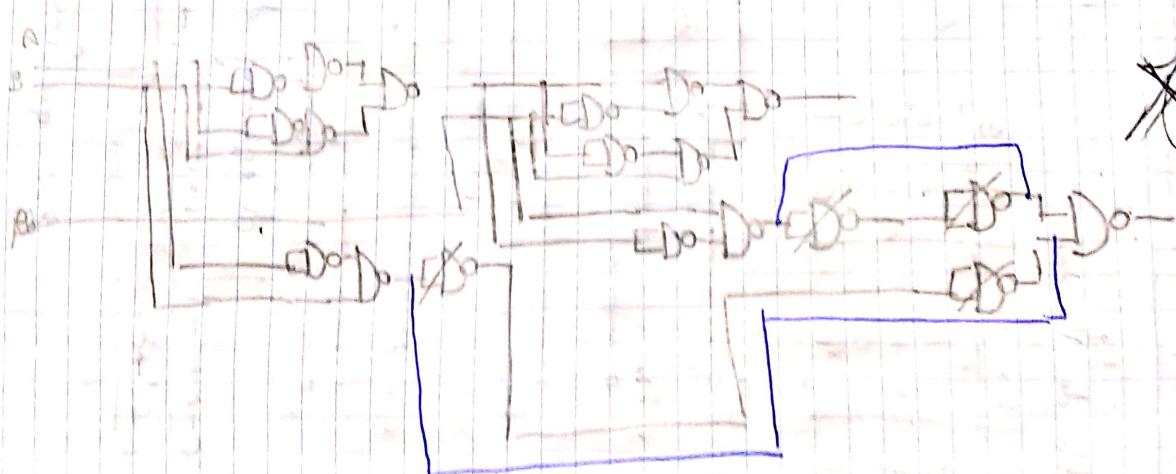
* cable

5 CI



Restador Completo con NAND

4 CI



Reporte

$$\begin{matrix} 1 & 1 & 0 \\ 1 & 1 & 1 \end{matrix}$$

$$\begin{matrix} 1 \\ 0 \end{matrix}$$

$$\begin{matrix} \bar{A}BC \\ AB\bar{C} \end{matrix}$$

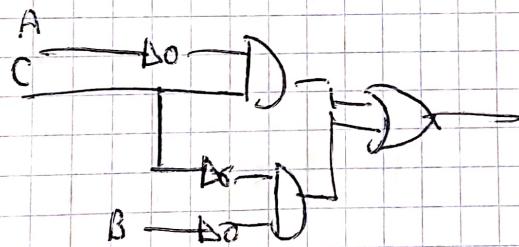
$$\begin{matrix} A + B + C \\ \bar{A} + \bar{B} + \bar{C} \end{matrix}$$

$$f(A, B, C) = \bar{A}\bar{B}\bar{C} + A\bar{B}\bar{C} + \bar{A}B\bar{C} + \bar{A}\bar{B}C \rightarrow \text{Minterms}$$

	A	B	C	000	001	111	110
	0	<input type="checkbox"/>					
	1	<input type="checkbox"/>					

$$f(A, B, C) = \bar{B}\bar{C} + \bar{A}C$$

Minterms

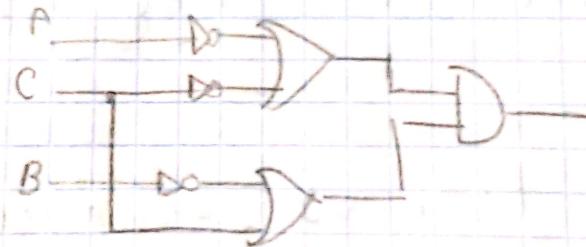
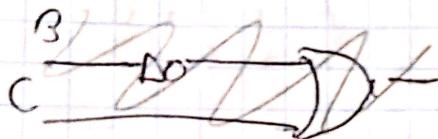


	00	01	11	10
0	0	0		
1			0	0

$$f(A, B, C) = \overline{B\bar{C}} + AC$$

$$= \overline{B} \bar{C} + AC$$

$$= (\overline{B} + C)(\overline{A} + \bar{C})$$



D C B A f(A, B, C, D)

0 0 0 0	1
0 0 0 1	0
0 0 1 0	0
0 0 1 1	1
0 1 0 0	1
0 1 0 1	1
0 1 1 0	0
0 1 1 1	1
1 0 0 0	0
1 0 0 1	0
1 0 1 0	0
1 0 1 1	1
1 1 0 0	0
1 1 0 1	1
1 1 1 0	0
1 1 1 1	1

Minterms
Maxterms

$$\bar{A}\bar{B}\bar{C}\bar{D}$$

Maxterms

$$\bar{A} + B + C + D$$

$$AB\bar{C}\bar{D}$$

$$A + \bar{B} + C + D$$

$$\bar{A}\bar{B}\bar{C}\bar{D}$$

$$\bar{A} + B + C + \bar{D}$$

$$A\bar{B}\bar{C}D$$

$$A + B + \bar{C} + \bar{D}$$

$$A\bar{B}CD$$

$$A + \bar{B} + \bar{C} + \bar{D}$$

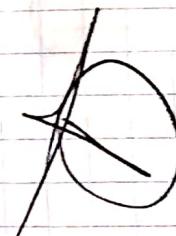
$$AB\bar{C}D$$

$$A + B + C + \bar{D}$$

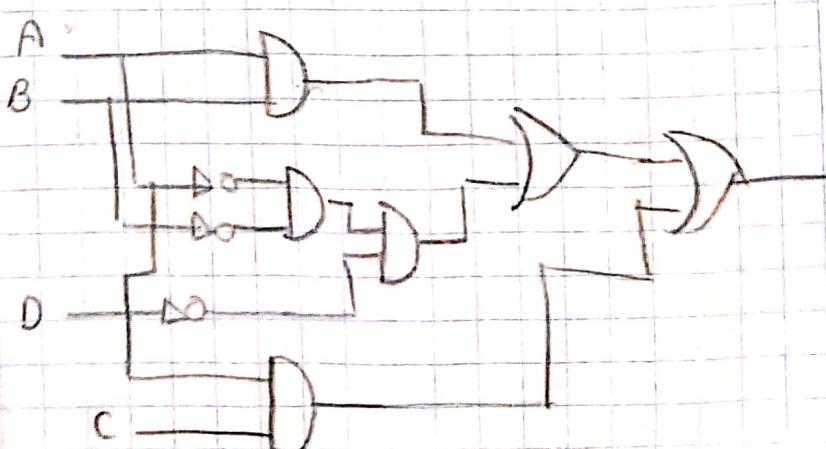
$$f(A, B, C, D) = \bar{A}\bar{B}\bar{C}\bar{D} + AB\bar{C}\bar{D} + \bar{A}\bar{B}C\bar{D} + A\bar{B}C\bar{D} + A\bar{B}C\bar{D}$$

$$+ AB\bar{C}D + A\bar{B}CD + ABCD$$

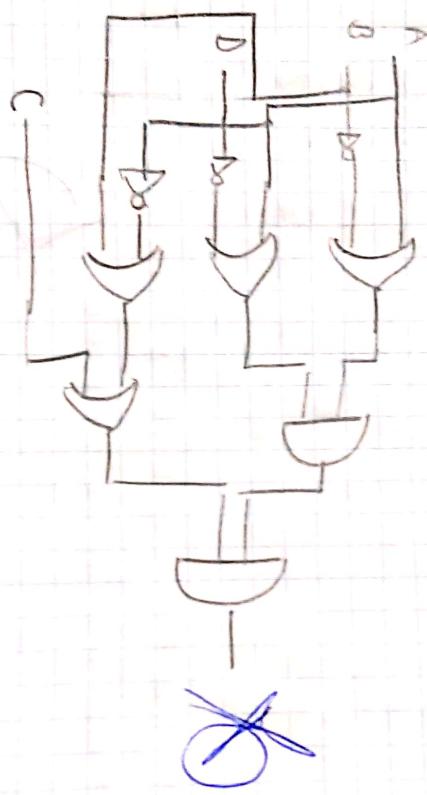
AB	00	01	11	10
CD	00	1	1	
00	1			
01				
11		1	1	
10	1		1	1



$$f(A, B, C, D) = AB + \bar{A}\bar{B}\bar{D} + AC$$

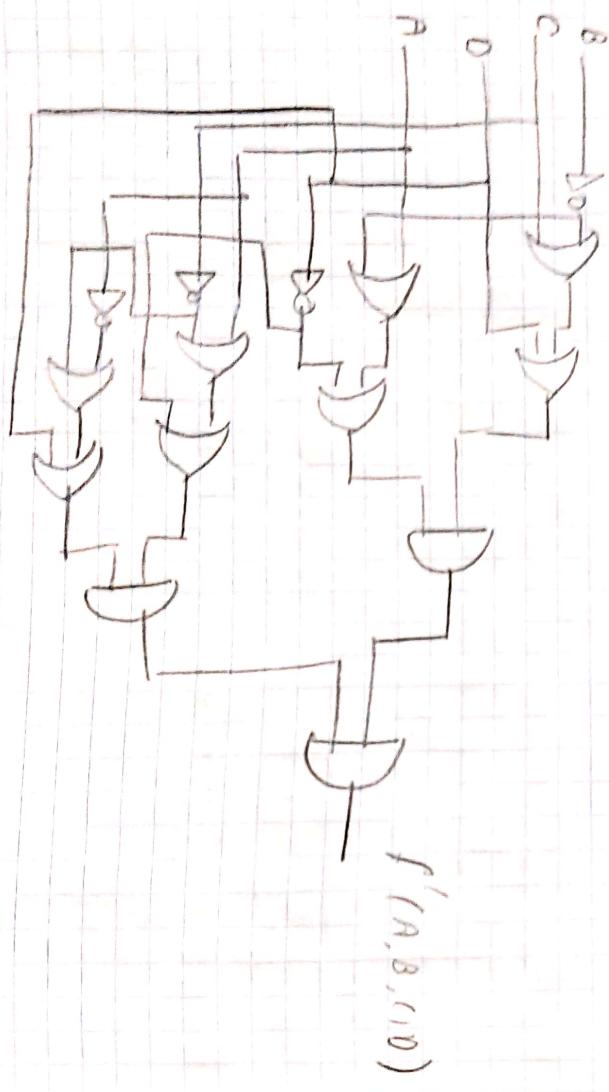


Prisoner's Dilemma

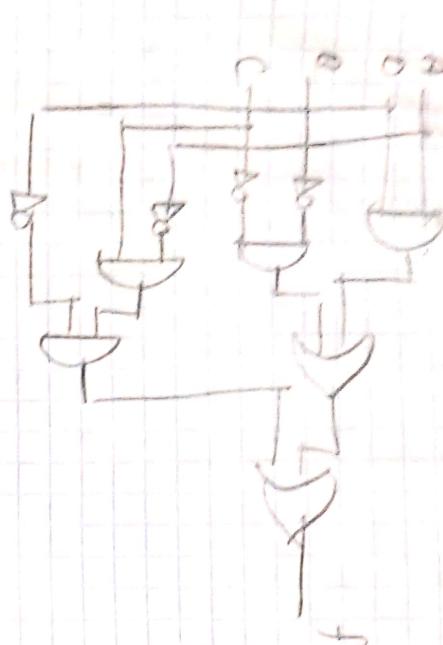


	A ₀	A ₁	B ₀	B ₁	C ₀	C ₁
10	0	0	0	0	0	0
11	0	0	0	1	0	0
12	0	1	0	0	0	0
13	0	1	0	1	0	0
14	1	0	0	0	0	0
15	1	0	0	1	0	0
16	1	1	0	0	0	0
17	1	1	0	1	0	0
18	1	1	1	0	0	0
19	1	1	1	1	0	0
20	1	1	1	1	1	0
21	1	1	1	1	1	1

$$f = (\bar{a} + \bar{b})(\bar{a} + \bar{b})(\bar{a} + b + c)$$



$$f'(A, B, C, D)$$



$$f(A, B, C, D)$$