

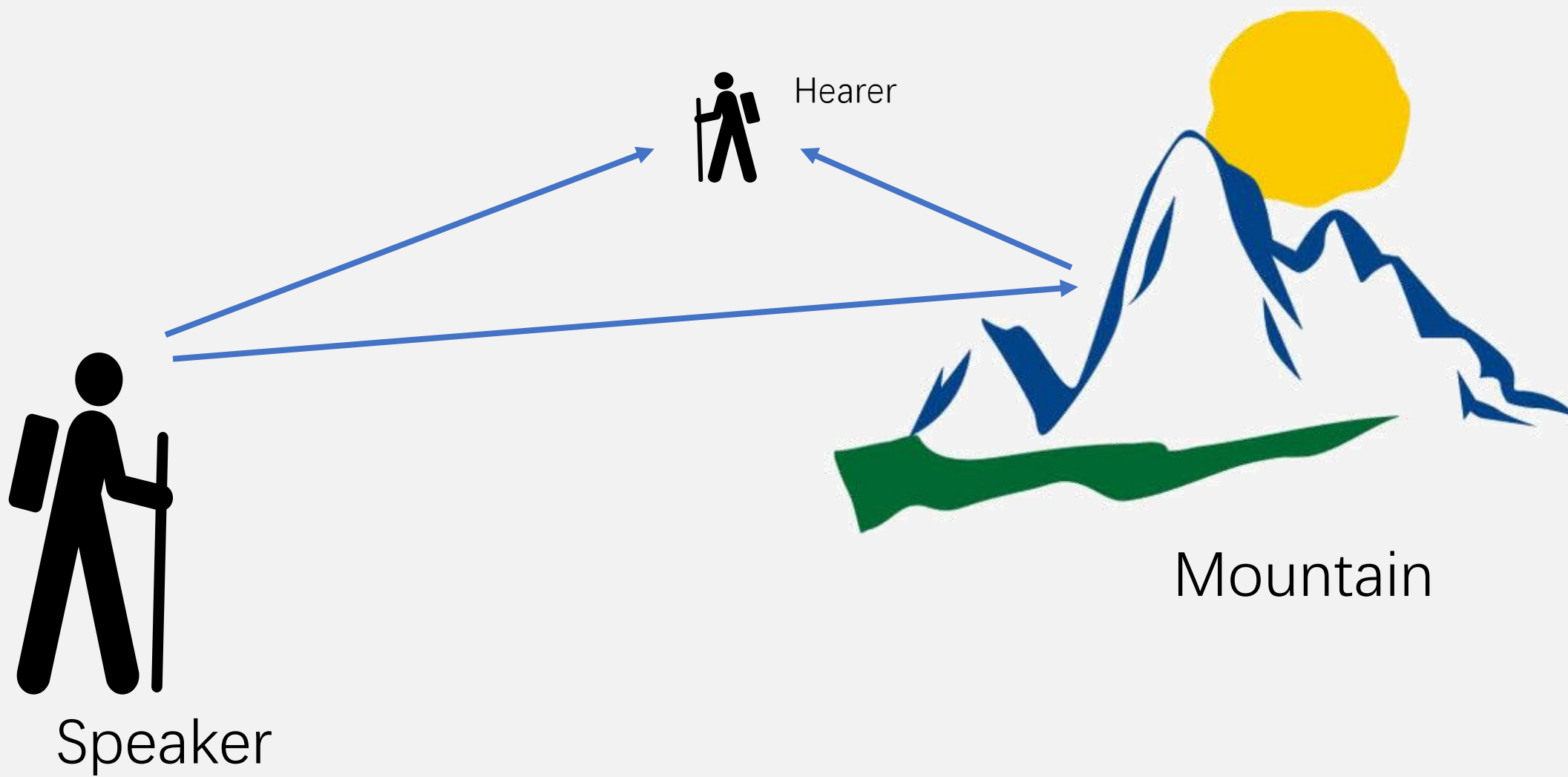
无线通信实验在线开放课程

主讲人：吴光 博士

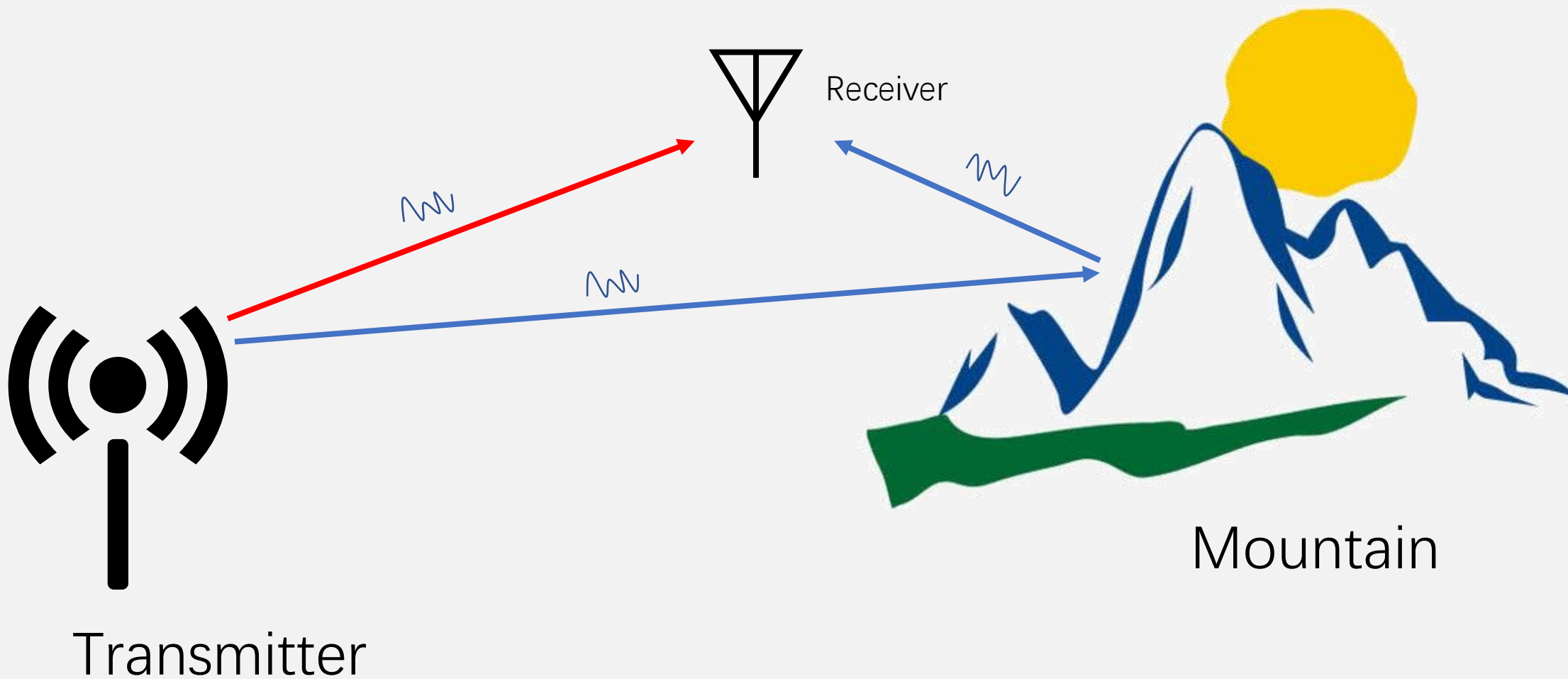
广东省教学质量工程建设项目



Echo



Multipath Propagation



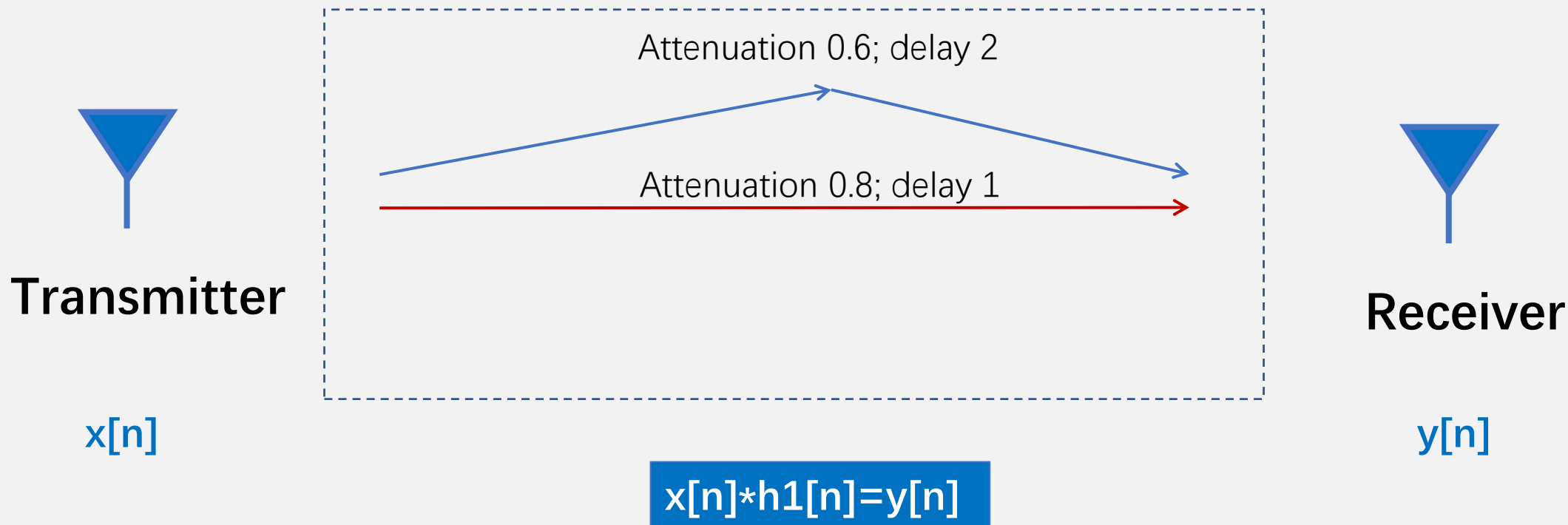


Introduction



$$y[n] = 0.8 x[n-1] + 0.6 x[n-2]$$

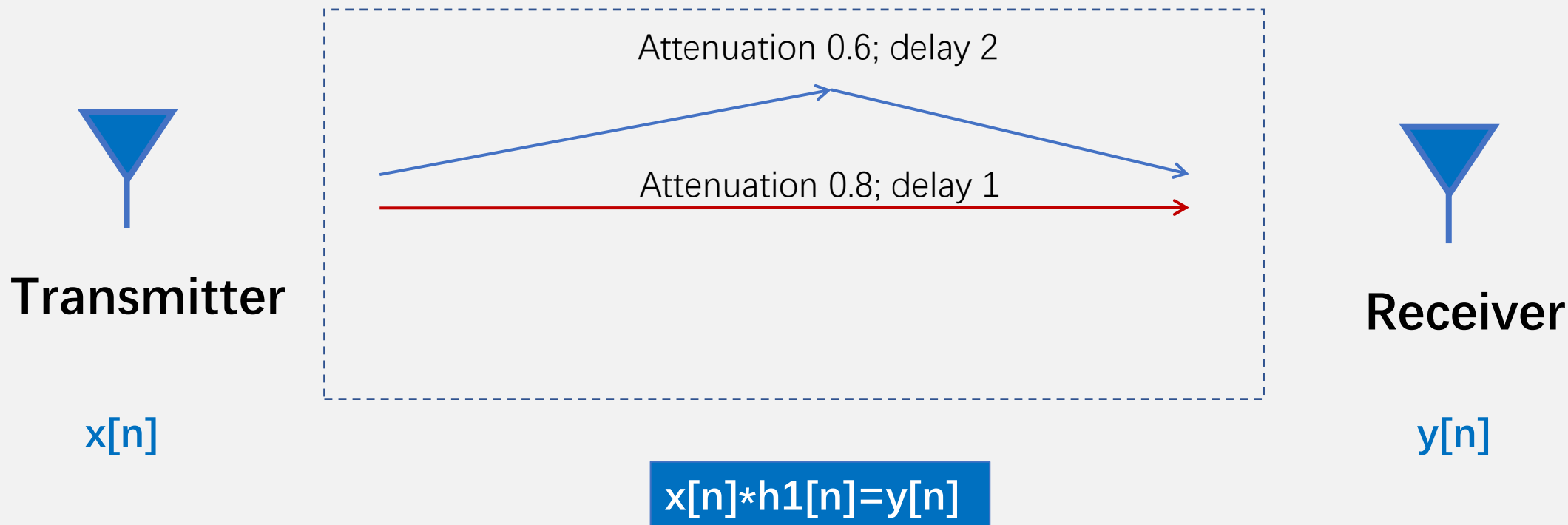
$$h1[n] = 0.8 \delta[n-1] + 0.6 \delta[n-2]$$

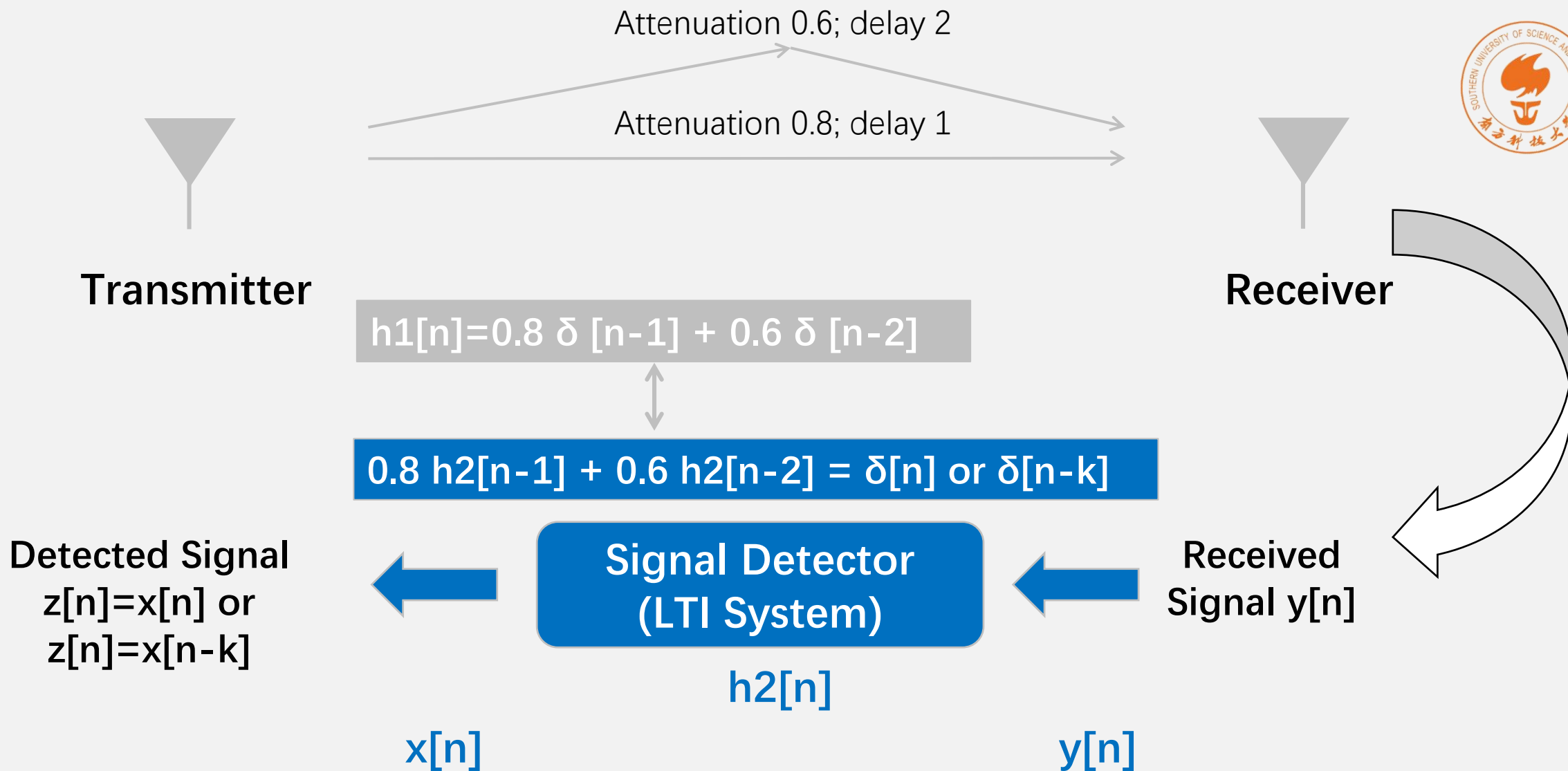


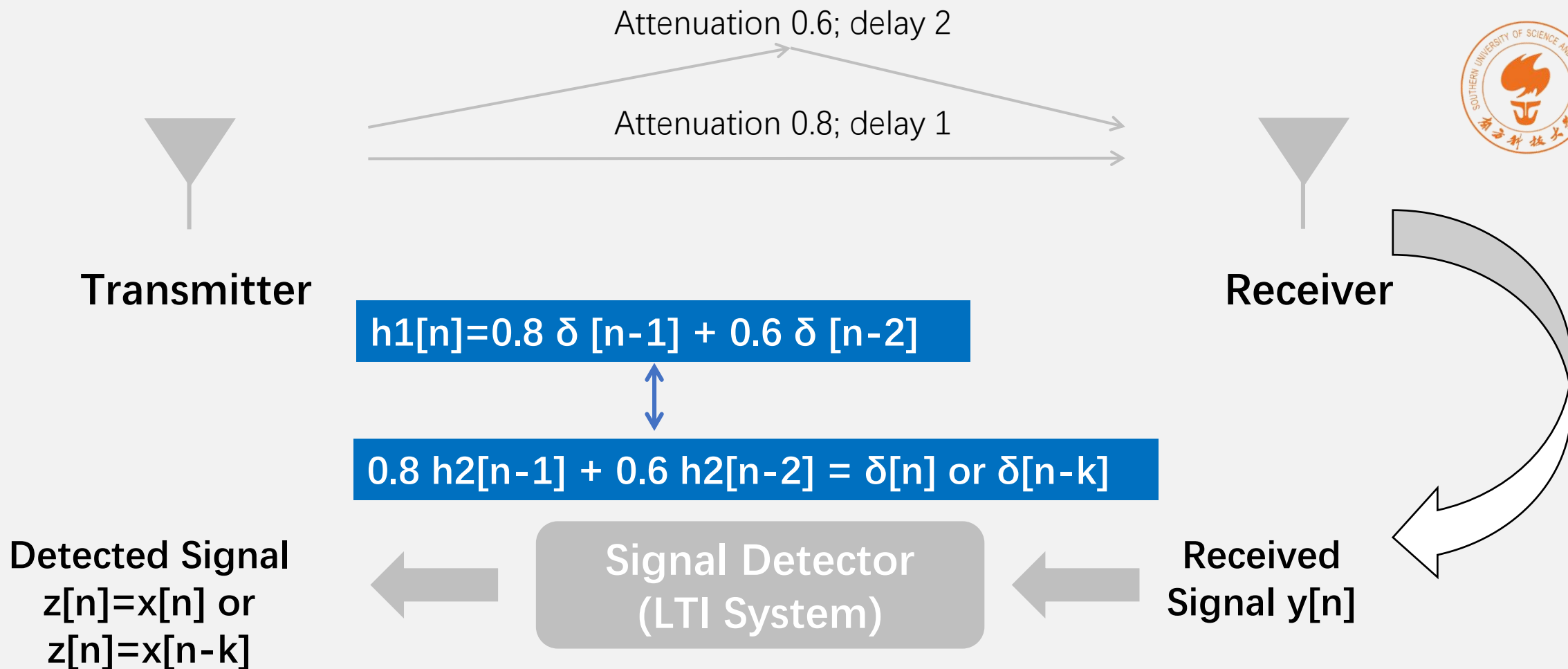


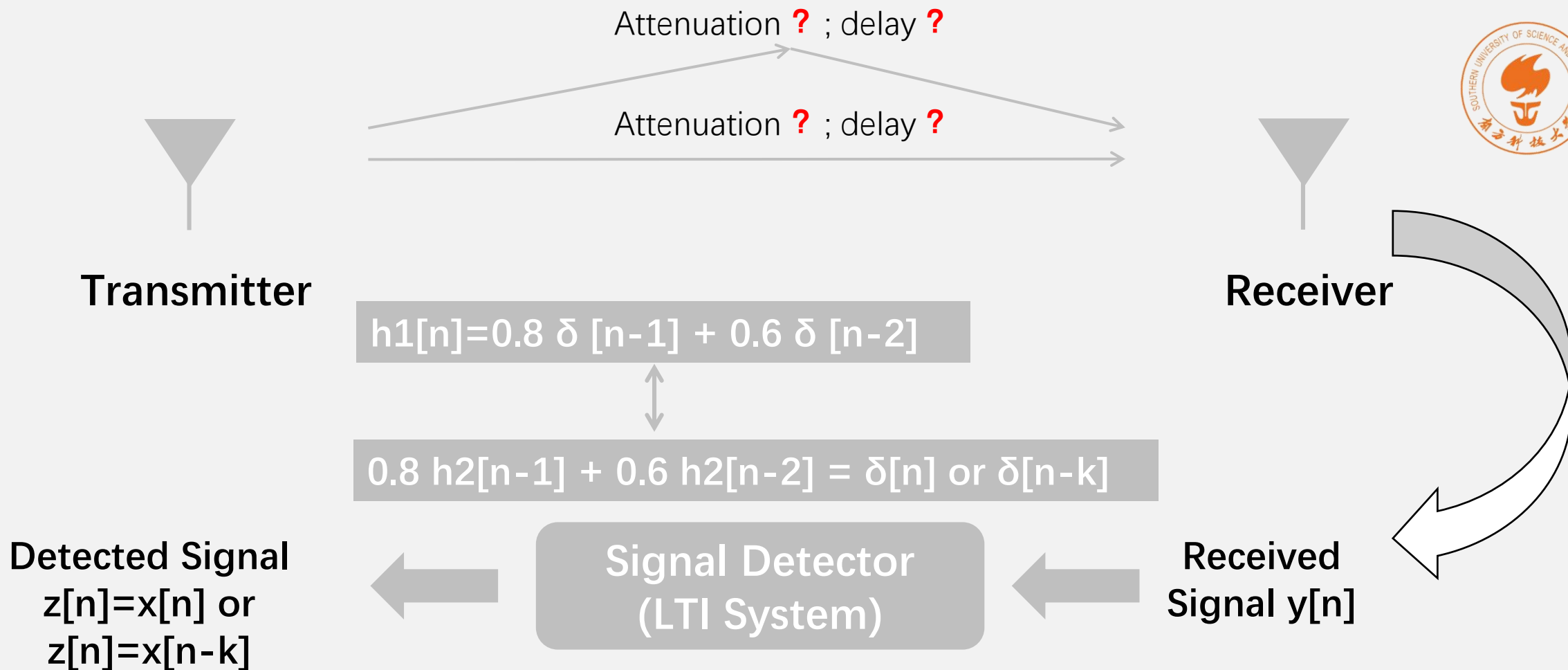
$$y[n] = 0.8 x[n-1] + 0.6 x[n-2]$$

$$h1[n] = 0.8 \delta[n-1] + 0.6 \delta[n-2]$$









Impulse response:

$$h2[n] * h1[n] = \delta[n] \text{ or } \delta[n-k]$$

Difference Equation:

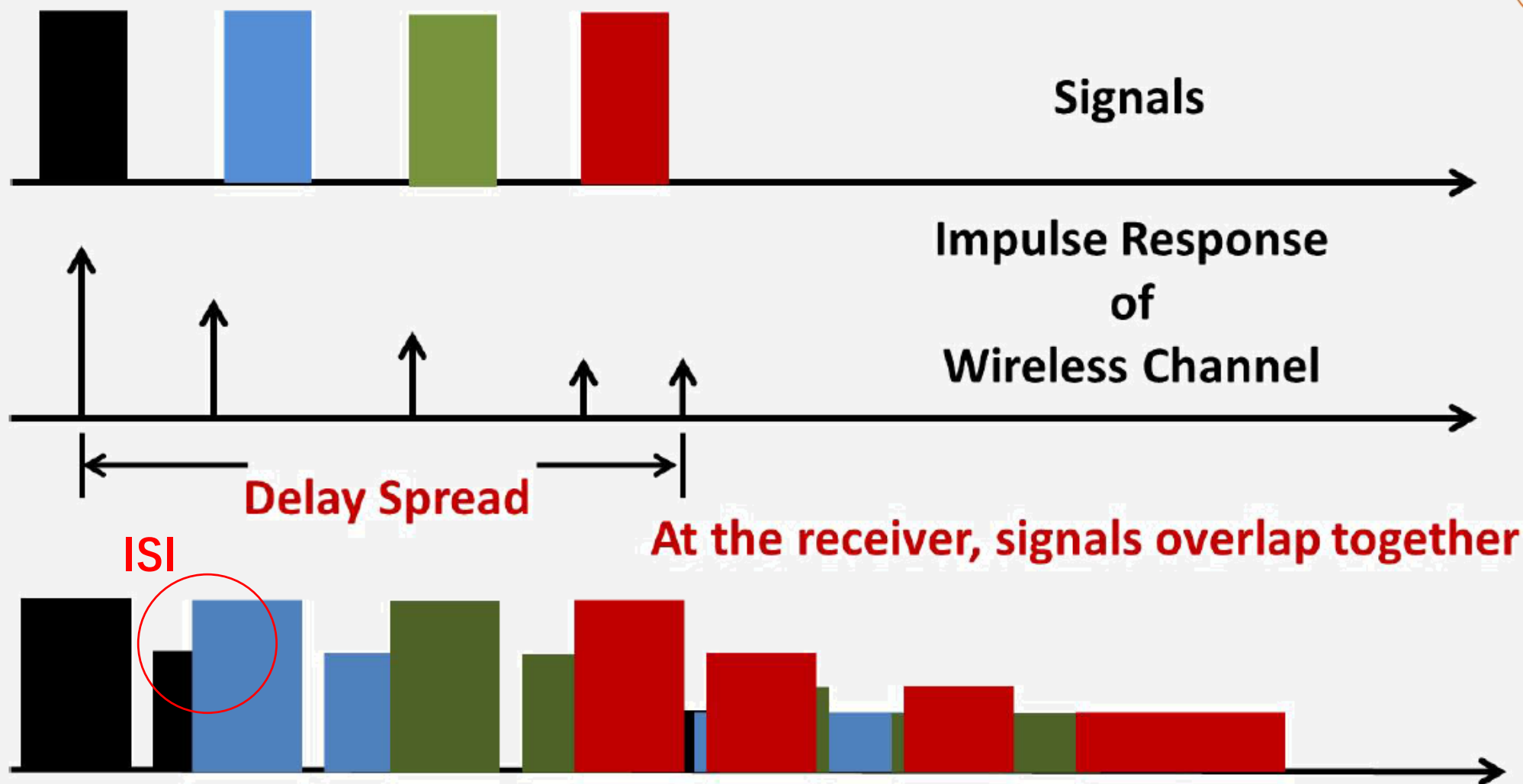
$$? z[n-?] + ? z[n-?] = y[n]$$



$$x[n]*h_1[n]=t[n]$$



Frequency Selective Channel



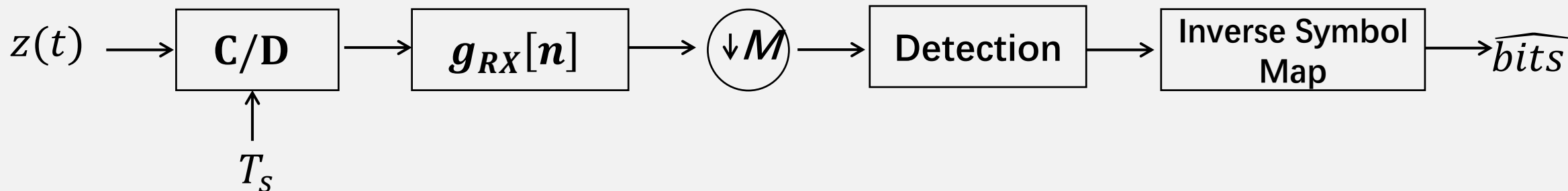


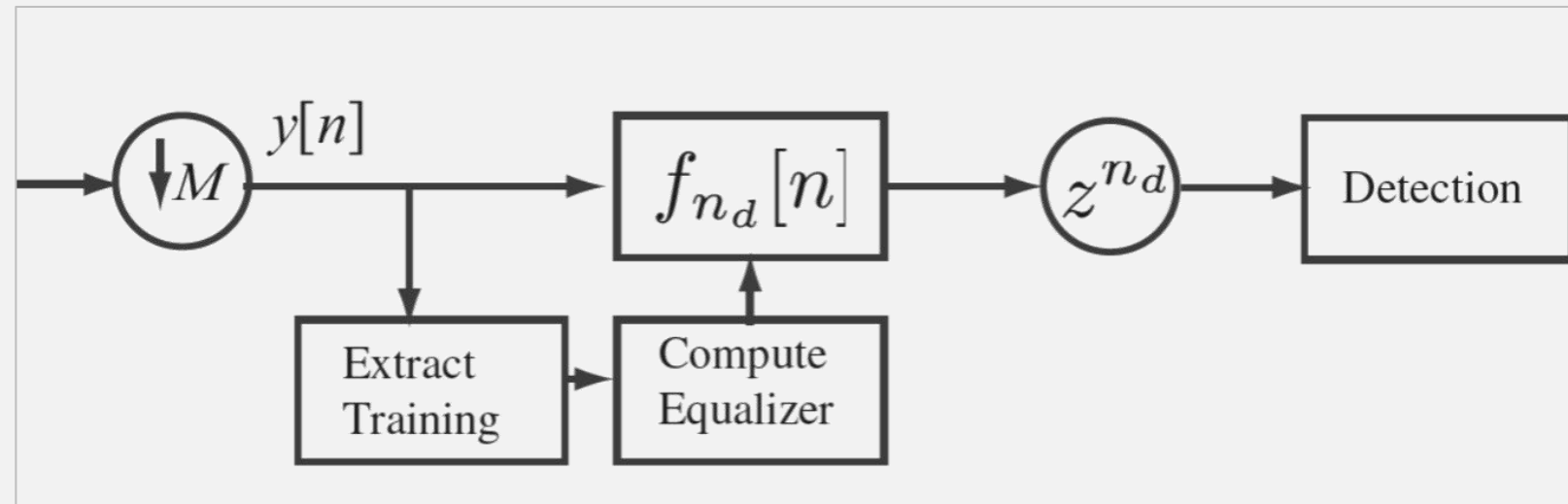
Channel Model

AWGN **Frequency Selective** Channel

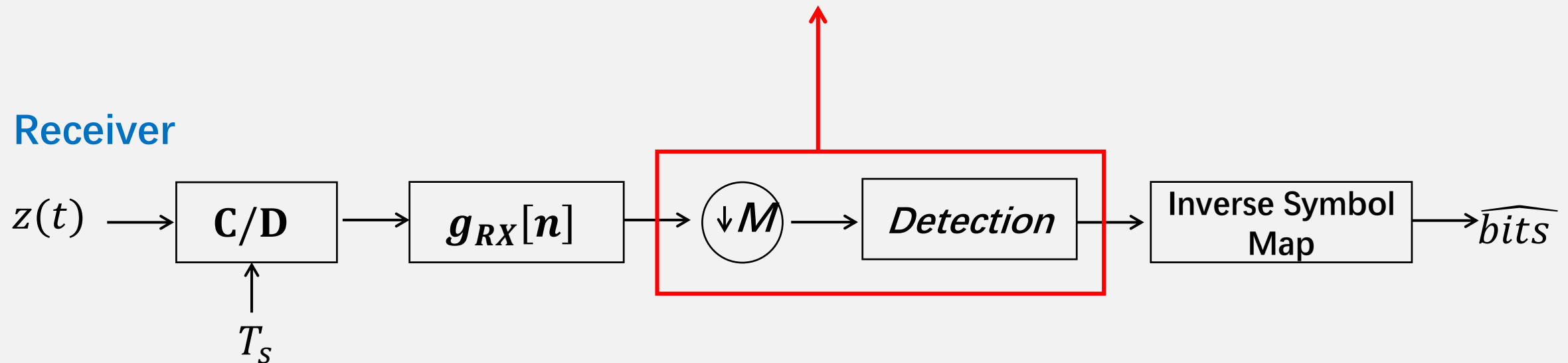
$$z(t) = \alpha_0 e^{j\varphi_0} x(t - \tau_0) + \alpha_1 e^{j\varphi_1} x(t - \tau_1) + v(t)$$

Receiver





Receiver

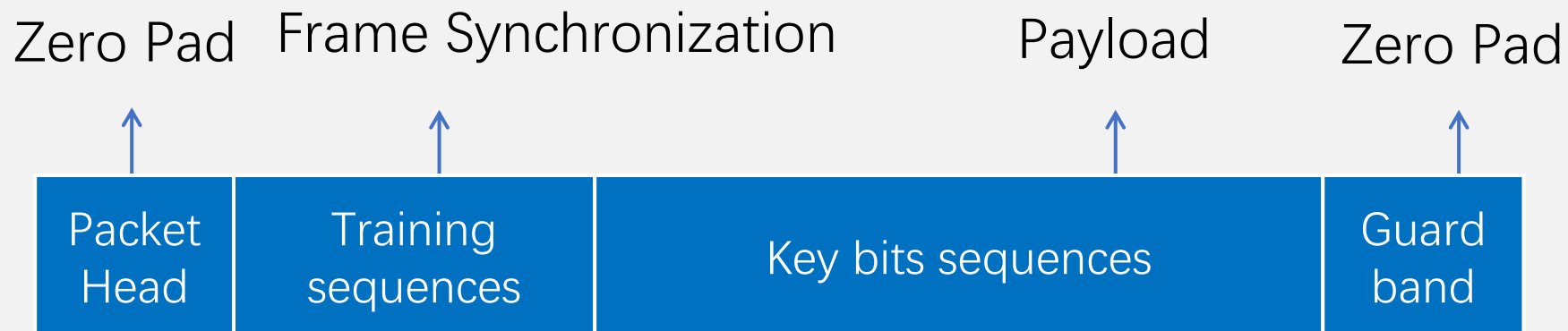




Channel estimate

Equalization

Frequency Offset Correction



Step1: $h1[n]$

Step3: $y[n]*h2[n]=x[n]*\underline{h1[n]*h2[n]}$

Step2: $h2[n]$

$\delta[n]$ or $\delta[n-k]$

Lab 13 : Channel Estimation and Equalization

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Email: wug@sustech.edu.cn



Algorithm Analysis and Verification

1 Channel Estimation

2 Indirect Equalizer Analysis

3 Algorithm Simulation

4 USRP Experiments

5 Discussion and Conclusion



Channel Estimation



$$\mathbf{Ax} = \mathbf{b}$$



$$\mathbf{Ax} = \mathbf{b}$$

$$\mathbf{N} = \mathbf{M}$$

$$\mathbf{x} = \mathbf{A}^{-1}\mathbf{b}$$



$$\min ||\mathbf{Ax} - \mathbf{b}||^2$$

$$N > M$$

$$\mathbf{x}_{LS} = (\mathbf{A}^* \mathbf{A})^{-1} \mathbf{A}^* \mathbf{b}$$



$$s[n] = t[n], n = 0, 1, \dots, N_t - 1$$

$$y[n] = \sum_{l=0}^L s[l]h[n-l] + v[n]$$

$$y[0] = s[0]h[0] + v[0]$$

$$y[1] = s[0]h[1] + s[1]h[0] + v[1]$$

...



$$s[n] = t[n], n = 0, 1, \dots, N_t - 1$$

$$y[n] = \sum_{l=0}^L s[l]h[n-l] + v[n]$$

$$y[n] = \sum_{l=0}^L h[l]t[n-l] + v[n]$$



$$s[n] = t[n], n = 0, 1, \dots, N_t - 1$$

$$\{\hat{h}[0], \hat{h}[1], \dots, \hat{h}[L]\}$$

$$= \underset{\{h[0], h[1], \dots, h[L]\}}{\operatorname{argmin}} \sum_{n=L}^{N_t-1} \|y[n] - \sum_{l=0}^L h[l]t[n-l]\|^2$$



$$\underbrace{\begin{bmatrix} y[L] \\ y[L+1] \\ \vdots \\ y[N_t-1] \end{bmatrix}}_y = \underbrace{\begin{bmatrix} t[L] & \cdots & t[0] \\ t[L+1] & \cdots & t[1] \\ \vdots & \ddots & \vdots \\ t[N_t-1] & \cdots & t[N_t-1-L] \end{bmatrix}}_T \underbrace{\begin{bmatrix} h[0] \\ h[1] \\ \vdots \\ h[L] \end{bmatrix}}_h + \underbrace{\begin{bmatrix} v[L] \\ v[L+1] \\ \vdots \\ v[N_t-1] \end{bmatrix}}_v$$



$$\underbrace{\begin{bmatrix} y[L] \\ y[L+1] \\ \vdots \\ y[N_t-1] \end{bmatrix}}_{\mathbf{y}} = \underbrace{\begin{bmatrix} t[L] & \cdots & t[0] \\ t[L+1] & \cdots & t[1] \\ \vdots & \ddots & \vdots \\ t[N_t-1] & \cdots & t[N_t-1-L] \end{bmatrix}}_{\mathbf{T}} \underbrace{\begin{bmatrix} h[0] \\ h[1] \\ \vdots \\ h[L] \end{bmatrix}}_{\mathbf{h}} + \underbrace{\begin{bmatrix} v[L] \\ v[L+1] \\ \vdots \\ v[N_t-1] \end{bmatrix}}_{\mathbf{v}}$$

$$\mathbf{y} = \mathbf{T}\mathbf{h} + \mathbf{v}$$

$$\mathbf{h}_{LS} = (\mathbf{T}^*\mathbf{T})^{-1}\mathbf{T}^*\mathbf{y}$$



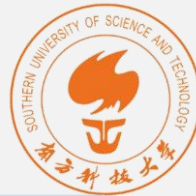
$$\underbrace{\begin{bmatrix} y[L] \\ y[L+1] \\ \vdots \\ y[N_t-1] \end{bmatrix}}_{\mathbf{y}} = \underbrace{\begin{bmatrix} t[L] & \cdots & t[0] \\ t[L+1] & \cdots & t[1] \\ \vdots & \ddots & \vdots \\ t[N_t-1] & \cdots & t[N_t-1-L] \end{bmatrix}}_{\mathbf{T}} \underbrace{\begin{bmatrix} h[0] \\ h[1] \\ \vdots \\ h[L] \end{bmatrix}}_{\mathbf{h}} + \underbrace{\begin{bmatrix} v[L] \\ v[L+1] \\ \vdots \\ v[N_t-1] \end{bmatrix}}_{\mathbf{v}}$$

$$\mathbf{y} = \mathbf{T}\mathbf{h} + \mathbf{v}$$

$$\mathbf{h}_{LS} = (\mathbf{T}^*\mathbf{T})^{-1}\mathbf{T}^*\mathbf{y}$$

$$N_t - L \geq L + 1$$

$$N_t \geq 2L + 1$$



Algorithm Analysis and Verification

1 Channel Estimation

2 Indirect Equalizer Analysis

3 Algorithm Simulation

4 USRP Experiments

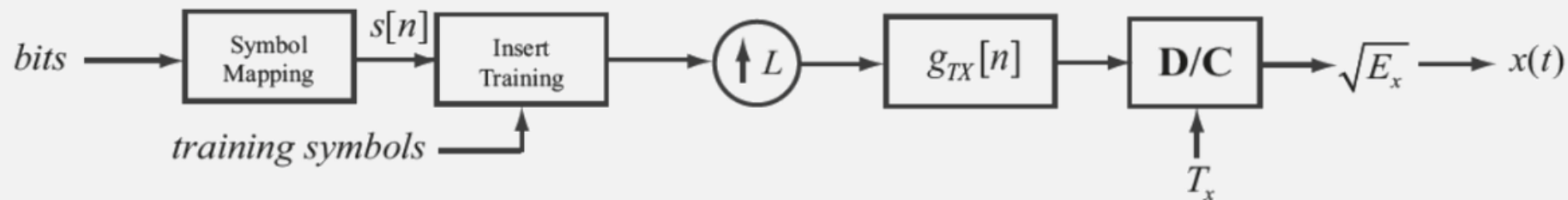
5 Discussion and Conclusion



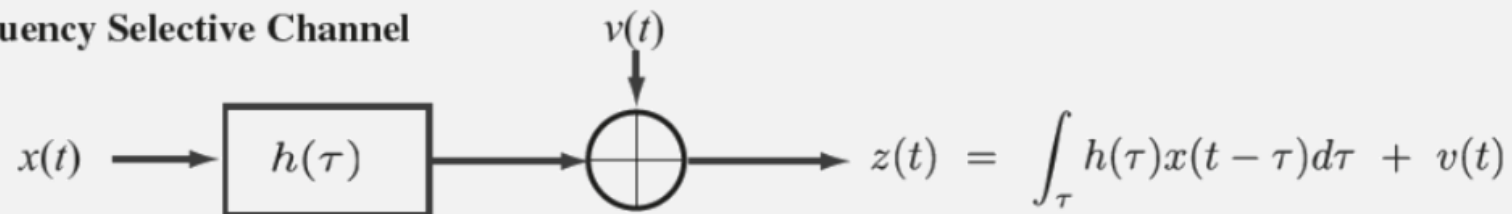
Programming for Channel Estimation



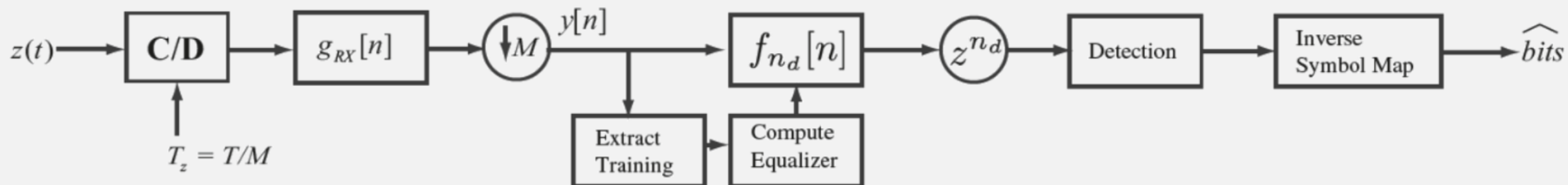
Transmitter



AWGN Frequency Selective Channel



Receiver





student_LLSE 1.vi Block Diagram *

File Edit View Project Operate Tools Window Help

17pt Application Font

Search

Student MMSE $A\hat{x}=b$

Functions

- Programming
- Measurement I/O
- Instrument I/O
- Vision and Motion
- Mathematics
 - Numeric
 - Elementary
 - Linear Alge...
 - Fitting
 - Interp & Ex...
 - Integ & Diff
 - Prob & Stat
 - Optimization
 - Differential ...
 - Geometry
 - Polynomial
 - Script & Fo...
- Signal Processing
- Data Communication
- Connectivity
- Control Design & Simulation
- Express

Linear Algebra

$A \times B$

$A \times B$

Inverse Matrix VI

mean square error

DBL

x.estimate

DBL

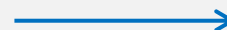
error in (no error)

error out

Simulation setup

Test your block diagram with these parameters!

Set the channel model: ISI



TRANSMITTER

TX oversample factor TX sample rate
4 4M

TX channel model parameters

channel model
ISI

noise power (dB)
-Inf

channel response
0 1 + 0 i 0 + 0 i 0 + 0 i

frequency offset delay (sec)
0 0

Measured channel impairments

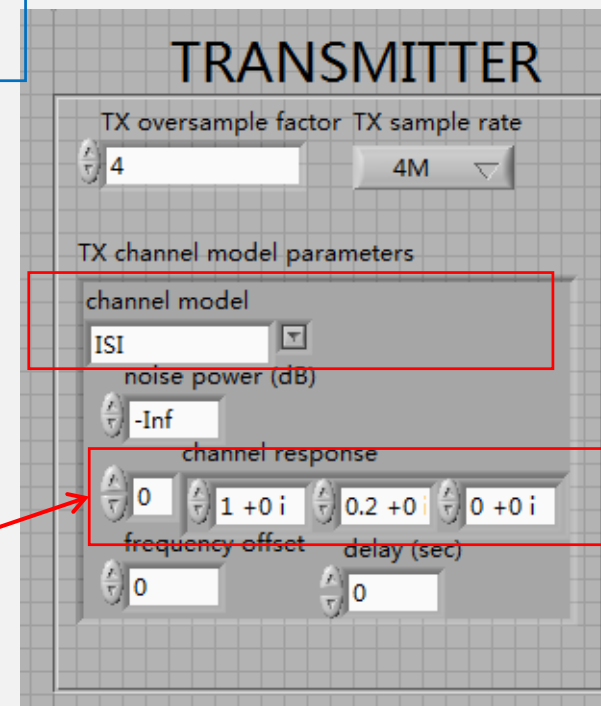
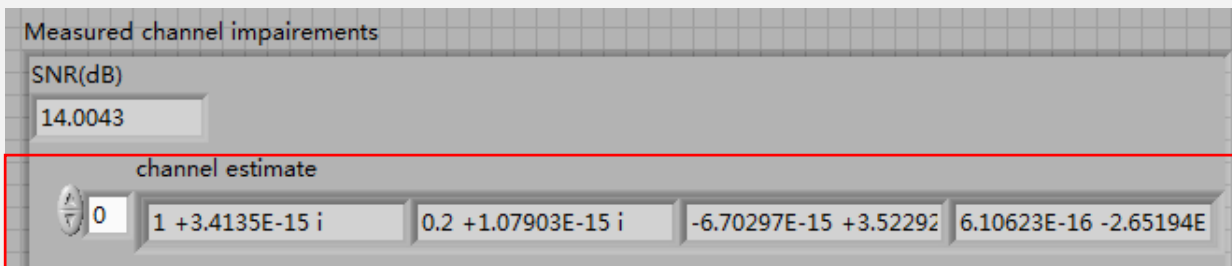
SNR(dB)
261.428

channel estimate
0 1 + 3.83363E-15 i 4.17461E-14 + 1.77557i -1.2134E-14 + 4.16131E 3.63598E-15 + 1.36408i

Simulation setup

Test your block diagram with these parameters!

Configure the channel model: ISI





Demo: Linear Equalization



$$z[n] = \sum_{l=0}^{L_f} f_{n_d}[l]y[n-l] \approx \hat{s}[n-n_d]$$

$$f_{n_d}(n) * \hat{h}_c(n) = \delta(n-n_d)$$

$$\sum_{l=0}^{L_f} f_{n_d}[l]\hat{h}[n-l] \approx \delta[n-n_d]$$



$$z[n] = \sum_{l=0}^{L_f} f_{n_d}[l]y[n-l] \approx \hat{s}[n-n_d]$$

$$f_{n_d}(n) * \hat{h}_c(n) = \delta(n-n_d)$$

$$\sum_{l=0}^{L_f} f_{n_d}[l]\hat{h}[n-l] \approx \delta[n-n_d]$$



$$\underbrace{\begin{bmatrix} \hat{h}[0] & 0 & \dots & \dots \\ \hat{h}[1] & \hat{h}[0] & 0 & \dots \\ \vdots & \ddots & \ddots & \vdots \\ \hat{h}[L] & \hat{h}[L] & \dots & \dots \\ 0 & \hat{h}[L] & \dots & \dots \\ \vdots & & & \end{bmatrix}}_{\hat{H}}$$



$$\underbrace{\begin{bmatrix} \hat{h}[0] & 0 & \cdots & \cdots \\ \hat{h}[1] & \hat{h}[0] & 0 & \cdots \\ \vdots & \ddots & \ddots & \vdots \\ \hat{h}[L] & & & \\ 0 & \hat{h}[L] & \cdots & \cdots \\ \vdots & & & \end{bmatrix}}_{\hat{H}} \underbrace{\begin{bmatrix} f[0] \\ f[1] \\ \vdots \\ \vdots \\ f[L_f] \end{bmatrix}}_f = \underbrace{\begin{bmatrix} 0 \\ \vdots \\ 1 \\ \vdots \\ 0 \end{bmatrix}}_{e_{n_d}}$$

n_d+1



$$\underbrace{\begin{bmatrix} \hat{h}[0] & 0 & \cdots & \cdots \\ \hat{h}[1] & \hat{h}[0] & 0 & \cdots \\ \vdots & \ddots & \ddots & \vdots \\ \hat{h}[L] & & & \\ 0 & \hat{h}[L] & \cdots & \cdots \\ \vdots & & & \end{bmatrix}}_{\hat{H}} \underbrace{\begin{bmatrix} f[0] \\ f[1] \\ \vdots \\ f[L_f] \end{bmatrix}}_{\mathbf{f}} = \underbrace{\begin{bmatrix} 0 \\ \vdots \\ 1 \\ \vdots \\ 0 \end{bmatrix}}_{\mathbf{e}_{n_d}} \quad n_d+1$$

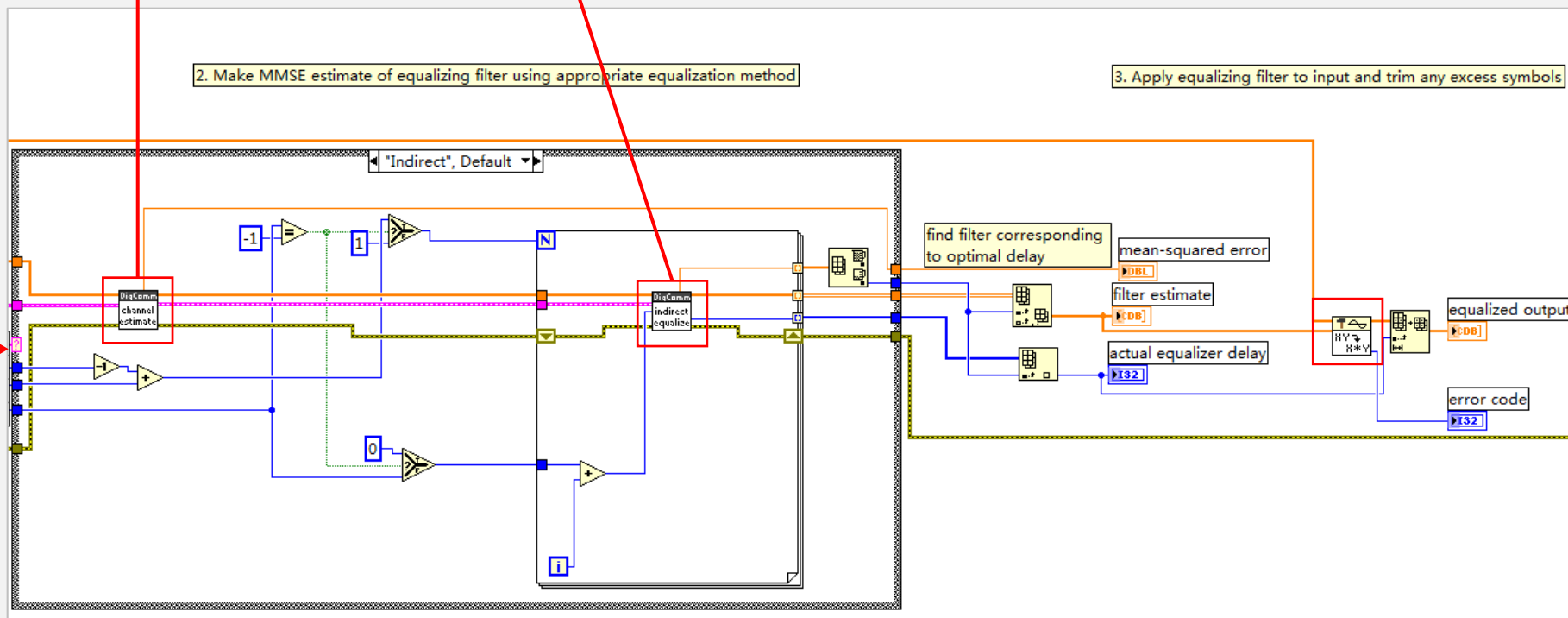
$$\hat{\mathbf{f}}_{n_d} = (\hat{H}^* \hat{H})^{-1} \hat{H}^* \mathbf{e}_{n_d}$$

$$J_f[n_d] = || \hat{H} \hat{\mathbf{f}} - \mathbf{e}_{n_d} ||^2$$

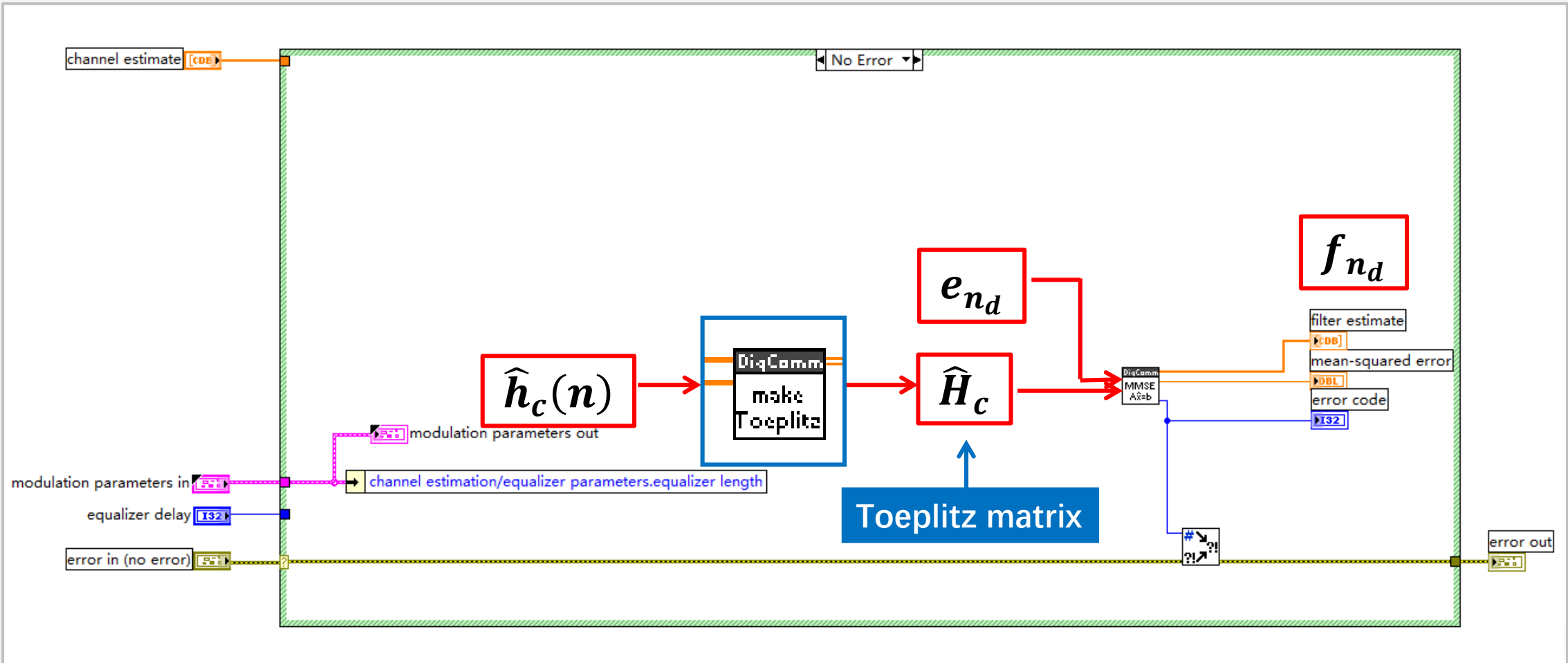


Programming for Equalization

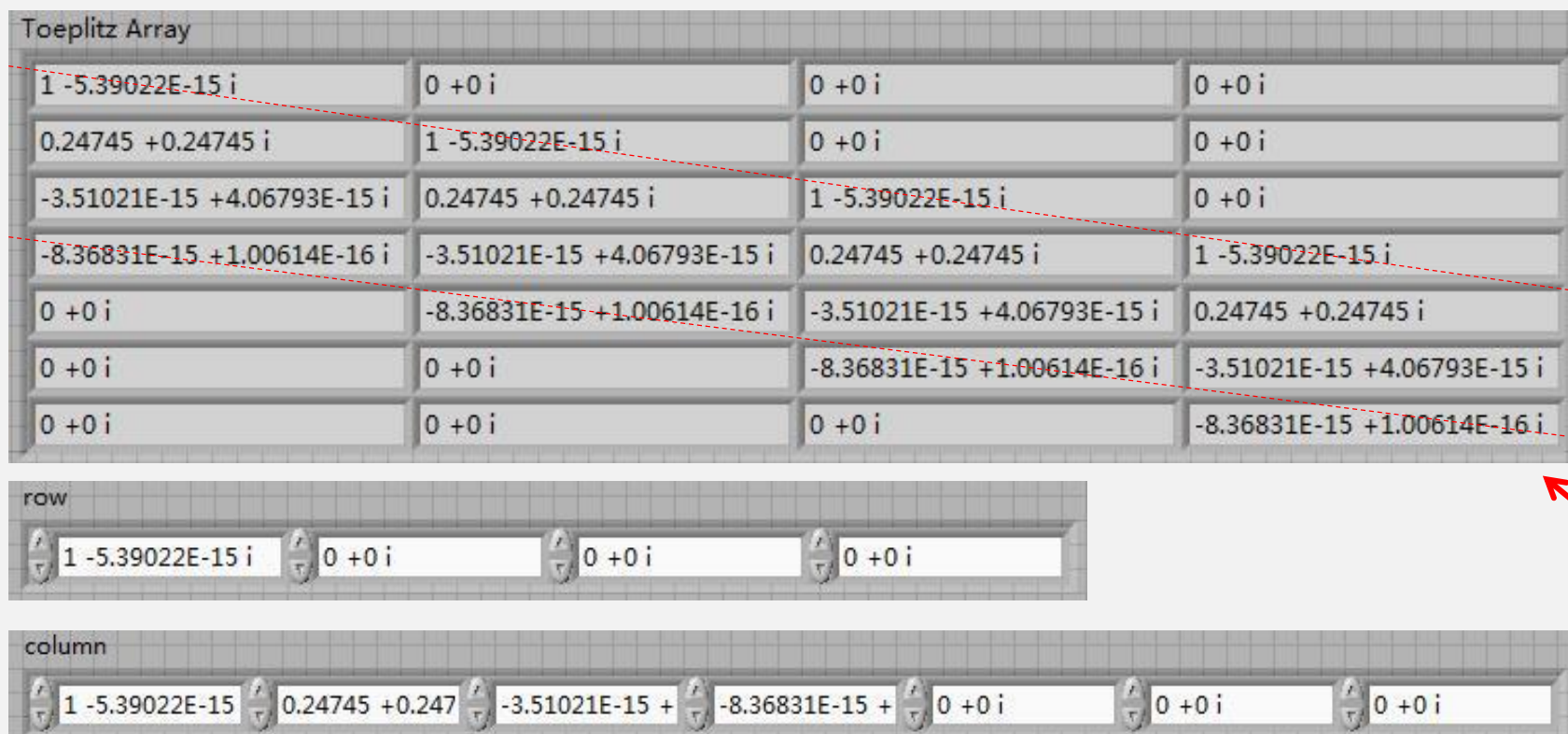
7、均衡编程



Indirect_equalizer.vi



Channel response: $h[0] = 1, h[1] = 0.35e^{j\pi/4}$
Sample rate: $2M$ *Oversample factor:* 20
Noise power: $-\text{Inf}$ *Channel est. length:* 4



Toeplitz matrix



TRANSMITTER

TX oversample factor TX sample rate
20 2M

TX channel model parameters

channel model
ISI ☐

noise power (dB)
-Inf

channel response
0 1 + 0 i 0.2474s 0 + 0 i
frequency offset delay (sec)

0 0

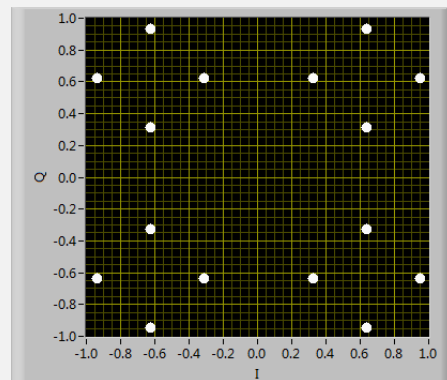
channel estimation/equalizer parameters

Equalization Method
Indirect

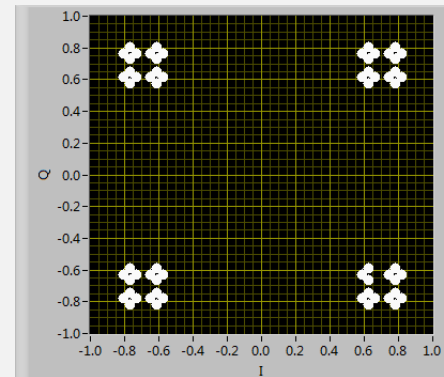
channel estimate length
2

equalizer length
1

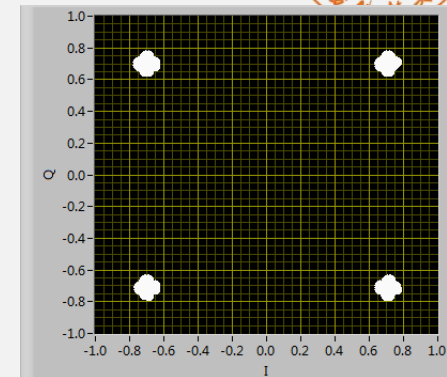
equalizer delay
-1



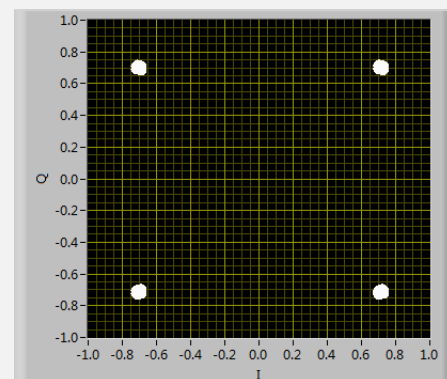
Length=1



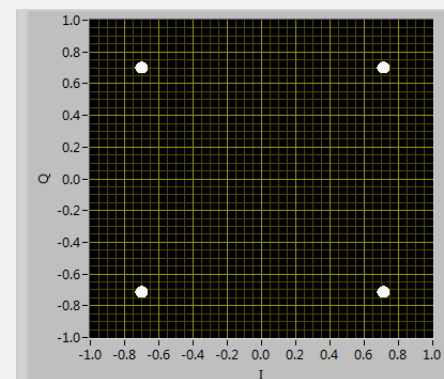
Length=2



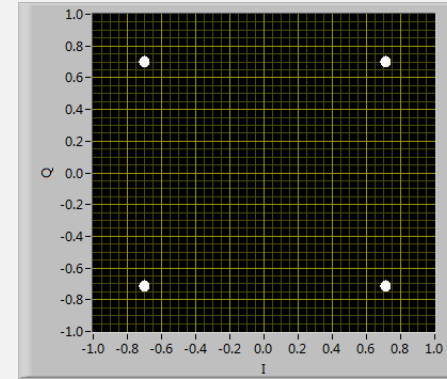
Length=3



Length=4



Length=5



Length=6



Algorithm Analysis and Verification

1 Channel Estimation

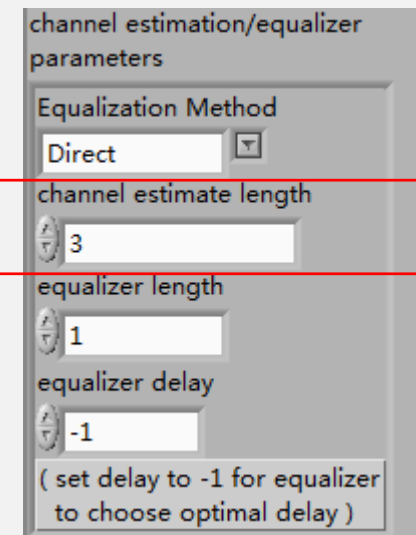
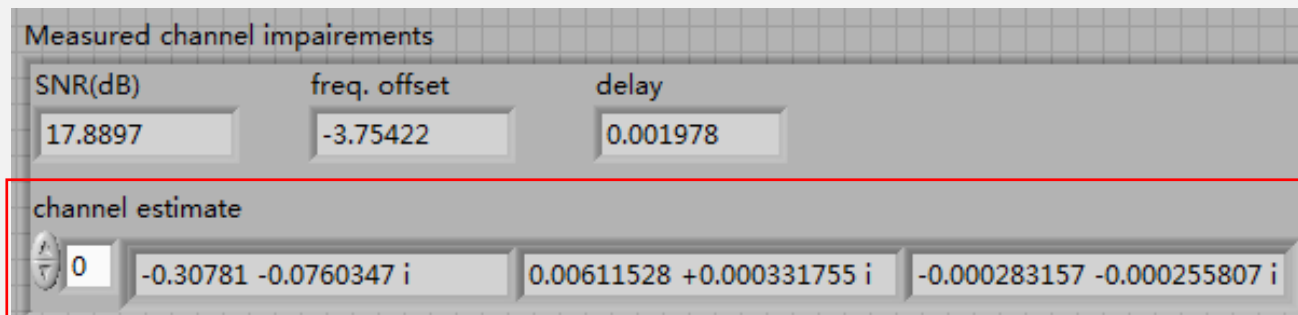
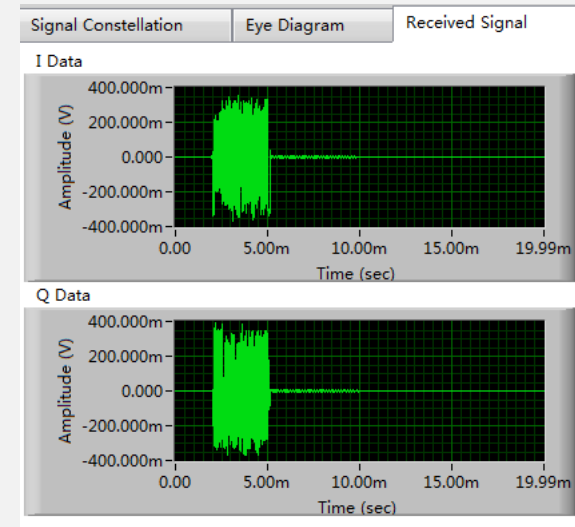
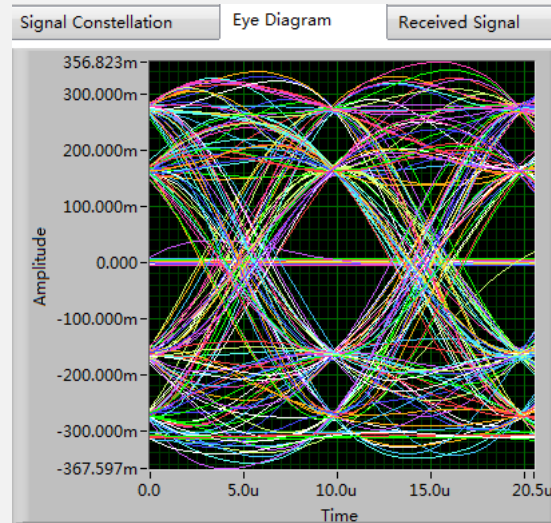
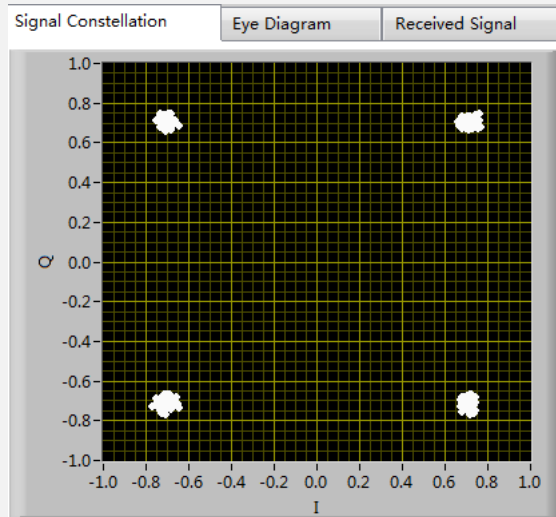
2 Indirect Equalizer Analysis

3 Algorithm Simulation

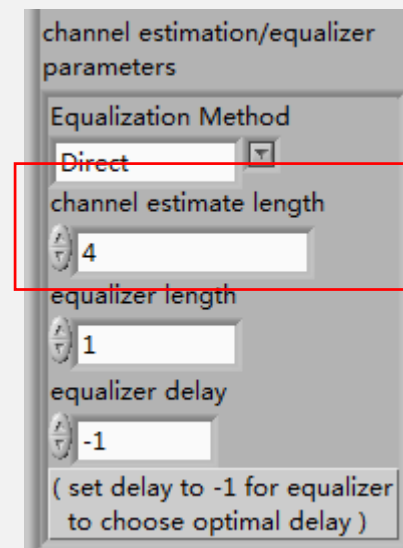
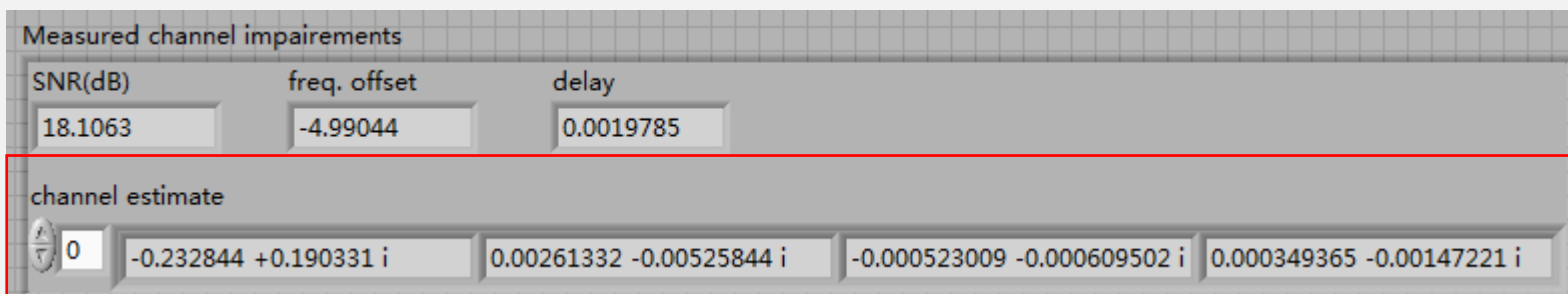
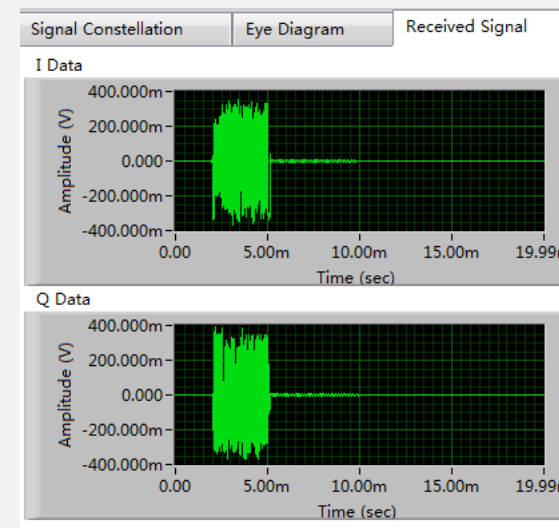
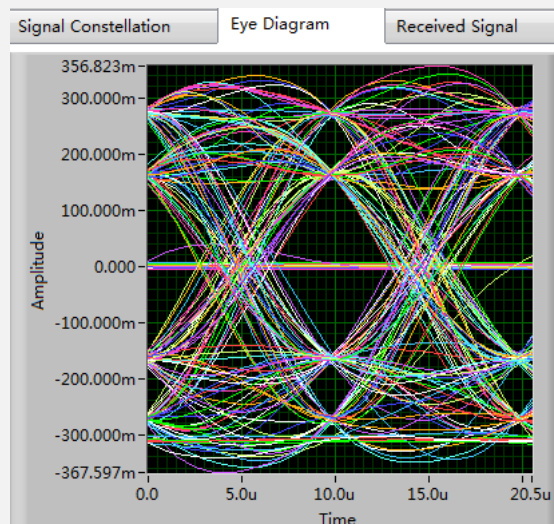
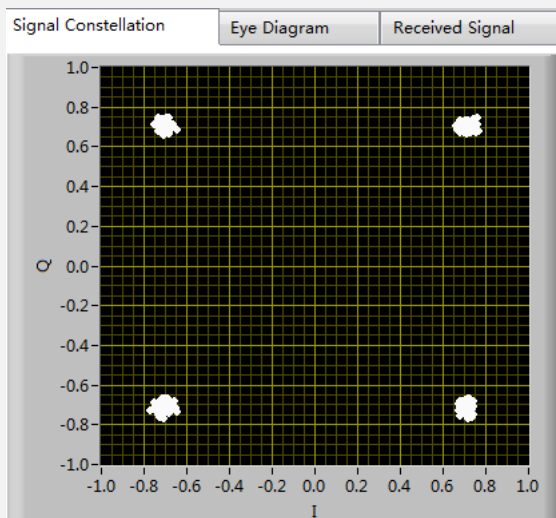
4 USRP Experiments

5 Discussion and Conclusion

USRP experiment



USRP experiment



channel estimation/equalizer parameters

Equalization Method
Indirect

channel estimate length
3

equalizer length
1

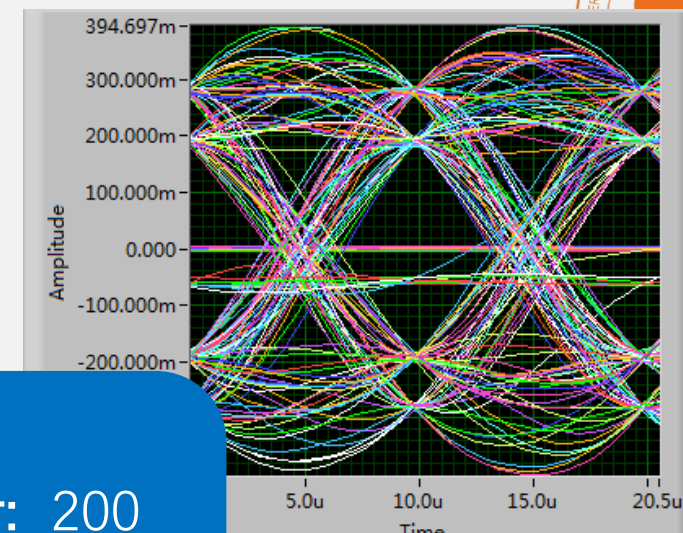
equalizer delay
-1
(set delay to -1 for equalizer to choose optimal delay)

Measured channel impairments

SNR(dB)
25.8855

channel estimate
0 0.25697 0.00534 -0.0013

freq. offset
-1.85903



TX Sample rate: 20M
TX Oversample factor: 200
RX Sample rate: 2M
RX Oversample factor: 20
Symbol rate: 100k

channel estimation/equalizer parameters

Equalization Method
Indirect

channel estimate length
3

equalizer length
6

equalizer delay
-1
(set delay to -1 for equalizer to choose optimal delay)

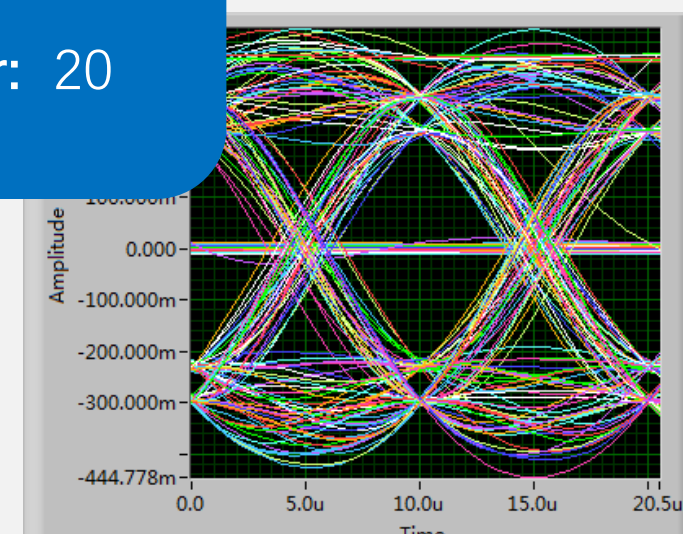
Measured channel

SNR(dB)
30.0754

channel estimate
0 0.37046 0.00184 -0.0002

freq. offset
1.53805

delay
0.000978



channel estimation/equalizer parameters

Equalization Method
Indirect ☐

channel estimate length
3

equalizer length
1

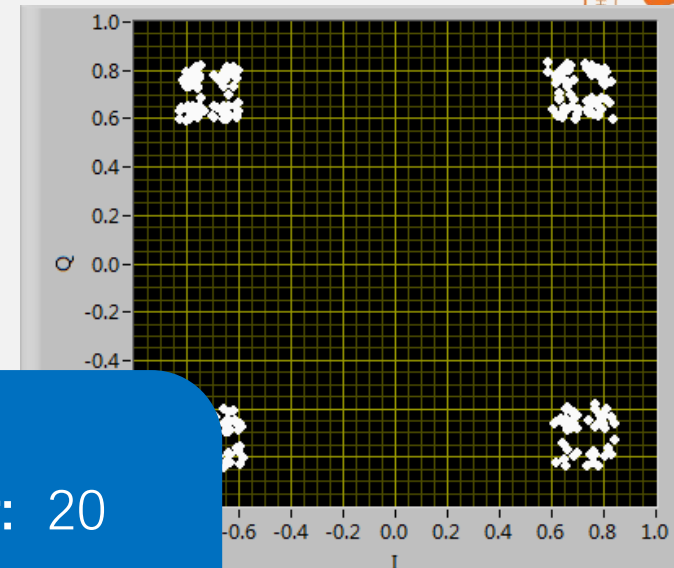
equalizer delay
-1
(set delay to -1 for equalizer to choose optimal delay)

Measured channel impairments

SNR(dB)
14.0143

channel estimate
0 -0.0718 0.00250 -0.0007

freq. offset
185.505



TX Sample rate: 20M
TX Oversample factor: 20
RX Sample rate: 2M
RX Oversample factor: 2
Symbol rate: 1M

channel estimation/equalizer parameters

Equalization Method
Indirect ☐

channel estimate length
3

equalizer length
6

equalizer delay
-1
(set delay to -1 for equalizer to choose optimal delay)

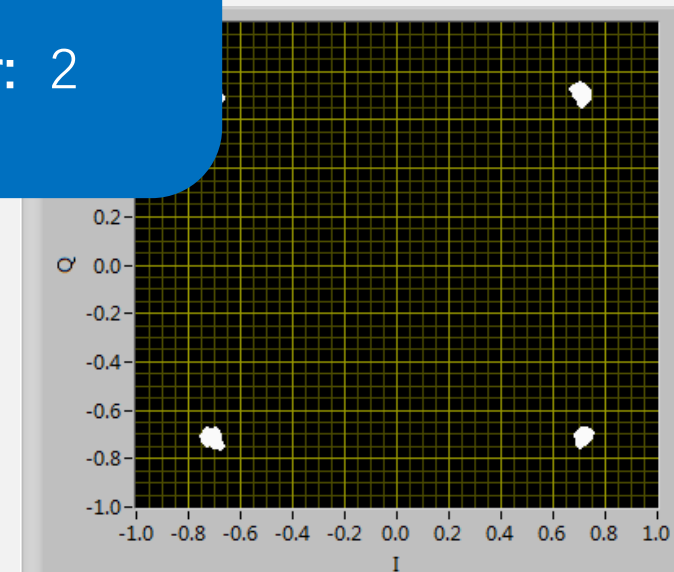
Measured channel impairments

SNR(dB)
27.1681

channel estimate
0 -0.1076 -0.0031 0.00195

freq. offset
-19.3333

delay
0.002997



channel estimation/equalizer parameters

Equalization Method
Indirect

channel estimate length
3

equalizer length
1

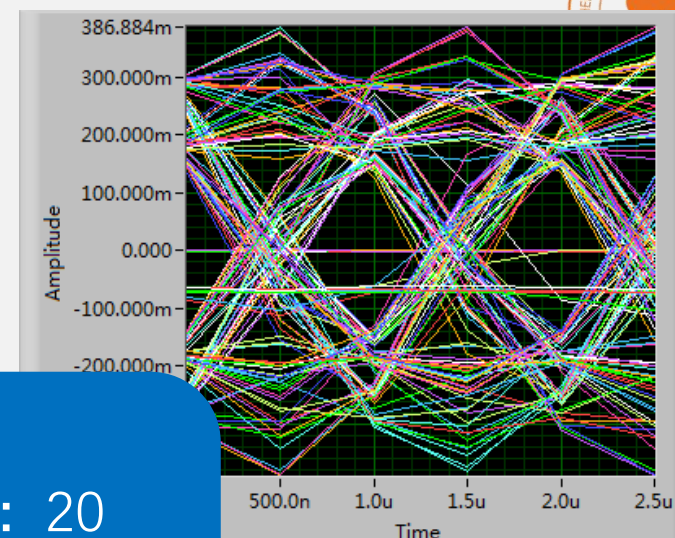
equalizer delay
-1
(set delay to -1 for equalizer to choose optimal delay)

Measured channel impairments

SNR(dB)
14.0143

channel estimate
0 -0.0718 0.00250 -0.0007

freq. offset
185.505



TX Sample rate: 20M
TX Oversample factor: 20
RX Sample rate: 2M
RX Oversample factor: 2
Symbol rate: 1M

channel estimation/equalizer parameters

Equalization Method
Indirect

channel estimate length
3

equalizer length
6

equalizer delay
-1
(set delay to -1 for equalizer to choose optimal delay)

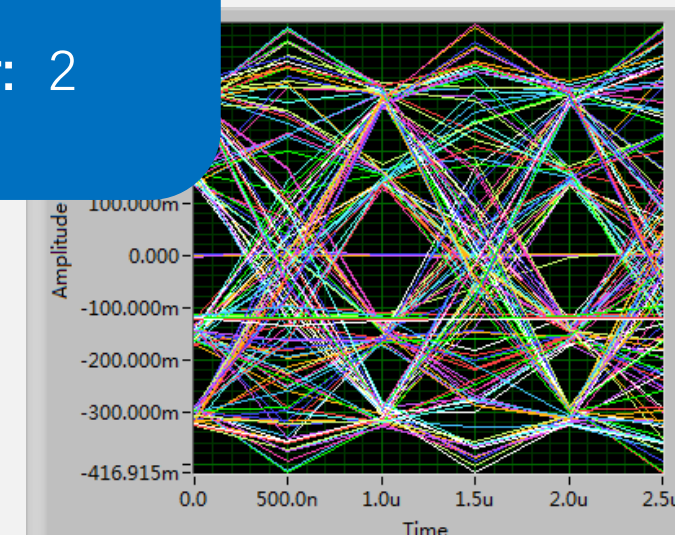
Measured channel

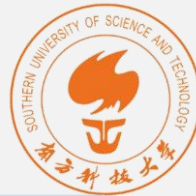
SNR(dB)
27.1681

channel estimate
0 -0.1076 -0.0031 0.00195

freq. offset
-19.3333

delay
0.002997





Algorithm Analysis and Verification

1 Channel Estimation

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- Question ?

