

# The importance of considering **extreme** and rare events in decision making

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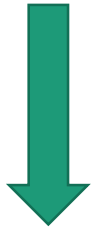
[Ullrika.Sahlin@cec.lu.se](mailto:Ullrika.Sahlin@cec.lu.se)

<http://www.cec.lu.se/ullrika-sahlin>





Now



Train departs



Time



Now



I leave the  
office

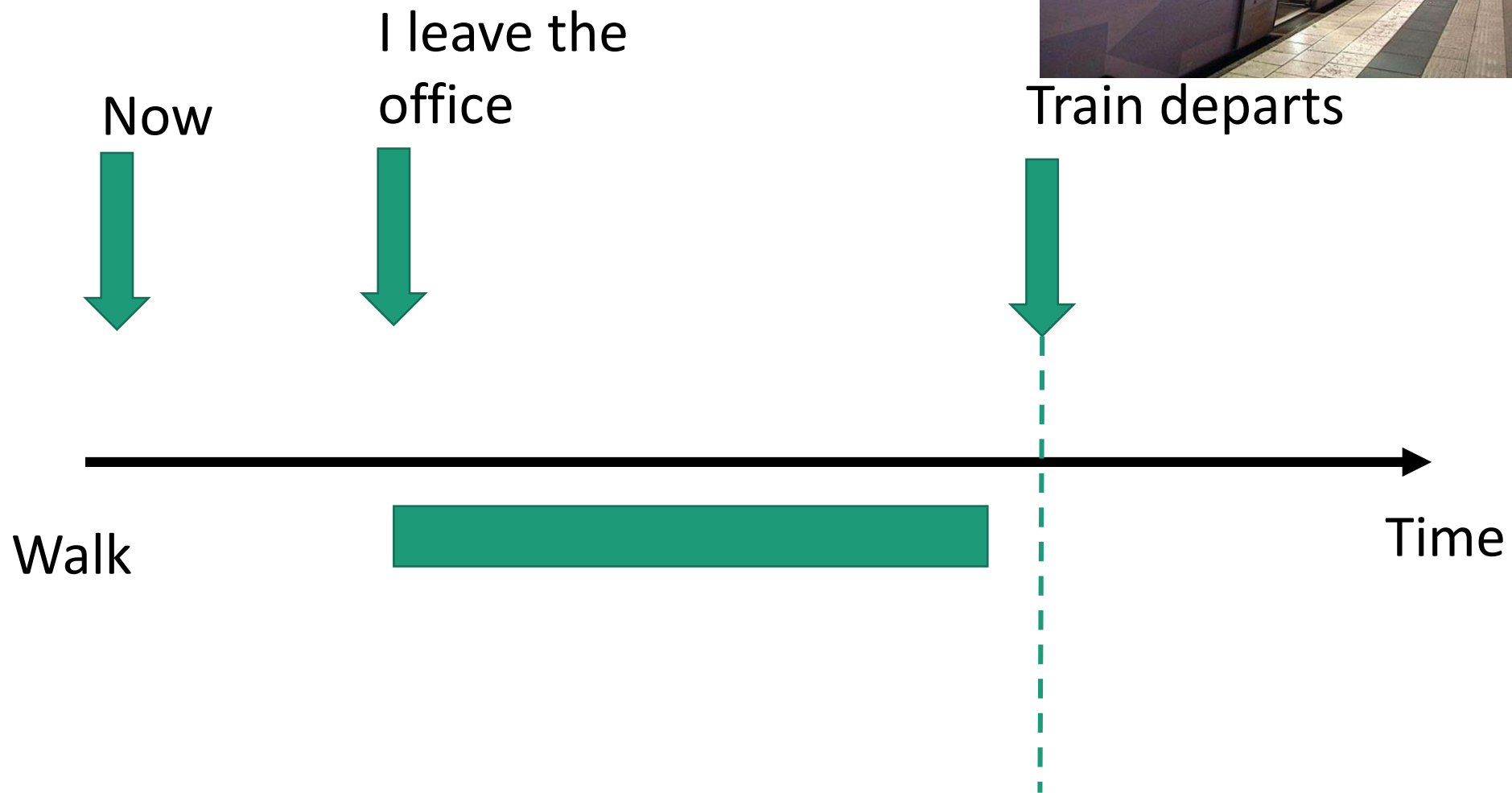


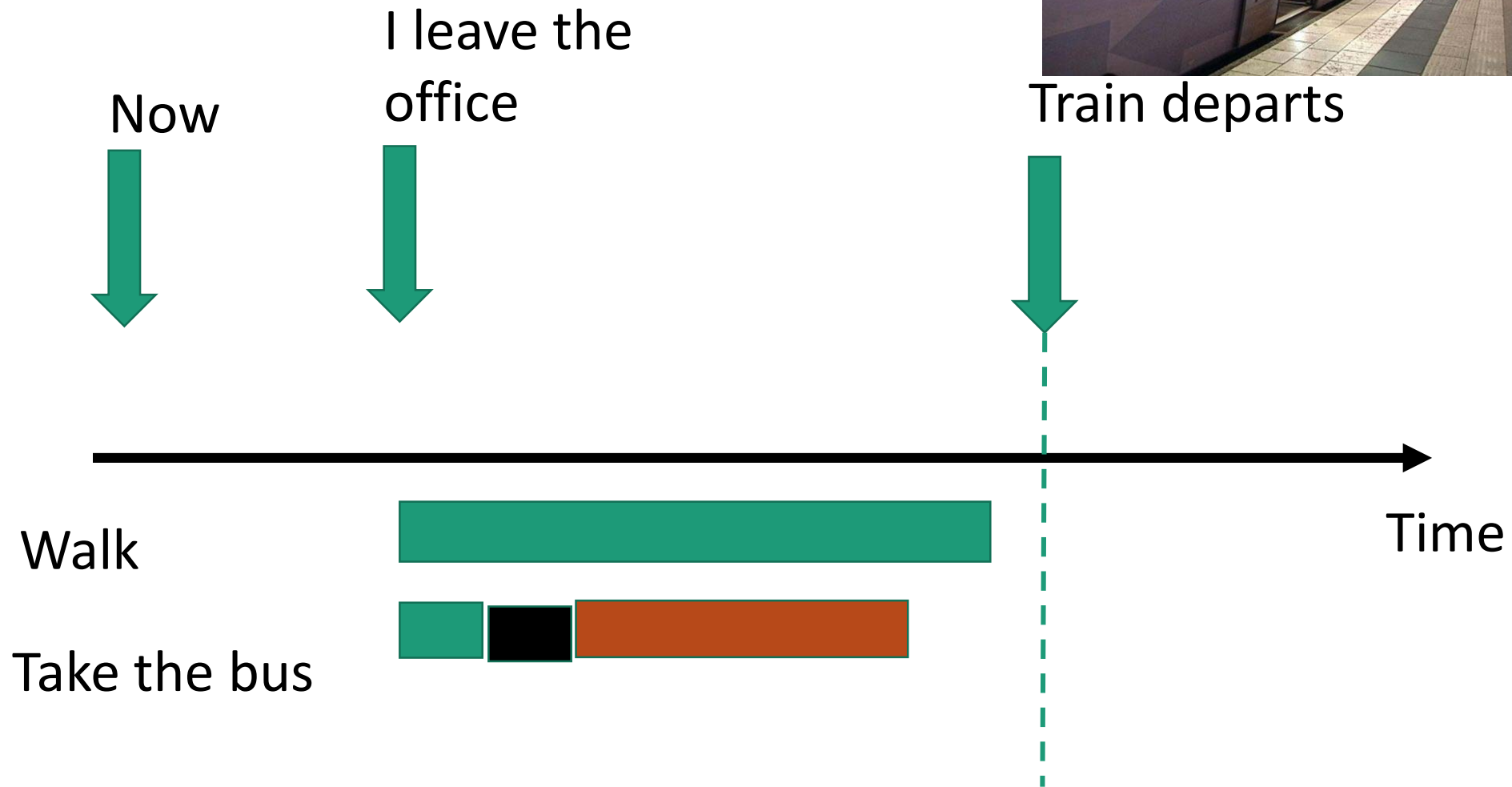
Train departs

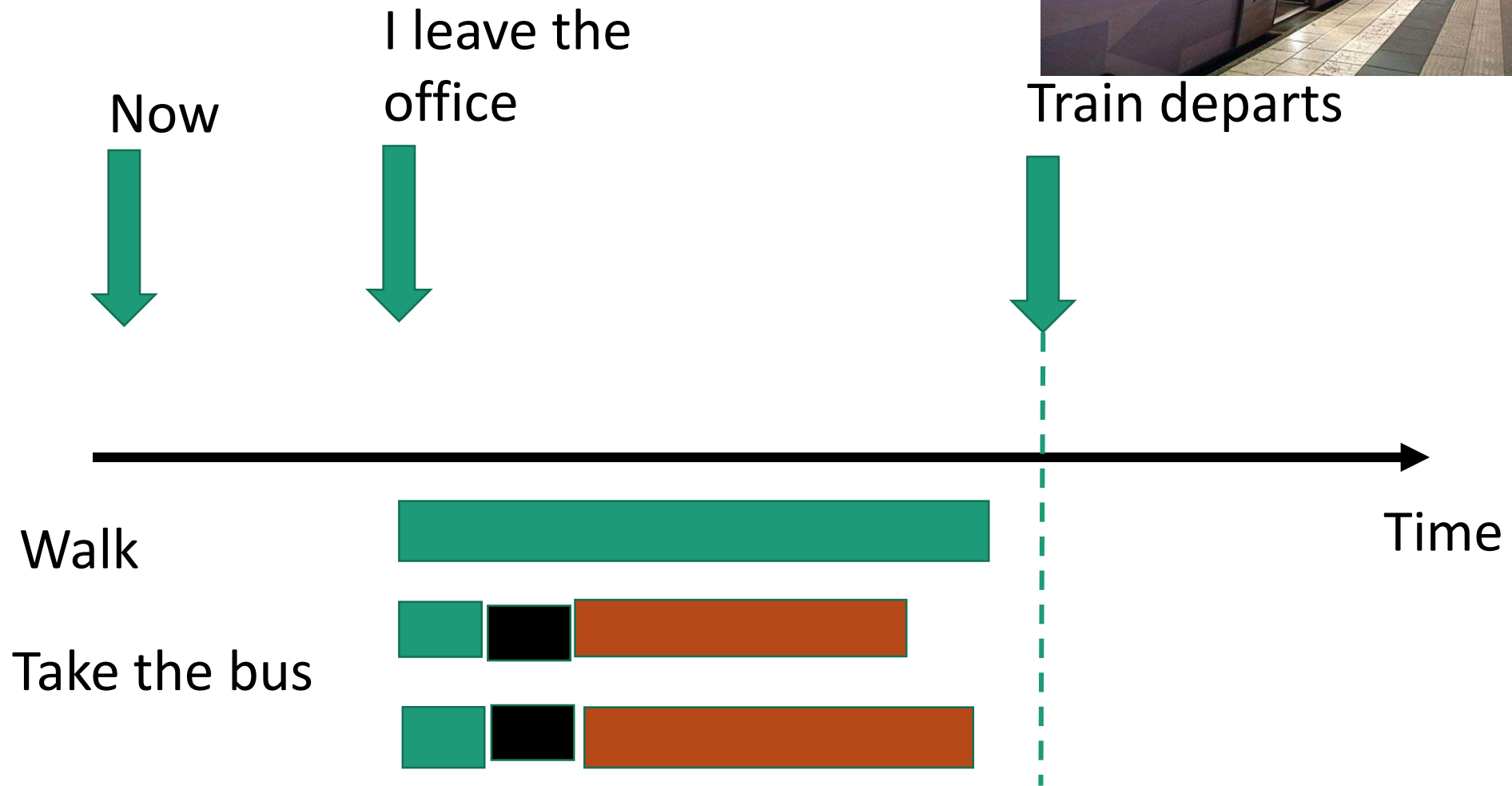


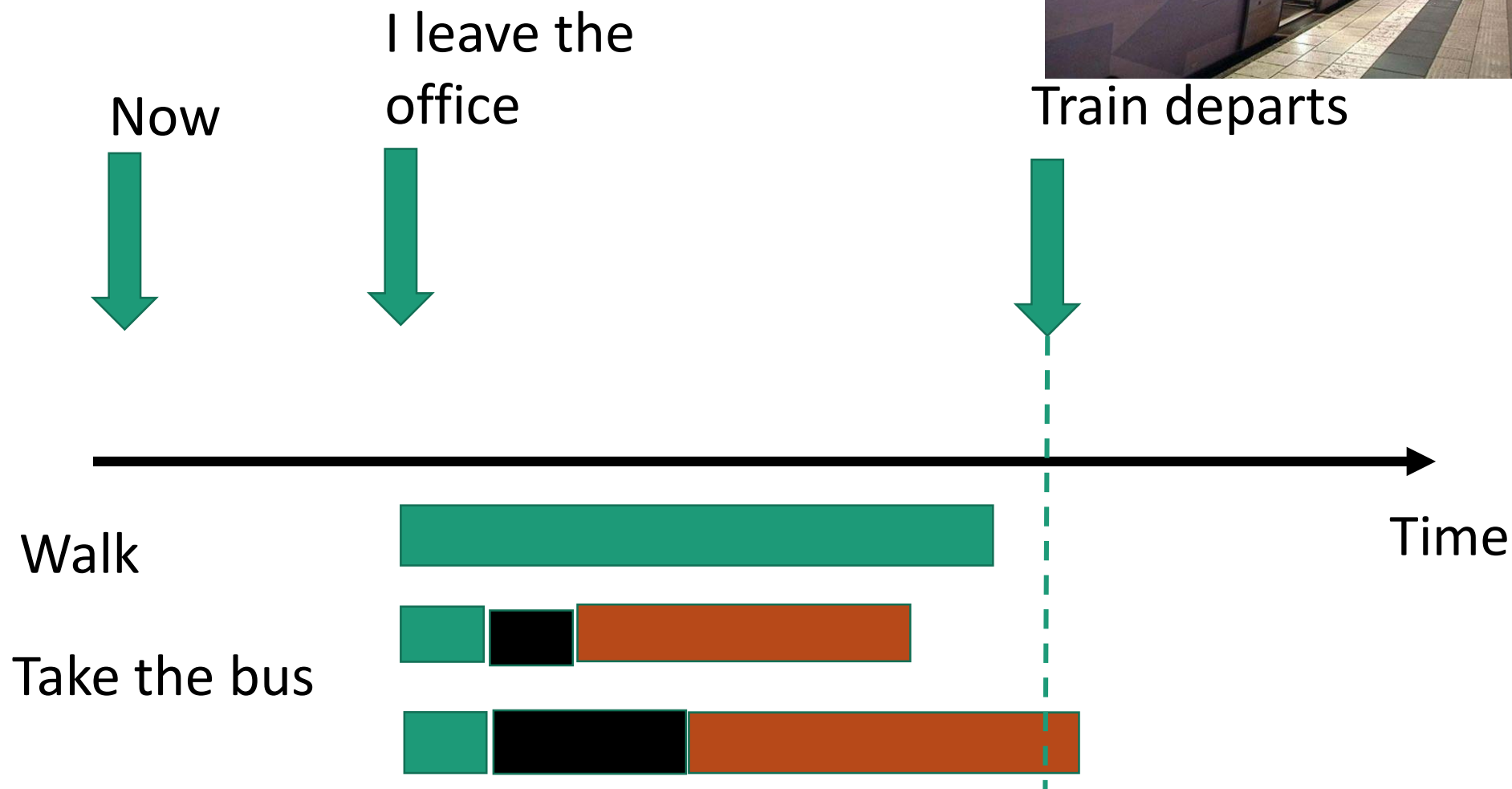
Time

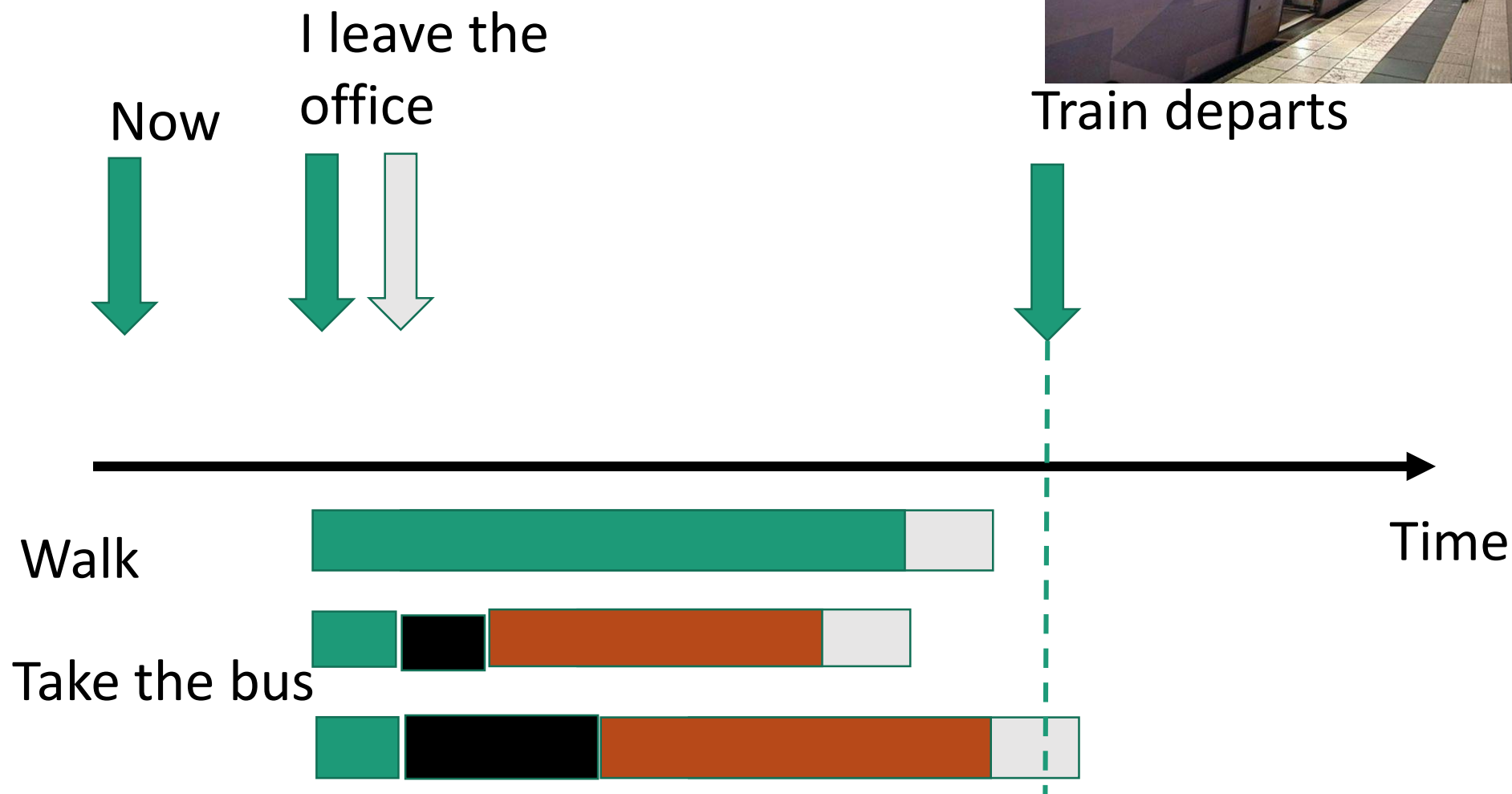




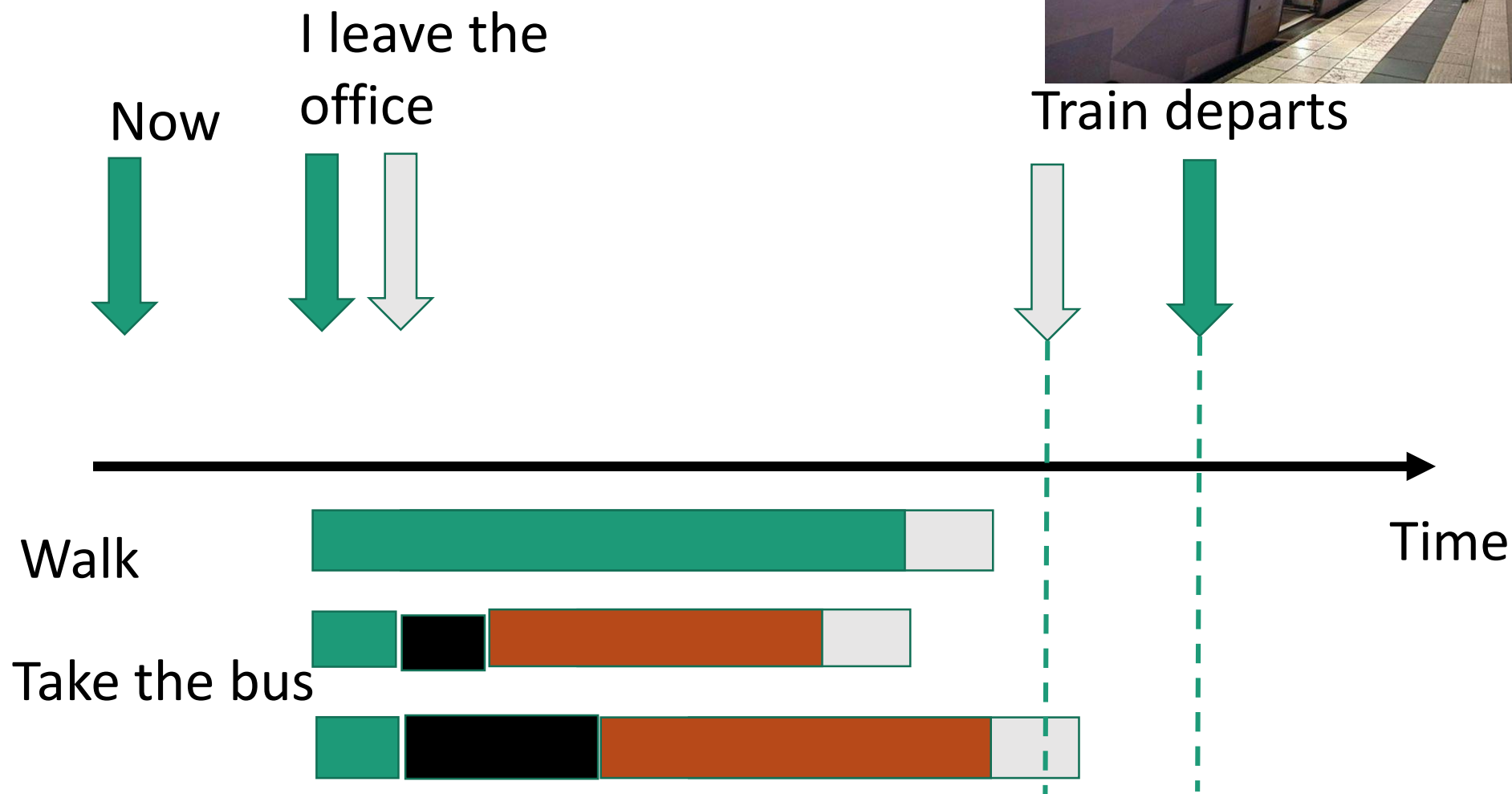






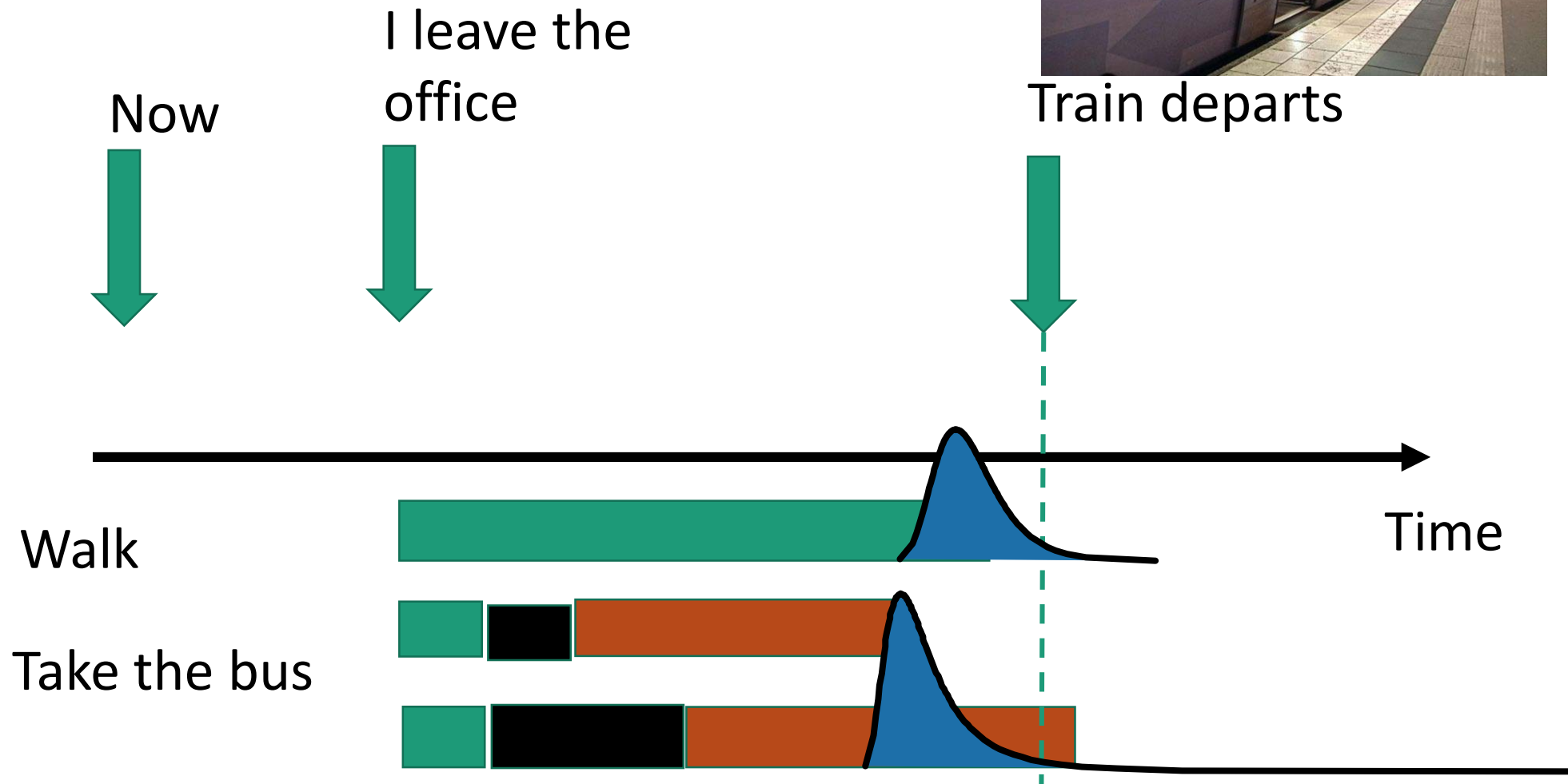






# What makes a decision?

- An agent
- Her values
- An idea of what is a good decision
- Decision alternatives
- Uncertainties (including certainty) in the outcomes of these alternatives





# Outline

- Decisions are often far from simple
- Learning & forecasting to make decisions
- Extreme events and uncertainty
- Consider extreme events in system and knowledge dimensions
- More than one scientific perspective on extreme events



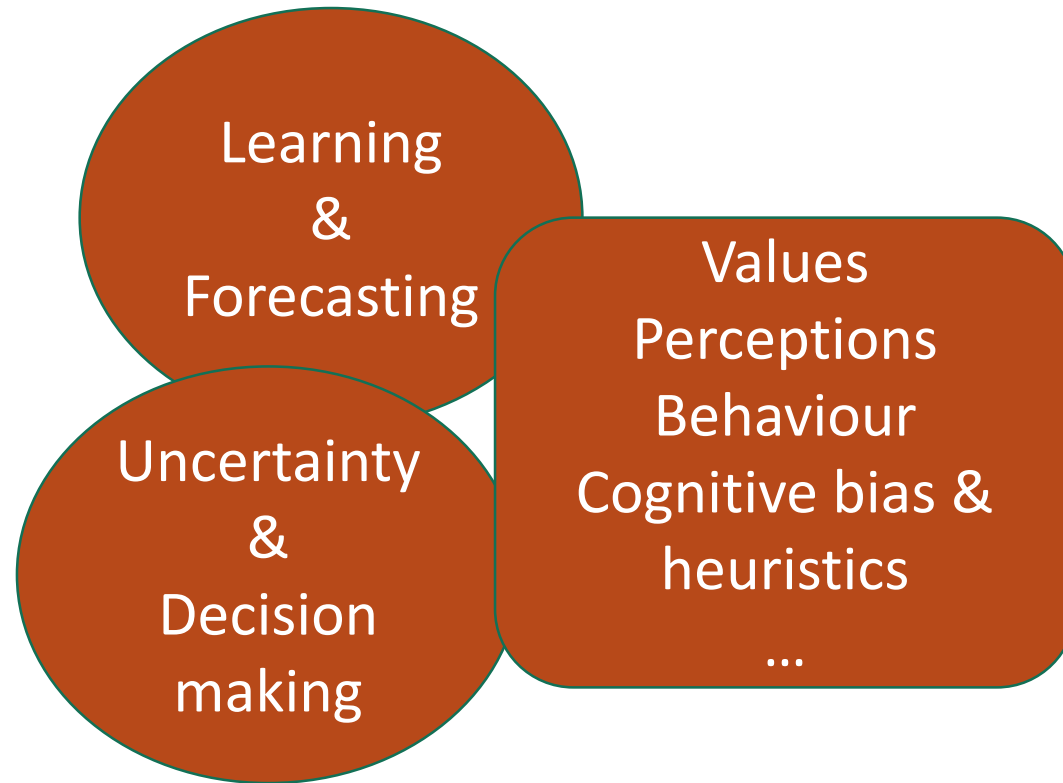
# Coastline erosion and sea level rise



- It is desirable to live close to the sea, but coastline erosion cause
- Large economic loss
- Threatens biodiversity and recreation
- Loss of protection against high sea levels
- Requires coordinated management



Caroline Fredriksson and Hans Hansson, LTH.  
Aktuella Frågor 27 April 2017



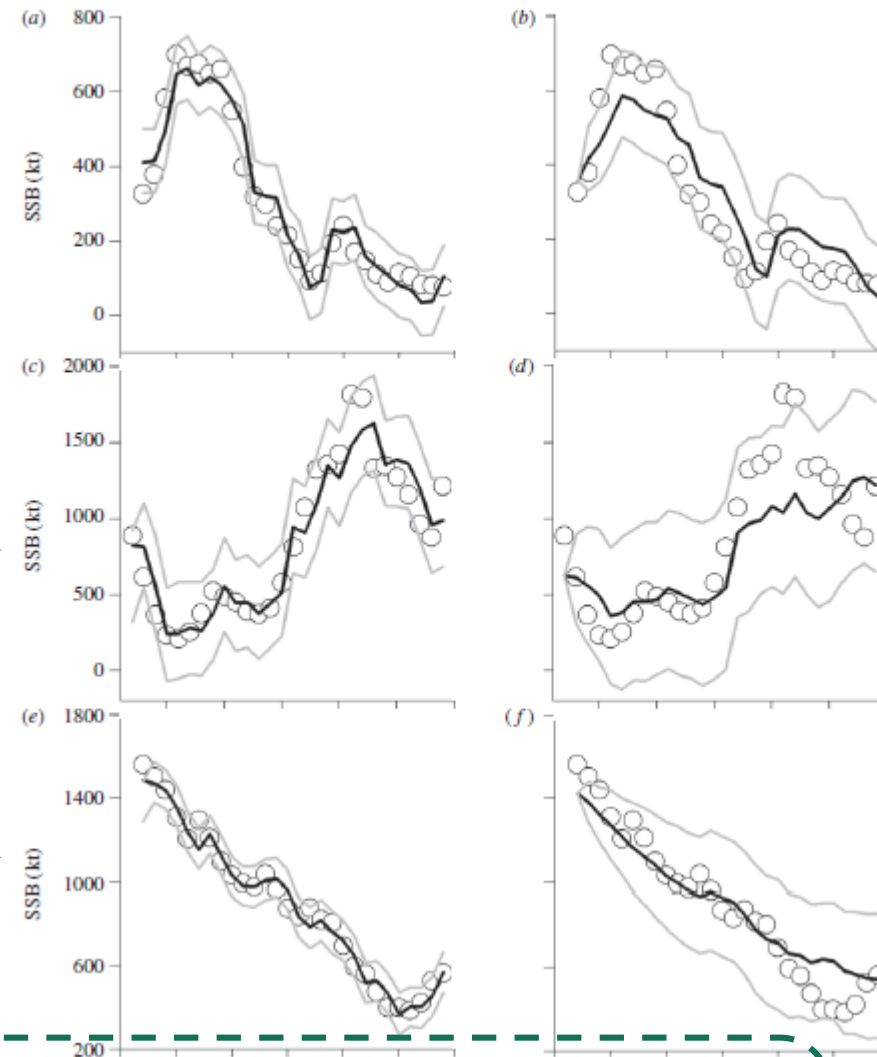
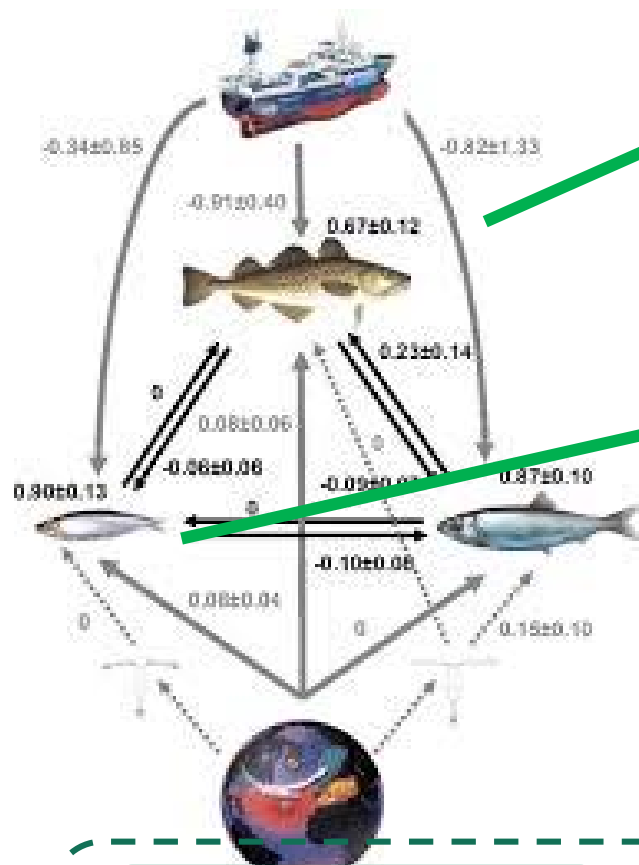
# On the board

- The DM is interested in uncertainty in the event  $A$
- Uncertainty in  $A$  is described using probability  $P(A|K)$
- $K$  is our knowledge
- $P(A|K) = P(A|\theta)P(\theta|K)$
- $P(A|\theta)$  "forecasting"
- $P(\theta|K)$  "learning"



# Fishery management

Learning



THEORY

EXPERT  
KNOWLEDGE

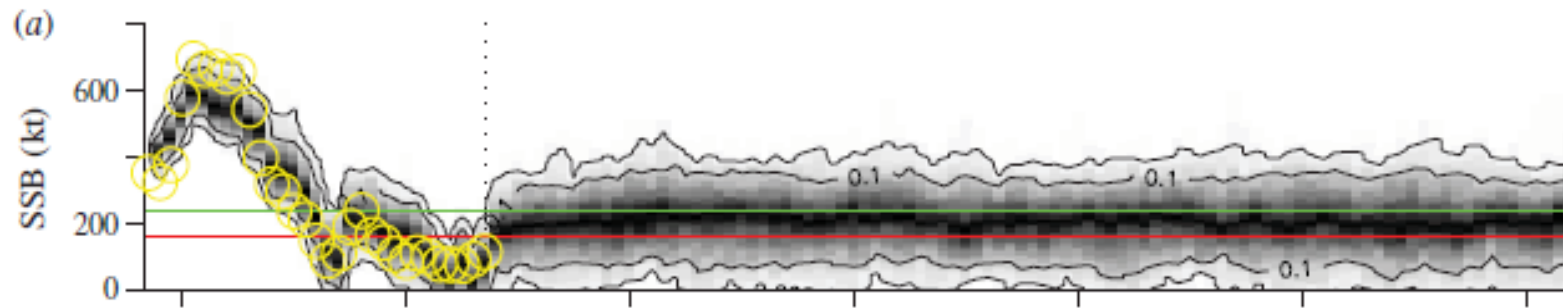
DATA



# Fishery management

2126 M. Lindegren *et al.* *Forecasting under climate change*

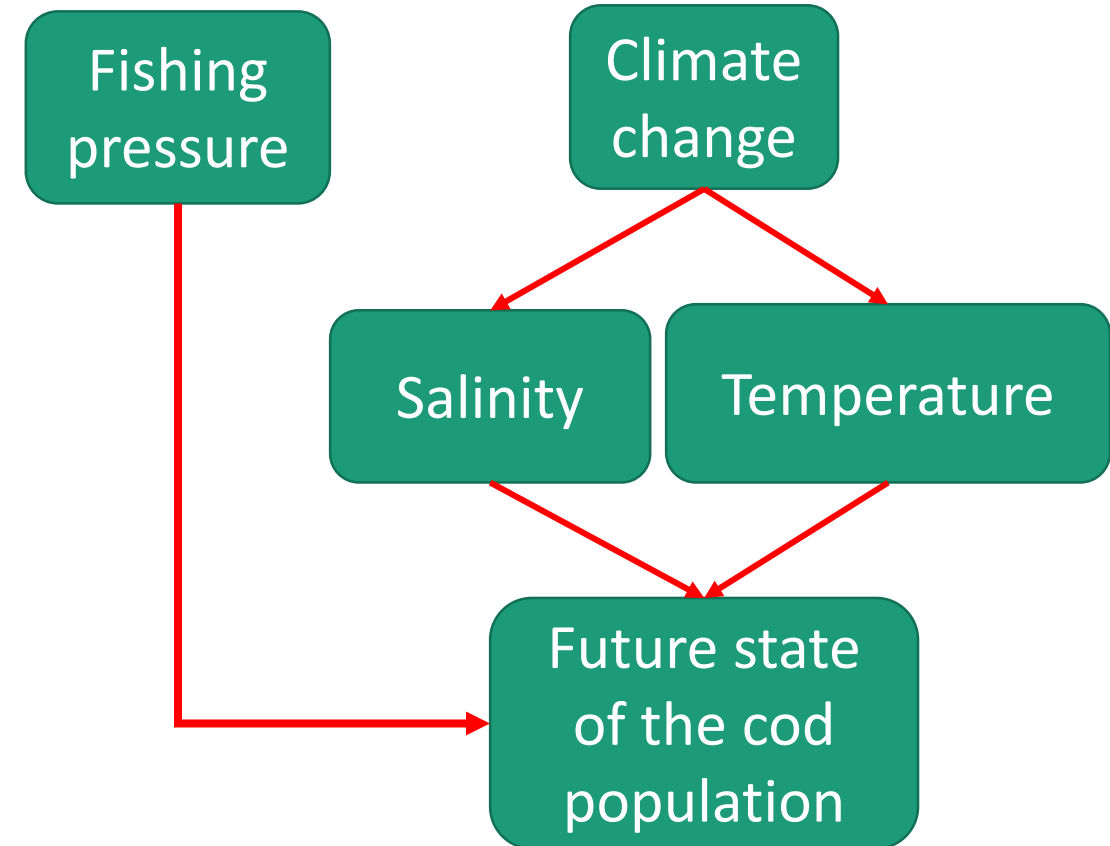
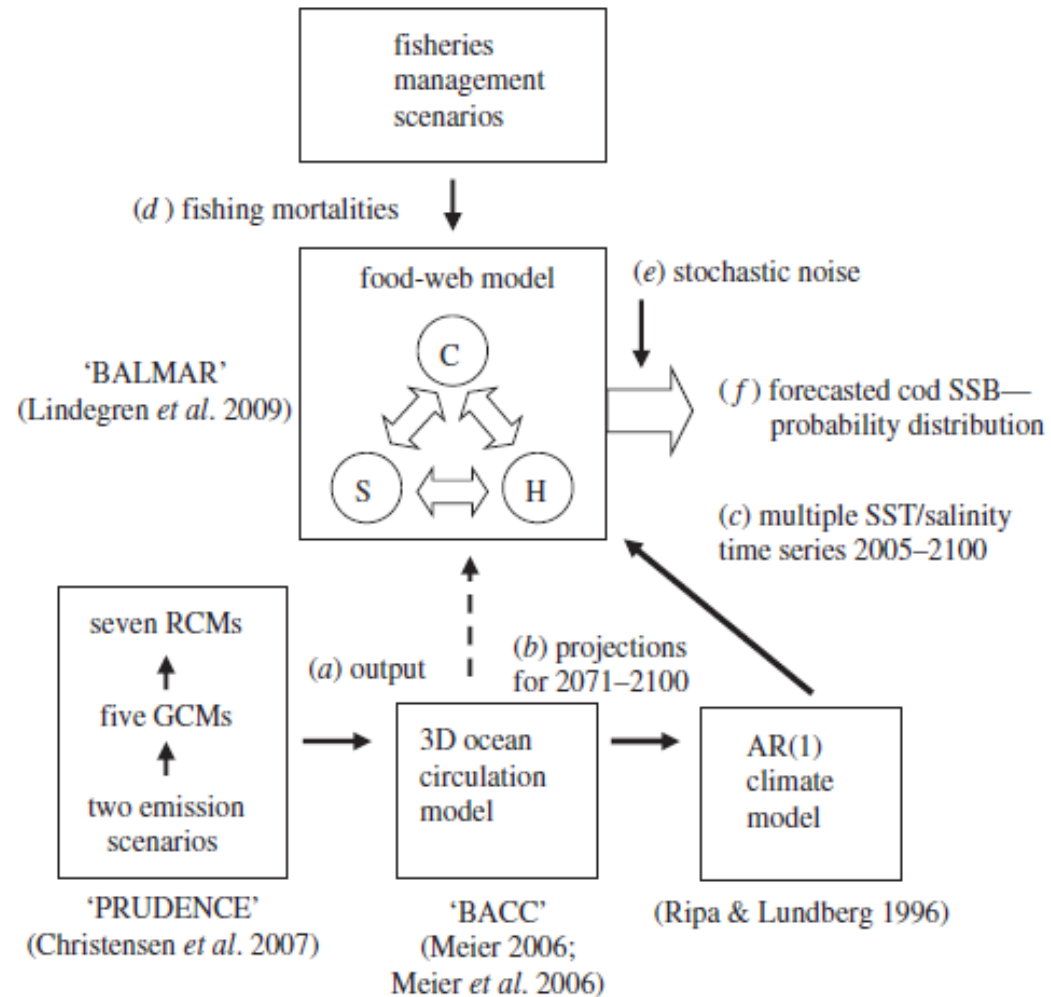
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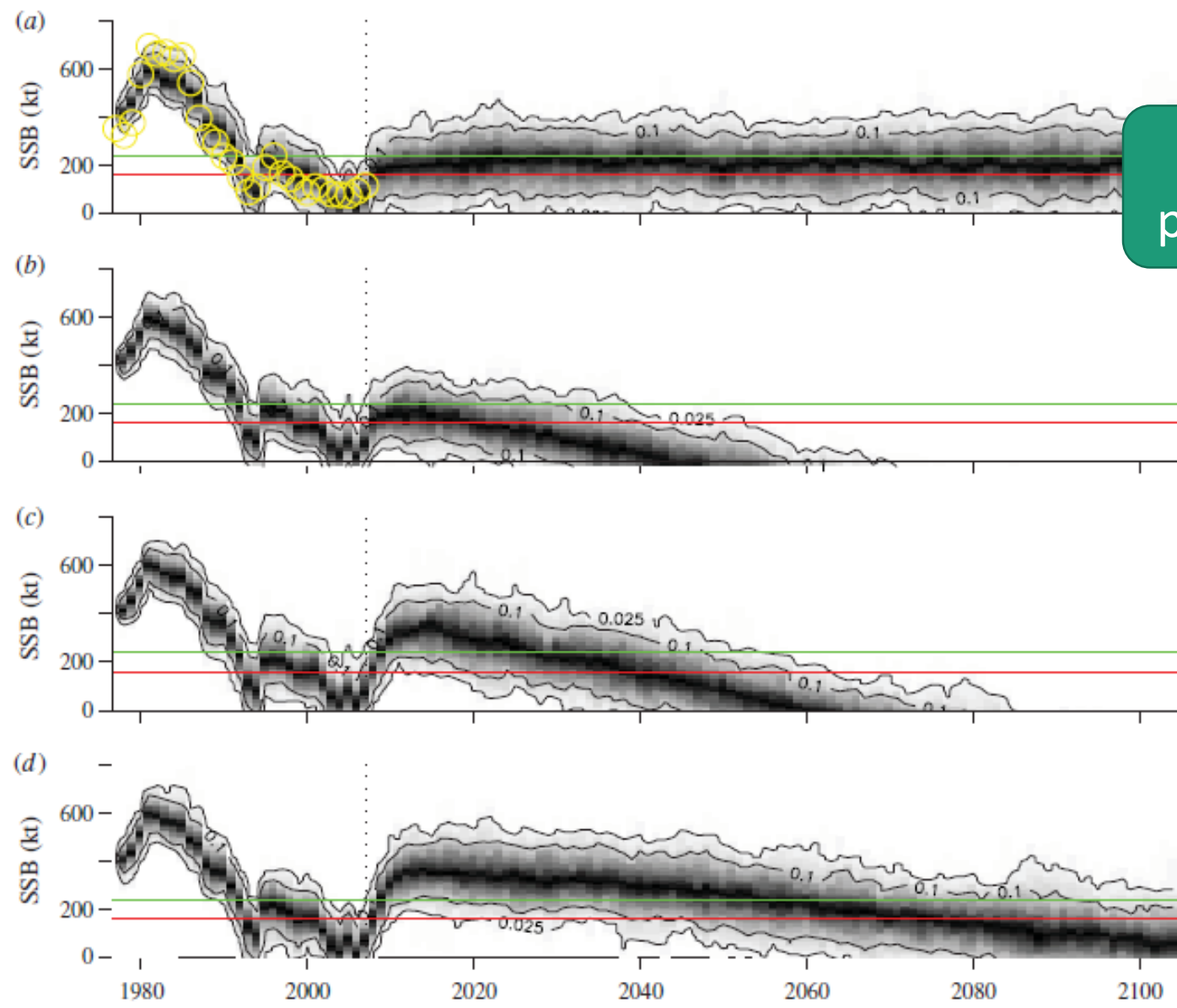


Learning

Forecasting

# Forecasting under climate change





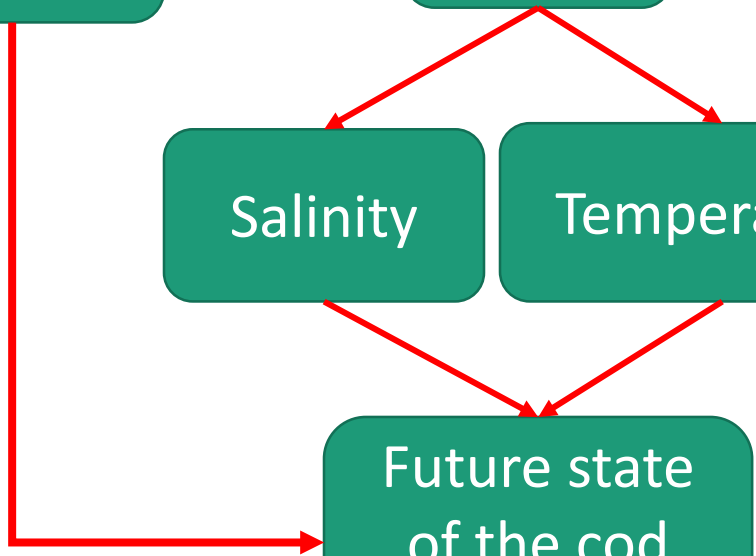
Fishing pressure

Climate change

Salinity

Temperature

Future state of the cod population

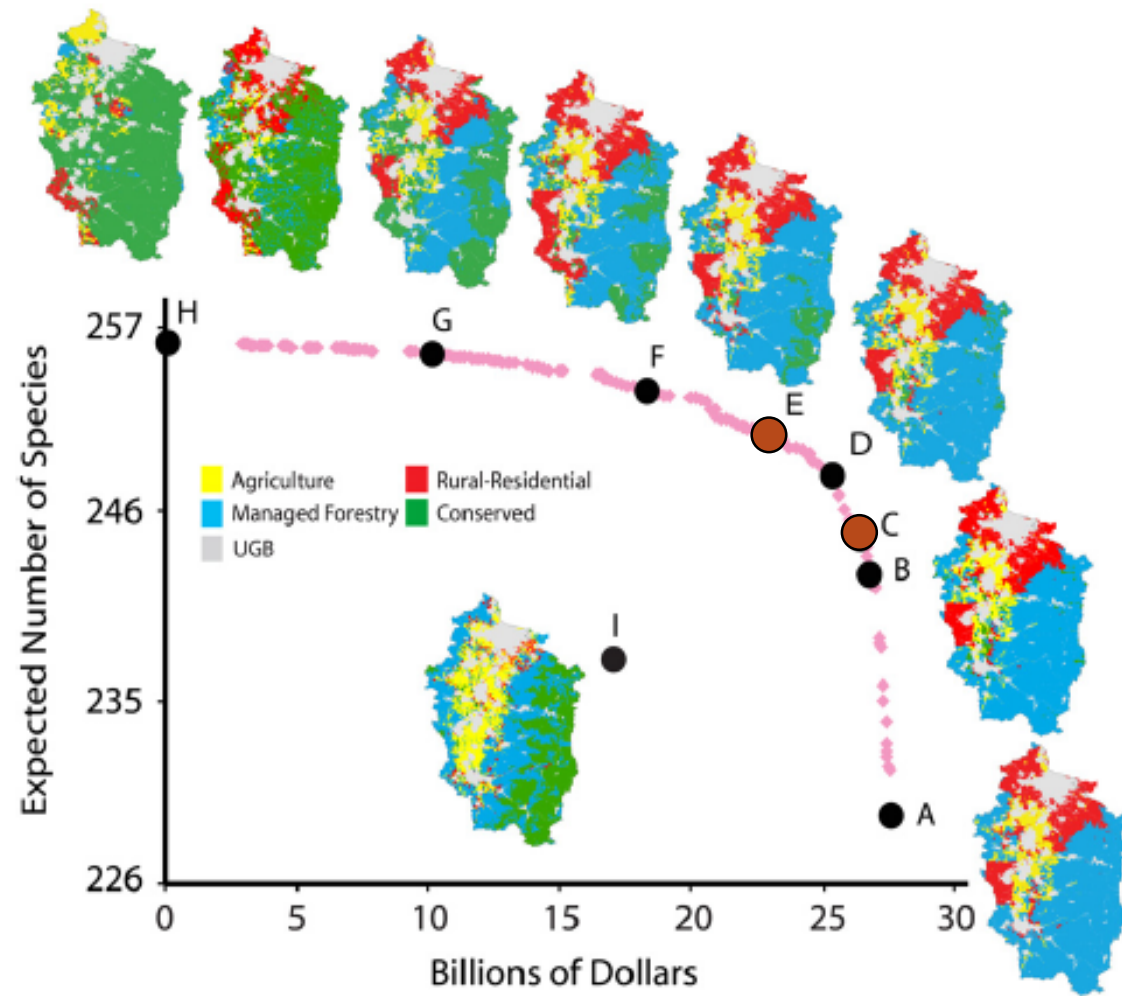




# Biodiversity by land-use management

1516

BIOLOGICAL CONSERVATION 141 (2008) 1505–1524



- Spatial planning
- Trade-offs and synergies
- Efficiency frontiers

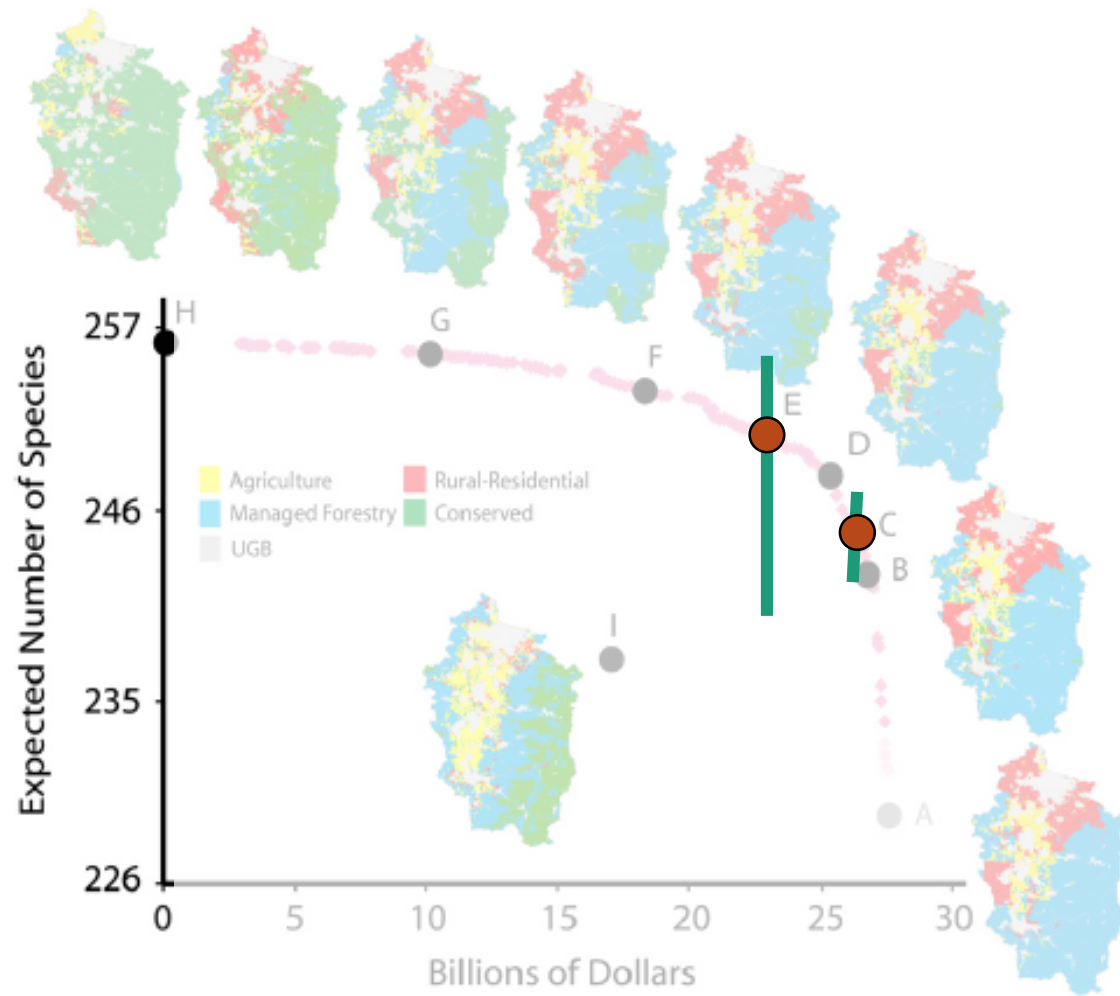


LUND  
UNIVERSITY

# Biodiversity by land-use management

1516

BIOLOGICAL CONSERVATION 141 (2008) 1505–1524



- Spatial planning
- Trade-offs and synergies
- Efficiency frontiers
- Uncertainty in outcomes

Expectation:  
Mean - a location  
Prevision - a quantity  
important for decisions

# What is an extreme event?



# What is an extreme event?



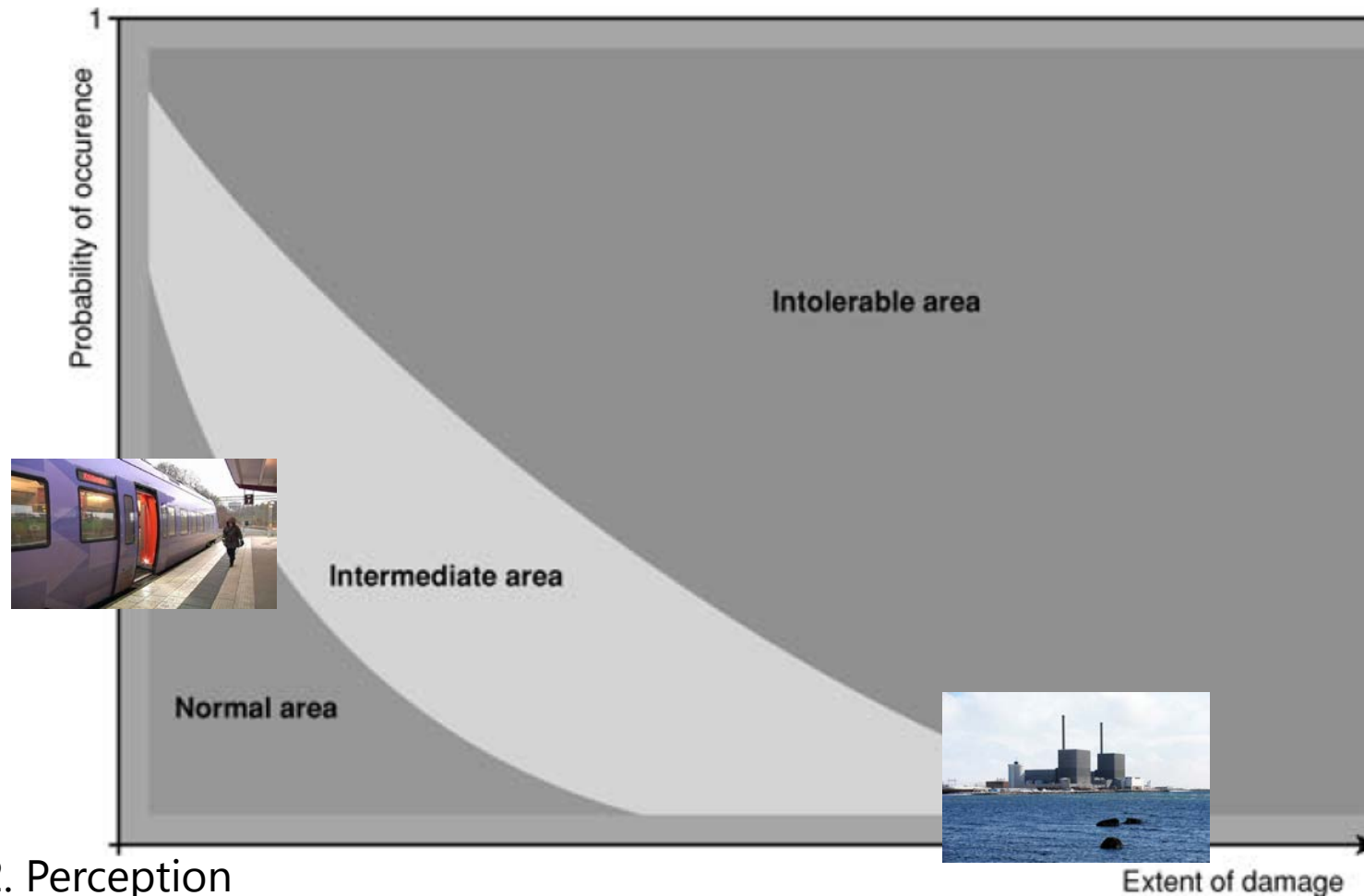
Kaplan and Garrick. 1981. On The Quantitative Definition of Risk. Risk Analysis



Klinke and Renn. 2002. Risk Analysis.

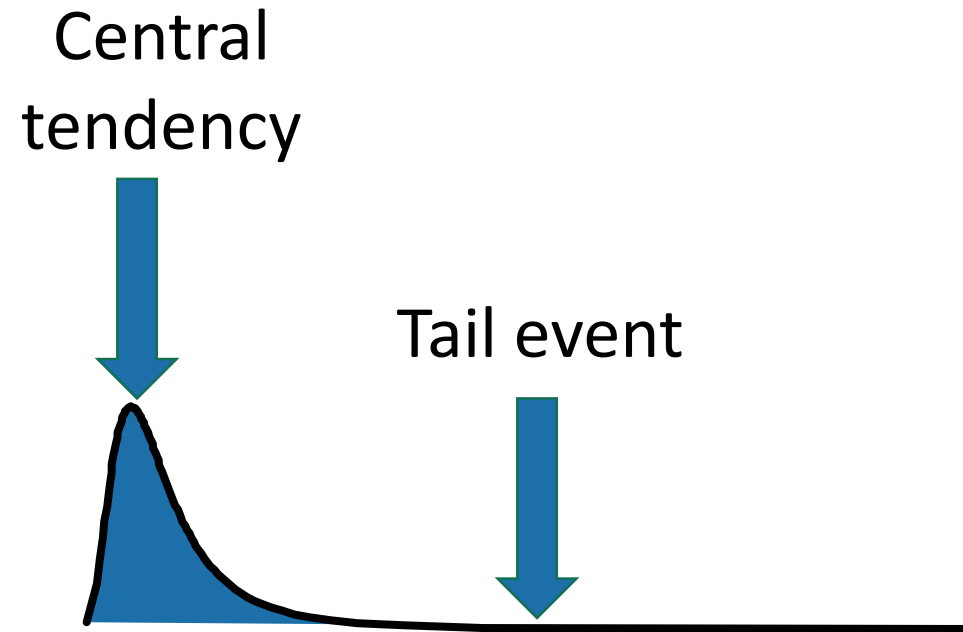


Slovic and Weber. 2002. Perception of risk posed by extreme events.





# What is an extreme event?

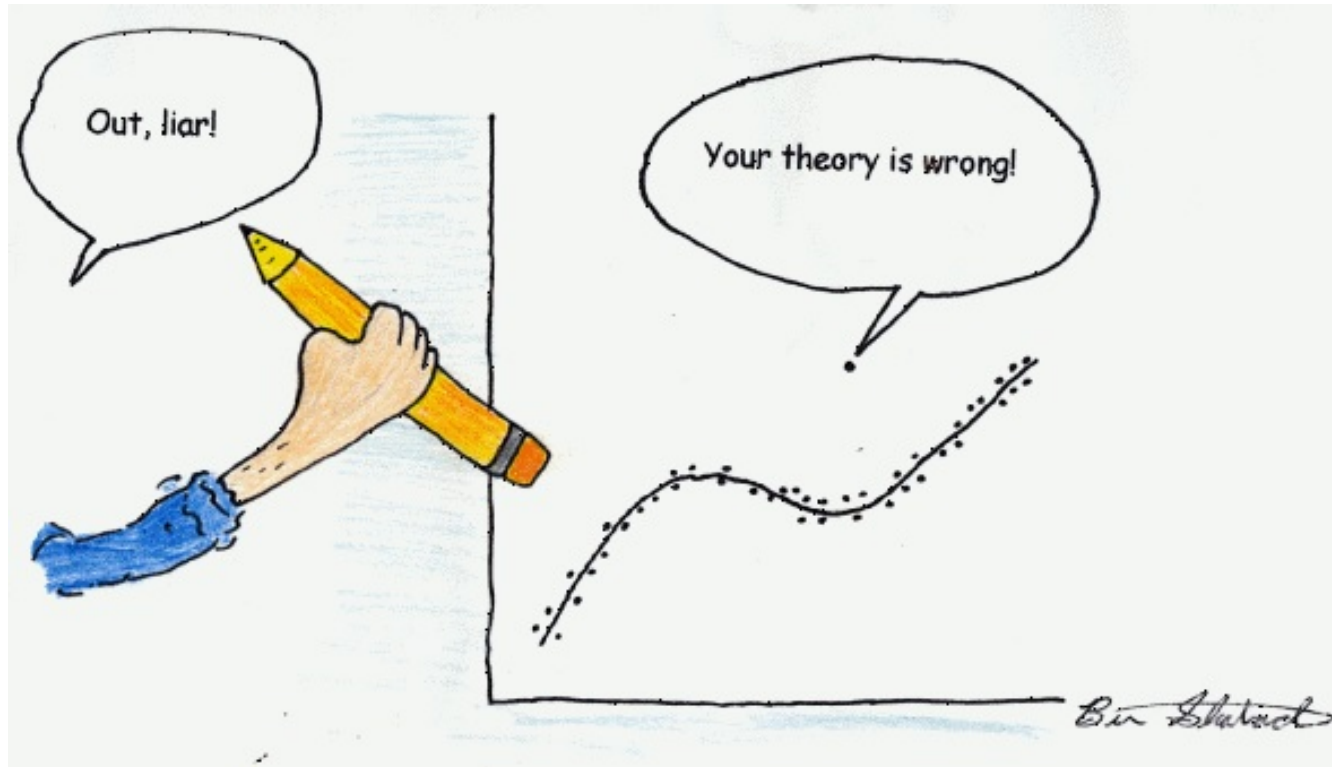




# What is an extreme event?



# What is an extreme event?





# What is an extreme event

System dimension:

- Unlikely – rare, low frequency
- Large consequence

Knowledge dimension:

- Unlikely – low weight among possible outcomes, surprise in relation to central tendency
- Surprise – large uncertainty due to lack of knowledge
- Unknown unknown – the unforeseen

Probability-  
based thinking

$P(A|K)$

Strength in  
knowledge

$S(K)$

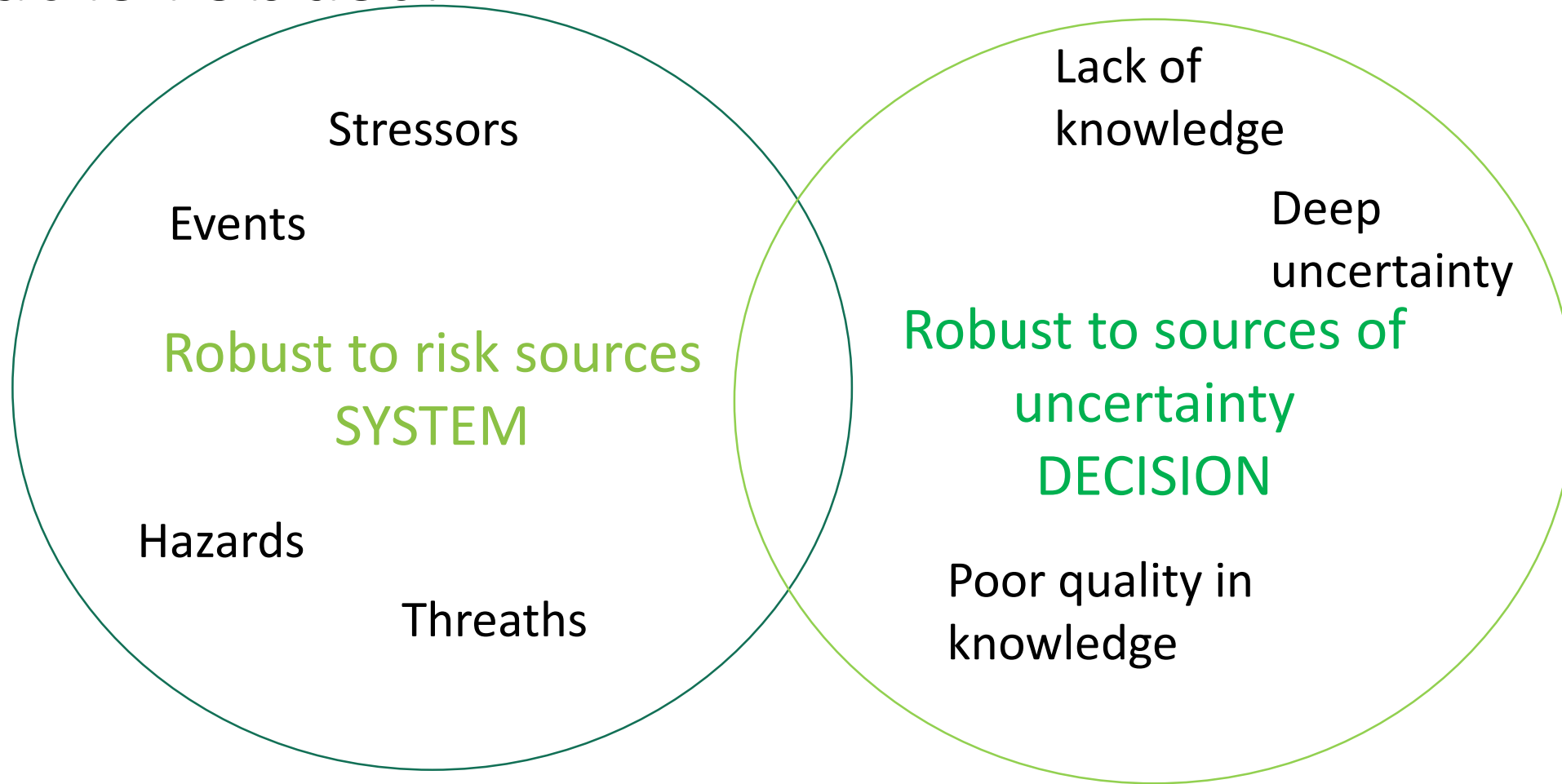
Surprises  
(black swans)

$K'$



Considering extreme events in Learning & Forecasting  
is required to make robust decisions

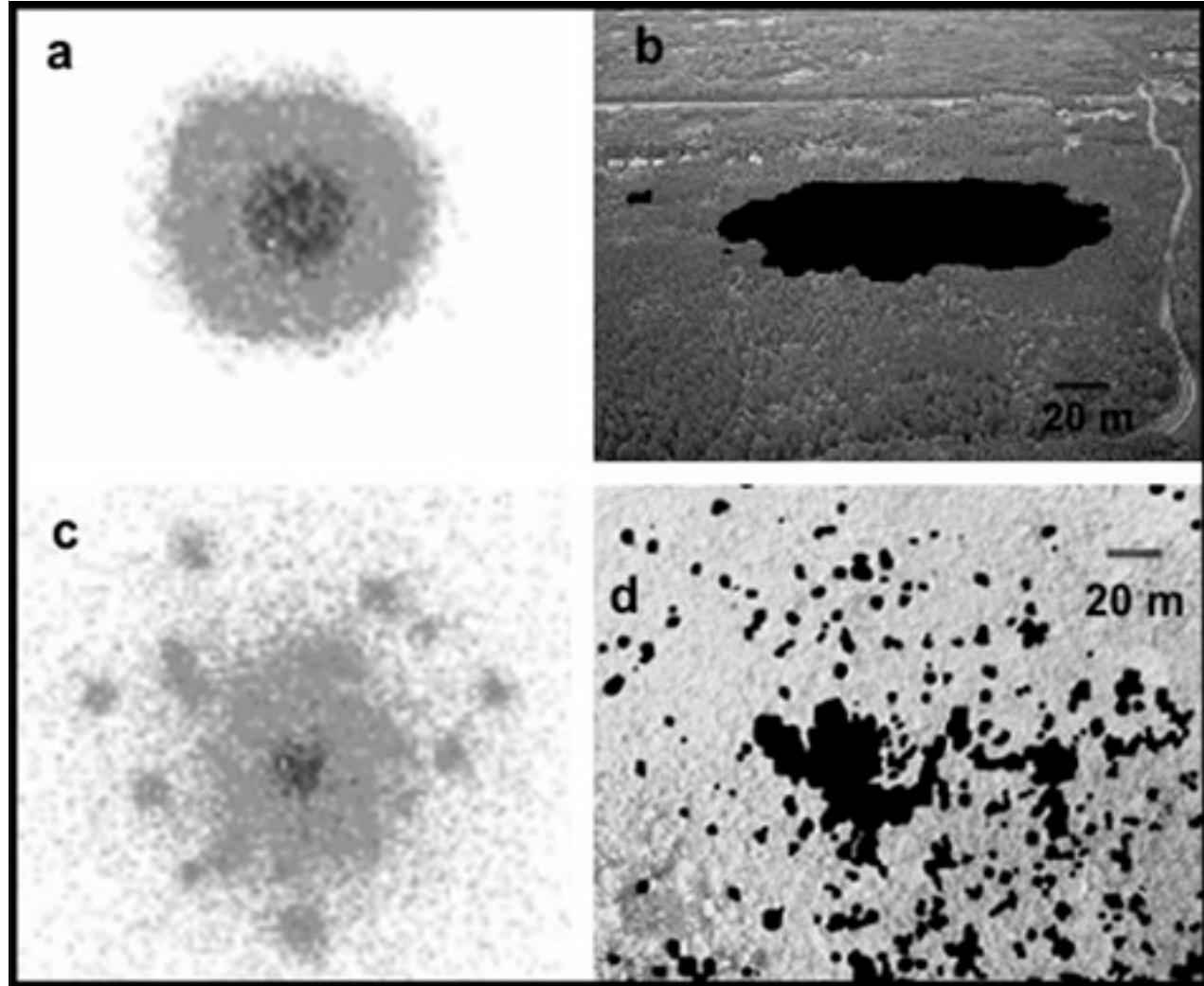
# What is robust?



- “Robust to uncertainty” refers to a decision’s ability to be acceptable despite prevailing sources of uncertainty

# Include extreme events in modelling

Short and long distance dispersal



Marco, et al. 2011. Comparing short and long-distance dispersal: modelling and field case studies. *Ecography*

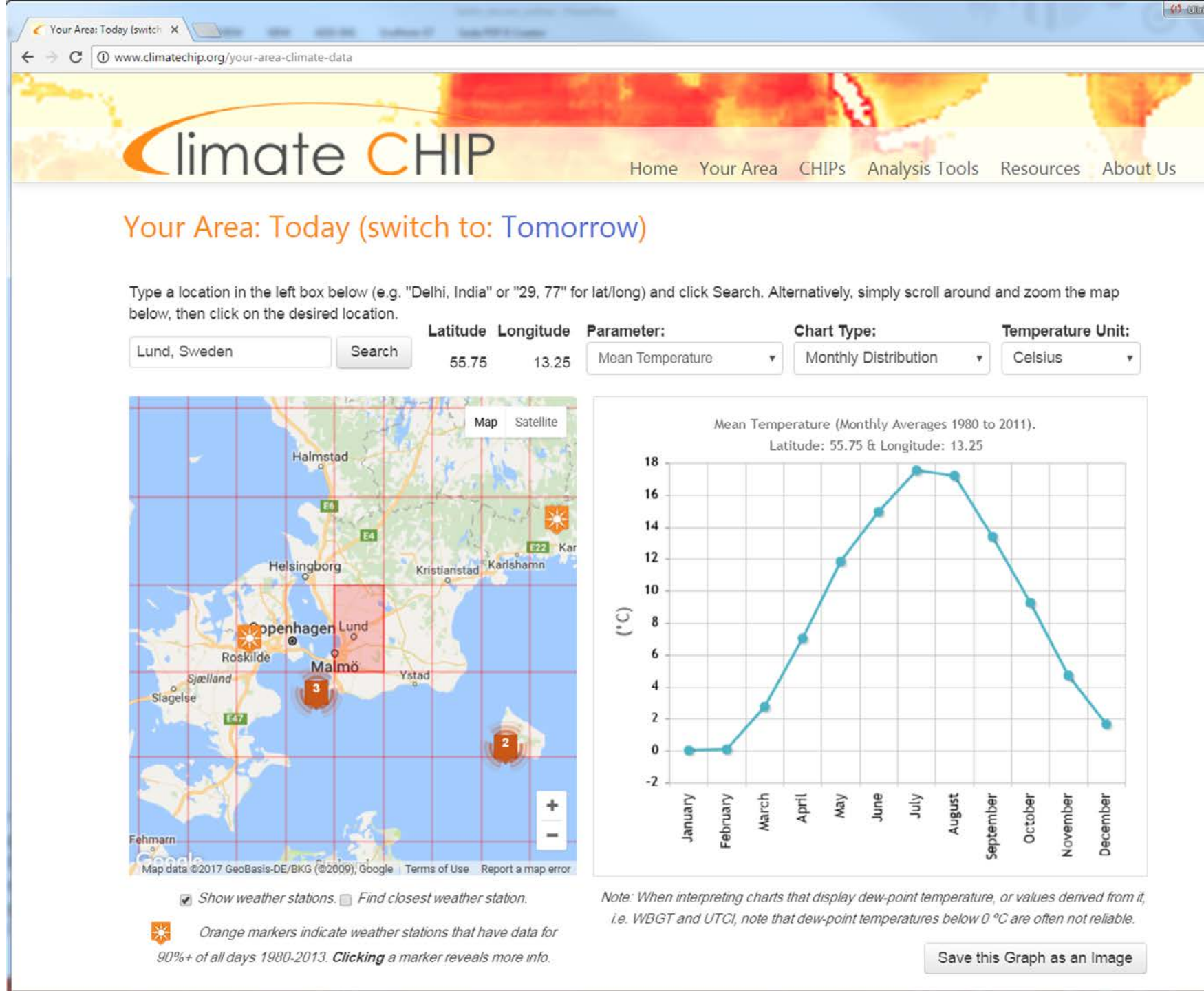
# Include extreme events in modelling

Climate projections



# Include extre

## Climate projections



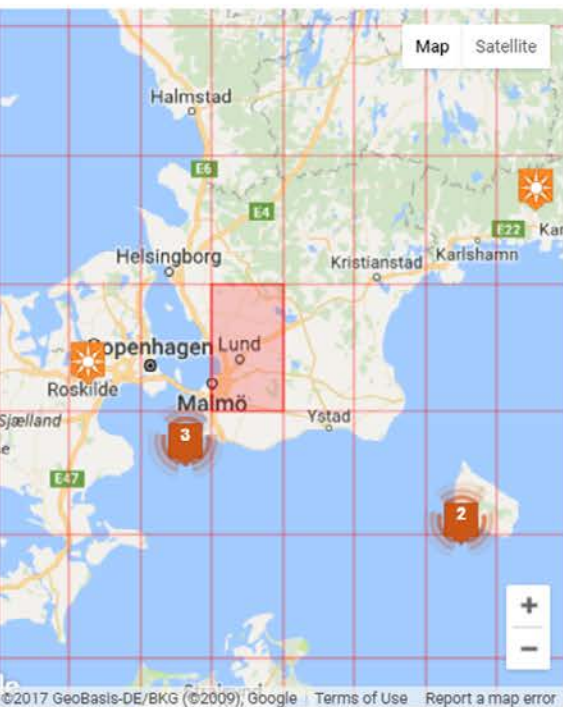
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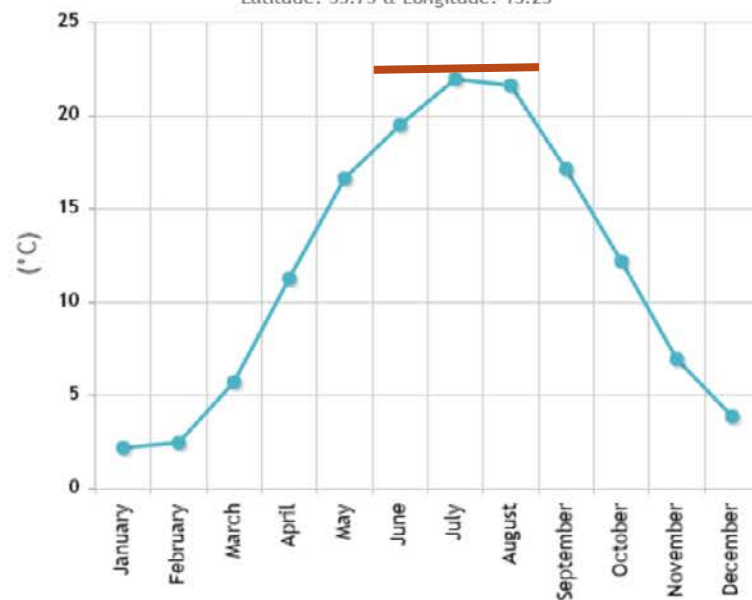
Latitude  Longitude 
 Parameter: 
 Chart Type: 
 Temperature Unit:



Show weather stations. Find closest weather station.

Orange markers indicate weather stations that have data for all days 1980-2013. Clicking a marker reveals more info.

Maximum Temperature (Monthly Averages 1980 to 2011).  
Latitude: 55.75 & Longitude: 13.25



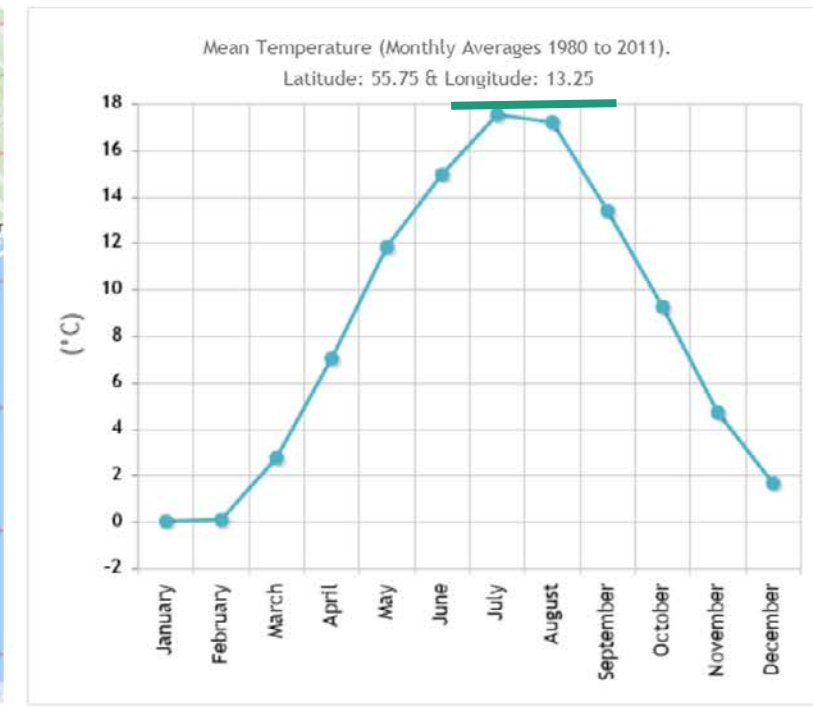
Note: When interpreting charts that display dew-point temperature, or values derived from it, i.e. WBGT and UTCI, note that dew-point temperatures below 0 °C are often not reliable.

Save this Graph as an Image

Area: Tomorrow

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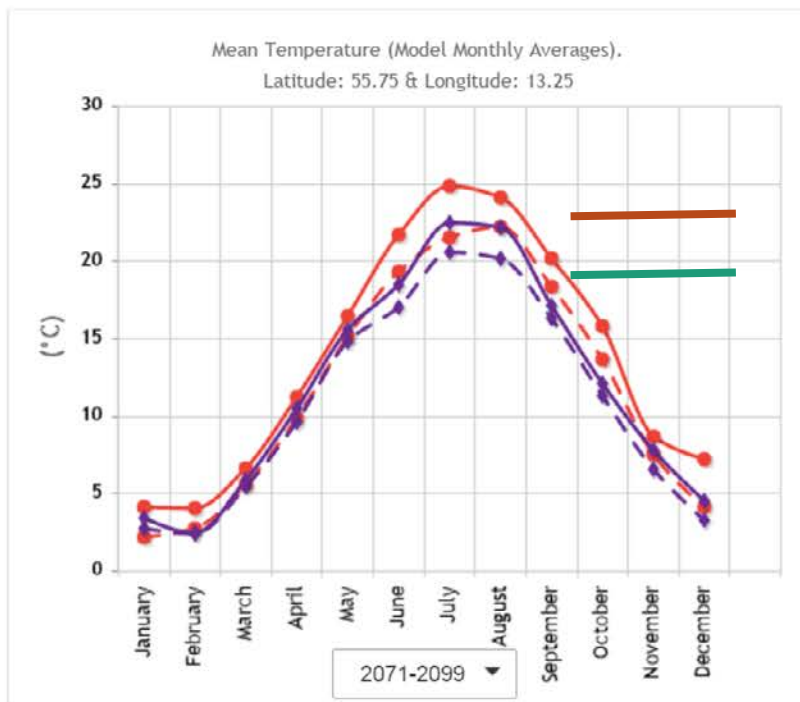
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Latitude  Longitude 
 Parameter: 
 Chart Type: 
 Temperature Unit:



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☒ RCP 8.5 —

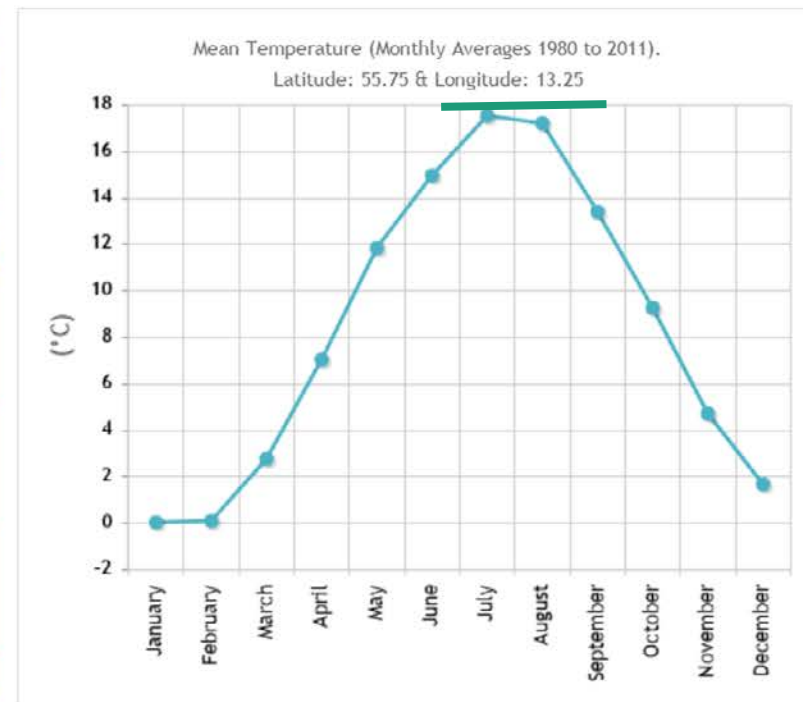
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Latitude  Longitude 
 Parameter: 
 Chart Type: 
 Temperature Unit:

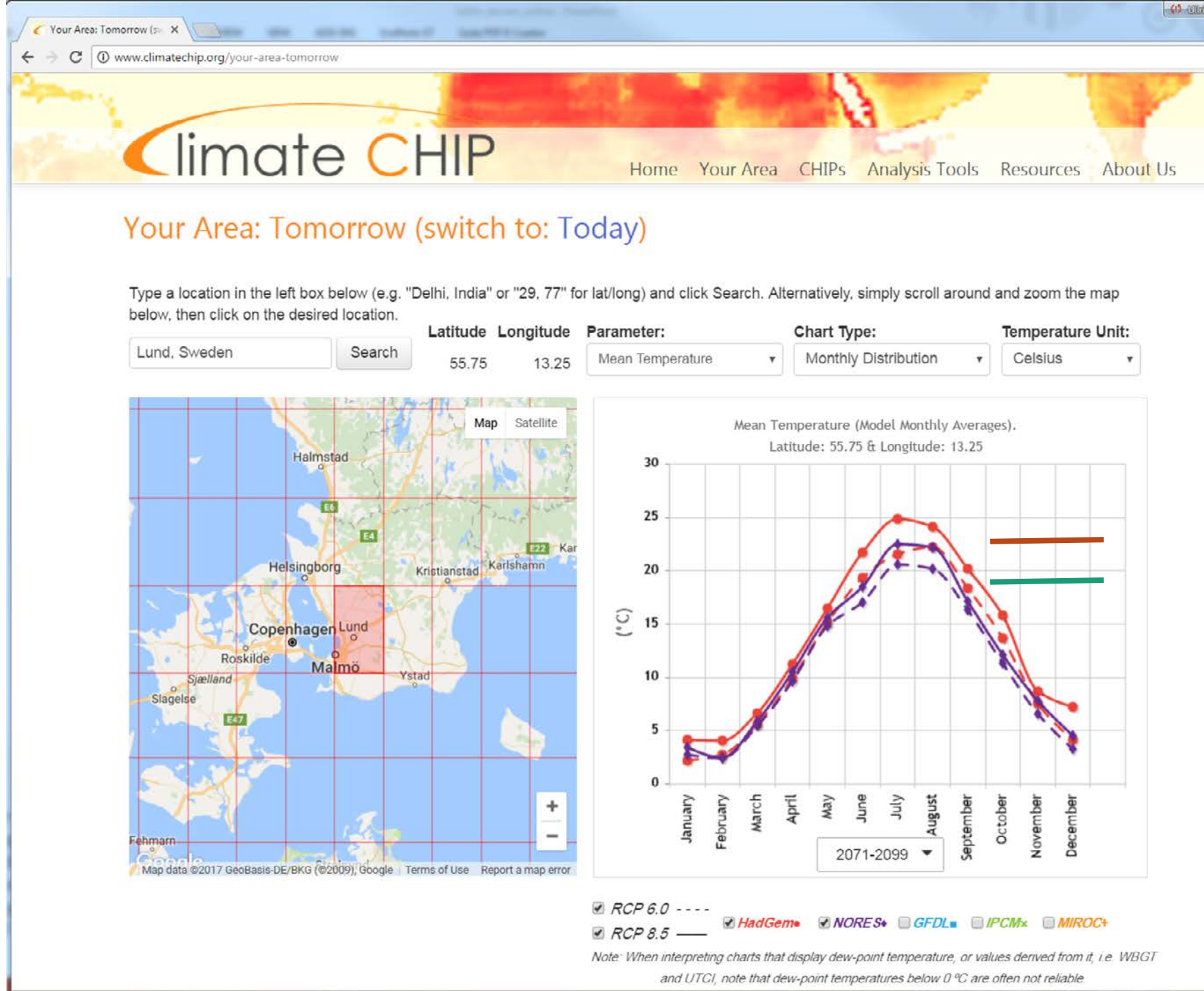


Note: When interpreting charts that display dew-point temperature, or values derived from it, i.e. WBGT and UTCI, note that dew-point temperatures below 0 °C are often not reliable.

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# Include extre

## Climate projections





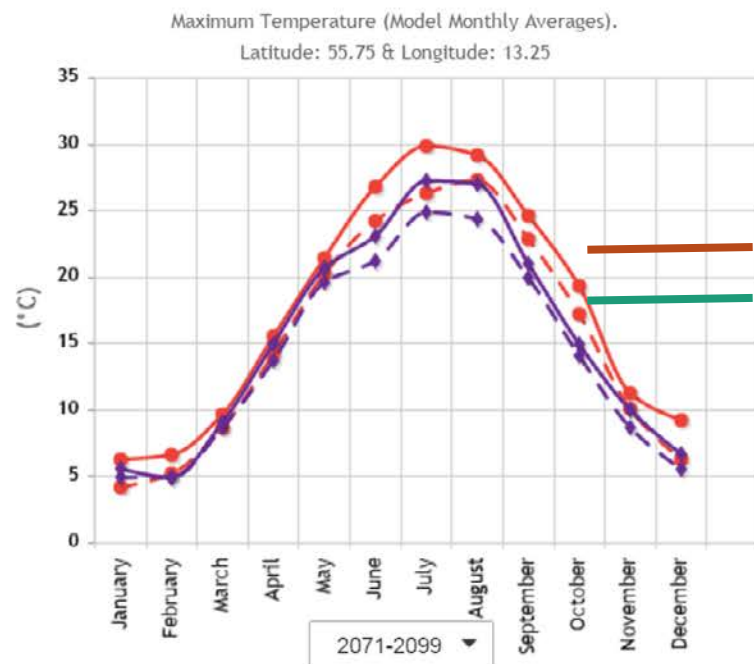
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Sweden  Latitude: 55.75 Longitude: 13.25 Parameter: Maximum Temperature Chart Type: Monthly Distribution Temperature Unit: Celsius



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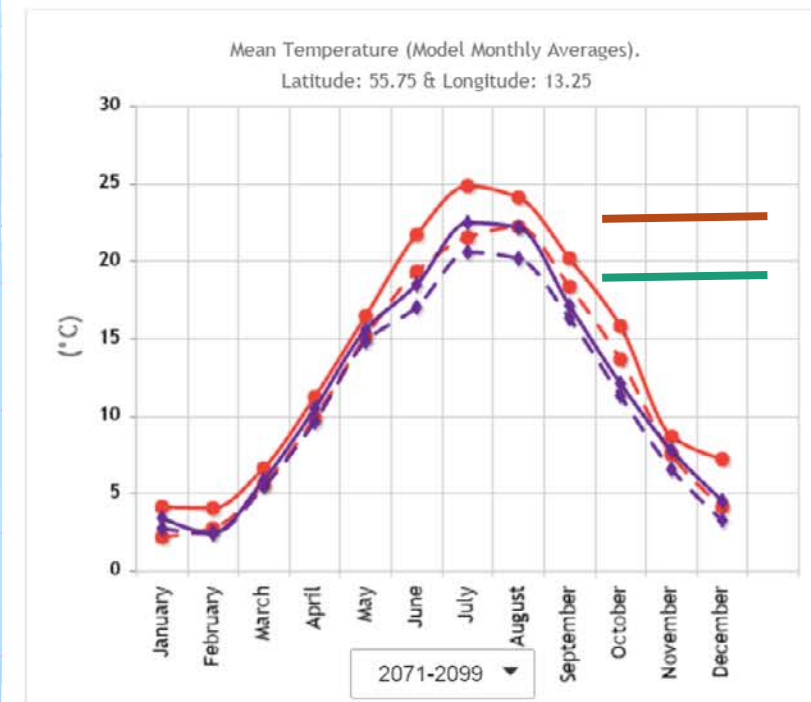
☒ RCP 8.5 ———

Note: When interpreting charts that display dew-point temperature, or values derived from it, i.e. WBGT and UTCI, note that dew-point temperatures below 0 °C are often not reliable.

oday)

or lat/long) and click Search. Alternatively, simply scroll around and zoom the map

Parameter: Mean Temperature Chart Type: Monthly Distribution Temperature Unit: Celsius



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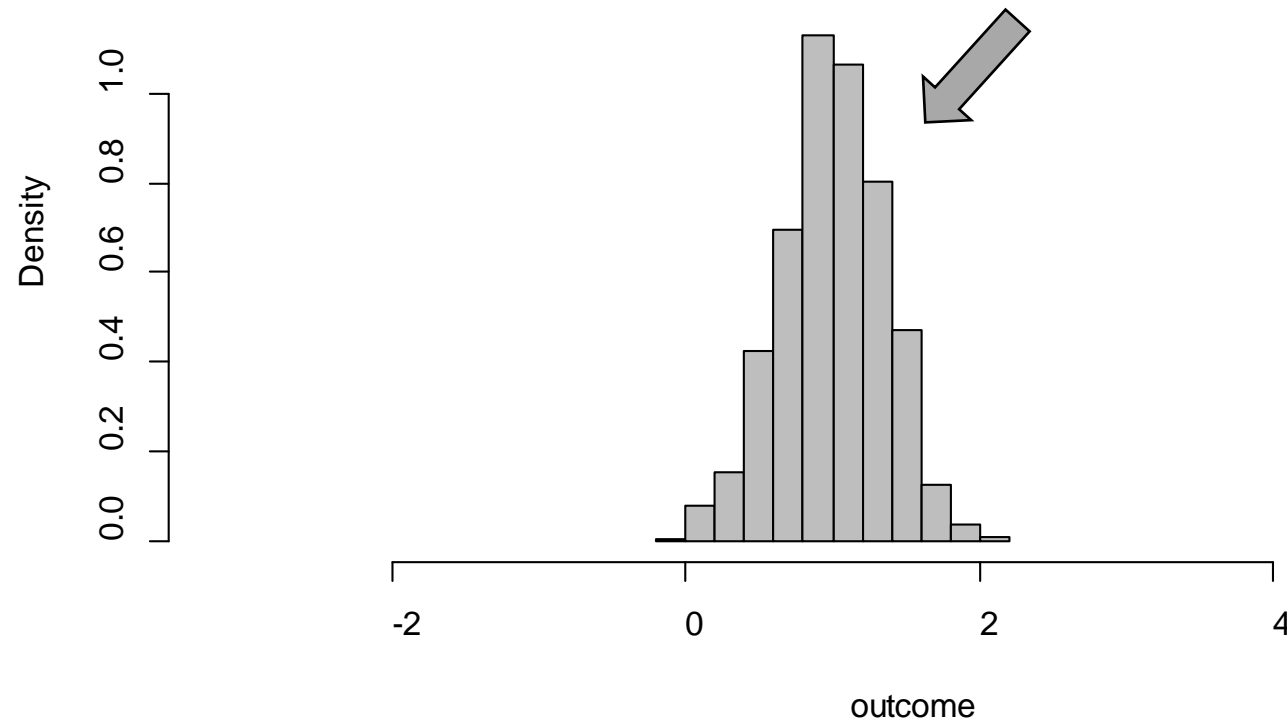
☒ RCP 8.5 ———

Note: When interpreting charts that display dew-point temperature, or values derived from it, i.e. WBGT and UTCI, note that dew-point temperatures below 0 °C are often not reliable.

# Use statistical theory for extreme events

Law of large numbers

A sample of sample means is Normally distributed

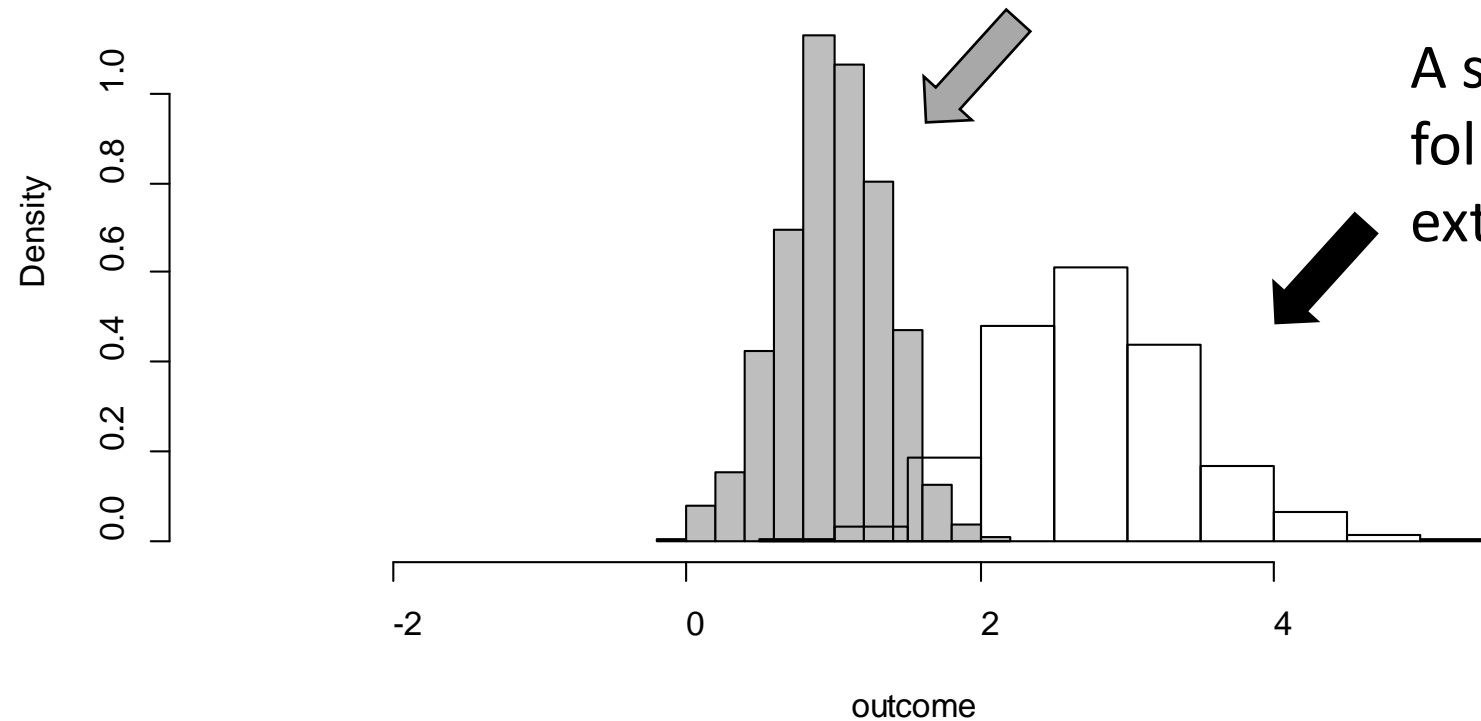


# Use statistical theory for extreme events

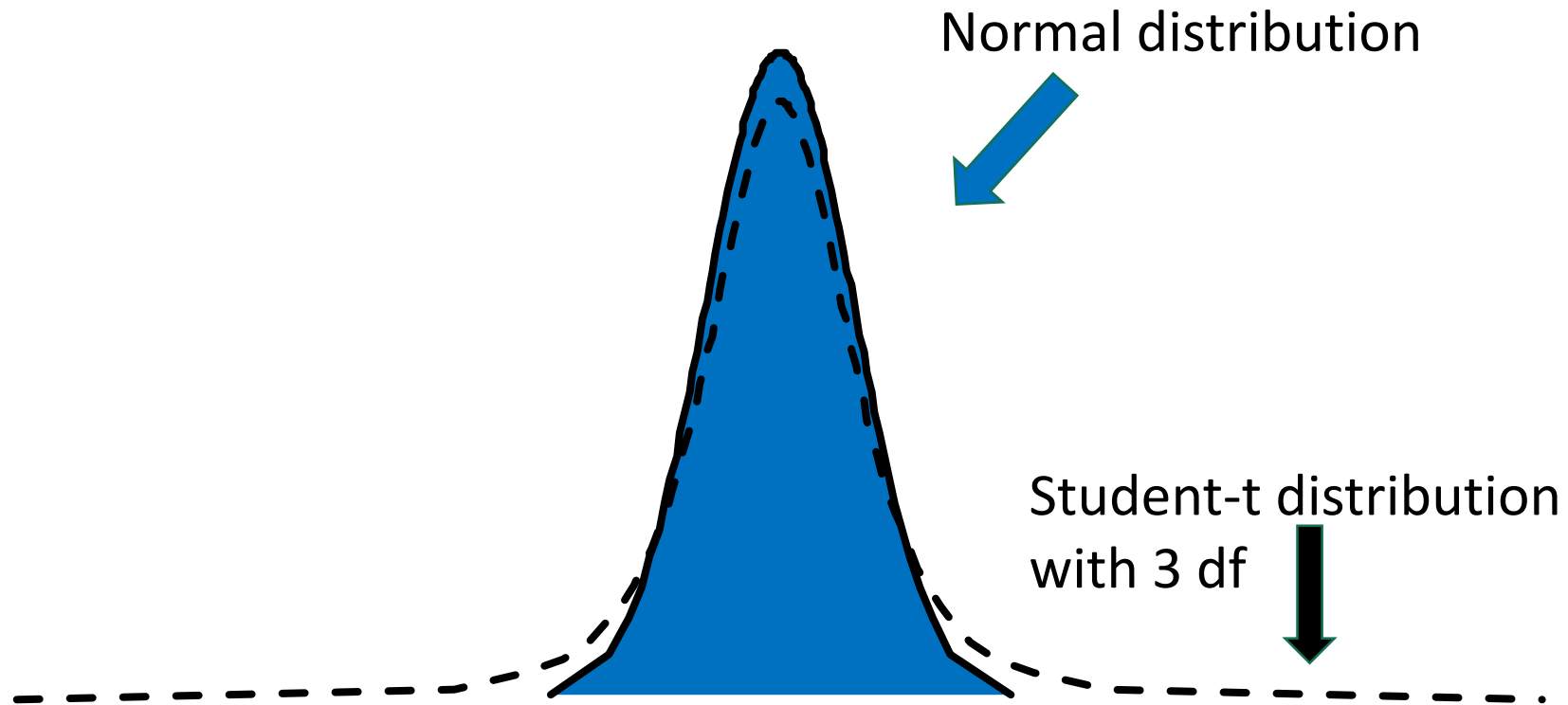
Law of large numbers

A sample of sample means is Normally distributed

A sample of sample extremes follows a Generalised extreme value distribution

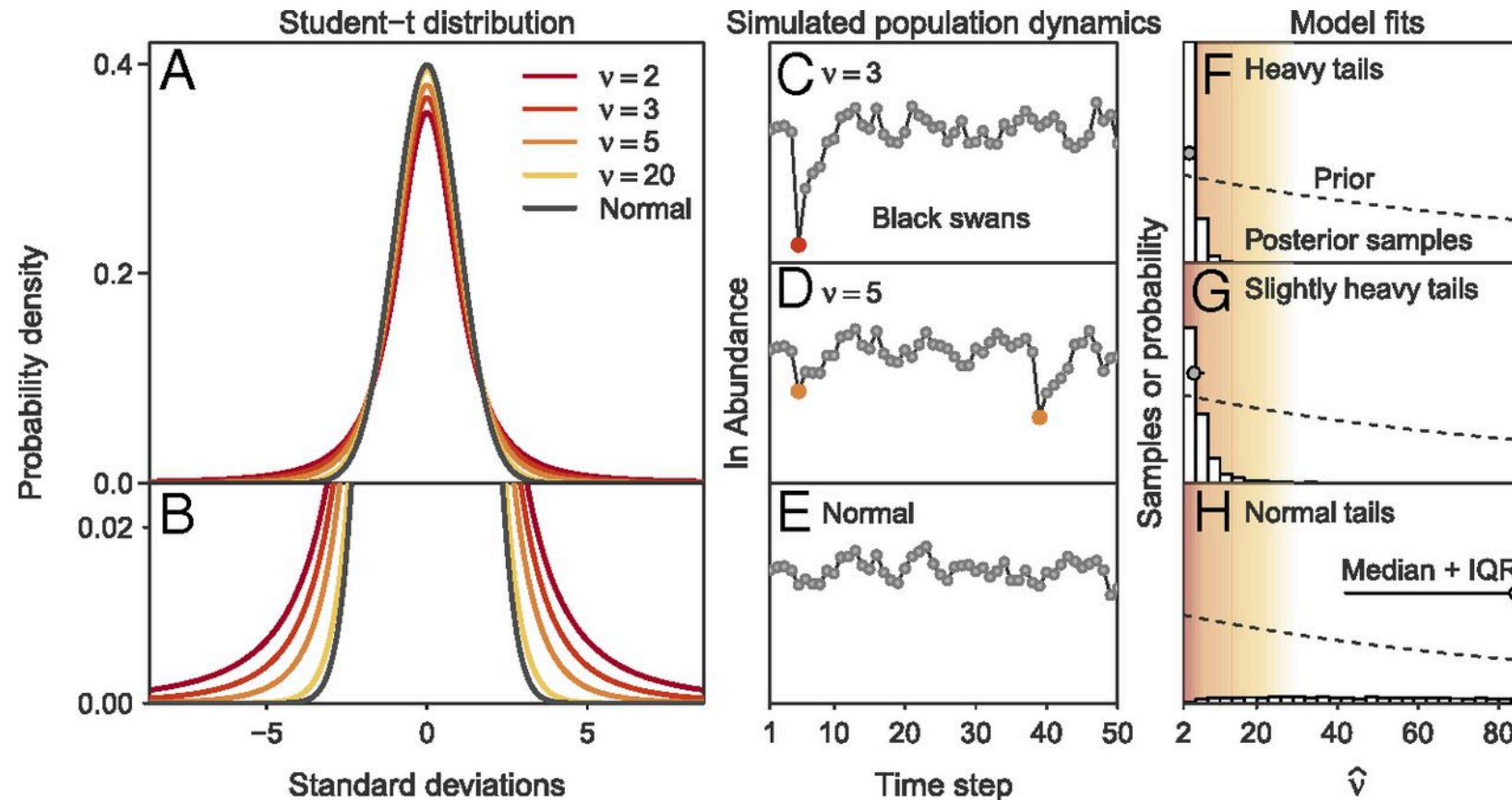


# Include extreme events in random processes





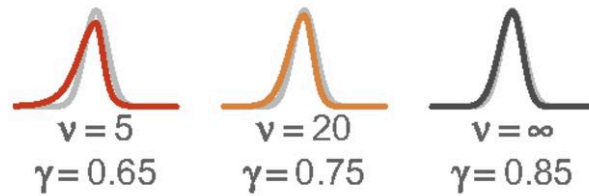
# Illustration of population dynamic models that allow for heavy tails



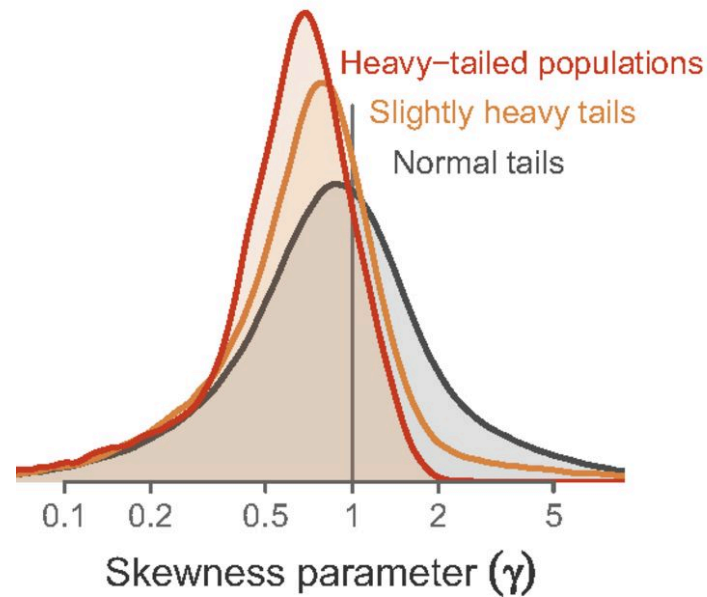
Sean C. Anderson et al. PNAS 2017;114:3252-3257

# Ignoring heavy tails can underestimate risk

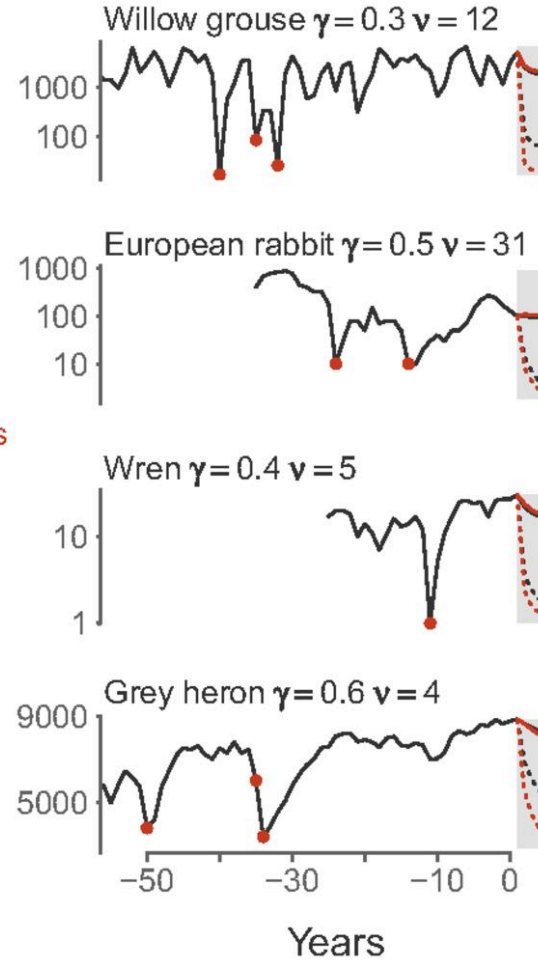
**A** Process deviation shape



**B** Skewness parameter posteriors



**C** Example time series

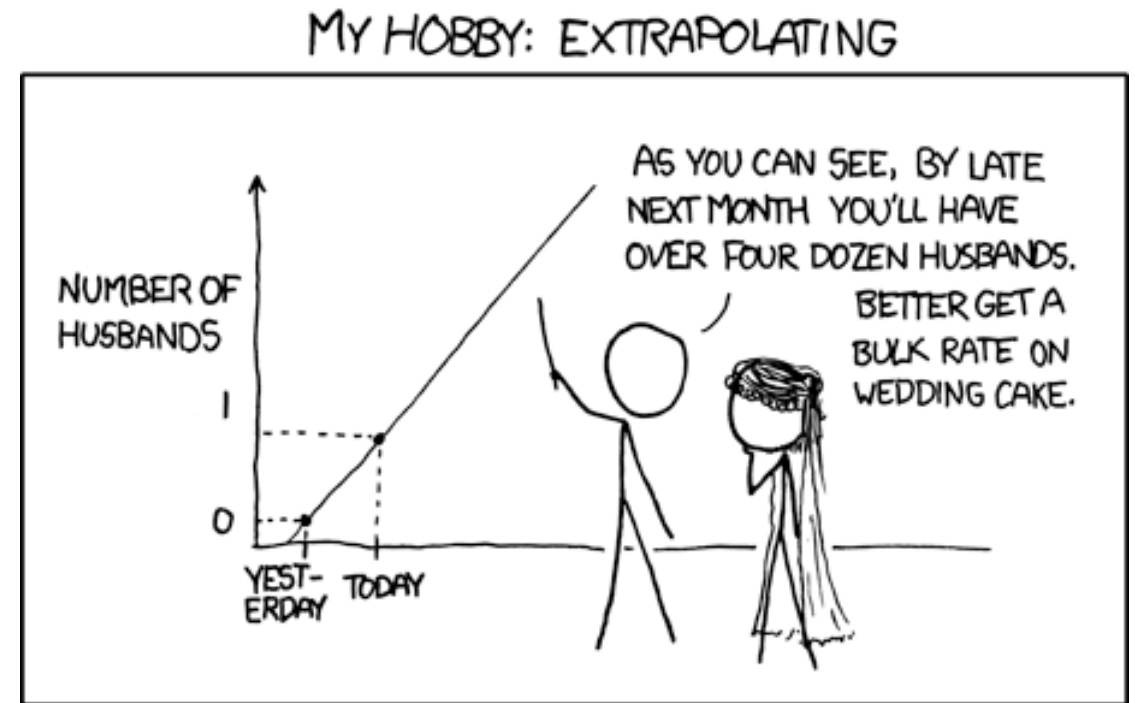


Sean C. Anderson et al. PNAS 2017;114:3252-3257

# Our knowledge is seldom ideal to make decisions

Law of large  
~~small~~ numbers

*I asked four people in the street  
and three were happy.  
75% of people are happy.*



Consider extreme events in the knowledge dimension





# The number of visitors to this lecture

- Statistical population
  - Sample mean: 24

| 29 | 13 | 10 | 22 | 45 |
|----|----|----|----|----|
|    |    |    |    |    |
|    |    |    |    |    |

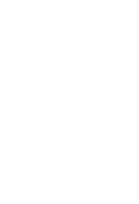




# The number of visitors to this lecture

- Statistical population
  - Sample mean: 24
- Analogy prediction
  - Friday & Maths: 13

| 29     | 13     | 10      | 22      | 45      |
|--------|--------|---------|---------|---------|
| Birds  | Maths  | Birds   | Maths   | Birds   |
| Friday | Friday | Tuesday | Tuesday | Tuesday |

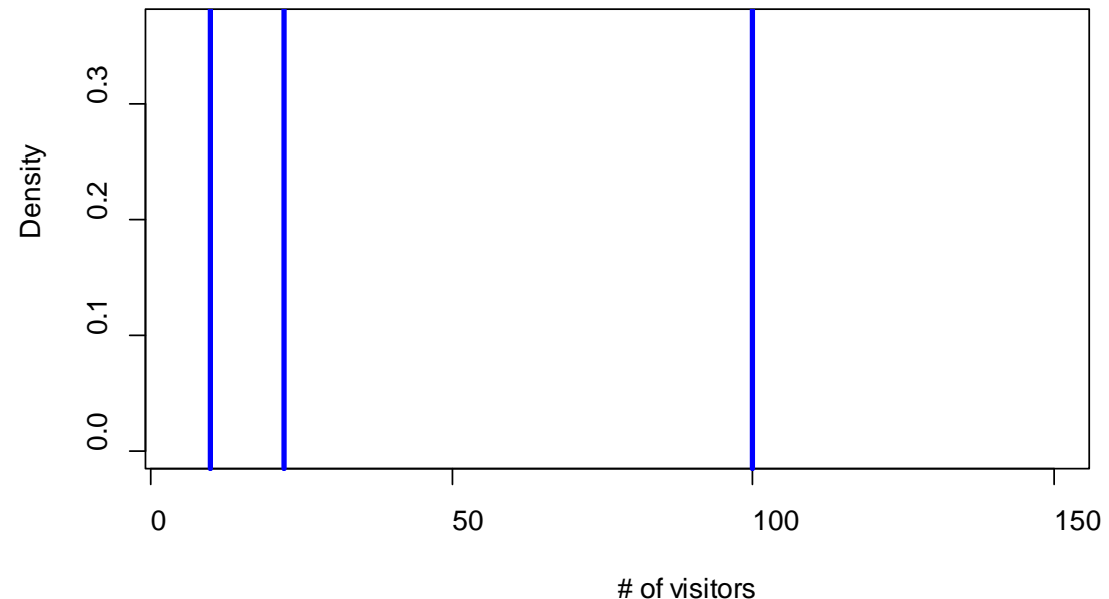




# The number of visitors to this lecture

- Statistical population
  - Sample mean: 24
- Analogy prediction
  - Friday & Maths: 13
- Just guess
  - Lower value: 10
  - Higher value: 100
  - Most likely value: 22

|        |        |         |         |         |
|--------|--------|---------|---------|---------|
| 29     | 13     | 10      | 22      | 45      |
| Birds  | Maths  | Birds   | Maths   | Birds   |
| Friday | Friday | Tuesday | Tuesday | Tuesday |





# The number of visitors to this lecture

- Statistical population

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- Analogy prediction

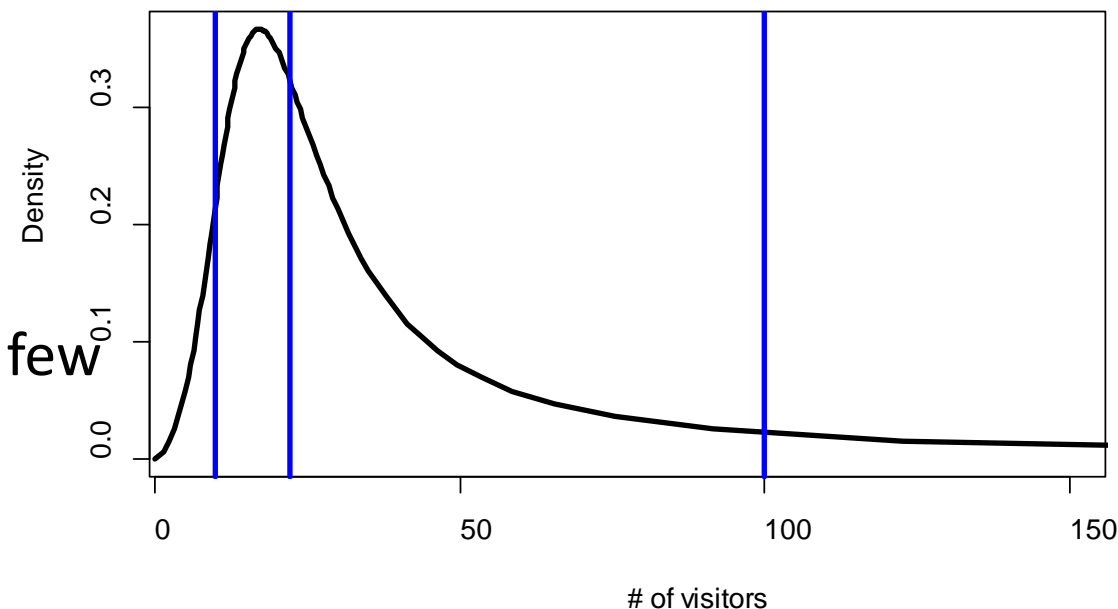
- Friday & Maths: 13

- Just guess

- Lower value: 10
  - Higher value: 100
  - Most likely value: 22
  - 1% chance 200 sets are too few

|        |        |         |         |         |
|--------|--------|---------|---------|---------|
| 29     | 13     | 10      | 22      | 45      |
| Birds  | Maths  | Birds   | Maths   | Birds   |
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LogT(2.84,0.578)



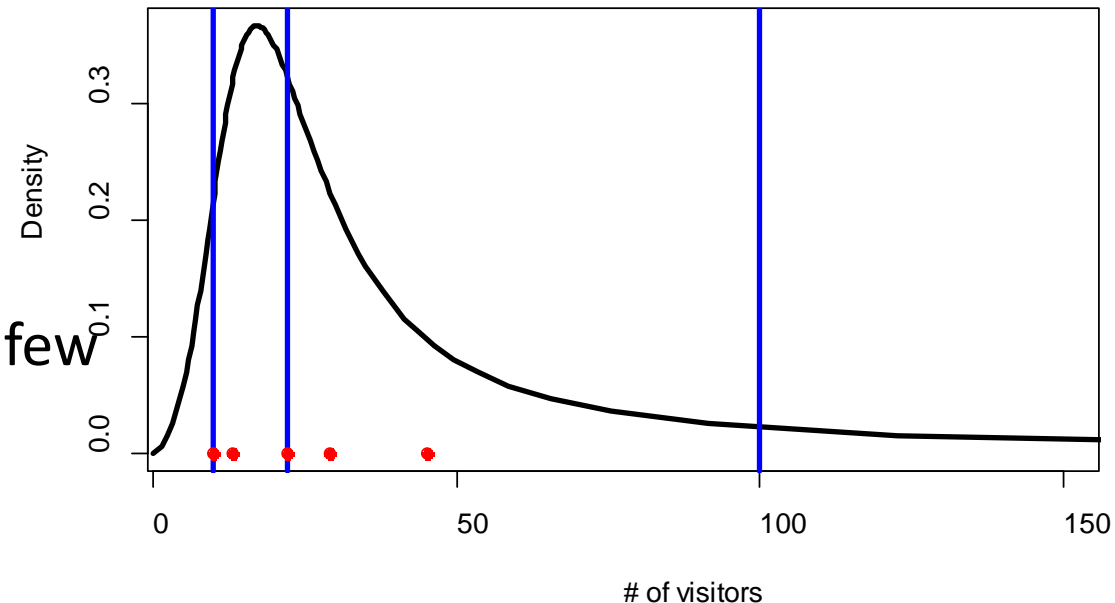


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$\text{LogT}(2.84, 0.578)$



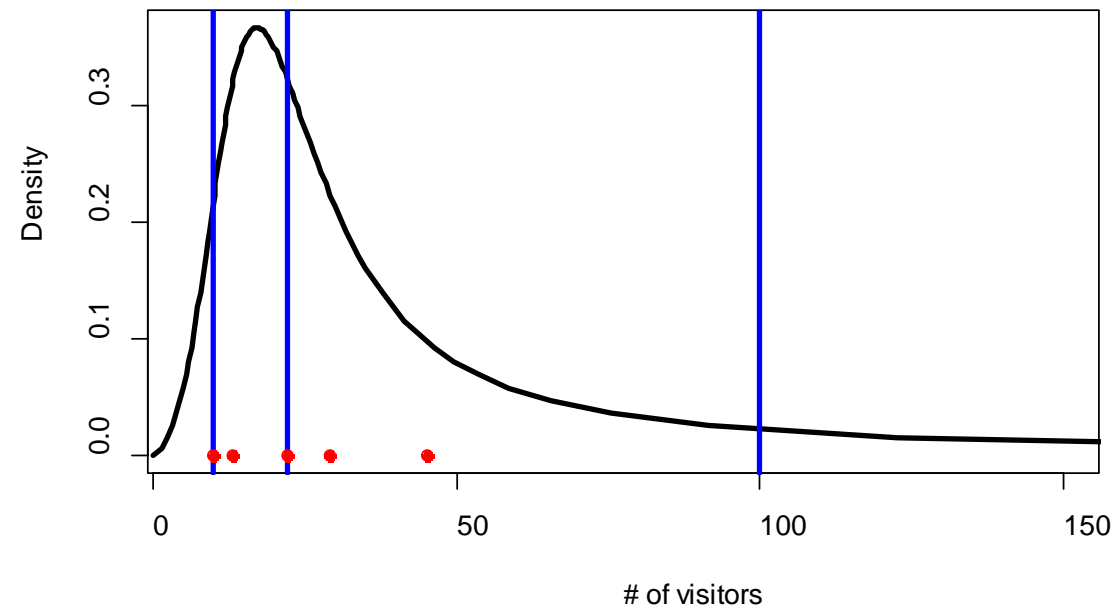


# The number of visitors to this lecture

- Statistical population
  - Sample mean: 24
- Analogy prediction
  - Friday & Maths: 13
- A simple guess
  - Lower value: 10
  - Higher value: 100
  - Most likely value: 22

| 29     | 13     | 10      | 22      | 45      |
|--------|--------|---------|---------|---------|
| Birds  | Maths  | Birds   | Maths   | Birds   |
| Friday | Friday | Tuesday | Tuesday | Tuesday |

$\text{LogT}(2.84, 0.578)$



Relative  
frequency



Personal  
probability



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# Different types of uncertainty

Relative  
frequency



Personal  
probability

## Irreducible uncertainty

- Variability
- Inherent randomness
- Stochasticity
- Aleatory uncertainty



## Reducable uncertainty

- Lack of knowledge
- Ignorance
- Incertitude
- Epistemic uncertainty



# Different types of uncertainty

Relative  
frequency



Personal  
probability

## Decision making under risk

- Maximise prevision taken over a relative frequency
- Risk aversion



## Decision making under uncertainty

- Maximise prevision taken over probability representing our believes (personal probability)
- Cautionary principles



## Decision making under deep uncertainty

- Apply robust decision criteria
- Adapt management
- Precautionary principle



# Different types of uncertainty

**Decision making under  
risk**

**Decision making under  
uncertainty**

**Decision making under  
deep uncertainty**

Strength in knowledge



# Assess strenght in knowledge

Strength in knowledge

**Table 2:** Example of quality indicators for scientific evidence (after Bowden, 2004).

| Indicators of evidence quality |           |   |   |                                       |                                      |  |                     |
|--------------------------------|-----------|---|---|---------------------------------------|--------------------------------------|--|---------------------|
| Quality rank                   |           | Theoretical basis                         | Scientific method   | Auditability                          | Calibration                          | Calibration  | Objectivity         |
|                                | Very high | Well established theory                   | Best available practice: large sample; direct measure                     | Well documented trace to data         | An exact fit to data                 | Independent measurement of sample variable           | No discernable bias |
|                                | High      | Accepted theory; high degree of consensus | Accepted reliable method; small sample; direct measure                    | Poor documented but traceable to data | Good fit to data                     | Independent measurement of high correlation variable | Weak bias           |
|                                | Moderate  | Accepted theory; low consensus            | Accepted method; derived or surrogate data; analogue; limited reliability | Traceable to data with difficulty     | Moderately well correlated with data | Validation measure not truly independent             | Moderate bias       |
|                                | Low       | Preliminary theory                        | Preliminary method of unknown reliability                                 | Weak and obscure link to data         | Weak correlation to data             | Weak indirect validation                             | Strong bias         |
|                                | Very low  | Crude speculation                         | No discernable rigour   | No link back to data                  | No apparent correlation              | No validation presented                              | Obvious bias        |

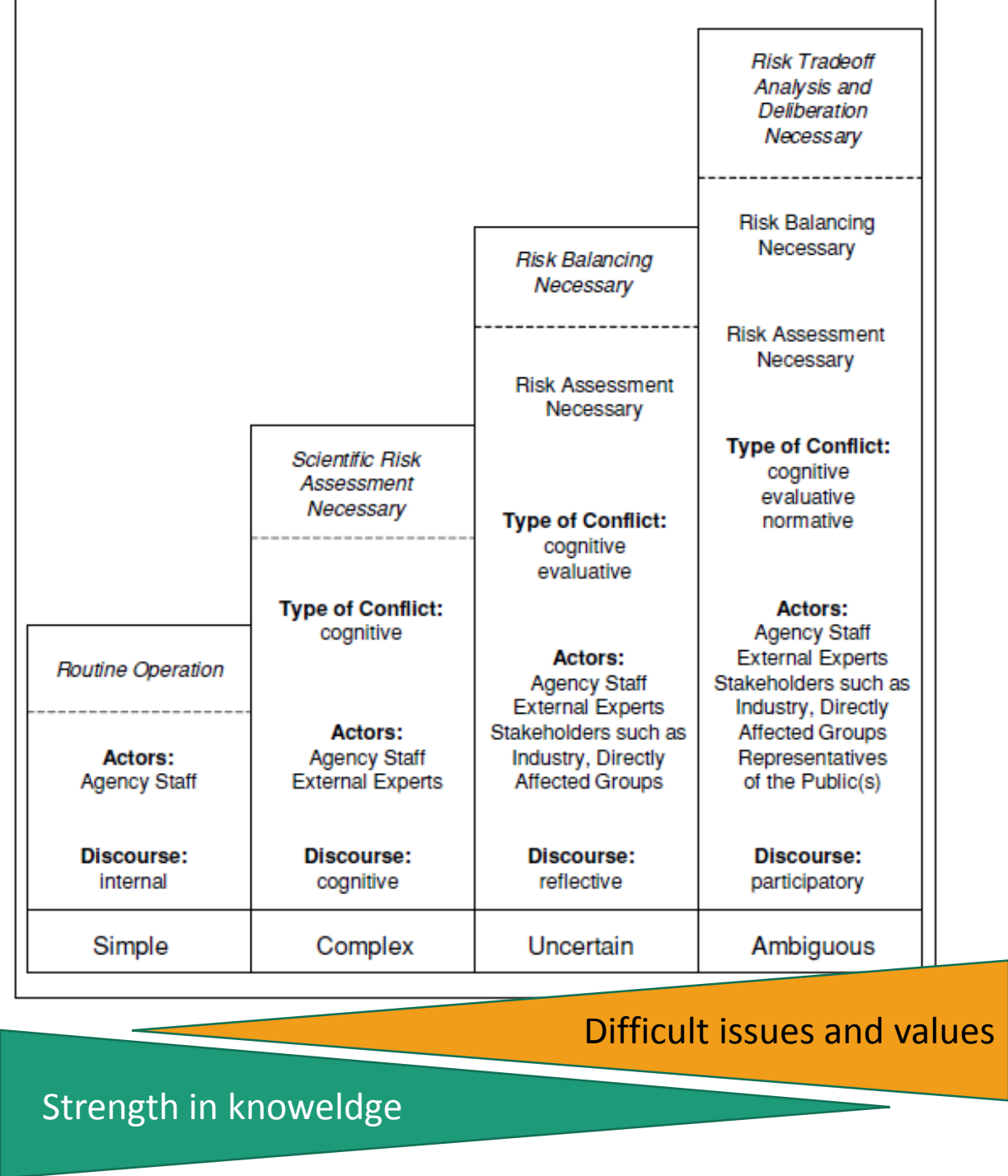




# Adapt management

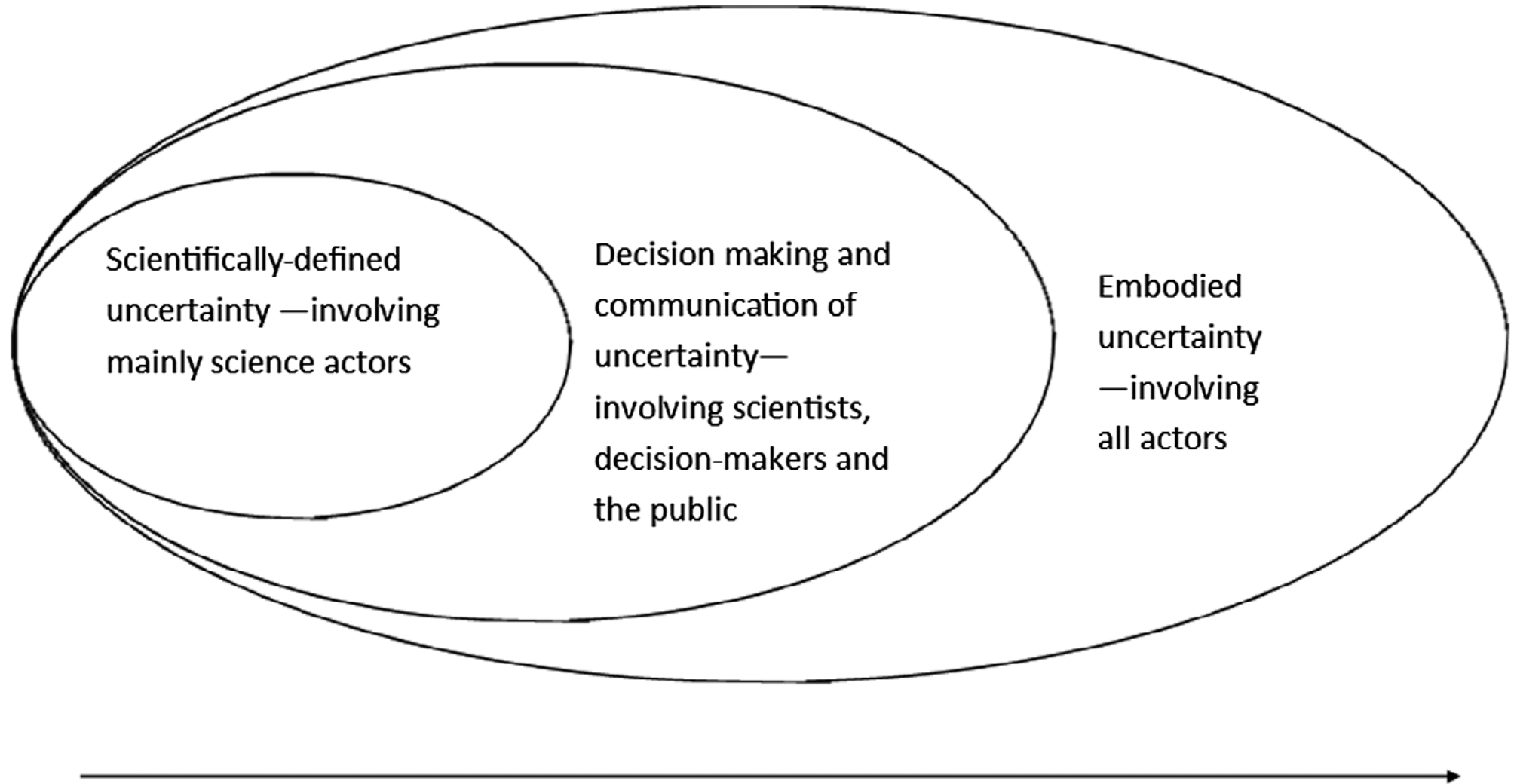


Klinke and Renn. 2002. A new approach to risk evaluation and management: Risk-based, precaution-based, and discourse-based strategies. Risk Analysis.





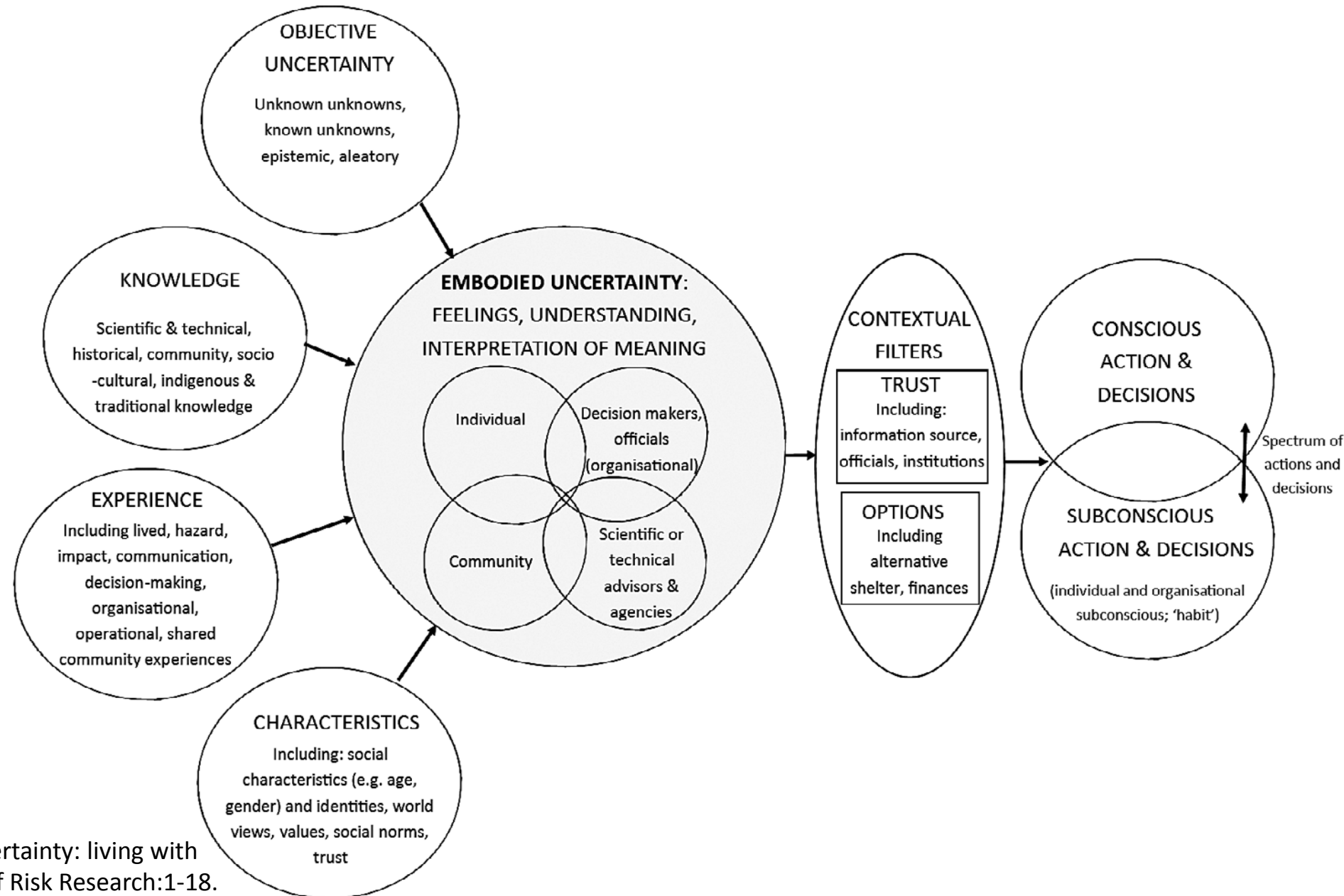
# Broaden the uncertainty concept







# Broaden the uncertainty concept







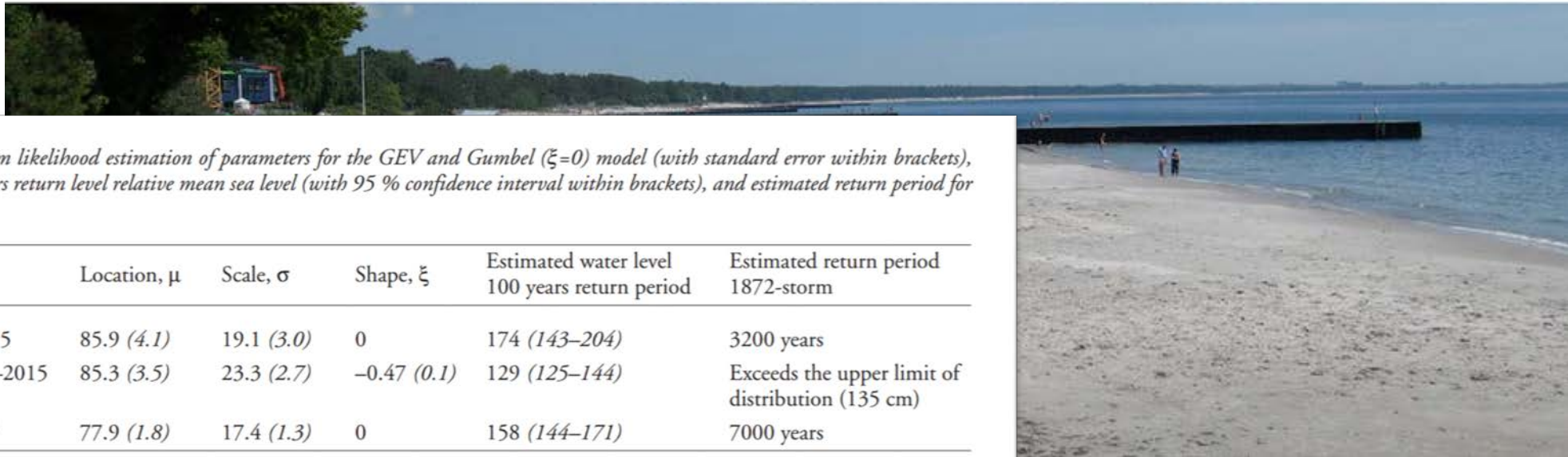


Table 4. Maximum likelihood estimation of parameters for the GEV and Gumbel ( $\xi=0$ ) model (with standard error within brackets), estimated 100-years return level relative mean sea level (with 95 % confidence interval within brackets), and estimated return period for the 1872 storm.

|                     | Location, $\mu$ | Scale, $\sigma$ | Shape, $\xi$ | Estimated water level<br>100 years return period | Estimated return period<br>1872-storm               |
|---------------------|-----------------|-----------------|--------------|--|---|
| Skanör 1992–2015    | 85.9 (4.1)      | 19.1 (3.0)      | 0            | 174 (143–204)                                    | 3200 years  |
| Klagshamn 1961–2015 | 85.3 (3.5)      | 23.3 (2.7)      | −0.47 (0.1)  | 129 (125–144)                                    | Exceeds the upper limit of<br>distribution (135 cm) |
| Ystad 1886–1987     | 77.9 (1.8)      | 17.4 (1.3)      | 0            | 158 (144–171)                                    | 7000 years  |

