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## Improvement of a Uniqueness-and-Anonymity-Preserving User Authentication Scheme for Connected Health Care

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Abstract: Patient's privacy-preserving, security and mutual authentication between patient and the medical server are the important mechanism in connected health care applications, such as telecare medical information systems and personally controlled health records systems. In 2013, Wen showed that Das et al.'s scheme is vulnerable to the replay attack, user impersonation attacks and off-line guessing attacks, and then proposed an improved scheme using biometrics, password and smart card to overcome these weaknesses. However, we show that Wen's scheme is still vulnerable to off-line password guessing attacks, does not provide user's anonymity and perfect forward secrecy. Further, we propose an improved scheme to fix these weaknesses, and use the applied pi calculus based formal verification tool ProVerif to prove the security and authentication.

Keywords: Connected health care. Authentication. Anonymity. Biometrics. Smart card.

## 1. Introduction

The traditional medical records mode is changing due to the rapid development of computer and communication technology. Telecare medical information systems (TMIS) and personally controlled health records systems, the applications of connected health care, have attracted much attention. Take TMIS as example, it maintains the patients' diagnostic records, when a doctor wants to know one patient's anamnesis, he can easily access to TMIS and diagnose quickly, and the repeated physical examination is not needed. TMIS can save the patients' expenses and time. In order to prevent medical records from being damaged or accessed by illegal users, authentication scheme with patient's anonymity-preserving plays an important role in connected health care applications [1,2]. However, some recently proposed user authentication schemes for TMIS can not achieve patient's anonymity [3-7].

In order to provide user's anonymity against an adversary knows user's identity from the authentication process, Das et al. [8] proposed a dynamic ID-based password authentication scheme. But Awashti [9] and Ku-Chang [10] showed that Das et al.'s scheme is vulnerable to password guessing attack and impersonation attack, and can not provide user's anonymity. After that, Wang et al. [11] proposed another improved scheme, but Khan et al. [12] showed that their scheme can not provide user's anonymity and proposed a further improved scheme. Unfortunately, Chen et al. [13] showed that Khan et al.'s scheme can not achieve the user's anonymity and proposed a new dynamic ID-based password authentication scheme using smart card. In 2013, Xie et al. [14] showed that Chen et al.'s scheme does not provide user privacy protection and perfect forward secrecy, is vulnerable to off-line password guessing attack and impersonation attack once an adversary can know all information stored in smart card.

All above mentioned schemes are based on smart card and password, the security is only based on the password. In 2013, Chang et al. [15] proposed a uniqueness-and-anonymity-preserving user authentication scheme for connected health care using biometric, password and smart card. The advantages of using biometric (e.g. irises) are that it can not be guessed, forged, lost and forgotten, and is difficult to copy. Unfortunately, Das et al. [16] showed that their scheme has some weaknesses, such as, is vulnerable to privileged insider attack and manin-the middle attack, and proposed an improved scheme. Wen [17] showed that Das et al.'s scheme is insecure against the replay attack, user impersonation attacks and off-line guessing attacks, and presented the further improved scheme. Very recently, Tsai et al. [18] and Tan [19] also proposed biometric, password and smart card based user anonymous authentication schemes.

In this paper, we show that a uniqueness-and-anonymity-preserving user authentication scheme for connected health care proposed by Wen [17] does not provide user anonymity and perfect forward secrecy, is vulnerable to off-line password guessing attack. Then we propose a new scheme to solve their security weaknesses.

The rest of the paper is organized as follows. In Sections 2 and 3, we review and cryptanalysis of Wen's scheme. An improved scheme is proposed in Section 4. After that, we present security analysis and formal verification in Sections 5

and 6. In Section 7, we present the performance evaluation, and conclude the paper in Section 8.

#### 2. Review of Wen's Scheme

In this section, we only review the first two phases of Wen's scheme, which consists of registration, login and verification, password change phases. The following notation will be used in this paper:

 $U_i$ : The user

 $ID_i$ :  $U_i$ 's identity.

 $PW_i$ :  $U_i$ 's password.

 $S_i$ : A trustworthy server.

 $B_i$ : Personal biometrics of  $U_i$ .

 $C_i$ : Smart card of  $U_i$ .

 $X_s$ : Secret key of  $S_j$ .

K: Secret number of  $U_i$ .

 $NID_i$ : A random identity chosen by  $S_i$  for  $U_i$ .

 $h(\cdot)$ : A secure collision-free one-way hash function.

 $H(\cdot)$ :BioHashing.

⊕: The bitwise XOR operation.

||:The concatenation operation.

 $E_{\nu}()/D_{\nu}()$ : The symmetric encryption and decryption algorithms with key k.

#### 2.1 Registration phase

In registration phase,  $U_i$  and  $S_i$  perform the following steps:

Step 1:  $U_i$  chooses a random number K, his identity  $ID_i$ , password  $PW_i$  and enters his biometrics  $B_i$  on a specific device, and computes

$$f_i = H(ID_i || PW_i || B_i), RPW_i = h(ID_i || K || PW_i).$$

Then he sends  $\{ID_i, f_i, RPW_i\}$  to  $S_i$  via a secure channel.

Step 2: After receiving the message  $\{ID_i, f_i, RPW_i\}$  from  $U_i, S_j$  chooses a random identity  $NID_i$  for  $U_i$  and computes

$$e_i = h(ID_i \parallel X_s) \oplus h(RPW_i \parallel f_i), TD_i = NID_i \oplus h(ID_i \parallel RPWi), D_i = TD_i,$$

where  $X_s$  is a secret key of  $S_j$ .  $S_j$  generates a counter  $ctr_{U_i} = 0$  and creates a

record  $(ID_i, NID_i, ctr_{U_i})$  for  $U_i$  in its database.

Step 3:  $S_j$  issues a smart card  $C_i$  to  $U_i$  via a secure channel, which contains  $\{TD_i, D_i, h(\cdot), H(\cdot), ctr_{U_i}, f_i, e_i\}$ .

After receiving the smart card  $C_i$ ,  $U_i$  stores K in the smart card.

#### 2.2 Login and authentication phase

When a legal user  $U_i$  wants to login  $S_j$ , they need perform the following steps. In order to resist DoS attack, Wen's scheme has two cases according to whether the latest identities kept by  $C_i$  and  $S_j$  are matched or not.

Step 1:  $U_i$  inserts his smart card  $C_i$  into a card reader, and inputs his biometrics  $B_i$ ,  $ID_i$ ,  $PW_i$ ,  $C_i$  computes  $H(ID_i || PW_i || B_i)$  and verifies whether it equals to  $f_i$  or not. If not, terminates. Otherwise,  $U_i$  executes the following two cases.

Case I: the latest identities kept by  $C_i$  and  $S_i$  are matched.

Step 2:  $C_i$  selects a random nonce  $R_c$  and computes

$$RPW_{i} = h(ID_{i} || K || PW_{i}),$$

$$NID_{i} = h(ID_{i} || RPW_{i}) \oplus D_{i},$$

$$M_{1} = e_{i} \oplus h(RPW_{i} || f_{i}) = h(ID_{i} || X_{s}),$$

$$M_{2} = E_{M_{1}}(R_{c}),$$

$$ctr'_{U_{i}} = ctr_{U_{i}} + 1,$$

$$M_{3} = h(ID_{i} || R_{c} || ctr'_{U_{i}}).$$

Then,  $C_i$  sends  $\left\{ctr'_{U_i}, NID'_i, M_2, M_3\right\}$  to  $S_j$ .

Step 3: After receiving  $\{ctr'_{U_i}, NID'_i, M_2, M_3\}$  from  $U_i, S_j$  checks the format of  $NID_i$  and finds the  $NID_i$ ,  $ID_i$  and  $ctr_{U_i}$  in the database. If  $NID_i$  is found, does Step 4; Otherwise,  $S_i$  does the Step7 in Case II.

Step 4:  $S_j$  computes  $M_4 = h(ID_i \parallel X_s)$ ,  $M_5 = D_{M_4}(M_2) = R_c$  and  $ctr'_{U_i} = ctr_{U_i} + 1$ , and then verifies if  $h(ID_i \parallel M_5 \parallel ctr'_{U_i}) = M_3$  and  $ctr'_{U_i} > ctr_{U_i}$ . If not,  $S_j$  rejects it. Otherwise,  $S_j$  chooses a random nonce  $R_s$  and  $NID_i^{new}$ , computes  $M_6 = E_{M_4}(R_s)$ ,  $M_7 = h(R_s \parallel M_5) \oplus NID_i^{new} = h(R_s \parallel R_c) \oplus NID_i^{new}$ ,  $M_8 = h(M_4 \parallel M_5 \parallel R_s \parallel ID_i \parallel NID_i^{new})$ , and sends  $\{M_6, M_7, M_8\}$  to  $C_i$ .

Step 5:  $C_i$  computes  $M_9 = D_{M_1}(M_6) = R_s$ ,  $NID_i^{new} = M_7 \oplus h(M_9 \parallel R_c)$ , and verifies whether  $M_8 = h(M_1 \parallel R_c \parallel M_9 \parallel ID_i \parallel NID_i^{new})$  or not. If not, terminates. Otherwise,  $C_i$  updates  $TD_i$  and  $D_i$  with  $D_i$  and  $D_i \oplus NID_i^{new} \oplus NID_i^{new}$ , respectively. Then  $C_i$  computes and sends  $M_{10} = h((M_9 + 1) \parallel ID_i \parallel NID_i^{new} \parallel (R_c + 1))$  to  $S_j$ .  $C_i$  also computes the session key  $SK_{U_i,S_i} = h(ID_i \parallel R_c \parallel M_9 \parallel M_2 \parallel M_1)$ .

Step 6:  $S_j$  computes  $h((R_s + 1) || ID_i || NID_i^{new} || (M_5 + 1))$  and checks if it equals to  $M_{10}$ . If not, terminates. Otherwise,  $S_j$  updates  $(NID_i, ctr_{U_i})$  with  $(NID_i^{new}, ctr_{U_i} + 1)$  in its database and  $S_j$  computes the session key  $SK_{U_i,S_j} = h(ID_i || M_5 || R_s || M_2 || M_4)$ .

Thus, both  $U_i$  and  $S_i$  share the same session key

$$SK_{U_{i,S_{s}}} = h(ID_{i} || R_{c} || R_{s} || M_{2} || h(ID_{i} || X_{s})).$$

Case II: the latest random identities kept by  $C_i$  and  $S_i$  are distinct.

Step 7: All steps in this case are almost the same as those in **Case I** except  $NID_i' = h(ID_i || RPW_i) \oplus TD_i$  in Step2, and  $C_i$  needs to update  $D_i$  with  $D_i \oplus NID_i' \oplus NID_i^{new}$  without changing  $TD_i$  in Step5.

## 3. Weaknesses of Wen's Scheme

In this section, we show that Wen's scheme has some weaknesses, the details are as follows.

#### 3.1 Off-line password guessing attack

Wen claimed that their scheme can resist off-line password guessing attack even if an adversary can know all information  $\{TD_i, D_i, h(\cdot), H(\cdot), ctr_{U_i}, f_i, e_i, K\}$  stored in smart card. However, the adversary can get the transmitted messages  $\{ctr_{U_i}, NID_i, M_2, M_3\}$  in public channel, and can guess  $\{ID_i, PW_i\}$  and compute  $RPW_i' = h(ID_i' || K || PW_i') ,$ the adversary if thus can check  $TD_i \oplus h(ID_i' || RPW_i') = NID_i'$ . If yes, the guessed  $\{ID_i', PW_i'\}$  are correct. Otherwise, the adversary can guess another identity and password and tries again. Since the identity and password is short and easy to remember, in particular, the adversary can easy to obtain the user's identity as an insider attacker, therefore, this attack is valid.

On the other hand, the adversary can also compute

$$M_1' = (h(ID_i \parallel X_s))' = e_i \oplus h(RPW_i' \parallel f_i),$$
  
$$(R_c)' = D_{M_i} \cdot (M_2),$$

and can also check if  $M_3 = h(ID_i' || R_c' || ctr'_{U_i})$ . If yes, the guessed  $\{ID_i', PW_i'\}$  are correct. Otherwise, the adversary guesses another identity and password and tries again.

Therefore, Wen's scheme is vulnerable to off-line password guessing attacks. Thus, the adversary can impersonate the user easily.

#### 3.2 Lack of perfect forward secrecy

In Wen's scheme, the session key is  $SK_{U_i,S_j} = h(ID_i \parallel R_c \parallel R_s \parallel M_2 \parallel h(ID_i \parallel X_s))$ . Therefore, if an adversary can know all long-term secret information, e.g., the server's secret key  $X_s$  and user's identity  $ID_i$ , and can get all transmitted messages  $\left\{ctr_{U_i}, NID_i, M_2, M_3\right\}$ ,  $\left\{M_6, M_7, M_8\right\}$  in public channel, then he can compute  $M_1 = h(ID_i \parallel X_s)$ ,  $R_c = D_{M_1}(M_2)$ ,  $R_s = D_{M_1}(M_6)$ . Thus, the adversary can know the session key  $SK_{U_i,S_j} = h(ID_i \parallel R_c \parallel R_s \parallel M_2 \parallel h(ID_i \parallel X_s))$ , and can know all transmitted messages encrypted by  $SK_{U_i,S_j}$ .

#### 3.3 Lack of user's anonymity

Wen claimed that his scheme can achieve  $U_i$ 's anonymity by using the random identity  $NID_i$ . However, Since  $(ID_i, NID_i, ctr_{Ui})$  are stored in account table in plaintext. Therefore, if an adversary can access to account table (or steal the account table), and have obtained the login message  $\{ctr_{U_i}, NID_i, M_2, M_3\}$  from the public network. Then, the adversary can lookup  $ID_i$  in account table and can know the  $U_i$ 's identity.

## 4. The Proposed Scheme

The proposed scheme also consists of three phases: registration, login and verification, password change phases. Let h() be a one-way collision resistant cryptographic hash function which maps to an integer, E be an elliptic curve defined over a finite field with large order n and P be a generator on E with large order n. The details of our scheme are as follows.

#### 4.1 Registration

In this phase, the patient  $U_i$  and the medical server  $S_i$  perform the following steps.

Step 1:  $U_i$  chooses his identity  $ID_i$  and password  $PW_i$ , scans and enters his personal biometrics  $B_i$ . It is worth mentioning that no one can get  $B_i$  except  $U_i$ , and the biometrics scanner can be combined in the smart card reader. Then  $U_i$  computes  $RPW_i = h(B_i || ID_i || PW_i)$  and  $f_i = h(RPW_i)$ , and sends  $ID_i$  to  $S_j$  via a secure channel.

Step 2: After receiving the message  $ID_i$ ,  $S_j$  checks the validity of  $ID_i$  and chooses a random identity  $NID_{ij}$  and computes  $e_i = h(ID_i || X_s)$ , where  $X_s$  is a secret number kept by  $S_j$ .  $S_j$  computes  $y_i = E_{X_s}(ID_i, ctr_{U_i})$  for  $U_i$  and creates a record  $(NID_{ij}, y_i)$  in its database, where  $ctr_{U_i} = 0$ .

Step 3: Finally,  $S_j$  stores  $\{NID_{ij}, P, h(\cdot), ctr_{U_i}, e_i\}$  into a smart card and sends it to  $U_i$  via a secure channel.

Step 4: After receiving the smart card,  $U_i$  computes

$$TID_i = RPW_i \oplus e_i = h(B_i \parallel ID_i \parallel PW_i) \oplus h(ID_i \parallel X_s)$$
,

and stores  $f_i$  into the smart card, change  $e_i$  with  $TID_i$ . That is, the smart card contains  $\{NID_{ij}, P, h(\cdot), ctr_{U_i}, f_i, TID_i\}$ .

#### 4.2 Login and Verification

When  $U_i$  wants to logon to the TMIS system, he inserts his smart card into a device, inputs his  $ID_i$ , password  $PW_i$  and biometrics  $B_i$ , then the smart card performs the following steps. Figure 1 illustrates this phase.

Step 1: Smart card computes  $RPW_i = h(B_i || ID_i || PW_i)$  and checks if  $f_i = h(RPW_i)$ . If not,  $U_i$  inputs his  $ID_i$ , password  $PW_i$  and biometrics  $B_i$  again. Otherwise, it generates a random number a, computes

$$\begin{split} e_i &= RPW_i \oplus TID_i = h(ID_i \parallel X_s), \\ r_1 &= aP, \\ ctr'_{U_i} &= ctr_{U_i} + 1 \\ M_1 &= E_{e_i}(r_1 \parallel ctr'_{U_i}), \\ M_2 &= h(ID_i \parallel r_1 \parallel ctr'_{U_i} \parallel NID_{ii}). \end{split}$$

Then, smart card sends  $\{M_1, M_2, ctr'_{U_i}, NID_{ii}\}$  to  $S_i$ .

Step 2: After receiving the message  $\{M_1, M_2, ctr'_{U_i}, NID_{ij}\}$ ,  $S_j$  checks  $NID_{ij}$  in database and finds  $y_i$ , computes

$$D_{X_i}(y_i) = \{ID_i, ctr_{U_i}\},$$

$$h(ID_i \parallel X_s)$$
 , 
$$D_{h(ID_i \parallel X_s)}(M_1) = \{r_1, ctr'_{U_i}\},$$

and checks if  $ctr'_{v_i} > ctr_{U_i}$ . If not, terminates it. Otherwise,  $S_j$  computes  $h(ID_i || r_i || ctr'_{U_i} || NID_{ij})$  and checks if it equals to  $M_2$ . If not, rejects it. Otherwise,  $S_j$  generates a random number b, a random identity  $NID_{ij}$ , and computes

$$r_{2} = bP,$$
 $r = br_{1} = baP,$ 
 $M_{3} = h(r_{1} || r) \oplus NID_{ij}'$ 
 $M_{4} = h(r_{2} || r_{1} || r || NID_{ij}')$ 

Then,  $S_i$  sends  $\{M_3, M_4, r_2\}$  to  $U_i$ .

Step 3: When  $U_i$  receives  $\{M_3, M_4, r_2\}$ , he computes

$$r = ar_2 = baP, \ NID_{ij}' = h(r_1 || r) \oplus M_3,$$

and  $h(r_2 || r_1 || r || NID_{ij})$ , then checks if  $h(r_2 || r_1 || r || NID_{ij})$  equals to  $M_4$ . If not, terminates it. Otherwise, he computes  $M_5 = h(NID_{ij})||r|$  and the session key  $SK = h(r_2 || r_1 || r || ctr_{U_i})$ , updates  $(NID_{ij}, ctr_{U_i})$  with  $(NID_{ij}, ctr_{U_i})$  in smart card. Finally,  $U_i$  sends  $M_5$  to  $S_i$ .

Step 4: After receiving the message  $M_5$ ,  $S_j$  checks the validity of  $M_5$ , if not,  $S_j$  sends  $M_6 = E_{h(ID_i||X_S)}(M_5 \text{ is not correct})$  and terminates it. Otherwise,  $S_j$  computes the session key  $SK = h(r_2 || r_1 || r || ctr'_{U_i})$ ,  $y_i' = E_{X_s}(ID_i, ctr'_{U_i})$  and updates the record  $(NID_{ij}, y_i')$  of  $U_i$ , where  $NID_{ij} = NID_{ij}'$ .

If  $U_i$  receives  $M_6$ , he has to re-authenticate with  $S_j$  and does not update  $(NID_{ii}, ctr_{U_i})$  in his smart card.

#### 4.3 Password change

When  $U_i$  wants to change his password, he inserts his smart card into a device, inputs his old password  $PW_i$  and new password  $PW_i^{new}$ , his  $ID_i$  and  $B_i$ , then the smart card first checks the correctness of  $RPW_i = h(B_i \parallel ID_i \parallel PW_i)$  by  $f_i = h(RPW_i)$ , then computes

```
\begin{split} e_i &= RPW_i \oplus TID_i = h(ID_i \parallel X_s) \;, \\ RPW_i^{new} &= h(B_i \parallel ID_i \parallel PW_i^{new}) \;, \\ f_i^{new} &= h(RPW_i^{new}) \;, \\ TID_i^{new} &= RPW_i^{new} \oplus e_i = h(B_i \parallel ID_i \parallel PW_i^{new}) \oplus h(ID_i \parallel X_s) \;, \end{split}
```

and updates  $f_i$  and  $TID_i$  with  $f_i^{new}$  and  $TID_i^{new}$ .

Fig. 1 Login and authentication phase of the proposed scheme.

```
U
  RPW_i = h(B_i || ID_i || PW_i)
  f_i = h(RPW_i)
  e_i = RPW_i \oplus TID_i = h(ID_i \parallel X_s)
  ctr'_{U_i} = ctr_{U_i} + 1
  M_1 = E_{e_i}(r_1 \parallel ctr'_{U_i})
  M_2 = h(ID_i \parallel r_1 \parallel ctr'_{U_i} \parallel NID_{ij})
                                                                                            Check NID_{ii}, find y_i
                                                                                            D_{X_s}(y_i) = \{ID_i, ctr_{U_i}\}
                                                                                            h(ID_i \parallel X_s)
                                                                                            D_{h(ID_i||Xs|)}(M_1) = \{r_1, ctr'_{U_i}\}
                                                                                            check ctr'_{U_i} > ctr_{U_i}
                                                                                            h(ID_i \parallel r_1 \parallel ctr'_{U_i} \parallel NID_{ii}) \stackrel{?}{=} M_2
                                                                                            r_2 = bP, r = br_1 = baP
                                                                                            M_3 = h(r_1 || r) \oplus NID_{ii}
                                                                                            M_4 = h(r_2 || r_1 || r || NID_{ij}')
                                                         \{M_3, M_4, r_2\}
r = ar_2 = baP
NID_{ij}' = h(r_1 \parallel r) \oplus M_3
h(r_2 \parallel r_1 \parallel r \parallel NID_{ij}') \stackrel{?}{=} M_4
M_5 = h(NID_{ij} ' || r)
SK = h(r_2 \parallel r_1 \parallel r \parallel ctr'_{U_i})
                                                                                       Verify M_4
                                                                                       SK = h(r_2 \parallel r_1 \parallel r \parallel ctr'_{U_i})
                                   The session key is SK = h(r_2 || r_1 || r || ctr'_{U_i})
```

## 5. Security Analysis

In this section, we show that the proposed scheme can resist various attacks.

#### 5.1 Patient's privacy protection

If an adversary can get all information  $\{NID_{ij}, P, h(\cdot), ctr_{U_i}, f_i, TID_i\}$  stored in smart card, and all transmitted messages  $\{M_1, M_2, ctr'_{U_i}, NID_{ij}\}$ ,  $\{M_3, M_4, r_2\}$  and  $M_5$  in public channel, and he wants to know the patient  $U_i$ 's identity  $ID_i$ . Since the adversary can not know  $U_i$ 's biometrics  $B_i$ , so he can not know  $ID_i$  by guessing  $\{ID_i, PW_i, B_i\}$  and checking whether  $f_i = h(h(B_i || ID_i || PW_i))$  or not.

On the other hand, the adversary can not identify  $ID_i$  from  $M_2 = h(ID_i || r_1 || ctr'_{U_i} || NID_{ij})$  and  $y_i = E_{X_s}(ID_i, ctr_{U_i})$  without knowing  $r_1$  and the medical server  $S_j$ 's secret key  $X_s$ , even if he can get account table in server's database, as we know, the random identity of  $U_i$  is changed in each session run.

Therefore, our scheme provides patient's anonymity and untraceability.

#### **5.2 Off-line password guessing attack**

If an adversary can get all information  $\{NID_{ij}, P, h(\cdot), ctr_{U_i}, f_i, TID_i\}$  stored in smart card, and all transmitted messages  $\{M_1, M_2, ctr'_{U_i}, NID_{ij}\}$ ,  $\{M_3, M_4, r_2\}$  and  $M_5$  in public channel, and he wants to launch off-line password guessing attack. However, the adversary can not compute  $RPW_i = h(B_i \parallel ID_i \parallel PW_i)$  for guessed  $ID_i$  and password  $PW_i$  without knowing  $U_i$ 's biometrics  $B_i$ , and can not check if  $f_i = h(RPW_i)$ . On the other hand, the transmitted messages do not conducive to the adversary to guess the password because he can not compute  $RPW_i$ .

So our scheme can resist off-line password guessing attack.

#### 5.3 Replay attacks

If an adversary replays  $\{M_1, M_2, ctr'_{U_i}, NID_{ij}\}$  to  $S_j$ ,  $S_j$  will detect that  $ctr'_{U_i} > ctr_{U_i}$  is not hold; if the adversary changes  $ctr'_{U_i}$  to  $ctr'_{U_i} + 1$ , then  $M_2 = h(ID_i \parallel r_1 \parallel ctr'_{U_i} \parallel NID_{ij})$  will not hold.

If an adversary replays  $\{M_3, M_4, r_2\}$  to  $U_i$ ,  $U_i$  will find that  $M_4 = h(r_2 || r_1 || r || NID_{ii})$  will not hold because  $r_1$  is changed in each session run.

#### 5.4 Impersonation attacks

If an adversary gets all information stored in smart card and all transmitted messages in public channel, and impersonates the patient to pass through the authentication process of  $S_j$ . Because he does not know the  $U_i$ 's biometrics  $B_i$  and can not compute  $RPW_i$  from  $f_i = h(RPW_i)$ , so he can not know  $e_i = RPW_i \oplus TID_i = h(ID_i \parallel X_s)$  and compute  $M_1' = E_{e_i}(r_1' \parallel ctr'_{U_i})$ , where  $r_1' = a'P$  for randomly chosen a'. Therefore, the login message  $\{M_1', M_2', ctr'_{U_i}, NID_{ij}\}$  will not pass the authentication process of  $S_j$ , where  $M_2' = h(ID_i \parallel r_1' \parallel ctr'_{U_i} \parallel NID_{ij})$ .

If an adversary wants to impersonate the medical server  $S_j$ , however, he can not decrypt  $M_1$  to obtain  $r_i$  without knowing  $S_j$ 's secret key  $X_s$ , and can not compute  $r = br_1 = baP$ , and the valid  $M_4 = h(r_2 || r_1 || r || NID_{ij}')$  to pass through the authentication of  $U_i$ .

#### 5.5 Verification table stolen attack

If an adversary can get account table  $(NID_{ij}, y_i) = (NID_{ij}, E_{X_s}(ID_i, ctr_{U_i}))$ , however, it is no use, since  $ID_i$  is encrypted by the medical server  $S_i$ 's secret key  $X_s$ .

#### 5.6 Perfect forward secrecy and known key security

In the proposed scheme, the session key is  $SK = h(r_2 || r_1 || r || ctr'_{U_i})$ , where  $r_1 = aP$ ,  $r_2 = bP$  and r = abP. Since a and b are random nonces chosen by  $U_i$  and  $S_j$ , respectively, which are changed in each session run. Therefore, if the adversary can know  $\{X_s, ID_i, PW_i\}$ , then he can know  $r_1$ , but he can not compute r from  $r_1$  and  $r_2$  due to the intractability of CDH problem, so our scheme provides perfect forward secrecy.

Since all the session keys are independent and dependent on random nonces a and b, so an adversary can not compute other session keys when he knows one session key.

## 6. Formal Verification

In this section, we use formal verification tool ProVerif [20], which is based on applied pi calculus [21] to prove the session key secrecy and authentication, instead of the formal security proof. Since the formal security proof is presented by artificial structure, and the errors may not easy to be found; while ProVerif is performed automatically, and the errors can be detected easily. On the other hand, it supports many cryptographic primitives such as symmetric and asymmetric encryption, digital signature, hash function, etc.

The ProVerif code for the definition of functions, reduction, equation, free names and constants is as follows.

```
(*function*)
     fun h(bitstring):bitstring. (*hash function*)
     fun co(bitstring,bitstring):bitstring.
     fun xor(bitstring, bitstring): bitstring.
     fun mult(bitstring,bitstring):bitstring.
     fun senc(bitstring,bitstring):bitstring. (*symmetric encryption*)
     fun add(bitstring,bitstring):bitstring.
     (*reduction*)
     reduc forall x: bitstring, y: bitstring; sdec(senc(x, y), y) = x.
     (*equation*)
     equation for all x: bitstring, y: bitstring; xor(xor(x, y), y) = x.
     (*free names and constants*)
     const PW:bitstring [private].
     const ID:bitstring [private].
     const Bi:bitstring[private].
     const Xs:bitstring[private].
     const P:bitstring.
     const k:bitstring.
     const zero:bitstring.
     const one:bitstring.
     free SK:bitstring [private].
     free SK':bitstring [private].
The core message sequences for the proposed scheme are given below.
```

```
Message 1: U --> S: (M1, M2, ctrU', NID)
Message 2: S --> U: (M3, M4, r2)
Message 3: U--> S: (M5)
```

The protocol was modeled as the parallel execution of two processes: the patient user U and the medical server S:

```
process !U | S
```

The processes are the core of protocol model, which define the behavior of each participant in applied pi calculus. The process of user defines the behavior of U, who computes e2, r1, trU', M1 and M2, and sends message (M1, M2, ctrU', NID) through a public channel. After that, U receives message (M3, M4, r2) and computes M5 and SKA. The process of U is modeled as below:

```
let U=
     let RPW=h(co(Bi,xor(ID,PW))) in
     let f=h(RPW) in
     out(sch,ID);
     in(sch,(NID1:bitstring,P1:bitstring,ctrU1:bitstring,e1:bitstring));
     let TID=xor(RPW,e1) in
     !
      event UserStarted(ID);
      new a:bitstring;
      let e2=xor(RPW,TID) in
      let r1=mult(a,P) in
      let ctrU'=add(ctrU1,one) in
      let M1=senc(co(r1,ctrU'),e1) in
      let M2=h(co(ID,co(r1,co(ctrU',NID1)))) in
      out(sch,(M1,M2,ctrU',NID1));
      in(sch,(M3':bitstring,M4':bitstring,r2':bitstring));
      let r'=mult(a,r2')in
      let NID3=xor(h(co(r1,r')),M3') in
      let M4"=h(co(r2',co(r1,co(r',NID3)))) in
      if M4"=M4' then
      let M5=h(co(NID3,r')) in
      let SK=h(co(r2',co(r1,co(r',ctrU')))) in
      out(sch,M5);
      0
     ).
```

The process of trust sever defines the behavior of S during authentication, it authenticates the message (M1, M2, ctrU', NID) received from U, computes and sends (M3, M4, r2) to U through a public channel. After that, S receives and verifies the message M5, and computes SK'. The process of S is modeled as follows:

let S=

```
in(sch,ID1:bitstring);
            new NID:bitstring;
            let e=h(co(ID,Xs)) in
            let ctrU=zero in
            let M=(ID,ctrU) in
            let y=senc(M,Xs) in
            out(sch,(NID,P,ctrU,e));
            in(sch,(M1':bitstring,M2':bitstring,ctrU2:bitstring,NID2:bitstring));
            let (ID2:bitstring,ctrU3:bitstring)=sdec(y,Xs) in
            event UserAuthed(ID2);
            let(r1':bitstring,ctrU4:bitstring)=sdec(M1',h(co(ID2,Xs))) in
            let M=h(co(ID2,co(r1',co(ctrU4,NID2)))) in
            if M=M2' then
            new b:bitstring;
            new NID':bitstring;
            let r2=mult(b,P) in
            let r=mult(b,r1') in
            let M3=h(xor(co(r1',r),NID')) in
            let M4=h(co(r2,co(r1',co(r,NID')))) in
            out(sch,(M3,M4,r2));
            in(sch,M5':bitstring);
            let M5''=h(co(NID',r)) in
            if M5'=M5" then
            let SK'=h(co(r2,co(r1',co(r,ctrU4)))) in
            0.
     The secrecy of the session key and the authentication of the protocol are
modeled as:
     query attacker(SK).
     query attacker(SK').
     event UserAuthed(bitstring).
     event UserStarted(bitstring).
     query id: bitstring; inj-event(UserAuthed(id)) ==> inj-event(UserStarted(id)).
```

We perform the above process in the latest version 1.88 of ProVerif and the performance results show that the proposed scheme achieves security and authentication.

## 7. Performance Comparison

In this section, we present the performance comparison among our scheme and five related schemes [15-19]. Li et al. [22,23] showed that it needs 0.0005 second for one hash operation, 0.063075 second for a scalar multiplication on elliptic curve, and 0.0087 second to perform a symmetric encryption/decryption, respectively.

Let  $T_m$ ,  $T_h$  and  $T_s$  be the time for performing a scalar multiplication on elliptic curve, a one-way hash function, and a symmetric encryption/decryption, respectively. Compared to above operations, exclusive OR and string concatenation operations can be ignored. Since the registration and password change phases only perform one time or off-line, so we mainly focus on the computation of login and verification phase, which is given in Table 1.

Table 1: The computation cost comparison

	$U_{i}$	$S_{j}$	Total
Chang et al. (2013) [15]	$6T_h$	$4T_h$	$10T_h\approx 0.005s$
Das et al. (2013) [16]	$10T_h$	$7 T_h$	$17T_h\approx 0.0085s$
Wen (2013) [17]	$2T_s + 9T_h$	$2T_s + 6T_h$	$4T_s + 15T_h \approx 0.0423s$
Tsai et al. (2013) [18]	$3T_m + 6T_h$	$3T_m + 4T_h$	$6T_m + 10T_h \approx 0.38s$
Tan (2014) [19]	$3T_m + 6T_h$	$3T_m + 4T_h$	$6T_m + 10T_h \approx 0.38s$
Our scheme	$2T_m + T_s + 7T_h$	$2T_m + 2T_s + 6T_h$	$4T_m + 3T_s + 13T_h \approx 0.28s$

From Table 1, we can conclude that Chang et al. [15], Das et al. [16] and Wen [17] schemes are more efficient than others, but these schemes can not achieve perfect forward secrecy. In order to achieve perfect forward secrecy, we always use the Diffie-Hellmen Key Agreement technology, but it may need more computation costs. The proposed scheme is more efficient than Tsai et al. [18] and Tan [19] schemes.

## 8. Conclusion

In this paper, we showed that Wen.'s scheme can not resist off-line password guessing attack, and can not provide privacy protection and perfect forward secrecy. We then propose an improved scheme to overcome their weaknesses. According to formal verification and performance analysis, we show that the proposed scheme achieves security and highly efficient for connected health care.

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#### Reference

- 1. Lambrinoudakis, C., and Gritzalis, S., Managing medical and insurance information through a smart-card-based information system. *J. Med. Syst.* 24(4):213–234, 2000.
- 2. Lee, W. B., and Lee, C. D., A cryptographic key management solution for HIPAA privacy/security regulations. *IEEE Trans. Inf. Technol. Biomed.* 12(1):34–41, 2008.
- 3. Wu, Z. Y., Chung, Y., Lai, F., and Chen, T. S., Password-Based User Authentication Scheme for the Integrated EPR Information System. *J. Med. Syst.* 36:631–638, 2012.
- 4. Wu, Z. Y., Lee, Y. C., Lai, F., Lee H. C., and Chung, Y., A Secure Authentication Scheme for Telecare Medicine Information. Systems. *J. Med. Syst.* 36:1529–1535, 2012.
- 5. He, D. B., Chen, J. H., and Zhang, R., A more secure authentication scheme for telecare medicine information systems. *J. Med. Syst.* 36:1989–1995, 2012.
- 6. Wei, J., Hu, X., and Liu, W., An Improved Authentication Scheme for Telecare Medicine Information Systems. *J. Med. Syst.* 36(6): 3597-3604, 2012.
- 7. Zhu, Z., An Efficient Authentication Scheme for Telecare Medicine Information Systems. *J. Med. Syst.* 36(6):3833-3838, 2012.
- 8. Das, M. L., Saxena, A., and Gulati, V. P., A dynamic ID-based remote user authentication scheme. *IEEE Trans. Consum. Electron.* 50(2):629–631, 2004. 508.
- 9. Awashti A K. Comment on a Dynamic ID-based Remote User Authentication Scheme. *Transactions on Cryptology.*, 1:15–16,2014.
- 10. Ku W C, Chang S T. Impersonation Attack on a Dynamic ID-based Remote User Authentication Scheme using Smart Cards. *IEICE Transactions on Communications.*, E88-B:2165–2167,2005.
- 11. Wang Y Y, Kiu J Y, Xiao F X, Dan J. A More Efficient and Secure Dynamic ID-based Remote User Authentication Scheme. *Comput. Commun.* 32: 583–585,2009.

- 12. Khan, M. K., KS. K., and Alghathbar, K., Cryptanalysis and security enhancement of a more efficient & secure dynamic id-based remote user authentication scheme. *Comput. Commun.* 34(3):305–309, 2010.
- 13. Chen, H. M., Lo, J. W., and Yeh, C. K., An Efficient and Secure Dynamic ID-based Authentication Scheme for Telecare Medical Information Systems. *J. Med. Syst.* 36(6): 3907-3915, 2012.
- 14. Xie, Q., Zhang, J., and Dong, N., Robust Anonymous Authentication Scheme for Telecare Medical Information Systems. *J. Med. Syst.* 37(2):1-8, 2013.
- 15. Chang, Y. F., Yu, S. H., and Shiao, D. R., An uniqueness-and anonymity-preserving remote user authentication scheme for connected health care. *J. Med. Syst.* 37:9902, 2013.
- 16. Das, A. K., and Goswami, A., A Secure and Efficient Uniqueness-and-Anonymity-Preserving Remote User Authentication Scheme for Connected Health Care. *J. Med. Syst.* 37:9948, 2013.
- 17. Wen, F., A Robust Uniqueness-and-Anonymity-Preserving Remote User Authentication Scheme for Connected Health Care. *J. Med. Syst.* 37:9980, 2013.
- 18. Tsai, J.,Lo, N., and Wu. T., Novel Anonymous Authentication Scheme Using Smart Cards. *IEEE Trans. Ind. Electron.*,9(4):2004-2013, 2013.
- 19. Tan, Z., A User Anonymity Preserving Three-Factor Authentication Scheme for Telecare Medicine Information Systems. *J. Med. Syst.* 38:16, 2014.
- Abadi, M., Blanchet, B., and Lundh, H. C., Models and Proofs of Protocol Security: A Progress Report. 21st International Conference on Computer Aided Verification, Grenoble, France, pp. 35-49, 2009.
- 21. Abadi, M., and Fournet, C., Mobile Values, New Names, and Secure Communication. *Proceedings of the 28th ACM SIGPLAN-SIGACT symposium on Principles of programming languages*. ACM New York, pp. 104-115, 2001.
- 22. Li, C. T., Hwang, M. S., and Chu, Y. P., A secure and efficient communication scheme with authenticated key establishment and privacy preserving for vehicular ad hoc networks. *Comput. Commun.* 31: 2803-2814, 2008.
- 23. Li, W., Wen, Q., Su, Q., and Jin, Z., An efficient and secure mobile payment protocol for restricted connectivity scenarios in vehicular ad hoc network. *Comput. Commun.* 35:188-195,2012.