$$\pi(X,x) \xrightarrow{g_* \circ f_*} \begin{matrix} \pi(Y,(g \circ f)(x)) \\ \downarrow \\ \downarrow \\ \pi(Y,\varphi_1(x_0)) \end{matrix}$$