# Uncertain Reasoning

COMP9414: Artificial Intelligence

### Lecture Overview

- Introduction
- Probabilistic inference: Bayes' rule
- Belief networks
- Fuzzy logic

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### Introduction

- Classic logic and reasoning assume events either occur or do not occur, but not necessarily the same in real world.
- For instance, in weather prediction, probabilities can be used.
- People can cope well with uncertainty in complex situations assuming default or common values when precise data is unknown.
- However, the more data is missing, the more guesses have to be made, the lower the quality of the final reasoning.

## Introduction

- A system designed to emulate the human reasoning process needs to generate and rank several potential solutions.
- Uncertainty might be expressed as confidence in which continuous values are allowed.
- Uncertainty can be expressed both in the information and in the reasoning process.
- The conclusion of a rule cannot be guaranteed.
  - For example: high blood pressure (HBP) increases the chance of a heart attack, but not everyone having HBP will have a heart attack.

## Uncertainty in rules

- Rules can express many types of knowledge
- But how can *uncertainty* be handled?
- Uncertainty may arise from:
  - Uncertain evidence (Not certain that Joe Bloggs works for ACME.)
  - Uncertain link between evidence and conclusion.
     (Cannot be certain that ACME employee earns a large salary, just likely.)
  - Vague rule. (What is a "large"?)

Bayesian inference

Confidence factors

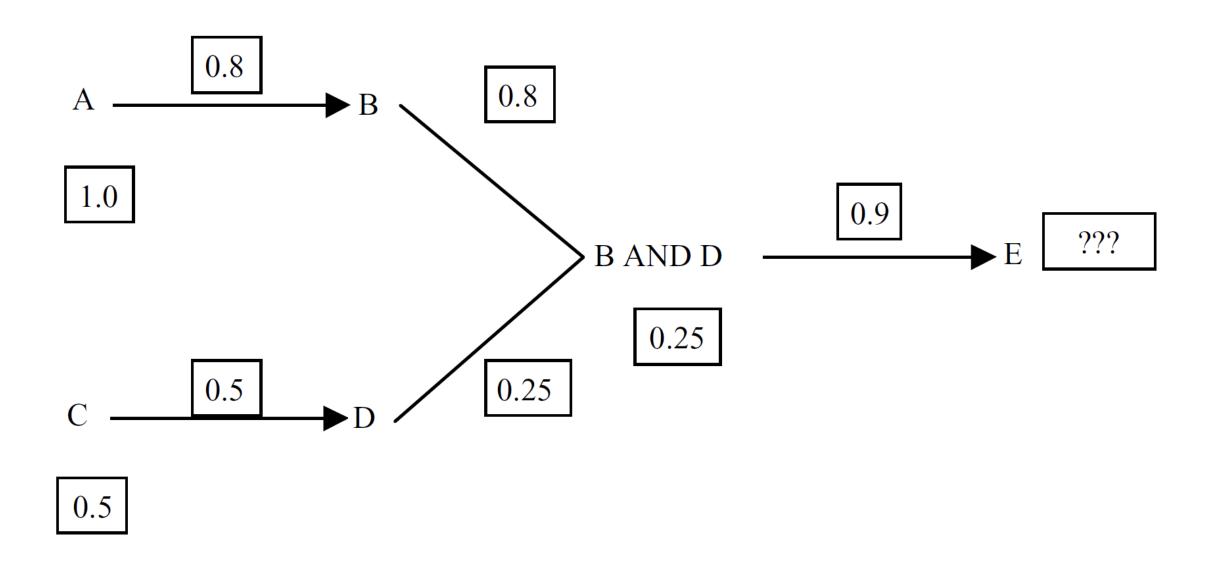
Fuzzy Logic

- Uncertainty in antecedents: based on user information and deduced from another rule.
- Uncertainty in a rule: based on expert's rule confidence and propagated to the conclusion.
- For example, a simple rule: if A is true, then B is true (A => B)
- If we are uncertain about A, we are uncertain about B:

However, there might be uncertainty about the validity of the rule. For instance:

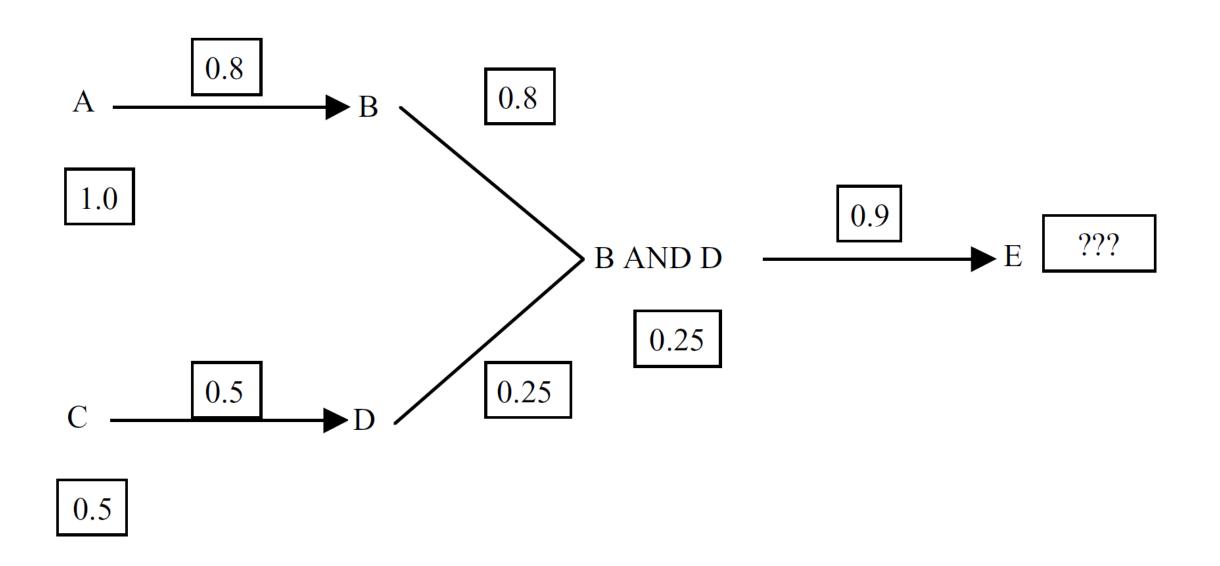
 Reasoning with confident factors: two independent pieces of evidence should increase confidence. Then the rule is inverted, for instance:

 Inference network: sequence of relationships between facts and confidence factors.



- $CF(B) = CF(A) \times CF(IF A THEN B) = 1 \times 0.8 = 0.8$
- $CF(D) = CF(C) \times CF(IF C THEN D) = 0.5 \times 0.5 = 0.25$
- CF(B&D) = min(CF(B), CF(D)) = min(0.8, 0.25) = 0.25
- CF(E) = CF(B&D) × CF (IF B&D THEN E) = ?

 Inference network: sequence of relationships between facts and confidence factors.



- $CF(B) = CF(A) \times CF(IF A THEN B) = 1 \times 0.8 = 0.8$
- $CF(D) = CF(C) \times CF(IF C THEN D) = 0.5 \times 0.5 = 0.25$
- CF(B&D) = min(CF(B), CF(D)) = min(0.8, 0.25) = 0.25
- $CF(E) = CF(B\&D) \times CF (IF B\&D THEN E) = 0.225$

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## Propositions

Propositions are entities (facts or non-facts) that can be true or false

#### Examples:

- "The sky is blue" the sky is blue (here and now).
- "Socrates is bald" (assumes 'Socrates', 'bald' are well defined)
   "The car is red" (requires 'the car' to be identified)
- "Socrates is bald and the car is red" (complex proposition)
- Use single letters to represent propositions, e.g. P: Socrates is bald
- Reasoning is independent of definitions of propositions

## Propositional Logic

- Letters stand for "basic" propositions
- Combine into more complex sentences using operators not, and, or, implies, iff
- Propositional connectives:

_	negation	$\neg P$	"not P"
$\wedge$	conjunction	$P \wedge Q$	"P and Q"
V	disjunction	$P \vee Q$	"P or Q"
$\longrightarrow$	implication	$P \rightarrow Q$	"If P then Q"
$\longleftrightarrow$	bi-implication	$P \leftrightarrow Q$	"P if and only if Q"

## From English to Propositional Logic

- "It is not the case that the sky is blue":  $\neg B$  (alternatively "the sky is not blue")
- "The sky is blue and the grass is green":  $B \wedge G$
- "Either the sky is blue or the grass is green":  $B \vee G$
- "If the sky is blue, then the grass is not green":  $B \rightarrow \neg G$
- "The sky is blue if and only if the grass is green":  $B \leftrightarrow G$
- "If the sky is blue, then if the grass is not green, the plants will not grow":  $B \to (\neg G \to \neg P)$

- It is not always possible to create a complete, consistent model of the world.
- Probability theory will serve as the formal language for representing and reasoning with uncertain knowledge.
- Bayes theorem allows computing a conditional probability.
- It is useful to calculate the probability of events where intuition often fails.
- Widely used in machine learning. For instance, classification predictive modelling problems such as the Bayes Optimal Classifier and Naive Bayes.

- For each primitive proposition or event, attach a degree of belief to the sentence.
- For proposition A, probability  $0 \le P(A) \le 1$ .
  - If A is true, P(A) = 1.
  - If A is false, P(A) = 0.
- Proposition A is either true or false. But P(A) is the degree of belief in A being true or false.

- Boolean variables abbreviated, P(A=true) = P(A) and  $P(A=false) = P(\sim A)$
- Examples:
- P(Weather = sunny) = 0.6 (we believe weather will be sunny with 60% certainty from {sunny, rainy, snowy, cloudy}).
- P(Cavity = true) = 0.05 (we believe there is a 5% possibility that a person has a cavity).
- P(A=a ^ B=b) = P(A=a, B=b) = 0.2, with A=Mood, a=happy, B=Weather, and b=rainy (we believe there is a 20% chance that when it is raining my mood is happy).

#### Axioms:

- $0 \le P(A=a) \le 1$
- P(True) = 1, P(False) = 0
- $P(A \lor B) = P(A) + P(B) P(A \land B)$

#### Properties:

- $P(\sim A) = 1 P(A)$
- $P(A) = P(A ^ B) + P(A ^ B)$
- Sum{P(A=a)} = 1, where the sum is over all possible values a in the sample space of

## Joint Probability Distribution

Probability of two (or more) simultaneous events, often described in terms of events A
and B from two dependent random variables, e.g., X and Y.

 $P(A \text{ and } B) \text{ or } P(A \land B) \text{ or } P(A, B).$ 

- The joint probability is symmetrical: P(A, B) = P(B, A).
- Full joint probability distribution assigns probabilities to all possible combinations.

## Joint Probability Distribution

- For n Boolean variables, rows in the table 2<sup>n</sup>.
- For k possible values, rows in the table k<sup>n</sup>.
- Sum in the right column must be 1. For n Booleans, we need to know 2<sup>n</sup>-1 other values.
- If we know all the values, we can compute any probability in the domain:
  - P(Bird=T) = P(B) = 0.0 + 0.2 + 0.04 + 0.01 = 0.25
  - P(Bird=T, Flier=F) = P(B,  $\sim$ F) = P(B,  $\sim$ F, Y) + F(B,  $\sim$ F,  $\sim$ Y) = 0.04 + 0.01 = 0.05

#### **Bird Flier Young Probability**

T	T	T	0.0
T	T	F	0.2
T	F	T	0.04
T	F	F	0.01
F	T	T	0.01
F	T	F	0.01
F	F	T	0.23
F	F	F	0.5

## Conditional Probability

- Probability of one (or more) event given the occurrence of another event, denoted P(A | B).
- Conditional probabilities are key for reasoning as they accumulate evidence.
- P(A | B) = 1 is equivalent to B => A in propositional logic. Thus, P(A | B) = 0.9 is B => A with 90% certainty.
- The conditional probability is defined as:

$$P(A|B) = \frac{P(A,B)}{P(B)}$$

- Joint probability is symmetrical: P(A, B) = P(B, A).
  - However, conditional probability is not: P(A | B) != P(B | A)
- Chain Rule: P(A,B,C,D) = P(A|B,C,D)P(B|C,D)P(C|D)P(D)

## Conditional Probability

Example: P(~Bird | Flier)

$$P(\sim B|F) = P(\sim B,F) / P(F)$$
  
=  $(P(\sim B,F,Y) + P(\sim B,F,\sim Y)) / P(F)$   
=  $(.01 + .01)/P(F)$ 

- $P(\sim B|F) = 0.02/0.22 = 0.091$
- This is intractable as it means that we must compute and store the full joint probability distribution table.

#### **Bird Flier Young Probability**

T	T	T	0.0
T	T	F	0.2
T	F	T	0.04
T	F	F	0.01
F	T	T	0.01
F	T	F	0.01
F	F	T	0.23
F	F	F	0.5

$$P(A|B) = \frac{P(A,B)}{P(B)}$$

## Bayes' Rule

Bayes theorem:

$$P(A|B) = \frac{P(B|A)P(A)}{P(B)}$$

$$P(A|B) = \frac{P(B|A)P(A)}{P(B|A)P(A) + P(B|^{\sim}A)P(^{\sim}A)}$$

- P(A|B) is referred to as the posterior probability
- P(A) is referred to as the prior probability.
- P(B|A) is referred to as the likelihood.
- P(B) is referred to as the evidence.

## Bayes' Rule

- Often, we want to know P(A|B) but we only have access to P(B|A).
- Example: If S represents a given patient has a stiff neck and M the patient has meningitis.
- The doctor and patient may like to know P(M|S), but from the general population is difficult.
- Doctors may be able to accumulate statistics that define P(S|M).
- Then, if P(M) = 1/50,000, P(S) = 1/20, and P(S|M) =1/2. Using Bayes's Rule P(M|S) = 1/5000 = 0.0002 or 0.02%

$$P(A|B) = \frac{P(B|A)P(A)}{P(B)}$$

## Bayes' Rule

Base rates of women having breast cancer and having no breast cancer are 0.02% and 99.98% respectively. The true positive rate or sensitivity P(positive mammography | breast cancer) = 85% and the true negative or specificity P(negative mammography | ~breast cancer) = 95%. Compute P(C | M).

$$P(C \mid M) = P(M \mid C) * P(C) / P(M)$$
  
 $P(C \mid M) = 0.85 * 0.0002 / P(M)$ 

From Bayes' rule: 
$$P(B) = P(B|A) * P(A) + P(B|A) * P(A)$$
  
 $P(M) = P(M|C) * P(C) + P(M|C) * P(C)$   
 $P(M) = 0.85 * 0.0002 + 0.05 * 0.9998 = 0.05016$ 

$$P(C \mid M) = 0.85 * 0.0002 / 0.05016 = 0.00339 \text{ or } 0.34\%$$

$$P(A|B) = \frac{P(B|A)P(A)}{P(B)}$$

$$P(A|B) = \frac{P(B|A)P(A)}{P(B|A)P(A) + P(B|^*A)P(^*A)}$$

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#### Belief Networks

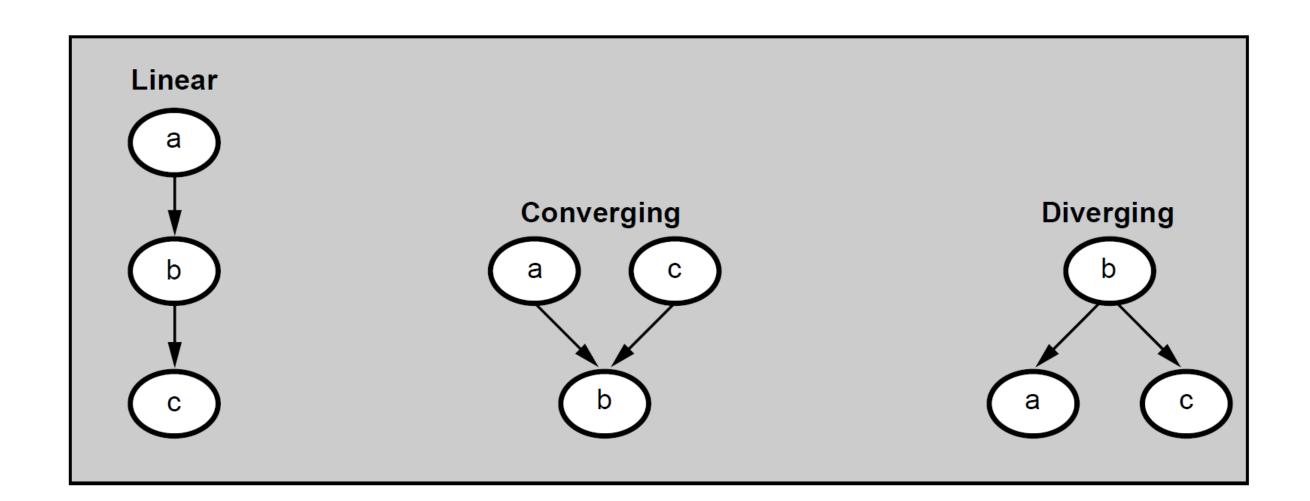
- Bayesian network, Bayes nets, causal nets.
- Space-efficient data structure for full joint probability distribution.
- Represent causal relations: arcs from cause variables to immediate effects.
  - Predictive reasoning from causes to effects (top-down).
  - Diagnostic reasoning from effects to causes (bottom-up).

#### Belief Networks

- Useful in situations in which causality plays a role but our understanding is incomplete.
- Formally, it's a directed, acyclic graph (DAG)
  - Include a node for each variable and a directed arc from A to B if A is a direct causal influence on B.
- For a probability distribution, we need only to give the prior probabilities for root nodes and conditional probabilities for non-root nodes considering all combinations from the direct predecessors.

#### Belief Networks

- Topology: Three connection types.
- Variables are true or false and certain independence assumptions hold.
- For instance in diverging: A and C are conditionally independent given B  $\rightarrow$  P(C|B,A) = P(C|B) and symmetrically P(A|B,C) = P(A|B).

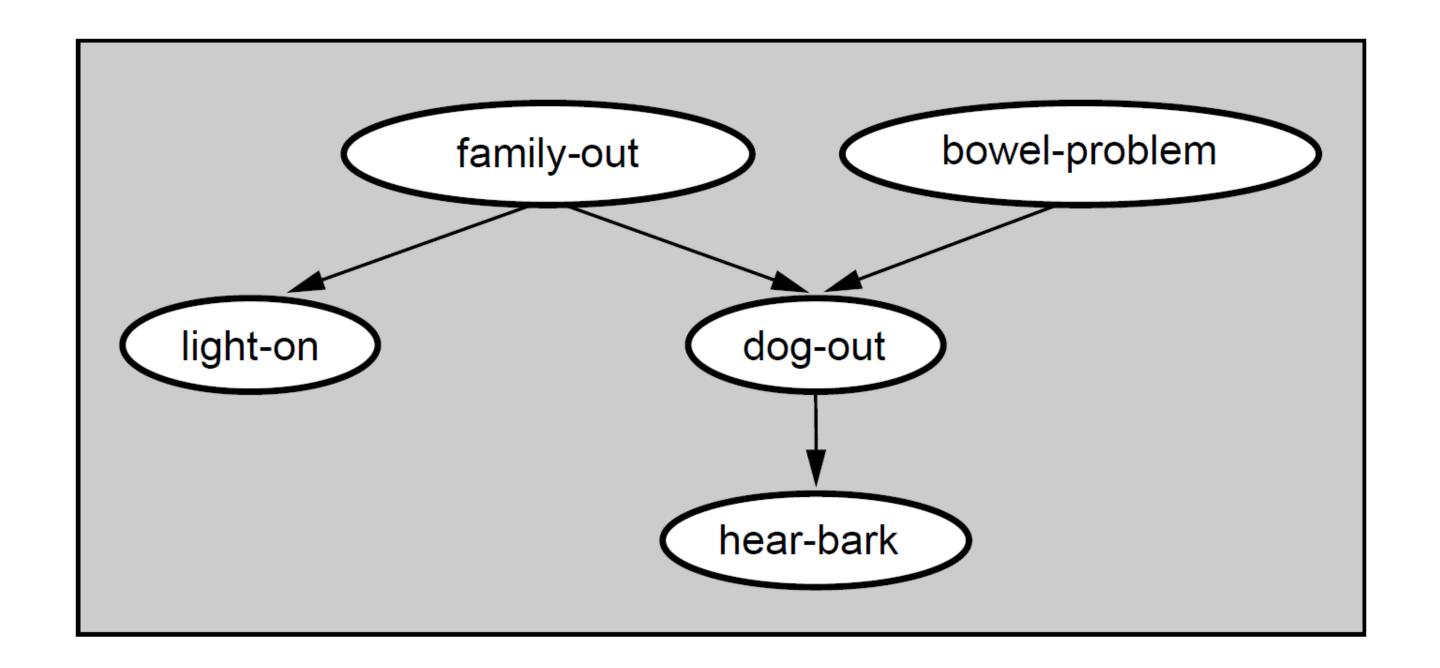


- Consider the problem domain in which I go home, and I want to know if someone from my family is home before I go in. Let's say I know the following information:
  - (1) When my wife leaves the house, she often (but not always) turns on the outside light.
  - (2) When nobody is home, the dog is often left outside.
  - (3) If the dog has bowel troubles, it is also often left outside.
  - (4) If the dog is outside, I will probably hear it barking (though it might not bark, or I might hear a different dog barking and think it's my dog).

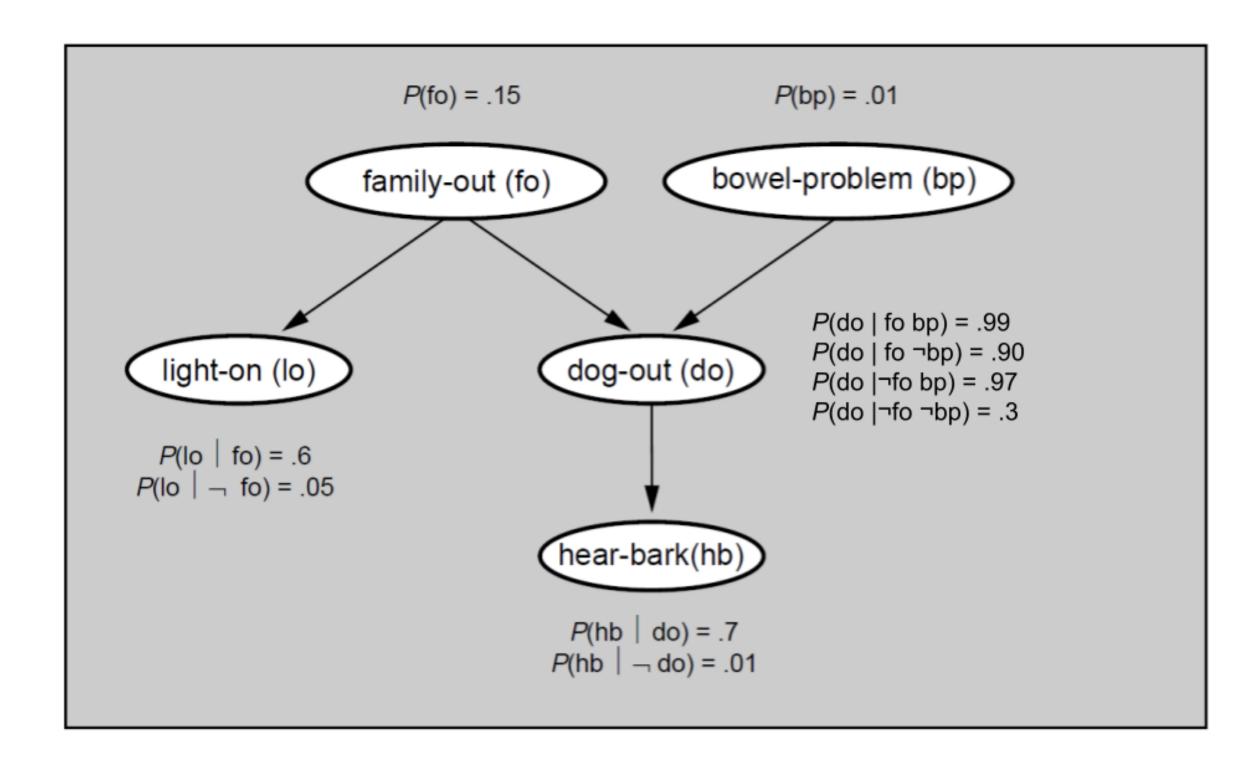
- Given the previous information, we can consider the following five Boolean random variables:
  - family-out (fo): everyone is out of the house.
  - light-on (*lo*): the light is on.
  - dog-out (do): the dog is outside.
  - bowel-problem (bp): the dog has bowel troubles.
  - hear-bark (hb): I can hear the dog barking.

- From this information, the following direct causal influences seem appropriate:
  - 1. *hb* is only directly influenced by *do*. Hence *hb* is conditionally independent of *lo*, *fo* and *bp* given *do*.
  - 2. *do* is only directly influenced by *fo* and *bp*. Hence *do* is conditionally independent of *lo* given *fo* and *bp*.
  - 3. *Io* is only directly influenced by *fo*. Hence *Io* is conditionally independent of *do*, *hb* and *bp* given *fo*.
  - 4. fo and bp are independent.

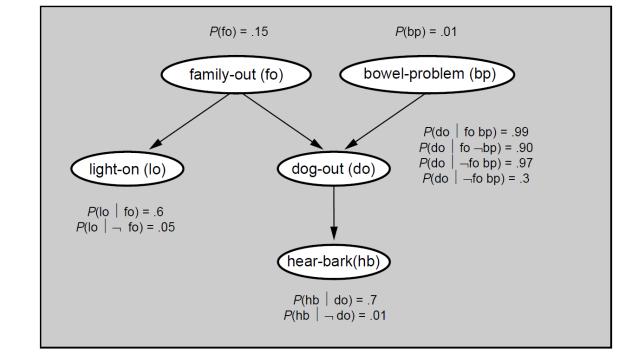
• Belief network representing these direct causal relationships (though these causal connections are not absolute, i.e., they are not implications):



- For each root node, the prior probability of the random variable needs to be determined.
- For each non-root node, the conditional probabilities of the node's variable given all possible combinations of its immediate parent nodes need to be determined.
- In this example, a total of 10 probabilities are computed and stored in the net (not 32!)
  - The reduction is due to the conditional independence of many variables.



## Computing Joint Probability



Example: Compute P(BP,~FO,DO,~LO,HB)

```
P(BP, \sim FO, DO, \sim LO, HB) = P(HB, \sim LO, DO, \sim FO, BP)
     = P(HB \mid \sim LO, DO, \sim FO, BP) * P(\sim LO, DO, \sim FO, BP)
                                                                         by Product Rule
     = P(HB|DO) * P(\sim LO, DO, \sim FO, BP)
                                                                         by Conditional Independence of
                                                               HB and LO,FO, and BP given DO
     = P(HB|DO) P(\sim LO \mid DO, \sim FO, BP) P(DO, \sim FO, BP)
                                                                         by Product Rule
     = P(HB|DO) P(\sim LO|\sim FO) P(DO,\sim FO,BP)
                                                                         by Conditional Independence of
                                                               LO and DO, and LO and BP, given FO
     = P(HB|DO) P(\sim LO|\sim FO) P(DO|\sim FO,BP) P(\sim FO,BP)
                                                                         by Product Rule
     = P(HB|DO) P(\sim LO|\sim FO) P(DO|\sim FO,BP) P(\sim FO|BP) P(BP)
                                                                         by Product Rule
     = P(HB|DO) P(\sim LO|\sim FO) P(DO|\sim FO,BP) P(\sim FO) P(BP)
                                                                         by Independence of FO and BP
     = (.7)(1 - .05)(.97)(1 - .15)(.01) = 0.005483
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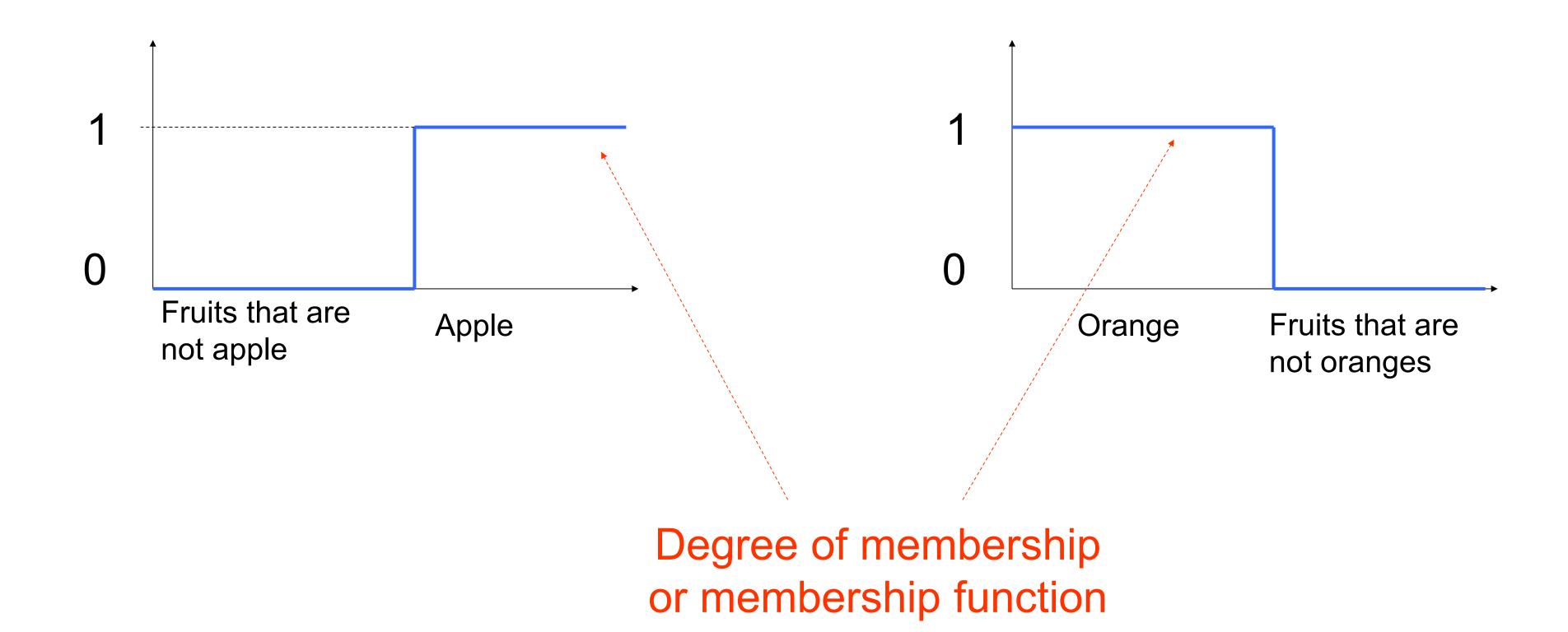
All values are available directly in the network (since  $P(\sim A|B) = 1 - P(A|B)$ )

### Lecture Overview

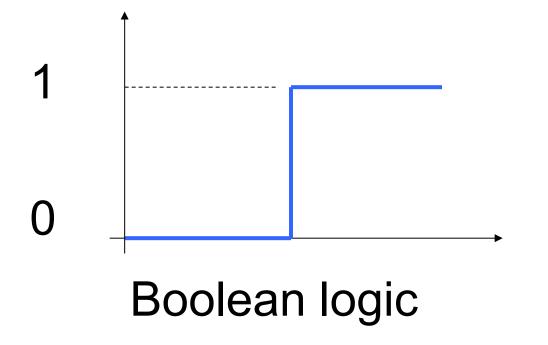
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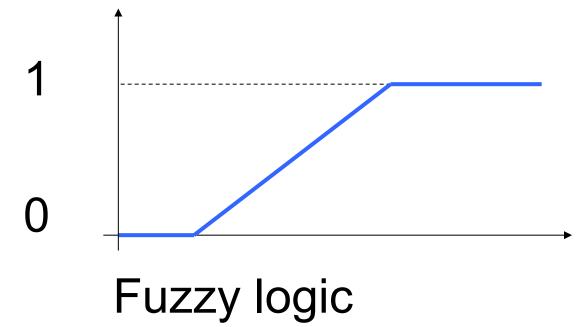
- Crisp or Boolean logic uses only two binary values: true, false.
- Fuzzy logic is an extension of classic logic and is based on the idea that at a given moment, it is not possible to precisely determine the value of a variable X.
- In fuzzy logic, one can only know the degree of membership in each of the sets that have participated in defining the range of variation of the variable.
- For example: low, medium, or high temperature.

Boolean logic. Set of fruits: Apple|Fruit, Orange|Fruit

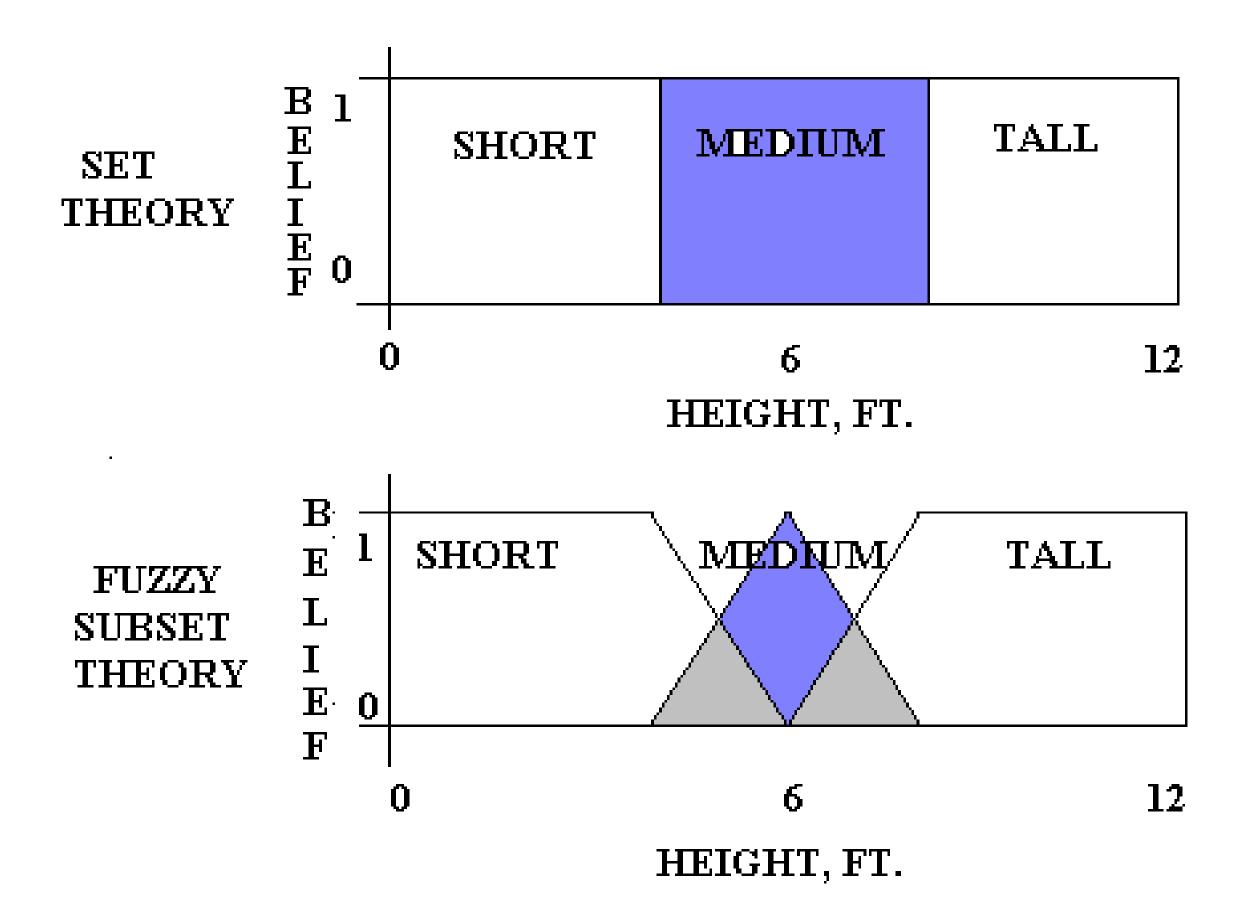


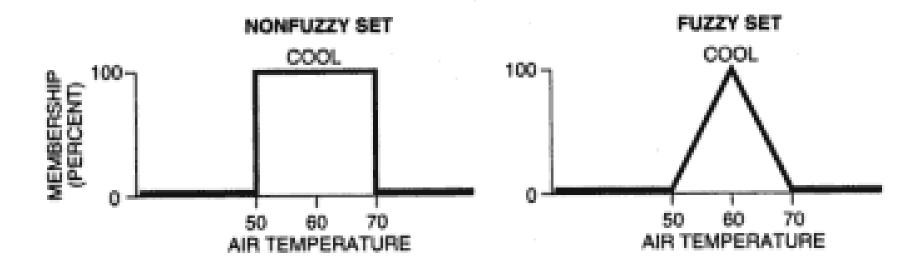
 Fuzzy logic is an extension of Boolean logic to handle the concept of partial truth when truth values lie between "absolutely true" and "absolutely false."

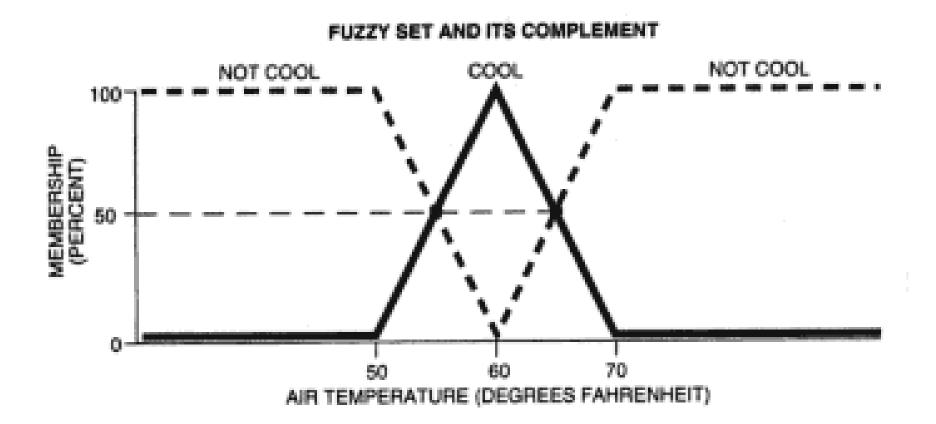




#### FUZZINESS VS. PROBABILITY







#### Ambiguity

#### Uncertainty:

- It is related to information (lack of information).
- Occurs when the timing of a certain event is unknown.

#### Probability:

- It determines the likelihood of a certain event occurring.
- It is calculated and verified through experimentation.

#### Imprecision or ambiguity:

- It is a characteristic of human communication language.
- It is related to the degree to which an event occurs.

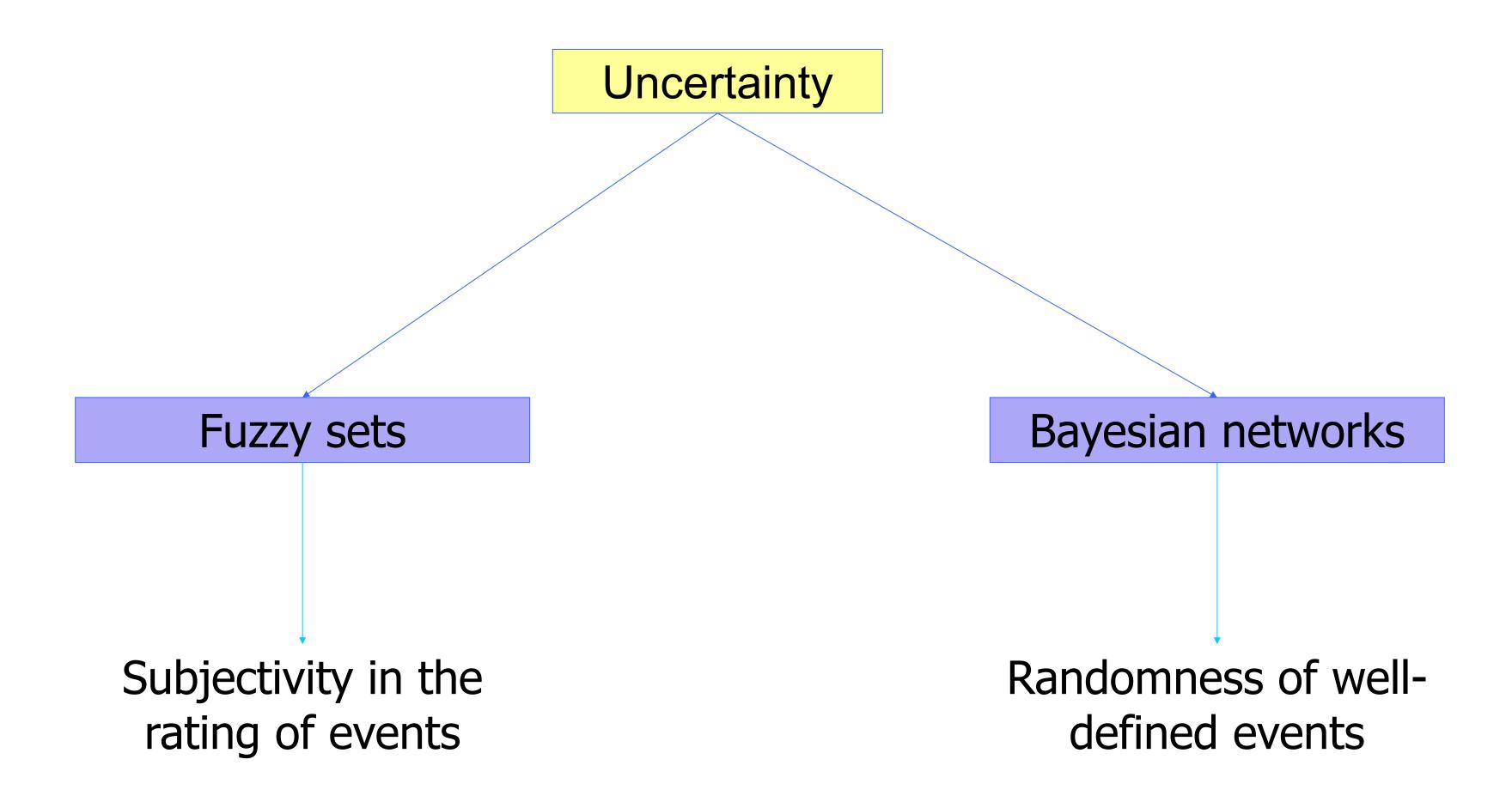
#### Ambiguity

- Ambiguity is related to the degree to which events occur regardless of the probability of their occurrence.
- For example, the degree of youth in a person is a fuzzy event regardless of being a random variable.
- Probabilistic uncertainty dissipates with an increase in the number of occurrences, whereas fuzziness does not.
- If an event occurs, it is random. The degree to which it occurs is fuzzy.

#### Ambiguity

- Ambiguity is a characteristic of human language. For example:
  - If you study hard, then you will get good grades.
  - The second Al assignment is progressing strongly.
  - Students put effort into their projects.
  - Easy-going lecturer.
  - Difficult exam.
  - If the teacher is kind-hearted, then the exam will be easy.

## Ambiguity vs. Probability



- They relax the degree of membership restriction, A:  $X \rightarrow [0,1]$ , interval
- A fuzzy set in the universe U is characterized by the membership function A(x), which takes values in the interval [0,1], unlike classical sets that take either the value zero or one {0, 1}.
- The fuzzy set A can be represented as:
  - $A = \{ (\mu_A(x), x) \mid x \in U \}$
  - $A = \{ (\mu_A(x) / x) | x \in U \}$
- Where  $\mu_A(x)$  is the degree of membership.

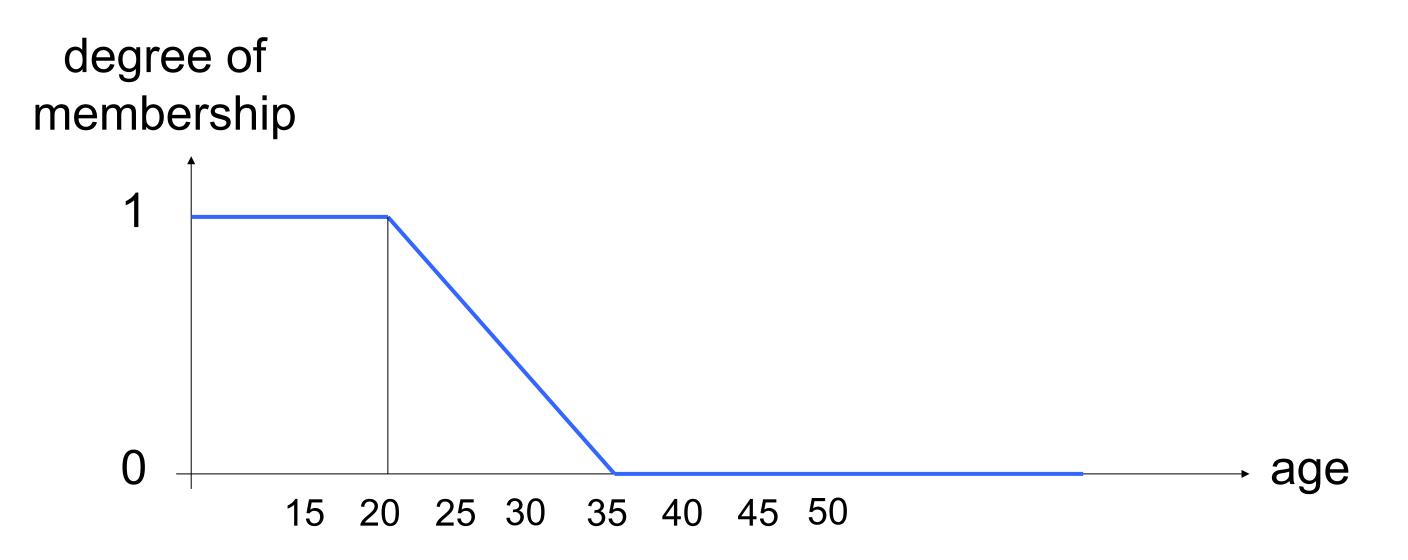
A fuzzy set can be alternatively denoted as:

• If x is discrete: 
$$A = \sum_{x_i \in X} \mu_A(x_i) / x_i$$

• If x is continuous: 
$$A = \int_X \mu_A(x) / x$$

 Note: In this notation, summation and integral represent the union of the membership degrees and therefore / does not mean division.

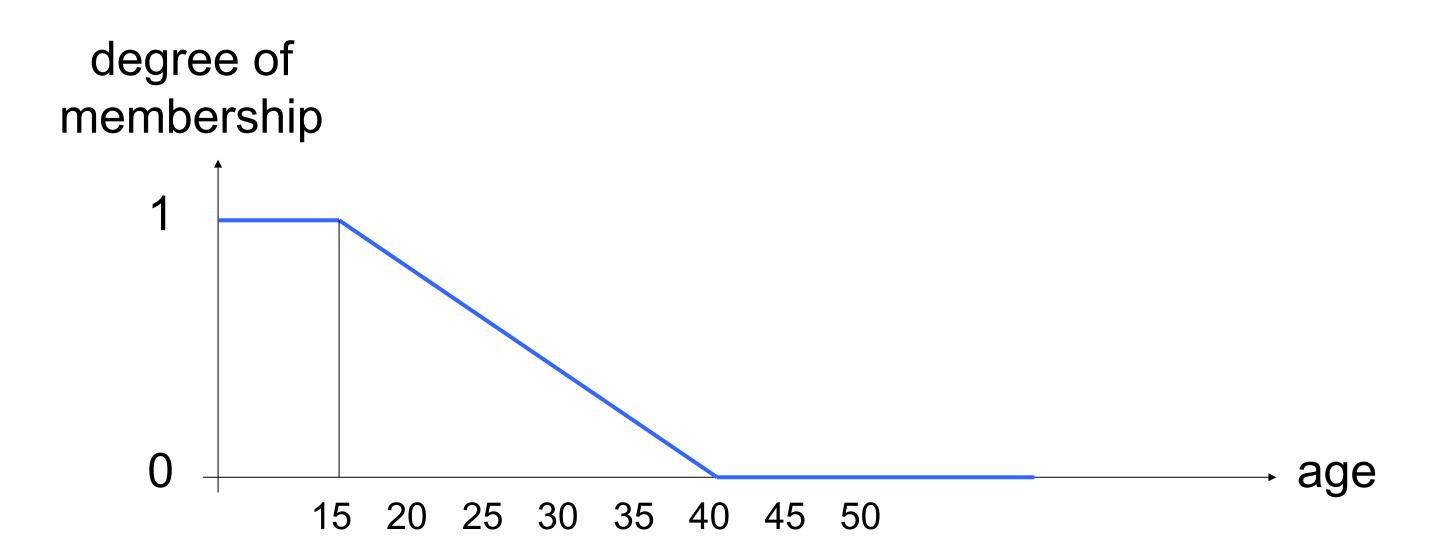
Define the fuzzy set young:



 $A = \{1/10, 1/15, 1/20, 0.75/25, 0.25/30, 0/35\}$ 

 $A = \{(1,10), (1,15), (1,20), (0.75,25), (0.25,30), (0,35)\}$ 

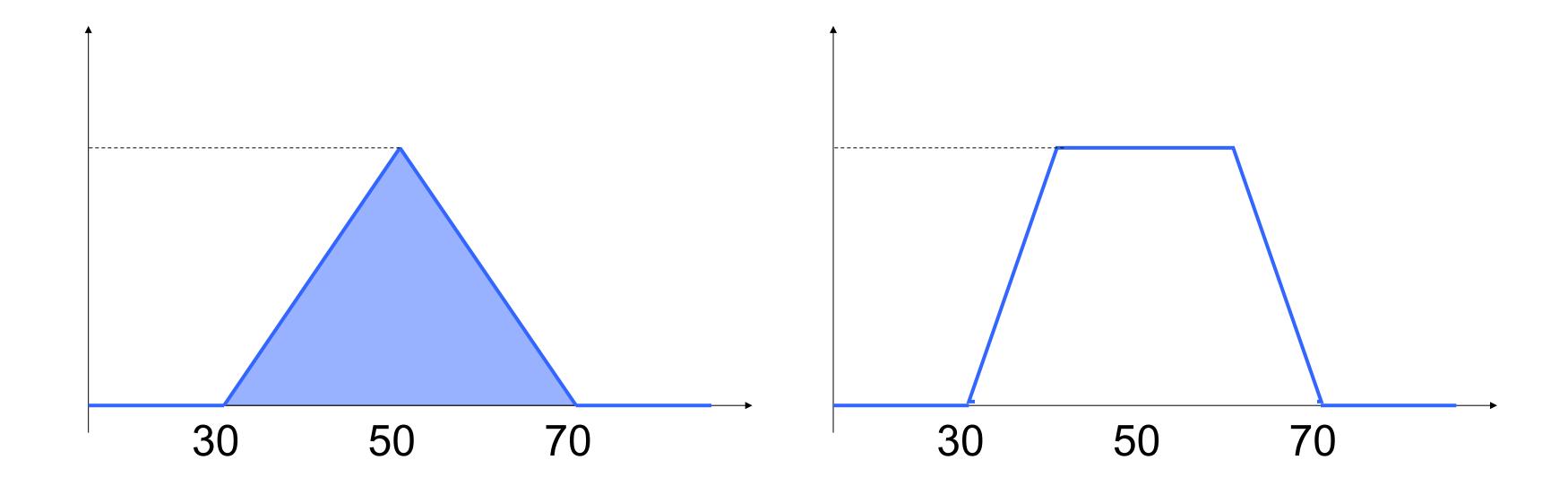
Define the fuzzy set young:



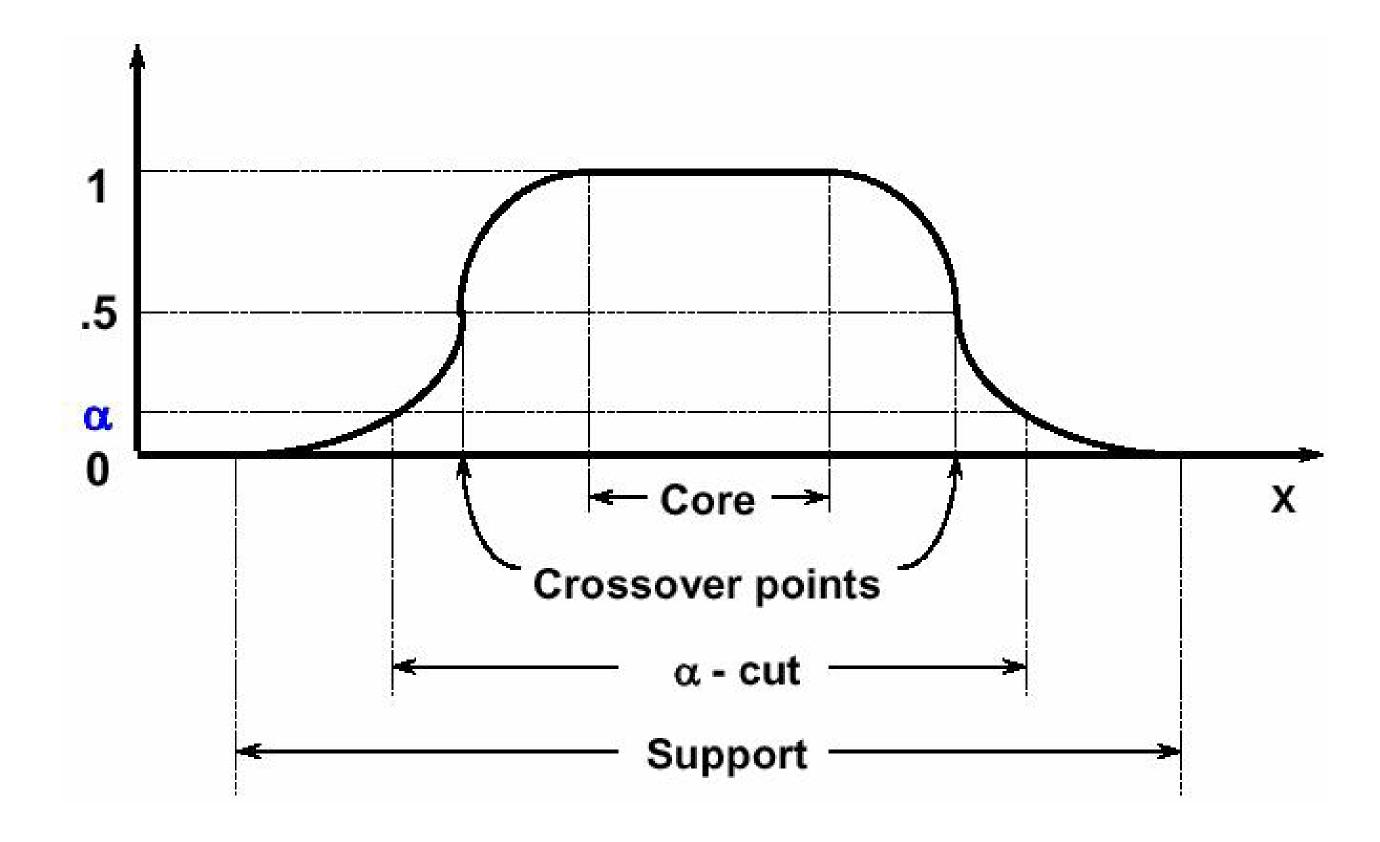
 $A = \{1/10, 1/15, 0.80/20, 0.60/25, 0.40/30, 0.20/35, 0.0/40\}$ 

 $A = \{(1,10), (1,15), (0.80,20), (0.60,25), (0.40,30), (0.20,35), (0.0,40)\}$ 

Plot the fuzzy set near 50 years old:

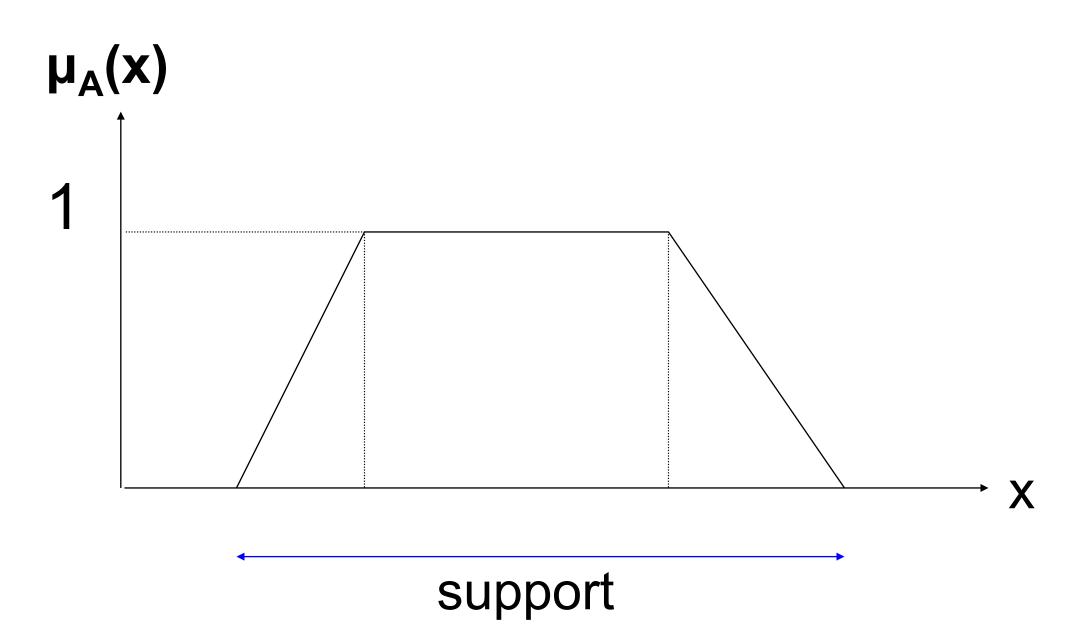


• Some basic concepts include: support, crossover points, core, height, centre value, and α-cut.



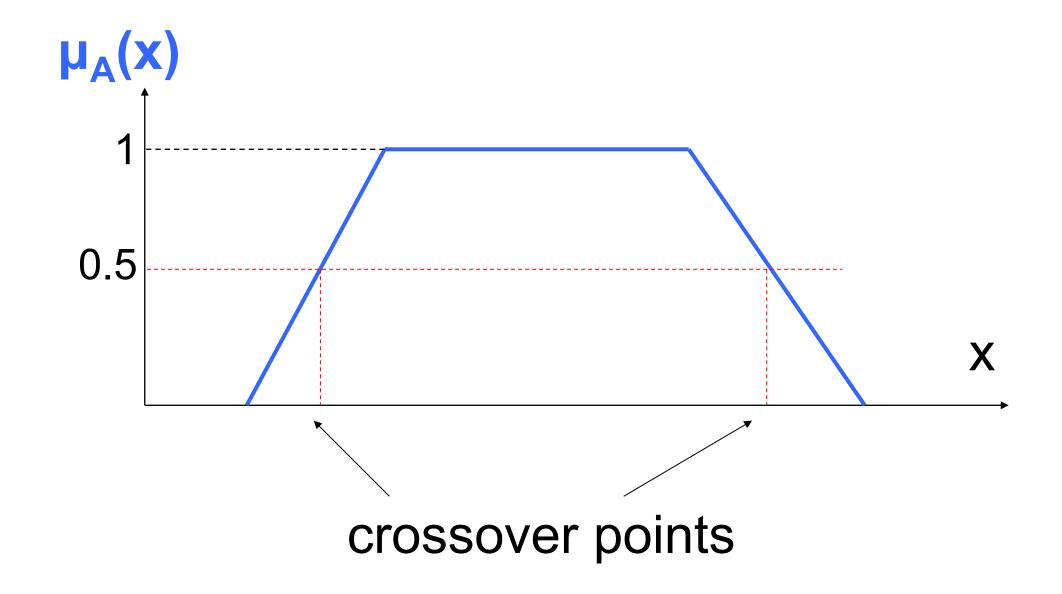
#### Fuzzy Sets: Support

- The support of a fuzzy set A in the universe of discourse U is a crisp set that contains all the elements of U that have non-zero membership values in A.
- If the support of a fuzzy set is empty, it is called an empty fuzzy set.
- If the support of the fuzzy set is represented by a single point in U, it is called a
  fuzzy singleton.
- Support(A) =  $\{x \in U / \mu_A(x) > 0\}$



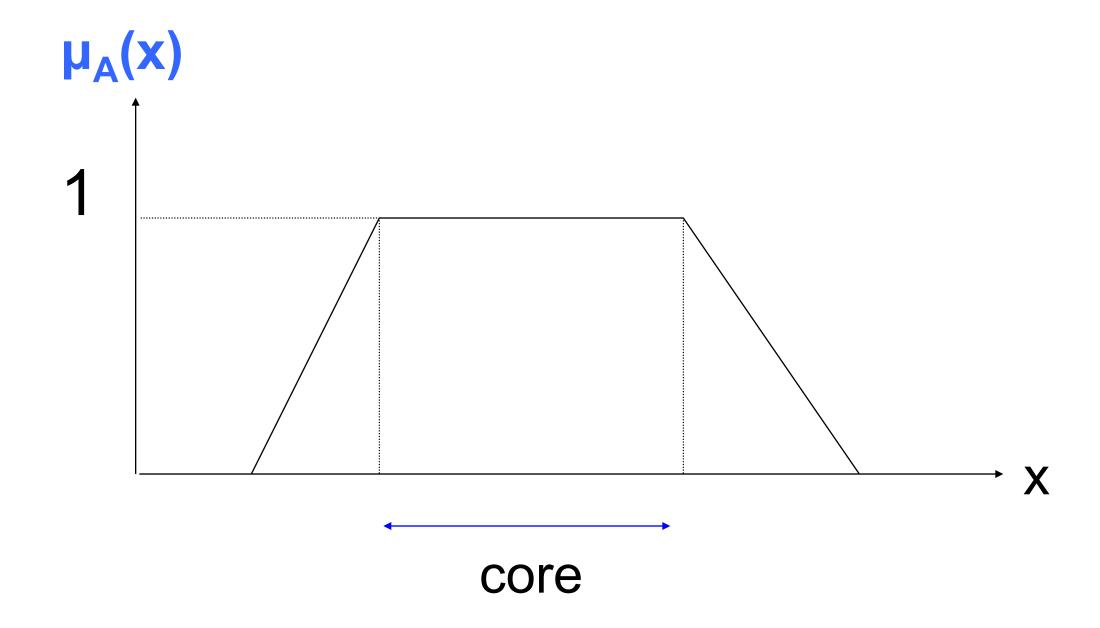
#### Fuzzy Sets: Crossover Point

• The crossover point of a fuzzy set is the point in U where the membership value in A is 0.5.



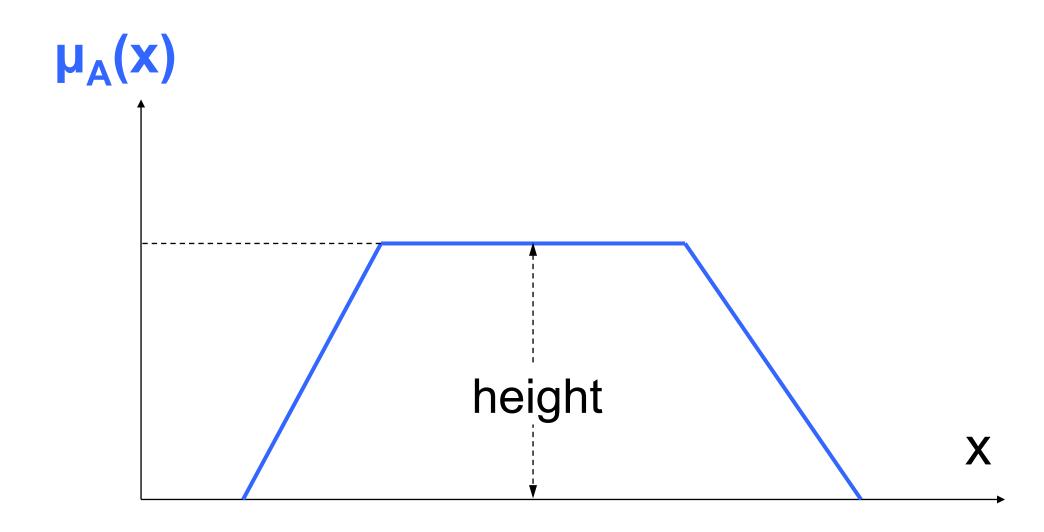
#### Fuzzy Sets: Core

• The set of x values where  $\mu_A(x)$  reaches the value of 1 is called the core of the fuzzy set A.



## Fuzzy Sets: Height

- The height of a fuzzy set is the highest membership value achieved by any point.
- In a normal fuzzy set, the height is 1.
  - normal:  $\mu_A(x) = 1$
  - subnormal:  $\mu_A(x) < 1$

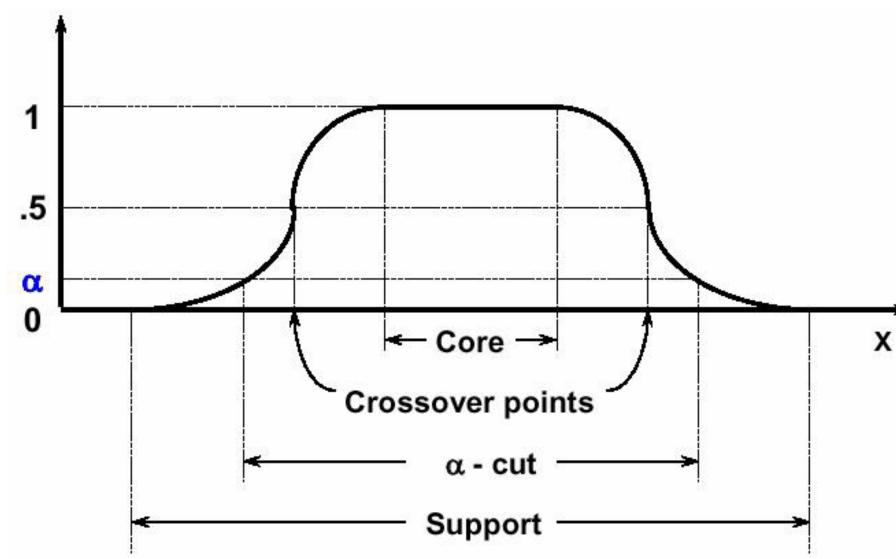


#### Fuzzy Sets: Centre Value

- If the mean value of all the points at which the membership function of a fuzzy set achieves its maximum value is finite, then the centre of the fuzzy set is the average of these values.
- If the mean value is infinite, then the centre is defined as the smallest among all the points that achieve the maximum membership value.

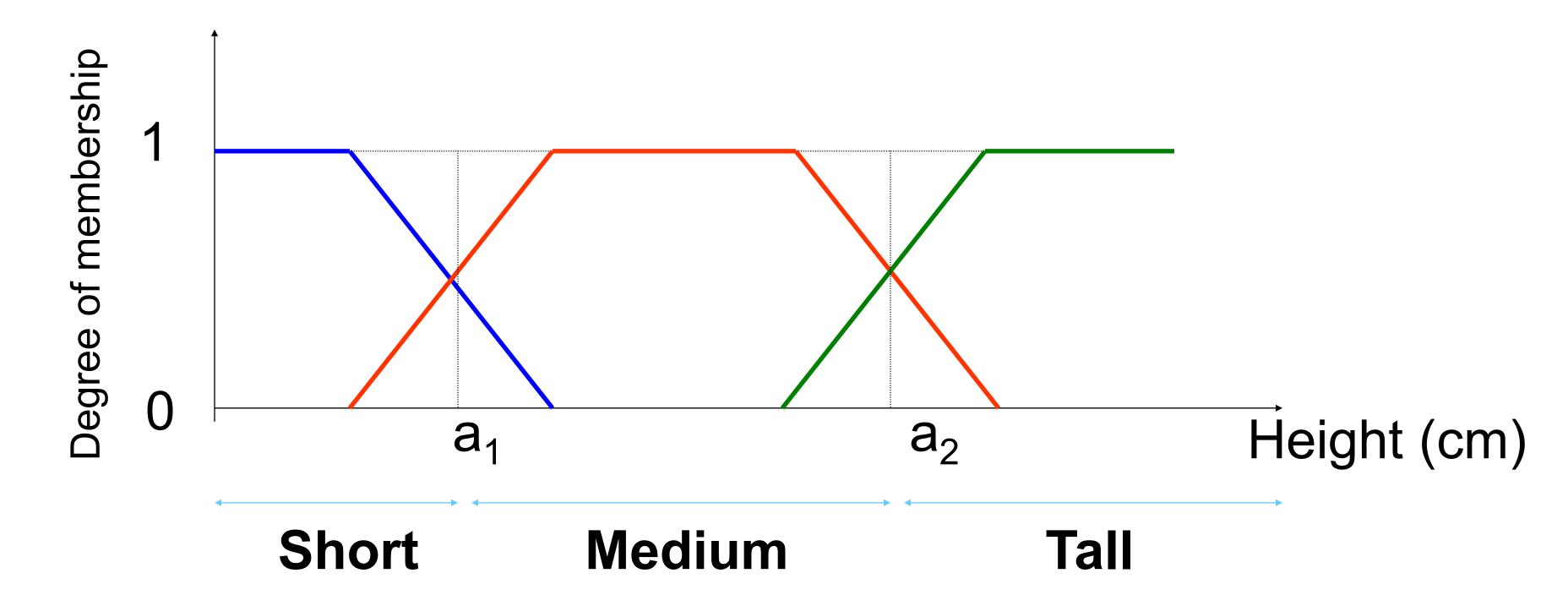
## Fuzzy Sets: α-cut

- Given a fuzzy set A defined in X and a number  $\alpha \in [0; 1]$ , an  $\alpha$ -cut is a crisp set that contains all the elements in U that have membership values in A greater than or equal to  $\alpha$ , defined by:
  - $A_{\alpha} = \{ x \in U / \mu_A(x) \ge \alpha \}$
  - $A_{\alpha^+} = \{ x \in U / \mu_A(x) > \alpha \}$  strong  $\alpha$ -cut
- Properties. Given a fuzzy set A defined in X and two values  $\alpha 1$  and  $\alpha 2 \in [0; 1]$  such that  $\alpha 1 > \alpha 2$ , then:
  - $A_{\alpha 1} \subset A_{\alpha 2}$  and  $A_{\alpha 1^+} \subset A_{\alpha 2^+}$
  - $(A_{\alpha 1} \cap A_{\alpha 2}) = A_{\alpha 1}$  and  $(A_{\alpha 1^+} \cap A_{\alpha 2^+}) = A_{\alpha 1^+}$
  - $(A_{\alpha 1} \cup A_{\alpha 2}) = A_{\alpha 2}$  and  $(A_{\alpha 1^{+}} \cup A_{\alpha 2^{+}}) = A_{\alpha 2^{+}}$



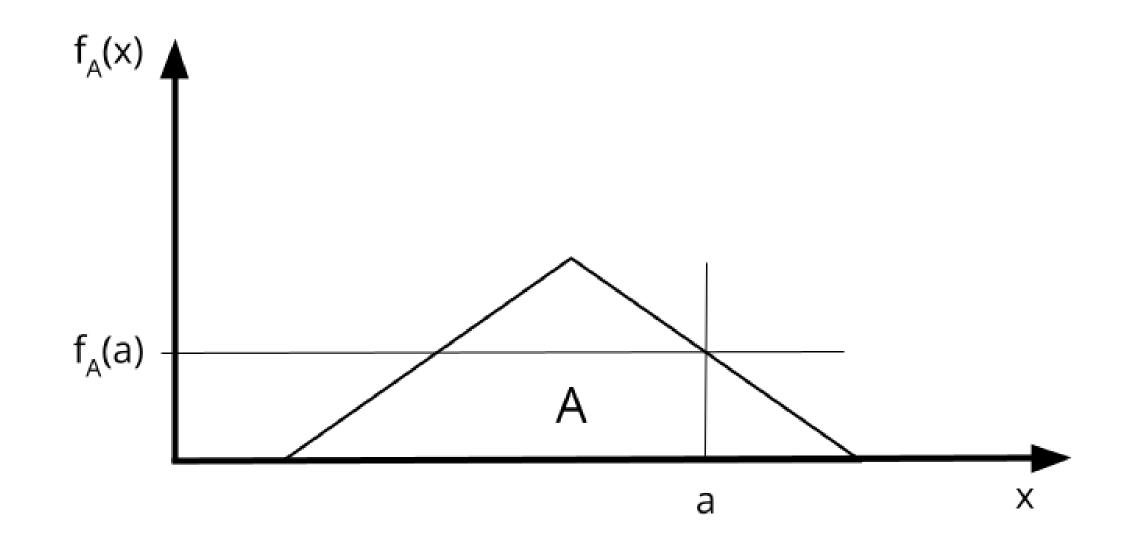
#### Membership functions

- It is defined through fuzzy sets notation, therefore, it can be either discrete or continuous.
- For example:

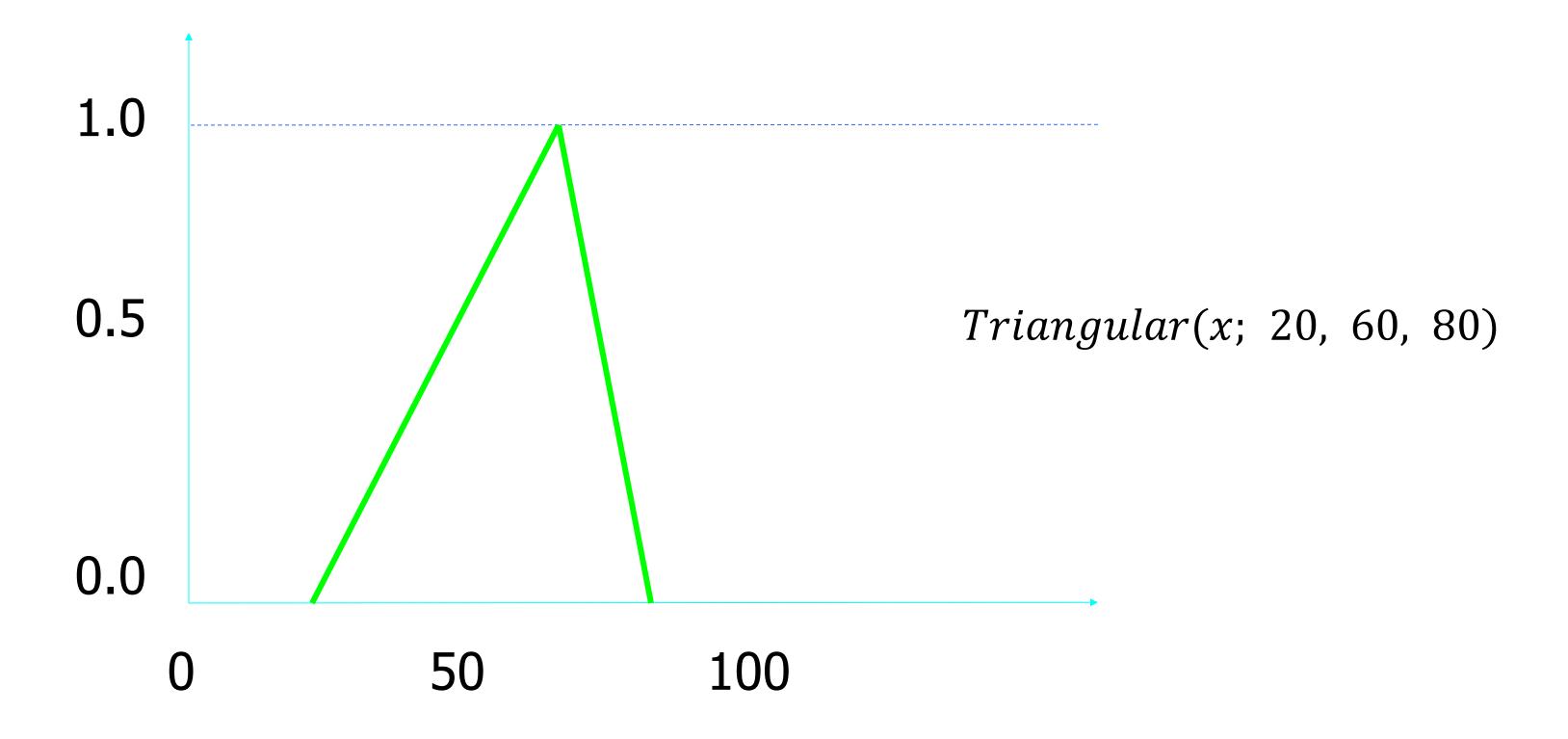


#### Membership functions

- If  $f_A(x)$  denotes the membership function of x to set A, then:
  - $f_A(x)$  is a value between 0 and 1.
  - if  $f_A(x) = 1$ , x belongs completely to A.
  - if  $f_A(x) = 0$ , x does not belong to A.
- From this definition, it is possible to verify the following properties:
  - $f_{A \text{ or } B}(x) = \max(f_{A}(x), f_{B}(x)).$
  - $f_{A \text{ and } B}(x) = \min(f_A(x), f_B(x)).$
  - $f_{\text{nor }A}(x) = 1 f_A(x)$

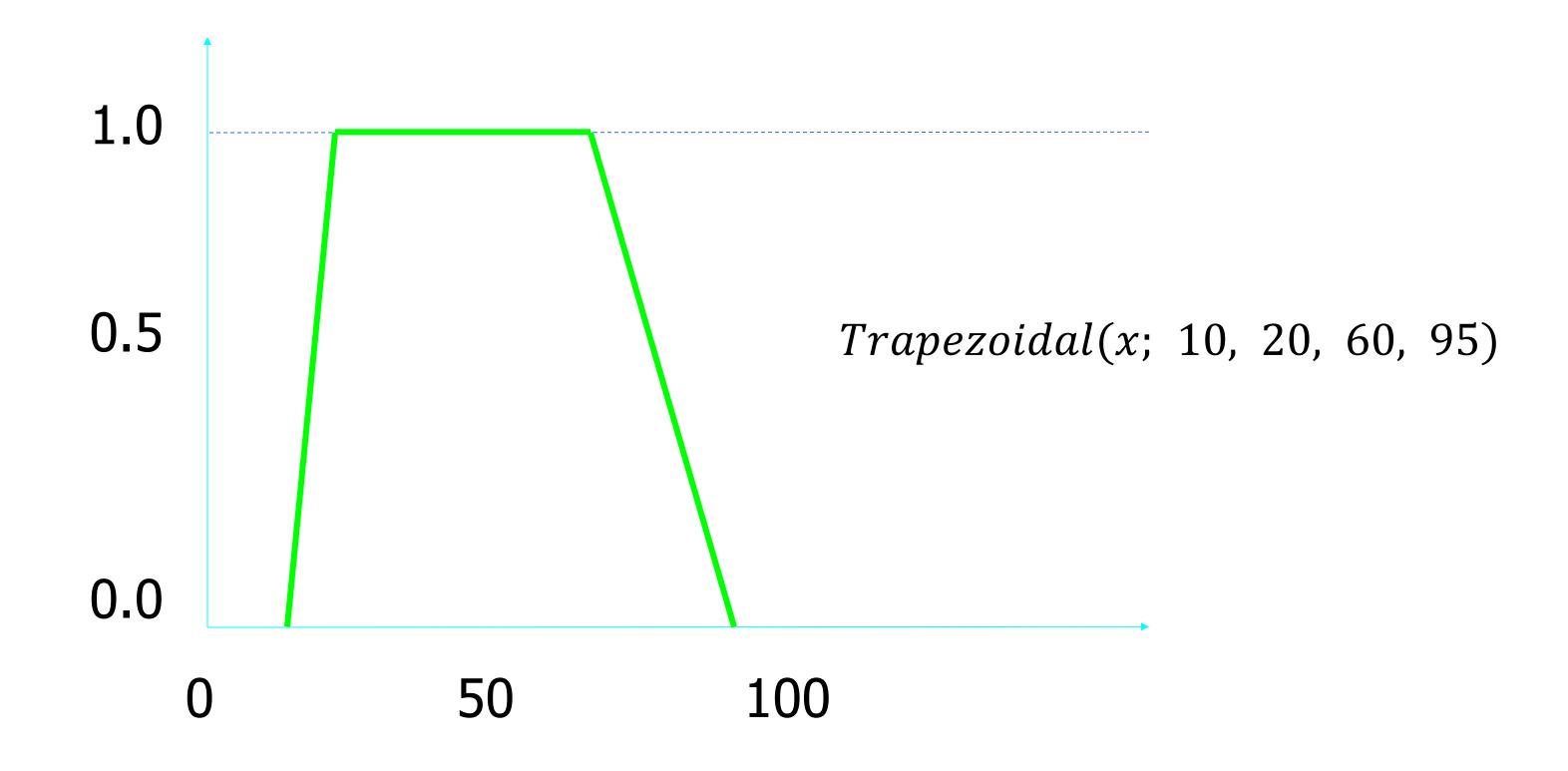


#### Membership functions: Triangular



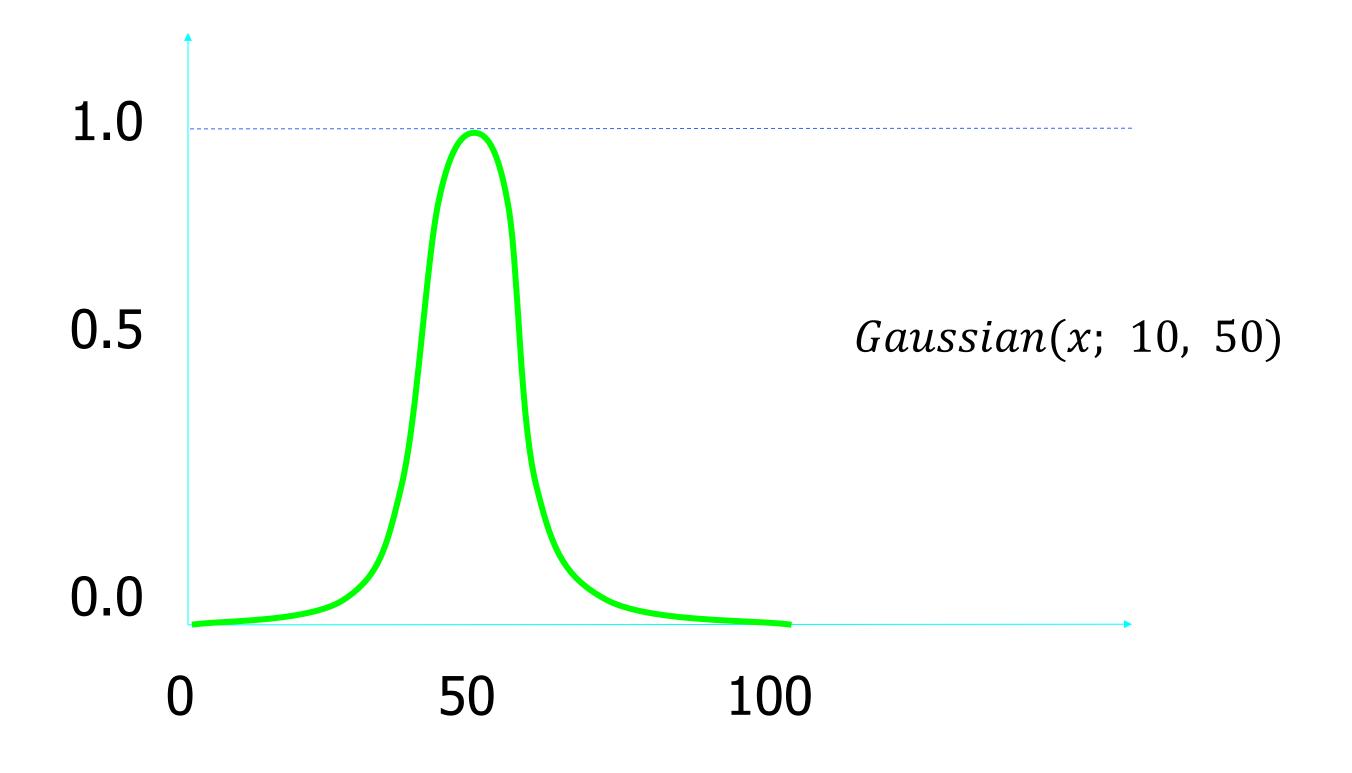
$$Triangular(x; a, b, c) = max \left( min \left( \frac{x - a}{b - a}, \frac{c - x}{c - b} \right), 0 \right)$$

#### Membership functions: Trapezoidal



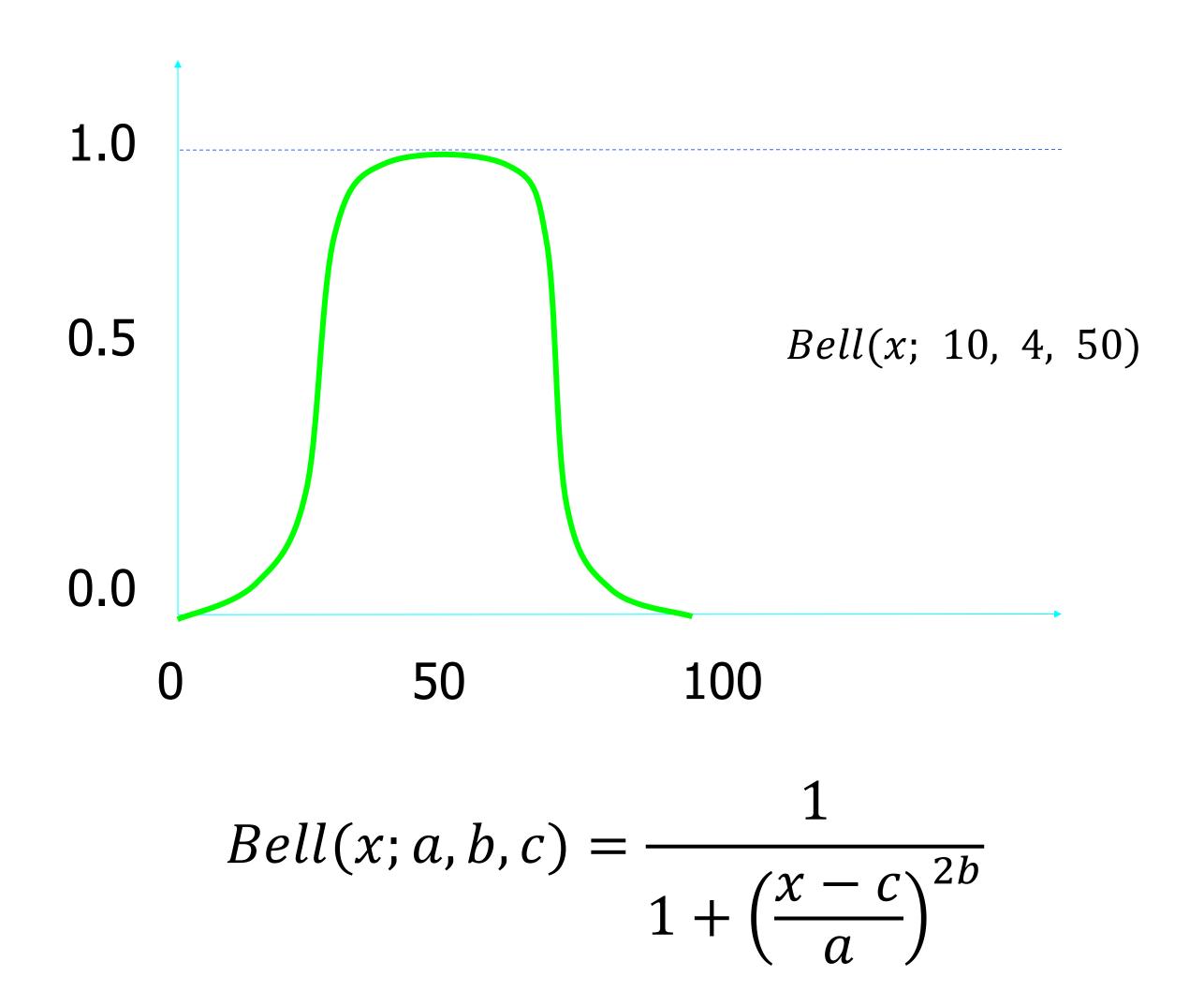
$$Trapezoidal(x; a, b, c, d) = max \left( min \left( \frac{x - a}{b - a}, 1, \frac{d - x}{d - c} \right), 0 \right)$$

#### Membership functions: Gaussian

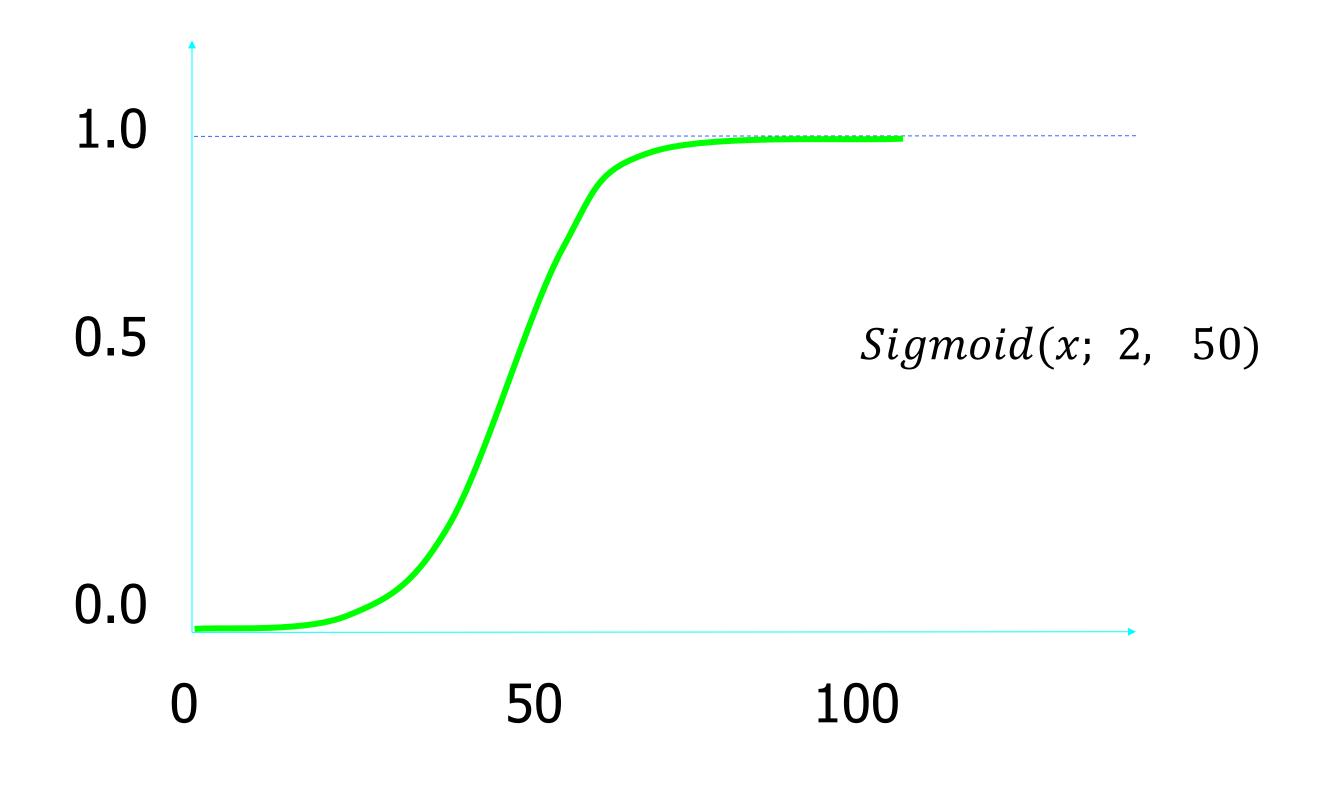


$$Gaussian(x; \sigma, c) = e^{-\left(\frac{x-c}{\sigma}\right)^2}$$

#### Membership functions: Bell-shaped



#### Membership functions: Sigmoid



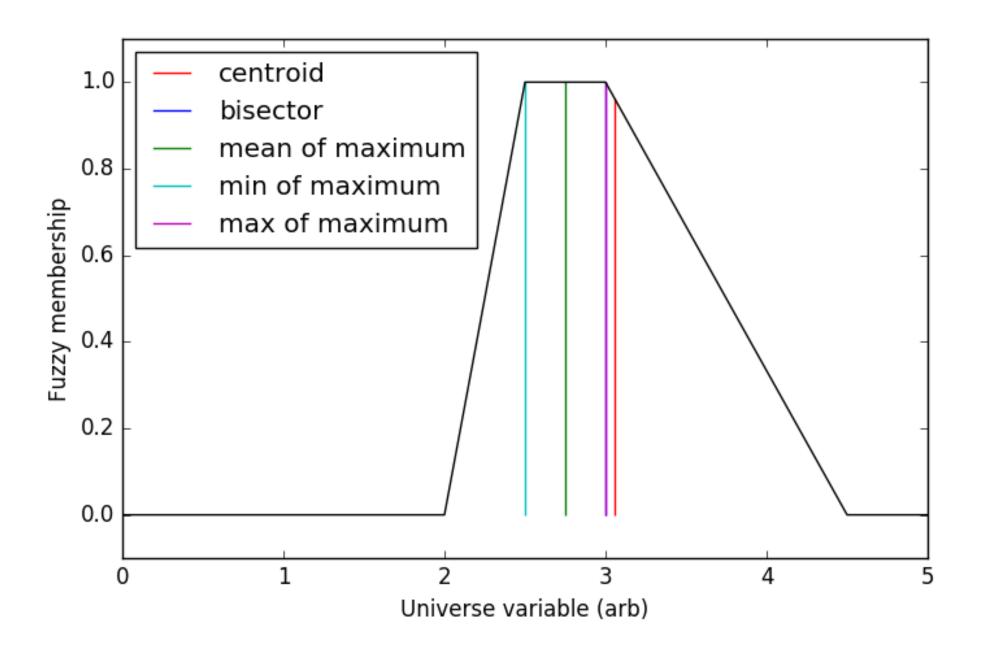
$$Sigmoid(x; a, c) = \frac{1}{1 + e^{-a(x-c)}}$$

#### Rules

- Rules are expressed in terms of linguistic variables as IF x is A THEN y is B
- Logic operators can be used, and the following properties apply:
  - $f_{A \text{ or } B}(x) = \max(f_{A}(x), f_{B}(x)).$
  - $f_{A \text{ and } B}(x) = \min(f_A(x), f_B(x)).$
  - $f_{nor A}(x) = 1 f_A(x)$
- For example:
  - IF the speed is high and the temperature is high, THEN the fuel injection should be low.
  - IF the food is delicious or the service excellent, THEN the tip should be generous.

#### Defuzzification

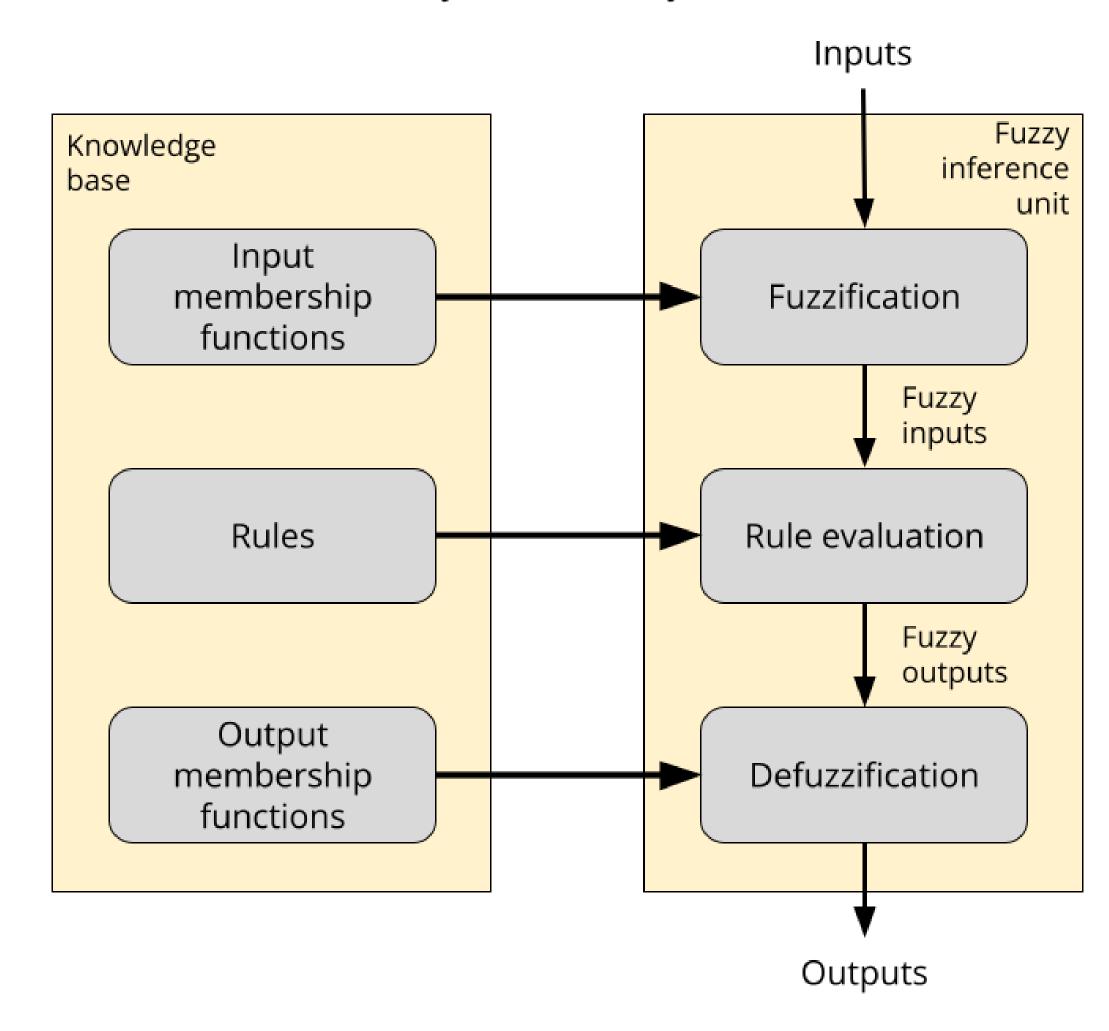
- The area for the resultant consequent should be converted from fuzzy to crisp, i.e., a quantifiable result.
- There are different methods for defuzzification, for instance, the ones implemented in scikit-fuzzy (a.k.a. skfuzzy) are: centroid, bisector, mean of maximum, min of maximum, max of maximum.



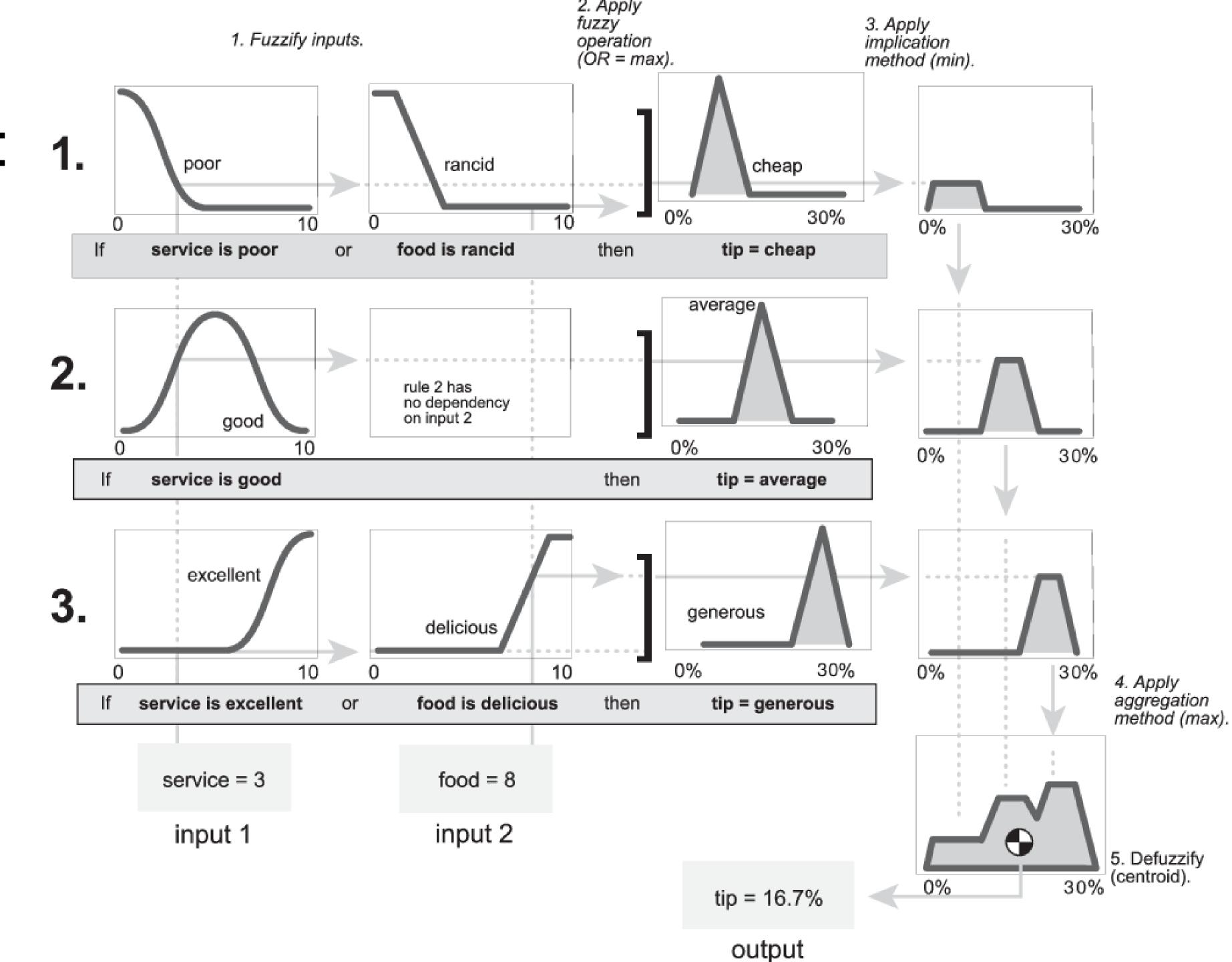
#### Fuzzy Inference

#### Fuzzy Inference System

- Mapping from given inputs to a crisp output using fuzzy logic is known as fuzzy inference.
- Inputs are crisp values and go through a fuzzification process (from input membership functions).
- Rules are evaluated as linguistic variables using IF-THEN structures.
- Output memberships functions establish the outputs area which is defuzzified using methods such as centroid.



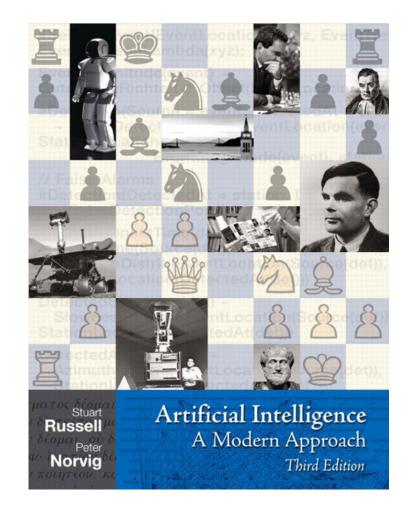
# Fuzzy Inference: 1. The Tipping Problem\*

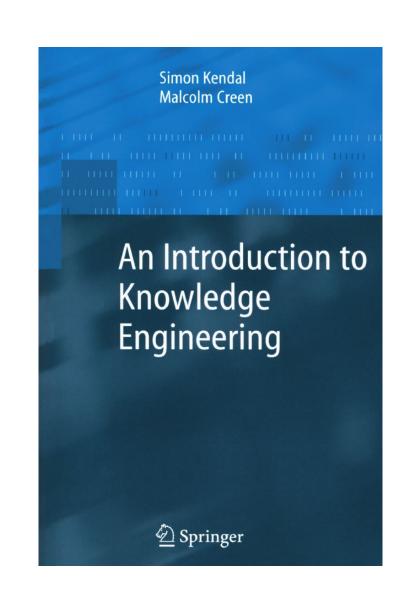


<sup>\*</sup>Image from MathWorks

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Articles

...making
Bayesian
networks more
accessible to
the probabilistically

Al Magazine Volume 12 Number 4 (1991) (© AAAI)

Bayesian Networks
without Tears

Eugene Charniak

vears, a method of reasoning using probabilities, variously called belief networks, Bayeslan networks, Bayeslan networks, and so on, has become popular within the Al probability and uncertainty community. Nevertheless, despite what seems to be their obvious importance, the ideas and techniques have not spread much beyond the resourch community. This method is best summarized in Judea Pearl's (1988) book, but the ideas are a product of many hands. I adopted Pearl's name, Bayeslan networks, or and so many the ideas are a product of many hands. I adopted Pearl's name, Bayeslan networks or the grounds that the name is completely neutral about the status of the networks of the probability and uncertain networks have been applied to problems in medical diagnosis (Heckerman 1990; Splegel-halter, Franklin, and Bull 1989), map learning (Dean 1990), language

#### Feedback

 In case you want to provide anonymous feedback on these lectures, please visit:

• https://forms.gle/KBkN744QuffuAZLF8

Muchas gracias!



