

# COMP9444: Neural Networks and Deep Learning

Week 3b. Hidden Unit Dynamics

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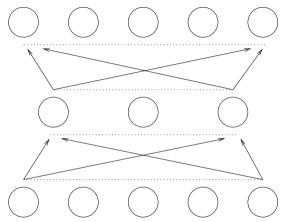
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#### **Outline**

- → geometry of hidden unit activations
- → limitations of 2-layer networks
- → vanishing/exploding gradients
- → alternative activation functions
- → ways to avoid overfitting in neural networks



#### **Encoder Networks**



Inputs	Outputs
10000	10000
01000	01000
00100	00100
00010	00010
00001	00001

- → identity mapping through a bottleneck
- → also called N-M-N task
- → used to investigate hidden unit representations

## N-2-N Encoder

Hidden Unit Space:



#### 8-3-8 Encoder

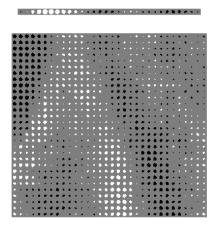
#### Exercise:

- → Draw the hidden unit space for 2-2-2, 3-2-3, 4-2-4 and 5-2-5 encoders.
- Represent the input-to-hidden weights for each input unit by a point, and the hidden-to-output weights for each output unit by a line.
- → Now consider the 8-3-8 encoder with its 3-dimensional hidden unit space.
  - → what shape would be formed by the 8 points representing the input-to-hidden weights for the 8 input units?
  - → what shape would be formed by the planes representing the hidden-to-output weights for each output unit?

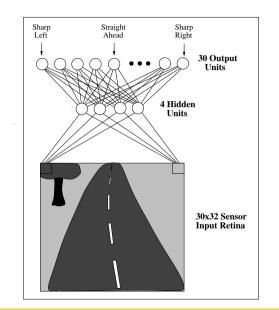
Hint: think of two platonic solids, which are "dual" to each other.



## **Hinton Diagrams**



- → used to visualize higher dimensions
- → white = positive, black = negative



# **Learning Face Direction**







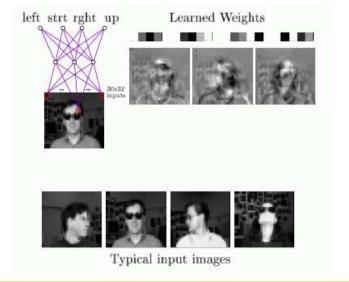




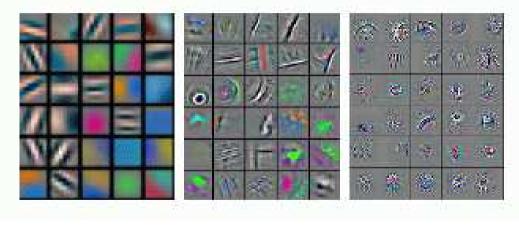
Typical input images



## **Learning Face Direction**



#### **Convolutional Filters**



First Layer

Second Layer

Third Layer



# Weight Space Symmetry

- → swap any pair of hidden nodes, overall function will be the same
- → on any hidden node, reverse the sign of all incoming and outgoing weights (assuming symmetric transfer function)
- → hidden nodes with identical input-to-hidden weights in theory would never separate; so, they all have to begin with different random weights
- → in practice, all hidden nodes may try to do similar job at first, then gradually specialize.



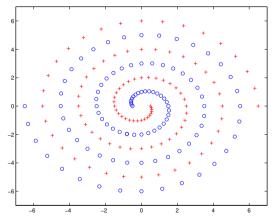
# **Controlled Nonlinearity**

- → for small weights, each layer implements an approximately linear function, so multiple layers also implement an approximately linear function.
- → for large weights, transfer function approximates a step function, so computation becomes digital and learning becomes very slow.
- → with typical weight values, two-layer neural network implements a function which is close to linear, but takes advantage of a limited degree of nonlinearity.



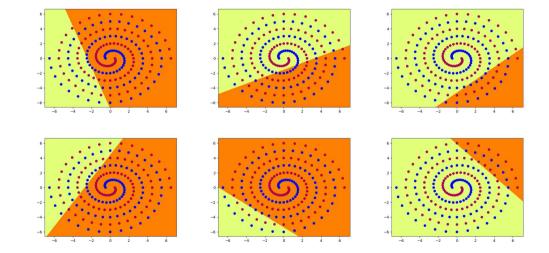
# **Limitations of Two-Layer Neural Networks**

Some functions are difficult for a 2-layer network to learn.



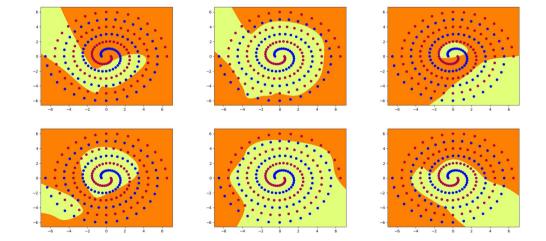
For example, this Twin Spirals problem is difficult to learn with a 2-layer network, but it can be learned using a 3-layer network.

# First Hidden Layer



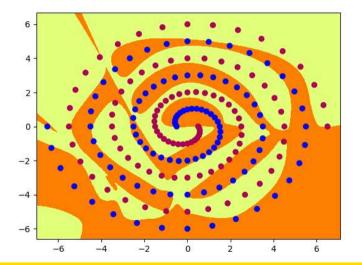


# **Second Hidden Layer**





# **Network Output**



## **Adding Hidden Layers**

- → twin spirals can be learned by 3-layer network
- → first hidden layer learns linearly separable features
- → second hidden layer combines these to produce more complex features
- learning rate and initial weight values must be small
- → learning can be improved using the Adam optimizer



## Vanishing / Exploding Gradients

- → training by backpropagation in networks with many layers is difficult
- when the weights are small, the differentials become smaller and smaller as we backpropagate through the layers, and end up having no effect
- → when the weights are large, the activations in the higher layers may saturate to extreme values
- when the weights are large, the differentials may sometimes get multiplied twice in succession in places where the transfer function is steep, causing them to blow up to large values



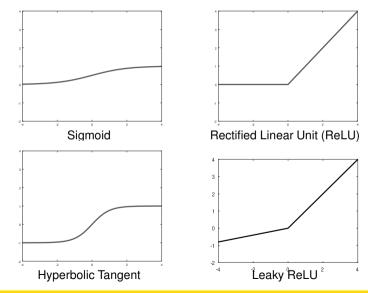
## **Vanishing / Exploding Gradients**

Ways to avoid vanishing / exploding gradients:

- new activations functions
- → weight initialization (Week 4)
- → batch normalization (Week 4)
- → skip connections (Week 4)
- → long short term memory (LSTM) (Week 5)



## **Activation Functions**





#### **Activation Functions**

- → sigmoid and hyperbolic tangent traditionally used for 2-layer networks, but suffer from vanishing gradient problem in deeper networks.
- → rectified linear units (ReLUs) are popular for deep networks (including convolutional networks); gradients will not vanish because derivative is either 0 or 1.

