Text_analysis Pierre Massé June 11, 2020

1 Préambule

1.1 Imports

```
[1]: # setting up sys.path for relative imports
       from pathlib import Path
       import sys
       project_root = str(Path(sys.path[0]).parents[1].absolute())
       if project_root not in sys.path:
            sys.path.append(project_root)
[201]: # imports and customization of diplay
       import os
       from functools import partial
       from collections import defaultdict
       import re
       import numpy as np
       from scipy.stats import linregress
       import pandas as pd
       pd.options.display.min_rows = 6
       {\tt pd.options.display.width=} 108
       from sklearn.feature_extraction.text import CountVectorizer
       from sklearn.feature_extraction.text import TfidfVectorizer
       from sklearn.base import clone
       from sklearn.model_selection import train_test_split
       from sklearn.model_selection import cross_val_score, cross_validate
       from sklearn.pipeline import Pipeline
       {\tt from \ sklearn.decomposition \ import \ Truncated SVD}
       from sklearn.decomposition import PCA
       from sklearn.manifold import Isomap
       from sklearn.preprocessing import StandardScaler
       from gensim.models import word2vec
       from matplotlib import pyplot as plt
       import matplotlib.patches as mpatch
       import matplotlib.cm as cm
       import matplotlib.colors as colors
       from matplotlib.colors import Normalize
       import matplotlib.ticker as mtick
       import seaborn as sns
       from src.pimest import ContentGetter
       from src.pimest import PathGetter
       from src.pimest import PDFContentParser
       from src.pimest import BlockSplitter
       from src.pimest import SimilaritySelector
       from src.pimest import custom_accuracy
       from src.pimest import text_sim_score
       from src.pimest import text_similarity
       from src.pimest import build_text_processor
```

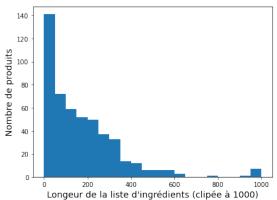
1.2 Acquisition des données de la ground truth

```
ground_truth_path=Path('..') / '..' / 'ground_truth',
                                                                                                                                   )).
                                                                      ('ContentGetter', ContentGetter(missing_file='to_nan')),
                                                                     ('ContentParser', PDFContentParser(none_content='to_empty')),
                                                                   ],
                                                                   verbose=True)
            texts_df = acqui_pipe.fit_transform(ground_truth_df)
            texts_df['ingredients'] = texts_df['ingredients'].fillna('')
            texts_df
           [Pipeline] ... (step 1 of 3) Processing PathGetter, total= 0.1s
           [Pipeline] ... (step 2 of 3) Processing ContentGetter, total= 0.1s
          Launching 8 processes.
           [Pipeline] ... (step 3 of 3) Processing ContentParser, total= 39.1s
[4]:
                                                                                                                                                                                               designation \
            nid
            a0492df6-9c76-4303-8813-65ec5ccbfa70
                                                                                                       Concentré liquide Asian en bouteille 980 ml CHEF
            d183e914-db2f-4e2f-863a-a3b2d054c0b8
                                                                                                                                  Pain burger curry 80 g CREATIV BURGER
            ab48a1ed-7a3d-4686-bb6d-ab4f367cada8
                                                                                                                                              Macaroni en sachet 500 g PANZANI
            e67341d8-350f-46f4-9154-4dbbb8035621
                                                                                                                                     PRÉPARATION POUR CRÈME BRÛLÉE BIO 6L
            a8f6f672-20ac-4ff8-a8f2-3bc4306c8df3 Céréales instantanées en poudre saveur caramel...
                                                                                                                                                         FARINE DE BLÉ TYPE 45, 10KG
            Ofaad739-ea8c-4f03-b62e-51ee592a0546
                                                                                                                                                                                               ingredients \
            uid
            a0492df6-9c76-4303-8813-65ec5ccbfa70 Eau, maltodextrine, sel, arômes, sucre, arôme …
            d183e914-db2f-4e2f-863a-a3b2d054c0b8 Farine de blé T65, eau, levure, vinaigre de ci…
                                                                                                      - 100% Semoule de BLE dur de qualité supérieur...
            ab48a1ed-7a3d-4686-bb6d-ab4f367cada8
            e67341d8-350f-46f4-9154-4dbb8035621 Sucre roux de canne*° (64%), amidon de maïs*, ...
            a8f6f672-20ac-4ff8-a8f2-3bc4306c8df3
                                                                                                     Farine 87,1 % (Blé (GLUTEN), Blé hydrolysé (GL...
            Ofaad739-ea8c-4f03-b62e-51ee592a0546
                                                                                                                                                                                 Farine de blé T45
                                                                                                                                                                                                                path \
            uid
            a0492df6-9c76-4303-8813-65ec5ccbfa70 ../../ground_truth/a0492df6-9c76-4303-8813-65e...
            d183e914-db2f-4e2f-863a-a3b2d054c0b8 ../../ground_truth/d183e914-db2f-4e2f-863a-a3b...
            \verb|ab48a1ed-7a3d-4686-bb6d-ab4f367cada8| ... / ... / ground\_truth / ab48a1ed-7a3d-4686-bb6d-ab4... |
            \tt e67341d8-350f-46f4-9154-4dbb8035621 \dots / \dots / ground\_truth / e67341d8-350f-46f4-9154-4db \dots / ground\_truth / e67341d8-
                                                                                                     ../../ground_truth/a8f6f672-20ac-4ff8-a8f2-3bc...
            a8f6f672-20ac-4ff8-a8f2-3bc4306c8df3
            Ofaad739-ea8c-4f03-b62e-51ee592a0546 ../../ground_truth/Ofaad739-ea8c-4f03-b62e-51e...
            uid
            a0492df6-9c76-4303-8813-65ec5ccbfa70 b'%PDF-1.5\r\n%\xb5\xb5\xb5\xb5\r\n1 0 obj\r\n...
             \tt d183e914-db2f-4e2f-863a-a3b2d054c0b8 \quad b'\%PDF-1.5\r\%\xe2\xe3\xcf\xd3\r\n4 \ 0 \ obj\r'<</L... }
            \verb|ab48a1ed-7a3d-4686-bb6d-ab4f367cada8| b'%PDF-1.4\n%\xc7\xec\x8f\xa2\n5| 0 obj\n<</li>
            \tt e67341d8-350f-46f4-9154-4dbbb8035621 b'\%PDF-1.7\r\n\%\xb5\xb5\xb5\r\n1 0 obj\r\n...
            a8f6f672-20ac-4ff8-a8f2-3bc4306c8df3 b'%PDF-1.5\r\n%\xb5\xb5\xb5\xb5\r\n1 0 obj\r\n...
            0 faad 739 - ea8c - 4f03 - b62e - 51ee592a0546 \\ b'\%PDF - 1.5 \\ r\n\% \\ xb5 \\ xb5 \\ xb5 \\ r\n1 \\ 0 \\ obj \\ r\n...
            a0492df6-9c76-4303-8813-65ec5ccbfa70 Concentré Liquide Asian CHEF® \n\nBouteille de...
            d183e914-db2f-4e2f-863a-a3b2d054c0b8
            \verb|ab48a1ed-7a3d-4686-bb6d-ab4f367| cada8 | | \textit{Direction Qualité } n\n \\ | n\n \n \\ | n\n \n \\ | n\n \n \\ | n\n \n \\ | n\n \
            e67341d8-350f-46f4-9154-4dbbb8035621 FICHE TECHNIQUE \n\nCREME BRÛLÉE 6L \n\nREF : ...
            a8f6f672-20ac-4ff8-a8f2-3bc4306c8df3 81 rue de Sans Souci - CS13754 - 69576 Limones...
                                                                                                        \n1050/10502066400 \n\n10502055300/1050202520...
            0faad739-ea8c-4f03-b62e-51ee592a0546
            [500 rows x 5 columns]
           On fusionne les corpus
[5]: target_df = texts_df['ingredients'].rename('text').to_frame()
            target_df.loc[:, 'source'] = 'target'
            content_df = texts_df['text'].to_frame()
            content_df['source'] = 'content'
            corpus_df = pd.concat([target_df, content_df])
            corpus_df = corpus_df.reset_index().set_index(['source', 'uid'])
corpus_df['text'].fillna('', inplace=True)
```

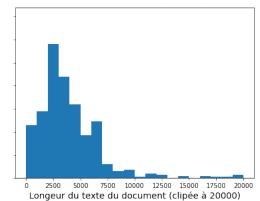
```
corpus_df
[5]:
                source uid
                                     a0492df6-9c76-4303-8813-65ec5ccbfa70
                target
                                                                                                                                                  Eau, maltodextrine, sel, arômes, sucre, arôme ...
                                      d183e914-db2f-4e2f-863a-a3b2d054c0b8 Farine de blé T65, eau, levure, vinaigre de ci...
                                      ab48a1ed-7a3d-4686-bb6d-ab4f367cada8
                                                                                                                                                   - 100% Semoule de BLE dur de qualité supérieur...
                \texttt{content} \ \ \texttt{e67341d8-350f-46f4-9154-4dbb8035621} \quad \texttt{FICHE} \ \ \texttt{TECHNIQUE} \ \ \texttt{n} \\ \texttt{nEME} \ \ \texttt{eL} \ \ \ \texttt{h} \\ \texttt{nREF} \ : \ \dots \\ \texttt{nMEF} \ : 
                                                                                                                                                  81 rue de Sans Souci - CS13754 - 69576 Limones...
                                      a8f6f672-20ac-4ff8-a8f2-3bc4306c8df3
                                      Ofaad739-ea8c-4f03-b62e-51ee592a0546
                                                                                                                                                     \n1050/10502066400 \n\n10502055300/1050202520...
                [1000 rows x 1 columns]
                              Analyses
                                  Analyse des longueurs des textes
[6]: lengths = corpus_df['text'].apply(len)
                print(
                lengths.reset_index()
                                       .groupby('source')
                                        .describe()
                                       .rename({'content': 'Texte des documents',
                                       'target': "Listes d'ingrédients"})
.to_latex(#Path('..') / 'tbls' / 'text_lengths.tex',
                                                                  bold_rows=True,
                                                                   column_format='lccccccc',
                                                                  index_names=False,
                lengths.reset_index().groupby('source').describe()
             \begin{tabular}{lccccccc}
             \toprule
             {} & \multicolumn{8}{1}{text} \\
             {} & count &
                                                                                                                                                                    25\% &
                                                                                                                                                                                                                                      75\% &
                                                                                                                std & min &
                                                                  mean &
             \midrule
             \textbf{Texte des documents} & 500.0 & 3937.630 & 3280.860732 & 0.0 & 2173.75 & 3247.5 & 5034.25 &
             \textbf{Listes d'ingrédients} & 500.0 & 199.686 & 457.044723 & 0.0 &
                                                                                                                                                                                                                                          43.00 & 122.0 & 250.75 &
             7963.0 \\
              \bottomrule
             \end{tabular}
[6]:
                                                                                                                std min
                                                                                                                                                        25%
                                                                                                                                                                               50%
                                                                                                                                                                                                          75%
                                         count
                                                                        mean
                content 500.0 3937.630 3280.860732 0.0 2173.75 3247.5 5034.25 37322.0
                target 500.0 199.686 457.044723 0.0
                                                                                                                                                  43.00
                                                                                                                                                                      122.0 250.75
[7]: fig, axs = plt.subplots(ncols=2, figsize=(15, 5), sharey=True)
                axs[0].hist(lengths.loc['target'].clip(0, 1000), bins=20)
                axs[0].set_title("Listes d'ingrédients par longueur", fontsize=16, pad=15)
axs[0].set_ylabel("Nombre de produits", fontsize=14)
axs[0].set_xlabel("Longeur de la liste d'ingrédients (clipée à 1000)", fontsize=14)
                axs[1].hist(lengths.loc['content'].clip(0, 20000), bins=20)
```

axs[1].set_title("Contenu des documents par longueur", fontsize=16, pad=15)
axs[1].set_xlabel("Longeur du texte du document (clipée à 20000)", fontsize=14)
fig.savefig(Path('..') / 'img' / 'text_lengths.png', bbox_inches='tight')





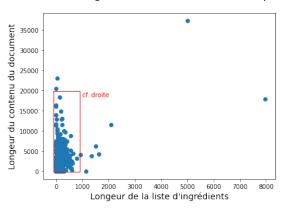
Contenu des documents par longueur

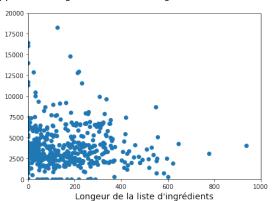


```
fig, axs = plt.subplots(ncols=2, figsize=(15, 5))

axs[0].scatter(x=lengths.loc['target'], y=lengths.loc['content'])
axs[0].set_xlabel("Longeur de la liste d'ingrédients", fontsize=14)
axs[0].set_ylabel("Longeur du contenu du document", fontsize=14)
axs[0].add_patch(mpatch.Rectangle((-100, -150), 1000, 20000, fill=False, color='red'))
axs[0].annotate('cf. droite', (1000, 18500), color='red')
axs[1].scatter(x=lengths.loc['target'], y=lengths.loc['content'])
axs[1].set_xlabel("Longeur de la liste d'ingrédients", fontsize=14)
axs[1].set_xlim(0, 10000)
axs[1].set_ylim(0, 20000)
fig.suptitle("Longeur du contenu des documents par rapport à la longueur des listes d'ingrédients", fontsize=16)
# fig.savefig(Path('..') / 'img' / 'text_lengths_2.png', bbox_inches='tight')
```

Longueur du contenu des documents par rapport à la longueur des listes d'ingrédients





```
[9]: linregress(x=lengths.loc['target'], y=lengths.loc['content']).rvalue ** 2
```

[9]: 0.139326761283587

2.2 Analyse des mots

```
[11]: tfidf_corpus = TfidfVectorizer(strip_accents='unicode',
                                      lowercase=True,
                                      stop_words=stop_words,
                                      ngram_range=(1, 1),
                                      max_df=1.0,
                                       \#min\_df=0.0, A TESTER !
                                      binary=False,
                                      norm=None, # set to l1 or l2
                                      use_idf=False,
                                      smooth_idf=False,
                                      sublinear_tf=False,
      vectorized_corpus = tfidf_corpus.fit_transform(corpus_df['text'])
      tokenizer = tfidf_corpus.build_analyzer()
     Comptage des mots du vocabulaire du corpus :
[12]: inverse_corpus_voc = {val: key for key, val in tfidf_corpus.vocabulary_.items()}
      word_counts = np.asarray(vectorized_corpus.sum(axis=0)).squeeze()
print(f'Corpus vocabulary size is ', len(tfidf_corpus.vocabulary_), '\n')
      print('Most frequent words in vocabulary are:')
      most_freq = dict()
      for idx in word_counts.argsort()[::-1][:20]:
          most_freq[inverse_corpus_voc[idx].ljust(12)] = int(word_counts[idx])
          print(f'{inverse_corpus_voc[idx].ljust(12)}: {word_counts[idx]:5} occurences')
      str_cpt_corpus = [f'{word.ljust(12)}: {most_freq[word]} occurences \\\\' for word in most_freq.keys()]
     Corpus vocabulary size is 15465
     Most frequent words in vocabulary are:
     produit
                : 2198.0 occurences
     non
                  : 2164.0 occurences
     produits
                : 1508.0 occurences
                 : 1404.0 occurences
     10
                  : 1290.0 occurences
     kg
                 : 1119.0 occurences
     base
     sel
                 : 1041.0 occurences
     poids
                 : 1021.0 occurences
     100
                 : 971.0 occurences
     palette
                 : 933.0 occurences
     ingredients: 917.0 occurences
                 : 904.0 occurences
     date
                  : 841.0 occurences
     sucre
                 : 803.0 occurences
     12
     code
                 : 801.0 occurences
                 : 733.0 occurences
     lait.
     absence
                  : 697.0 occurences
     fiche
                 : 688.0 occurences
     the
                  : 658.0 occurences
     france
                  : 657.0 occurences
     Constitution du vocabulaire des listes d'ingrédients
[13]: tfidf_ingred = clone(tfidf_corpus)
      vectorized_ingred = tfidf_ingred.fit_transform(corpus_df.loc['target', 'text'])
[14]: inverse_ingred_voc = {val: key for key, val in tfidf_ingred.vocabulary_.items()}
      word_counts = np.asarray(vectorized_ingred.sum(axis=0)).squeeze()
      print(f'Ingredient vocabulary size is ', len(tfidf_ingred.vocabulary_), '\n')
      print('Most frequent words in vocabulary are:')
      most_freq = dict()
      for idx in word_counts.argsort()[::-1][:20]:
          most_freq[inverse_ingred_voc[idx].ljust(12)] = int(word_counts[idx])
          print(f'{inverse_ingred_voc[idx].ljust(10)}: {word_counts[idx]:5} occurences')
      str_cpt_corpus_2 = [f'{word.ljust(12)}: {most_freq[word]} occurences &' for word in most_freq.keys()]
      str_latex = '\n'.join([str2 + ' ' + str1 for str1, str2 in zip(str_cpt_corpus, str_cpt_corpus_2)])
      #print(str_latex)
     Ingredient vocabulary size is 1324
     Most frequent words in vocabulary are:
     sucre
               : 363.0 occurences
     acide
               : 255.0 occurences
     sel
               : 240.0 occurences
               : 180.0 occurences
     sirop
               : 178.0 occurences
     eau
```

```
poudre
         : 176.0 occurences
         : 175.0 occurences
arome
lait
         : 171.0 occurences
         : 171.0 occurences
ble
huile
         : 146.0 occurences
citrique : 132.0 occurences
         : 128.0 occurences
farine
         : 125.0 occurences
amidon
glucose
         : 124.0 occurences
cacao
         : 122.0 occurences
extrait : 117.0 occurences
acidifiant: 114.0 occurences
        : 98.0 occurences
aromes
soja
         : 96.0 occurences
concentre: 92.0 occurences
```

On vérifie s'il existe des mots qui sont inclus dans les listes d'ingrédients mais pas dans les documents :

```
[15]: ingred_only = {word for word in tfidf_ingred.vocabulary_ if word not in tfidf_corpus.vocabulary_}
ingred_only
```

[15]: set()

Constitution d'une nouvelle feature qui sont les textes tokenisés via la méthode du CountVectorizer.

```
[16]: corpus_df['tokenized'] = corpus_df['text'].apply(tokenizer)
corpus_df
```

```
[16]:
                                                                                                   text \
      source uid
      target a0492df6-9c76-4303-8813-65ec5ccbfa70 Eau, maltodextrine, sel, arômes, sucre, arôme ...
              d183e914-db2f-4e2f-863a-a3b2d054c0b8 Farine de blé T65, eau, levure, vinaigre de ci...
              ab48a1ed-7a3d-4686-bb6d-ab4f367cada8 - 100% Semoule de BLE dur de qualité supérieur...
      content e67341d8-350f-46f4-9154-4dbbb8035621 FICHE TECHNIQUE \n\nCREME BRÛLÉE 6L \n\nREF : ...
              a8f6f672-20ac-4ff8-a8f2-3bc4306c8df3 81 rue de Sans Souci - CS13754 - 69576 Limones...
                                                      \n1050/10502066400 \n\n10502055300/1050202520...
              Ofaad739-ea8c-4f03-b62e-51ee592a0546
      source uid
      target a0492df6-9c76-4303-8813-65ec5ccbfa70 [eau, maltodextrine, sel, aromes, sucre, arome...
              d183e914-db2f-4e2f-863a-a3b2d054c0b8
                                                     [farine, ble, t65, eau, levure, vinaigre, cidr...
              ab48a1ed-7a3d-4686-bb6d-ab4f367cada8
                                                     [100, semoule, ble, dur, qualite, superieure, ...
      content e67341d8-350f-46f4-9154-4dbbb8035621
                                                     [fiche, technique, creme, brulee, 61, ref, nap...
              a8f6f672-20ac-4ff8-a8f2-3bc4306c8df3
                                                     [81, rue, sans, souci, cs13754, 69576, limones...
              Ofaad739-ea8c-4f03-b62e-51ee592a0546
                                                     [1050, 10502066400, 10502055300, 10502025200, ...
      [1000 rows x 2 columns]
```

3 Analyse de données

4 Représentation des mots

4.1 Document frequency

1- Déjà, on calcule une métrique qui permet de dire si un mot est plutôt un mot de type ingrédients ou un mot issu du corpus.

Représentation simple : on regarde simplement la document frequency de chacun des mots dans le corpus des ingrédients.

```
[17]: doc_freq_counter = clone(tfidf_ingred)
doc_freq_counter.set_params(binary=True).fit(corpus_df.loc['target', 'text'])
binary_ingred_counts = doc_freq_counter.transform(corpus_df.loc[:, 'text'])
```

```
shape of doc_freq_ingred : (1324,)
0.448
0.0
0.064
```

On constitue un array qui nous servira plus tard, avec le document frequency dans les ingrédients de tous les mots utilisés dans le contenu des documents.

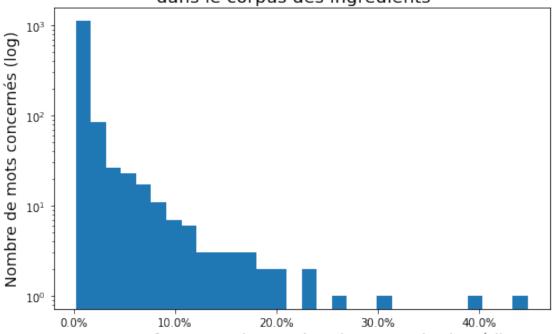
```
[19]: corpus_doc_freq_ingred = np.zeros(shape=(len(tfidf_corpus.vocabulary_)))
    for i in range(len(tfidf_corpus.vocabulary_)):
        corpus_doc_freq_ingred[i] = doc_freq_ingred_translator[inverse_corpus_voc[i]]
        corpus_doc_freq_ingred
```

```
[19]: array([0.004, 0. , 0. , ..., 0. , 0. , 0. ])
```

On peut sortir les top scorer de la doc frequency :

```
[28]: fig, ax = plt.subplots(figsize=(8, 5))
    ax.hist(doc_freq_ingred, bins=30, log=True)
    ax.xaxis.set_major_formatter(mtick.PercentFormatter(xmax=1.))
    ax.set_xlabel("Document frequency du mot dans le corpus des ingrédients", fontsize=14)
    ax.set_ylabel("Nombre de mots concernés (log)", fontsize=14)
    fig.suptitle("Répartition des mots par documents frequency\ndans le corpus des ingrédients", fontsize=16)
    # fig.savefig(Path('..') / 'img' / 'doc_freq_of_ingreds.png', bbox_inches='tight')
```

Répartition des mots par documents frequency dans le corpus des ingrédients



Document frequency du mot dans le corpus des ingrédients

```
for word_idx in doc_freq_ingred.argsort()[::-1][:20]:
    print(inverse_ingred_voc[word_idx], '&', f'{doc_freq_ingred[word_idx]*100:.2f}\\%', '\\\')

for word_idx in doc_freq_ingred.argsort()[:20]:
    print(inverse_ingred_voc[word_idx], '&', f'{doc_freq_ingred[word_idx]*100:.2f}\\%', '\\\')

sucre & 44.80\% \\
```

sel & 40.00\% \\
sel & 40.00\% \\
eau & 30.20\% \\
acide & 26.20\% \\
arome & 23.00\% \\
huile & 23.00\% \\

```
ble & 20.60\% \\
      amidon & 20.00\% \\
      aromes & 19.00\% \\
      sirop & 18.40\% \\
      citrique & 18.00\% \\
      lait & 17.20\% \\
      acidifiant & 17.00\% \\
      farine & 16.40\% \\
      extrait & 16.20\% \\
      glucose & 16.00\% \\
      concentre & 14.80\% \\
      jus & 14.00\% \\
      poudre & 14.00\% \\
      colza & 13.20\% \\
      ferrique & 0.20\% \\
      d3 & 0.20\% \\
      datte & 0.20\% \\
      dattes & 0.20\% \\
      debris & 0.20\% \\
      decafeine & 0.20\% \
      deciree & 0.20\% \\
      deconseille & 0.20\% \\
      nectar & 0.20\% \\
      necessaire & 0.20\% \\
      ne & 0.20\% \\
      delta & 0.20\% \\
      naturelles & 0.20\% \\
      denoyautees & 0.20\% \\
      dentier & 0.20\% \\
      depellicule & 0.20\% \\
      cysteine & 0.20\% \
      negra & 0.20\% \\
      new & 0.20\% \\
      nicotinamide & 0.20\% \\
[309]: # looking for first word in documents but not in ingredients
       for word_idx in np.array(vectorized_corpus[500:].sum(axis=0)).reshape(15465).argsort()[::-1]:
           print(inverse_corpus_voc[word_idx])
            if inverse_corpus_voc[word_idx] not in tfidf_ingred.vocabulary_:
               print('trouvé !')
                break
      produit
      non
      produits
      10
      kg
      base
      poids
      trouvé !
 [75]: ingred_scores.shape
 [75]: (1324,)
[291]: ingred_scores = np.log2(doc_freq_ingred * 500 + 1)
       sample = doc_freq_ingred.argsort()[::-1][[0, 10, 100, 250, 702]]
       sample_scores = ingred_scores[sample]
       labels = [inverse_ingred_voc[word_idx] + f'\n{ingred_scores[word_idx]:.2f}' for word_idx in sample] + ['poids\n0.00']
       labels
[291]: ['sucre\n7.81'
         'citrique\n6.51',
         'issus\n4.39',
         'si\n2.81',
         'plantations\n1.58',
         'poids\n0.00']
[292]: gradient = np.linspace(0, 8, 256)
       gradient = np.vstack((gradient, gradient, gradient ))
       fig, ax = plt.subplots(figsize=(8, 3))
       ax.imshow(gradient, aspect=3, cmap='seismic', vmin=-8, vmax=8)
       {\tt ax.set\_xticks(np.hstack((255 \ / \ 8 \ * \ sample\_scores, \ np.array([0]))))}
```

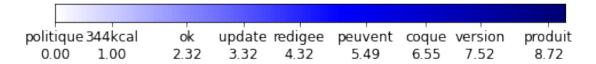
```
ax.set_xticklabels(labels, fontsize = 12)
#ax.set_xtim(0, 50)
ax.set_yticks([])
# fig.savefig(Path('..') / 'img' / 'scores_bar.png', bbox_inches='tight')
```

[292]: []



On calcule les document frequencies des mots issus des documents, et on compte sur les corpus.

```
[293]: doc_freq_counter_2 = clone(tfidf_corpus)
        doc_freq_counter_2.set_params(binary=False).fit(corpus_df.loc[: , 'text'])
        word_counts = np.array(doc_freq_counter_2.transform(corpus_df.loc[:, 'text']).todense())
        delta_doc_counts = (word_counts[500:] - word_counts[:500])
        binary_delta = np.where(delta_doc_counts > 0., np.ones(delta_doc_counts.shape), np.zeros(delta_doc_counts.shape))
docs_scores = np.log2(binary_delta.sum(axis=0) + 1)
[294]: docs_scores[tfidf_corpus.vocabulary_['produits']]
[294]: 8.005624549193879
[295]: sample = docs_scores.argsort()[::-1][[0, 90, 251, 550, 1200, 2200, 3803, 10005]]
        sample_scores = docs_scores[sample]
        labels = [inverse_corpus_voc[word_idx] + f'\n{docs_scores[word_idx]:.2f}' for word_idx in sample]
        labels
[295]: ['produit\n8.72',
          'version\n7.52',
         'coque\n6.55',
          'peuvent\n5.49',
          'redigee\n4.32',
          'update\n3.32'.
          'ok\n2.32',
          '344kcal\n1.00']
[298]: gradient = np.linspace(0, 8, 256)
        gradient = np.vstack((gradient, gradient, gradient ))
        fig, ax = plt.subplots(figsize=(8, 3))
        ax.imshow(gradient, aspect=3, cmap='seismic_r', vmin=-9, vmax=9)
ax.set_xticks(np.hstack((255 / 9 * sample_scores, np.array([0]))))
        ax.set_xticklabels(labels + ["politique\n0.00"], fontsize = 12)
        #ax.set_xlim(0, 50)
        ax.set_yticks([])
         \# \ fig.savefig(Path('..') \ / \ 'img' \ / \ 'corpus\_score\_bar.png', \ bbox\_inches='tight')
```



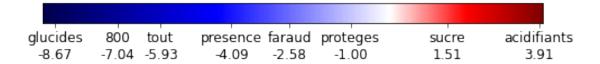
Et maintenant on calcule le score relatif de chacun des mots.

```
[299]: # new computation on ingredients, on corpus vocabulary indexing
binary_ingred = np.where(word_counts[:500] > 0., np.ones(word_counts[:500].shape), np.zeros(word_counts[:500].shape))
ingred_scores = np.log2(binary_ingred.sum(axis=0) + 1)
# check computation is coherent
print(ingred_scores[tfidf_corpus.vocabulary_['sucre']])
```

7.813781191217037

```
[300]: sample = np.hstack([relative_scores.argsort()[[0, 90, 251, 1200, 3000, 8007, 15464]], [14079]])
       sample_scores = relative_scores[sample]
       labels = [inverse_corpus_voc[word_idx] + f'\n{relative_scores[word_idx]:.2f}' for word_idx in sample]
       labels
[300]: ['glucides\n-8.67', '800\n-7.04'.
         'tout\n-5.93'
         'presence\n-4.09'.
         'faraud\n-2.58'.
         'proteges\n-1.00'
         'acidifiants\n3.91',
         'sucre\n1.51']
[301]: mmin, mmax, resolution = -9, 4, 1000
       divnorm = colors.TwoSlopeNorm(vmin=mmin, vcenter=0, vmax=mmax)
       gradient = np.linspace(mmin, mmax, resolution)
       gradient = np.vstack([gradient, gradient])
        # gradient = np.vstack([sorted(relative_scores), sorted(relative_scores)])
       def convert_to_width(num):
            return(int(resolution * (num - mmin) / (mmax - mmin)))
       fig, ax = plt.subplots(figsize=(8, 3))
       ax.imshow(gradient, aspect=20, cmap='seismic', norm=divnorm ) #, vmin=-9, vmax=9)
       ax.set_xticks(list(map(convert_to_width, sample_scores)))
       # ax.set_xticks(255 / 18 * sample_scores)
       ax.set_xticklabels(labels, fontsize = 12)
       #ax.set_xlim(0, 50)
       ax.set_yticks([])
       \# fig.savefig(Path('..') / 'img' / 'relative_score_bar.png', bbox_inches='tight')
```

[301]: []



4.2 Word embedings

4.2.1 Word2Vec

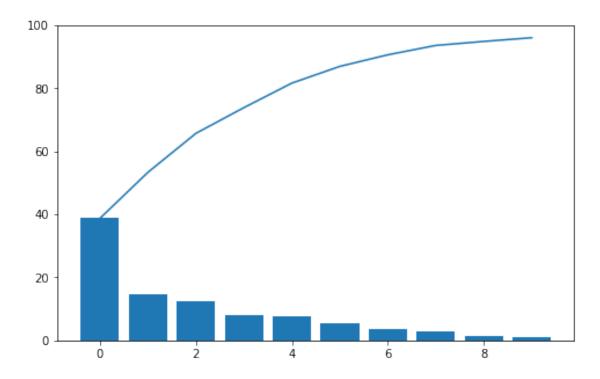
On calcule les embeddings avec Word2Vec

```
[265]: | ndarray_words_embeddings = np.vstack([word2vec_model.wv[inverse_corpus_voc[i]]
                                                             for i in range(len(tfidf_corpus.vocabulary_))])
          ndarray_words_embeddings
[265]: array([[-1.9143574e+00, -1.0786384e+00, -1.6952591e+00, ...,
                    2.1197143e-04, 6.8014598e-01, -9.4786072e-01], [-1.0596310e+00, -5.1570371e-02, -2.4971814e+00, ...,
                   -4.9154687e-01, 1.3782319e+00, -1.2871372e+00], [-2.1143033e-01, -1.3124047e-01, -2.7956560e-01, ..., -6.6144560e-03, 1.6432673e-02, -5.8027157e-03],
                   [-4.8991539e-02, -1.6540296e-02, -6.0264323e-02, ..., 3.1673540e-03, -9.9934675e-03, -1.2510464e-02],
                   3.16/3540e-03, -9.99346/5e-03, -1.2510464e-02],
[-8.2935727e-01, -6.4514387e-01, -8.7146807e-01, ...,
-1.7320616e-02, 3.3239821e-01, -3.0926281e-01],
[-2.5584301e-01, -1.5305966e-01, -5.1036954e-01, ...,
-1.5918270e-02, -3.0415934e-02, -2.4762219e-01]], dtype=float32)
         On effectue une PCA :
Г2661 :
          scaled_words_embeddings = StandardScaler().fit_transform(ndarray_words_embeddings)
          scaled_words_embeddings
4.966931 , -4.985649 ],
                   9.752907 , -0.29638907, -9.341663 , ..., -5.478642 , 9.752907 , -6.8654494 ], -0.92385375, -0.8646387 , -0.5741748 , ..., 0.06277785,
                       0.4166085 , 0.23393212],
                   ...,
[ 0.01353529, -0.04653592, 0.29284707, ..., 0.17455655,
                       0.23543474, 0.19676708],
                                                            -2.9142997 , ..., -0.05956358,
                    [ -4.489738 , -4.5300717
                   2.582823 , -1.4474237 ],

[-1.180147 , -1.0202649 , -1.4866732 , ..., -0.04353869,

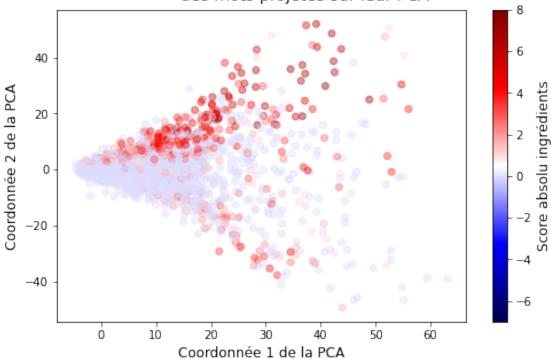
0.09542128, -1.1058966 ]], dtype=float32)
[267]: PCA_model = PCA(n_components=10)
          PCA_words_embeddings = PCA_model.fit_transform(scaled_words_embeddings)
          print(PCA_words_embeddings.shape)
         (15465, 10)
[268]: fig, ax = plt.subplots(figsize=(8, 5))
          ax.plot(PCA_model.explained_variance_ratio_.cumsum()*100)
          ax.bar(x=range(10), height=PCA_model.explained_variance_ratio_*100)
          ax.set_ylim(0, 100)
```

[268]: (0.0, 100.0)

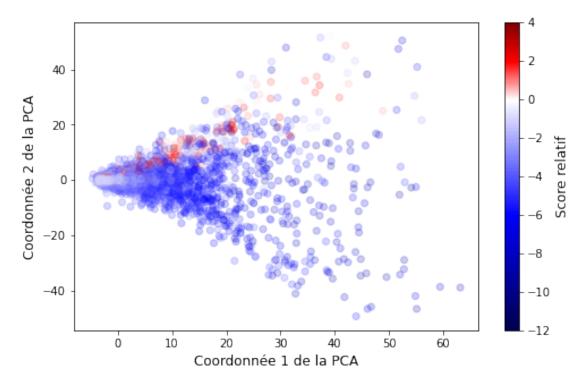


On la dessine :

Scores absolus des embeddings Word2Vec des mots projetés sur leur PCA



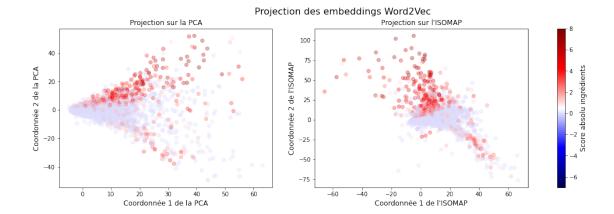
Scores relatifs des Word2Vec des mots projetés sur leur PCA



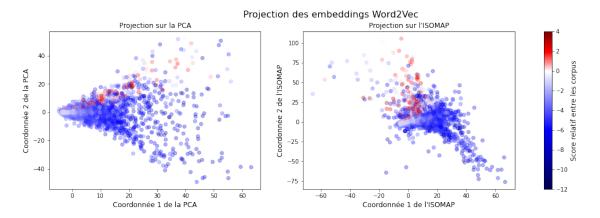
```
[275]: isomap_model = Isomap(n_neighbors=5, n_components=2, n_jobs=8) isomap_words_embeddings = isomap_model.fit_transform(scaled_words_embeddings) print(isomap_words_embeddings.shape)
```

(15465, 2)

```
[309]:
         fig, axs = plt.subplots(ncols=2, figsize=(18, 5))
          scat = axs[0].scatter(x=PCA_words_embeddings[:, 0],
                                      y=PCA_words_embeddings[:, 1],
                                      alpha=0.3,
                                      cmap='seismic',
                                       vmin=-7,
                                      vmax=8,
                                      c=np.log2(500 * corpus_doc_freq_ingred + 1),
          scat = axs[1].scatter(x=isomap_words_embeddings[:, 0],
                                      y=isomap_words_embeddings[:, 1],
                                      alpha=0.3,
                                      cmap='seismic',
                                      vmin=-7,
                                      vmax=8,
                                      c=np.log2(500 * corpus_doc_freq_ingred + 1),
          ScalMappable = cm.ScalarMappable(norm=Normalize(vmin=-7, vmax=8, clip=True), cmap = 'seismic')
          cb = fig.colorbar(ScalMappable, ax=axs)
          fig.axes[2].set_ylabel("Score absolu ingrédients", fontsize=12)
          fig.axes[0].set_ylabel("Coordonnée 1 de la PCA", fontsize=12)
fig.axes[0].set_ylabel("Coordonnée 2 de la PCA", fontsize=12)
          fig.axes[0].set_title("Projection sur la PCA", fontsize=12)
         fig.axes[1].set_xlabel("Coordonnée 1 de l'ISOMAP", fontsize=12) fig.axes[1].set_ylabel("Coordonnée 2 de l'ISOMAP", fontsize=12) fig.axes[1].set_title("Projection sur l'ISOMAP", fontsize=12)
         fig.suptitle("Projection des embeddings Word2Vec", fontsize=16)
# fig.savefig(Path('..') / 'img' / 'word2vec_projection.png', bbox_inches='tight')
```



```
[310]:
        mmin, mmax, resolution = -12, 4, 1000
        divnorm = colors.TwoSlopeNorm(vmin=mmin, vcenter=0, vmax=mmax)
        fig, axs = plt.subplots(ncols=2, figsize=(18, 5))
        alpha=0.3,
                                  cmap='seismic',
                                  norm=divnorm,
                                  c=relative_scores,
        scat = axs[1].scatter(x=isomap_words_embeddings[:, 0],
                                  y=isomap_words_embeddings[:, 1],
                                  alpha=0.3,
                                  cmap='seismic',
                                  norm=divnorm,
                                  c=relative_scores,
        ScalMappable = cm.ScalarMappable(norm=divnorm, cmap = 'seismic')
        cb = fig.colorbar(ScalMappable, ax=axs)
        fig.axes[2].set_ylabel("Score relatif entre les corpus", fontsize=12) fig.axes[0].set_xlabel("Coordonnée 1 de la PCA", fontsize=12) fig.axes[0].set_ylabel("Coordonnée 2 de la PCA", fontsize=12)
        fig.axes[0].set_title("Projection sur la PCA", fontsize=12)
        fig.axes[1].set_xlabel("Coordonnée 1 de l'ISOMAP", fontsize=12) fig.axes[1].set_ylabel("Coordonnée 2 de l'ISOMAP", fontsize=12)
        fig.axes[1].set_title("Projection sur l'ISOMAP", fontsize=12)
        fig.suptitle("Projection des embeddings Word2Vec", fontsize=16)
        # fig.savefig(Path('..') / 'img' / 'word2vec_projection_relative.png', bbox_inches='tight')
```



4.3 Représentations des textes

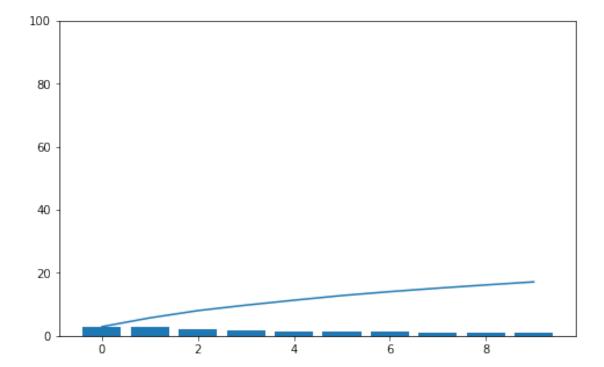
4.3.1 Bag of Words: comptes

Je fais une PCA sur les vecteurs de comptes. Mais d'abord, il faut standardiser.

```
[320]: vectorized_std = StandardScaler().fit_transform(np.array(vectorized_corpus.todense()))
PCA_model = PCA(n_components=10)
decomp = PCA_model.fit_transform(vectorized_std)
```

```
[321]: fig, ax = plt.subplots(figsize=(8, 5))
ax.plot(PCA_model.explained_variance_ratio_.cumsum()*100)
ax.bar(x=range(10), height=PCA_model.explained_variance_ratio_*100)
ax.set_ylim(0, 100)
```

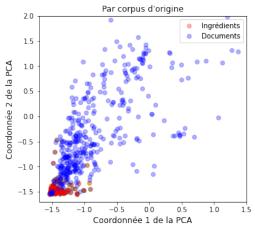
```
[321]: (0.0, 100.0)
```

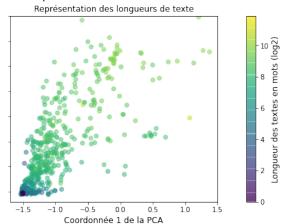


```
[322]: fig, ax = plt.subplots(ncols=2, figsize=(15, 5), sharey=True) handles = []
        ax[0].scatter(x=decomp[:500, 0],
                       y=decomp[:500, 1],
                        {\tt c=np.log2(np.array(vectorized\_corpus[:500,:].sum(axis=1)).flatten() + 1),} \\
                       cmap='viridis',
                       alpha=0.5)
        \verb| handles.append(ax[0].scatter(x=decomp[:500, 0],
                                       y=decomp[:500, 1],
                                       c=['red']*500,
                                        alpha=0.3))
        handles.append(ax[0].scatter(x=decomp[500:, 0],
                                       y=decomp[500:, 1],
                                        c=['blue']*500,
                                        alpha=0.3))
        \verb| handles.append(ax[1].scatter(x=decomp[:, 0],
                                       y=decomp[:, 1],
                                        c=np.log2(np.array(vectorized_corpus[:,:].sum(axis=1)).flatten() + 1),
                                        cmap='viridis',
                                       alpha=0.5))
```

```
ax[0].set_xlim(-1.7, 1.5)
ax[0].set_ylim(-1.7, 2)
ax[1].set_xlim(-1.7, 1.5)
ax[1].set_ylim(-1.7, 2)
ax[0].legend(handles[:-1], ['Ingrédients', 'Documents'])
cb = fig.colorbar(handles[-1], ax=ax)
fig.axes[2].set_ylabel("Longueur des textes en mots (log2)", fontsize=12)
fig.suptitle("PCA sur les comptes des mots", fontsize=16)
ax[0].set_ylabel("Coordonnée 2 de la PCA", fontsize=12)
ax[0].set_xlabel("Coordonnée 1 de la PCA", fontsize=12)
ax[0].set_title("Par corpus d'origine", fontsize=12)
ax[1].set_xlabel("Coordonnée 1 de la PCA", fontsize=12)
ax[1].set_title("Représentation des longueurs de texte", fontsize=12)
# fig.savefig(Path('..') / 'img' / 'PCA_counts.png', bbox_inches='tight')
```

PCA sur les comptes des mots





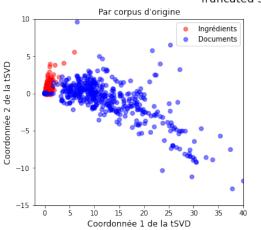
4.3.2 tSVD

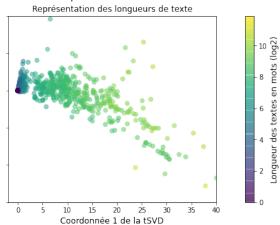
Je commence par faire un tSVD sur le corpus, en différenciant les ingrédients du texte des fiches techniques. Dans ce premier cas, on a les comptes des mots dans la vectorisation.

```
[323]: vectorized_corpus.todense()
[323]: matrix([[ 0., 0., 0., ..., 0., 0., 0.],
                [ 0., 0., 0., ...,
                                   0.,
               [ 0., 0., 0., ..., 0.,
                                        0.,
                                             0.],
               [ 1., 0., 0., ..., 0., 0., 0.],
                [ 2., 1., 0., ..., 0., 0., 0.],
                [11., 0., 0., ..., 0., 0., 0.]])
[324]:
       transformer = TruncatedSVD(n_components=100)
       projected = transformer.fit_transform(vectorized_corpus)
[325]:
      fig, ax = plt.subplots(ncols=2, figsize=(15, 5), sharey=True)
       handles = []
       handles.append(ax[0].scatter(x=projected[:500, 0], y=projected[:500, 1], c=['red']*500, alpha=0.5))
       handles.append(ax[0].scatter(x=projected[500:, 0], y=projected[500:, 1], c=['blue']*500, alpha=0.5))
       \verb| handles.append(ax[1].scatter(x=projected[:, 0],
                                    y=projected[:, 1],
                                     c=np.log2(np.array(vectorized_corpus[:,:].sum(axis=1)).flatten() + 1),
                                     cmap='viridis',
                                     alpha=0.5))
       ax[0].set_ylim(-15, 10)
       ax[0].set_xlim(-2, 40)
       ax[1].set_ylim(-15, 10)
       ax[1].set_xlim(-2, 40)
       ax[0].legend(handles[:-1], ['Ingrédients', 'Documents'])
       cb = fig.colorbar(handles[-1], ax=ax)
       fig.axes[2].set_ylabel("Longueur des textes en mots (log2)", fontsize=12)
       fig.suptitle("Truncated SVD sur les comptes des mots", fontsize=16)
```

```
ax[0].set_ylabel("Coordonnée 2 de la tSVD", fontsize=12)
ax[0].set_xlabel("Coordonnée 1 de la tSVD", fontsize=12)
ax[0].set_title("Par corpus d'origine", fontsize=12)
ax[1].set_xlabel("Coordonnée 1 de la tSVD", fontsize=12)
ax[1].set_title("Représentation des longueurs de texte", fontsize=12)
# fig.savefig(Path('..') / 'img' / 'tSVD_counts.png', bbox_inches='tight')
```

Truncated SVD sur les comptes des mots





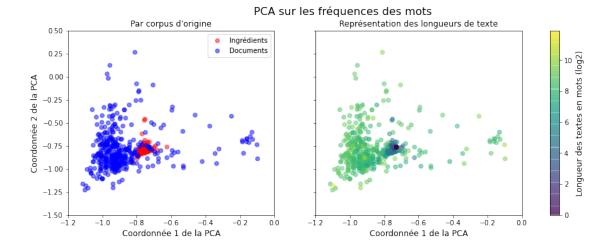
4.3.3 PCA: fréquences

En utilisant cette fois la term frequency. PCA

```
[326]: tf_corpus_model = clone(tfidf_corpus)
    tf_corpus = tf_corpus_model.set_params(norm='l1').fit_transform(corpus_df.loc[:, 'text'])

[327]: vectorized_std = StandardScaler().fit_transform(np.array(tf_corpus.todense()))
    decomp = PCA(n_components=10).fit_transform(vectorized_std)
```

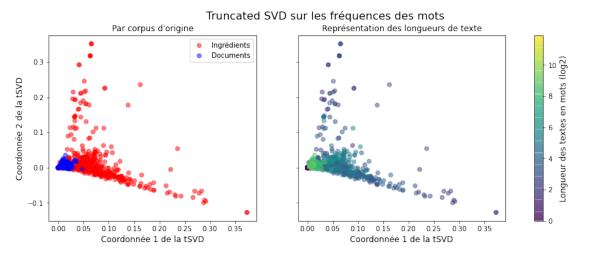
```
[332]: fig, ax = plt.subplots(ncols=2, figsize=(15, 5), sharey=True)
       handles = []
       handles.append(ax[0].scatter(x=decomp[:500, 0], y=decomp[:500, 1], c=['red']*500, alpha=0.5))
       \verb| handles.append(ax[1].scatter(x=decomp[:, 0],
                                   y=decomp[:, 1],
                                    c=np.log2(np.array(vectorized_corpus[:,:].sum(axis=1)).flatten() + 1),
                                    alpha=0.5.
                                    cmap='viridis'))
       ax[0].set_xlim(-1.2, 0)
       ax[0].set_ylim(-1.5, 0.5)
       ax[1].set_xlim(-1.2, 0)
       ax[1].set_ylim(-1.5, 0.5)
       ax[0].legend(handles[:-1], ['Ingrédients', 'Documents'])
       cb = fig.colorbar(handles[-1], ax=ax)
       fig.axes[2].set_ylabel("Longueur des textes en mots (log2)", fontsize=12)
       fig.suptitle("PCA sur les fréquences des mots", fontsize=16)
       ax[0].set_ylabel("Coordonnée 2 de la PCA", fontsize=12)
ax[0].set_xlabel("Coordonnée 1 de la PCA", fontsize=12)
       ax[0].set_title("Par corpus d'origine", fontsize=12)
       ax[1].set_xlabel("Coordonnée 1 de la PCA", fontsize=12)
       ax[1].set_title("Représentation des longueurs de texte", fontsize=12)
       fig.savefig(Path('..') / 'img' / 'PCA_freq.png', bbox_inches='tight')
```



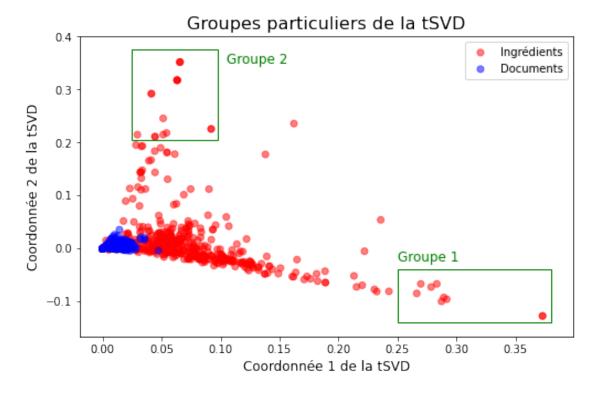
4.3.4 tSVD : fréquences

Voila.

```
transformer = TruncatedSVD(n_components=100)
[329]:
         projected = transformer.fit_transform(tf_corpus)
[330]: fig, ax = plt.subplots(ncols=2, figsize=(15, 5), sharey=True) handles = []
         \label{lem:lem:handles.append} $$ \mathtt{handles.append}(\mathtt{ax}[0].\mathtt{scatter}(\mathtt{x=projected}[:500,\ 0],\ \mathtt{y=projected}[:500,\ 1],\ \mathtt{c=['red']}*500,\ \mathtt{alpha=0.5}))$$ $$
         handles.append(ax[0].scatter(x=projected[500:, 0], y=projected[500:, 1], c=['blue']*500, alpha=0.5))
         \verb| handles.append(ax[1].scatter(x=projected[:, 0],
                                            y=projected[:, 1],
                                            c=np.log2(np.array(vectorized_corpus[:,:].sum(axis=1)).flatten() + 1),
                                            alpha=0.5,
                                            cmap='viridis'))
         # ax.set_ylim(-15, 10)
# ax.set_xlim(-2, 40)
         ax[0].legend(handles, ['Ingrédients', 'Documents'])
         cb = fig.colorbar(handles[-1], ax=ax)
         fig.axes[2].set_ylabel("Longueur des textes en mots (log2)", fontsize=12)
         fig.suptitle("Truncated SVD sur les fréquences des mots", fontsize=16)
         ax[0].set_ylabel("Coordonnée 2 de la tSVD", fontsize=12) ax[0].set_xlabel("Coordonnée 1 de la tSVD", fontsize=12)
         ax[0].set_title("Par corpus d'origine", fontsize=12)
         ax[1].set_xlabel("Coordonnée 1 de la tSVD", fontsize=12)
         ax[1].set_title("Représentation des longueurs de texte", fontsize=12)
          \# \ fig.savefig(Path('..') \ / \ 'img' \ / \ 'tSVD\_freq.png', \ bbox\_inches='tight')
```



```
fig, ax = plt.subplots(figsize=(8, 5))
handles = []
handles.append(ax.scatter(x=projected[:500, 0], y=projected[:500, 1], c=['red']*500, alpha=0.5))
handles.append(ax.scatter(x=projected[500:, 0], y=projected[500:, 1], c=['blue']*500, alpha=0.5))
ax.add_patch(mpatch.Rectangle((0.25, -0.14), 0.13, 0.1, fill=False, color='green'))
ax.add_patch(mpatch.Rectangle((0.025, 0.205), 0.073, 0.17, fill=False, color='green'))
ax.annotate('Groupe 1', (0.25, -0.025), fontsize=12, color='green')
ax.annotate('Groupe 2', (0.105, 0.35), fontsize=12, color='green')
ax.legend(handles, ['Ingrédients', 'Documents'])
ax.set_ylabel("Coordonnée 2 de la tSVD", fontsize=12)
ax.set_ylabel("Goordonnée 1 de la tSVD", fontsize=12)
ax.set_title("Groupes particuliers de la tSVD", fontsize=16)
# fig.savefig(Path('..') / 'img' / 'tSVD_freq_groups.png', bbox_inches='tight')
```



```
.replace(r'\textbackslash n', r' \newline '))
     print(tex_str)
 \# with open(Path('..') / 'tbls' / 'tSVD_sample.tex', mode='w') as file:
      file.write(tex_str)
\begin{tabular}{llcc}
\toprule
                                                                                                у \\
{} &
                                                                    Texte &
                                                                                    x &
\midrule
                                                                 Thon, eau, sel & 0.373079 & -0.127052 \setminus
Groupe 1 &
                                                        Pois chiches, eau, sel. & 0.266423 & -0.084501 \setminus \setminus
Groupe 1 &
                                                      Haricots beurre, eau, sel & 0.283409 & -0.066561 \
Groupe 1 &
                                                     Câpres, eau, vinaigre, sel & 0.291819 & -0.095479 \
Groupe 1 &
Groupe 1 &
                                                        Thon albacore, eau, sel & 0.287423 & -0.099627 \
Groupe 1 &
                                                      Eau, haricots verts, sel. & 0.278588 & -0.072474 \\
Groupe 1 &
                                                     Pommes de terre, eau, sel. & 0.289291 & -0.092162 \
Groupe 1 &
                                            Carottes rondelles, eau, sel, sucre & 0.269849 \& -0.066600 \setminus
Groupe 1 &
                                                                 Thon, eau, sel & 0.373079 & -0.127052 \\
Groupe 2 &
                                - 100\% Semoule de blé dur de qualité supérieure & 0.065551 & 0.351800 \\
Groupe 2 &
                                                           100\% haricots blancs & 0.051373 & 0.214921 \\
Groupe 2 &
                                  100\% Semoule de blé dur de qualité supérieure & 0.065551 & 0.351800 \\
Groupe 2 &
                         Semoule de blé dur* \newline *issu de l'agriculture biologique & 0.054211 &
0.218192 \\
Groupe 2 &
                                                                Tilleul (100\%). & 0.041323 & 0.292199 \\
Groupe 2 &
                                  100\% semoule de blé dur de qualité supérieure & 0.065551 & 0.351800 \\
Groupe 2 &
                                                              Farine de blé T45 & 0.092002 & 0.225689 \\
Groupe 2 &
                  - Semoule de blé dur de qualité supérieure \newline - 30\% oeufs frais & 0.044446 &
0.211188 \\
Groupe 2 &
           - 100\% Semoule de blé dur de qualité courante \newline - Contient du gluten & 0.051337 &
0.245649 \\
Groupe 2 &
                                      SEMOULE DE BLE' DUR de qualité supérieure & 0.063201 & 0.317653 \\
Groupe 2 &
                                                                  100\% Arabica & 0.041324 & 0.292222 \\
Groupe 2 &
                                                                 agar-agar 100\% & 0.029466 & 0.214845 \\
Groupe 2 &
                                      SEMOULE DE BLE' DUR de qualité supérieure & 0.063201 & 0.317653 \\
Groupe 2 &
                                      SEMOULE DE BLE' DUR de qualité supérieure & 0.063201 & 0.317653 \\
Groupe 2 &
                                      SEMOULE DE BLE' DUR de qualité supérieure & 0.063201 & 0.317653 \\
Groupe 2 &
                  - Semoule de blé dur de qualité supérieure \newline - 30\% oeufs frais & 0.044446 &
0.211188 \\
Groupe 2 &
                                                              Farine de blé T45 & 0.092002 & 0.225689 \\
\bottomrule
\end{tabular}
```