$$\omega_i = \omega_o \left(R_1 - \frac{w}{2}\right) / \left(R_1 + \frac{w}{2}\right)$$