

HERIOT-WATT UNIVERSITY

DOCTORAL THESIS

Multimodal Representation Learning

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Declaration of Authorship

I, Eli SHEPPARD, declare that this theis titled, 'Multimodal Representation Learning' and the work presented in it is my own. I confirm that this work submitted for assessment is my own and is expressed in my own words. Any uses made within it of the works of other authors in any form (e.g., ideas, equations, figures, text, tables, programs) are properly acknowledged at any point of their use. A list of the references employed is included.

Signed:

Date:

Abstract

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Abbreviations

MRL	Multimodal Representation Learning Network
ConvNet	Convolutional neural Network
AE	Autoencoder
MAE	Multimodal Autoencoder
RNN	Recurrent Neural Network
GRU	Gated Recurrent Unit
LSTM	Long Short-Term Memory
YARP	Yet Another Robotics Platform

Chapter 1

Introduction

Multimodal Representation Learning

What is Multimodal Representation Learning (MRL) and why is it useful? These are the questions that I will address in this thesis. Briefly, MRL is the act of learning an abstract representation of sensory data from multiple sensors. As sensors respond directly to the world in which they are situated, MRL is closely related to learning a world representation. Therefore, an accurate representation of sensory data contains in it, a representation of the world.

MRL is therefore useful any time we have more than one sensor and if we can abstract sensory data to learn more about the world, or how the different modalities relate to one and other. Perhaps the best example of this is Language Learning - when a baby learns its first words, it is doing MRL, learning the association of sounds to objects and actions and vice-versa.

Beyond the highly complex and abstract task of learning a language, MRL can also be used for sensor fusion. Providing auxilory information using extra sensors can help to improve classification accuracy (which I will demonstrate later) and can also be used to regenerate missing data when only one modality is available. A good example of this is when humans read lips in noisy environments, using the shape of the mouth to help recognise which words are being uttered even if they are not heard.

Motivation

One of the major challenges in robotics and machine learning is that of knowing how to develop systems capable of life long learning. If robots are to become common place in society, they must be capable to continuing to learn throughout their lives. They will not be very useful if they cannot learn new things that they weren't programmed with at the factory.

Multimodal representation learning addresses this by providing an unsupervised method for extracting useful and actionable information about the world. Let us return to the language learning scenario, except this time, instead of a bay, lets imagine a robot, fresh out of the box. Whilst we might expect that a robot would have some proficiency with language built into it, we cannot expect it to know the meaning of every single word, especially given the flexible and evolving way that humans use language. Our robot therefore needs a way to learn the meaning of new words.

Similarly, we cannot expect the robot to be able to recognise every single object in its environment. On my desk I have a Stirling engine, I would wager that most people that read this don't know what a Stirling engine is. However, if I showed you a picture of a Stirling engine (like the one in [Figure 1.1](#) you would be able to recognise what a Stirling engine is in future. Ideally, robots need to be able to do this.



FIGURE 1.1: The Stirling Engine from my desk.

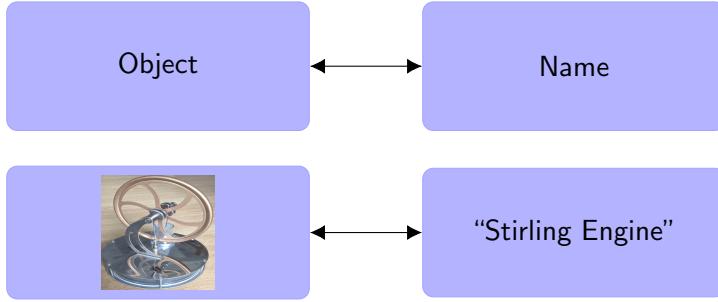


FIGURE 1.2: The bi-directional nature of language learning.

The Stirling engine example shows how language learning is a bi-directional process. Not only do you need to learn the name of the object *Stirling Engine* but also that the words “*Stirling Engine*” mean the object *Stirling Engine* as shown in [Figure 1.2](#).

Multimodal representation learning allows us to jointly model both the object *Stirling Engine* and the words “*Stirling Engine*”, relying on only one assumption: **Sensory percepts which occur together are related.**

Whilst this may not be true for all sensory percepts it is true enough that co-occurrence of percepts allows us to infer useful information about the relationship between different modalities. For example, smith et al. [Smith and Yu \[2008\]](#) show how infants learn object names based on “cross-situational statistics” i.e. how often a word and an object occur together. [Figure 1.3](#) illustrates this idea.

Green Circle	Green Square
Blue Circle	Blue Square

FIGURE 1.3: Associations among words and objects across multiple ambiguous scenes allow learners to find the proper mapping of words: ”Circle”, ”Square”, ”Green” and ”Blue” to objects and colours: *Circle*, *Square*, *Green* *Blue*

Chapter 2

Background

Introduction

In this section I will layout the key ideas and technologies which have inspired and enabled the research presented later in this thesis.

Due to the broad scope of the research carried out, the background section is loosely presented so as to compare and contrast the state-of-the-art artificail neural network technologies with their biological analogues (where possible). As such, I survey a large body of machine learning, psychology and biology literature.

In doing this, I aim to demonstrate how ANNs have exceeded human performance in specific areas, whilst lagging far behind in many others. By bringing these divergent fields together, perhaps it is possible to find ways to improve ANNs whilst also further developing our understanding of what makes humans tick.

What are Artifical Neural Networks good at?

Summary of sota literature demonstrating cool things ANNs can do.

Classification

Generation

Reinforcement Learning

What are Artificial Neural Networks bad at?

Explain how ANNs have specialised skill, not generalised skill - quote Rodney Brooks.

data inefficiency

look at other ML methods which require less data but are generally less capable/require more engineering.

How to Get Off the Symbol Grounding Merry-Go-Round

What is symbol grounding?

How do humans do it?

Barsalou

How do machines do it?

Why brains are better

Embodiment

Sensory Redundancy

Biological Filters

Retina, shape of ear etc.

Development

Biological Filters, again

Superior Colliculus guides learning in the visual cortex by controlling attention.

Pulling yourself up by the bootstraps

Machine Equivalency

How do we simulate Embodiment for ANNs?

How do we simulate Development for ANNs?

Where do we go from here?

Robot bodies

multimodality

transfer learning

Chapter 3

A Primer on Artificial Neural Networks

Introduction

This chapter presents an overview of the mathematical theory behind artificial neural networks and how they learn. It should serve as a quick guide to the techniques used in the experiments within this thesis.

Perceptrons

The perceptron is the parent of modern artificial neurons [?](#). Perceptrons arranged in layers, referred to as multi-layer perceptrons, are therefore the predecessor of modern artificial neural networks.

What is a Perceptron

Perceptrons are biologically inspired computation units and are a type of artificial neuron. They take a series of binary inputs, compute a weighted sum and produce a binary output based on the value of this sum as seen in [Figure 3.1](#).

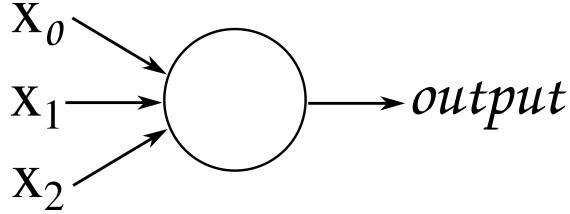


FIGURE 3.1: A perceptron with three binary inputs, x_0, x_1, x_2 .

$$\text{output} = \begin{cases} 0 & \text{if } \sum_j w_j x_j + b < 0 \\ 1 & \text{if } \sum_j w_j x_j + b \geq 0 \end{cases} \quad (3.1)$$

Where x_j is the jth input, w_j is it associated weight and b is a constant value called the bias, which affects how easy it is for the neuron to activate. The output of the perceptron is calculated using the formulation shown in [Equation 3.1](#).

By adjusting each of the weights we can change the output of the perceptron. For example, if we wanted to use a perceptron to decide whether to have a picnic today we can select a set of relevant inputs, “the weather is nice” and “the pollen count is low”.

If it is a sunny day, and the pollen count is high, the input to the perceptron would be $[1, 0]$.

We will set our weights depending on how important each of the inputs is. No one likes a picnic in the rain, so the weather is important, whilst the pollen count is only important if you suffer from hayfever. We will select a bias of -5 for our perceptron.

For person A, the weights might look like $[7, 0]$ (person A doesn’t suffer from hayfever). Therefore the output of the perceptron would be 1 as $1 \times 7 + 0 \times 0 - 5 = 2$ is greater than 0, so person A will go for a picnic.

Person B owns a large umbrella (so the weather doesn’t matter as much) but they do suffer from hayfever, their weights might look like $[4, 7]$. The output of the perceptron would be 0 as $1 \times 4 + 0 \times 7 - 5 = -1$ is less than 0. Therefore, person B would wait for a day with a lower pollen count for a picnic.

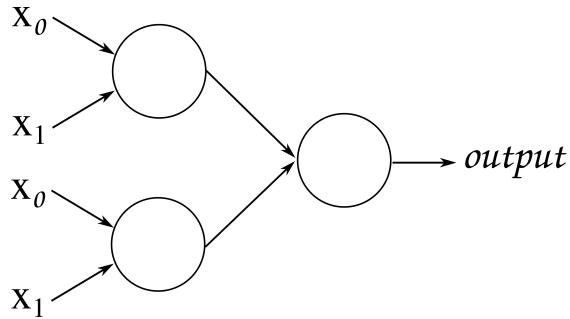


FIGURE 3.2: A multi-layer perceptron consisting of three perceptrons arranged in two layers, with three binary inputs, x_0, x_1, x_2 .

Multi-Layer Perceptron

In the previous section I demonstrated how a single perceptron can be used to make decisions based on a set of inputs. However, things get much more interesting when we start to link multiple perceptrons together into multi-layer perceptrons (MLP).

If we take the example from the previous section about deciding to go for a picnic or not, we can use the MLP shown in [Figure 3.2](#) to consider what happens if person A and B want to go for a picnic together.

Given the previous conditions of a sunny day with a high pollen count, person A wants to go whilst person B does not, as demonstrated by the outputs of their individual perceptrons. Taking these outputs as inputs to the second layer of our MLP, we can see whether the picnic will go ahead.

This time we will set the weights of the second layer based on who shouts the loudest. In this case, person A really wants to go and is very vocal about it. $1 \times 9 + 0 \times 5 - 5 = 4$ so the picnic will go ahead. This resulted in person B developing a headache and sneezing a lot. Clearly we need to find a way to adjust the weights of our MLP so that it makes better decisions in the future.

Activation Functions

Only being able to handle binary values is a major drawback of the perceptron. An artificial neuron which can handle continuous values is much more useful.

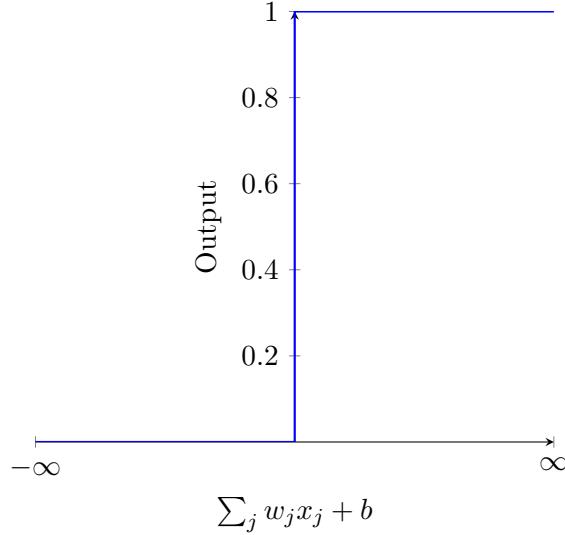


FIGURE 3.3: Visualisation of the perceptron activation function.

This limitation occurs due to the activation function of the perceptron shown in [Equation 3.1](#). Visualising the perceptron activation function highlights that changes in the output of the neuron are not proportional to changes in the weights of the neuron as seen in [Figure 3.3](#). With a few small changes we can make an artificial neuron that accepts continuous values and has a continuous output.

A continuous output is very important as it means that a small change in the weights of a neuron will cause a small change in its output. This makes it much easier to understand how changing the weights affects the output of the network as the change in output becomes proportional to the change in weights as shown in [Equation 3.2](#)

$$\delta \text{Output} \propto \delta W \quad (3.2)$$

Sigmoid Neurons

The sigmoid neuron uses the sigmoid function, shown in [Equation 3.3](#) as its activation function.

$$\sigma(z) = \frac{1}{1 + e^{-z}} \quad (3.3)$$

z is the sum of the weights multiplied by their respective inputs as seen in [Equation 3.4](#).

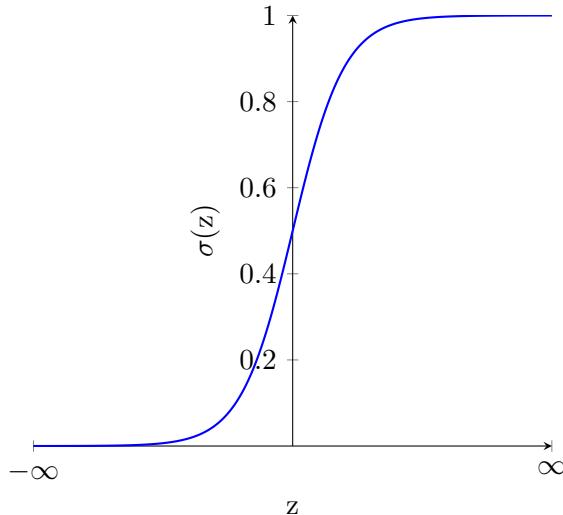


FIGURE 3.4: Visualisation of the sigmoid activation function.

$$z = \sum_j w_j x_j + b \quad (3.4)$$

As we can see in Figure 3.4, as z changes, there is a proportional change in the output $\sigma(z)$, unlike in Figure 3.3 where the output only changes when z crosses the y-axis.

Now that we have an activation function that can produce continuous values, we can consider a much more diverse range of data to train our neural networks with. So instead of just making yes or no decisions we can look at, for example, the colours of pixels and decide if there is a cat in the image or given todays weather, predict if it will rain tomorrow.

Other activation functions

There are two other important and commonly used activation functions, though many others exist. These are, the hyperbolic tangent (Tanh) shown in Figure 3.5 and rectified linear unit (Relu) shown in Figure 3.6.

The Tanh function looks similar to the sigmoid function, however it has an output between negative one and one, where the sigmoid goes from zero to one. This is useful when having negative values within the network is important.

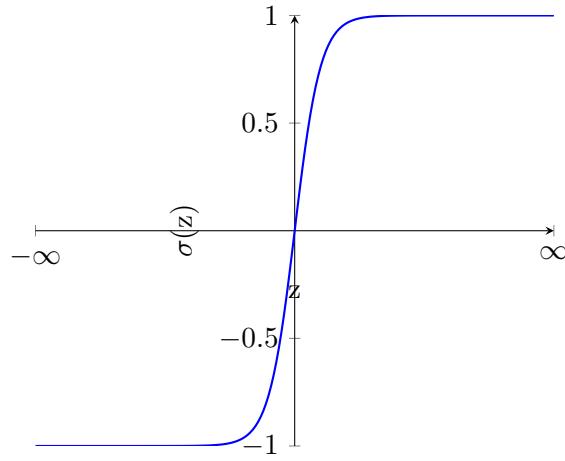


FIGURE 3.5: Visualisation of the hyperbolic tangent activation function.

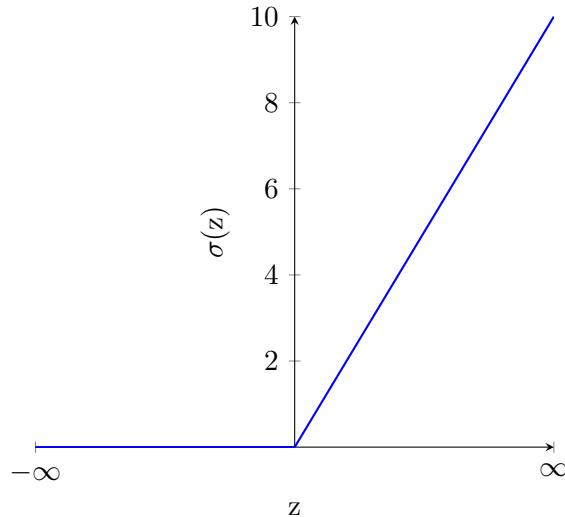


FIGURE 3.6: Visualisation of the rectified linear unit activation function.

The Relu was created to address an issue known as vanishing gradients. This is to do with how neural networks are trained, as explained in the next section. Briefly, as training depends on error gradients, having a linear activation function means that deeper networks¹ can be trained as non-linear functions like the sigmoid or Tanh will have reduced gradient magnitude when they are differentiated to backpropagate the error through the network. If that doesn't make sense yet, don't worry, it will become clear shortly.

¹Deeper networks are beneficial as they can make more complex decisions by layering more and more simple decisions as shown in the MLP example in [section 3.2](#)

Learning Algorithms

In section 3.2 we saw how simple computation units can make simple decisions and how these can be chained together to make more complex decisions. However, sometimes the decisions we make are wrong and we need to learn from our mistakes.

In general, perceptrons (and their more modern descendants) will have their initial weights set randomly, unlike in our example where I chose them.

Randomly setting weights is useful in practice as we will usually have large numbers of inputs, weights, layers and artificial neurons, so setting each by hand would be intractable. Also, if we knew what weights to set, we wouldn't need a neural network or a learning algorithm to solve our problem as we would likely have a more efficient mathematical description of the problem ²

With random weights our networks will make a lot of wrong decisions! However if we have a smart way of adjusting our weights we can make our neural networks get better at making decisions over time. This improvement is what I am referring to when I say “machine learning”.

Types of Training

There are many ways to train neural networks, supervised, unsupervised, reinforcement or adversarial learning (to name a few). The experiments in this thesis will focus on supervised and unsupervised learning.

Supervised learning - an external system is used to provide ground truth values for the desired output of the network. An example would be classification using standardised datasets like MNIST handwritten digits ?.

Unsupervised learning - no external system provides ground truth values, instead these are inferred directly from the data. Autoencoders (discussed in great detail in later chapters) are a good example of this.

²there is a large body of work concerning the best way to initialise neural networks, I will briefly comment on this in subsection 6.1.1.

Cost functions: How wrong am I?

In order for our neural networks to learn, they need feedback as to how wrong they are. This is done using a cost function, a formula which gives a measure of how good or bad our network is at a particular task.

Depending on the particular method we use to train our networks, the cost function may be given a different name. For example in reinforcement learning, the cost function is typically called a value function. However, they all serve the same purpose, which is to provide feedback as to how well our network is doing at the task it has been assigned. Therefore, to avoid jargon I will refer to this as a cost or loss function throughout this thesis.

The cost function can take on many forms, in supervised and unsupervised training alike. Here are a few of the more commonly used ones and an explanation of each.

Mean Squared Error

Mean squared error (MSE) measures the average difference between points as shown in [Equation 3.5](#).

$$C = \frac{1}{n} \sum_{i=0}^n (Y_i - \hat{Y}_i)^2 \quad (3.5)$$

When used as a loss function, MSE gives a measure of how bad our estimate \hat{Y}_i is of our true value Y_i on average for all n training samples in a given dataset. A perfect model would have an MSE of 0 as \hat{Y}_i would be equal to Y_i for all values of i .

In general, Y_i and \hat{Y}_i can be of arbitrary size and shape (as long as they match each other). That is, they can be scalers, vectors or matrices.

Cross-Entropy

Cross-entropy measures the error between two probability distributions P and Q using the formula shown in [??](#). P is the true probability distribution which we are trying to model with our predicted probability distribution Q .

$$C = - \sum_{i=0}^n P(i) \log(Q(i)) \quad (3.6)$$

When using cross-entropy as a loss function, we can view the output of our neural network as a probability distribution. For example, in a multiclass classification problem with k classes, each of the k outputs of the network tells us the probability that the network believes an input to belong to class k .

Here is a more concrete example: Given a dataset containing images of animals: cats, dogs, horses and snakes. A single image containing a cat would be labelled $[1, 0, 0, 0]$. This tells us the exact probability distribution of the image, P i.e. the image certainly contains a cat and does not contain any other animals.

now as our network trains, it may give a prediction of $[0.5, 0.3, 0.15, 0.05]$, this is our predicted probability distribution Q .

Calculating our cross-entropy we get: $C = -(1\log(0.5) + 0\log(0.3) + 0\log(0.15) + 0\log(0.05) = 0.301_{3s.f.})$

If we then do some training using gradient descent our network might then predict $[0.8, 0.2, 0, 0]$ giving a cross-entropy of $0.0969_{3s.f.}$. Clearly this represents an improvement, as the cost is closer to zero and our prediction is better. The network believes with 80% certainty that the image is of a cat.

Kullback-Leibler Divergence

Another method for defining the difference between two distributions is the Kullback-Leibler Divergence (KLD).

KLD is a non-symmetric distance measure between two distributions, P and Q . As it is non-symmetric $D_{KL}(P||Q) \neq D_{KL}(Q||P)$ unless $P = Q$.

$$D_{KL} = - \int_{i=0}^n P(i) \log\left(\frac{Q(i)}{P(i)}\right) \quad (3.7)$$

KLD is useful in machine learning when we wish to calculate how different a predicted distribution is from a desired distribution. Most commonly, we will want P to be a

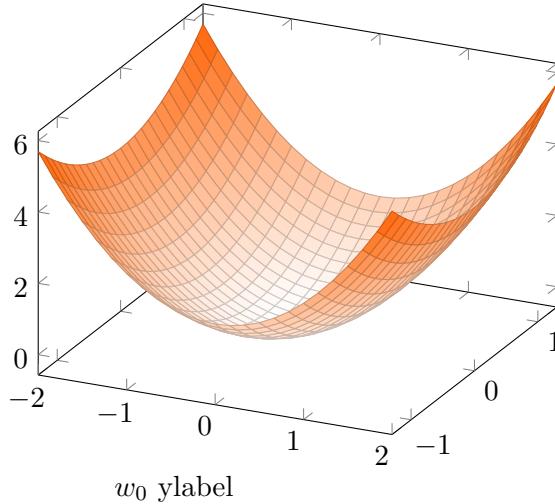


FIGURE 3.7: The cost landscape of a bivariate function

Gaussian distribution, though which distribution is chosen will depend on the specific problem. We will then use the KLD as a constraint to force our networks to make predictions which follow as closely as possible to this desired distribution, i.e. we will minimise $D_{KL}(P||Q)$.

Typically KLD is not used as a cost function on its own, but is used to constrain the output of a single layer of a network (usually not the output) whilst also minimising another cost function.

The best example of this is a Variational AutoEncoder (VAE), which will be discussed later.

Gradient Descent

Now that we have a method for determining how well our neural network performs at a task, we can observe how this changes as the weights of the network are changed.

To make things simple, let's assume our network only has two weights, though the following derivation generalises to any number of weights. This could give us a cost landscape like that shown in [Figure 3.7](#). Our aim is to minimise the cost as the cost is a measure of how wrong our network is.

In more definite terms we wish to minimise [Equation 3.8](#), where Y_i is the desired output value for input i and z is as defined in [Equation 3.4](#).

$$C(w_0, w_1) = \frac{1}{n} \sum_{i=0}^n (Y_i - \sigma(z_i))^2 \quad (3.8)$$

This is the mean squared error rewritten slightly to highlight the dependence on the weights of the network.

If we make a small change to either of the weights w_0 and w_1 we will get a small change in the cost, C as seen in [Equation 3.9](#).

$$\Delta C \approx \frac{\delta C}{\delta w_0} \Delta w_0 + \frac{\delta C}{\delta w_1} \Delta w_1 \quad (3.9)$$

We want to minimise C so we want ΔC to be negative. To make ΔC negative we will need to first denote that the gradient of C , ∇C .

$$\nabla C \equiv \left(\frac{\delta C}{\delta w_0}, \frac{\delta C}{\delta w_1} \right)^T \quad (3.10)$$

In [Equation 3.10](#) we can see that the gradient of C is equivalent to the partial derivatives of C with respect to the weights of the network. For simplicity we will collect the changes in weights into a single vector $\Delta w \equiv (\Delta w_0, \Delta w_1)^T$.

By substituting this into [Equation 3.9](#) we get [Equation 3.11](#).

$$\Delta C \approx \nabla C \cdot \Delta w \quad (3.11)$$

Looking at [Equation 3.11](#), we can see that to make ΔC negative we can set Δw as in [Equation 3.12](#), where η is a small positive constant called the learning rate.

$$\Delta w = -\eta \nabla C \quad (3.12)$$

By substituting [Equation 3.12](#) into [Equation 3.11](#) we can see that $\Delta C = -\eta |\nabla C|^2$ and because $|\nabla C|^2 \geq 0$ this guarantees that C will always decrease if the weights are changed in accordance to [Equation 3.12](#).

By iteratively making changes to the weights according to [Equation 3.12](#) we will eventually reach the minima of C so long as we select an appropriate learning rate ³.

Backpropagation

With a gradient descent providing a method for adjusting weights, we now only need one more ingredient to be able to train our neural networks. Whilst our cost function tells us about the error of our network at its output, we need a method to calculate the error for any neuron in any layer - this is exactly what backpropagation does.

Backpropagation is defined by four equations: 1) An equation for the error in the output layer, δ_L :

$$\delta_L = \nabla_a C \circ \sigma'(z_L) \quad (3.13)$$

[Equation 3.13](#) shows the output error δ_L equates to changes in the cost C with respect to its activations a and the derivative of the output layers activation function σ' when the input to that layer is z_L .

2) An equation for the error δ_l in terms of the error in the next layer:

$$\delta_l = ((w_{(l+1)})^T \delta_{(l+1)} \circ \sigma'(z_l)) \quad (3.14)$$

where $(w_{(l+1)})^T$ is the transpose of the weight matrix for the layer above. Multiplying the error from the layer above by the transposed weight matrix can be seen as moving the error backward through that weight matrix and the Hadamard product⁴ \circ with $\sigma'(z_l)$ moves the error backward through the activation function.

3) An equation for the rate of change of the cost with respect to any bias in the network:

$$\frac{\delta C}{\delta b_{lj}} = \delta_{lj} \quad (3.16)$$

³Learning rate is discussed in more detail in [subsubsection 3.4.5.1](#)

⁴The Hadamard product is the elementwise product of two matrices as shown in [Equation 3.15](#).

$$\begin{bmatrix} a & b \\ c & d \end{bmatrix} \circ \begin{bmatrix} e & f \\ g & h \end{bmatrix} = \begin{bmatrix} ae & bf \\ cg & dh \end{bmatrix} \quad (3.15)$$

where $\frac{\delta C}{\delta b_{lj}}$ is the rate of change of the cost C with respect to bias b of neuron j , in layer l and δ_{lj} is the j^{th} entry in the error matrix δ for layer l i.e. the error for the j^{th} neuron in layer l .

4) An equation for the rate of change of the cost with respect to any weight in the network:

$$\frac{\delta C}{\delta w_{ljk}} = a_{(l-1)k} \delta_{lj} \quad (3.17)$$

where $\frac{\delta C}{\delta w_{ljk}}$ is the rate of change of cost C with respect to the change in weight w_k of neuron j in layer l and $a_{(l-1)k}$ is its input activation.

Using these four [Equation 3.13](#), [Equation 3.14](#), [Equation 3.16](#) and [Equation 3.17](#), we can calculate the change in error due to any weight or bias in the network and thus can use gradient descent to optimise its value to reduce the error at the output of the network.

One consequence of the backpropagation algorithm is that we are limited in terms of the trainable depth of our networks. As we continually differentiate the error to pass it back through each layer and multiply it by transposed weight matrices, the magnitude of the error can shrink. This results in vanishing error gradients the deeper into the network we go. This means that at some point, the error with respect to a weight or bias will appear to be zero (or approximately zero) and thus we cannot adjust it by gradient descent, so we are limited to not having infinitely deep networks.

Extensions and Improvements

There are many extensions to simple gradient descent based learning, here are a few to be aware of.

Learning Rate Schedule

Depending on how far we are from the global error minima, we may wish to change the value of the learning rate η . Recall from [Equation 3.12](#) $\Delta w = -\eta \nabla C$, that the learning rate determines how big of a step we take, following the gradient of the error, each time we update the weights of our neural network.

If we are far from the minimum point for the cost with respect to the weights, we may wish to take larger steps, so that we can more quickly reduce the total cost. However, as we get closer we want to ensure that we do not step over the minimum.

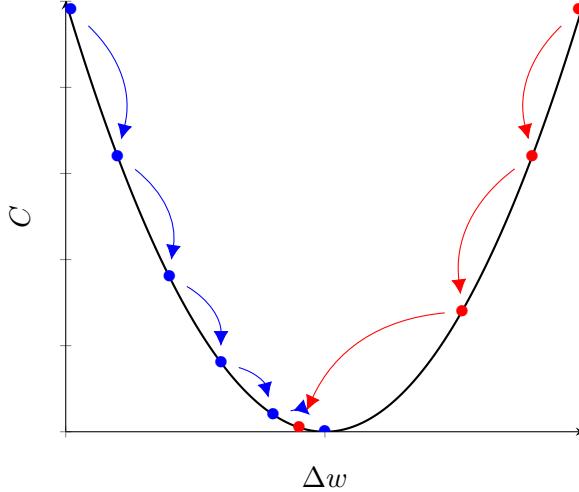


FIGURE 3.8: Visualisation of cost minimisation in two dimensions for different learning rate schedules. Blue: decreasing learning rate, Red: large fixed learning rate.

Figure 3.8 shows how changing the learning rate schedule can affect how the gradient descent optimiser navigates the cost landscape. The blue arrows show how reducing the learning rate as more training occurs, allows us to not miss the cost minimum. The red arrows show what can happen if we select a large learning rate and don't change it. Whilst at first, we make rapid progress towards the minimum, at somepoint we cross over it and will be unable to approach any closer without taking smaller steps.

This demonstrates nicely why we either select a small learning rate or make use of a learning rate scheduler. Learning rate schedulers can speed up convergence by allowing large steps to be taken when we are far from the cost minimum with respect to the weights, covering a large distance in a few updates and then slowing down to take smaller steps as we get closer.

This begs the question of: how do we know when to change the learning rate? in practice there are many ways we can achieve this, however these broadly fit into two categories, mathematical and heuristic.

There are many algorithms for calculating how to set the learning rate for example, Adam ? and ADADelta ?. They are both popular as they are both first order methods,

meaning that expensive, slow calculations of second order derivatives do not need to be made. Senior et al.⁷ provide an extensive testing of different learning rate schedulers.

Second order methods are desirable in that the second derivative of the cost provides information about how the cost gradient is changing. Figure 3.9 shows how the cost and its first and second derivatives change with respect to the weights. In region (A), where the cost (black line) is far from the minima the first derivative (blue) changes rapidly, causing the second derivative (red) to have a large magnitude. In region (B), the cost is closer to the minima, and thus the change in cost is lower so the steepness of the first derivative (blue) is lower as is the magnitude of the second derivative (red). At the minima, the second derivative is exactly zero, so we know we have reached the minima if the second derivative equals zero.

Second order methods have the major draw back of being very slow to calculate. Thus it is more efficient to make use of first order estimates than the exact information provided by second order methods. Many more weight updates can be carried out using first order methods than can be done using second order methods in a given time frame. So whilst second order methods should require less total weight updates to minimise the cost, the first order methods will reach the minimum faster as the weight updates will occur much more quickly in the first order case.

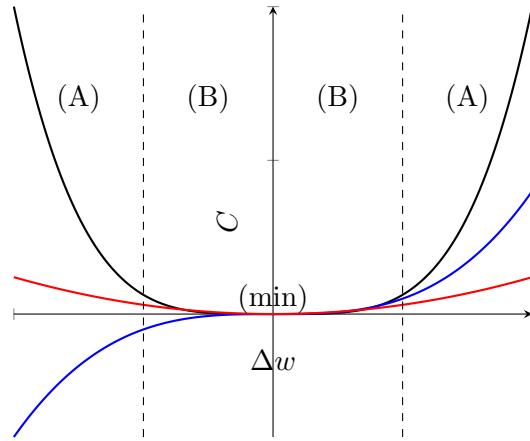


FIGURE 3.9: Visualisation of the cost (black), its first derivative (blue) and second derivative (red).

Heuristic methods provide a very simple method for adjusting the learning rate. A commonly used one is to simply gradually reduce the learning rate by a small amount each epoch. This has the advantage of requiring almost no computational overhead

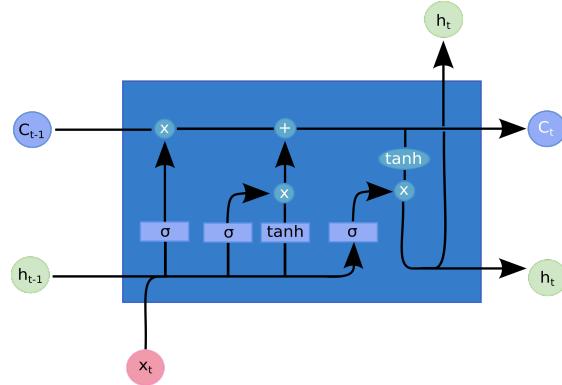


FIGURE 3.10: A Long Short-Term Memory Unit

and being very easy to understand. When training starts, we expect performance to be poor, so improvements can be made rapidly. As training progresses, we expect that improvements will be slower as we are approaching the minimum cost.

Convolutional Neural Networks

What is Convolution?

Kernels

Strides

Dilations

Transposed Convolutions

Recurrent Neural Networks

Vanilla RNN

Gated RNN

Summary

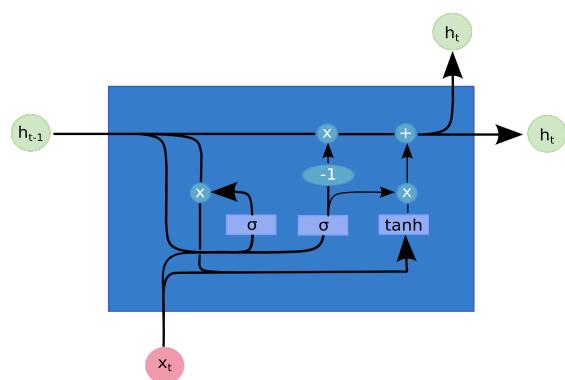


FIGURE 3.11: A Gated Recurrent Unit

Chapter 4

Sensory Redundancy: Are two heads better than one?

Why have one sensor when two are better?

A key part of the human experience is that it is multisensory. In ?, Lawrence Barsalou speaks about how multisensory processing aids human cognition in a number of ways. Firstly, multisensory information aids in the classification of experiences by providing additional and complimentary information that is not accounted for in only a single modality.

The McGurk effect ? demonstrates how the visual stimuli of lip reading affects the classification of heard sounds. Whilst this effect can lead to incorrect classifications when misaligned data is provided e.g. utterances of the syllable [ba] dubbed on to lip movements for [ga], lead to normal adults hearing [da]; in normal circumstances i.e. when two people are speaking to one another, lip reading aids in classifying heard sounds ?. This is particularly important in noisy environments, which leads to another of Barsalou's ideas about multisensory processing: information redundancy.

The reason that lip reading can aid hearing in noisy environments is that it provides an additional vector along which the human brain can reconstruct missing information. I.e. when something is mis-heard due to background noise, the visual information gained from looking at the face of the speaker can be used to reconstruct their utterance.

The ability to reconstruct missing data from a secondary modality has not only been seen in humans ?? but has been demonstrated in computational models for example, Ngiam et al.??.

In order to be able to reconstruct missing data from a secondary modality, symbol grounding needs to have occurred, i.e. the meaning of a percept in modality A must be known in modality B. If both the forward and inverse relationship between modalities is known, then bidirectional symbol grounding has occurred and we are able to reconstruct modality A from modality B and modality B from modality A.

In this chapter I will explore these two ideas, improved classification and reconstruction of missing information through bidirectional symbol grounding using multimodal autoencoders (MAE).

Generating images from natural language

Aims

The experiment in this section looks at whether having access to a second modality improves classification accuracy over the baseline accuracy of classification of either of the two individual modalities as well as how well missing data can be reconstructed from a secondary modality.

UCU Arabic Spoken Digits and MNIST

This experiment utilises two datasets, UCU Arabic Spoken Digits and MNIST Handwritten Digits.

UCU Arabic Spoken Digits

UCU Arabic Spoken Digits (UCU) is a dataset containing the 13 Mel Frequency Cepstrum Coefficients representing the audio of the digits 0 to 9 being said by 88 different speakers ???. It contains 8800 utterances (10 digits x 10 repetitions x 88 speakers). Audio was sampled at 11025Hz.

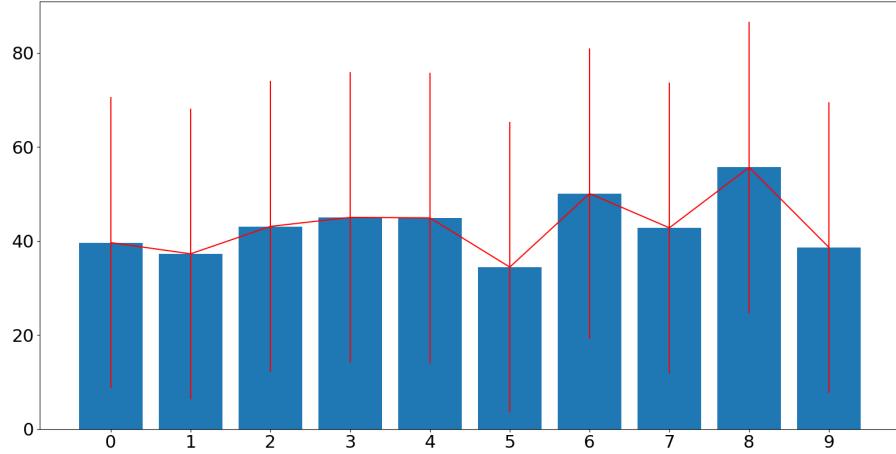


FIGURE 4.1: Mean number of samples for each digit in the UCU Arabic Spoken Digits Dataset. Red bars show the standard deviation in length for each each digit.

As utterances are not of a fixed length, it is necessary to pad the utterances to be equal length. The longest utterance in the dataset contains 93 samples. For ease of downsampling within the neural network, we pad all uttereances to be 100 samples long by appending zeros. We also pad each sample to contain 16 features, the 13 MFCCs and 3 zeros to further facilitate down sampling¹.

As we will be classifying the digits, it is necessary to check that padding the digits does not provide a cheat for this. As such, we analise the mean number of samples for each digit and their standard deviations as depicted in Figure 4.1. We then perform a linear regression on the number of samples to demonstrate that it is not possible to accurately predict a digits class given only the length of the utterance.

Figure 4.1 shows the mean number of samples for each digit in the UCU dataset. Whilst there is a difference in the mean length of each digit, the standard deviation for each digit is relatively large as can be seen in Table 4.1. Therefore, trying to classify the digits just by the number of samples in an example, would be ineffective.

Performing a linear regression on the number of samples for each digit versus its class, we get an accuracy of 6.18% when classifying the test set.

¹Downsampling is easier with even numbers of features and samples as we can half the size of the data using strided convolutions, $s=(2,2)$, without worrying about integer division errors e.g. $5/2 = 2$ but $2 \times 2 \neq 5$

Digit	Mean Length (samples)	Standard Deviation
0	39.66	± 29.25
1	37.27	± 25.58
2	43.11	± 31.43
3	45.02	± 34.05
4	44.92	± 31.63
5	34.44	± 23.63
6	50.10	± 35.90
7	42.81	± 30.41
8	55.67	± 41.01
9	38.63	± 30.94

TABLE 4.1: Mean length and standard deviation of digits in the UCU dataset.

MNIST Handwritten Digits

MNIST Handwritten Digits (MNIST) is a well known and often used dataset in the machine learning community. It contains 60000 training samples and 10000 test samples, evenly split between the digits 0 to 9. Each digit is presented as a grey-scale, 28x28 pixel image ?.

Problem Description

The experiments with these datasets will explore two problems, classification and bidirectional symbol grounding.

Classification

Each of the utterances or images from the UCU or MNIST datasets are classified as being a numeric digit, 0 to 9. By combining both datasets, we can explore whether the addition of a second modality enhances overall classification accuracy.

I start off exploring the classification abilities of neural networks by performing a linear regression with a single, dense neural network layer with a softmax activation on the embedding of an autoencoder. To generate baseline classifications accuracies for each dataset, I use autoencoders for each dataset separately.

Once a classification baseline has been established for each dataset, I make use of a multimodal autoencoder, using paired examples from each dataset to train it.

Bidirectional Symbol Grounding

I demonstrate that a neural network can perform bidirectional symbol grounding ? when presented with aligned images and utterances. To explore this, I show how a MAE can learn to reconstruct the correct image of a digit given an utterance as well as MFCCs which have a small mean squared error from the correct utterance given an image of a digit. This shows that an internal symbolic language has been learnt in the form of the latent embedding created by the encoders of the MAE.

Experiment Details

Dataplumbing

Images from the MNIST dataset are kept at their original scale of 28x28 pixels and are normalised such that each pixel has a value from 0 to 1 based on it's intensity, with zero equating to black and 1 being white.

The UCU dataset is normalised so that all MFCCs take a value from 0 to 1 based on the value of the MFCC such that the highest value is 1 and the lowest 0. Utterances are padded to be 100x16 as previously described.

Combining Datasets

Due to the difference in size between the datasets, 8,800 samples for UCU and 80,000 samples for MNIST, I randomly sample from the UCU dataset and pair this with a sample from MNIST. This means that each sample from UCU is repeated approxiamtely 9.1 times ($80000/8800 = 9.0909$).

Merging Modalities

In order to combine the two different modalities, I explore different merging techniques: Concatenation (*Concat*) and Addition (*Add*). To do this, the embeddings of both modalities are ensured to have the same shape and then are merged using the methods described in [Equation 4.1](#) and [Equation 4.2](#), concatenation and addition, respectively.

$$\text{merged} = \text{im}_i^{\text{emb}} || \text{mfcc}_i^{\text{emb}} \quad (4.1)$$

$$\text{merged} = \text{im}_i^{\text{emb}} + \text{mfcc}_i^{\text{emb}} \quad (4.2)$$

Where im_i^{emb} and $\text{mfcc}_i^{\text{emb}}$ represent the embeddings, output by the image and MFCC encoders respectively for image and MFCC inputs im_i and mfcc_i .

Training Procedures

The MAEs are trained in two different ways for both types of merging, these are referred to as bimodal (Bi) and randomly degraded (RD).

Bimodal

Under the bimodal (Bi) training procedure, the MAE is presented with bimodal input for all training instances. That is, both image and MFCC inputs are present for all inputs and the MAE is trained to reproduce this input as its output.

Randomly Degraded

Under the randomly degraded (RD) training procedure, one third of image inputs are removed at random and a third of MFCC inputs are removed at random. It is ensured that each training instance always has at least one input modality present. That is, a training instance never has both its image and MFCC input removed.

The removed modality is replaced with an array of zeros of the same shape as the original input (28x28 for the image and 100x16 for MFCCs).

The MAE is then trained to reproduce both the image and MFCCs regardless of whether one of these has been omitted from the input.

Testing Conditions

Each MAE (Concatenate and Addition) was tested in three different ways, bimodal, image only and MFCC only.

Bimodal

In the bimodal (bi) testing condition both image and MFCC data are used as input for each testing instance and we are interested in observing the classification accuracy as well as the total regeneration loss.

Image Only

In the image only (Im) testing condition, only images are provided as input data. We are interested in the classification accuracy as well as the MFCC reconstruction loss. We are not interested in the image reconstruction loss, as it is expected that, as the image is provided as input this will be low (which it is for all models and training procedures as seen in [Table 4.5](#)).

MFCC Only

Similarly to the image only condition, the MFCC only (MFCC) condition provides only MFCCs as input and we are interested in the classification accuracy as well as the image reconstruction loss. We are not interested in the MFCC regeneration loss as MFCCs are given as input it will be low (which it is for all models and training procedures as seen in [Table 4.5](#)).

Network Description

Baseline Models

To generate the baseline classification accuracies for both the UCU and MNIST data, I make use of unimodal autoencoders. The description of the autoencoder for the MNIST dataset can be found in [Table 4.2](#) and the autoencoder for the UCU dataset in [Table 4.3](#).

Block	Layer	Type	Neurons	Kernel	Strides	Activation
Encoder	1	2D Conv	32	(3,3)	(1,1)	Relu
	2	2D Conv	64	(3,3)	(2,2)	Relu
	3	2D Conv	64	(3,3)	(2,2)	Relu
	4	Dropout p=0.25				
Embedding	5	2D Conv	32	(3,3)	(1,1)	Relu
Classifier	6c	Dense	10			Softmax
Decoder	6	Dropout p=0.25				
	7	2D Trans Conv	64	(3,3)	(2,2)	TanH
	8	2D Transp Conv	64	(3,3)	(2,2)	TanH
	9	2D Trans Conv	32	(3,3)	(1,1)	TanH
	10	2D Trans Conv	1	(3,3)	(1,1)	Sigmoid

TABLE 4.2: Image autoencoder and classifier. Layer 6c performs classification, whilst the branch starting at layer 6 regenerates the image.

Block	Layer	Type	Neurons	Kernel	Strides	Activation
Encoder	1	2D Conv	32	(3,3)	(1,1)	Relu
	2	2D Conv	64	(3,3)	(2,2)	Relu
	3	Dropout p=0.25				
	4	Dense	3136			
	5	Reshape (7,7,64)				
Embedding	6	2D Conv	32	(3,3)	(1,1)	Relu
Classifier	7c	Dense	10			Softmax
Decoder	7	Dropout p=0.25				
	9	Dense	3200			
	10	Reshape (25,4,32)				
	11	2D Trans Conv	64	(3,3)	(2,2)	TanH
	12	2D Trans Conv	64	(3,3)	(2,2)	TanH
	13	2D Trans Conv	32	(3,3)	(1,1)	TanH
	14	2D Trans Conv	1	(3,3)	(1,1)	Sigmoid

TABLE 4.3: MFCC autoencoder and classifier. Layer 7c performs classification, whilst the branch starting at layer 7 regenerates the MFCCs. The addition of reshape layers is to ensure the final shape of the regenerated MFCCs matches the target shape whilst the embedding shape matches that of the embedding of the image autoencoder.

Multimodal Autoencoder

By combining the two autoencoders described in [Table 4.2](#), and [Table 4.3](#), a multimodal autoencoder is created. The embeddings from each of the unimodal autoencoders are merged by either, concatenation or addition.

Block	Layer	Type	Neurons	Kernel	Strides	Activation
Image Encoder	1i	2D Conv	32	(3,3)	(1,1)	Relu
	2i	2D Conv	64	(3,3)	(2,2)	Relu
	3i	2D Conv	64	(3,3)	(2,2)	Relu
	4i	Dropout p=0.25				
MFCC Encoder	1m	2D Conv	32	(3,3)	(1,1)	Relu
	2m	2D Conv	64	(3,3)	(2,2)	Relu
	3m	Dropout p=0.25				
	4m	Dense	3136			
	5m	Reshape (7,7,64)				
Merge	6im	Merge				
Embedding	7im	2D Conv	32	(3,3)	(1,1)	Relu
Classifier	8c	Dense	10			Softmax
Image Decoder	8i	Dropout p=0.25				
	9i	2D Trans Conv	64	(3,3)	(2,2)	TanH
	10i	2D Trans Conv	64	(3,3)	(2,2)	TanH
	11i	2D Trans Conv	32	(3,3)	(1,1)	TanH
	12i	2D Trans Conv	3	(3,3)	(1,1)	Sigmoid
MFCC Decoder	8m	Dropout p=0.25				
	9m	Dense	3200			
	10m	Reshape (25,4,32)				
	11m	2D Trans Conv	64	(3,3)	(2,2)	TanH
	12m	2D Trans Conv	64	(3,3)	(2,2)	TanH
Decoder	13m	2D Trans Conv	32	(3,3)	(1,1)	TanH
	14m	2D Trans Conv	1	(3,3)	(1,1)	Sigmoid

TABLE 4.4: Image and MFCC multimodal autoencoder. Layers marked i, m, im and c are image, MFCC, image and MFCC and classification respectively.

Results

Classification Results

[Table 4.5](#) shows the complete results for all of the experiments run on the combined UCU and MNIST dataset. For convenience, this table is broken down into three other tables: [Table 4.6](#) for the bimodal testing condition, [Table 4.7](#) for the image only condition and [Table 4.8](#) for the MFCC only testing condition.

All results reported here are the mean of a four-fold cross validation. That is, each training and testing condition was run four times and the average results are shown.

In [Table 4.6](#) it can be seen that both Concatenate and Addition merging produce models with better prediction accuracy than the baseline models, regardless of training procedure.

Model	Training	Testing	Im MSE	MFCC MSE	Lb MSE	Total MSE	Acc
Image AE	Im	Im	0.0027		0.0019	0.0046	0.9883
MFCC AE	MFCC	MFCC		0.0113	0.0026	0.0139	0.9832
Add MAE	Bi	Bi	0.0030	0.0401	0.0006	0.0437	0.9967
		Im	0.0076	0.1641	0.0763	0.2479	0.4501
		MFCC	0.1138	0.0399	0.0057	0.1594	0.9624
	RD	Bi	0.0033	0.0176	0.0001	0.0210	0.9993
		Im	0.0027	0.0455	0.0025	0.0508	0.9834
		MFCC	0.0556	0.0166	0.0031	0.0752	0.9789
Concat MAE	Bi	Bi	0.0031	0.0423	0.0009	0.0462	0.9945
		Im	0.0055	0.2029	0.0843	0.2927	0.3496
		MFCC	0.1138	0.0420	0.0079	0.1637	0.9455
	RD	Bi	0.0030	0.0426	0.0002	0.0458	0.9986
		Im	0.0026	0.0737	0.0026	0.0788	0.9834
		MFCC	0.0554	0.0416	0.0026	0.0996	0.9827

TABLE 4.5: Results from the combined MNIST Handwritten Digits and UCU Arabic Spoken Digits

Model	Training	Im MSE	MFCC MSE	Acc
Image AE	Im	0.0027		0.9883
MFCC AE	MFCC		0.0113	0.9832
Add MAE	Bi	0.0030	0.0401	0.9967
	RD	0.0033	0.0176	0.9993
Concat MAE	Bi	0.0031	0.0423	0.9945
	RD	0.0030	0.0426	0.9986

TABLE 4.6: Results from the combined MNIST Handwritten Digits and UCU Arabic Spoken Digits for the bimodal only testing condition.

Model	Training	MFCC MSE	Acc
Image AE	Im		0.9883
Add MAE	Bi	0.1641	0.4501
	RD	0.0455	0.9834
Concat MAE	Bi	0.2029	0.3496
	RD	0.0737	0.9834

TABLE 4.7: Results from the combined MNIST Handwritten Digits and UCU Arabic Spoken Digits for the image only testing condition.

In comparison to the results shown in Table 4.6, the results in Table 4.7 show that the MAEs trained using the bimodal training procedure do not generalise well when only a single input modality is available. Whereas the MAEs trained using the randomly degraded training procedure perform almost as well as the baseline model.

Similarly, the results in Table 4.8 show that the behaviour of the MAEs is very similar under the randomly degraded training procedure regardless of whether it is MFCCs

Model	Training	Im MSE	Acc
MFCC AE	MFCC		0.9832
Add MAE	Bi	0.1138	0.9624
	RD	0.0556	0.9789
Concat MAE	Bi	0.1138	0.9455
	RD	0.0554	0.9827

TABLE 4.8: Results from the combined MNIST Handwritten Digits and UCU Arabic Spoken Digits for the MFCC only testing condition.

or Images being used as input. However, we see that classification accuracy remains reasonably good under the bimodal training procedure when only MFCCs are present.

Reconstruction Results

In [Figure 4.2](#) and [Figure 4.3](#) we see examples of reconstructed digits generated by both the Addition and Concatenation MAEs.

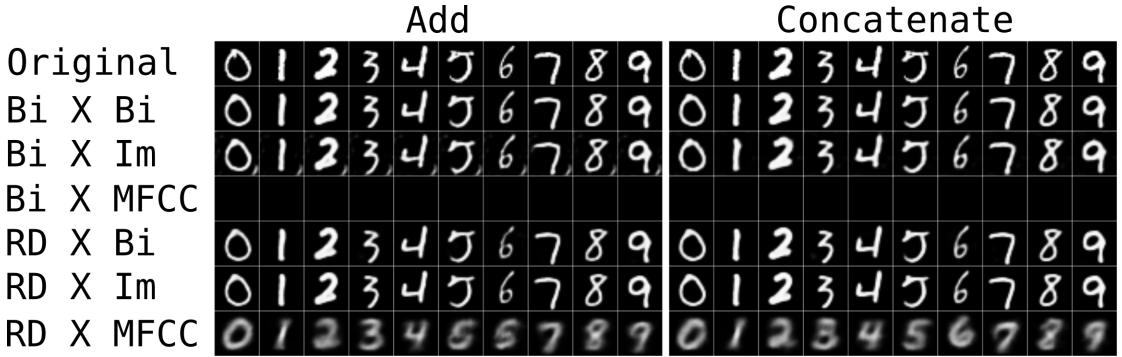


FIGURE 4.2: A selection of randomly sampled digits generated in different training and testing conditions for both *Add* and *Concat* merging methods.

[Figure 4.3](#) shows a comparison of two different examples of the digit “5”. One is (subjectively) poorly written and the other is more prototypical and well formed. We see that under different testing conditions, the MAEs regenerate different “fives”.

Discussion

Discussion of Classification Results

Looking at [Table 4.6](#) we see that both the Add and Concatenate MAEs have better classification accuracy than the baseline, unimodal autoencoder models. However, it is

	A	C
Original	5 5 5 5	
Bi X Bi	5 5 5 5	
Bi X Im	5 5 5 5	
Bi X MFCC		
RD X Bi	5 5 5 5	
RD X Im	5 5 5 5	
RD X MFCC	5 5 5 5	

FIGURE 4.3: Two examples of the digit 5 being generated in different training and testing conditions for both *Add* and *Concat* merging methods.

not clear that there is a difference in between the two training procedures, Bimodal and Randomly Degraded.

The difference between the two training procedures becomes clear when we look at table [Table 4.7](#) where we see that the MAEs trained using the Bimodal training procedure have much worse classification rates when presented with only images as input, performing less than half as well as the baseline model, 0.4501 and 0.3496 for the Addition and Concatenation MAEs respectively versus 0.9832 for the baseline image autoencoder.

We also start to see a trade off between unimodal accuracy and multimodal accuracy when we look at the Randomly Degraded training procedure MAEs. Whilst both the Addition and Concatenation MAEs outperform the baseline models in the bimodal test condition, they have slightly worse performance when tested in either a unimodal image or MFCC manner. For example, the best performance is given by the Addition MAE under the Randomly Degraded training procedure when both images and MFCCs are present as inputs, with an accuracy of 0.9993. However, if one of the modalities is removed, the accuracy drops to 0.9834 and 0.9789 for image only and MFCC only testing respectively. Comparing this to the baseline unimodal autoencoders, we see classification accuracies of 0.9883 and 0.9832 for image and MFCC autoencoders respectively.

This means there is a drop of 0.0049 and 0.0043 for image only and MFCC only testing using the Addition MAE. However, this reduction in performance is counterbalanced by the improvement in performance when both modalities are present, 0.9993 versus the

0.9883 and 0.9832 of the baseline models. This improvement of 0.0110 to 0.0161 over the baseline image and MFCC autoencoders is more than twice the decrease in performance seen when only one modality is available.

Specifically, the improvement of bimodal classification is 2.2449 times larger than the decrease in performance when only images are available ($0.011/0.0049 = 2.2449$). Comparing to the MFCC baseline, the bimodal performance improvement is 3.7442 times larger than the decrease in performance when only MFCCs are available.

Discussion of Reconstruction Results

Observing [Table 4.6](#), [Table 4.7](#) and [Table 4.8](#) we can see that different models had different reconstruction losses (Mean Squared Error). Whilst all MAE models had higher reconstruction losses than the baseline models, this is to be expected. The MAE models are trading off between representing each modality well, whilst the unimodal autoencoders that give the baseline numbers can use their full capacity to minimise the reconstruction loss of their modality as they do not have to reconstruct the second modality.

That being said, the image reconstruction loss, is comparable across all MAE models, approximately 0.0031, (see table [Table 4.6](#) and is very close to the baseline of 0.0027 under the bimodal testing condition (i.e. when the images to be reconstructed are available as input). Further to this, the image reconstruction loss for the MFCC only testing condition is still quite low, though an order of magnitude worse, for the MAEs trained using the Randomly Degraded procedure.

Image reconstruction from MFCCs

The increase in image reconstruction loss when only MFCCs are provided is due to the construction of an internal symbolic language which represents the meaning of both the utterances but not necessarily their fine details. For example, looking at [Figure 4.3](#) we see that there are different ways to write the number 5, however both of these images have the same meaning i.e. the symbol “five”. We should be more interested in preserving this meaning than the minutia of the original images. The same can be said

for reconstructing MFCCs, we are more interested in their meaning than their exact enunciation.

The reconstruction of MFCCs, the reconstruction loss is best for the baseline model but is only 4.0265 times worse for the best performing model on this task. Considering how small the baseline construction error is, being four times worse, is still good performance, especially considering the difficulty of the task.

MFCC reconstruction from Images

The MFCC reconstruction error is an order of magnitude worse than the image reconstruction error. In part this is due to the nature of the data, as seen by the difference in baseline reconstruction errors. I.e. it appears to be more difficult to reconstruct MFCCs than images, even when MFCCs are given as input. Another contributing factor to the worse MFCC reconstruction error for the MAEs, is the imbalance between sample numbers for MNIST and UCU. Whilst both datasets are balanced within themselves (there are an equal number of training samples for each class) there is a big difference between the sizes of MNIST and UCU as discussed previously in section [paragraph 4.2.4.1.1](#).

The difference in sizes between the datasets means that reconstructing MFCCs from image inputs will map a large number of inputs to a smaller number of outputs and vice-versa for generating images from MFCC inputs. Therefore images in the test set which look similar to images in the training set, will be mapped to MFCCs similar to those which the training images map too. As there are a smaller number of MFCC examples to map to, our output is less Gaussian. Whilst ideally we would like to map similar looking digits to similar sounding utterances, there is no guarantee that this is true, either in our dataset or in general. I.e. People with similar handwriting don't necessarily have similar voices. This is simulated by the random assignment of images to MFCCs but this results in discontinuities in the latent space of the network, particularly with respect to generating MFCCs, of which we have fewer examples to capture the true distribution of the data.

Conversely, as there are more examples of images of digits, the distribution of the latent space with respect to the images can get closer to modelling the real distribution of the images. Therefore, given a test MFCC, regardless of whether it is similar to a training

MFCC example, its target image, is more likely to be similar to images in the training data.

Effects of randomly degrading inputs

In [Figure 4.2](#) we can clearly see that randomly degrading the training data has a significant effect, beyond just the improvements to classification accuracy seen in [Table 4.6](#), [Table 4.7](#) and [Table 4.8](#). Both the Addition and Concatenation MAEs fail to learn to generate images from MFCC data when only bimodal data is presented as training data.

Comparing the images generated by the Add and Concatenate MAEs for the MFCC test condition when the training data has been randomly degraded, we see that the concatenate MAE outperforms the Addition MAE. This is particularly clear when you look at the 5 and 6 generated by the Addition MAE for RD X MFCC, where the MAE has failed to correctly generate a six and has instead generated a five, which is similar to the prototypical five generated when MFCCs for a five are presented. Unlike the Addition MAE, the Concatenation MAE, correctly generates all digits, including six.

Multiple generations of the same digit

In [Figure 4.3](#) we see that different examples of the same digit produce different generation results. Most interestingly however, is that the generated fives shown in the RD X MFCC row, you can see that a more prototypical five is generated from MFCCs than if an image of a non-prototypical five is given. This shows that the meaning of the MFCCs have been grounded in the image modality and that an internal symbolic language has been learnt, i.e. the latent embedding of MFCCs are a symbolic representation which has meaning in both MFCC and image space, hence the ability to generate meaningful images and MFCCs from these embeddings.

Conclusion

Whilst multimodal systems can provide better classification accuracy, this comes at the cost of higher computational costs and lower classification accuracy when only one modality is available as demonstrated by the results presented in this chapter.

The ability to reconstruct missing data from a secondary modality demonstrates how an internal symbolic language can be learnt in an unsupervised fashion by processing aligned percepts in multiple modalities.

In future it would be worth while to observe how the reconstructed data can be exploited to improve classification accuracy, for example by first generating a missing data point from modality A and then performing a classification on the embedding of data from modality B and the generated modality A.

This experiment lays the ground work for the next chapter where I will look at how a more complex internal symbolic language can be developed and exploited. I will also discuss how this can be applied to creating robots capable of life long learning.

Chapter 5

Magical Vectors and Where to Find Them

ANN Latent space: the Final Frontier

Tomas Mikilov $V(\text{king}) - V(\text{man}) + V(\text{woman}) = V(\text{Queen})$

Vector Arithematic Explained

Artifical Shapes Dataset

dataset description

problem description

network description

results

Image Generation

Multilabel classification

Vector Arithematic

discussion

Real Shapes Dataset

dataset description

problem description

network description

results

Image Generation

Multilabel classification

Vector Arithematic

discussion

Chapter 6

Transfer Learning: kick-starting the learning process

What is transfer learning

randomly initialised networks

A biological analogue

The importance of transfer learning

MultiSense 1 dataset

dataset description

problem description: image generation from raw speech audio

network description

results

discussion

Chapter 7

What have we learnt and more importantly, what have our neural nets learnt?

Summary of important points

Conclusion

Chapter 8

Future Work

Where do we go now?

More Sensors

Better Sensors

Swarm Robots and the Cloud

Bibliography

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