

$$\text{corr} = \frac{\text{cov}}{\sigma_x \sigma_y} = r$$

$$\text{cov} = \frac{\sum (x_i - \bar{x}) \cdot (y_i - \bar{y})}{N}$$

$$\sigma_x = \sqrt{\frac{\sum (x_i - \bar{x})^2}{N}}$$

$$\text{corr} = \frac{\sum (x_i - \bar{x}) (y_i - \bar{y})}{\sqrt{\sum (x_i - \bar{x})^2} \sqrt{\sum (y_i - \bar{y})^2}}$$

cov & corr
 ↓ ↓
 scale Invariant
 variant



$$z = y$$

x	y
2	2
4	4
6	6
8	8



$$y = mx + c \rightarrow \text{simple}$$

$$y = m_1x_1 + m_2x_2 + \dots + m_Nx_N + c$$

PL

SL

Hgt	Wt

$$Wt = m \times Hgt + c$$

Gradient Descent

$$f(x) = x^2$$

$$x^n \Rightarrow n \cdot x^{n-1}$$

$$\frac{\partial f(x)}{\partial x} = 2x^{2-1} = 2x$$

$$f(x) = 4x^2y + 5x + 100 \rightarrow \partial$$

$$= 8xy + 5 + 0$$

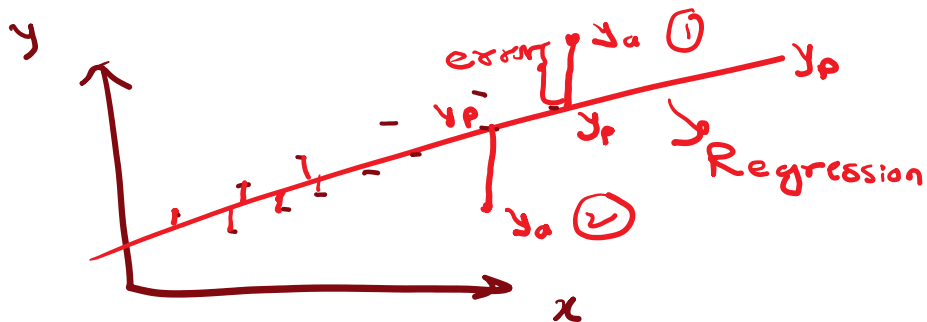
$$= 8xy + 5 + 0$$

$$b(x) = 7x^4y^2 + 9y + 20x + 40$$

$$\frac{\partial b(x)}{\partial x} = 28x^3y^2 + \downarrow 0 + 20 + 0$$

$$b(x) = (4x^3 + y^2)^3$$

$$\begin{aligned} \frac{\partial b(x)}{\partial x} &= 3 \cdot (4x^3 + y^2)^2 \cdot (12x^2 + 0) \\ &= 36x^2 \cdot (4x^3 + y^2)^2 \end{aligned}$$



$$\begin{aligned} \textcircled{1} \text{ error} &= (y_a - y_p) \\ &= 20 - 15 = +5 \end{aligned}$$

$$\begin{aligned} \textcircled{2} E &= 10 - 15 = -5 \\ E &= +5 - 5 = 0 \end{aligned}$$

$$\sum (y_a - y_p)^2$$

$$-5^2 = 25$$

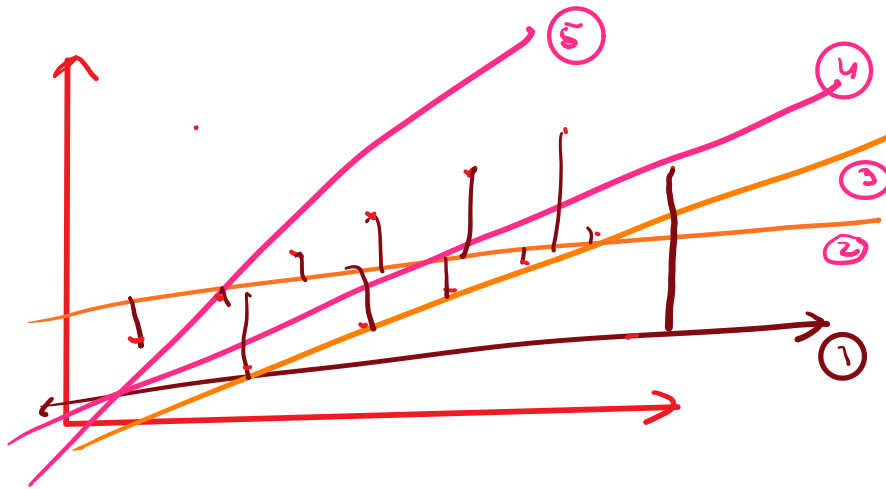
$$+5^2 = 25$$

$$\textcircled{1} \text{ Error} = y_a - y_p$$

$$\begin{aligned} \textcircled{2} SSE &= \sum (y_a - y_p)^2 \\ &\downarrow \quad \quad \downarrow \\ &\text{Sum of Squared Error} \end{aligned}$$

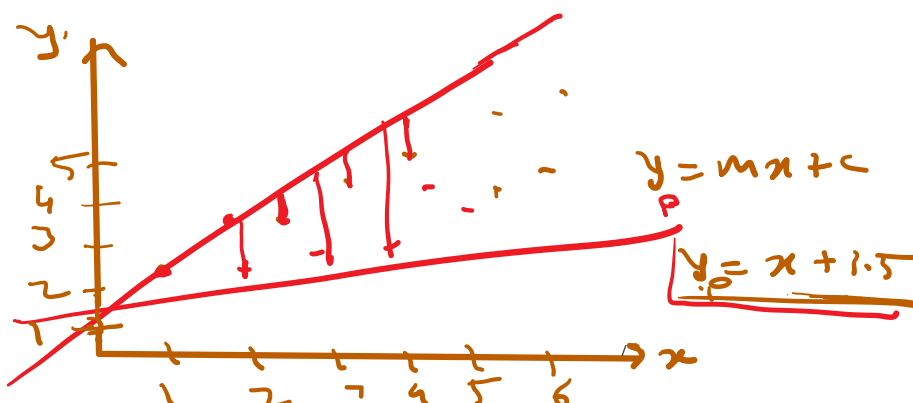
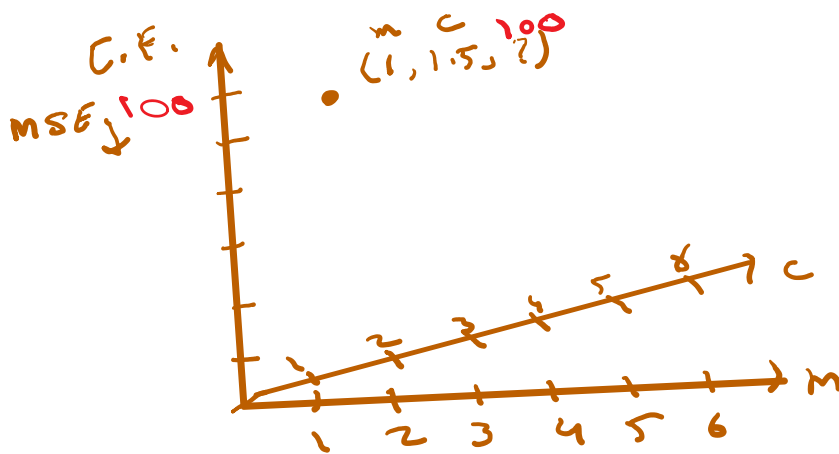
$$\begin{aligned} \textcircled{3} MSE &= \frac{\sum (y_a - y_p)^2}{N} \\ &\downarrow \\ &\text{Cost Function} \end{aligned}$$

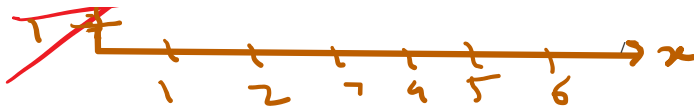
Loss Function



	MSE
①	100
②	150
③	120
④	80
⑤	110

→ Min MSE ↓





$$y = x + 1.5$$

$$x=1, y=2.5$$

$$x=2, y=3.5$$

$$MSF = 10$$

$$m_{new} = m_{old} - L \frac{\partial CF}{\partial m}$$

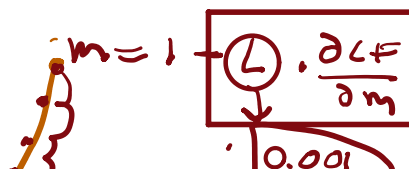
$$c_{new} = c_{old} - L \frac{\partial CF}{\partial c}$$

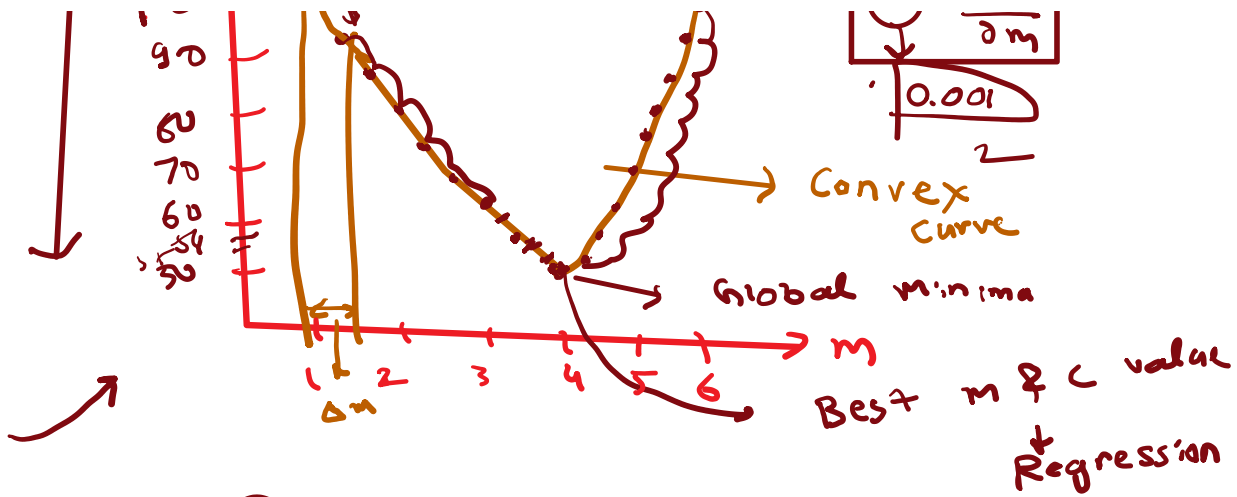
$$\begin{aligned} \frac{\partial CF}{\partial m} &= \frac{\partial}{\partial m} \frac{\sum (y_a - y_p)^2}{N} \\ &= \frac{1}{N} \frac{\partial}{\partial m} \sum [y_a - (mx + c)]^2 \\ &= \frac{1}{N} 2 \cdot [y_a - (mx + c)] \cdot (-x) \end{aligned}$$

$$\boxed{\frac{\partial CF}{\partial m} = \sum \frac{-2x}{N} [y_a - y_p]}$$

$$\begin{aligned} \frac{\partial CF}{\partial c} &= \frac{\partial}{\partial c} \frac{\sum (y_a - y_p)^2}{N} \\ &= \frac{\partial}{\partial c} \frac{\sum (y_a - (mx + c))^2}{N} \\ &= \frac{1}{N} \cdot 2 (y_a - (mx + c)) \cdot (-1) \end{aligned}$$

$$\boxed{\frac{\partial CF}{\partial c} = \frac{-2}{N} (y_a - y_p)}$$





$$\begin{aligned} m_2 &= 1 - 0.001 \times (-200) \\ &= 1 - (-2) \\ &= 1 + 0.2 = 1.2 \end{aligned}$$

$$c_2 = 1.8 \quad y = 1.2x + 1.8$$

$$MSE = 90$$

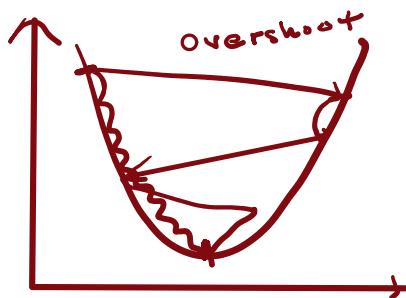
$$m_1 = 6$$

$$m_2 = 5.5$$

$$m_3 = 5.3$$

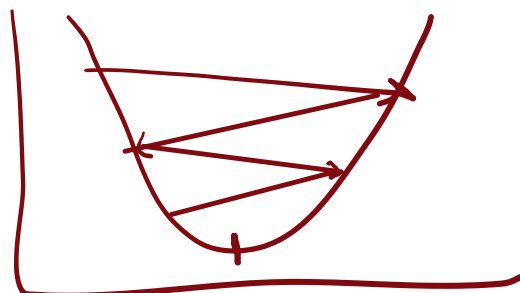
$$m_4 = 5.0$$

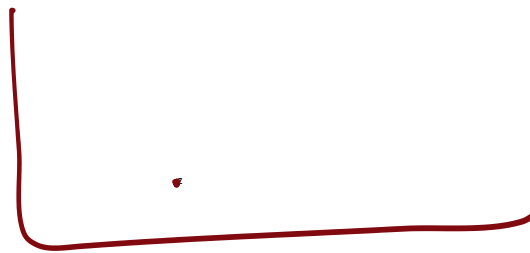
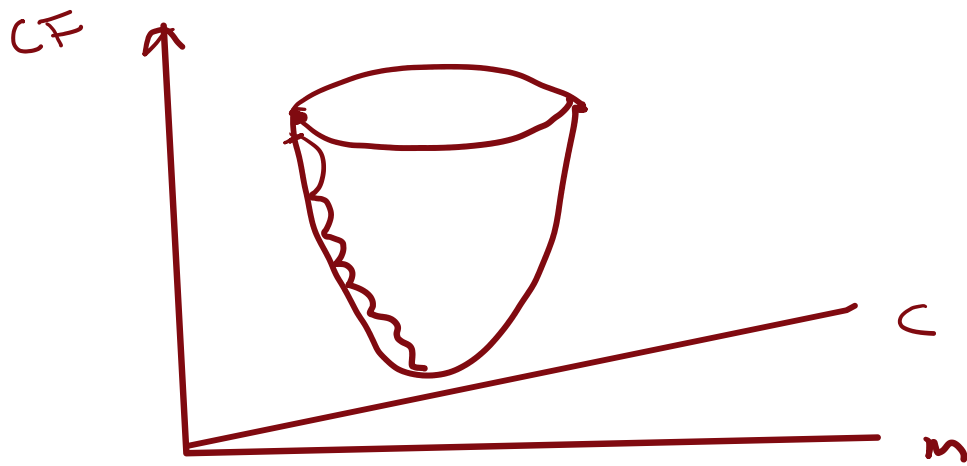
$$m_5 = 4$$



$$m_1 = 1$$

$$\begin{aligned} m_2 &= 1 - (2) \times (-2) \\ &= 1 + 4 = 5 \end{aligned}$$





Line	m	C	MSE(CF)
①	1	1	100
②	1.5	1.2	80
③	2	3	60
④	3	5	40
⑤	4	6	300 → <u>BFL</u>

BFL → Best m
 → Best C