Support Vector Machines

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Classification Techniques

- Decision Tree based Methods
- Rule-based Methods
- Memory based reasoning
- Neural Networks
- Naïve Bayes and Bayesian Belief Networks
- Support Vector Machines

Support Vector Machines

- Theoretically well motivated algorithm: developed from Statistical Learning Theory (Vapnik & Chervonenkis) since the 60s

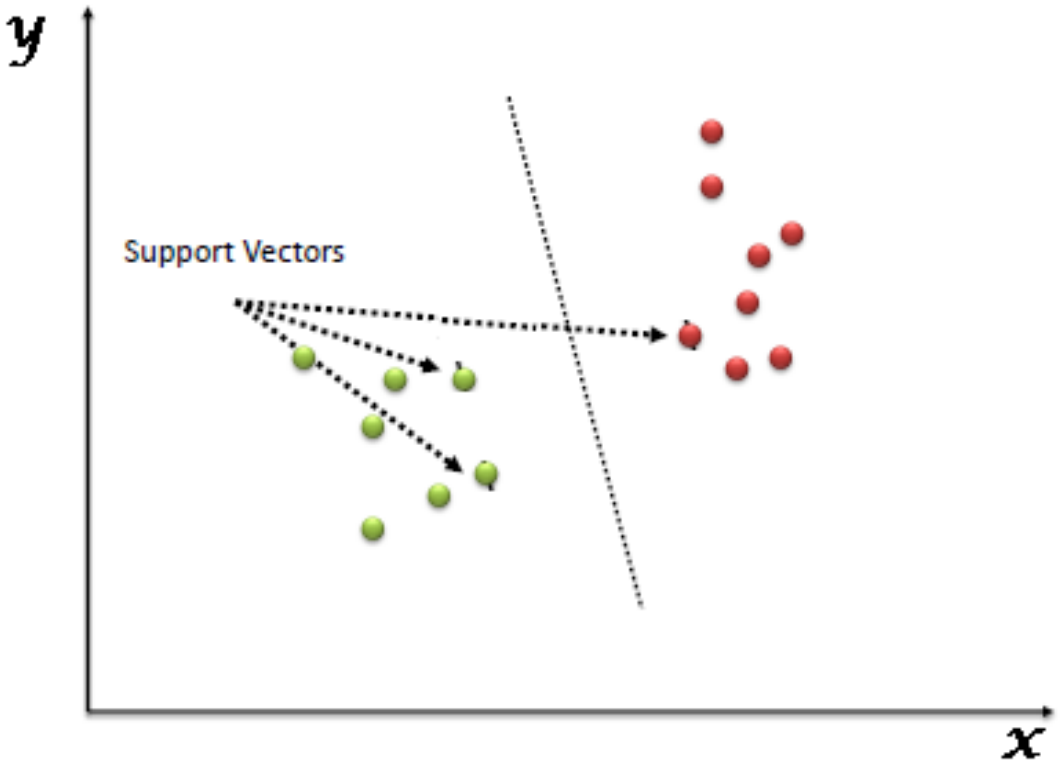
- Empirically good performance: successful applications in many fields (bioinformatics, text, image recognition, . . .)

Support Vector Machines

- Centralized website: www.kernel-machines.org.
- Several textbooks, e.g. ”An introduction to Support Vector Machines” by Cristianini and Shawe-Taylor is one.
- A large and diverse community work on them: from machine learning, optimization, statistics, neural networks, functional analysis, etc

Support Vector Machine

- *The goal of a support vector machine is to find the optimal separating hyperplane which maximizes the margin of the training data*
- Support Vector Machine" (SVM) is a supervised machine learning algorithm which can be used for both classification or regression challenges
- However, it is mostly used in classification problems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Support Vectors
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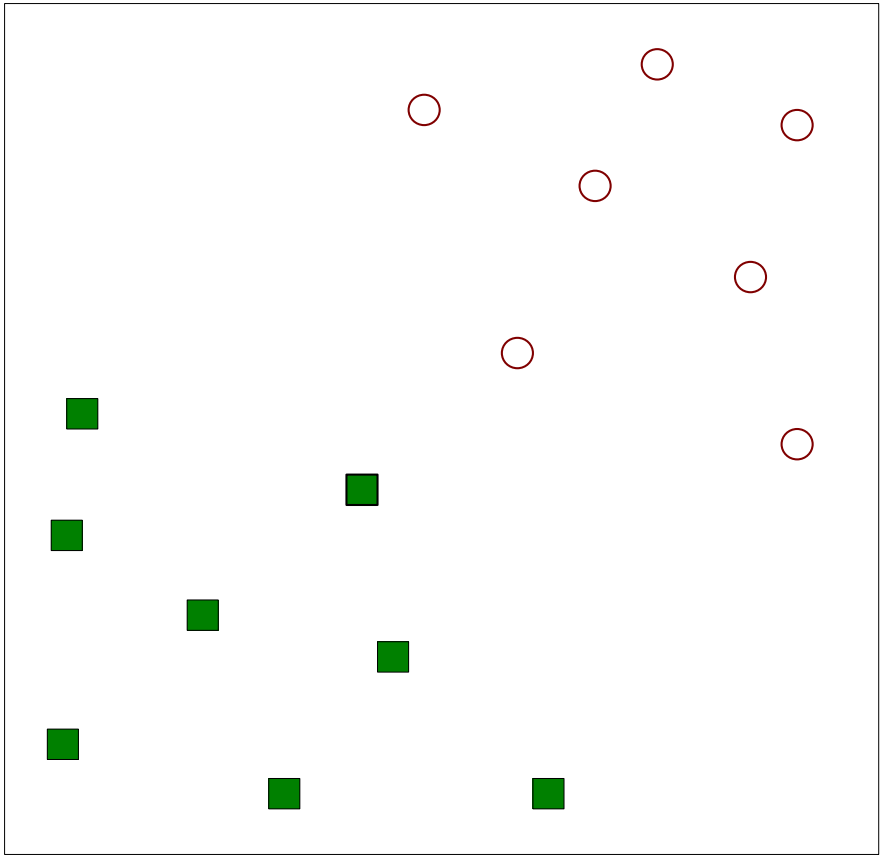
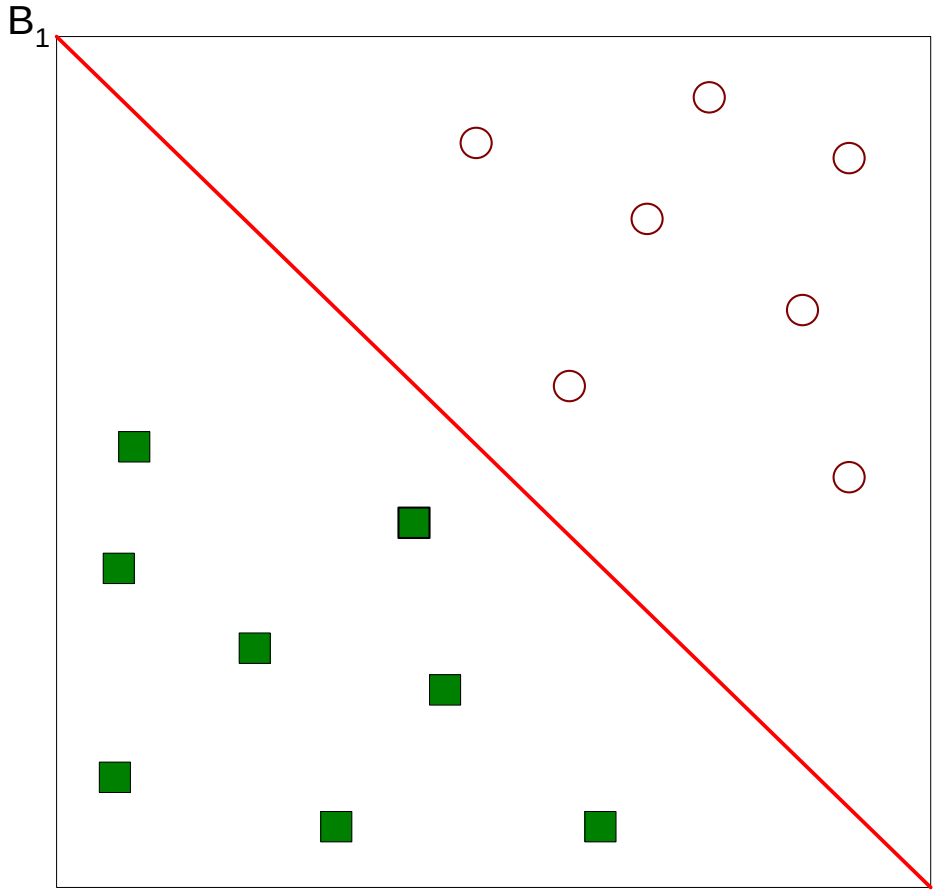
Support Vector Machines



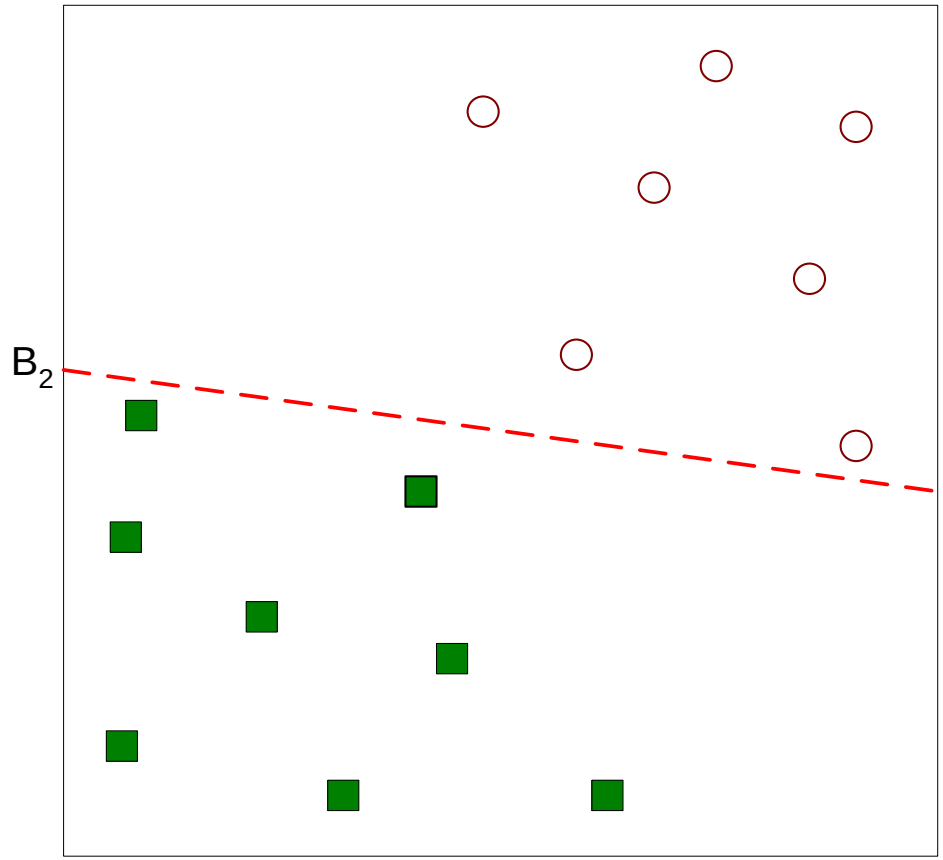
- Find a linear hyperplane (decision boundary) that will separate the data

Support Vector Machines



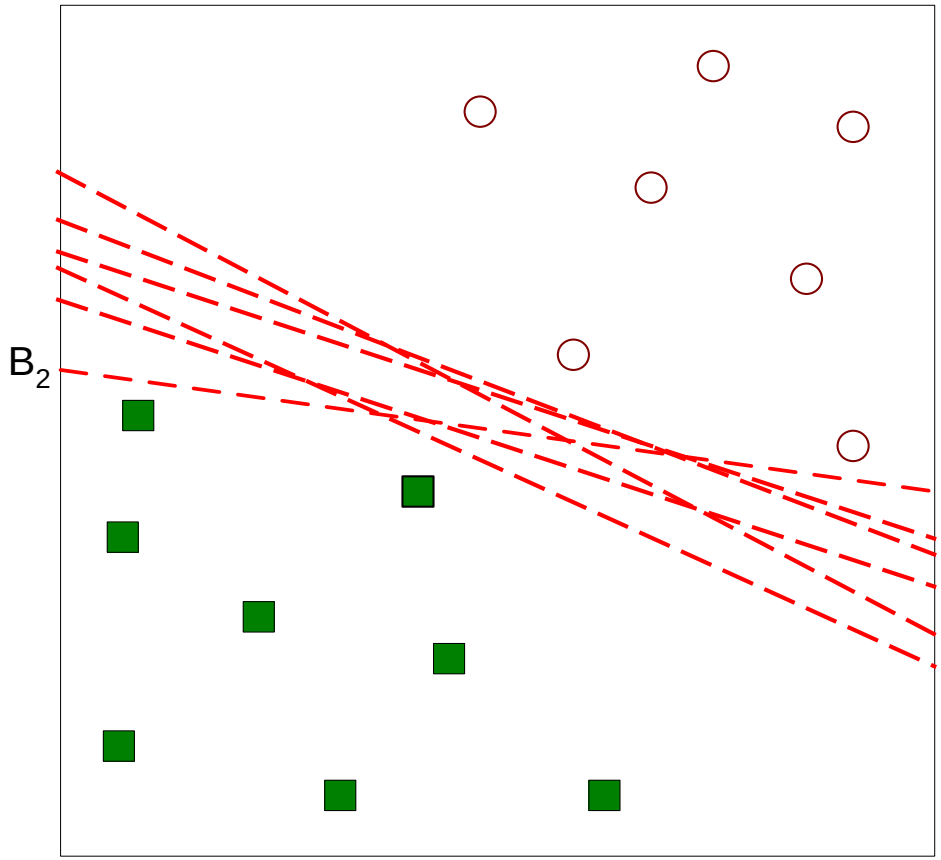
- One Possible Solution

Support Vector Machines



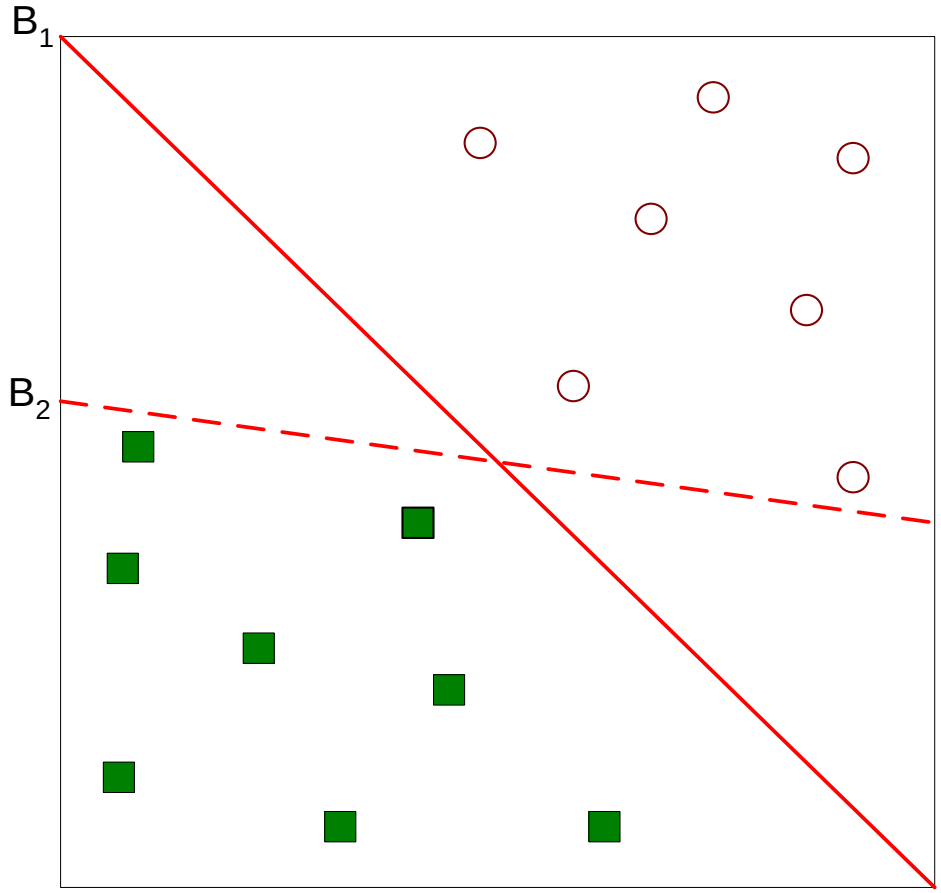
- Another possible solution

Support Vector Machines



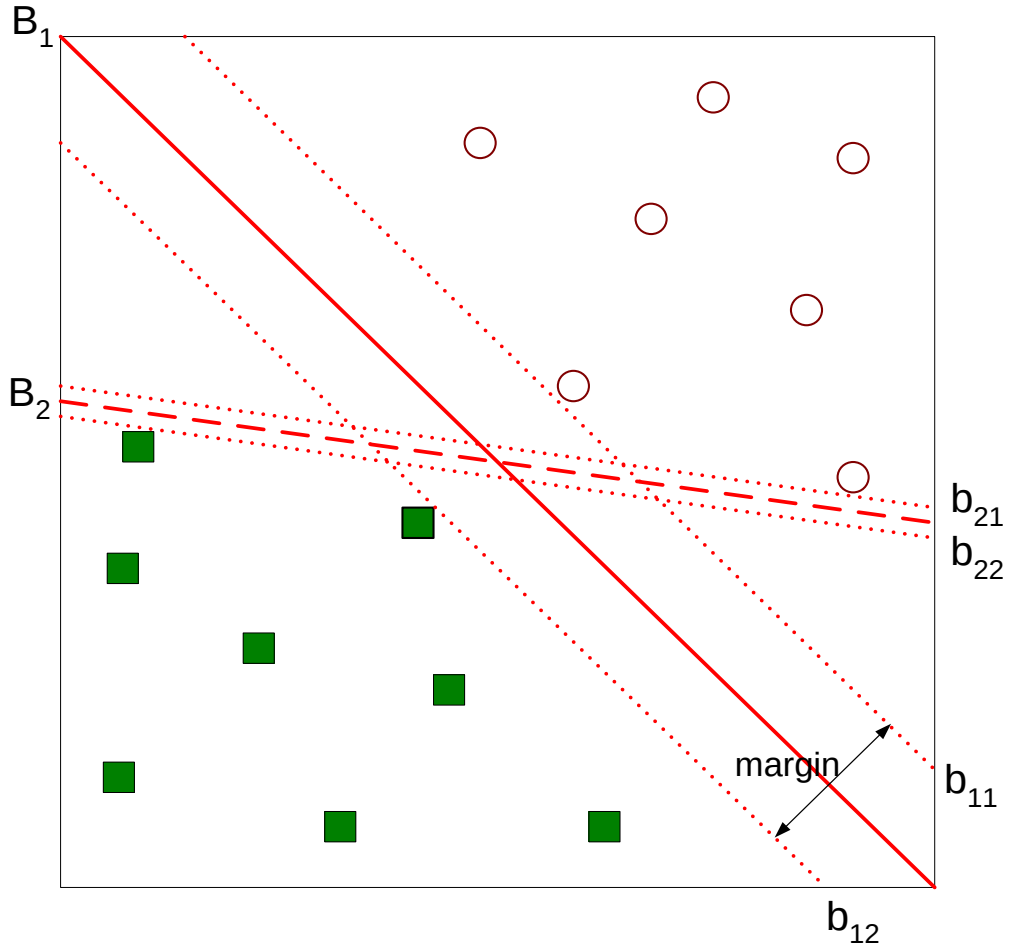
- Other possible solutions

Support Vector Machines



- Which one is better? B1 or B2?
- How do you define better?

Support Vector Machines



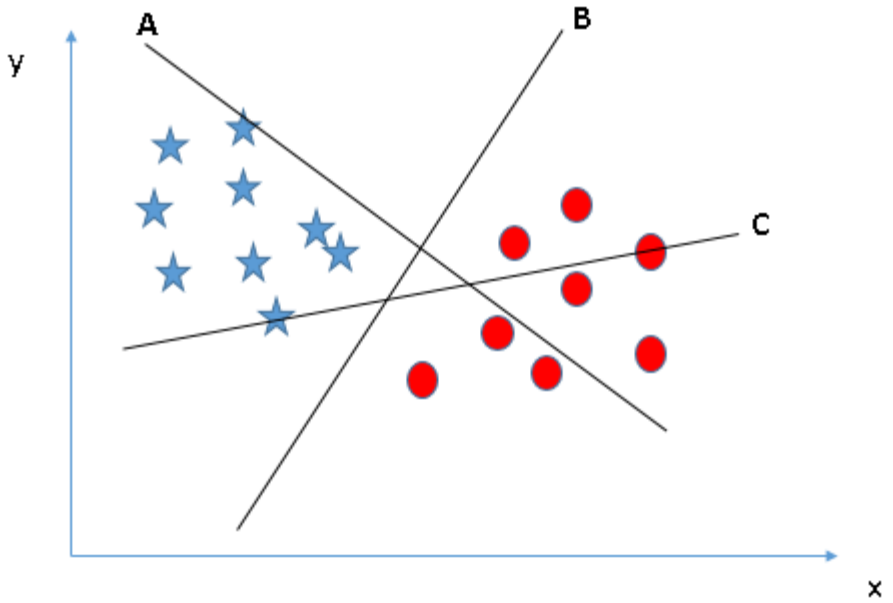
- Find hyperplane maximizes the margin => B1 is better than B2

What is a Hyperplane

An hyperplane is a generalization of a plane

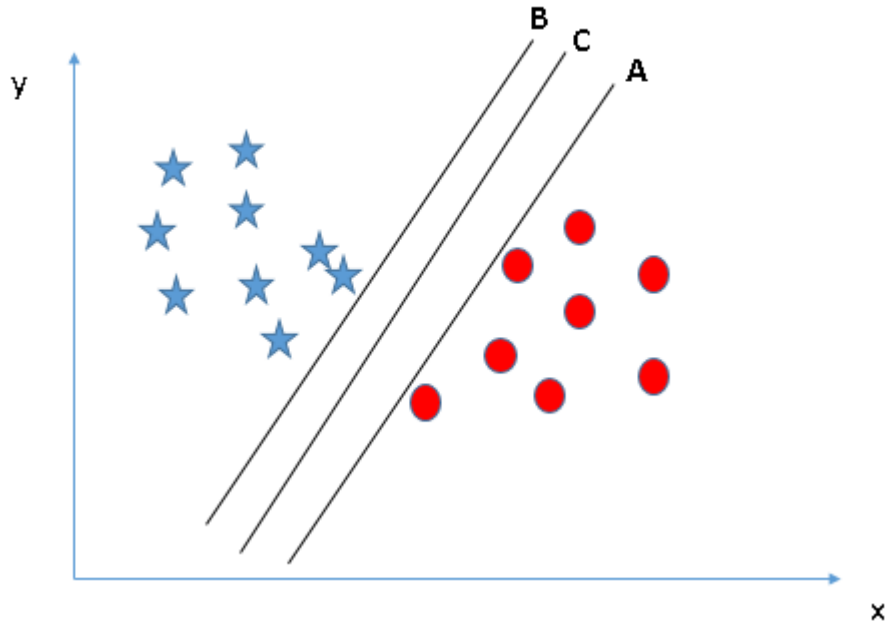
- in one dimension, an hyperplane is called a point
- in two dimensions, it is a line
- in three dimensions, it is a plane
- in more dimensions you can call it an hyperplane

Identify the right hyper-plane (Scenario-1)



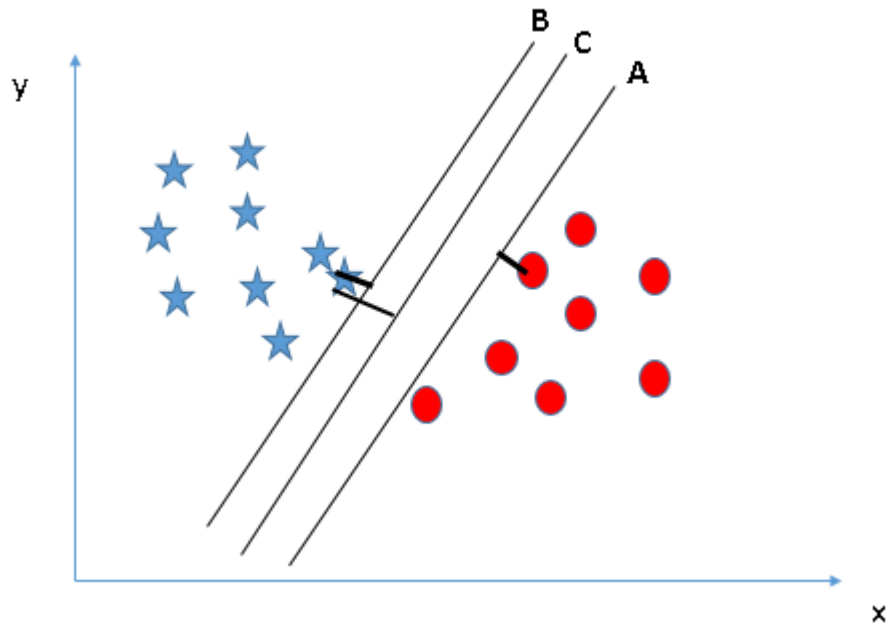
Select the hyper-plane which segregates the two classes better". In this scenario, hyper-plane "B" has excellently performed this job

Identify the right hyper-plane (Scenario-2)



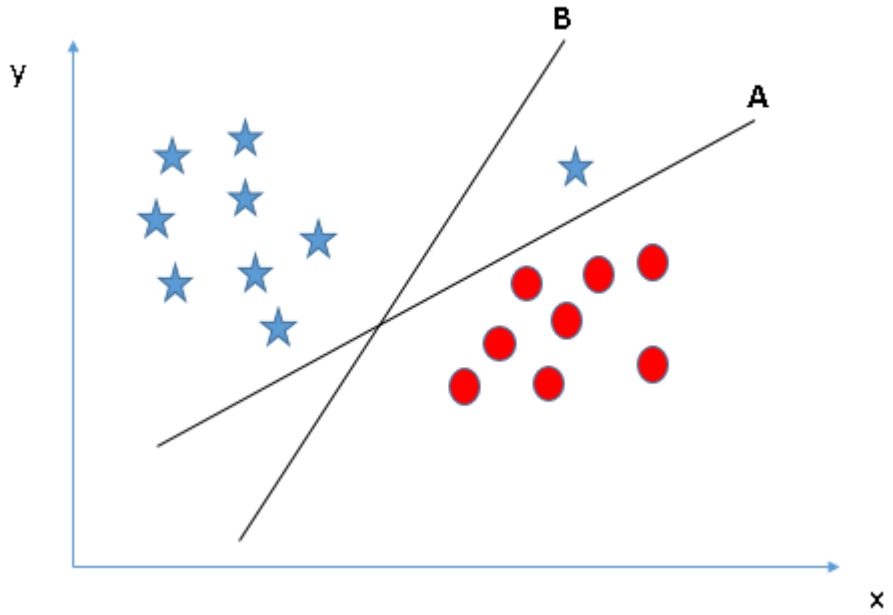
- A, B and C are all good hyperplanes
- Here, maximizing the distances between nearest data point (either class) and hyper-plane will help us to decide the right hyper-plane
- This distance is called as **Margin**

Identify the right hyper-plane (Scenario-2)



- Margin for hyper-plane C is high as compared to both A and B
- Hence, we name the right hyper-plane as C
- Another lightning reason for selecting the hyper-plane with higher margin is robustness
- If we select a hyper-plane having low margin then there is high chance of miss-classification

Identify the right hyper-plane (Scenario-3)

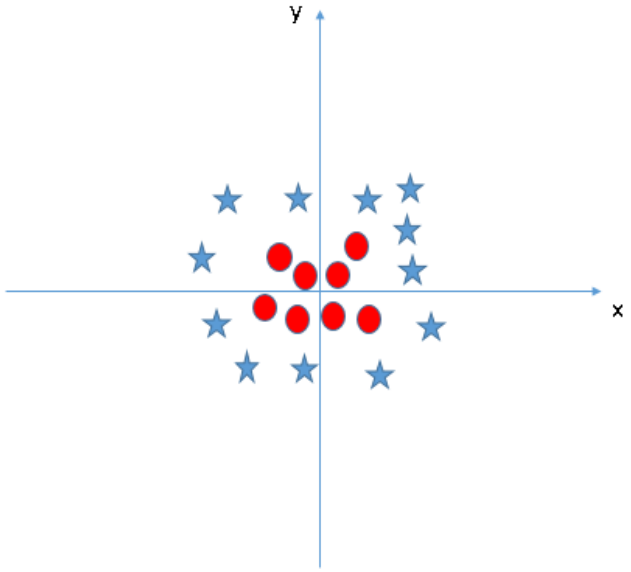


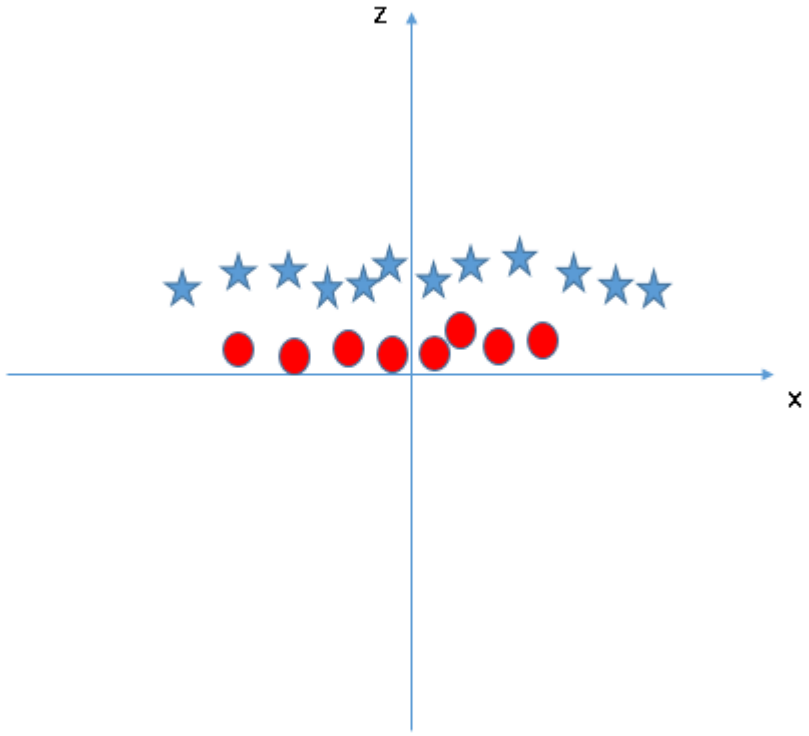
- Hyper-plane **B** may be selected due to higher margin compared to **A**
- But, here is the catch, SVM selects the hyper-plane which classifies the classes accurately prior to maximizing margin
- Here, hyper-plane B has a classification error and A has classified all correctly. Therefore, the right hyper-plane is **A**

Identify the right hyper-plane (Scenario-4)

- Outliers ignored by SVM

Identify the right hyper-plane (Scenario-5)

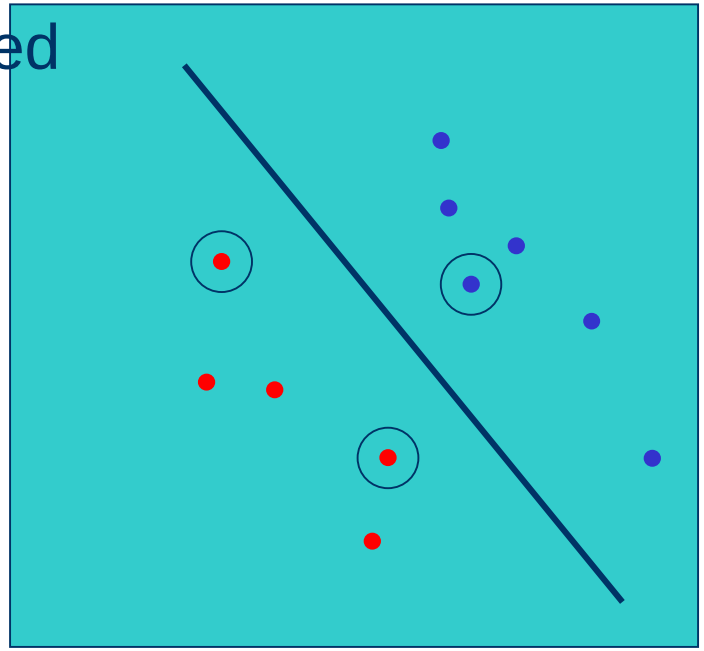




- z=x^2+y^2

Support Vector Machines

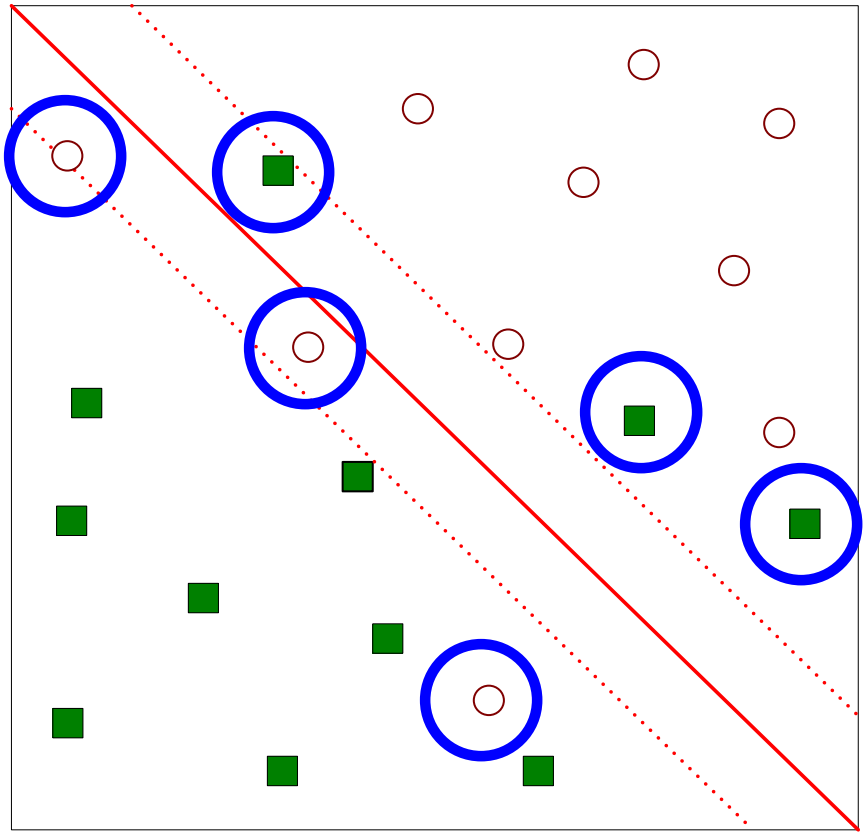
- The support vectors are indicated by the circles around them



- Datapoints in this subset are called “support vectors”
- It will be useful computationally if only a small fraction of the data points are support vectors,
- Since, we use the support vectors to decide which side of the separator a test case is on

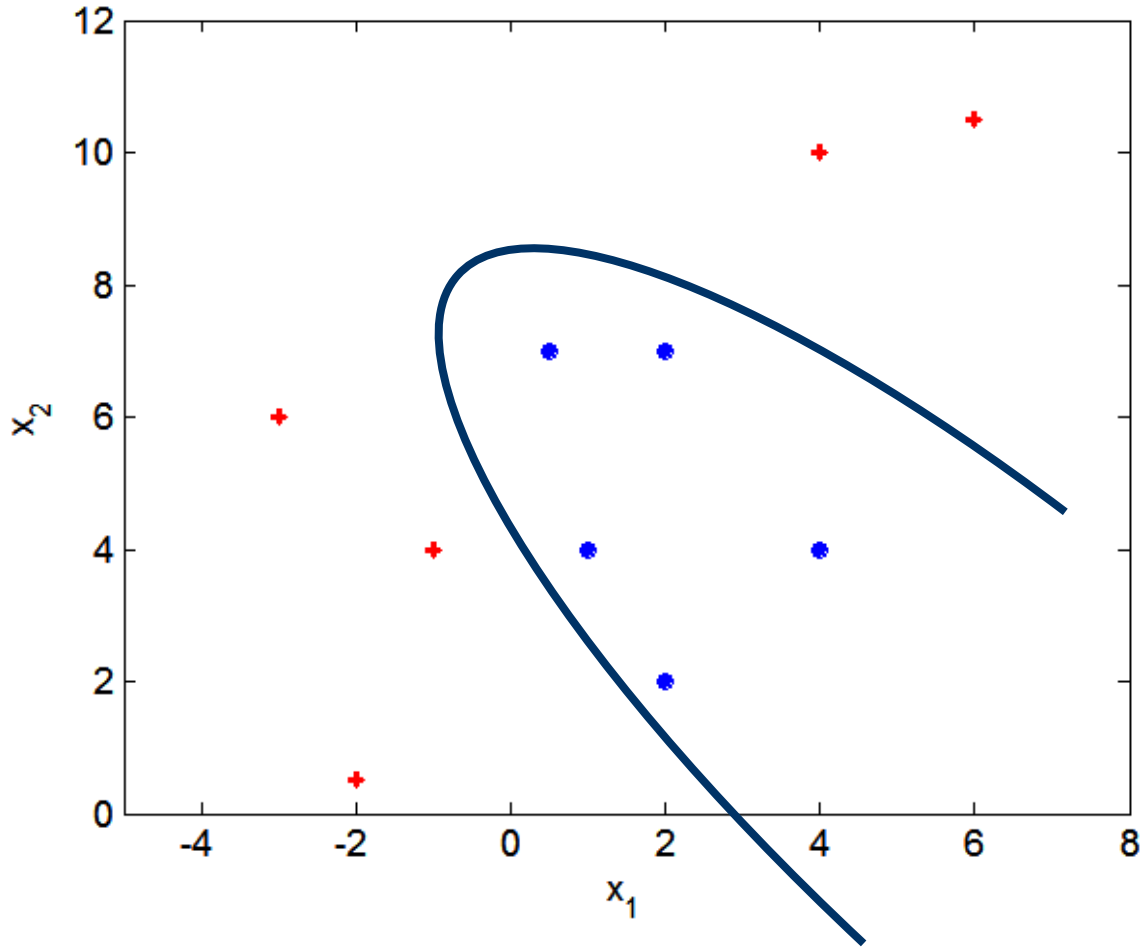
Support Vector Machines

- What if the problem is not linearly separable?



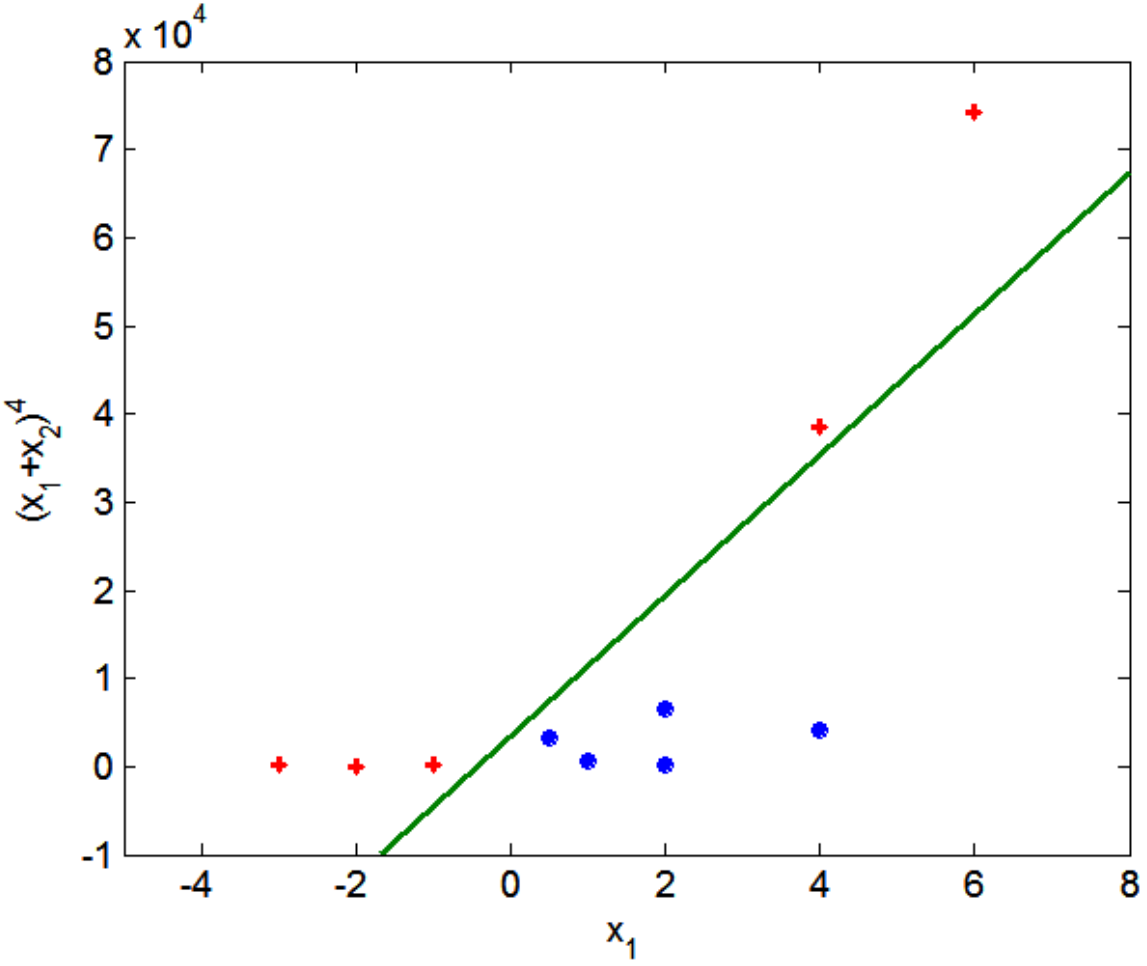
Nonlinear Support Vector Machines

- What if decision boundary is not linear?



Nonlinear Support Vector Machines

- Transform data into higher dimensional space



Nonlinear Support Vector Machines

- Kernel Trick
  - SVM has a technique called the kernel **trick**
  - These are functions which takes low dimensional input space and transform it to a higher dimensional space
  - i.e. it converts not separable problem to separable problem, these functions are called kernels
  - It is mostly useful in non-linear separation problem
  - http://crsouza.com/2010/03/17/kernel-functions-for-machine-learning-applications/

References

- Introduction to Data Mining by Tan, Steinbach, Kumar (Lecture Slides)
- https://www.analyticsvidhya.com/blog/2015/10/understaing-support-vector-machine-example-code/
- http://www.svm-tutorial.com/2014/11/svm-understanding-math-part-1/

Questions!