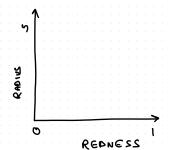
K-Nearest Neighbors

Nipun Batra

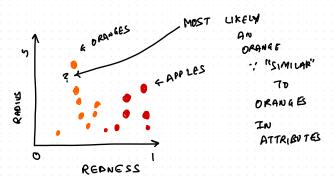
July 21, 2025

IIT Gandhinagar

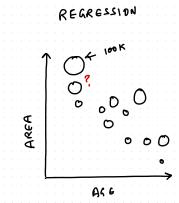






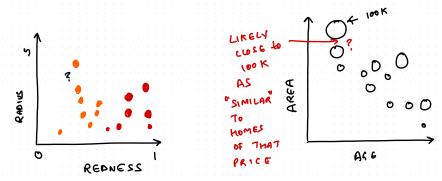




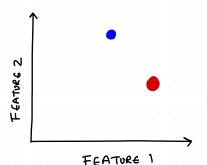




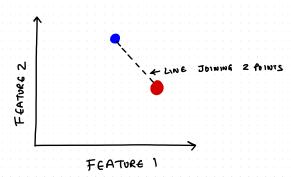
REGRESSION



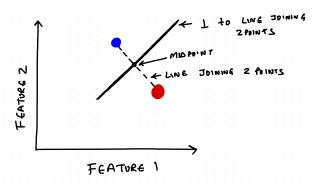
VORONOL DIAGRAM FOR I-NA

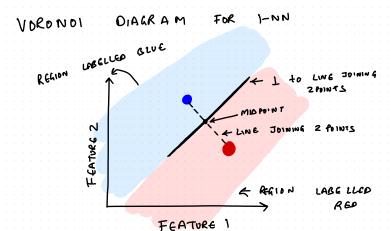


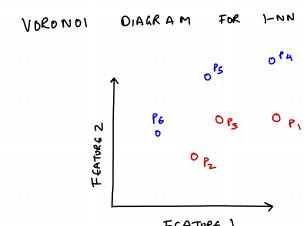
VIDRONOL DIAGRAM FOR I-NN

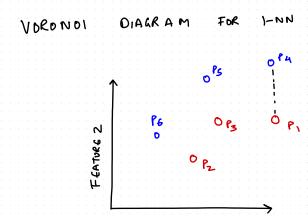


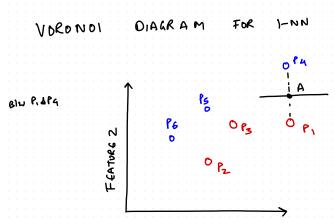
VINRONOL DIAGRAM FOR I-NN

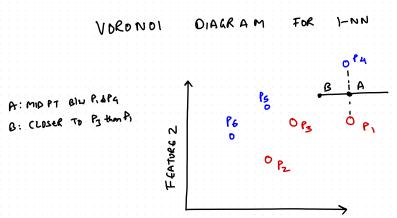


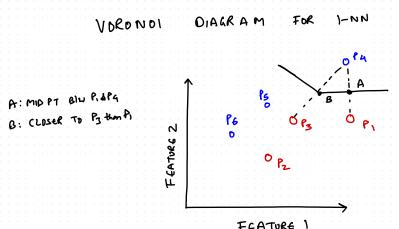


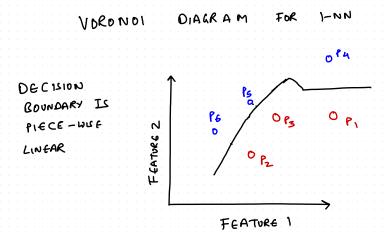


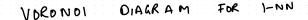


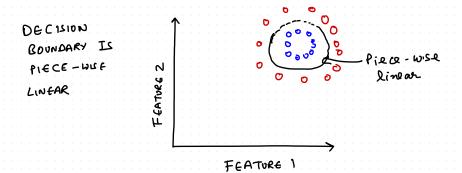






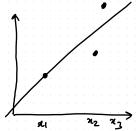


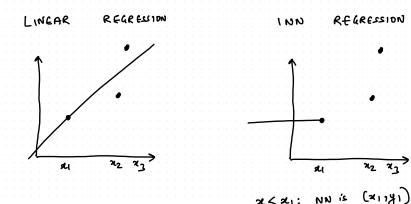


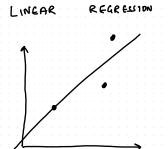


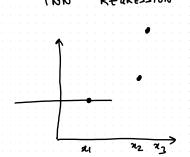
LINCAR REGRESSION

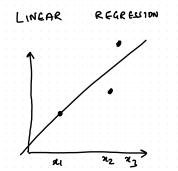
REGRESSION

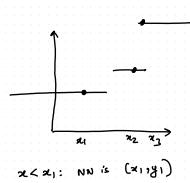












KNN IS NON- PARAMETRIC

MODEL

LINEAR

IS NOW- PARAMETRIC

LINEAR MODEL

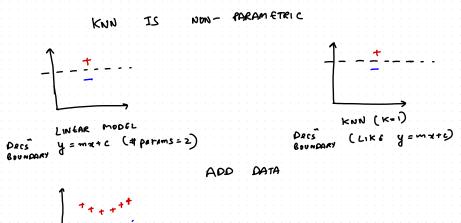
y = matc (# params = 2)

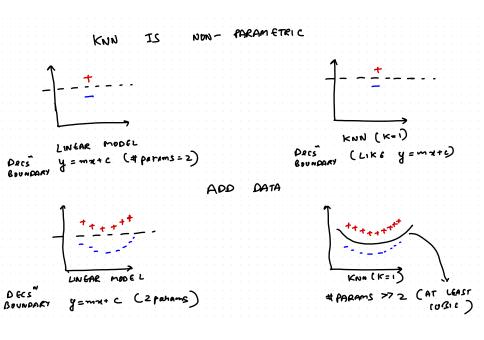
LINEAR MODEL

S Y = mate (# params = 2)

RNN (K=1)

Pars (LIKE Y = mate





PARAMETRIC

TRARAMS FIXED WRT DATASET SIZE

MAKE ASSUMPTIONS
(LIKE FUNCTIONAL FORM)

SUALLY QUICKER

Eq: LINEAR MODELS,
SUM (LINEAR, POZY NOMIAL)

ON -PARAM ETRIC

PARAMS GROWS WRT DATASET SIZE

SLER ASSUMPTION

Eg: KNN, DT, Sum (with



Parametric vs Non-Parametric Models

	Parametric	Non-Parametric
Parameter	Number of parame-	Number of parame-
	ters is fixed w.r.t	ters grows w.r.t. to
	dataset size	an increase in dataset
		size
Speed	Quicker (as the num-	Longer (as number of
	ber of parameters are	parameters are less)
	less)	
Assumptions	Strong Assumptions	Very few (sometimes
	(like linearity in Linear	no) assumptions
	Regression)	
Examples	Linear Regression	KNN, Decision Tree

Lazy vs Eager Strategies

	Lazy	Eager
Train Time	0	≠ 0
Test	Long (due to compar-	Quick (as only
	ison with train data)	"parameters" are
		involved)
Memory	Store/Memorise en-	Store only learnt pa-
	tire data	rameters
Utility	Useful for online set-	
	tings	
Examples	KNN	Linear Regression,
		Decision Tree

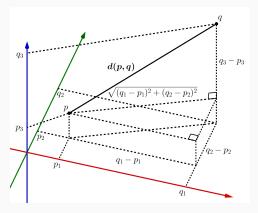
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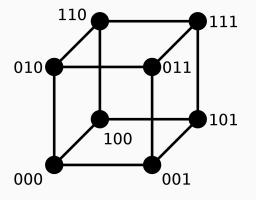
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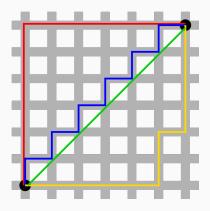
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- What is the distance metric that will be used to calculate data similarity?
- What is the aggregation function that is going to be used?
- What are the number of neighbors that you are going to take into consideration?
- What is the computational complexity of the algorithm that you are implementing?



Euclidean Distance



Hamming Distance



Manhattan Distance

Choosing the correct value of K is difficult.

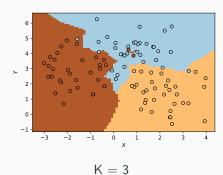
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Low values of K will result in each point having a very high influence on the final output ⇒ noise will influence the result

High values of K will result in smoother decision boundaries ⇒ lower variance but also higher bias



Aggregating data

There are different ways to go about aggregating the data from the K nearest neighbors.

Median

Aggregating data

There are different ways to go about aggregating the data from the ${\sf K}$ nearest neighbors.

- Median
- Mean

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- Median
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- Mode

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- For a query vector *q*:

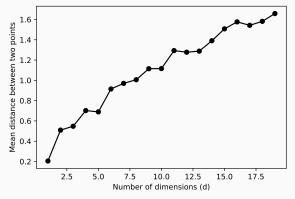
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 - 1. Find the k-closest data point(s) x^*

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- For a query vector *q*:
 - 1. Find the k-closest data point(s) x^*
 - 2. Predict y^*

With an increase in the number of dimensions:

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1. the distance between points starts to increase



For a unifromly random dataset

With an increase in the number of dimensions:

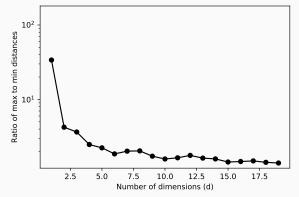
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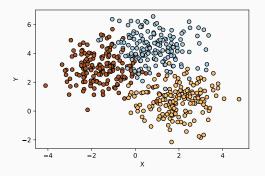
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Example of a big dataset

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- Vector approximation files

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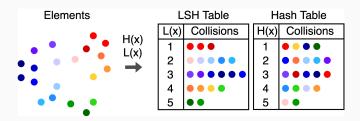
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Such techniques include:

- Locality sensitive hashing
- Vector approximation files
- Greedy search in proximity neighborhood graphs

Locality sensitive hashing

Normal hash functions H(x) try to keep the collision of points across bins uniform.

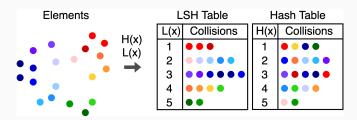


Example of a big dataset

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A locality sensitive hash (LSH) function L(x) would be designed such that similar values are mapped to similar bins.

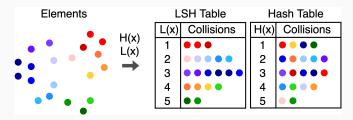


Example of a big dataset

Locality sensitive hashing

A locality sensitive hash (LSH) function L(x) would be designed such that similar values are mapped to similar bins.

For such cases, all elements in a bin would be given the same label, which again can be decided on the basis of different aggregation methods



Example of a big dataset

