# Reinforcement Learning

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# **Forecasting**

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## Acknowledgement

Forecasting: Principles and Practice

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- New open standards created in the mobile era, such as HTML5, will win on mobile devices (and PCs too). Perhaps Adobe should focus more on creating great HTML5 tools for the future, and less on criticizing Apple for leaving the past behind. (Steve Jobs about Flash in 2010)

### **Applications**

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- Stocking an inventory based on forecast of stock requirements

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- whether the forecasts can affect the thing we are trying to forecast.

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- the fact that we can forecast stock prices will lead to change in market dynamics and it will affect the forecast

## **Example of Forecasting**

Forecast of production of beer in Australia

Dark blue lines show the mean forecast Light blue band shows the confidence interval

### Three Types of Forecasting Models

Task: Forecast Electricity Demand at Time T

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3. Mixed model

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- A large increase in passenger load occurred in the second half of 1991.
- There are some large dips in load around the start of each year. These are due to holiday effects.

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- **Season**: Time series is affected by seasonal factors such as the time of the year or the day of the week
- Cyclic: A cycle occurs when the data exhibit rises and falls that are not of a fixed frequency.

## Seasonal v/s Cyclic

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- Seasonality: within every year, there is pattern of sales
- $\bullet$  Cyclic: Every 6 years or so, there is a similar pattern

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  - Let us assume we are forecasting monthly and we want to forecast for Mar 2020 (month=3) and current time is Jan 2020 (month=1). Thus, h=2. Let us assume yearly seasonality, i.e. m=12. Thus, prediction for Mar 2020 is value at (Jan+2 months)  $12 \times 2 1\%12 = Mar 2020 12 Months = Mar 2019$

Learning: Simple solutions often work well, especially if you know about the domain.

## **Evaluating Forecast Accuracy**

Timeseries cross-validation for 1 timestep ahead prediction

Question: How do you nested CV?

Answer: Similarly divide the train into train and validation

preserving the notion of timeseries.

# **Evaluating Forecast Accuracy**

Timeseries cross-validation for k=4 timestep ahead prediction

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- White noise series is stationary it does not matter when you
  observe it, it should look much the same at any point in time.

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- Series with seasonality: d, h, i
- Stationary: b and g (cycles are aperiodic)

## Differencing

What is the relation between a and b? b is the first order time difference of a! b is stationary, while a is not!

## Differencing

For (a) the ACF is significant For (b), the ACF declines rapidly

## Autoregression

$$y_t = c + \phi_1 y_{t-1} + \phi_2 y_{t-2} + \dots + \phi_p y_{t-p} + \varepsilon_t$$
, where  $\varepsilon_t$  is white noise.