# Bias-Variance and Cross Validation

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At very high depths, test accuracy is not good
(overfitting).

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Why can't we directly optimize for test error?

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- **Model Selection**: Choose complexity that balances bias and variance
- **No Free Lunch**: Cannot reduce both bias and variance simultaneously

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