Cross-Validation

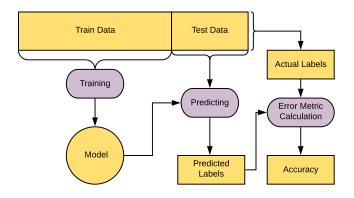
Nipun Batra and teaching staff

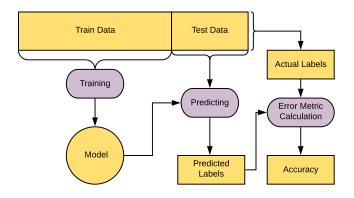
IIT Gandhinagar

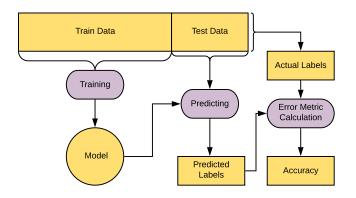
August 1, 2025

Outline

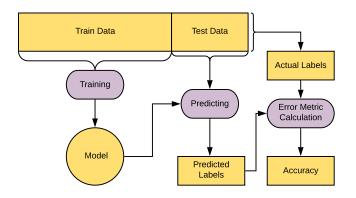
- 1. Introduction to Cross-Validation
- 2. Full Dataset Utilization
- 3. K-Fold Cross-Validation
- 4. Hyperparameter Optimization
- 5. Nested Cross-Validation
- 6. Cross-Validation Variants
- 7. Time Series Cross-Validation
- 8. Common Pitfalls and Best Practices
- 9. Summary and Key Takeaways



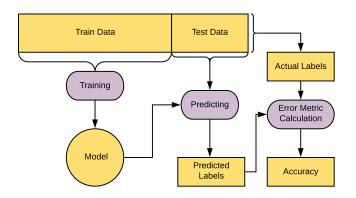




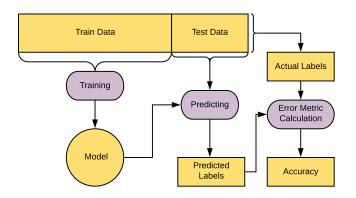
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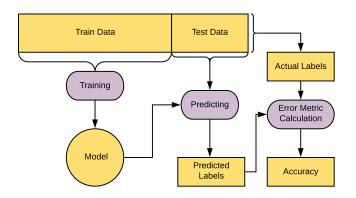
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- Does not use the full dataset for training and does not test on the full dataset
- No way to optimize hyperparameters
- This simple train/test split has limitations we need to

Question

What are the main limitations of using only a single train/test split?

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- Does not utilize the full dataset for training
- · Cannot optimize hyperparameters systematically
- Results depend on the particular split chosen
- May not get reliable performance estimates

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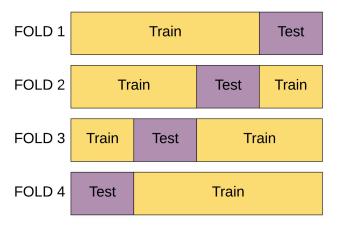
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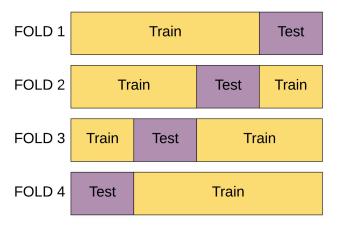
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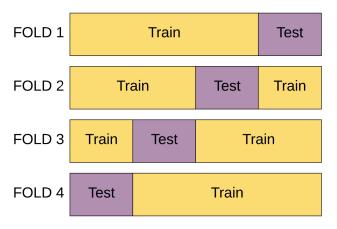
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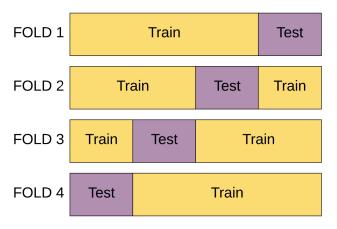
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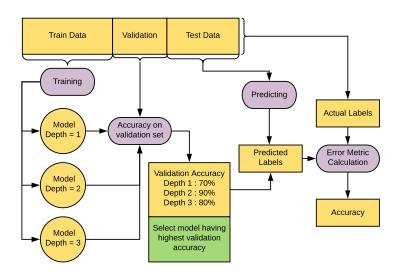
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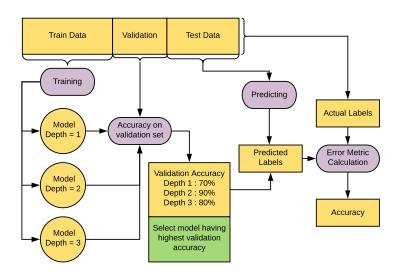
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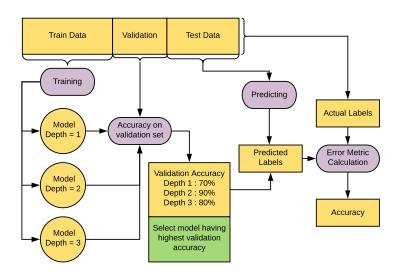
80 data points (4 out of 5 folds = $4/5 \times 100 = 80$)

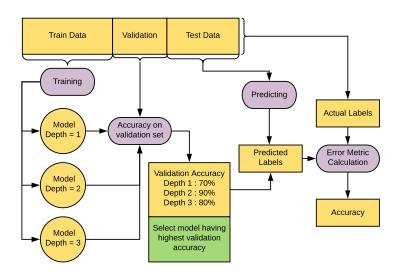
Optimizing Hyperparameters via the Validation Set

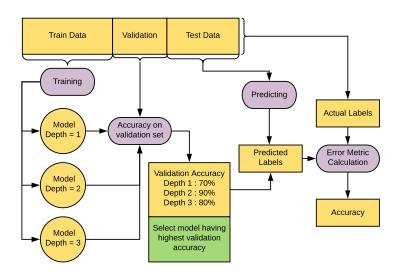


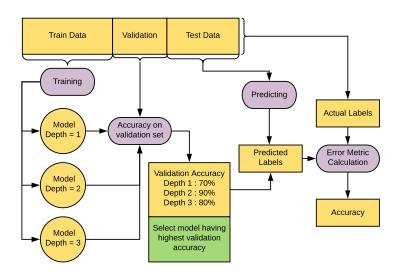
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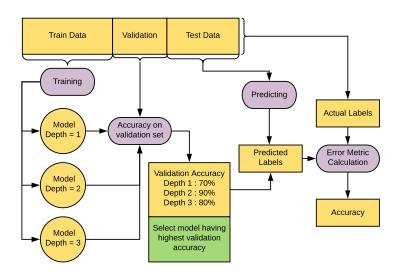






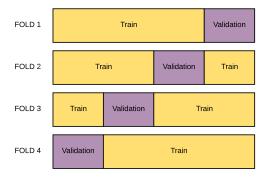






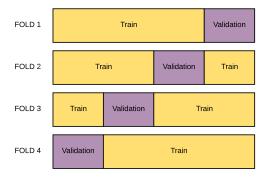
Divide your training set into k equal parts. Cyclically use 1 part as "validation set" and the rest for training.

Here k=4



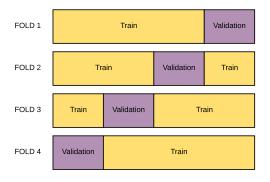
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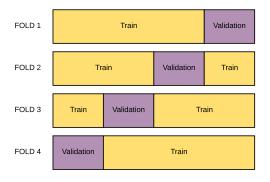
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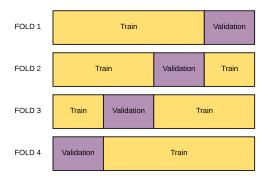
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- · Each fold provides one validation score
- Process is systematic and exhaustive

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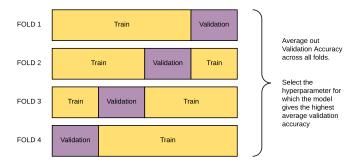
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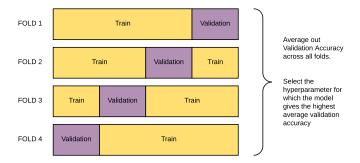
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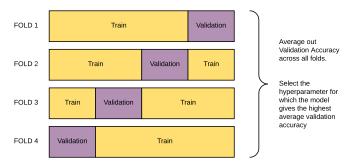
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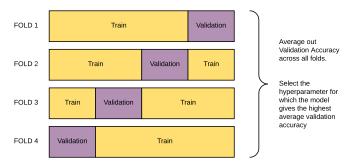


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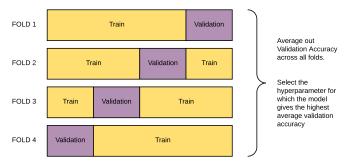
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- Final model is trained on entire training set
- Standard deviation gives confidence in results

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- Never use future data to predict past!

Common Cross-Validation Mistakes

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- Ignoring Class Imbalance: Not using stratified CV when needed

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- This gives more realistic performance estimates

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