

# Unsupervised Learning

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## Places where you will see unsupervised learning

- ▶ It can be used to segment the market based on customer preferences.

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- ▶ It can be used to segment the market based on customer preferences.
- ▶ A data science team reduces the number of dimensions in a large dataset to simplify modeling and reduce file size.

**REQUIREMENTS:** A predefined notion of similarity/dissimilarity.

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**Examples:**

Market Segmentation: Customers with similar preferences in the same groups. This would aid in targeted marketing.

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where  $|C_i|$  is the number of points in  $C_i$

Then,

$$\begin{aligned} WCV(C_i) &= \frac{1}{|C_i|} \sum_{a \in C_i} \sum_{b \in C_i} \|x_a - x_b\|_2^2 \\ &= 2 \sum_{a \in C_i} \|x_a - x_i\|_2^2 \end{aligned}$$

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This shows that K-Means gives the **local minima**.



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k\_bad\_1.png

k\_bad\_2.png

Examples where K-Means fails

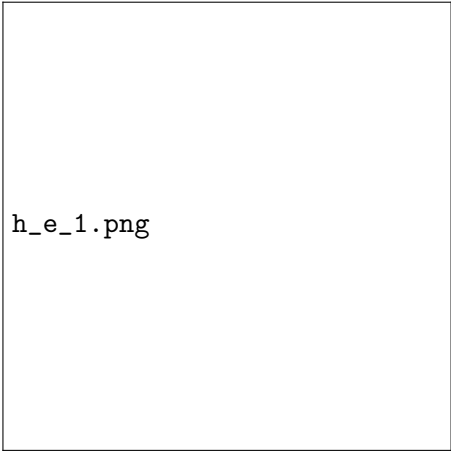
# Algorithm for Hierarchical Clustering

1. Start with all points in a single cluster

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- 2.1 Identify the 2 closest points



h\_e\_1.png

Example Dataset

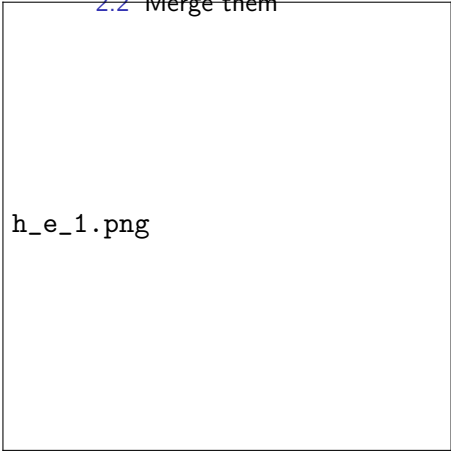
# Algorithm for Hierarchical Clustering

1. Start with all points in a single cluster

2.1 Identify the 2 closest points

2.2 Merge them

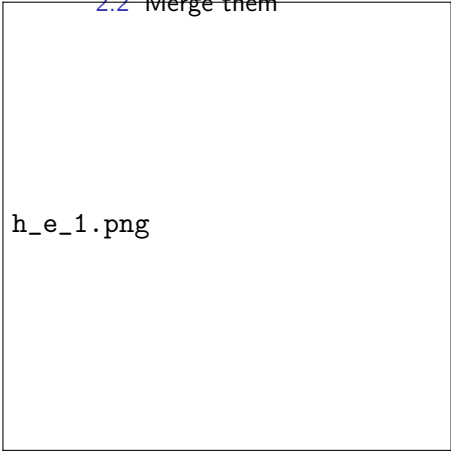
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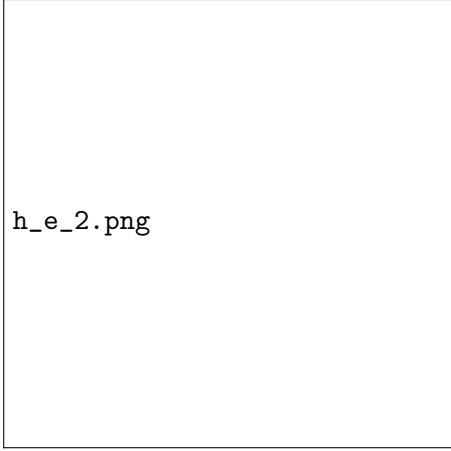
Example Dataset

# Algorithm for Hierarchical Clustering

1. Start with all points in a single cluster
2. Repeat until all points are in a single cluster
  - 2.1 Identify the 2 closest points
  - 2.2 Merge them



h\_e\_1.png



h\_e\_2.png

Example Dataset

Final Clustering

# Joining Clusters/Linkages

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## **Complete**

Max inter-cluster  
similarity



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## **Centroid**

Dissimilarity between  
cluster centroids

## More Code

[Google Colab Link](#)