Conventions, Accuracy Metrics, Classification, Regression

Nipun Batra July 19, 2025

IIT Gandhinagar

Demo

• Complete PoseNet Demo

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- Complete PoseNet Demo
- Blog post from Google

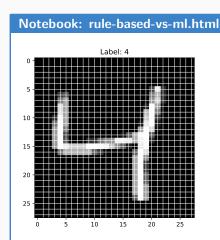
Demo

- Complete PoseNet Demo
- Blog post from Google
- Rock Paper Scissors

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Let us work on the digit recognition problem.



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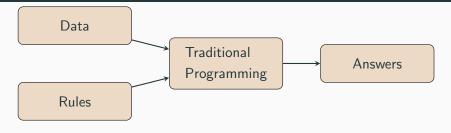
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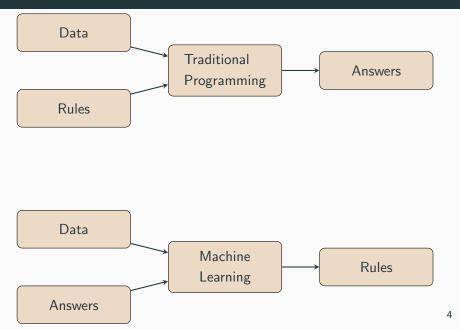
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- There can be some cases of 4 where the width of each stroke is different

Traditional Programming vs Machine Learning



Traditional Programming vs Machine Learning



"A computer program is said to learn from experience E with respect to some class of tasks T and performance measure P if its performance at tasks in T, as measured by P, improves with experience E." - Tom Mitchell

First ML Task: Grocery store tomato quality prediction

Problem statement: You want to predict the quality of a tomato given its visual features.

Imagine you have some past data on quality of tomatoes. What visual features do you think will be useful?

Size

Imagine you have some past data on quality of tomatoes. What visual features do you think will be useful?

Size

- Size
- Colour

- Size
- Colour

- Size
- Colour
- Texture

Sample Dataset

Here is our example dataset with tomato features:

Sample	Colour	Size	Texture	Condition
1	Orange	Small	Smooth	Good
2	Red	Small	Rough	Good
3	Orange	Medium	Smooth	Bad
4	Yellow	Large	Smooth	Bad

Useful Features

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Answer: Usually no! Sample numbers are typically arbitrary identifiers and not meaningful features. Let us remove it.

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Let us modify our data table for now.

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Training Set

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- 2. Output or Response Variable

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• Thus,
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Estimate condition for unseen tomatoes (#5, 6) based on data set.

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Orange	Medium	Smooth	Bad
Yellow	Large	Smooth	Bad
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Orange	Large	Rough	?

Testing Set

Testing set is similar to training set, but, does not contain labels for output variable.

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- 3. To Predict the condition for the Testing set

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- Q: Is predicting on test set enough to say our model generalises?
- A: Ideally, no!
- Ideally we want to predict "well" on all possible inputs. But, can we test that?
- No! Since, the test set is only a sample from all possible inputs.

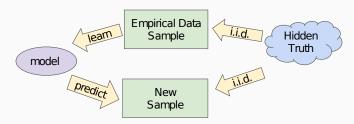


Image courtesy Google ML crash course

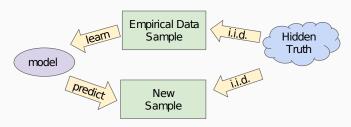


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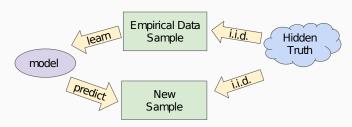


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More discussion later once we study bias and variance

Second ML Task: Predict energy consumption of campus

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# People	Temp (C)	Energy (kWh)
4000	30	30
4200	30	32
4200	35	40
3000	20	?
1000	45	?

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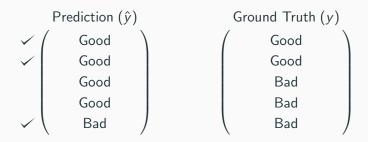
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 - Examples Predicting:
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 - How much rainfall will fall?

Metrics for Classification

Ground Truth: From the actual training set

Prediction: Made by the model

Accuracy



Accuracy

Prediction
$$(\hat{y})$$
 Ground Truth (y)
 \checkmark Good
Good
Good
Good
Good
Bad
Bad
Bad
Bad

Accuracy =
$$\frac{|\{i: y_i = \hat{y}_i\}|}{n}$$
$$= \frac{3}{5} = 0.6$$

- Set cardinality notation: $|\{i: y_i = \hat{y}_i\}|$
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Accuracy =
$$\frac{\sum_{i=1}^{n} \mathbf{1}[y_i = \hat{y}_i]}{n}$$

where
$$\mathbf{1}[\text{condition}] = \begin{cases} 1 & \text{if condition is true} \\ 0 & \text{if condition is false} \end{cases}$$

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 Both notations are mathematically equivalent and commonly used in ML literature

$$\begin{array}{c} \text{1 sample } \{ \begin{array}{c} \text{Bad} \\ \text{Good} \\ \text{Good} \\ \dots \\ \text{Good} \end{array} \right) \\ \text{Imbalanced Classes} \end{array}$$

$$\begin{array}{c} 1 \text{ sample } \{ \left(\begin{array}{c} \mathsf{Bad} \\ \mathsf{Good} \\ \mathsf{Good} \\ \cdots \\ \mathsf{Good} \end{array} \right) \end{array} \\ \\ \mathsf{Imbalanced \ Classes} \\ \end{array}$$

Cases for this:

Cancer Screening

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Imbalanced Classes

Cases for this:

- Cancer Screening
- Planet Detection

Accuracy Metrics: Precision

Precision =
$$\frac{|\{i : y_i = \hat{y}_i = \text{Good}\}|}{|\{i : \hat{y}_i = \text{Good}\}|} = \frac{2}{4} = 0.5$$

"the fraction of relevant instances among the retrieved instances", i.e. "out of the number of times we predict Good, how many times is the condition actually Good"

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Accuracy Metrics: Recall

Recall =
$$\frac{|\{i : y_i = \hat{y}_i = \text{Good}\}|}{|\{i : y_i = \text{Good}\}|} = \frac{2}{3} = 0.67$$

"the fraction of the total amount of relevant instances that were actually retrieved"

Given predictions of whether a tissue is cancerous or not (n = 100).

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$$\mbox{Accuracy} = \frac{98}{100} = 0.98 \qquad \qquad \mbox{Recall} = \frac{0}{1} = 0$$

$$\mbox{Precision} = \frac{0}{1} = 0$$

		Ground Truth	
		Yes	No
ted	Yes	0	1
redicted	No	1	98
Д			

		Ground	d Truth
		Yes	No
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Д			

		Ground Truth	
		Yes	No
ted	Yes	True Positive	False Positive
redicted	No	False Negative	True Negative
_			

		Ground Truth	
		Yes	No
redicted	Yes	True Positive	False Positive
redi	No	False Negative	True Negative
Д			

$$\mathsf{Precision} = \tfrac{\mathsf{TP}}{\mathsf{TP} + \mathsf{FP}}$$

		Ground	Ground Truth	
		Yes	No	
redicted	Yes	True Positive	False Positive	
redi	No	False Negative	True Negative	
Д				

$$\mathsf{Precision} = \tfrac{\mathsf{TP}}{\mathsf{TP} + \mathsf{FP}}$$

		Ground	Ground Truth	
		Yes	No	
cted	Yes	True Positive	False Positive	
redicted	No	False Negative	True Negative	
Д				

$$\mathsf{Recall} = \tfrac{\mathsf{TP}}{\mathsf{TP} + \mathsf{FN}}$$

		Ground	Ground Truth		
		Yes	No		
redicted	Yes	True Positive	False Positive		
redi	No	False Negative	True Negative		
Д					

$$\mathsf{Recall} = \tfrac{\mathsf{TP}}{\mathsf{TP} + \mathsf{FN}}$$

Accuracy Metrics: F-Score

		Ground Truth	
		Yes	No
cted	Yes	True Positive	False Positive
redicted	No	False Negative	True Negative
Д			

$$F-$$
 Score = $\frac{2 \times Precision \times Recall}{Precision + Recall}$

Accuracy Metrics: Matthew's Correlation Coefficient

		Ground Truth	
		Yes	No
cted	Yes	True Positive	False Positive
redicted	No	False Negative	True Negative
Д			

$$\frac{\text{TP} \times \text{TN} - \text{FP} \times \text{FN}}{\sqrt{(\text{TP} + \text{FP})(\text{TP} + \text{FN})(\text{TN} + \text{FP})(\text{TN} + \text{FN})}}$$

Accuracy Metrics: Example

For the data given below, calculate:

$$\begin{array}{cccc} & & G.T. \ \mbox{Positive} & G.T. \ \mbox{Negative} \\ \mbox{Pred Positive} & & 90 & 4 \\ \mbox{Pred Negative} & & 1 & 1 \\ \end{array}$$

Precision = ?

Recall = ?

F-Score = ?

Matthew's Coeff. =?

Accuracy Metrics: Answer

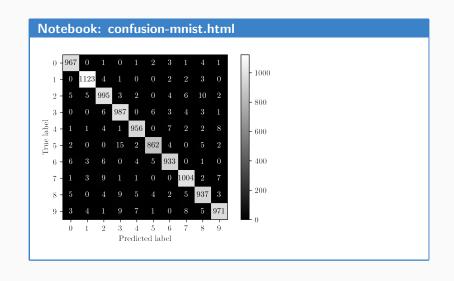
For the same data

G.T. Positive G.T. Negative Pred Positive
$$\begin{pmatrix} 90 & 4 \\ 1 & 1 \end{pmatrix}$$

Precision =
$$\frac{90}{94}$$

Recall = $\frac{90}{91}$
F-Score = 0.9524
Matthew's Coeff. = 0.14

Confusion Matrix for multi-class classification



Metrics for Regression MSE & MAE

Prediction
$$(\hat{y})$$
 Ground Truth (y)

$$\begin{pmatrix}
10 \\
20 \\
30 \\
40 \\
50
\end{pmatrix}$$
Ground Truth (y)

Mean Squared Error (MSE) =
$$\frac{\sum_{i=1}^{n} (\hat{y}_i - y_i)^2}{n}$$
 Root Mean Square Error (RMSE) = $\sqrt{\text{MSE}}$

Accuracy Metrics: MAE & ME

Prediction
$$(\hat{y})$$
 Ground Truth
$$\begin{pmatrix} 10 \\ 20 \\ 30 \\ 40 \\ 50 \end{pmatrix} \qquad \begin{pmatrix} 20 \\ 30 \\ 40 \\ 50 \\ 60 \end{pmatrix}$$

Mean Absolute Error (MAE) =
$$\frac{\sum_{i=1}^{n} |\hat{y}_i - y_i|}{n}$$
 Mean Error =
$$\frac{\sum_{i=1}^{n} (\hat{y}_i - y_i)}{n}$$

Accuracy Metrics: MAE & ME

Prediction
$$(\hat{y})$$
 Ground Truth

 $\begin{pmatrix}
10 \\
20 \\
30 \\
40 \\
50
\end{pmatrix}$
Ground Truth

 $\begin{pmatrix}
60 \\
60 \\
60
\end{pmatrix}$

Mean Absolute Error (MAE) =
$$\frac{\sum_{i=1}^{n} |\hat{y}_i - y_i|}{n}$$
Mean Error =
$$\frac{\sum_{i=1}^{n} (\hat{y}_i - y_i)}{n}$$

Is there any downside with using mean error?

Accuracy Metrics: MAE & ME

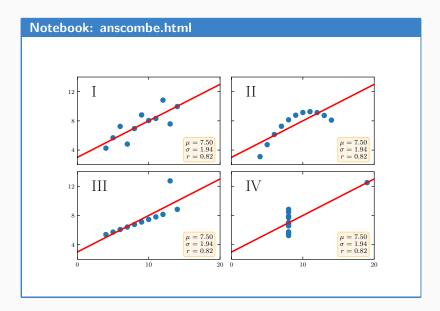
Prediction
$$(\hat{y})$$
 Ground Truth

 $\begin{pmatrix}
10 & & & \\
20 & & & \\
30 & & & \\
40 & & & \\
50 & & & & \\
60 & & & & \\
\end{pmatrix}$

Mean Absolute Error (MAE) =
$$\frac{\sum_{i=1}^{n} |\hat{y}_i - y_i|}{n}$$
Mean Error =
$$\frac{\sum_{i=1}^{n} (\hat{y}_i - y_i)}{n}$$

Is there any downside with using mean error? Errors can get cancelled out

The Importance of Plotting



Dummy Baselines

Notebook: dummy-baselines.html

The Importance of Plotting

Property Value		Across datasets
mean(X)	9	exact
mean(Y)	7.5	up to 3 decimal places
Linear regression line	y = 3.00 + 0.500x	up to 2 decimal places