Cross-Validation

Nipun Batra and teaching staff

IIT Gandhinagar

July 31, 2025

Outline

- 1. Introduction to Cross-Validation
- 2. Full Dataset Utilization
- 3. K-Fold Cross-Validation
- 4. Hyperparameter Optimization
- 5. Nested Cross-Validation
- 6. Cross-Validation Variants
- 7. Time Series Cross-Validation
- 8. Common Pitfalls and Best Practices
- 9. Summary and Key Takeaways

Limitations of single train-test split:

 Does not use the full dataset for training and does not test on the full dataset

Limitations of single train-test split:

 Does not use the full dataset for training and does not test on the full dataset

Limitations of single train-test split:

- Does not use the full dataset for training and does not test on the full dataset
- No way to optimize hyperparameters

Limitations of single train-test split:

- Does not use the full dataset for training and does not test on the full dataset
- No way to optimize hyperparameters

Limitations of single train-test split:

- Does not use the full dataset for training and does not test on the full dataset
- No way to optimize hyperparameters
- This simple train/test split has limitations we need to address

Pop Quiz: Train-Test Split Issues

Quick Quiz 1

What's the main problem with using only a single train-test split?

a) It's too computationally expensive

Answer: b) Different splits can give very different performance estimates!

Pop Quiz: Train-Test Split Issues

Quick Quiz 1

What's the main problem with using only a single train-test split?

- a) It's too computationally expensive
- b) Results depend on the particular split chosen

Answer: b) Different splits can give very different performance estimates!

Pop Quiz: Train-Test Split Issues

Quick Quiz 1

What's the main problem with using only a single train-test split?

- a) It's too computationally expensive
- b) Results depend on the particular split chosen
- c) It requires too much data

Answer: b) Different splits can give very different performance estimates!

· Does not utilize the full dataset for training

- Does not utilize the full dataset for training
- Cannot optimize hyperparameters systematically

- Does not utilize the full dataset for training
- Cannot optimize hyperparameters systematically

- Does not utilize the full dataset for training
- · Cannot optimize hyperparameters systematically
- · Results depend on the particular split chosen

- Does not utilize the full dataset for training
- · Cannot optimize hyperparameters systematically
- · Results depend on the particular split chosen
- May not get reliable performance estimates

Typically done via different random splits of the dataset

Typically done via different random splits of the dataset

Typically done via different random splits of the dataset

Challenge: How to ensure systematic evaluation?

Typically done via different random splits of the dataset

Challenge: How to ensure systematic evaluation?

Typically done via different random splits of the dataset

Challenge: How to ensure systematic evaluation?

May not use every data point for training or testing with random splits

Typically done via different random splits of the dataset

Challenge: How to ensure systematic evaluation?

May not use every data point for training or testing with random splits

Typically done via different random splits of the dataset

Challenge: How to ensure systematic evaluation?

May not use every data point for training or testing with random splits

May be computationally expensive

· Each data point is used for testing exactly once

- · Each data point is used for testing exactly once
- Each data point is used for training (k-1)/k of the time

- · Each data point is used for testing exactly once
- Each data point is used for training (k-1)/k of the time

- · Each data point is used for testing exactly once
- Each data point is used for training (k-1)/k of the time
- Provides more robust performance estimates

80 data points (4 out of 5 folds = $4/5 \times 100 = 80$)

Validation set helps select the best hyperparameters

Validation set helps select the best hyperparameters

Validation set helps select the best hyperparameters Test set remains untouched until final evaluation Validation set helps select the best hyperparameters Test set remains untouched until final evaluation Validation set helps select the best hyperparameters Test set remains untouched until final evaluation This prevents overfitting to the test set Each fold provides one validation score

Each fold provides one validation score

Each fold provides one validation score Process is systematic and exhaustive

Simple CV: Used for model evaluation only

- Simple CV: Used for model evaluation only
- Nested CV: Outer loop for model evaluation, inner loop for hyperparameter tuning

- Simple CV: Used for model evaluation only
- Nested CV: Outer loop for model evaluation, inner loop for hyperparameter tuning

- Simple CV: Used for model evaluation only
- Nested CV: Outer loop for model evaluation, inner loop for hyperparameter tuning
- Nested CV provides unbiased estimates when doing hyperparameter search

Final model is trained on entire training set

Final model is trained on entire training set

Final model is trained on entire training set Standard deviation gives confidence in results

Single fold results can be misleading due to data variance

- Single fold results can be misleading due to data variance
- Averaging provides more robust performance estimates

- Single fold results can be misleading due to data variance
- Averaging provides more robust performance estimates

- Single fold results can be misleading due to data variance
- Averaging provides more robust performance estimates
- Reduces impact of lucky/unlucky splits

- Single fold results can be misleading due to data variance
- Averaging provides more robust performance estimates
- Reduces impact of lucky/unlucky splits
- Standard deviation indicates reliability of the estimate

Special case where k = n (number of data points)

Special case where k = n (number of data points)

Maximum use of data for training

- Maximum use of data for training
- Deterministic (no randomness)

- Maximum use of data for training
- Deterministic (no randomness)

- Maximum use of data for training
- Deterministic (no randomness)

- Maximum use of data for training
- Deterministic (no randomness)

Disadvantages:

Computationally expensive

- Maximum use of data for training
- Deterministic (no randomness)

Disadvantages:

- · Computationally expensive
- · High variance in estimates

Maintains class distribution in each fold

Maintains class distribution in each fold

Maintains class distribution in each fold Important for imbalanced datasets Maintains class distribution in each fold Important for imbalanced datasets

Example: If dataset is 70% class A, 30% class B, each fold maintains this ratio

Example: If dataset is 70% class A, 30% class B, each fold maintains this ratio

Maintains class distribution in each fold Important for imbalanced datasets

Each fold has approximately same proportion of classes

Example: If dataset is 70% class A, 30% class B, each fold maintains this ratio

Reduces variance in performance estimates



Regular CV might create folds with very few (or zero) positive examples

- Regular CV might create folds with very few (or zero) positive examples
- This would give misleading performance estimates

- Regular CV might create folds with very few (or zero) positive examples
- This would give misleading performance estimates

- Regular CV might create folds with very few (or zero) positive examples
- This would give misleading performance estimates
- Stratified CV ensures each fold has \sim 10% positive examples

- Regular CV might create folds with very few (or zero) positive examples
- This would give misleading performance estimates
- Stratified CV ensures each fold has \sim 10% positive examples
- Results in more reliable and consistent evaluation

Regular CV assumes data points are independent

Regular CV assumes data points are independent

Regular CV assumes data points are independent Time series data has temporal dependencies **Forward Chaining:** Train on past, test on future Regular CV assumes data points are independent Time series data has temporal dependencies **Forward Chaining:** Train on past, test on future Regular CV assumes data points are independent Time series data has temporal dependencies Forward Chaining: Train on past, test on future Rolling Window: Fixed-size training window Regular CV assumes data points are independent Time series data has temporal dependencies Forward Chaining: Train on past, test on future Rolling Window: Fixed-size training window

Forward Chaining: Train on past, test on future

Rolling Window: Fixed-size training window

Expanding Window: Growing training set over time

Forward Chaining: Train on past, test on future

Rolling Window: Fixed-size training window

Expanding Window: Growing training set over time

Forward Chaining: Train on past, test on future

Rolling Window: Fixed-size training window

Expanding Window: Growing training set over time

Never use future data to predict past!

Incorrect Splitting: Not accounting for grouped data

Incorrect Splitting: Not accounting for grouped data

Incorrect Splitting: Not accounting for grouped data **Overfitting to CV:** Too much hyperparameter tuning

Incorrect Splitting: Not accounting for grouped data **Overfitting to CV:** Too much hyperparameter tuning

Incorrect Splitting: Not accounting for grouped dataOverfitting to CV: Too much hyperparameter tuningWrong Preprocessing: Scaling on entire dataset before

splitting

Incorrect Splitting: Not accounting for grouped dataOverfitting to CV: Too much hyperparameter tuningWrong Preprocessing: Scaling on entire dataset before

splitting

Incorrect Splitting: Not accounting for grouped data

Overfitting to CV: Too much hyperparameter tuning

Wrong Preprocessing: Scaling on entire dataset before splitting

Ignoring Class Imbalance: Not using stratified CV when needed

· This causes data leakage!

- This causes data leakage!
- Test fold statistics influence the training preprocessing

- This causes data leakage!
- Test fold statistics influence the training preprocessing

- This causes data leakage!
- Test fold statistics influence the training preprocessing
- Should compute statistics only on training folds

- This causes data leakage!
- Test fold statistics influence the training preprocessing
- Should compute statistics only on training folds
- Apply same transformation to corresponding test fold

- This causes data leakage!
- Test fold statistics influence the training preprocessing
- Should compute statistics only on training folds
- Apply same transformation to corresponding test fold
- This gives more realistic performance estimates

Robust Evaluation: Multiple train/test splits reduce variance

Robust Evaluation: Multiple train/test splits reduce variance

Robust Evaluation: Multiple train/test splits reduce variance

Hyperparameter Tuning: Systematic way to select best parameters

Robust Evaluation: Multiple train/test splits reduce variance

Hyperparameter Tuning: Systematic way to select best parameters

Robust Evaluation: Multiple train/test splits reduce variance

Hyperparameter Tuning: Systematic way to select best parameters

Model Comparison: Fair comparison between different algorithms

Robust Evaluation: Multiple train/test splits reduce variance

Hyperparameter Tuning: Systematic way to select best parameters

Model Comparison: Fair comparison between different algorithms

Robust Evaluation: Multiple train/test splits reduce variance

Hyperparameter Tuning: Systematic way to select best parameters

Model Comparison: Fair comparison between different algorithms

Confidence Estimates: Standard deviation indicates reliability

Stratified: Imbalanced classification problems

Stratified: Imbalanced classification problems

Stratified: Imbalanced classification problems

LOOCV: Small datasets, when computational cost is acceptable

Stratified: Imbalanced classification problems

LOOCV: Small datasets, when computational cost is acceptable

Stratified: Imbalanced classification problems

LOOCV: Small datasets, when computational cost is acceptable

Time Series CV: Temporal data with dependencies

Stratified: Imbalanced classification problems

LOOCV: Small datasets, when computational cost is acceptable

Time Series CV: Temporal data with dependencies

Stratified: Imbalanced classification problems

LOOCV: Small datasets, when computational cost is acceptable

Time Series CV: Temporal data with dependencies

Nested CV: When doing extensive hyperparameter

search

Always preprocess within each fold separately

Always preprocess within each fold separately

Always preprocess within each fold separately Use stratification for classification problems Always preprocess within each fold separately Use stratification for classification problems Always preprocess within each fold separately Use stratification for classification problems Report mean \pm standard deviation

Always preprocess within each fold separately Use stratification for classification problems Report mean \pm standard deviation

Always preprocess within each fold separately Use stratification for classification problems Report mean \pm standard deviation Don't overfit to cross-validation results

Always preprocess within each fold separately Use stratification for classification problems Report mean \pm standard deviation Don't overfit to cross-validation results

Always preprocess within each fold separately Use stratification for classification problems Report mean \pm standard deviation Don't overfit to cross-validation results Consider computational cost vs. benefit trade-off

Always preprocess within each fold separately Use stratification for classification problems Report mean \pm standard deviation Don't overfit to cross-validation results Consider computational cost vs. benefit trade-off

Always preprocess within each fold separately Use stratification for classification problems Report mean \pm standard deviation Don't overfit to cross-validation results Consider computational cost vs. benefit trade-off Use nested CV for unbiased hyperparameter search

How to combine various models?

- How to combine various models?
- Why combine multiple models?

- How to combine various models?
- Why combine multiple models?

- How to combine various models?
- Why combine multiple models?
- · How can we reduce bias?

- · How to combine various models?
- Why combine multiple models?
- · How can we reduce bias?
- How can we reduce variance?

- How to combine various models?
- Why combine multiple models?
- · How can we reduce bias?
- How can we reduce variance?
- Bootstrap aggregating (Bagging)

- How to combine various models?
- Why combine multiple models?
- · How can we reduce bias?
- How can we reduce variance?
- Bootstrap aggregating (Bagging)

- · How to combine various models?
- Why combine multiple models?
- · How can we reduce bias?
- How can we reduce variance?
- Bootstrap aggregating (Bagging)
- Boosting methods