Cross-Validation

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No way to optimize hyperparameters

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This simple train/test split has limitations we need to address

▶ Does not utilize the full dataset for training

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- Cannot optimize hyperparameters systematically
- Results depend on the particular split chosen
- ► May not get reliable performance estimates

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May be computationally expensive

► Each data point is used for testing exactly once

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- ▶ Provides more robust performance estimates

80 data points (4 out of 5 folds = $4/5 \times 100 = 80$)

Test set remains untouched until final evaluation

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Validation set helps select the best hyperparameters

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This prevents overfitting to the test set

Each fold provides one validation score

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Process is systematic and exhaustive

► Simple CV: Used for model evaluation only

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- Nested CV: Outer loop for model evaluation, inner loop for hyperparameter tuning
- Nested CV provides unbiased estimates when doing hyperparameter search

Final model is trained on entire training set

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Standard deviation gives confidence in results

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- Averaging provides more robust performance estimates
- ► Reduces impact of lucky/unlucky splits
- Standard deviation indicates reliability of the estimate

Each fold uses exactly one data point for testing

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Special case where k = n (number of data points) Each fold uses exactly one data point for testing

Advantages:

► Maximum use of data for training

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- Deterministic (no randomness)

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Disadvantages:

- Computationally expensive
- ► High variance in estimates

Maintains class distribution in each fold Important for imbalanced datasets Maintains class distribution in each fold Important for imbalanced datasets Maintains class distribution in each fold Important for imbalanced datasets

Each fold has approximately same proportion of classes

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Example: If dataset is 70% class A, 30% class B, each fold maintains this ratio

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Reduces variance in performance estimates

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- \triangleright Stratified CV ensures each fold has $\sim 10\%$ positive examples
- ▶ Results in more reliable and consistent evaluation

Time series data has temporal dependencies

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Forward Chaining: Train on past, test on future

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Rolling Window: Fixed-size training window

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Expanding Window: Growing training set over time

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Never use future data to predict past!

Data Leakage: Information from test set influences training Incorrect Splitting: Not accounting for grouped data

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Wrong Preprocessing: Scaling on entire dataset before splitting

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Ignoring Class Imbalance: Not using stratified CV when needed

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- Test fold statistics influence the training preprocessing
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- Apply same transformation to corresponding test fold
- ▶ This gives more realistic performance estimates

Robust Evaluation: Multiple train/test splits reduce variance

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Hyperparameter Tuning: Systematic way to select best parameters

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Model Comparison: Fair comparison between different algorithms

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Better Data Utilization: Every point used for both training and testing

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Hyperparameter Tuning: Systematic way to select best parameters

Model Comparison: Fair comparison between different algorithms

Confidence Estimates: Standard deviation indicates reliability

Stratified: Imbalanced classification problems

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Nested CV: When doing extensive hyperparameter search

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Use stratification for classification problems

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Don't overfit to cross-validation results

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Use nested CV for unbiased hyperparameter search

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- Boosting methods