# Conventions, Accuracy Metrics, Classification, Regression

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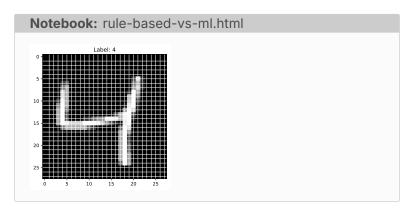
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#### **Outline**

- 1. Introduction to Machine Learning
- 2. Machine Learning Fundamentals
- 3. Classification vs Regression
- 4. Evaluation Metrics
- 5. Advanced Topics

#### Digit Recognition Problem

Let us work on the digit recognition problem.



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- There can be some cases of 4 where the width of each stroke is different

#### Pop Quiz: Rule-Based vs ML

#### **Quick Quiz 1**

Why is it difficult to write rules for digit recognition?

a) Digits are always the same

**Answer:** b) Handwriting variations make rule-based approaches extremely complex!

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- a) Digits are always the same
- b) Variations in handwriting, rotation, thickness make rules complex
- c) Rules are faster than ML

**Answer:** b) Handwriting variations make rule-based approaches extremely complex!

Size

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#### Should We Include Sample Numbers?

Answer: Usually no! Sample numbers are typically arbitrary identifiers and not meaningful features. Let us remove it.

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Let us modify our data table for now.

Colour	Size	Texture	Condition
Orange	Small	Smooth	Good
Red	Small	Rough	Good
Orange	Medium	Smooth	Bad
Yellow	Large	Smooth	Bad

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- 1. Features (Input Variables)
- 2. Output or Response Variable

#### **Dataset Notation**

We call this matrix as  $\mathcal{D}_{i}$ , containing:

1. Feature matrix  $(\mathbf{X} \in \mathbb{R}^{n \times d})$  containing data of n samples each of which is d dimensional.

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We call this matrix as  $\mathcal{D}_{i}$ , containing:

- 1. Feature matrix  $(\mathbf{X} \in \mathbb{R}^{n \times d})$  containing data of n samples each of which is d dimensional.
- 2. Output vector ( $\mathbf{y} \in \mathbb{R}^n$ ) containing output variable for n samples.

#### **Dataset Example**

```
Example (after encoding): \mathbf{x}_1 = \begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix} (Orange=1, Small=0, Smooth=1)
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 (Orange=1, Small=0, Smooth=1)

• Complete dataset:  $\mathcal{D} = \{(\mathbf{x}_i^\top, y_i)\}_{i=1}^n$ 

### Machine Learning Goal

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- 1. From Training Dataset
- 2. To Predict the condition for the Testing set

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#### A: Ideally, no!

- Ideally we want to predict "well" on all possible inputs. But, can we test that?
- No! Since, the test set is only a sample from all possible inputs.

#### Training vs Test Sets

Both the training set and the test set are samples drawn from the hidden true distribution (also sometimes called population)

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More discussion later once we study bias and variance

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# People	Temp (C)	Energy (kWh)
4000	30	30
4200	30	32
4200	35	40
3000	20	?
1000	45	?

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What makes a good feature for machine learning?

a) Sample ID numbers

**Answer:** b) Features should be meaningful and related to what you're predicting!

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What makes a good feature for machine learning?

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- b) Meaningful characteristics that relate to the output
- c) Random numbers

**Answer:** b) Features should be meaningful and related to what you're predicting!

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#### Regression

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  - How much rainfall will fall?

## Pop Quiz: Problem Types

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Predicting house prices is an example of:

a) Classification (discrete output)

**Answer:** b) Regression - house prices are continuous values!

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#### **Quick Quiz 3**

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- a) Classification (discrete output)
- b) Regression (continuous output)
- c) Neither

**Answer:** b) Regression - house prices are continuous values!

# **Accuracy Calculation**

Accuracy = 
$$\frac{|\{i : y_i = \hat{y}_i\}|}{n} = \frac{3}{5} = 0.6$$

• Set cardinality notation:  $|\{i: y_i = \hat{y}_i\}|$ 

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- Alternative: Indicator function notation

Accuracy = 
$$\frac{\sum_{i=1}^{n} 1[y_i = \hat{y}_i]}{n}$$

where 
$$\mathbf{1}[\text{condition}] = \begin{cases} 1 & \text{if condition is true} \\ 0 & \text{if condition is false} \end{cases}$$

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 Both notations are mathematically equivalent and commonly used in ML literature

#### When Precision/Recall Matter

#### Cases for this:

Cancer Screening

## When Precision/Recall Matter

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- Cancer Screening
- Planet Detection

#### **Precision Metric**

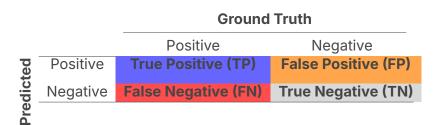
Precision = 
$$\frac{|\{i : y_i = \hat{y}_i = \text{Good}\}|}{|\{i : \hat{y}_i = \text{Good}\}|} = \frac{2}{4} = 0.5$$

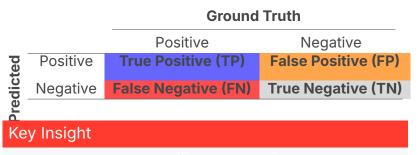
**Definition:** "The fraction of relevant instances among the retrieved instances"

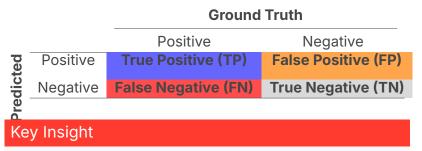
**In simple terms:** Out of all times we predict "Good", how many times is it actually "Good"?

# Accuracy vs Precision/Recall

$$\label{eq:accuracy} \begin{aligned} \text{Accuracy} &= \frac{98}{100} = 0.98 \\ \text{Recall} &= \frac{0}{1} = 0 \\ \text{Precision} &= \frac{0}{1} = 0 \end{aligned}$$







Each cell represents a different type of prediction outcome:

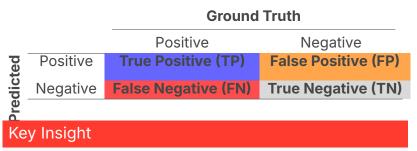
• TP: Correctly predicted positive



- TP: Correctly predicted positive
- FP: Incorrectly predicted positive

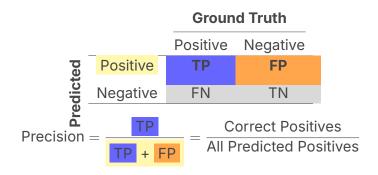


- TP: Correctly predicted positive
- FP: Incorrectly predicted positive
- FN: Missed a positive (dangerous!)

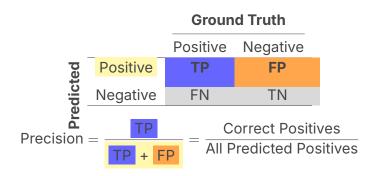


- TP: Correctly predicted positive
- FP: Incorrectly predicted positive
- FN: Missed a positive (dangerous!)
- TN : Correctly predicted negative

# Precision: "How accurate are my positive predictions?"



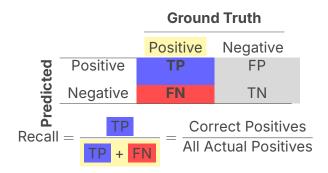
# Precision: "How accurate are my positive predictions?"



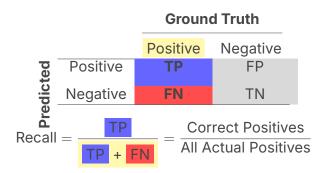
#### Focus: Look at the PREDICTED POSITIVE ROW

**Question:** When I predict "positive", how often am I right? **Answer:** Out of all my positive predictions (TP + FP), TP are correct.

#### Recall: "How many actual positives did I find?"



#### Recall: "How many actual positives did I find?"



#### Focus: Look at the ACTUAL POSITIVE COLUMN

Question: Of all things that ARE positive, how many did I

catch?

**Answer:** Out of all actual positives (TP + FN), I found TP

of them.

	Actu	<b>Actually Has Disease</b>	
	Yes	No	
Positive	90	10	
Negative	5	895	

		<b>Actually Has Disease</b>			
		Yes	No		
Fest Says	Positive	90	10		
	Negative	5	895		
Precision = $\frac{90}{90 + 10} = \frac{90}{100} = 0.90 \text{ (90\%)}$					
R	ecall = 90		$= \frac{90}{95} = 0.95 (95\%)$		
Accu	racy = 90	+ 89 1000	= 0.985 (98.5%)		

		Actually Has Disease	
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•	ision = 90	90 + 10	$=\frac{90}{100}=0.90 \text{ (90\%)}$

Accuracy = 
$$\frac{90 + 895}{1000} = 0.985 \text{ (98.5\%)}$$

		Actually Has Disease		
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• Prec	ision = 90	90 + 10 90 + 5	$= \frac{90}{95} = 0.95 (95\%)$	
Accu	racy = 90	+ <b>89</b> 1000	5 = 0.985 <b>(98.5%)</b>	

#### Mean Error Issues

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#### Pop Quiz: Metrics Choice

#### **Quick Quiz 4**

For cancer detection (1 positive case in 1000), which metric is most important?

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**Answer:** b) Recall - we cannot afford to miss cancer cases!

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Which metrics should you use for imbalanced datasets?

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**Answer:** c) Precision, recall, and F1-score give a more complete picture!

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#### · Visualization is crucial:

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#### · Use baselines:

Simple baseline models help validate your approach

# **Summary: Evaluation Metrics**

Task	Common Metrics	When to Use
Classification	Accuracy, Precision, Recall, F1	Balanced/Imbalanced data
	Confusion Matrix	Multi-class problems
Regression	MSE, RMSE, MAE	Continuous predictions
	Mean Error	Check for bias

#### Remember

Choose metrics based on your problem's characteristics and business requirements!