Seeing with Algorithms: Deep Dive into Object Detection

From Classification to Localization and Detection Metrics

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- Learn to evaluate object detectors thoroughly and effectively

Roadmap

- 1. Motivation and Applications
- 2. What is Object Detection?
- 3. Our 3-Class Detection Example
- 4. Detection Pipeline
- 5. Evaluation Metrics: The Foundation
- 6. Precision-Recall Curves and Average Precision
- 7. Mean Average Precision (mAP)
- 8. Advanced Topics

Task Definitions

Definition: Three Fundamental Computer Vision Tasks

Classification: What is present in the image?

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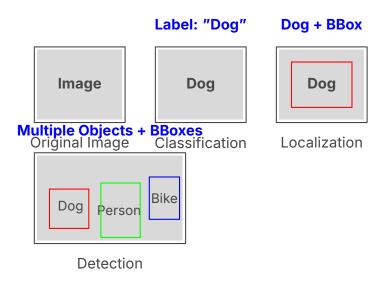
Task Definitions

Definition: Three Fundamental Computer Vision Tasks

- Classification: What is present in the image?
- Localization: Where is the object in the image?
- Detection = Classification + Localization (for multiple objects)

Each task builds upon the previous one, increasing in complexity and practical utility.

Visual Examples



Output Formats

| Task | Output Format | Example |
|----------------|-------------------------|--|
| Classification | label | "dog" |
| Localization | label, bbox | "dog", (30,3 |
| Detection | [label, conf, bbox] × N | ["dog", 0.95 ["person", 0 ["bike", 0.7 |

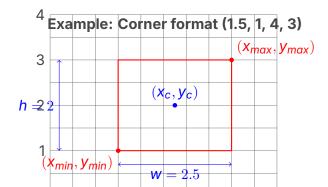
Key Points

Key Insight: Detection outputs include confidence scores, enabling ranking and threshold-based filtering!

What is a Bounding Box?

Definition: Bounding Box Formats

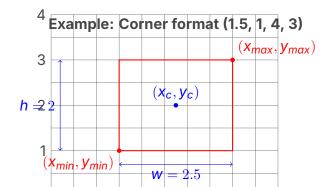
• Corner format: $(x_{min}, y_{min}, x_{max}, y_{max})$



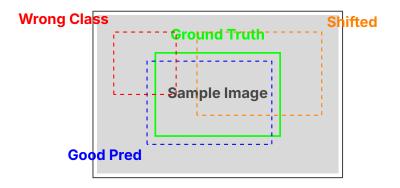
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- Corner format: $(x_{min}, y_{min}, x_{max}, y_{max})$
- **Center format**: (*x*_{center}, *y*_{center}, width, height)



Ground Truth vs Predictions



Key Points

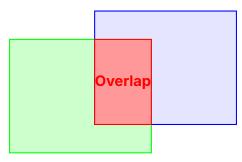
Matching Question: How do we decide which predictions correspond to which ground truth objects?

IoU Definition

Definition: Intersection over Union (IoU)

$$\mathsf{IoU} = \frac{\mathsf{Area\ of\ Overlap}}{\mathsf{Area\ of\ Union}} = \frac{|A \cap B|}{|A \cup B|}$$

Prediction

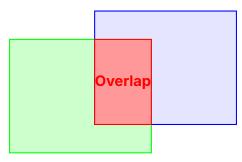


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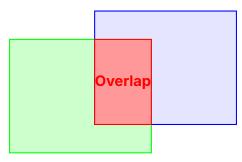


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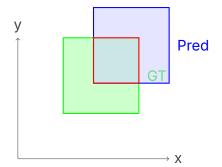
IoU Calculation Example

Example: Step-by-Step IoU Calculation

Ground Truth: (30, 30, 100, 100)**Prediction**: (50, 50, 120, 120)

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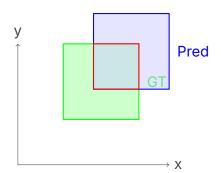
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Ground Truth: (30, 30, 100, 100) **Prediction**: (50, 50, 120, 120)



Step 1: Find intersection

 $X_{min} = \max(30, 50) = 50$ $Y_{min} = \max(30, 50) = 50$ $X_{max} = \min(100, 120) = 100$

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Step 2: Calculate areas Intersection: $50 \times 50 = 2500$

GT area: $70 \times 70 = 4900$

Pred area: $70 \times 70 = 4900$

Union:

4900 + 4900 - 2500 = 7300

Definition: Core Metrics

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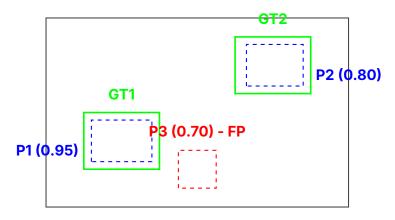
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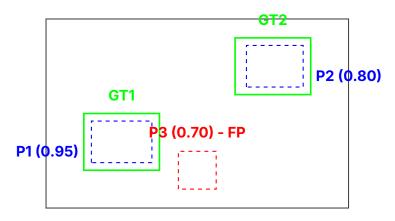
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- FN: False Negative (missed ground truth object)

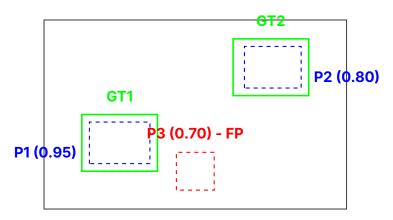


Scenario: 2 GT objects, 3 predictions



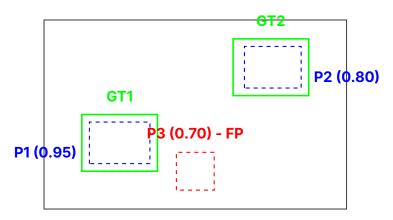
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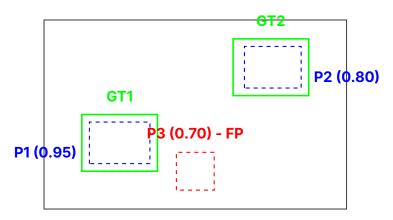
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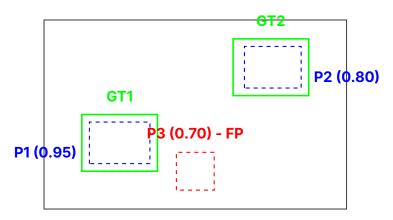
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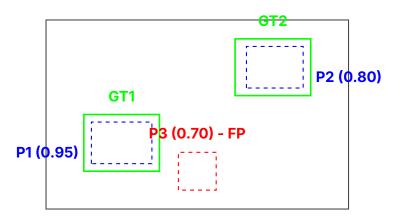
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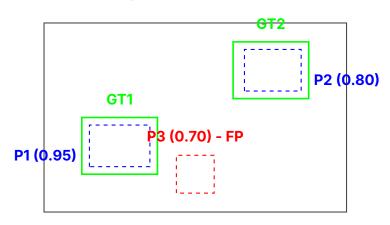
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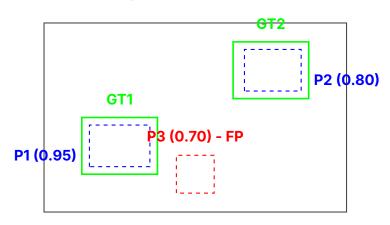
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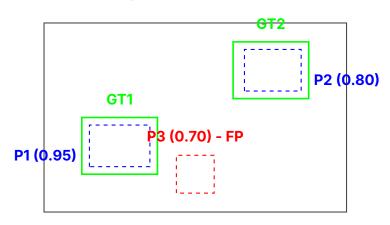
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Ranked Predictions Table

Example: Detection Results Sorted by Confidence

Given 5 predictions from our detector across the test set:

| Confidence | Class | Вох | TP/FP |
|------------|--------|-------------------|-------|
| 0.95 | Dog | (30,30,100,100) | TP |
| 0.88 | Bike | (150,120,200,180) | FP |
| 0.80 | Dog | (50,50,120,120) | TP |
| 0.70 | Person | (200,50,280,150) | TP |
| 0.40 | Cat | (100,100,150,150) | FP |

Key Points

By varying the confidence threshold, we can trade off

Precision-Recall Table

| Threshold | Predictions | TP | FP | Precision | Recall |
|-----------|-------------|----|----|-----------|--------|
| 0.95 | 1 | 1 | 0 | 1.000 | 0.333 |
| 0.88 | 2 | 1 | 1 | 0.500 | 0.333 |
| 0.80 | 3 | 2 | 1 | 0.667 | 0.667 |
| 0.70 | 4 | 3 | 1 | 0.750 | 1.000 |
| 0.40 | 5 | 3 | 2 | 0.600 | 1.000 |

Assumptions: 3 ground truth objects total, IoU threshold = 0.5

As threshold decreases → more predictions → recall increases

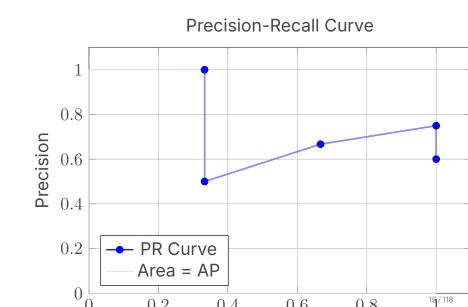
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Assumptions: 3 ground truth objects total, IoU threshold = 0.5

- As threshold decreases → more predictions → recall increases
- But also more false positives → precision can decrease

Precision-Recall Curve



Definition: Average Precision Calculation

$$AP = \int_0^1 P(R) dR$$

In practice: Numerical integration or 11-point interpolation

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 Sample at recall levels: 0, 0.1, 0.2, ..., 1.0

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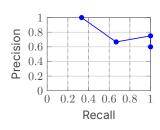
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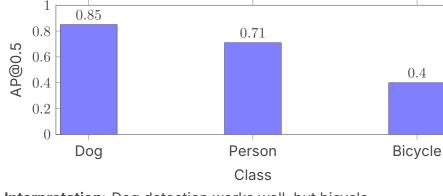
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Class-wise AP Example

| Class | AP@0.5 | Visual |
|---------|--------|-----------|
| Dog | 0.85 | Excellent |
| Person | 0.71 | Good |
| Bicycle | 0.40 | Poor |



17 / 118

Interpretation: Dog detection works well, but bicycle

Mean Average Precision (mAP)

Definition: mAP Calculation

$$\mathsf{mAP} = \frac{1}{\mathsf{C}} \sum_{c=1}^{\mathsf{C}} \mathsf{AP}_c$$

where C is the number of classes

Example: Our Example

$$\begin{split} \text{mAP} &= \frac{\text{AP}_{dog} + \text{AP}_{person} + \text{AP}_{bicycle}}{3} \\ &= \frac{0.85 + 0.71 + 0.40}{3} = \textbf{0.653} \end{split}$$

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Ignore class labels when matching predictions to ground truth.

Match based on IoU overlap alone.

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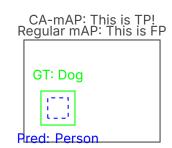
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Strict Evaluation: COCO Metrics

Definition: COCO Evaluation Protocol

• AP@50: IoU threshold = 0.5 (lenient)

| Metric | Value | Interpretation |
|--------------|-------|-------------------------------|
| mAP@50 | 0.71 | Good localization (loose) |
| mAP@75 | 0.45 | Moderate precise localization |
| mAP@[.5:.95] | 0.42 | Overall localization quality |

Key Points

Strict Evaluation: COCO Metrics

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AP@75: IoU threshold = 0.75 (strict)

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Strict Evaluation: COCO Metrics

Definition: COCO Evaluation Protocol

- AP@50: IoU threshold = 0.5 (lenient)
- AP@75: IoU threshold = 0.75 (strict)
- AP@[.5:.95]: Average over IoU thresholds 0.5, 0.55, 0.6, ..., 0.95

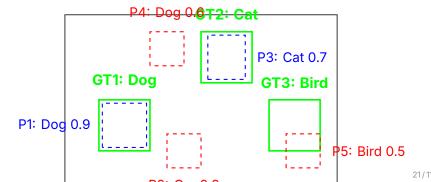
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Pop Quiz 1: Compute Precision & Recall

Quick Quiz Pop Quiz 0

Given the detection scenario below, compute precision and recall (IoU threshold = 0.5):



Example: Solution

Analysis (with IoU > 0.5 matching):

P1 (Dog 0.9) matches GT1 (Dog): TP

Precision =
$$\frac{2}{2+3} = 0.40$$
 Recall = $\frac{2}{2+1} = 0.67$

Example: Solution

Analysis (with IoU > 0.5 matching):

- P1 (Dog 0.9) matches GT1 (Dog): TP
- P2 (Car 0.8) no GT match: FP

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- P3 (Cat 0.7) matches GT2 (Cat): TP

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- GT3 (Bird) unmatched: FN

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Summary Table

| Concept | Meaning | Key Insight |
|-----------|-------------------------|---------------------------------------|
| IoU | Box overlap quality | Matching criterion (usua |
| Precision | Detection quality | $\frac{TP}{TP+FP}$ (fewer false alarm |
| Recall | Detection coverage | $\frac{TP}{TP+FN}$ (fewer missed ob |
| AP | Area under PR curve | Single-class performand |
| mAP | Average AP over classes | Multi-class detector per |
| CA-mAP | Class-agnostic mAP | Localization-only evalua |
| COCO | Multi-IoU evaluation | AP@[.5:.95] for precise |

Key Points

Golden Rule "Detection is not just about finding objects, but finding them right."

 Task hierarchy: Classification → Localization → Detection



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- Evaluation pipeline: IoU matching → TP/FP counting
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- Evaluation pipeline: IoU matching → TP/FP counting
 → PR curves → AP/mAP
- Trade-offs: Precision vs Recall, lenient vs strict IoU thresholds
- Practical metrics: COCO-style evaluation for real-world deployment

