

MIT SCHOOL OF ENGINEERING

Rajbaug, Loni-Kalbhor, Pune



MIT-ADT
UNIVERSITY
PUNE, INDIA
A step towards Smart Nation Education

Name - Umang Patel

Roll No. - 2193271

Subject - Information Security

Assignment - 1.

Chinese Remainder Theorem

Problem Statement: Implement a number theory such as Chinese remainder Theorem.

Objective: To study & implement Chinese Remainder Theorem.

Theory: Chinese Remainder Theorem is used to solve set of congruent equations with one variable but different modulus, which are relatively prime.

$$x = a_1 \bmod m_1$$

$$x = a_2 \bmod m_2$$

$$x = a_3 \bmod m_3$$

.....

$$x = a_k \bmod m_k$$

The Chinese Remainder Theorem States that the above equations have unique solution if the moduli are relatively prime. Below are the steps needed to follow to solve set of congruent equations using Chinese Remainder Theorem

Step 1: Find $M = m_1 \times m_2 \times m_3 \dots m_k$ where M is common modulus.

Step 2: Find $M_1 = M/m_1, m_2 = M/m_2$ & so on.

Step 3: Find multiplicative inverse for M_1, M_2 & so on

Step 4: Put the values in the below equation to solve for x .

$$x = (a_1 \times m_1 \times M_1^{-1} + a_2 \times M_2 \times M_2^{-1} + a_3 \times M_3 \times M_3^{-1}) \bmod M.$$

Example:

$$x \equiv 4 \pmod{5}$$

$$x \equiv 6 \pmod{8}$$

$$x \equiv 8 \pmod{9}$$

Step 1: $M = 5 * 8 * 9 = 360$

Step 2: $M_1 = M/m_1 = 360/5 = 72$

$$M_2 = M/m_2 = 360/8 = 45$$

$$M_3 = M/m_3 = 360/9 = 40$$

Step 3:- Find M_1 inverse, Solve for $\text{GCD}(m_1, M_1)$ using Extended Euclidean Algorithm

$$\text{GCD}(5, 72)$$

q	r ₁	r ₂	r	t ₁	t ₂	t
0	5	72	5	0	1	0
14	72	5	2	1	0	1
2	5	2	1	0	1	-2

The inverse value cannot be negative, so add modulus into it to make it positive.

$$M_1 \text{ inverse} = -2 + 5 = 3.$$



Find M_2 inverse, Solve for $\text{GCD}(m_2, m_2)$ using Extended Euclidean Algorithm,
 $\text{GCD}(8, 45)$

q	r ₁	r ₂	r	t ₁	t ₂	t
0	8	45	8	0	1	0
5	45	8	5	1	0	1
1	8	5	3	0	1	-1
1	5	3	2	1	-1	2
1	3	2	1	-1	2	-3

To find M_3 inverse, for $\text{GCD}(m_3, m_3)$

$\text{GCD}(9, 40)$

q	r ₁	r ₂	r	t ₁	t ₂	t
0	9	40	9	0	1	0
4	40	9	4	1	0	1
2	9	4	1	0	1	-2

Step 4: Put values in the below equation solve for x.

$$x = (a_1 \times M_1 \times M_1^{-1} + a_2 \times M_2 \times M_2^{-1} + a_3 \times M_3 \times M_3^{-1}) \mod M.$$

$$x = (4 \times 72 \times 3 + 6 \times 45 \times 5 + 8 \times 40 \times 7) \mod 360.$$

$$x = (864 + 1350 + 2240) \mod 360$$

$$x = 4454 \mod 360$$

$$x = 134.$$

Applications:

The Chinese Remainder Theorem has several applications in cryptography. One is to solve the quadratic congruence & the other is to represent very large number in terms of list of small integers.

Conclusion:

We have studied & implemented Chinese Remainder Theorem.

Rishabh
131012

```
main.py
1.4 - def findMinX(num, rem, k):
15     x = 1; # Initialize result
16
17     # As per the Chinese remainder
18     # theorem, this loop will
19     # always break.
20     while(True):
21
22         # Check if remainder of
23         # x % num[j] is rem[j]
24         # or not (for all j from
25         # 0 to k-1)
26         j = 0;
27         while(j < k):
28             if (x % num[j] != rem[j]):
29                 break;
30             j += 1;
31
32         # If all remainders
33         # matched, we found x
34         if (j == k):
35             return x;
36
37         # Else try next number
38         x += 1;
39
40     num = [3, 4, 5];
41     rem = [2, 3, 1];
42     k = len(num);
43     print("x is", findMinX(num, rem, k));
```

input

Program finished with exit code 0
Press ENTER to exit console.

Assignment - 2.

Extended Euclidian Algorithm.

Problem Statement : Implement Euclidean & Extended Euclidean algorithm to find out GCD & solve the inverse mod problem.

Objectives: To study Euclidean & Extended Euclidean algorithm.

Theory: The extended Euclidean algorithm is an extension to the Euclidean algorithm. Besides finding the greatest common divisor of integers $a \neq b$, as the Euclidean algorithm does, it also finds integers x by $ax + by = \text{gcd}(a, b)$ or $sa + tb = \text{gcd}(a, b)$.

The extended Euclidean algorithm is particularly useful when a & b are coprime, since x is the multiplicative inverse of a modulo b , & y is the multiplicative inverse of b modulo a .

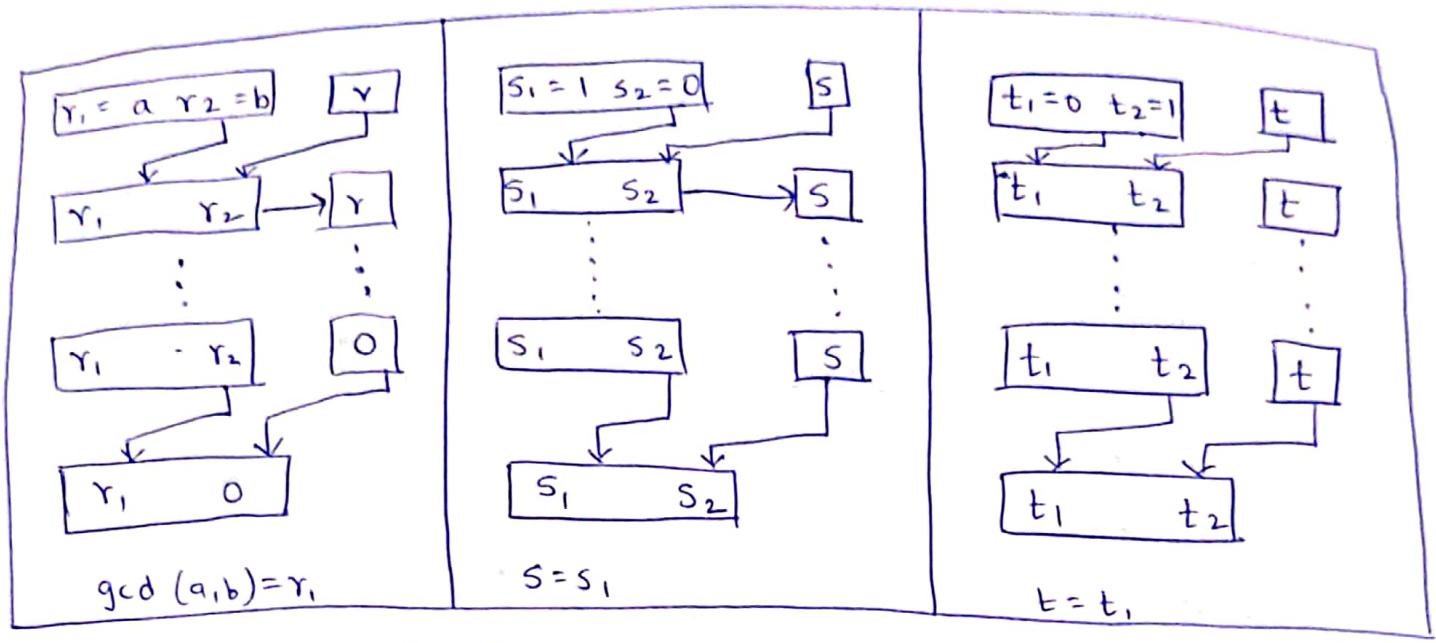


Fig:- Extended Euclid's Algorithm Process

Algorithm:- Extended the algorithm to compute the integer coefficients x & y such that $\text{gcd}(a, b) = ax + by$ Extended - Euclid (a, b) .

```

 $r_1 \leftarrow a; \quad r_2 \leftarrow b$ 
 $s_1 \leftarrow 1; \quad s_2 \leftarrow 0;$ 
 $t_1 \leftarrow 0; \quad t_2 \leftarrow 1;$ 

{ while ( $r_2 > 0$ )
     $q \leftarrow r_1 / r_2;$ 
     $r \leftarrow r_1 - q \times r_2;$ 
     $r_1 \leftarrow r_2; \quad r_2 \leftarrow r;$            (updating r's)
     $s \leftarrow s_1 - q \times s_2$ 
     $s_1 \leftarrow s_2; \quad s_2 \leftarrow s;$           (updating s's)

     $t \leftarrow t_1 - q \times t_2;$              (updating t's)
     $t_1 \leftarrow t_2; \quad t_2 \leftarrow t;$ 
}

 $\text{gcd}(a, b) \leftarrow r_1; \quad s \leftarrow s_1; \quad t \leftarrow t_1$ 

```

Example: $\text{GCD}(161, 28)$

q	r_1	r_2	r	s_1	s_2	s	t_1	t_2	t
5	161	28	21	1	0	1	0	1	-5
1	28	21	7	0	1	-1	1	-5	6
3	21	7	0	1	-1	4	-5	6	-23
	7	0		-1	4		6	-23	

Here GCD value we are getting as 7. Value of s is -1 & value of t is 6. If we put these values into equation,

$$ax + by = \text{gcd}(a, b)$$

$$161 * (-1) + 28 * (6) = 7.$$

This satisfies the equation for Extended Euclidean Algorithm.

Conclusion:-

We have studied & implemented the Extended Euclidean algorithm.

~~Rajbaug
13/10/17~~

main.py

```
1 # Python program to demonstrate working of extended
2 # Euclidean Algorithm
3
4 # function for extended Euclidean Algorithm
5 # Name- Umang Patel
6
7 def gcdExtended(a, b):
8     # Base Case
9     if a == 0:
10        return b, 0, 1
11
12
13 gcd, x1, y1 = gcdExtended(b % a, a)
14
15 # Update x and y using results of recursive
16 # call
17 x = y1 - (b//a) * x1
18 y = x1
19
20
21 return gcd, x, y
22
23
24 # Driver code
25 a, b = 35, 15
26 g, x, y = gcdExtended(a, b)
27 print("gcd(35, 15) = ", g)
28
```

Language Python 3

Input

```
gcd( 35 , 15 ) = 5
```

Program finished with exit code 0
Press ENTER to exit console.



Assignment - 3

RSA Algorithm.

Problem Statement: Implement RSA public key cryptosystem
for key generation & cipher verification.

Objectives: To understand,

- 1) Public Key algorithm.
- 2) RSA algorithm.
- 3) Concept of Public Key & Private Key.

Theory:-

• Public Key Algorithm:

Asymmetric algorithms rely on one key for encryption & a different but related key for decryption.

These algorithms have the following characteristics.

- It is computationally infeasible to determine the decryption key given only knowledge of the cryptographic algorithm and the encryption key.

In addition, some algorithms, such as RSA, also exhibit the following characteristic:

- Either of the two related keys can be used for encryption, with other used for decryption.

A public key encryption scheme has six ingredients:-

- Plaintext : This is readable message or data that is fed into the algorithm as input.
- Encryption algorithm : The encryption algorithm performs various transformations on the plaintext.
- Public & Private Key : This is a pair of keys that have been selected so that if one is used for encryption, the other is used for decryption.
- Cipher Text : - This is the scrambled message produced as output.
~~It depends on the plaintext & the key. For a given message, two different keys will produce two different cipher texts.~~
- Decryption algorithm : This algorithm accepts the ciphertext & the matching key & produces the original plaintext.

The RSA Algorithm :-

The scheme developed by Rivest, Shamir & Aldeman makes use of an expression with exponentials. ~~Plaintext is encrypted in blocks, with each block having a binary values less than some number n . That is the block size must be less than or equal to $\log_2(n)$; in practice the block size is 1 bits,~~ Encryption & decryption are of the following form,

$$C = M^e \text{ mod } n$$

$$M = C^d \text{ mod } n.$$



Both sender & receiver must know the value of n . The sender known the value of e , & only the receiver knows the value of d .

Thus, this is a public key encryption algorithm. with a public key of $PV = \{e, n\}$ & a private key of $PR = \{d, n\}$, for this to be satisfactory, the following requirements must meet:

- 1) It is possible to find values of e, d, n .
- 2) It is relatively easy to calculate $m^e \bmod n$ & $c^d \bmod n$ for all values of $m < n$.
- 3) It is feasible to determine d given $e & n$.

Key Generation.

Select p, q

$p \neq q$ both prime, $p \neq q$

Calculate $n = p * q$

Calculate $\phi(n) = (p-1)(q-1)$

Select integer e

$\gcd(\phi(n), e) = 1; 1 < e < \phi(n)$

Calculate d

$d = e^{-1} \pmod{\phi(n)}$

Public key

$PV = \{e, n\}$

Private key

$PR = \{d, n\}$

Encryption

Plaintext

$M < n$

Ciphertext

$C = m^e \pmod{n}$

Decryption

Ciphertext

C

Plaintext

$M = C^d \pmod{n}$

fig: The RSA Algorithm.

Example :

$$P=7, Q=13, M=10.$$

$$\text{Step 1: } n = 3 * 11 = 33$$

$$\text{Step 2: } \phi(n) = 2 * 10 = 20$$

Step 3: Select e , such that $\gcd(\phi(n), e) = 1$, $\gcd(20, 3) = 1$, so we can select $e=3$.

Step 4: To calculate d , solve for $\gcd(\phi(n), e)$ using extended Euclid's algorithm & pick up the value of t .

q	r ₁	r ₂	r	t ₁	t ₂	t
6	20	3	2	0	1	-6
1	3	2	1	1	-6	7

$$d=7.$$

Step 5 : for Encryption,

$$\begin{aligned} C &= M^e \bmod n \\ &= 2^3 \bmod 33 \\ &= 8 \bmod 33 \\ &= 8. \end{aligned}$$

Step 6 : for Decryption,

$$\begin{aligned} M &= C^d \bmod n \\ &= 8^7 \bmod 33 \\ &= ((8^2 \bmod 33) (8^2 \bmod 33) (8^2 \bmod 33) (8^1 \bmod 33)) \bmod 33 \\ &= (31 * 31 * 8 * 31) \bmod 33 \\ &= (961 \bmod 33) (248 \bmod 33) \bmod 33 \\ &= 68 \bmod 33 \\ &= 2. \end{aligned}$$

Advantage:

- 1) Easy to implement.

Disadvantage:

- 1) Anyone can announce the public key.

Algorithm:

- 1) Start
- 2) Input two prime numbers p & q .
- 3) Calculate $n = pq$.
- 4) Calculate $\phi(n) = (p-1)(q-1)$.
- 5) Input value of e .
- 6) Determine d .
- 7) Determine PV & PR.
- 8) Take input plaintext.
- 9) Encrypt the plaintext & Show output.
- 10) Stop.

Conclusion:

We have studied & implemented the public key algorithm that is RSA algorithm.

~~Kulhaya
BTM~~

```
1 import math
2 def gcd(a, b):
3     temp = 0
4     while(1):
5         temp = a % b
6         if (temp == 0):
7             return b
8         a = b
9         b = temp
10    p = 3
11    q = 7
12    n = p*q
13    e = 2
14    phi = (p-1)*(q-1)
15    while (e < phi):
16        if(gcd(e, phi) == 1):
17            break
18        else:
19            e = e+1
20    k = 2
21    d = (1 + (k*phi))/e
22    msg = 12.0
23    print("Message data = ", msg)
24    c = pow(msg, e)
25    c = math.fmod(c, n)
26    print("Encrypted data = ", c)
27    m = pow(c, d)
28    m = math.fmod(m, n)
29    print("Original Message Sent = ", m)
```

Input

```
message data = 12.0
Encrypted data = 3.0
Original Message Sent = 12.0
```

Program finished with exit code 0

Name - Umang Patel
Roll No. - 2193271

Subject - I.S

Class - LY IS - 3.

Assignment - 04.

Problem Statement :- Implement Diffie Hellman Key exchange algorithm for secret key generation & distribution of public key.

Objective :-

- 1) To learn the basics of key management.
- 2) To study & implement Diffie Hellman Key exchange algorithm.

Theory :-

The purpose of the algorithm is to enable two users to securely exchange a key that can then be used for subsequent encryption of messages. The algorithm itself is limited to the exchange of secret or secret values.



Algorithm:-

- There are two publicly known numbers a prime no. q & an integer a that is a primitive root of q .
- Suppose the users A & B wish to exchange a key. User A selects a random integer $x_A < q$ & computes $y_A = a^{x_A} \text{ mod } q$. Similarly User B independently selects a random integer $x_B < q$ & computes $y_B = a^{x_B} \text{ mod } q$.
Each side keeps the value x private & makes the value y available publicly to the other side.

User A computes the key K as $K = y_B^{x_A} \text{ mod } q$.

User B computes the key K as $K = y_A^{x_B} \text{ mod } q$.

then two calculation produce identical results.

Eg:- 1) Users Alice & Bob who wish to swap keys.

2) Agree on prime $q = 353$ & $a=3$.

3) Select random secret keys:

- A chooses $x_A = 97$, B choose $x_B = 233$.

4) Compute public keys.

$$- y_A = 3^{97} \text{ mod } 353 = 40 \text{ (Alice)}$$

~~$- y_B = 3^{233} \text{ mod } 353 = 248 \text{ (Bob)}$~~

5) Compute shared session key as

$$K_{AB} = y_B^{x_A} \text{ mod } 353 = 248^{97} = 160 \text{ (Alice)}$$

$$K_{AB} = y_A^{x_B} \text{ mod } 353 = 40^{233} = 160 \text{ (Bob)}$$



Global Public Elements

q

Prime number

a

$a < q$ & a primitive root
of q .

User A key Generation

Select private x_A

$x_A < q$

Calculate public y_A

$$y_A = a^{x_A} \bmod q$$

Calculation of Select key by User A

$$k = (y_B)^{x_A} \bmod q$$

Calculation of Secret key by User B.

$$k = (y_A)^{x_B} \bmod q$$

Figure :- Diffie Hellman B Process.

Conclusion:-

We have studied & implemented Diffie Hellman key exchange algorithm

~~Pathways~~

Name: Umang Patel

Roll no: 2193271

Is lab – Assignment 04 - Deffie Hellman Algorithm

Code:

```
from random import randint

if __name__ == '__main__':

    P = 23
    G = 9

    print('The Value of P is :%d'%(P))
    print('The Value of G is :%d'%(G))

    a = 4
    print('The Private Key a for Alice is :%d'%(a))

    x = int(pow(G,a,P))

    b = 3
    print('The Private Key b for Bob is :%d'%(b))

    y = int(pow(G,b,P))

    ka = int(pow(y,a,P))

    kb = int(pow(x,b,P))

    print('Secret key for the Alice is : %d'%(ka))
    print('Secret Key for the Bob is : %d'%(kb))
```



Name - Umang Patel.

Subject - Information Security

Roll No. - 2193271

Class - LY-IS-3

Assignment - 06

Aim :-

Install and Configure Kali Linux for pentesting.

Objective :-

- 1) To learn the basics of Kali-Linux.
- 2) To Configure Kali Linux for penetration testing.

Theory :-

Kali Linux is an open source, Debian-based Linux distribution aimed at advanced Penetration Testing & Security Auditing. It does this by providing common task tools, configuration & automations which allow the user to focus on the task that needs to be completed, not the surrounding activity. It is geared towards various information security tasks such as Penetration testing, Security Research, Computer forensics & Reverse Engineering.

Kali Linux is a multi-platform solution, accessible & freely available to information Security professionals & hobbyists.

Kali Linux Installation.

Different ways of installing Kali Linux

- 1) Bootable device.
- 2) Hard disk installation.
- 3) Dual Boot.
- 4) Virtual - Box.

Kali Linux using Bootable USB.

~~Step 1: Download Kali Linux ISO. Download the ISO image file of Kali Linux from its official website. www.kali.org.~~

~~Step 2: You should download any bootable Image file processing tool, which allows you to create a bootable USB drive.~~

~~Step 3: Play your USB drive into your Windows PC & remember the drive name associated with it ("R:X")~~

~~Step 4: launch Rufus & choose the Kali Linux ISO file. that you want to copy on the USB drive. Match the name of the device selected, which corresponds to the name of the USB ~~drive~~ device you inserted.~~



Step 5: Click the Start button to overwrite the contents of USB drive.

Step 6:- Once the Status bar is completed 100%, close & safely rename USB drive from the PC. You can now use your USB drive to boot Kali Linux.

Step 7:- Insert your bootable USB drive to your PC & start your PC. Press "Esc" on the first prompt to enter into the Startup Menu.

Step 8:- Press F9 to enter into Boot Device option. It will redirect you to the Boot Manager. This option may vary from device to device.

Step 9:- Select USB hard drive to boot from your bootable USB drive. It will redirect you to the Kali Linux Live Boot Menu.

Step 10:- Select Live System & press enter to boot Kali Linux.

You can now use Kali Linux on the same hardware without disturbing your host operating system.

Conclusion :- We have installed Kali Linux on Windows using bootable USB device.

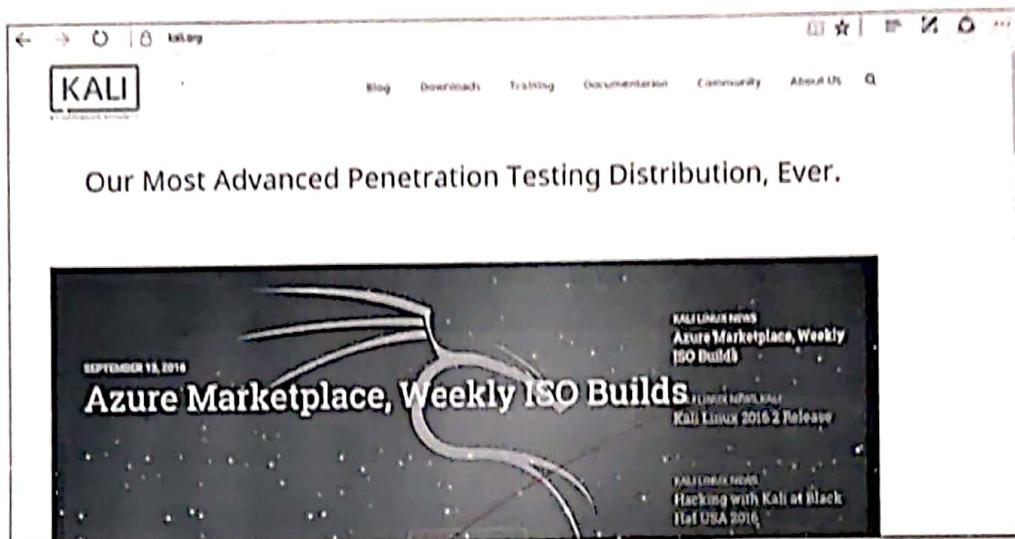
Name: Umang Patel

Roll no: 2193271

Is lab – Assignment 05 Kali Linux

Implementation:-

official webpage of kali Linux is <https://www.kali.org>. Backtrack was the old version of Kali Linux distribution. The latest release is Kali 2016.1 and it is updated very often.



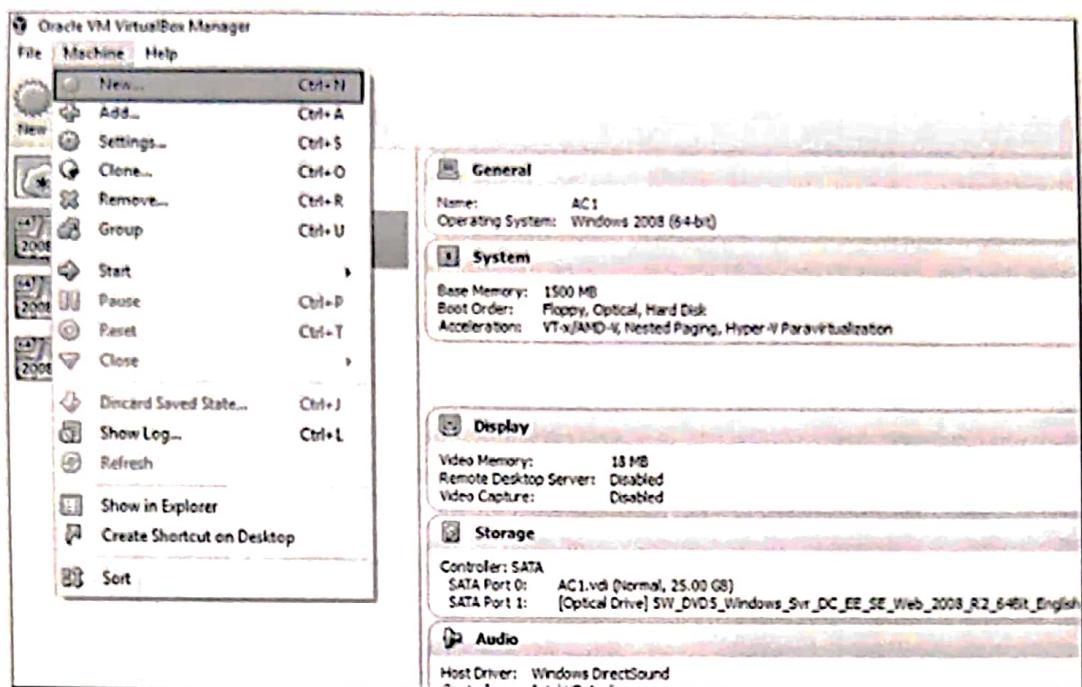
Install Kali Linux

Step 1) Download the Kali Linux package from its official website: <https://www.kali.org/downloads/>

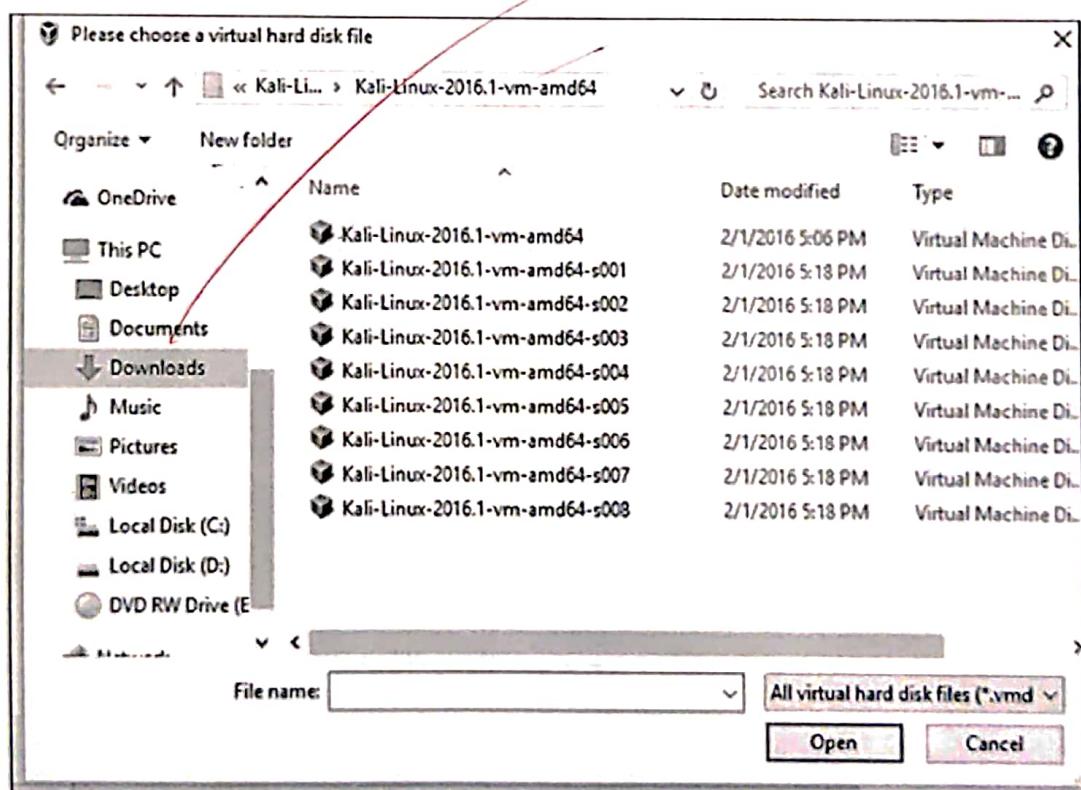
A screenshot of the offensive-security.com website. The header includes the "OFFENSIVE SECURITY" logo and links for "Blog", "Courses", "Certifications", and "Online Labs". Below the header, there are two sections: "Prebuilt Kali Linux VMware Images" and "Prebuilt Kali Linux VirtualBox Images". A red arrow points from the "Downloads" link on the Kali Linux website screenshot above to the "Prebuilt Kali Linux VMware Images" section here. A table below lists two download options:

Image Name	Torrent	Size	Version	SHA1Sum
Kali Linux 64 bit VM	Torrent	2.0G	2016.1	2b49bf1e77c11ecb5618249ca69a46f23a6f5d2d
Kali Linux 32 bit VM PAE	Torrent	2.0G	2016.1	e71867a8bbf7ad55fa437eb7c93fd69e450f6759

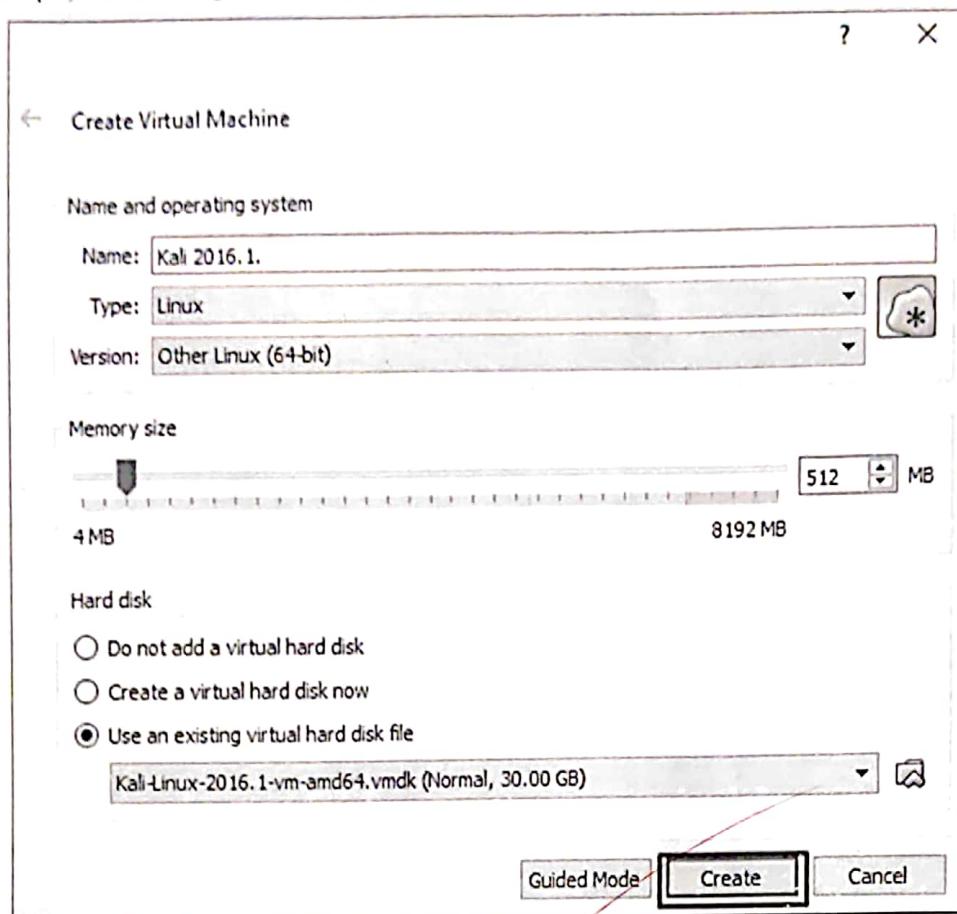
Step 2) Click VirtualBox → New as shown in the following screenshot.



Step 3) Choose the right virtual hard disk file and click Open.



Step 4) The following screenshot pops up. Click the Create button.



Step 5) Start Kali OS. The default username is **root** and the password is **toor**.

