#### **Bias Variance**

Prepared By: Dr.Mydhili K Nair, Professor, ISE Dept, RIT

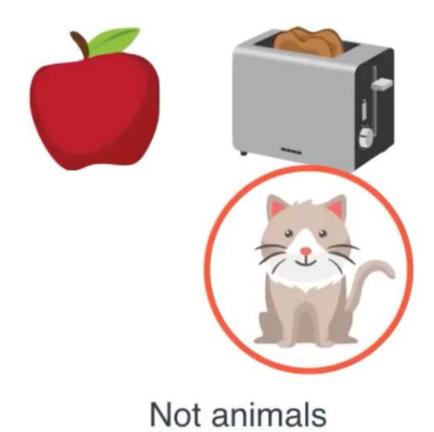
**For: Machine Learning Elective Class** 

**Target Audience: Sem 6 Students** 

**Term: Feb to June 2019** 

#### Bias

#### Our Classification Model is too simple









**Animals** 

#### Our Classification Model is too specific

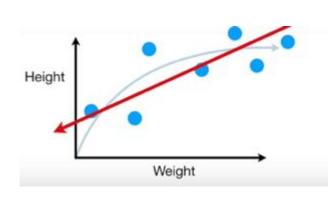


Anything but dogs that are wagging their tail

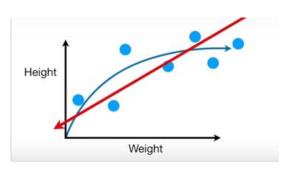


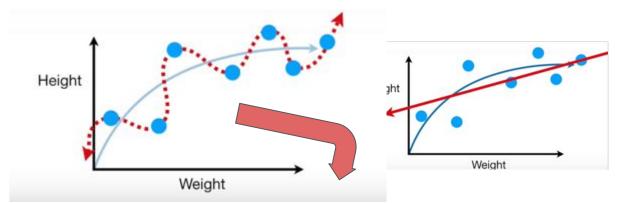
Too specific

Dogs that are wagging their tail



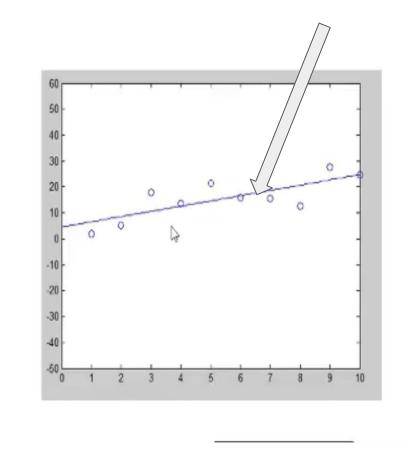
Linear Model: How much ever you vary the "prediction regression line" it will not fit the curve and there will always be a bias between actual value and predicted value.





Bias error is completely eliminated. This non-linear model fits the data points perfectly. Zero Bias.

### Model 1: $y = b_0 + b_1 x$

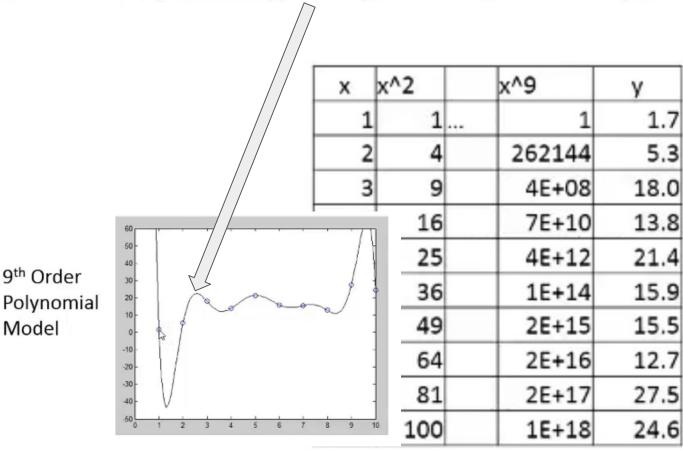


Linear

Model

| Х  | У    |
|----|------|
| 1  | 1.7  |
| 2  | 5.3  |
| 3  | 18.0 |
| 4  | 13.8 |
| 5  | 21.4 |
| 6  | 15.9 |
| 7  | 15.5 |
| 8  | 12.7 |
| 9  | 27.5 |
| 10 | 24.6 |

Model 2:  $y = b_0 + b_1 x + b_2 x^2 + b_3 x^3 + \dots + b_9 x^9$ 

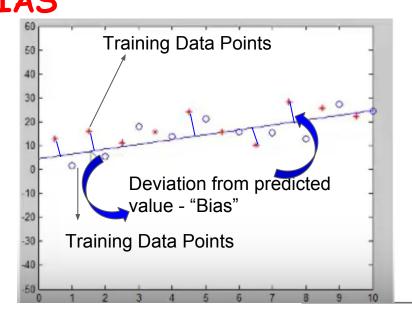


9<sup>th</sup> Order

Model

#### Model 1: $y = b_0 + b_1 x$

Our Classification Model is too simple - HIGH BIAS



| Х  | У    |
|----|------|
| 1  | 1.7  |
| 2  | 5.3  |
| 3  | 18.0 |
| 4  | 13.8 |
| 5  | 21.4 |
| 6  | 15.9 |
| 7  | 15.5 |
| 8  | 12.7 |
| 9  | 27.5 |
| 10 | 24.6 |

### Model 2: $y = b_0 + b_1 x + b_2 x^2 + b_3 x^3 + \dots + b_9 x^9$

| 60     |                             |
|--------|-----------------------------|
| 50 -   | / 1                         |
| 30 -   |                             |
| 20 -   | ( ) o o o                   |
| 10 - * | Bias is very high for these |
| 0- 4   | two data points, because    |
| -10 -  | the model has over-fitted   |
| -20 -  | to the training set. This   |
| -30    | means the model will have   |
| -40 V  | high "variance" among       |
| -50 1  | 2 test data.5 6 7 8 9 10    |
|        |                             |

| X  | x^2 | x^9    | У    |
|----|-----|--------|------|
| 1  | 1   | <br>1  | 1.7  |
| 2  | 4   | 262144 | 5.3  |
| 3  | 9   | 4E+08  | 18.0 |
| 4  | 16  | 7E+10  | 13.8 |
| 5  | 25  | 4E+12  | 21.4 |
| 6  | 36  | 1E+14  | 15.9 |
| 7  | 49  | 2E+15  | 15.5 |
| 8  | 64  | 2E+16  | 12.7 |
| 9  | 81  | 2E+17  | 27.5 |
| 10 | 100 | 1E+18  | 24.6 |

Our Classification Model is too specific -HIGH VARIANCE

## Error due to bias (underfitting)







Too simple



**Animals** 



## Error due to variance (overfitting)



Anything but dogs that are wagging their tail





Too specific



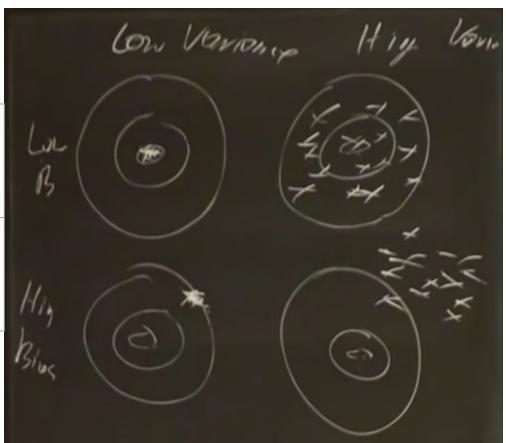
Dogs that are wagging their tail



**Low Variance** 

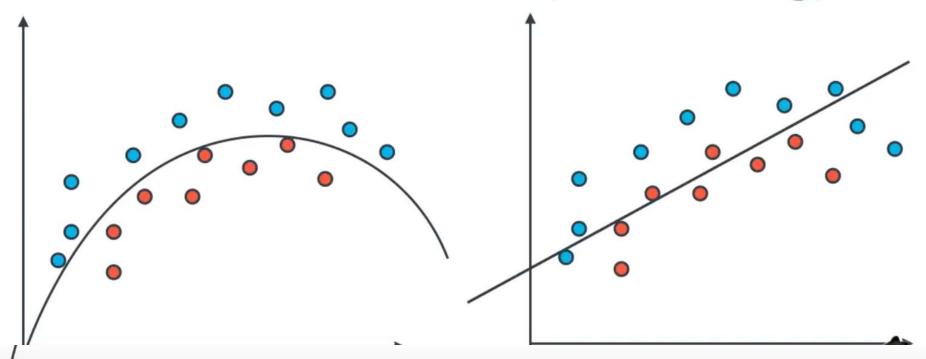
**High Variance** 



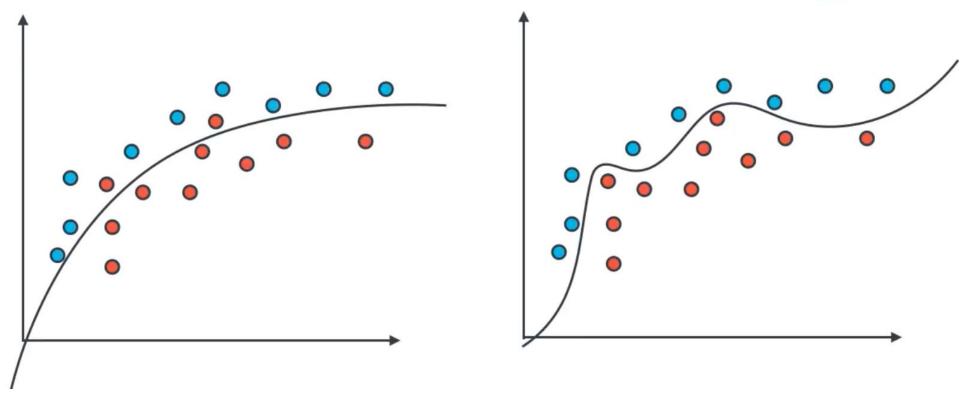


#### Bias - Variance Tradeoff

## Error due to bias (underfitting)



## Error due to variance (overfitting)



#### Tradeoff

High bias (Underfitting)

Not animals



Animals



Bad on Training set
Bad on Testing set

Just Right

Not dogs



Dogs



Good on Training set
Good on Testing set

High variance (Overfitting)

Not dogs who wag their tail



Dogs who wag their tail



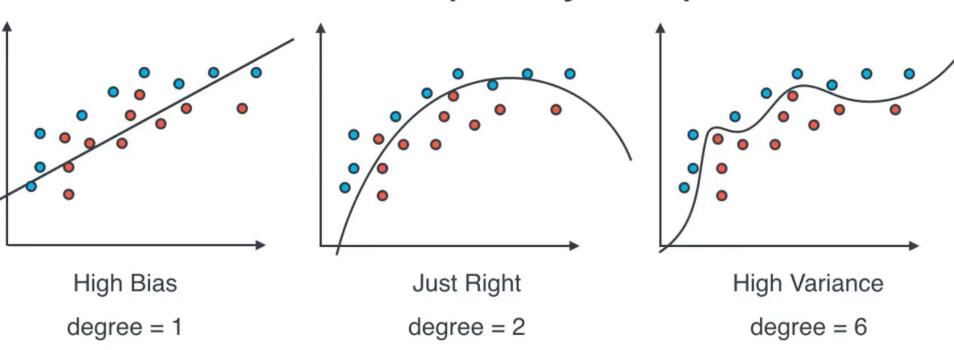


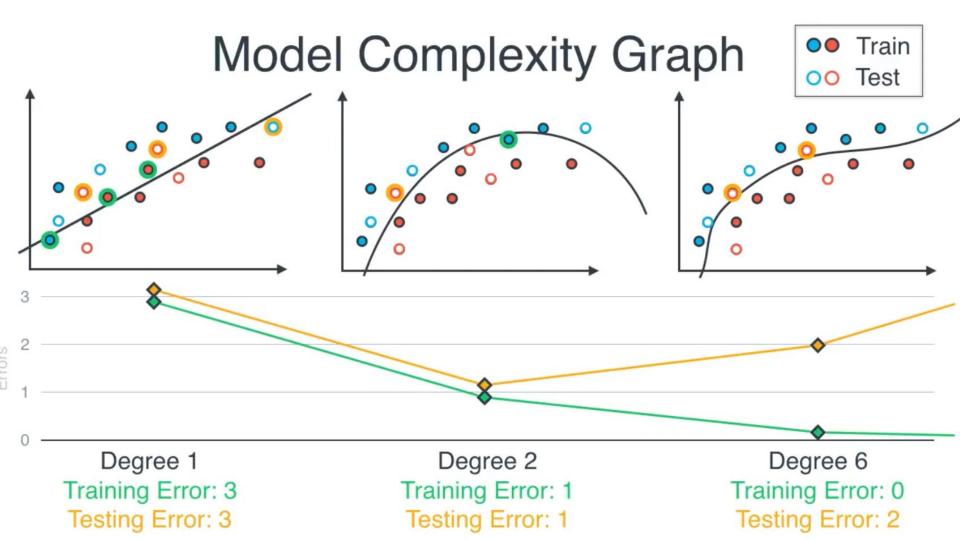


Great on Training set

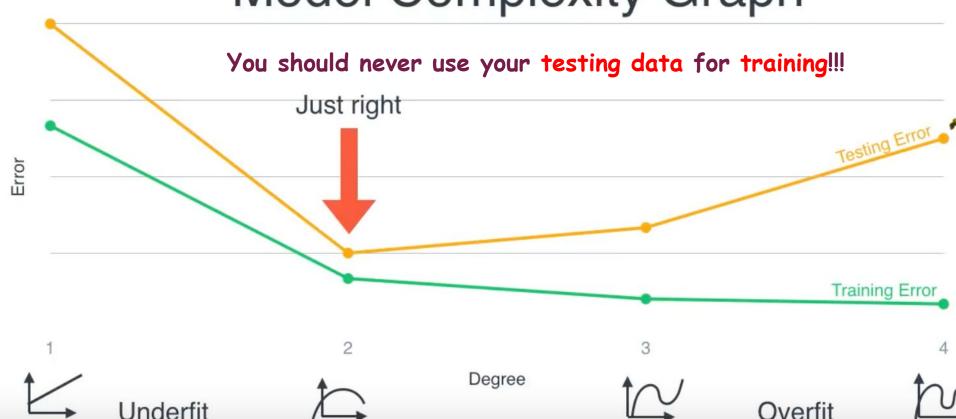
Bad on Testing set

## Model Complexity Graph



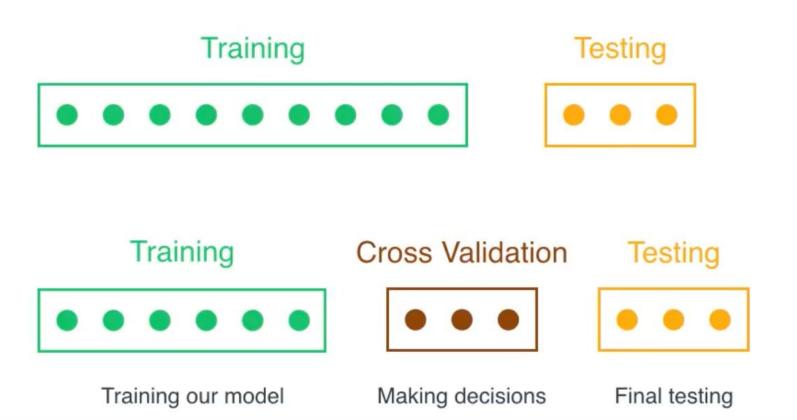


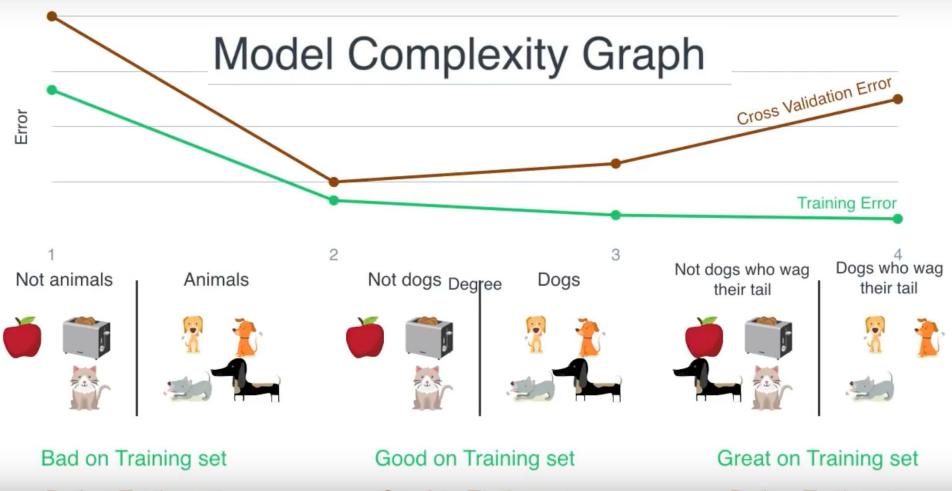
## Model Complexity Graph



### Training - Testing - Validation Datasets

### Solution: Cross Validation

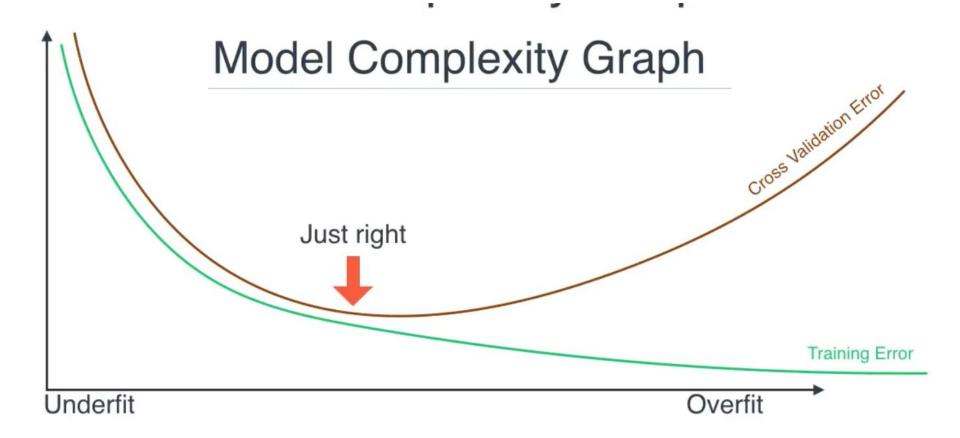




Bad on Testing set

Good on Testing set

Bad on Testing set



### Training a Decision Tree

Hyperparameters Parameters

Depth = 1

Depth = 2

Depth = 3

Depth = 4

F1 Score

0.5

0.8

0.4

0.2

**Training** 



**Cross Validation** 



Testing



## Training a Logistic Regression Model

Degree = 1



**Parameters** 

F1 Score



Training



Degree = 2



0.8





Degree = 3



0.4

Testing

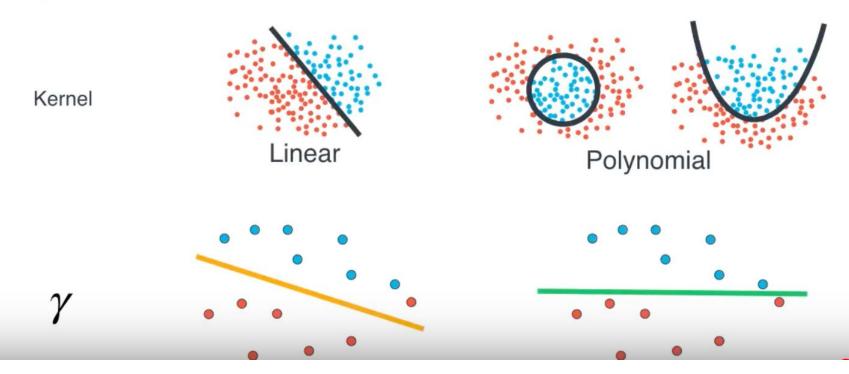




0.2

## Training a Support Vector Machine

Hyperparameters



# Parameters and Hyperparameters

| Algorithm                  | Parameters                     | Hyperparameters          |
|----------------------------|--------------------------------|--------------------------|
| Random Forest              | Features<br>Thresholds         | Number of trees<br>Depth |
| Logistic Regression        | Coefficients of the polynomial | Degree of the polynomial |
| Support Vector<br>Machines | Coefficients                   | Kernel<br>Gamma<br>C     |

### How to use machine learning

