

Name : Amesh Sharma - 2301010128

Que:

$$A = \begin{bmatrix} 1 & 2 & 3 & 0 \\ 2 & 4 & 3 & 2 \\ 3 & 2 & 1 & 3 \\ 6 & 8 & 7 & 5 \end{bmatrix}$$

$$R_2 \rightarrow R_2 - 2R_1$$

$$R_3 \rightarrow R_3 - 3R_1$$

$$R_4 \rightarrow R_4 - 6R_1$$

$$\begin{bmatrix} 1 & 2 & 3 & 0 \\ 0 & 0 & -3 & 2 \\ 0 & -4 & -8 & 3 \\ 0 & -4 & -11 & 5 \end{bmatrix}$$

$$R_2 \leftrightarrow R_3 \Rightarrow \begin{bmatrix} 1 & 2 & 3 & 0 \\ 0 & -4 & -8 & 3 \\ 0 & 0 & -3 & 2 \\ 0 & -4 & -11 & 5 \end{bmatrix}$$

$$R_4 \rightarrow R_4 - R_2$$

$$\begin{bmatrix} 1 & 2 & 3 & 0 \\ 0 & -4 & -8 & 3 \\ 0 & 0 & -3 & 2 \\ 0 & 0 & -3 & 2 \end{bmatrix}$$

$$\rightarrow R_4 \rightarrow R_4 - R_3 \quad \begin{bmatrix} 1 & 2 & 3 & 0 \\ 0 & -4 & -8 & 3 \\ 0 & 0 & -3 & 2 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

So Because we have Two non-zero
Row in Row echelon form

$$\boxed{\text{Rank} = 3}$$

$$T = x_1 = \begin{bmatrix} 1 \\ 1 \end{bmatrix}, \quad x_2 = \begin{bmatrix} -1 \\ 1 \end{bmatrix}$$

umesh

Que 2:- $T: W \rightarrow P_2$
Given

$$T \begin{bmatrix} a & b \\ c & d \end{bmatrix} = (a-b) + (b-c)x + (c-d)x^2$$

→ dimension of W :-

Symmetric 2×2 Have $\frac{n(n+1)}{2} = \frac{2 \times 3}{2} = 3$

Independent Value

→ The diagonal Element $\begin{bmatrix} a & b \\ c & d \end{bmatrix} \rightarrow \begin{bmatrix} b=c \\ T(a) & (d) \end{bmatrix}$
And off diagonal element

$$\boxed{\dim(W) = 3}$$

Rank of T :- T mapping to all polynomial of degree ≤ 2
Rank = 3 so nullity = $\dim(V) - \text{Rank} = 0$

Que 3:- $A = \begin{bmatrix} 2 & -1 \\ -1 & 2 \end{bmatrix}$

STUDENT'S NAME: Umesh Sharma

CLASS:

SUBJECT:

ROLL NO.:

DATE:

TOTAL MARKS OBTAINED:

→ Find THE Eigenvalue And Eigenvectors of A^T And $A+I$

Sol:- Finding Eigen Value of A

$$\det(A - \lambda I) = 0$$

$$A = \begin{bmatrix} 2 & -1 \\ -1 & 2 \end{bmatrix}$$

$$\det(A - \lambda I) = \begin{vmatrix} 2-\lambda & -1 \\ -1 & 2-\lambda \end{vmatrix}$$

$$(2-\lambda)^2 - (-1)(-1) = 0$$

$$\Rightarrow \lambda^2 - 4\lambda + 3 = 0$$

$$(\lambda - 1)(\lambda - 3) = 0$$

So $\boxed{\lambda = 1, 3}$ Eigenvalue of $\boxed{A = \begin{bmatrix} 2 & -1 \\ -1 & 2 \end{bmatrix}}$

→ Eigenvalue of $A = 1, 3$

→ Eigenvalue of A^{-1} = Reciprocal of Eigenvalue of A

$$\text{So } \boxed{A^{-1} \text{ Eigenvalues} = 1; 1/3}$$

→ Eigenvalue of $A + I = 4 + \text{Eigenvalue of } A$

$$4 + 1 = 5$$

$$4 + 3 = 7$$

$$\boxed{A + I \text{ Eigenvalue} = 5, 7}$$

→ Eigenvector

$$\text{For } A^{-1} = \begin{bmatrix} 2 & -1 \\ -1 & 2 \end{bmatrix}$$

$$\text{adj } A \quad \det(A) = 1 \times 1 = 1$$

$$(x=1) \text{ then } (y=1)$$

→ Queg - continue → answer shown

→ Now $A^{-1} = \frac{1}{3} \begin{bmatrix} 2 & 1 \\ 1 & 2 \end{bmatrix}$ And λ for $A^{-1} = 1$ or $1/3$

we Assume $A^{-1} = B$

To find Eigenvector

$$[B - \lambda I]X = 0 \rightarrow \text{for } \lambda = 1 \quad [B - I]X = 0$$

$$= \begin{bmatrix} \frac{2}{3} & \frac{1}{3} \\ \frac{1}{3} & \frac{2}{3} \end{bmatrix} - \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

$$= \begin{bmatrix} -\frac{1}{3} & \frac{1}{3} \\ \frac{1}{3} & -\frac{1}{3} \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

$$-\frac{x}{3} + \frac{y}{3} = 0 \quad \left(\frac{x}{3} = \frac{y}{3} \right) \quad (x = y)$$

→ if $x=1, y=1$

$$[(B-3I)x] = 0$$

STUDENT'S NAME		TOTAL MARKS OBTAINED
CLASS:	Arushi Shah	
ROLL NO.:	DATE:	

$$\Rightarrow \begin{bmatrix} \frac{2}{3} & \frac{1}{3} \\ \frac{1}{3} & \frac{2}{3} \end{bmatrix} - \begin{bmatrix} \frac{1}{3} & 0 \\ 0 & \frac{1}{3} \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} \frac{1}{3} & \frac{1}{3} \\ \frac{1}{3} & \frac{1}{3} \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

$$= \frac{x+y}{3} = 0, \quad \frac{x+y}{3} = 0 \quad \text{if } (x=1, y=-1)$$

For A^{-1} Eigenvectors $x_1 = \begin{bmatrix} 1 \\ 1 \end{bmatrix}, x_2 = \begin{bmatrix} -1 \\ 1 \end{bmatrix}$

Now $(A+4I) \Rightarrow \begin{bmatrix} 2 & -1 \\ -1 & 2 \end{bmatrix} + \begin{bmatrix} 4 & 0 \\ 0 & 4 \end{bmatrix} = C$

$$C = \begin{bmatrix} 6 & -1 \\ -1 & 6 \end{bmatrix} \Rightarrow \boxed{\lambda = 5, 7}$$

$$\boxed{[C - \lambda I]x = 0}$$

For $\lambda = 5$

$$\begin{bmatrix} 6 & -1 \\ -1 & 6 \end{bmatrix} - \begin{bmatrix} 5 & 0 \\ 0 & 5 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = 0$$

$$= \begin{bmatrix} 1 & -1 \\ -1 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = 0$$

For $\lambda = 7$

$$\begin{bmatrix} 6 & -1 \\ -1 & 6 \end{bmatrix} - \begin{bmatrix} 7 & 0 \\ 0 & 7 \end{bmatrix}$$

$$= \begin{bmatrix} -1 & -1 \\ -1 & -1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

$$= -x - y = 0$$

$$\boxed{x = -y}$$

Super

Que:- Matrix A is given

→ Que-2- dimensional

Eigenvectors $A+4I$ If $x_1 = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$, $x_2 = \begin{bmatrix} -1 \\ 1 \end{bmatrix}$

To summarize:-

Eigenvalues:- A : $\lambda_1 = 1, \lambda_2 = 3$

$A^{-1} = A^{-1}$: $\lambda_1 = 1, \lambda_2 = 1/3$

$A+4I$: $\lambda_1 = 5, \lambda_2 = 7$

Eigenvectors:-

$A^{-1} = x_1 = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$, $x_2 = \begin{bmatrix} -1 \\ 1 \end{bmatrix}$

$A+4I = x_1 = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$, $x_2 = \begin{bmatrix} -1 \\ 1 \end{bmatrix}$

$A = x_1 = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$, $x_2 = \begin{bmatrix} -1 \\ 1 \end{bmatrix}$

que:- $3x - 0.1y - 0.2z = 7.05$ (1)

(4)

$0.1x + 7y - 0.3z = 19.3$ (2)

$0.3x + 0.1y + 10z = 71.4$ (3)

STUDENT'S NAME

CLASS: 19-3

ROLL NO.:

SUBJECT:

DATE:

TOTAL MARKS OBTAINED

fix circuit

→ sol Assume $y=0, z=0$

$3x - 0.1(0) - 0.2(0) = 7.05$

$3x = 7.05$

$x = \frac{7.05}{3} = 2.35$

for y, $[z=0]$

$0.1(2.35) + 7y - 0.3(0) = -19.3$

$= 0.235 + 7y = -19.3$

$7y = -19.3 - 0.235$

$7y = -19.535$

$y = -2.7907$

for z,

$\Rightarrow 0.3x - 0.2(8) + 10z = 71.4$

$= 0.3(2.35) - 0.2(-2.7907) + 10z = 71.4$

$= 0.705 - 0.55814 + 10z = 71.4$

$0.14686 + 10z = 71.4$

$10z = 71.4 - 0.14686$

$= 71.25314$

$z = 7.125314$

(umesh
sharma)

Second iteration :-

$$3x - 0.1y_1 - 0.2z_1 = 7.85$$

$$3x - 0.1(-2.788) - 0.2(7.117) = 7.85$$

$$3x + 0.2788 - 1.4234 = 7.85$$

$$3x - 1.1446 = 7.85$$

$$3x = 7.8500 + 1.1446 = 8.9946$$

$$x_2 = 2.9982$$

for y $\rightarrow x_1 = 2.9982$

$$z_1 = 7.1172$$

$$= 0.1(2.9982) + 7y - 0.3(7.1172) = -19.3$$

$$\Rightarrow 0.29982 + 7y - 2.13516 = -19.3$$

$$7y - 1.83534 = -19.3$$

$$7y = -19.3 + 1.83534$$

$$y_2 = -2.4949$$

for z $\rightarrow x_1 = 2.9982$

$$y_2 = -2.4949$$

$$\Rightarrow 0.3(x_2) - 0.2(-4.2) + 10z = 71.4$$

$$\Rightarrow 0.3(2.9982) - 0.2(-2.4949) + 10z = 71.4$$

$$\Rightarrow 0.89946 + 0.49898 + 10z = 71.4$$

$$\Rightarrow 1.39844 + 10z = 71.4$$

$$z_2 = 7.000156$$

for Third iteration $(y_2 = -2.4949, z_2 = 7.000156)$

$$for x: 3x - 0.1(-2.4949) + 0.2(7.000156) = 7.85$$

$$3x + 0.24949 - 1.4000312 = 7.85$$

$$3x = 9.000517$$

$$x = 3.0001809$$

For y_2 0.1

$$\Rightarrow 0.3000$$

$$\Rightarrow 0.3000$$

For z_2 0.3

$$= 0.3$$

$$\Rightarrow 0.900$$

$$x_3 =$$

for satisfy

$$\Rightarrow 3$$

$$\Rightarrow 9$$

$$\Rightarrow$$

$$\Rightarrow 0.30001804 + 74 - 0.3(7.000156) = -19.3$$

$$\Rightarrow 0.30001804 + 74 - 2.1000468 = -19.3$$

$$74 - 1.8000208 = -19.3$$

$$74 = -19.3 + 1.8000208$$

$$74 = -17.4999712$$

$$y_3 = -2.499995806 \quad \checkmark$$

FoA Z3

$$0.3(23) - 0.2(y_3) + 162 = 71.4$$

$$= 0.3(3.0001804) - 0.2(-2.499995806) + 162 = 71.4$$

$$\Rightarrow 0.90005412 + 0.499999171 + 162 = 71.4$$

$$= 1.400053291 + 162 = 71.4$$

$$162 = 70.000$$

$$z_3 = 7.00000$$

$$x_3 = 3.00018, \quad y_3 = -2.49999, \quad z_3 = 7.00001$$

for satisfy:-

$$\Rightarrow 3(3.00018) - 0.1(-2.4999) - 0.2(7.0001) =$$

$$\Rightarrow 9.00054 + 0.24999 - 1.40002$$

$$\Rightarrow 9.25053 - 1.40004$$

$$= 7.85049 \approx 7.85$$

Ques 17

$$x + 3y + 2z = 0$$

$$2x - y + 8z = 0$$

$$3x - 5y + 4z = 0$$

$$x + 17y + 4z = 0$$

$AX=0$ form

$$\begin{bmatrix} 1 & 3 & 2 \\ 2 & -1 & 3 \\ 3 & -5 & 4 \\ 1 & 17 & 4 \end{bmatrix} \quad x = \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$

Augmented Matrix = $\begin{bmatrix} 1 & 3 & 2 & : & 0 \\ 2 & -1 & 3 & : & 0 \\ 3 & -5 & 4 & : & 0 \\ 1 & 17 & 4 & : & 0 \end{bmatrix}$

Row-echelon form:

$$\begin{array}{l} R_2 \rightarrow R_2 - 2R_1 \\ R_3 \rightarrow R_3 - 3R_1 \\ R_4 \rightarrow R_4 - R_1 \end{array} \quad \begin{bmatrix} 1 & 3 & 2 & : & 0 \\ 0 & -7 & -1 & & \\ 0 & -14 & -2 & & \\ 0 & 14 & 2 & & \end{bmatrix} \quad R_4 \rightarrow R_4 + R_3$$

$$\Rightarrow \begin{bmatrix} 1 & 3 & 2 \\ 0 & -7 & -1 \\ 0 & -14 & -2 \\ 0 & 0 & 0 \end{bmatrix} \quad R_3 \rightarrow R_3 - 2R_2 = \begin{bmatrix} 1 & 3 & 2 \\ 0 & -7 & -1 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

$\rho(A) = 2$

$\rho(A:B) = 2$

$\rho(A) = \rho(A:B)$

\Rightarrow Consistent

$$\begin{bmatrix} 1 & 3 & 2 & : & 0 \\ 0 & -7 & -1 & & \end{bmatrix}$$

$\rho(A) < \text{no. of unknown (infinite sol)}$

Que 5-Continue - umesh, sharma

$$\begin{bmatrix} 1, 3, 2 \\ 0, -7, -1 \\ 0, 0, 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$

$$= 2 + 3y + 2z = 0 \quad \text{--- (1)}$$

$$-7y - z = 0 \quad \text{--- (2)}$$

$$\boxed{z = -7y} \text{ Put in (1)}$$

$$2 + 3y + 2(-7y) = 0$$

$$2 + 3y + 14y = 0$$

$$\boxed{2 + 17y = 0}$$

$$\Rightarrow \boxed{x = -17y = -\frac{11}{7}z}$$

$$\boxed{x = -17y = -\frac{11}{7}z}$$

$$\text{So } \boxed{x=0, y=0, z=0}$$

A.S.O.

Q6: Given :- $T(a+bx+cx^2) = (a+1) + (b+1)x + (c+1)x^2$

Additivity :- $T(u+v) = T(u) + T(v)$

for all u, v in P_2

Homogeneity :- $T(au) = aT(u)$ for all u in P_2 and a scalar

①

Soln :- $u = a+bx+cx^2$ and $v = a'+b'x+c'x^2$ in P_2

Then $u+v = (a+a') + (b+b')x + (c+c')x^2$

Now $T(u) = (a+1) + (b+1)x + (c+1)x^2$ and

$T(v) = (a'+1) + (b'+1)x + (c'+1)x^2$

$T(u+v) = (a+a'+1) + (b+b'+1)x + (c+c'+1)x^2$

↓

$T(u) + T(v) = (a+1) + (b+1)x + (c+1)x^2 + (a'+1) + (b'+1)x + (c'+1)x^2$

$= (a+a'+1) + (b+b'+1)x + (c+c'+1)x^2$

$$T(u+v) = (a+a'+1) + (b+b'+1)x + (c+c'+1)x^2$$

↓

$$T(u) + T(v) = (a+1) + (b+1)x + (c+1)x^2 + (a'+1) + (b'+1)x + (c'+1)x^2$$

$$= (a+a'+1) + (b+b'+1)x + (c+c'+1)x^2$$

$$T(u+v) = T(u) + T(v) \Rightarrow \text{so satisfied}$$

② $U = q + b_1 x + c_1 x^2 \rightarrow P_2$ let a any scalar

$$aU = aa + ab_1x + ac_1x^2$$

$$T(aU) = (aa+1) + (ab_1+1)x + (ac_1+1)x^2$$

↓

$$a(T(U)) = a(a+1) + a(b+1)x + a(c+1)x^2$$

$$= (aa+1) + (ab+1)x + (ac+1)x^2$$

Satisfy \rightarrow satisfy both it's Linear Transform

UMesh Sharma

Q7 :- $S = \begin{bmatrix} 1 & 2 & 3 \\ 3 & 1 & 0 \\ -2 & 1 & 3 \end{bmatrix}$

Applying R.R.E.F.

$$\begin{array}{l} R_2 \rightarrow R_2 - 3R_1 \\ R_3 \rightarrow R_3 + 2R_1 \end{array} = \begin{bmatrix} 1 & 2 & 3 \\ 0 & -5 & -9 \\ 0 & 5 & 7 \end{bmatrix} \quad \begin{array}{l} R_3 \rightarrow R_3 + R_2 \end{array} \begin{bmatrix} 1 & 2 & 3 \\ 0 & -5 & -9 \\ 0 & 0 & 0 \end{bmatrix}$$

$\rho(A) < \text{no. of unknown} \rightarrow$ linearly dependent
And Having infinite many solution

\rightarrow So it's not a basis $V_3(\mathbb{R})$.

To determine dimension and basis subspace spanned by S . we use row-reduced form $(1, 2, 3)$ and $(3, 3, 0)$

Then dimension of sub-space = 2

$$x - 3y + 7z = 16 \quad \text{--- (8)}$$

With initial value $x_0 = 1, y_0 = 1, z_0 = 1$

Step 1

$$\underline{x_1}:- 3x_1 - 6y_0 + 2z_0 = 23 \Rightarrow 3x_1 - 6 + 2 = 23, \\ 3x_1 = 27, \quad \boxed{x_1 = 9} \quad \checkmark$$

$$\underline{y_1}:- 4x_0 + y_1 - z_0 = -18, \quad -4 + y_1 - 1 = -18, \quad \boxed{y_1 = -10}$$

$$\underline{z_1}:- x_0 - 3y_0 + 7z_0 = 16 \Rightarrow 1 - 3 + 7z_0 = 16, \quad 7z_0 = 18 \\ z_0 = \boxed{18/7}$$

$$\rightarrow \boxed{x_1 = 9, y_1 = -10, z_1 = 2.571}$$

Iteration 2 using value of 1:-

$$\underline{x_2}:- 3x_2 - 6(-10) + 2 \times 2.571 = 23 \Rightarrow 3x_2 = 23 - 65.14 \\ \boxed{x_2 = -14.04}$$

$$\underline{y_2}:- -4x_1 + y_2 - z_0 = -15 \\ -4 \times 9 + y_2 - 2.57 = -15, \quad y_2 = -15 + 38.57$$

$$\boxed{y_2 = 23.571}$$

$$\underline{z_2}:- x_1 - 3(y_1) + 7z_2 = 16 \Rightarrow 9 - 3(-10) + 7z_2 = 16 \\ 7z_2 = 16 - 39 \quad z_2 = \frac{-23}{7} = \boxed{-3.28571}$$

$$\boxed{z_2 = -3.28571}$$

Que - 8 - Continue - Lemesh

Now working on 3rd iteration using
2nd iteration value:

$$\boxed{x_2 = -14.04} \quad y_2 = 23.571 \quad z_2 = -3.28571$$

$$x_3: 3x_2 - 6y_2 + 2z_2 = 23$$

$$\Rightarrow 3(-14.04) - 6(23.571) + 2(-3.28) = 23$$

$$\Rightarrow -42.12 - 141.426 + 6.56 = 23$$

$$3x_3 = 170.98$$

$$\boxed{x_3 = 56.9933}$$

$$y_3: -4x_2 + y_3 - z_2 = -15$$

$$-4(-14.04) + y_3 - (-3.28) = -15$$

$$= 56.16 + y_3 + 3.28 = -15$$

$$\boxed{y_3 = -74.44}$$

$$z_3: x_2 - 3y_2 + 7z_3 = 16$$

$$-14.04 - 3(23.571) + 7z_3 = 16$$

$$\Rightarrow -14.04 - 70.713 + 7z_3 = 16$$

$$= -84.753 + 7z_3 = 16$$

$$7z_3 = 100.753$$

last iteration
value is

$$x_3 = 56.9933$$

$$y_3 = -74.44$$

$$z_3 = 14.37$$

Que 9

soln: The

Image

The

rotating

Repro

Blurring

To unders

understa

→ digital

Curse

Pixel

Grad

→ A digit

which as

Image

a dig

→ basically

① Black-

① Black-

An

format

→ Computer

→ in Que

1-255

Que 9:- Umesh

STUDENT'S NAME:		
CLASS:	SUBJECT:	
ROLL NO.:	DATE:	

Soln:- There are many use of matrix operations in image processing one of them is image transformation. The transformation include such transition like rotating, scaling, and shearing which can be represented by matrix multiplication.

Blurring an image is also one of them. To understand blurring process first we have to understand what are the digital images:-

- digital image made up a series of pixels. Currently, we use "24 bit RGB" system of color each pixel. That mean each color have 256 gradient.
- A digital image formed by small bit of data which are stored in computers. When we capture an image in camera presence of light. The camera works like a digital sensor and convert into digital signals.

→ Basically image has three types

(1) Black-white (2) Gray-scale (3) R.G.B

(1) Black-white:- In this image we use 1 as white and 0 as black at for every pixel in format of matrix it one dimension

→ Computer see image only on the basis of matrix

→ In grey scale picture, 0 - black, 255 - white (1-255) - different shades

RGB:- image → it is a 3-D matrix first comp
Red, Then Green Then Blue ^{Value} _{Matrix}

on using

2 - 3.28571

6.9933

last iteration
Value is

$z_3 = 56.9933$

$y_3 = -74.49$

$z_3 = 19.37$

If we select Any value it Return

RGB(150, 200, 150)

Que-9-umesl

→ Blurring a image:- Computer Take A Kernel Matrix. And it's place multiplied with every 3×3 matrix formation on The Image Matrix. After The done of multiplication

Average value placed on central pixel That Region But on a new-empty image Matrix.

→ Then That process Goes over The All matrix Place Appropriate value in new matrix.

→ After done we get Another matrix which consist value of Blurred image with The Help of Average value pixel. which is Nothing But The Required Blurred image

→ The particalar blur which we'll get by multiply Kernel containing All $1/9$ element called Box-Blur

STUDENT'S NAME:		TOTAL MARKS OBTAINED
CLASS:	SUBJECT:	
ROLL NO.:	DATE:	

Q10 :- A Linear Transformation for Rotating a 2D Image involves applying a mathematical operation to the image matrix that effectively rotates the images by a specified angle around a chosen center point.

Transformation can be represented by a 2×2 rotation matrix:

$$\begin{pmatrix} \cos(\theta) & -\sin(\theta) \\ \sin(\theta) & \cos(\theta) \end{pmatrix} \rightarrow \theta \text{ is rotation in radians}$$

To rotate each pixel rotate and mapped to a new position to the rotated image according to the transformation matrix.

Rotated-coordinate can be calculated by multiplying the original coordinates of each pixel of rotation matrix.

Linear Transformation preserve the straightness of lines and angle in the image, making it a common operation in computer-vision task such as image processing, object recognition and Geometric Transformation.