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# AI1103-Assignment 2

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#### Download latex-tikz codes from

https://github.com/Umesh-k26/AI-1103/blob/main/Assignment2/assignment2.tex

## and python codes from

https://github.com/Umesh-k26/AI-1103/blob/main/Assignment2/codes/assignment2.py

### QUESTION

Let the probability density function of a random variable X be

$$f(x) = \begin{cases} x & 0 \le x < \frac{1}{2} \\ c(2x-1)^2 & \frac{1}{2} < x \le 1 \\ 0 & \text{otherwise} \end{cases}$$

then, the value of c is equal to \_\_\_\_\_.

#### Solution

For a probability density function of a continuous random variable,

$$\int_{-\infty}^{\infty} f(x) \, dx = 1 \tag{0.0.1}$$

$$\int_{-\infty}^{\infty} f(x) dx = \int_{0}^{1/2} f(x) dx + \int_{1/2}^{1} f(x) dx \qquad (0.0.2)$$

$$= \int_{0}^{1/2} x dx + \int_{1/2}^{1} c(2x - 1)^{2} dx \qquad (0.0.3)$$

$$= \frac{x^{2}}{2} \Big|_{0}^{1/2} + c \left( \frac{4x^{3}}{3} - 2x^{2} + x \right) \Big|_{1/2}^{1} \qquad (0.0.4)$$

$$= \frac{1}{8} + c \left( \frac{1}{3} - \frac{1}{6} \right) \qquad (0.0.5)$$

$$= \frac{1}{8} + \frac{c}{6} \qquad (0.0.6)$$

from (0.0.1) and (0.0.6) we get

$$1 = \frac{1}{8} + \frac{c}{6} \tag{0.0.7}$$

$$\therefore c = \frac{21}{4} \tag{0.0.8}$$

Graph of the function f(x) using python:

