

University of Moratuwa

Department of Electronic and Telecommunication Engineering



BM4152

Bio-signal Processing

Assignment 2

Tilakarathna. U.A.

200664P

Table of Contents

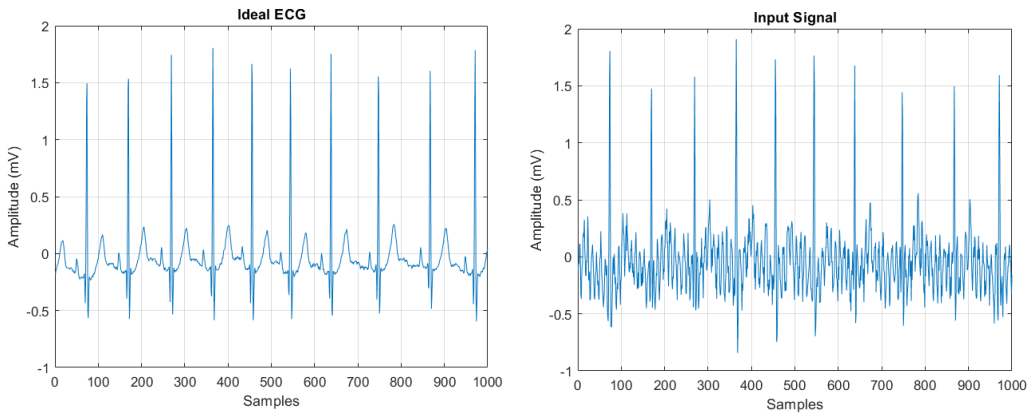
1. Wiener filtering.....	3
Data construction.....	3
1.1 Discrete time-domain implementation of the Wiener filter	3
Part 1.....	3
Part 2	6
1.2 Frequency domain implementation of the Wiener filter	9
1.3 Effect on non-stationary noise on Wiener filtering	9
2. Adaptive filtering.....	10
Data construction.....	10
2.1 LMS method	11
2.2 RLS method	12

Optimum and Adaptive Filters

1. Wiener filtering

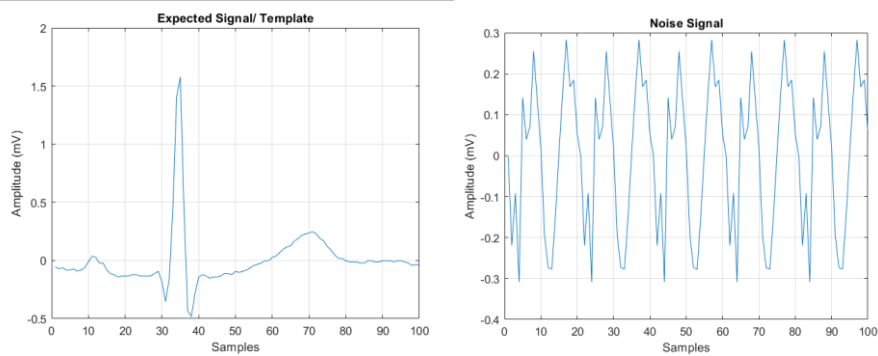
Data construction

Zoomed versions of the data signals are added.



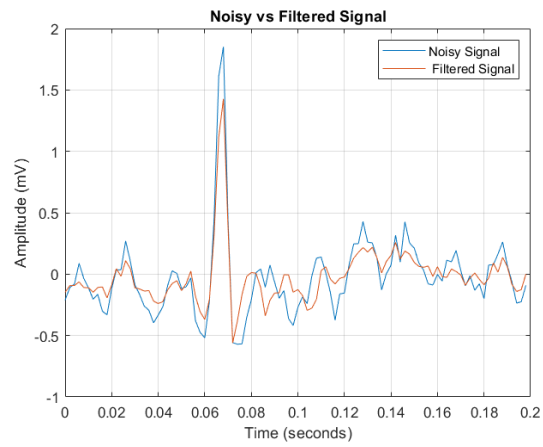
1.1 Discrete time-domain implementation of the Wiener filter

Part 1



Noise signal is the noise template extracted from the input ECG.

a) Wiener filtered signal for order = 25.

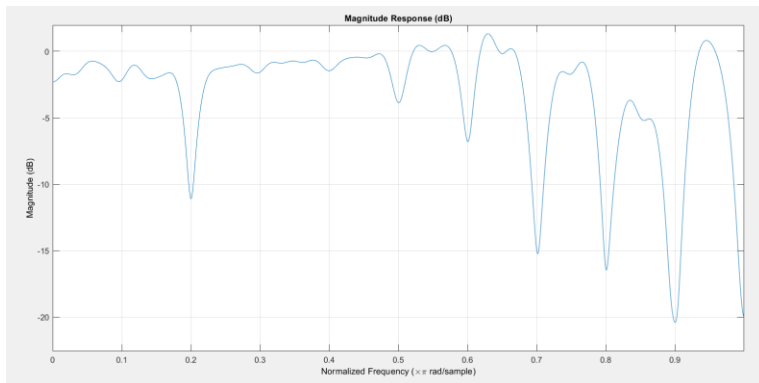


b) Calculating optimum order:

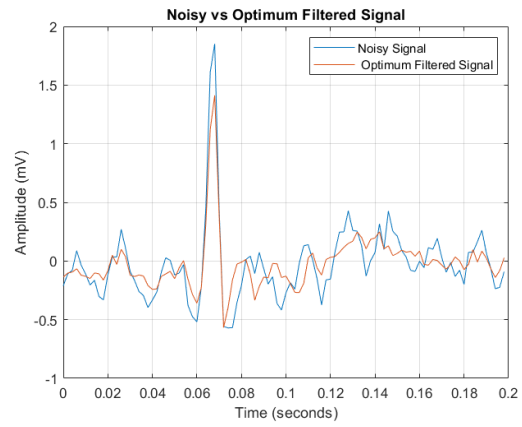


Optimum order for Wiener filter: 62

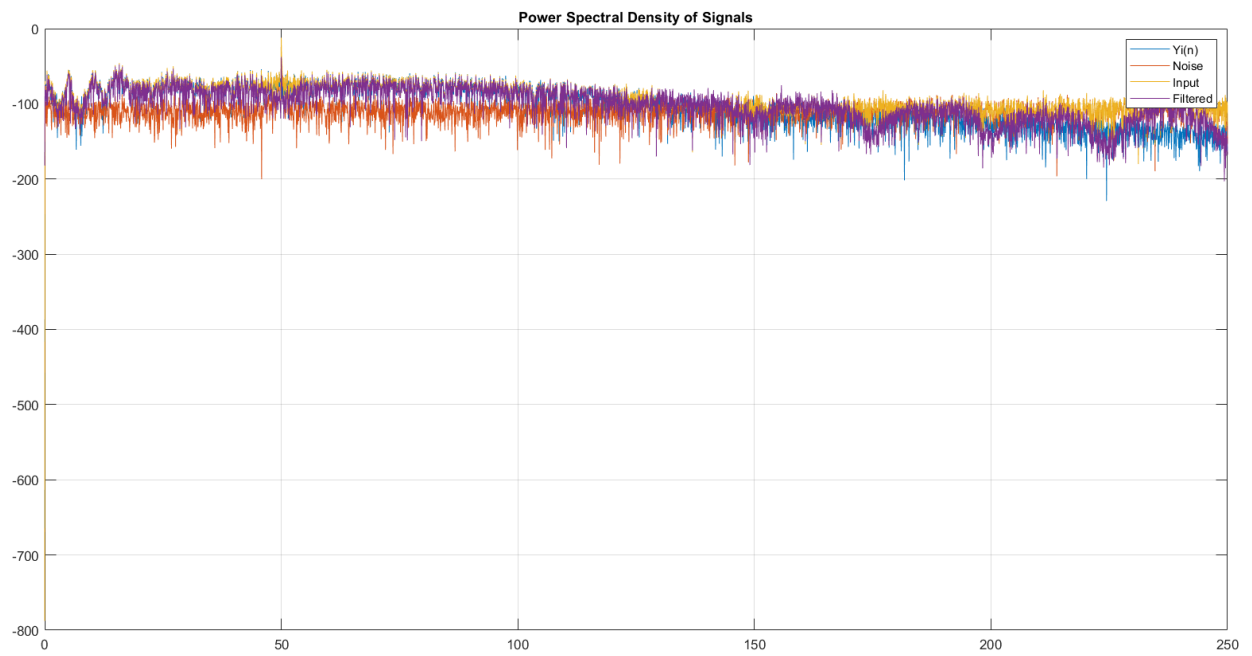
Magnitude response of optimum order filter:



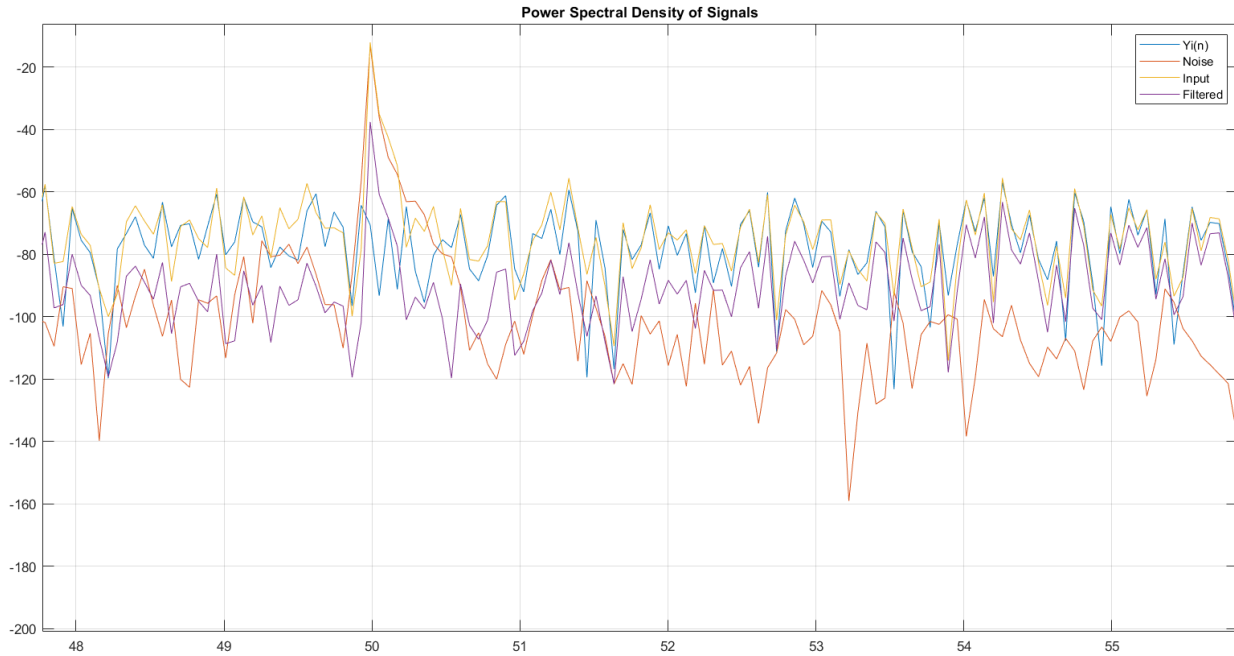
c)



d)



Zoomed:

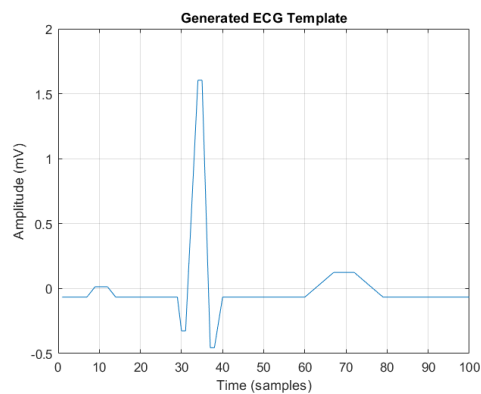


e)

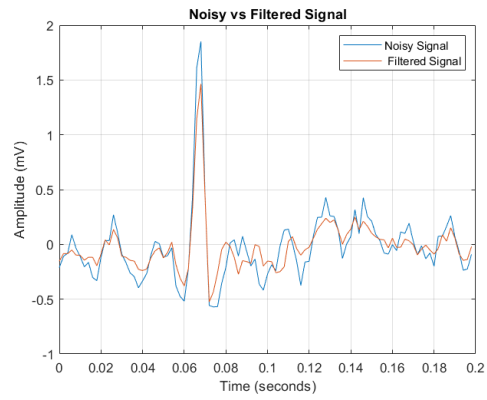
Since the added noise contained 50 Hz, noise, we can see a drop in the magnitude response at 50 Hz, and also in the power spectral density of the filtered signal at 50 Hz.

Also the ECG signal is only comprised of frequencies upto 150 Hz. The magnitude response shows that it has attenuated for higher frequencies which have been correctly identified as noise.

Part 2

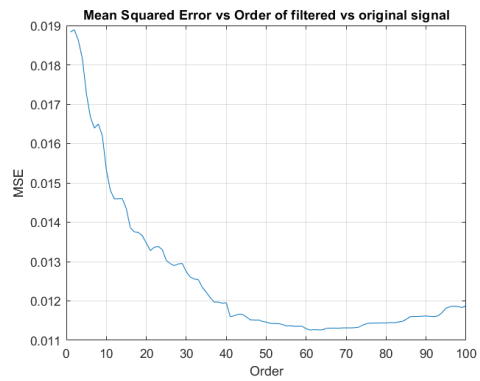


a)

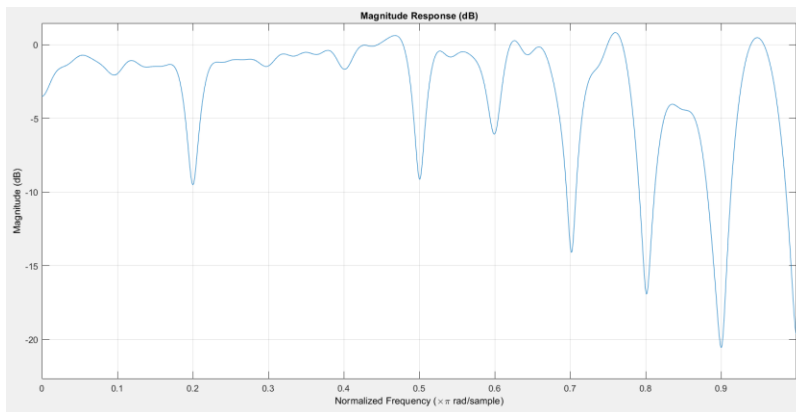


For order = 25

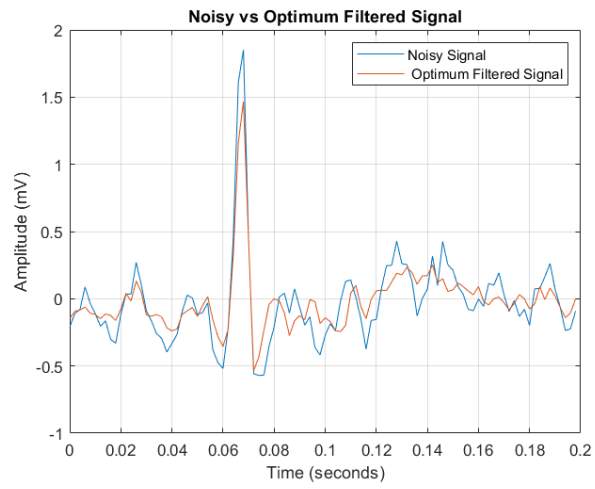
b)



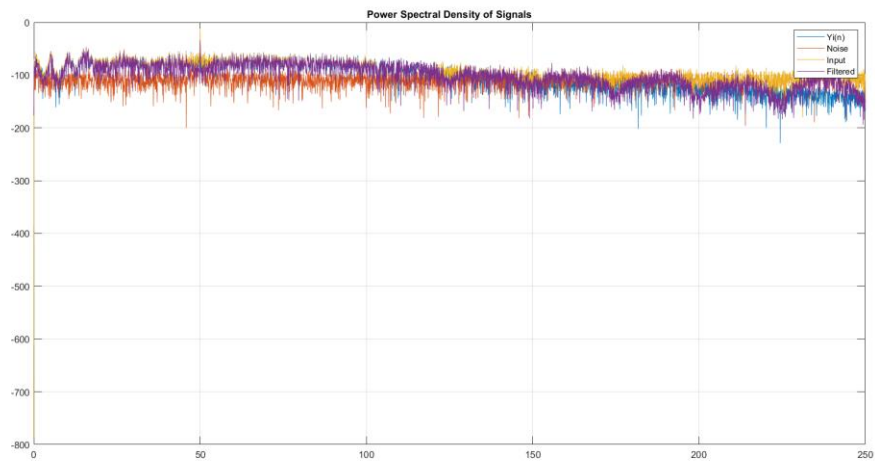
Optimum order for Weiner filter with constructed ECG: 61



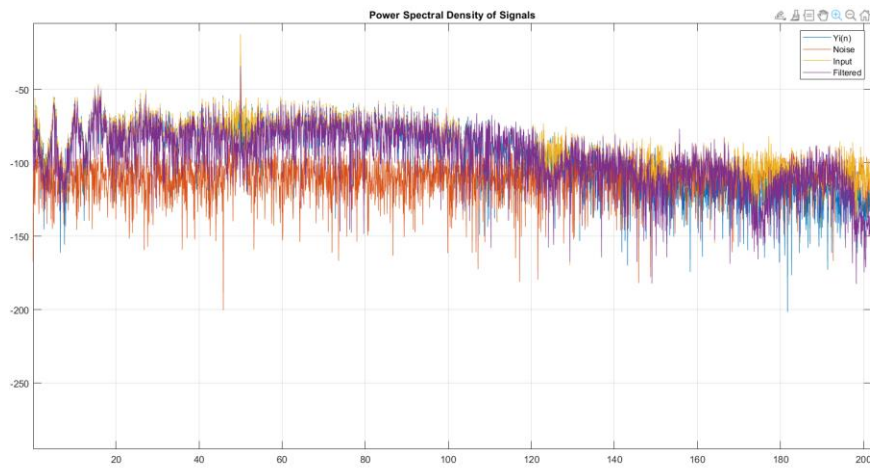
c)



d)

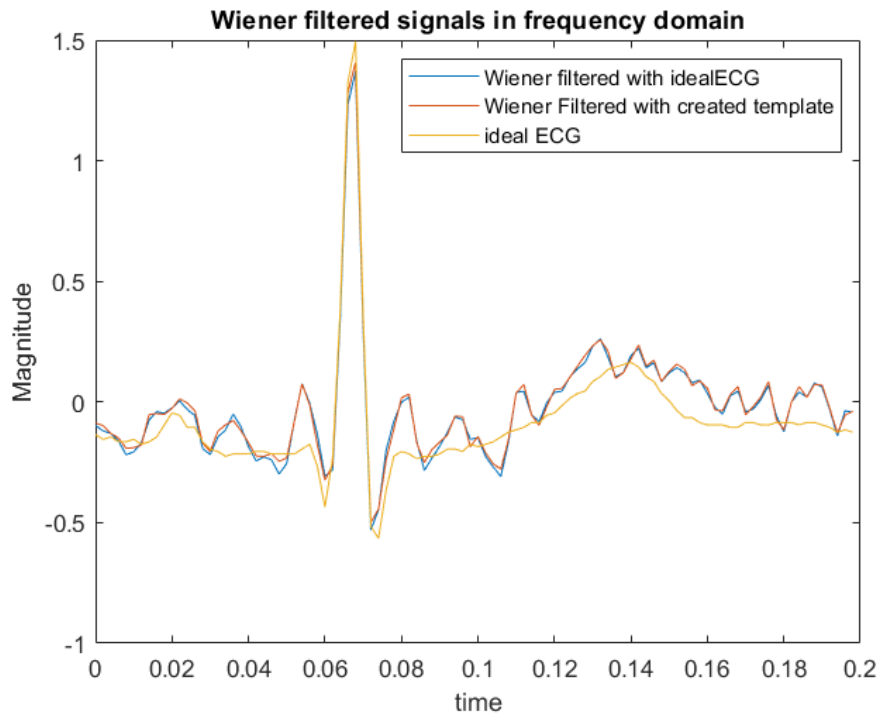


Zoomed:

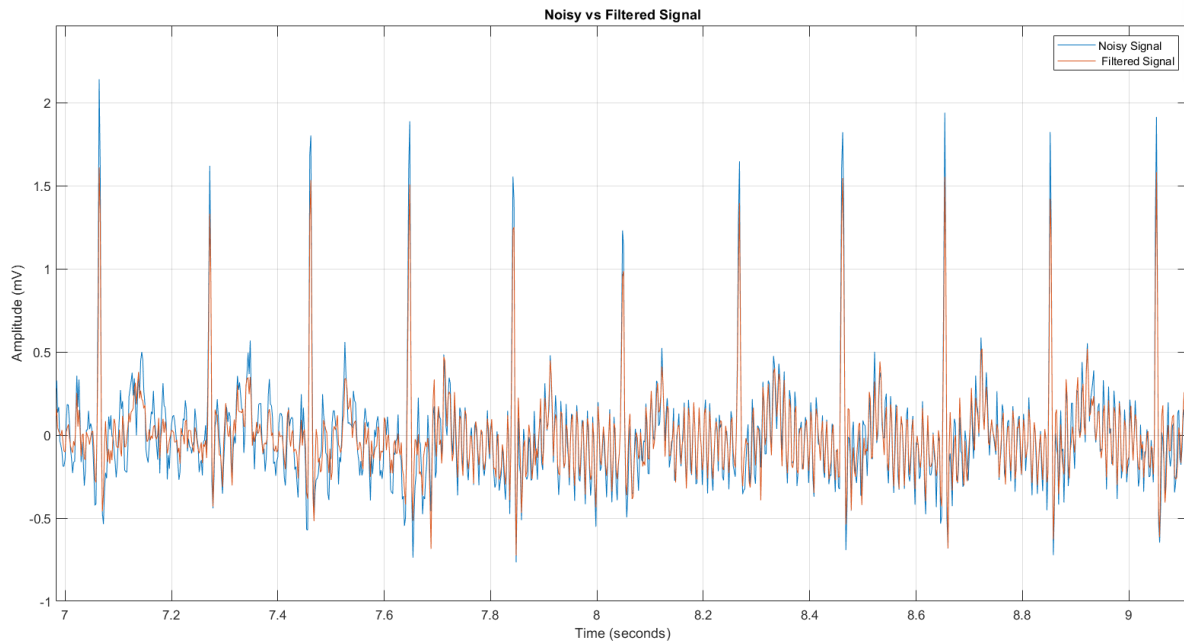


A similar situation to the previous case is observed in the magnitude response and the power spectra. The noise at 50 Hz and at higher frequencies are identified and removed by the filter.

1.2 Frequency domain implementation of the Wiener filter



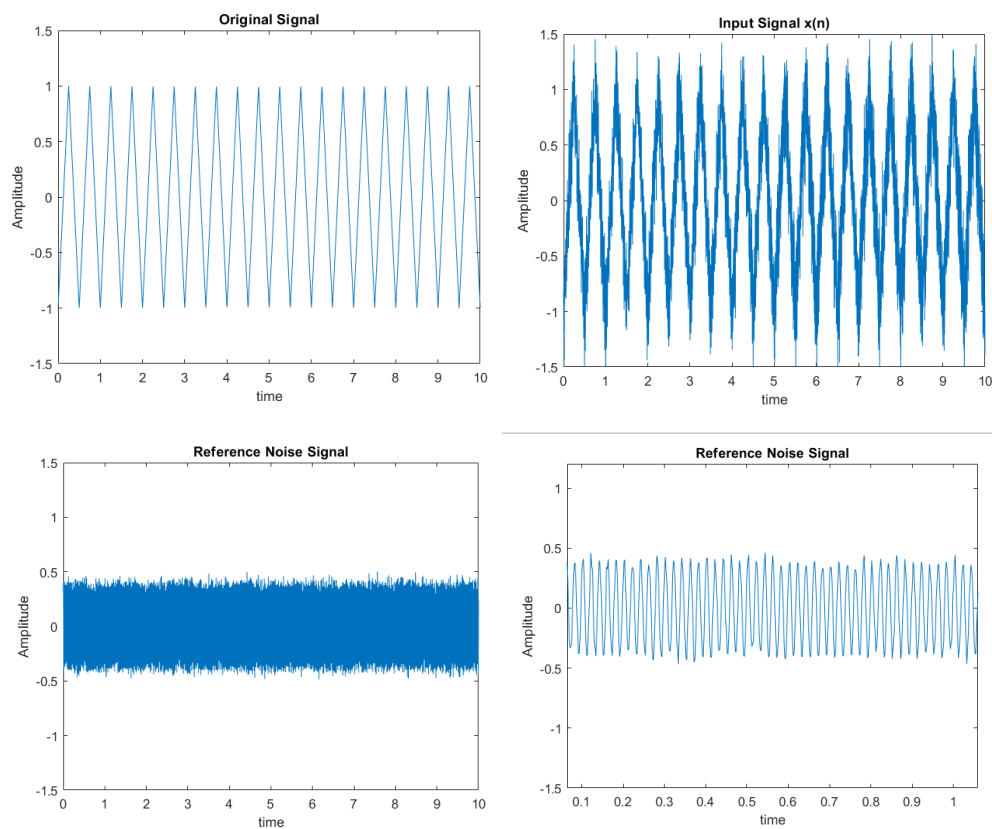
1.3 Effect on non-stationary noise on Wiener filtering



Even though the filter is successful at removing 50 Hz noise, the high frequency noise at 100 Hz, has not been filtered. This is because the Wiener filter has not adapted to the new noise, as it uses the same set of coefficients learnt from the known template noise to filter the signal. This known filter did not include 100 Hz noise.

2. Adaptive filtering

Data construction



Coefficients used:

$\text{snr} = 10; \text{ (dB)}$

$a = 0.2;$

$\phi = \pi/3;$

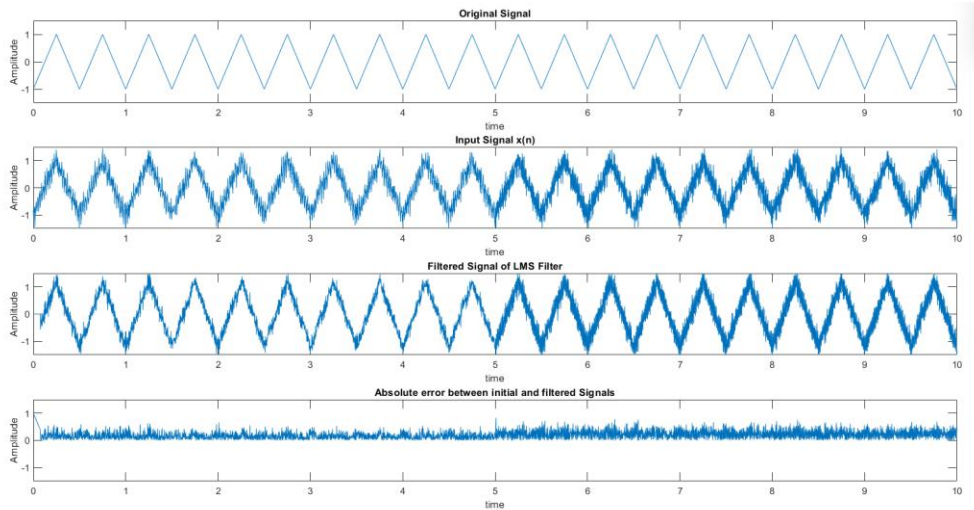
$\phi_1 = \pi/6;$

$\phi_2 = \pi/4;$

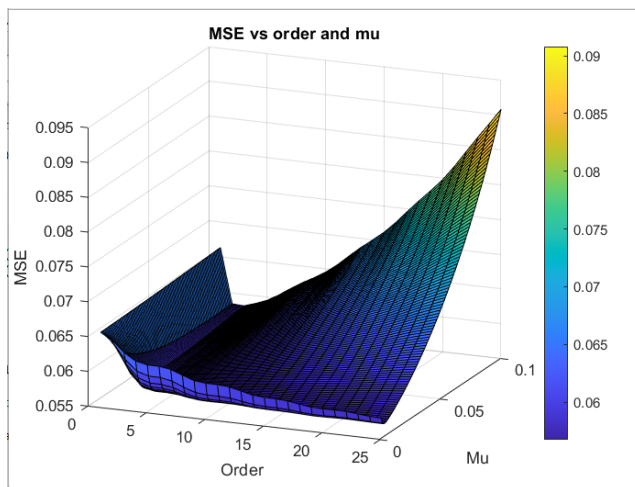
2.1 LMS method

b)

Order = 40; $\mu = 0.05$;



c)



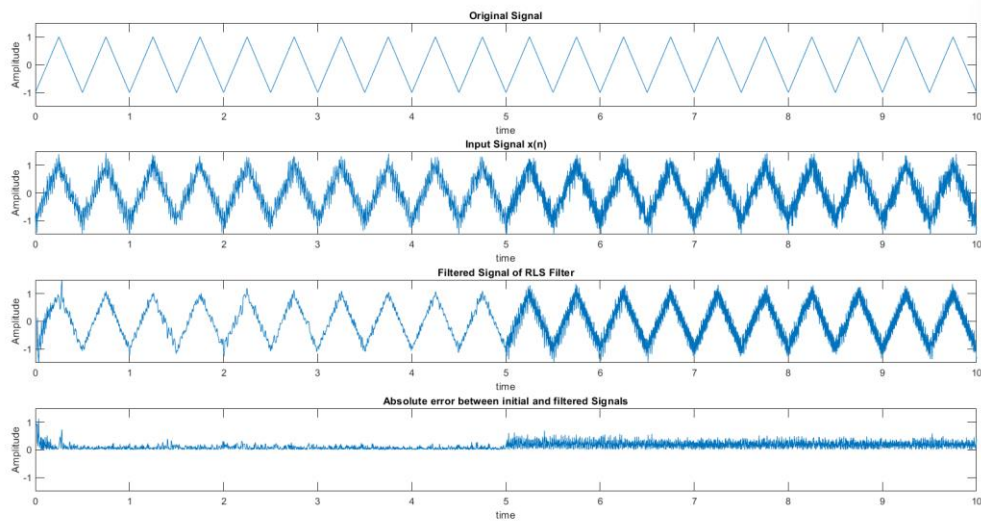
Optimum \rightarrow Order: 9 μ : 0.01

2.2 RLS method

a)

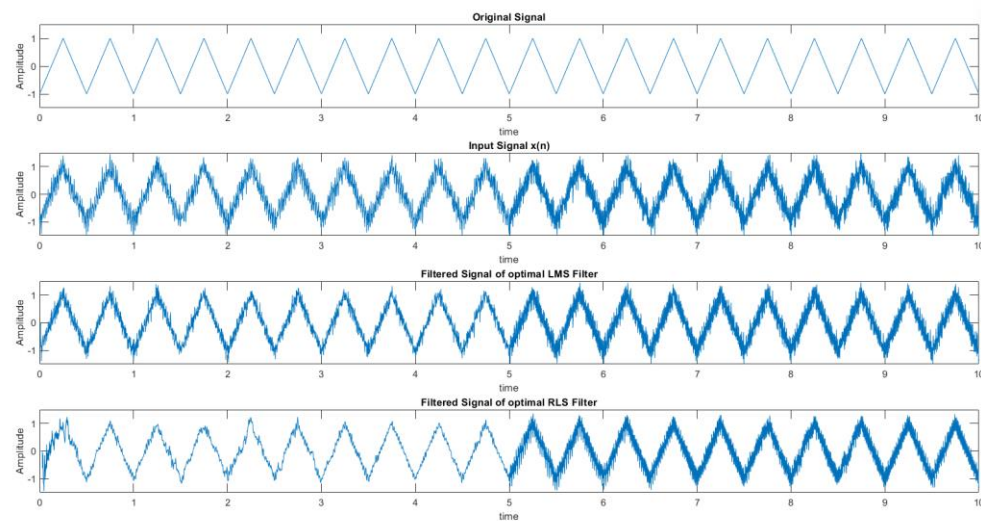
$\lambda = 0.999$;

order = 10;

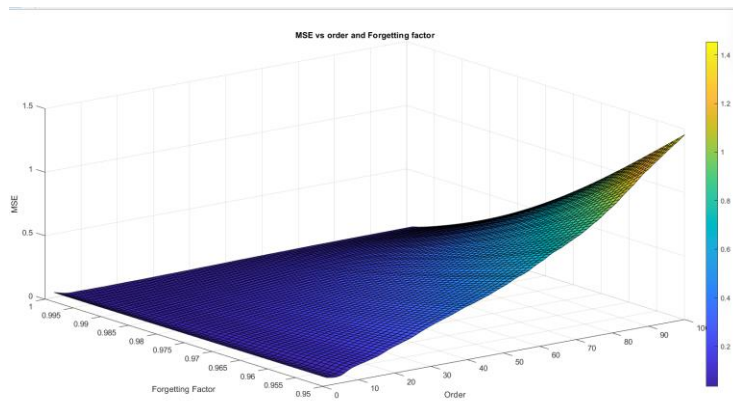


b)

Comparing performance:

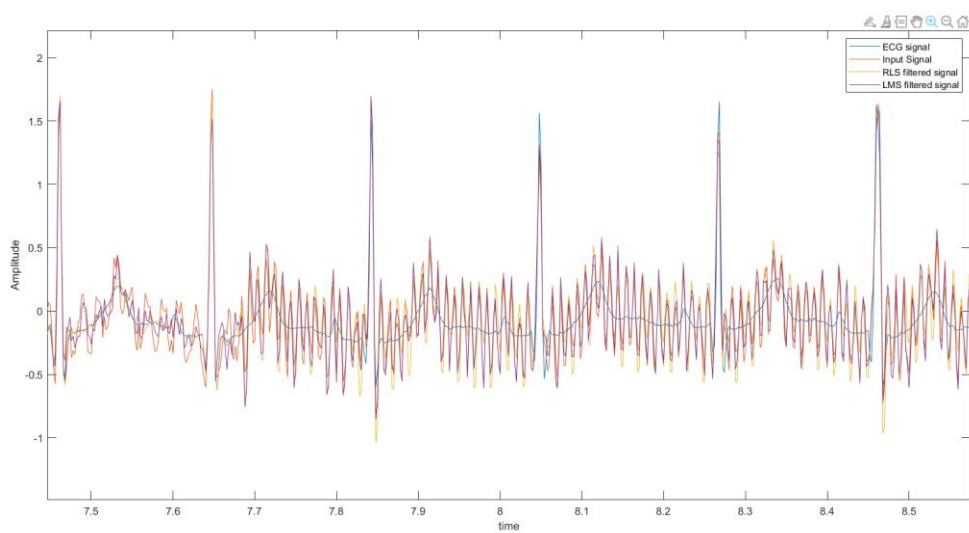
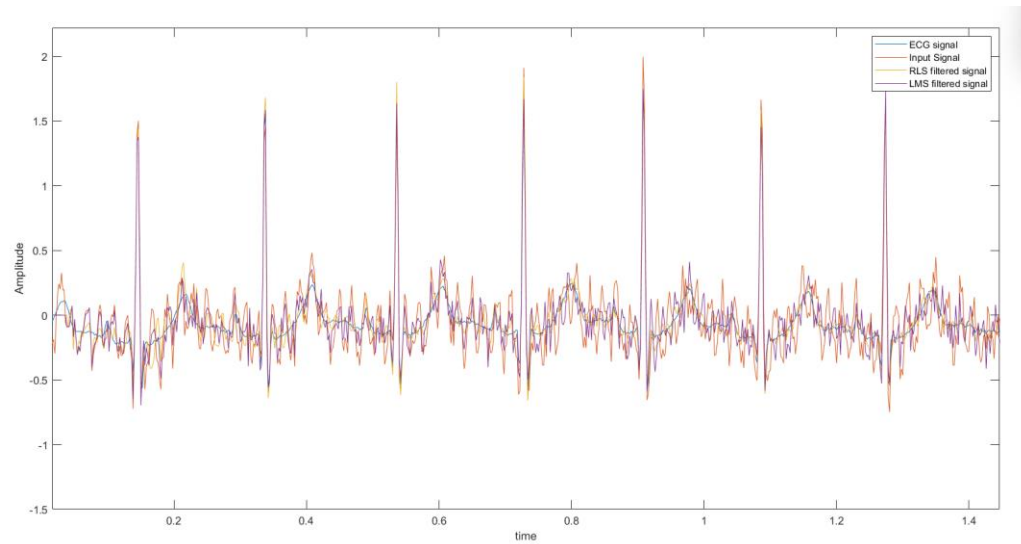


c)



Optimum \rightarrow Order: 15 μ : 0.999

d)



Here, RLS and LMS were filtered using the previous optimal parameters. We can see the optimal order of RLS filter is higher. However, also by observing the initial part and the region where the noise shifts, we can see that the RLS filter has adapted to the noise comparatively faster. This scenario can also be observed in the previously plotted sawtooth signals.