

# Lecture 25

## Final Exam Review

EECS 281: Data Structures & Algorithms

# Time and Location

- When: Friday 18 December, 8:00am (sharp) - 10:00am (120min)
- Accommodation (extended time) exam starts at 8:00am
- Location: check CTools announcements, rooms assigned by username

# Policies

- Closed book and closed notes
- One “cheat sheet”, limited to 8.5"x11", double-sided, hand-written by you, with your name on it
- No calculators or electronics of any kind
- Engineering Honor Code applies

# Don't forget!

The University of Michigan  
Electrical Engineering & Computer Science  
EECS 281: Data Structures and Algorithms  
Fall 2015



FINAL EXAM  
**Multiple-Choice Portion, KEY 1**  
Friday December 18, 2015  
8:00AM – 10:00AM (120 minutes)

Record your NAME, Student ID# and Exam KEY # on the Scantron form. There will be a penalty for incorrectly filling out the form.

Name: _____	Uniqname: _____
Student ID: _____	
Uniqname of person to your left: _____	
Uniqname of person to your right: _____	
<b>Honor Pledge:</b> "I have neither given nor received unauthorized aid on this examination, nor have I concealed any violations of the Honor Code."	
Signature: _____	

Record your NAME, Uniqname and Student ID# LEGIBLY! on the written portion

**SIGN THE HONOR PLEDGE ON THE WRITTEN PORTION!**  
We won't post a final grade without it!

# Study Materials

- Practice questions posted on CTools
- Lecture slides and recordings
- In-class exercises
- Discussion materials
- Study group
- Another idea: programming interview questions

# Topics

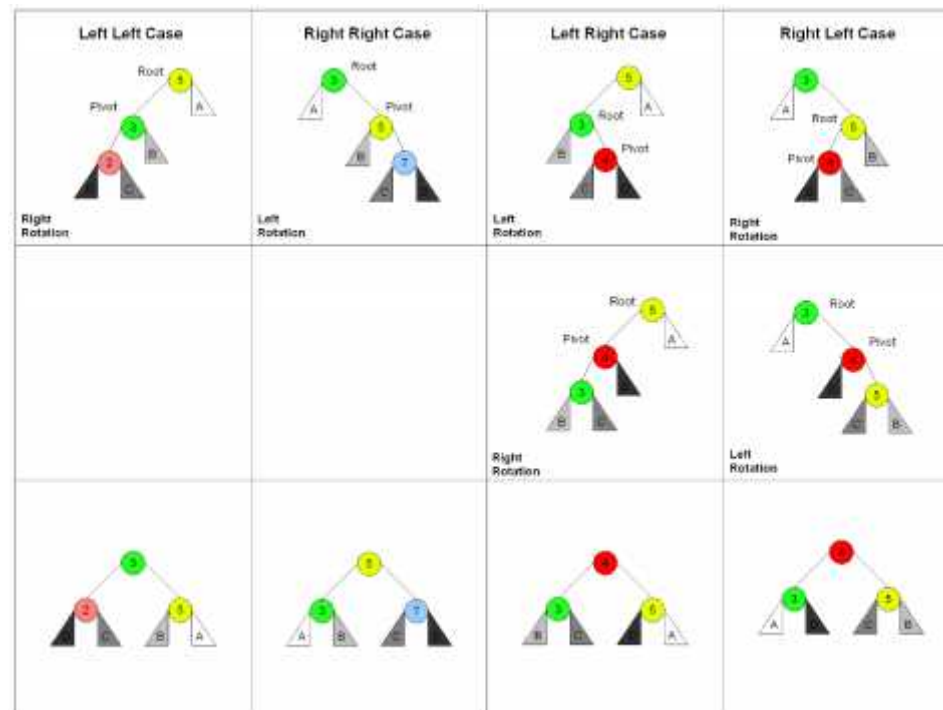
- Cumulative, but we will focus on material that has not yet been tested
- Trees (general, binary, search, AVL)
- Hashing (and collision resolution)
- Graphs and graph algorithms
- Algorithm Families

# Trees

- General trees
- Binary trees
- BSTs
- AVL trees

# Exercise

- Insert these keys into an AVL tree, rebalancing when necessary
- 4, 2, -1, 5, 7, 8, 9, 13, 12, 10





# Exercise

# Hashing

- Hash functions
- Hash tables
- Collision resolution
  - Separate Chaining
  - Linear Probing
  - Quadratic Probing
  - Double Hashing

# Hashing

- What is the complexity of inserting into a hash table with  $m$  slots that stores  $n$  **unique** keys?
- Separate chaining
  - Best, worst, average
- Linear probing
  - Best, worst, average

# Hashing

- Separate chaining
  - Best, worst, average
  - $O(1)$ ,  $O(n)$ ,  $O(n/m)$     $O(1)$
- Linear probing
  - Best, worst, average
  - $O(1)$ ,  $O(n)$ ,  $O(n/m)$     $O(1)$
- Same as insert

# Graphs

# Graphs

- Graphs in general
  - Terminology and types
  - Adjacency matrix vs. adjacency list
- Search
  - DFS, BFS
- MST
  - Prim's, Kruskal's
- Shortest path
  - Dijkstra, Floyd-Warshall

# Graph Terminology

- edge
- vertex/node
- degree
- weight
- directed / undirected
- simple graph (no loops or parallel edges)
- adjacency matrix
- adjacency list
- sparse graph
  - $|E| \ll |V|^2$ , adjacency list
- dense graph
  - $|E| \sim |V|^2$ , adjacency matrix
- simple path
- connected graph
- cycle
- spanning tree / MST
- Hamiltonian cycle

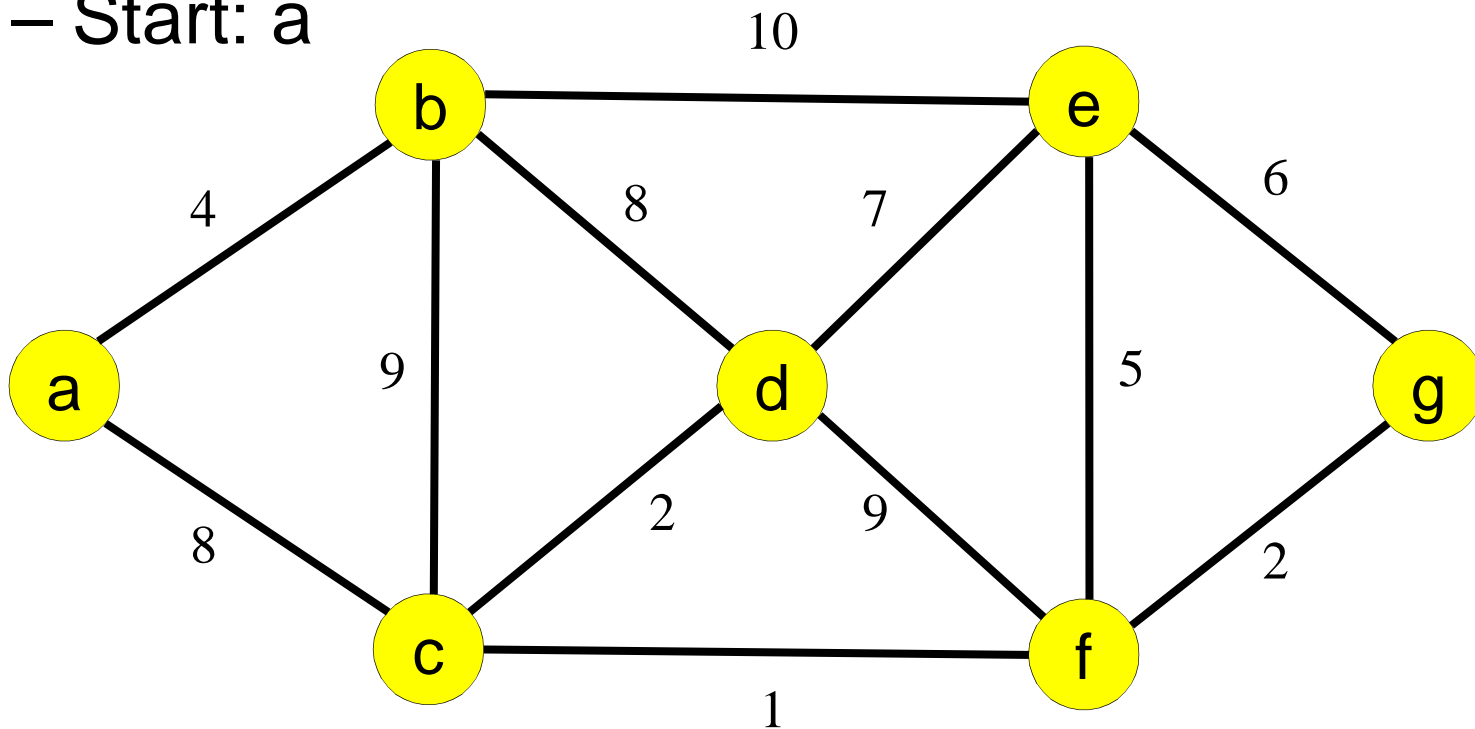
# Graph Problems

- Traveling salesman
- Graph coloring
- Knapsack
- N-Queens

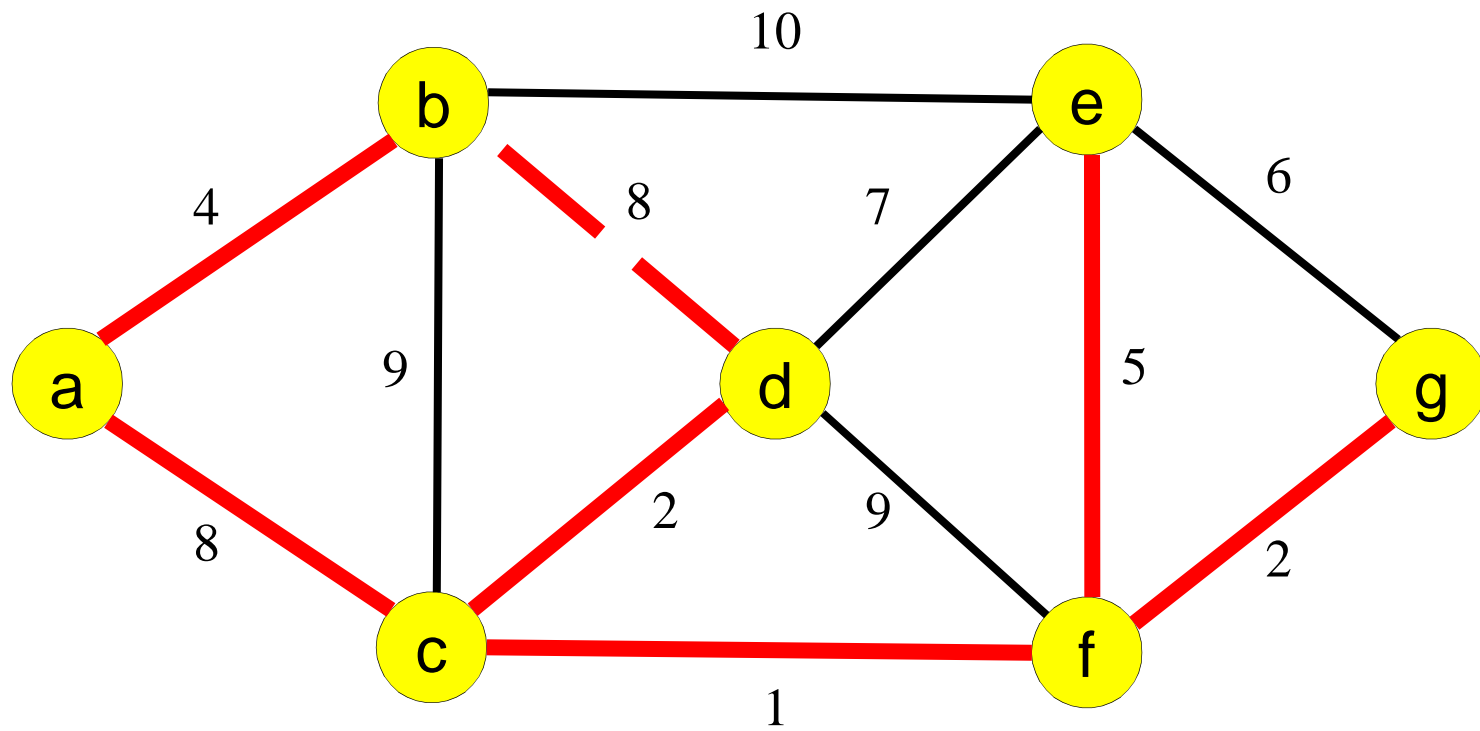


# MSTs

- Do Prim's and Kruskal's on this graph
  - Start: a



# MSTs



# Prim's Algorithm

Repeat until every  $k_v$  is true:

1. From the set of vertices for which  $k_v$  is false, select the vertex  $v$  having the smallest tentative distance  $d_v$
  2. Set  $k_v$  to true
  3. For each vertex  $w$  adjacent to  $v$  for which  $k_w$  is false, test whether  $d_w$  is greater than  $d_v$ . If it is, set  $d_w$  to  $d_v$  and set  $p_w$  to  $v$ .
- $O(V^2)$  or  $O(E \log V)$  with heaps

# Kruskal's Algorithm

- Greedy MST algorithm for edge-weighted, connected, *undirected* graph
  - Presort all edges:  $O(E \log E) = O(E \log V)$  time
  - Try inserting in order of increasing weight
  - Some edges will be discarded so as not to create cycles
- Initial two edges may be disjoint
  - We are growing a forest (union of disjoint trees)

# Dijkstra's Algorithm

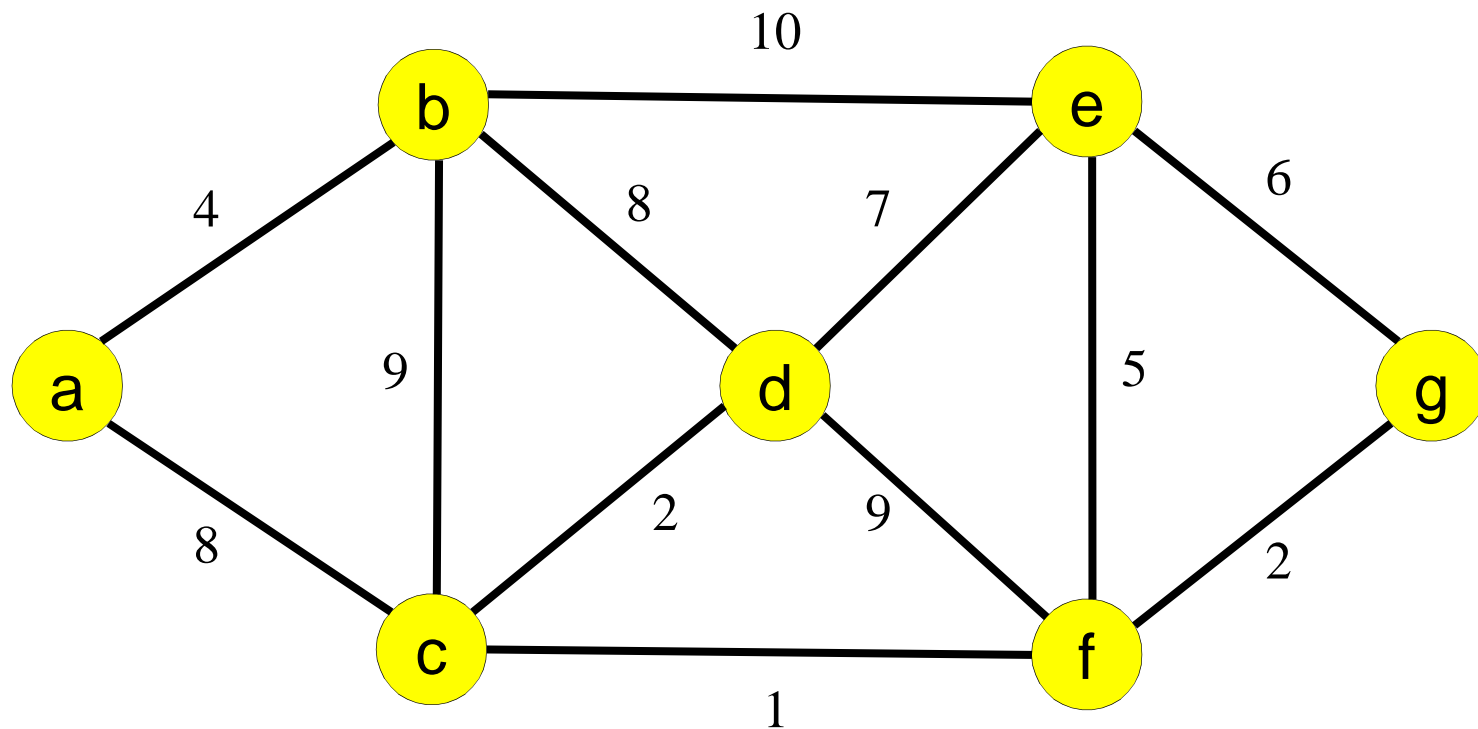
- Greedy algorithm for solving shortest path problem
- Assume non-negative weights
- Find shortest path from  $v_s$  to each other vertex

# Dijkstra's Algorithm

- For each vertex  $v$ , need to know:
  - $k_v$ : Is the shortest path from  $v_s$  to  $v$  known? (initially false for all  $v \in V$ )
  - $d_v$ : What is the length of the shortest path from  $v_s$  to  $v$ ? (initially  $\infty$  for all  $v \in V$ , except  $v_s = 0$ )
  - $p_v$ : What vertex precedes (is parent of)  $v$  on the shortest path from  $v_s$  to  $v$ ? (initially unknown for all  $v \in V$ )
- $O(V^2)$ , or  $O(E \log V)$  with heaps

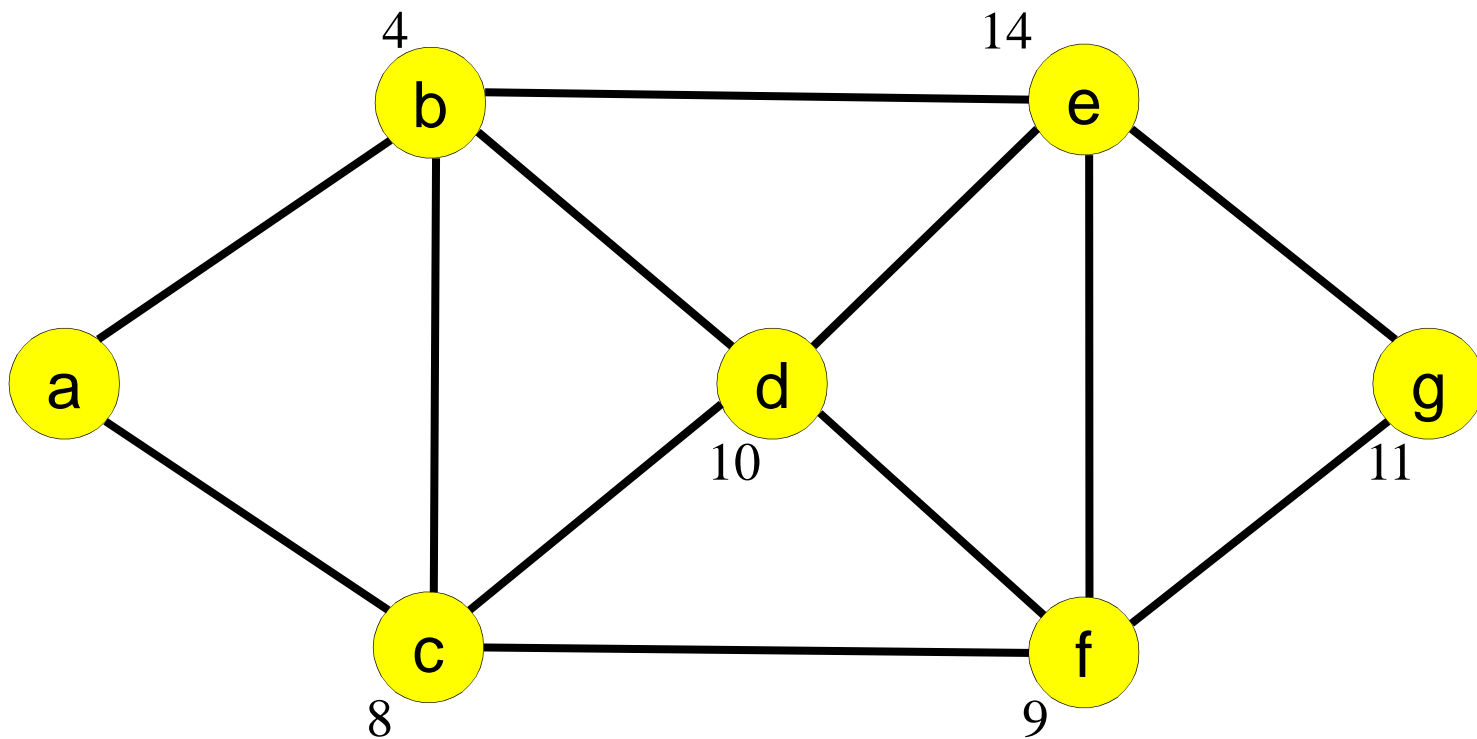
# Shortest Path

- Do Dijkstra's algorithm starting at node a



# Shortest Path

- $V_s = a$





# Algorithm Families

# Algorithm Families

- Brute-Force
- Greedy
- Divide and Conquer
- Dynamic Programming
- Backtracking
- Branch and Bound

# Algorithm Families

- Brute force
  - “Simple” straight-forward way
  - Usually inefficient
- Greedy
  - Decisions never reconsidered
  - Are never optimal?

# Algorithm Families

- Brute force
  - “Simple” straight-forward way
  - Usually inefficient
- Greedy
  - Decisions never reconsidered
  - Are never optimal? -- FALSE, e.g. fractional knapsack

# Algorithm Families

- Divide and conquer
  - Divide in 2 or more sub-problems
  - Non-overlapping sub-problems
  - Usually recursive
- Dynamic programming
  - Divide into multiple overlapping sub-problems
  - Remember partial solutions and reuse
  - “Memoization”

# Algorithm Families

- Backtracking
  - Systematically check all possible solutions
  - Prune those that don't satisfy constraints
  - Stop when constraints are satisfied
- Branch and bound
  - For optimization problems, e.g., best solution
  - Can't stop early

# Dynamic Programming

- Write two versions of this function, using top-down and bottom-up DP
- What family best describes the implementation below?

```
1 // returns the nth Fibonacci number
2 long long fib(int n) {
3     if (n <= 0) return 0;
4     if (n <= 1) return 1;
5     return fib(n - 1) + fib(n - 2);
6 }
```

# Dynamic Programming

- What family best describes the implementation below?
  - Divide and conquer

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# Top-down Solution

```
1 long long fib(int n) {  
2     static unordered_map<int, long long> computed;  
3  
4     // base cases  
5     if (n <= 0) return 0;  
6     if (n == 1) return 1;  
7  
8     // look up  
9     auto found = computed.find(n);  
10    if (found != computed.end()) return found->second;  
11  
12    // compute  
13    computed[n] = fib(n - 1) + fib(n - 2);  
14    return computed[n];  
15 }
```

# Bottom-up solution

```
1  long long fib(int n) {
2      long long fib_prev = 0;
3      long long fib_cur = 1;
4      for (int i = 0; i < n - 1; ++i) {
5          long long tmp = fib_cur;
6          fib_cur += fib_prev;
7          fib_prev = tmp;
8      }
9
10     return fib_cur;
11 }
```

# What You Have Learned

- At the beginning of the semester
  - You mean we *don't get starter files?!!!*
- At the end of the semester
  - Design, implement, test, debug and optimize your own complex programs
  - Mathematically analyze code complexity and compare different design choices
- You've come a long way!

# What's Next

- (Almost) all the upper level CS courses!
  - 388 Introduction to Computer Security, 442 Computer Vision, 445 Introduction to Machine Learning, 467 Autonomous Robotics, 475 Introduction to Cryptography, 477 Introduction to Algorithms, 478 Logic Circuit Synthesis and Optimization, 480 Logic and Formal Verification , 481 Software Engineering , 482 Introduction to Operating Systems, 483 Compiler Construction, 484 Database Management Systems, 485 Web Database and Information Systems, 487 Interactive Computer Graphics , 489 Computer Networks, 490 Programming Languages, 492 Introduction to Artificial Intelligence, 493 User Interface Development, 494 Computer Game Design and Development
- EECS 381
  - Advanced C++
  - Object-oriented programming
- Learning on your own
  - Evaluate libraries written by others (e.g., Boost) and decide when to borrow, and when to “roll your own”

Thank you!