## Lecture 7 Stacks and Queues

EECS 281: Data Structures & Algorithms

#### The Stack Container

Supports insertion/removal in LIFO order

Method	Description	
push(object)	Add object to top of the stack	
pop()	Remove top element	
object ⊤()	Return a reference to top element	
size()	Number of elements in stack	
empty()	Checks if stack has no elements	

#### Examples

- Web browser's "back" feature
- Text editor's "Undo" feature
- Function calls in C++

## Stack Example: Web Browsing

- 1. Open Browser to <a href="http://www.google.com">http://www.google.com</a>
- 2. Search for "STL"
- 3. Go to SGI STL Guide
- 4. Click on the Table of Contents
- 5. Go to the stack page
- 6. Go back to the Table of Contents
- 7. Go to the basic\_string page
- 8. Finished, close browser

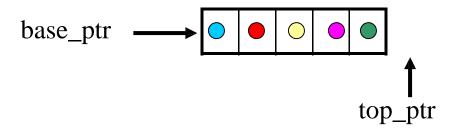
STL Stacks, Strings
Table of Contents
SGI STL Guide
Search Results: STL
Google Homepage

**URL Stack** 

Should we use arrays or linked lists to implement stacks?

## Stacks Using Arrays

Keep a pointer (top\_ptr) to the last element of array

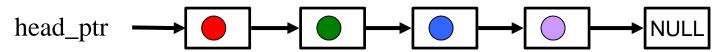


Method	Implementation	
push(object)	Add new element at, and then increment top_ptr	
	Allocate more space if necessary (requires copying)	
pop()	Decrement top_ptr.	
object ⊤()	Dereference top_ptr - 1.	
size()	Subtract base_ptr from top_ptr pointer.	
empty()	Are base_ptr and top_ptr equal?	

What is the asymptotic runtime of each method?

## Stacks Using Linked Lists

Singly-linked is sufficient



Method	Implementation
push(object)	Prepend node to list
pop()	Delete head node of list
object ⊤()	Return reference to data in head node
size()	Use existing LinkedList::size() method
	Be careful: size() in STL <slist> takes O(n) time</slist>
	(it computes size from scratch every time)
empty()	Use existing LinkedList::empty() method

What is the asymptotic runtime of each method?

Is an array or linked list more efficient for stacks?

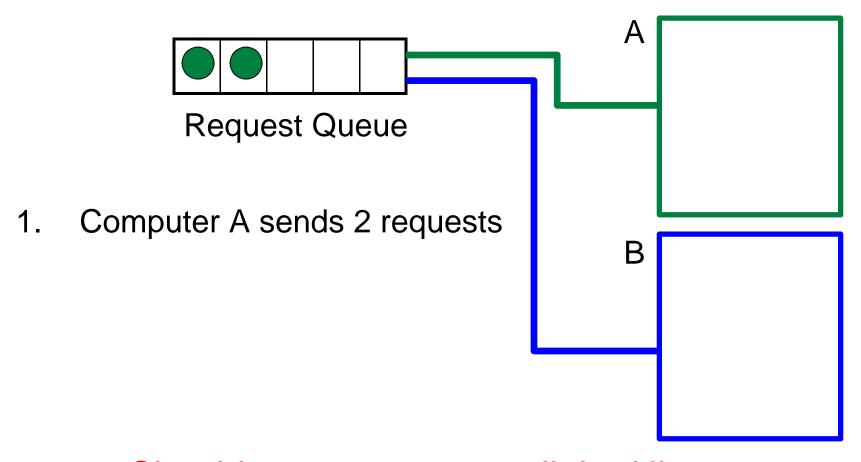
### The Queue Container

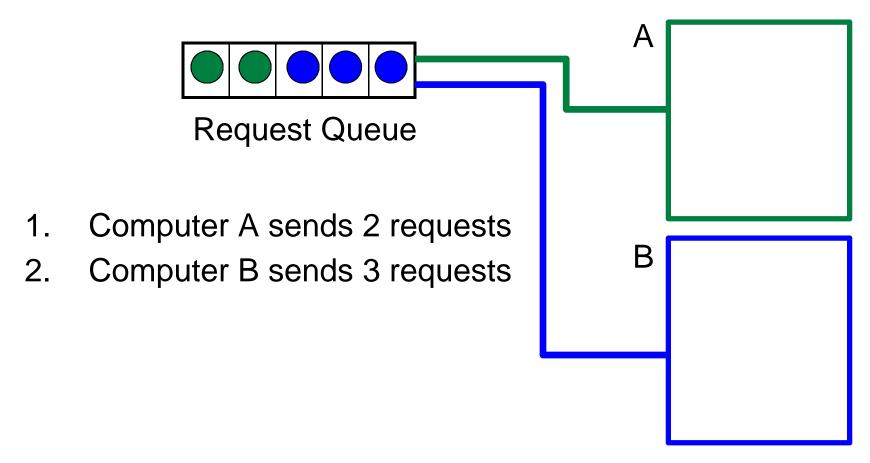
Supports insertion/removal in FIFO order

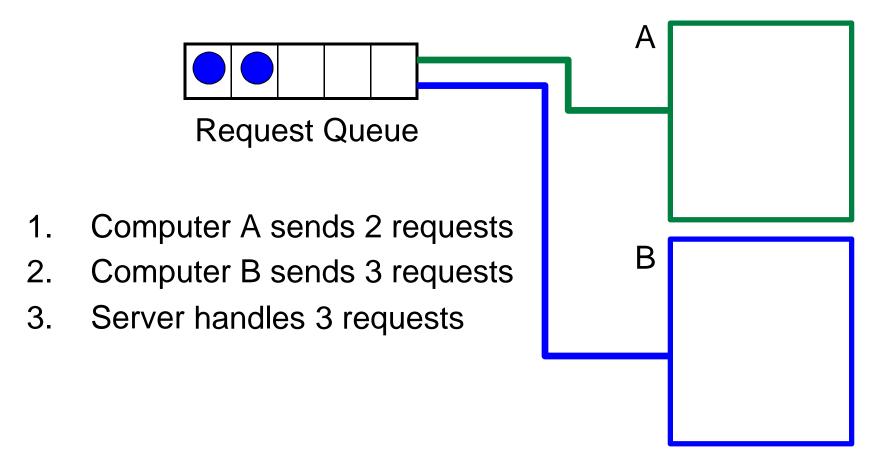
Method	Description
push(object)	Add element to back of queue
pop()	Remove element at front of queue
object &front()	Return reference to element at front of the queue
size()	Number of elements in queue
empty()	Checks if queue has no elements

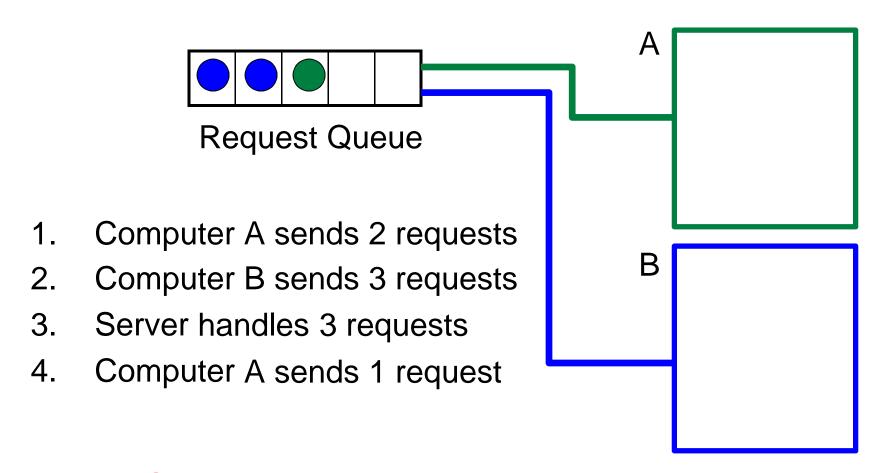
# Queue Example: Web Browsing History

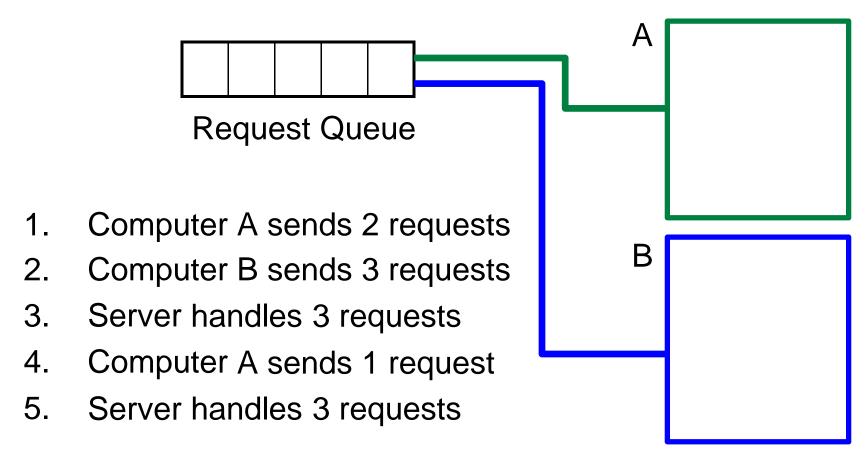
- The history starts empty
- New pages are added to history on the "today" end
- Old pages are removed from history on the "30 days ago" end
- This particular kind of queue (unlike STL queue) allows iterating through elements

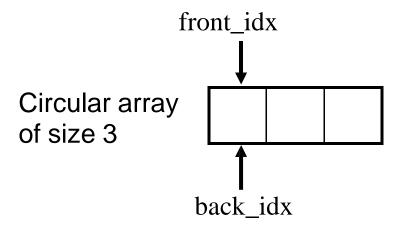






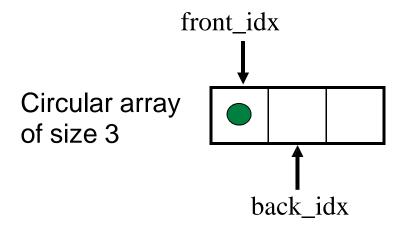






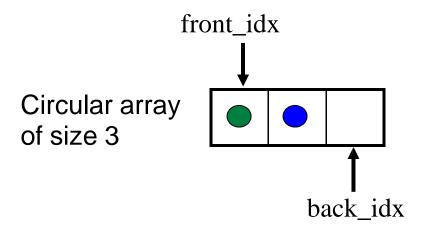
#### **Event Sequence**

1. back\_idx == front\_idx since array is empty



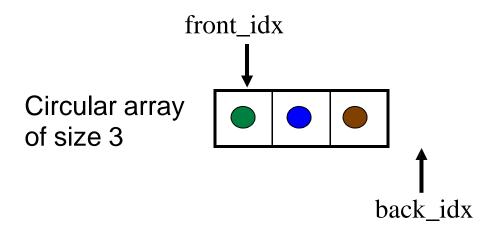
#### **Event Sequence**

- back\_idx == front\_idx
   since array is empty
- 2. enqueue element



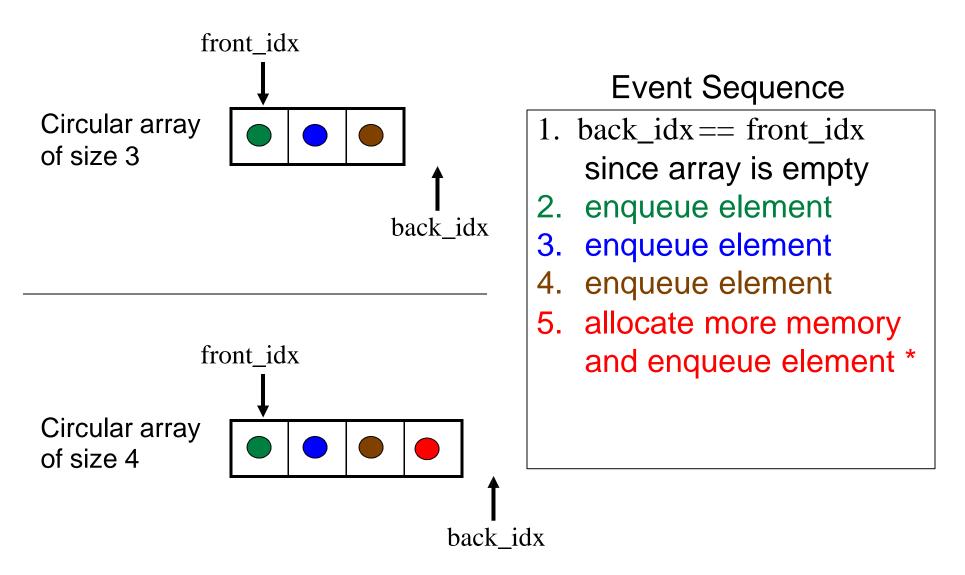
#### **Event Sequence**

- 1. back\_idx == front\_idx since array is empty
- 2. enqueue element
- 3. enqueue element

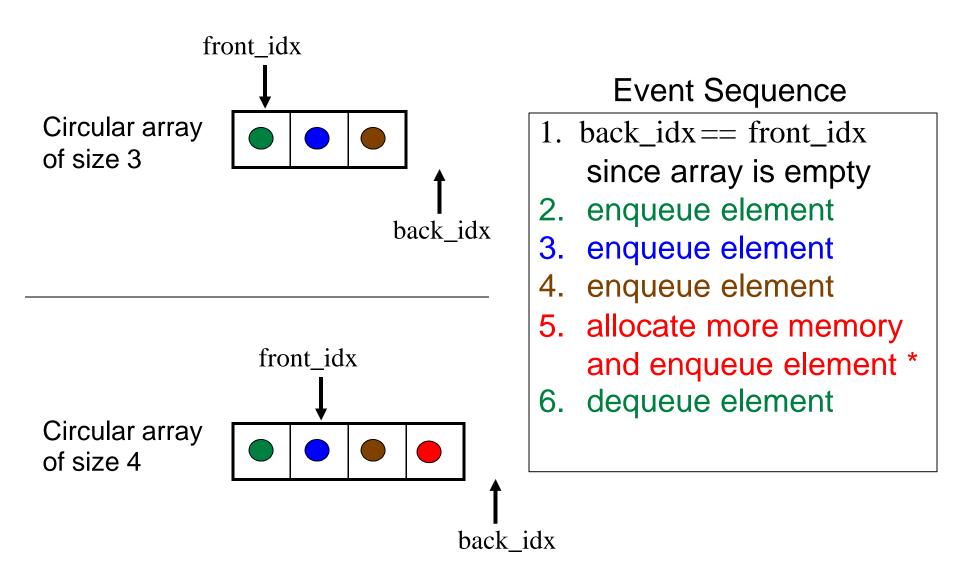


#### **Event Sequence**

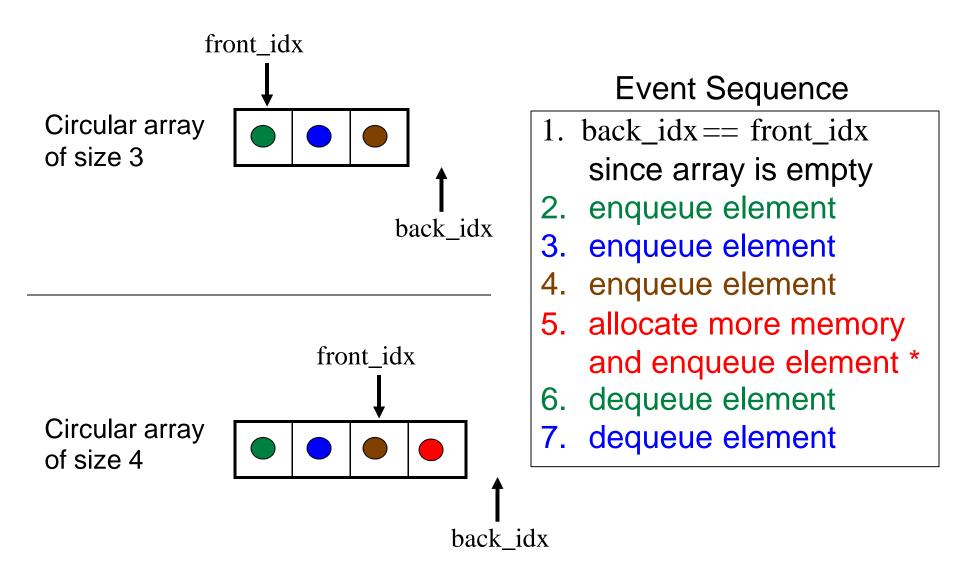
- back\_idx == front\_idx
   since array is empty
- 2. enqueue element
- 3. enqueue element
- 4. enqueue element



<sup>\*</sup> When allocating more memory, it is more common to double memory



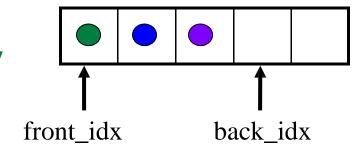
<sup>\*</sup> When allocating more memory, it is more common to double memory



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### Queues Using Arrays

Use a circular array

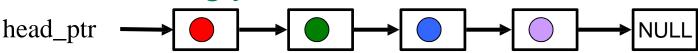


Method	Implementation
enqueue(object)	Increment back_idx, wrapping to front when end of allocated space is reached  If back_idx becomes front_idx, reallocate array and unroll
dequeue()	Delete item at front_idx and increment front_idx
object &front()	Return reference to element at front_idx
size()	<pre>If (back_idx &gt;= front_idx) returns back_idx - front_idx else returns array_size + back_idx - front_idx</pre>
empty()	returns back_idx == front_idx

What is the asymptotic runtime of each method?

### Queues Using Linked Lists

#### Singly-linked is sufficient



Method	Implementation
push(object)	Append node to list
pop()	Delete head node of list
object &front()	Return reference to data in head node
size()	Use existing LinkedList::size() method
	Be careful: size() in STL <slist> takes O(n) time (computes size from scratch every time)</slist>
empty()	Use existing LinkedList::empty() method

What is the asymptotic runtime of each method?

Is an array or linked list more efficient for queues?

## Deque: a Queue and Stack in One (Double-ended Queue)

- Pronounced "deck"
- ADT that allows efficient insertion and removal from the front and the back
- 6 major methods

```
push_front(), pop_front(), front()push_back(), pop_back(), back()
```

- Minor methods
  - size(), empty()
- Can traverse using iterator

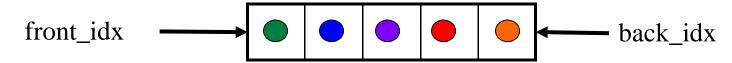
What's another pseudo-word invented to name a data structure?

Trie (pronounced "try"): a digital search tree

## Deque Implementation

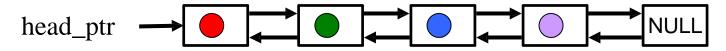
#### Circular Array

front\_idx and back\_idx both get incremented/decremented



#### Doubly-linked list

- Singly-linked doesn't support efficient removal
- Other operations map directly to doubly-linked list operations



See details in STL header <deque> for another implementation

### What is a Priority Queue?

- Each datum paired with a priority value
  - Priority values are usually numbers
  - Should be able to compare priority values (<)</li>
- Supports insertion of data and inspection
- Supports removal of datum with highest priority
  - Largest determined by given ordering

Like a group of bikers where the fastest ones exit the race first

What applications may benefit from a priority queue?

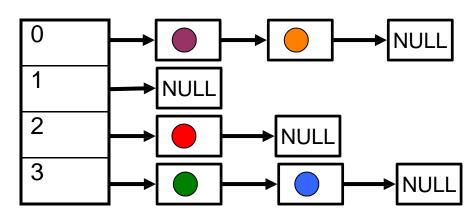
### Priority Queue Implementation

STL maintains a heap on top of any random access container you choose

	Insert	Remove Max
Unsorted sequence container	O(1)	O(n)
Sorted sequence container	O(n)	O(1)
Heap (covered in future lecture)	O(log n)	O(log n)
Array of linked lists	O(1)	O(1)
(for priorities of small integers)		

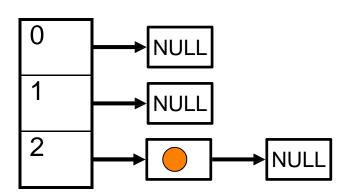
#### Array of Linked Lists

Priority value used as index value in array



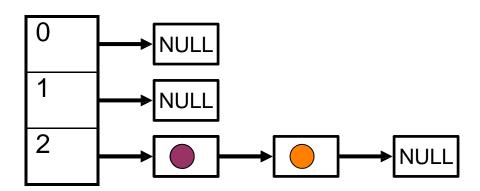
- Operators receive calls and assign levels of urgency
- Lower numbers indicate more urgent calls
- Calls are dispatched (or not dispatched) by computer to police squads based on urgency

#### 1. Level 2 call comes in



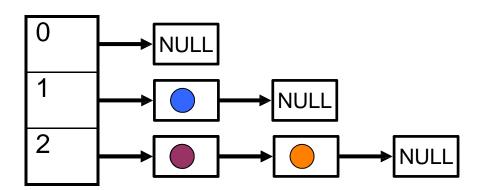
- Operators receive calls and assign levels of urgency
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- 1. Level 2 call comes in
- 2. Level 2 call comes in



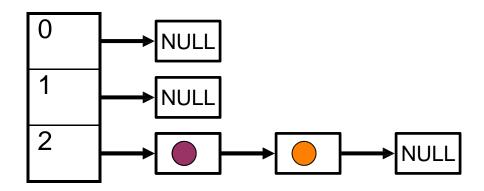
- Operators receive calls and assign levels of urgency
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- 1. Level 2 call comes in
- 2. Level 2 call comes in
- 3. Level 1 call comes in



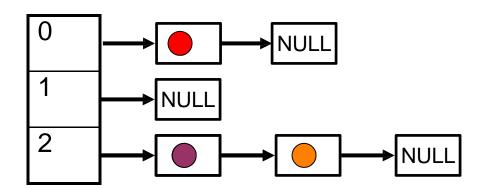
- Operators receive calls and assign levels of urgency
- Lower numbers indicate more urgent calls
- Calls are dispatched (or not dispatched) by computer to police squads based on urgency

- 1. Level 2 call comes in
- 2. Level 2 call comes in
- 3. Level 1 call comes in
- 4. A call is dispatched



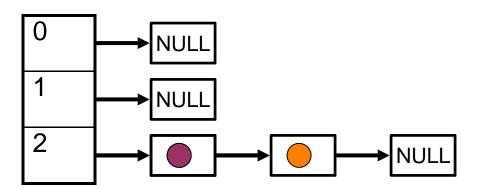
- Operators receive calls and assign levels of urgency
- Lower numbers indicate more urgent calls
- Calls are dispatched (or not dispatched) by computer to police squads based on urgency

- 1. Level 2 call comes in
- 2. Level 2 call comes in
- 3. Level 1 call comes in
- 4. A call is dispatched
- 5. Level 0 call comes in



- Operators receive calls and assign levels of urgency
- Lower numbers indicate more urgent calls
- Calls are dispatched (or not dispatched) by computer to police squads based on urgency

- 1. Level 2 call comes in
- 2. Level 2 call comes in
- 3. Level 1 call comes in
- 4. A call is dispatched
- 5. Level 0 call comes in
- 6. A call is dispatched



#### Stacks and Queues in STL

- You can choose the underlying container
- All operations are implemented generically on top of the given container
  - No specialized code based on given container

	Stack	Queue
Default Underlying Container	std::deque	std::deque
Optional Underlying Container	std::list	std::list
	std::vector	

Note: std::list is not the same as std::slist

## Choosing a Data Structure for a Given Application

- What to look for
  - The right operations (e.g., add\_elt, remove\_elt)
  - The right behavior (e.g., push\_back, pop\_back)
  - The right trade-offs for runtime complexities (empirical data will be shown soon)
  - Memory overhead
- Potential concern
  - Limiting interface to avoid problems (e.g., no insert\_mid)
- Examples
  - Order tracking at a fast-food drive-through (pipeline)
  - Interrupted phone calls to a receptionist
  - Your TODO list

## Data Structure Engineering

- Exercise 1
  - Given a stack class (e.g., from STL)
  - Build a MinStack class with the same
     Big-O complexities, and an additional getMin() function that runs in O(1) time
  - Note: all Big-O are worst-case
- Exercise 2
  - Same for a MinQueue

## Algorithm Engineering: Juggling with Stacks and Queues

- Task: for a given N generate all N-element permutations
- Ingredients of a solution
  - One recursive function
  - One stack
  - One queue
- Technique: moving elements between the two containers

#### Implementation: Helper Function

```
template <typename T>
   ostream & operator << (ostream & out, const
                                                 stack < T > & s 
     // print the contents of a stack on a single line
     // e.g., cout << mystack << endl;
5
      stack<T> tmpStack = s; // deep copy
      while (!tmpStack.empty()) {
        out << tmpStack.top() << '';</pre>
8
        tmpStack.pop();
9
      } // while
10
     return out;
    } // operator<<()
```

## Implementation

```
template <typename T>
   void genPerms(queue<T> &q, stack<T> &s) {
     // s: prefix of permutation, q: everything
                                                      else
      unsigned size = q.size();
5
      if (q.empty()) {
6
        cout \ll \leq \leq '\n';
        return:
8
      } // if
9
      for (unsigned k = 0; k != size; k++) {
10
        s.push(q.front());
11
        q.pop(); genPerms(q,
12
        s); q.push(s.top());
13
        s.pop();
14 } // for
15 } // genPerms()
16
```

#### Better Helper Function

```
template <typename T>
ostream &operator<<(ostream &out, const vector<T> &s)

// printthe contents of a vector on a single line
// e.g.,cout << myvector << endl;
for (auto &el: s)
   out << el << '';

return out;
} // operator<<()</pre>
```

## Better Implementation

```
template <typename T>
   void genPerms(deque<T> &q, vector<T> &s) {
     // s: prefix of permutation, q: everything
                                                      else
      unsigned size = q.size();
5
      if (q.empty()) {
6
        cout \ll \leq \leq '\n';
        return:
8
      } // if
9
      for (unsigned k = 0; k != size; k++) {
10
        s.push_back(q.front());
11
        q.pop_front(); genPerms(q,
12
        s); q.push_back(s.back());
13
        s.pop_back();
14 } // for
15 } // genPerms()
16
```

## Implementation: Sample Driver

```
int main() {
      unsigned n;
3
      string junk;
      cout << "Enter n: " << flush;
5
      while (!(cin \gg n)) {
        cin.clear(); getline(cin,
        junk);
8
        cout << "Enter n: " << flush;
9
      } // while
10
11
     vector<unsigned> s;
12
      deque<unsigned> q(n);
13
      iota(q.begin(), q.end(),
                                  1);
   genPerms(q, s);
14
     return 0;
15
16 } // main()
```

## Implement to Test

 Q: how does the recursive permutation enumerator compare to STL's function next\_permutation()?

http://en.cppreference.com/w/cpp/algorithm/next\_permutation

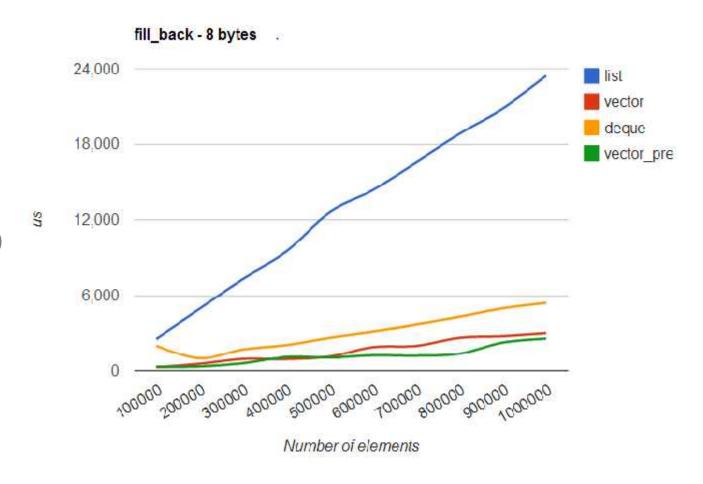
- A: each method has its advantages and can be more appropriate in some situations
- Interview brainteaser
  - You are given four digits: 3 3 8 8 (can reorder)
  - Can use any combination of +, -, \* and / (no power/exp, no concatenation)
  - Find a way to express 24
  - Examples: 22=3+3+8+8, 23=(8-3)\*3+8, 25=(8-3)\*(8-3)

# Relative Performance of STL Containers (1)

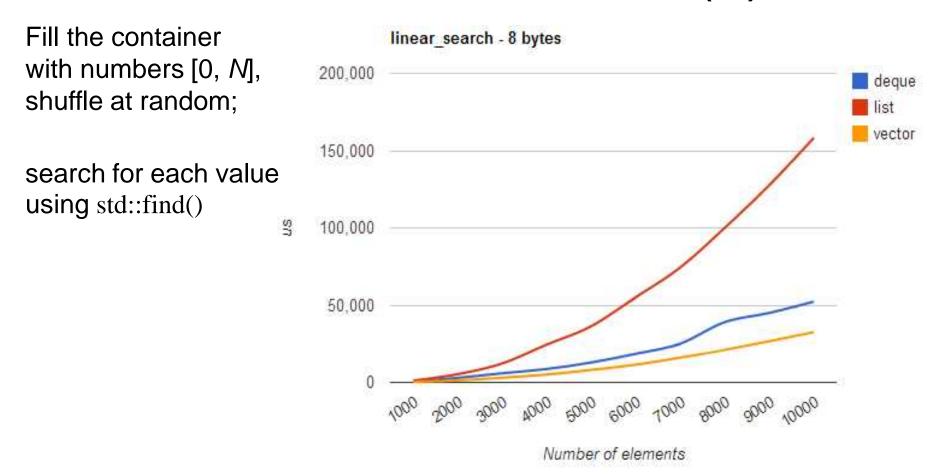
Filling an empty container with different values

vector\_pre used
vector::resize()
(a single allocation)

Intel Core i7 Q820 <u>@1.73GHz</u> GCC 4.7.2 (64b) -02 -std=c++11 -march=native



# Relative Performance of STL Containers (2)

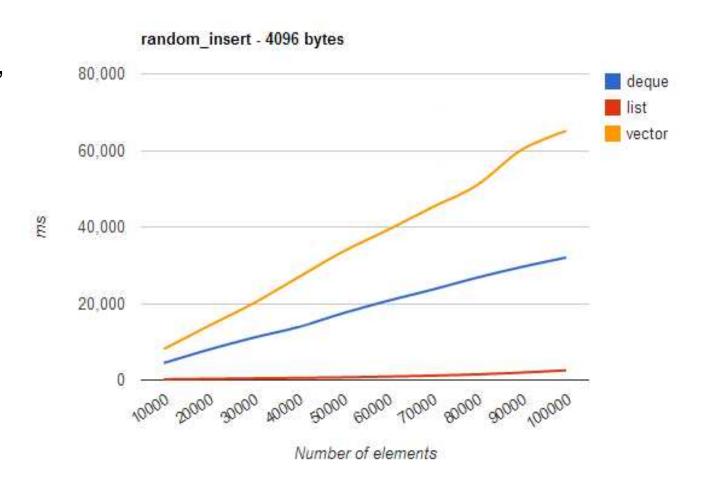


# Relative Performance of STL Containers (3)

Fill the container with numbers [0, N], shuffle at random;

Pick a random position by linear search

Insert 1000 values

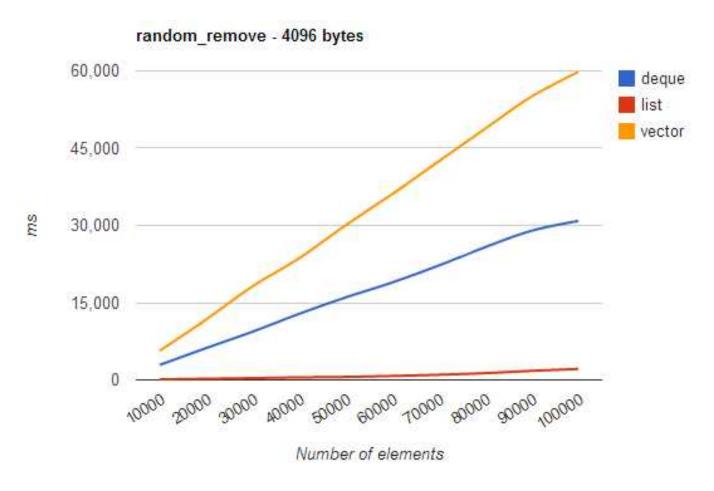


# Relative Performance of STL Containers (4)

Fill the container with numbers [0, N], shuffle at random;

Pick a random position by linear search

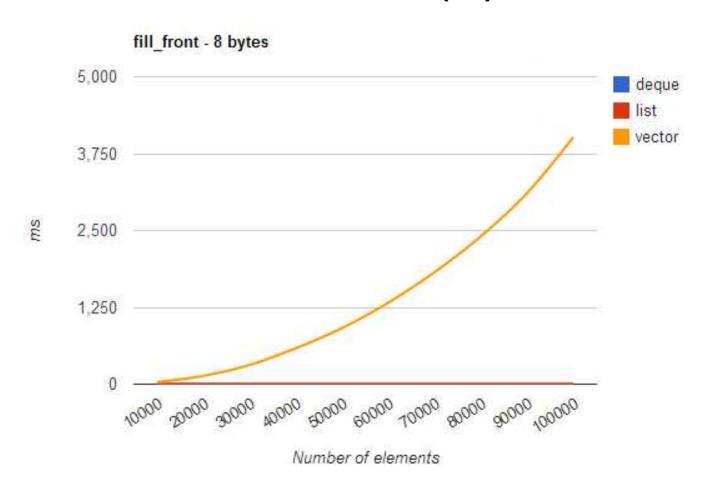
Remove 1000 elements



# Relative Performance of STL Containers (5)

Insert new values at the front

A vector needs to move all prior elts, but a list does not



## What to study?

- What is an ADT?
- Define the following:
  - Stack
  - Queue
  - Deque
  - Priority queue
- How would you implement each ADT above?
- Compare the performance of vector, deque and list classes based on their implementation
- Describe several applications where one data structure would be more relevant than another