

# SOLUTIONS

## CSC 384 Winter 2023 Test 2 Version B

February 13 and 14, 2023

Last Name: \_\_\_\_\_

First Name: \_\_\_\_\_

Email: \_\_\_\_\_

**Q1 (4 marks)**

**Q1.1 (1 mark)** Which is a **multiplayer** game? Circle the best answer.

- A. 8-puzzle
- B. Rubik's cube
- ☒ C. Chess

**Q1.2 (1 mark)** Which is a **stochastic** game? Circle the best answer.

- ☒ A. Monopoly
- B. Checkers
- C. Tic Tac Toe

**Q1.3 (1 mark)** Which is an **imperfect-information** game? Circle the best answer.

- A. Checkers
- B. Go
- ☒ C. Poker

**Q1.4 (1 mark)** Consider the game below. Player A has two actions: Up and Down. Player B has two actions: Left and Right. In each cell, the two numbers specify player A's and B's utility, respectively. For example, if player A chooses Up and player B chooses Right, player A gets a utility of 5, and player B gets a utility of 4.

		Player B	
		Left	Right
Player A	Up	6, 6	5, 4
	Down	4, 5	6, 6

Is this a **constant-sum** game? YES OR ☒ NO

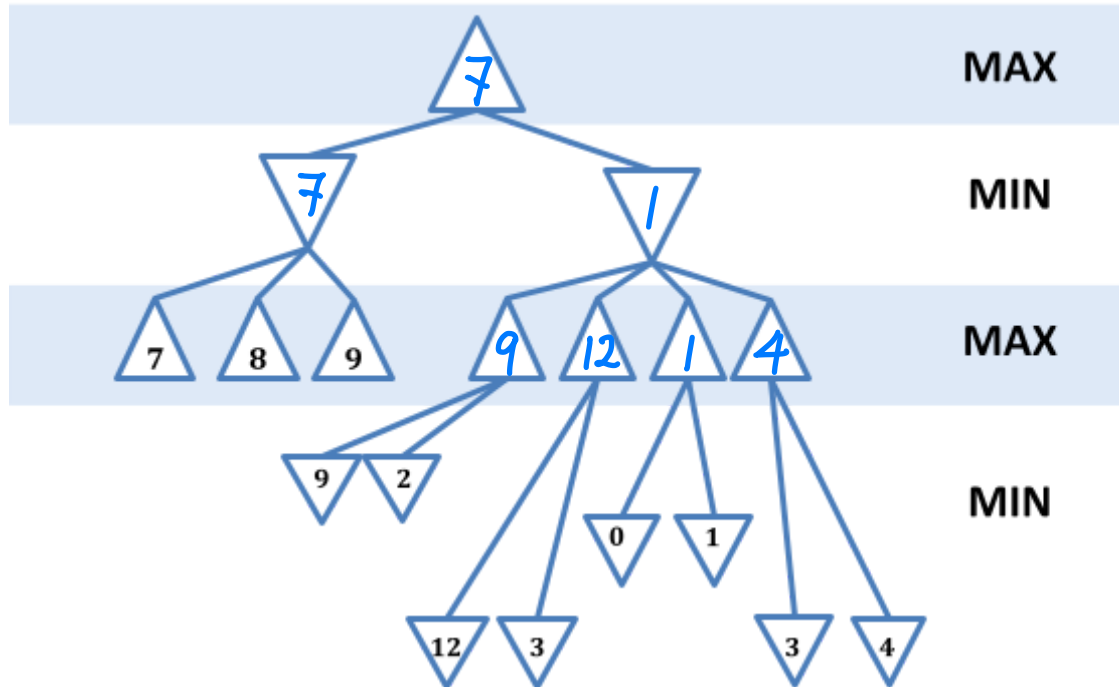
Justify your answer in at most two sentences:

*The total utility of the two players is NOT constant.*

*(up, left)  $6+6=12$       (up, right)  $5+4=9$*

*$12 \neq 9$*

Game Tree 1 Below



**Q2 (4 marks)**

Perform **Minimax search** with **NO Alpha-Beta Pruning** on **Game Tree 1** above.

**Q2.1 (2 marks)** Fill in the minimax value of every node.

**Q2.2 (1 mark)** How will the **results** differ if we used **Depth-First Minimax** instead of regular **Minimax** for Game Tree 1? Explain in one sentence.

*The results will NOT differ.*

**Q2.3 (1 mark)** How will the **performance** differ if we used **Depth-First Minimax** instead of regular **Minimax** for Game Tree 1? Explain in one sentence.

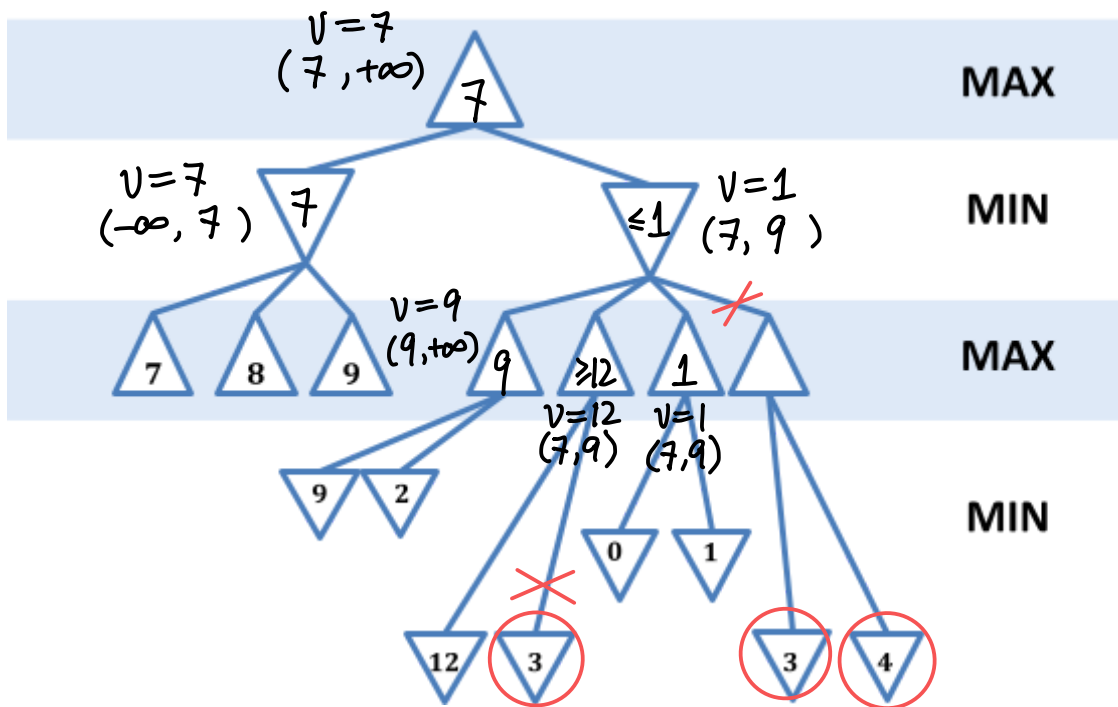
*Depth-First Minimax will use less memory.*

**Q3 (6 marks)**

Consider Game Tree 1 below. Perform **Alpha-Beta Pruning from left to right**.

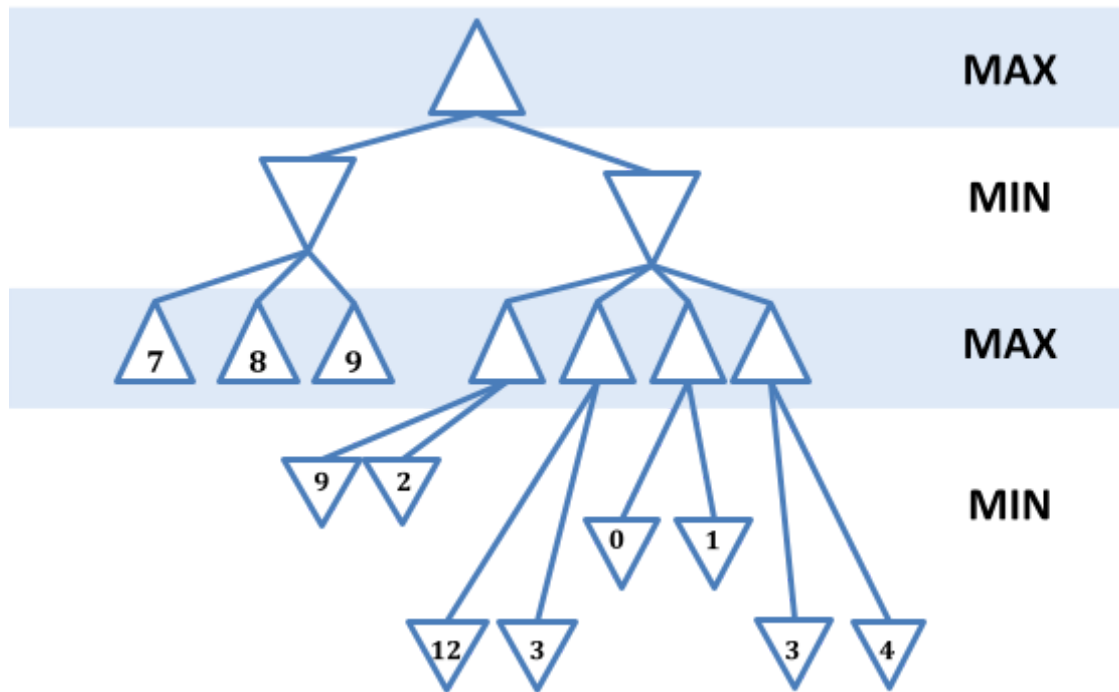
Circle all the **terminal** nodes that are **pruned (NOT visited)**.

**Copy of Game Tree 1 Below**

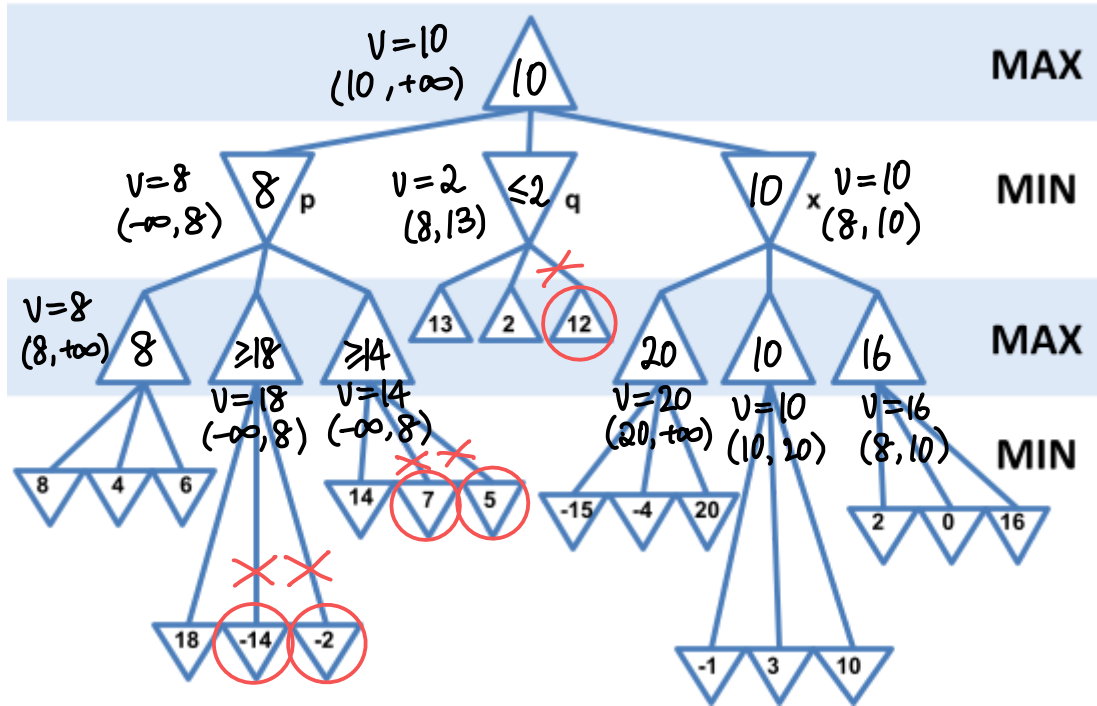


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**Copy of Game Tree 1 Below**



Game Tree 2 Below



**Q4 (8 marks)**

Consider **Game Tree 2** above.

**Q4.1 (6 marks)** Execute **Alpha-Beta Pruning** from **left to right**. Circle all the **terminal** nodes that are **pruned (not visited)**. *(5 terminal nodes pruned.)*

**Q4.2 (2 marks)**

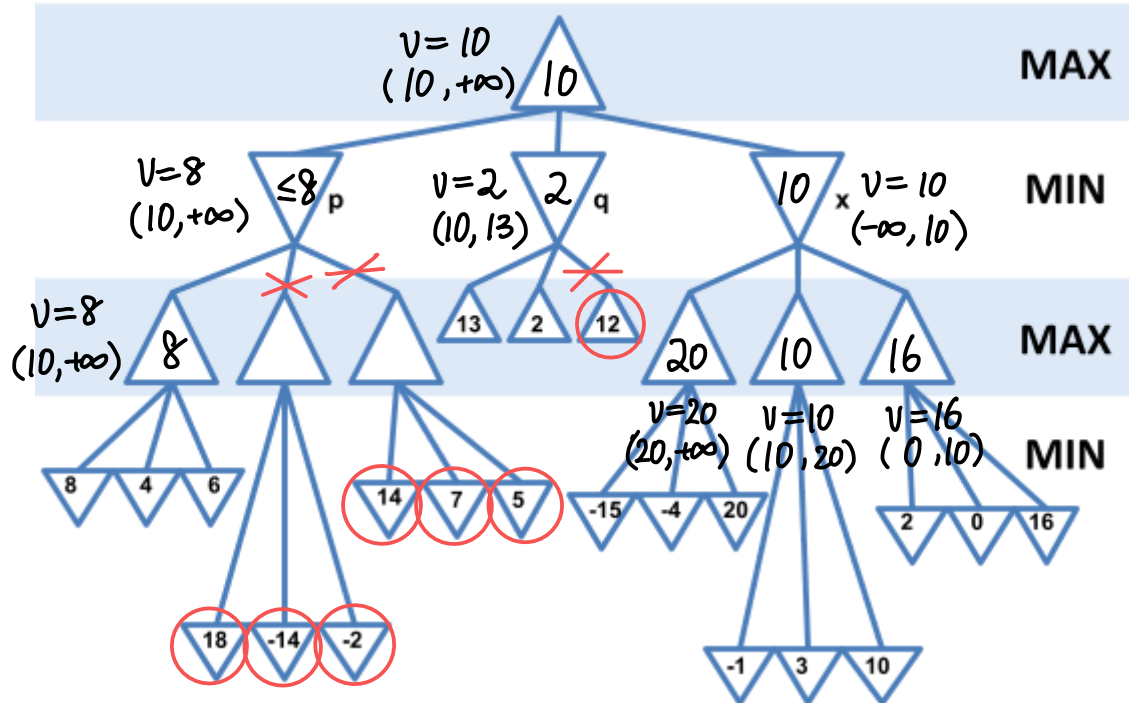
How can we re-order **p, q, and x** to **maximize** the number of terminal nodes pruned by Alpha-Beta Pruning? Write down the new order below. When reordering p, q, and x, the order of their descendants remains the same.

*x, p, q. (8 terminal nodes pruned.)*

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After re-ordering  
to  $x, p, q$ .

Copy of Game Tree 2 Below



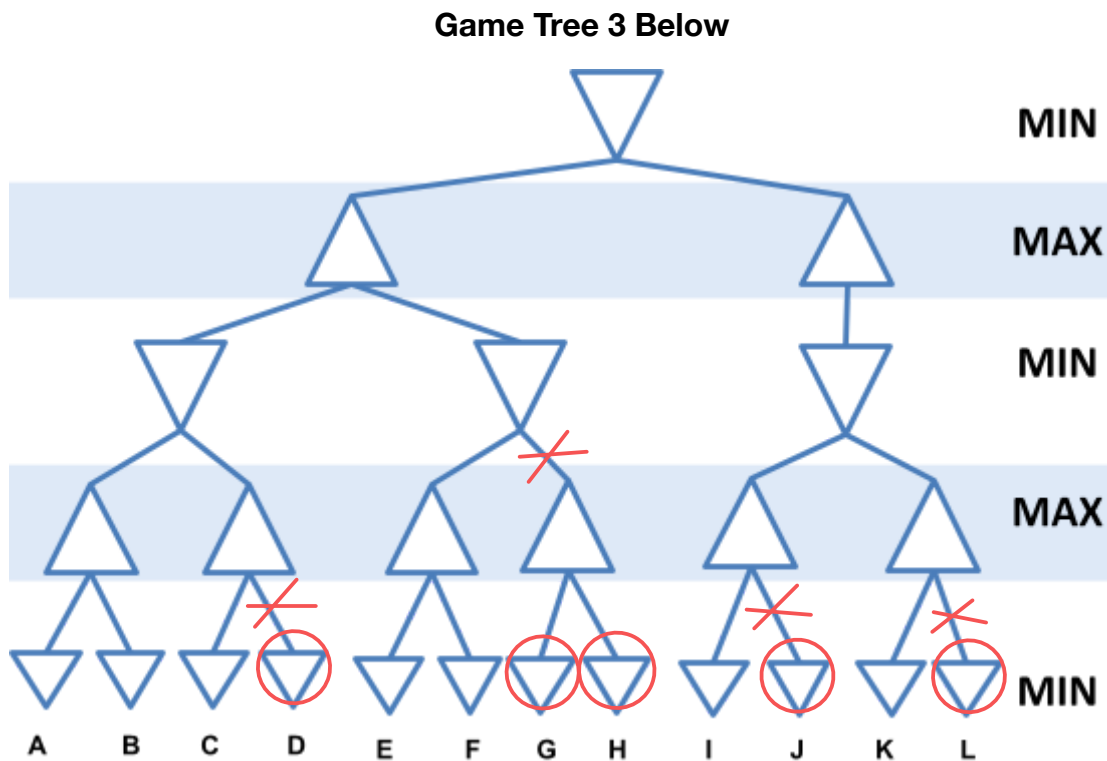
**Q5 (4 marks)**

Consider **Game Tree 3** below. The values of the terminal states are unknown.

You can make the following assumptions:

- All the nodes have been ordered such that **Alpha-Beta Pruning from left to right** will prune the **maximum** number of terminal nodes.
- The utility values of all the terminal nodes are all different.

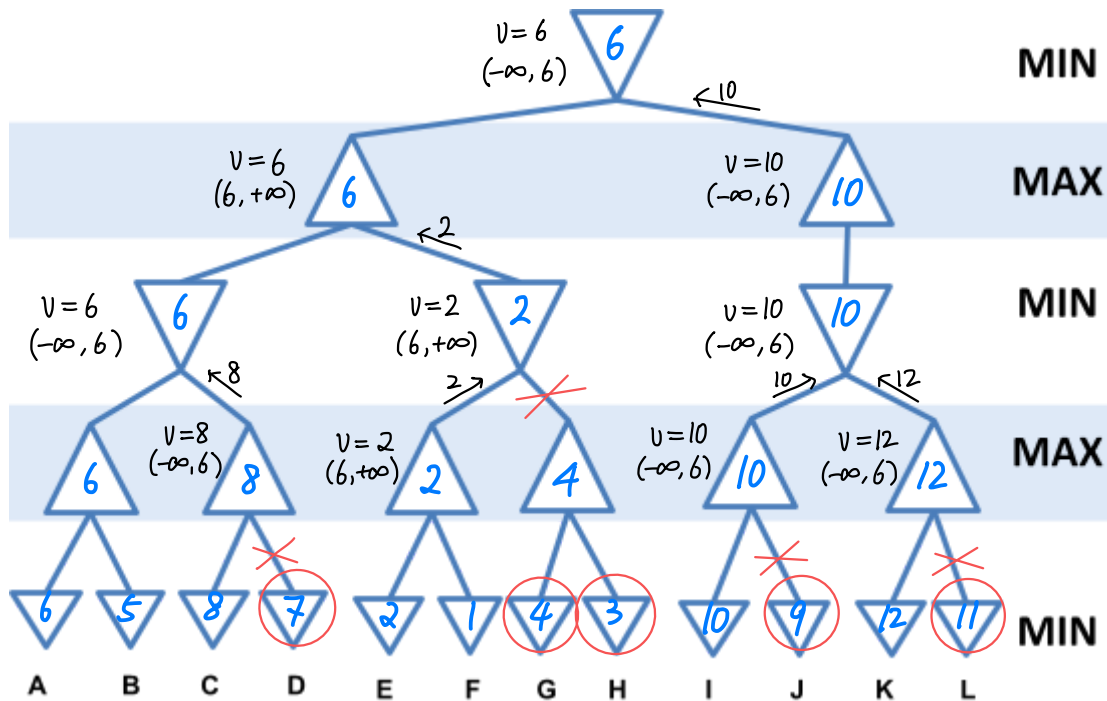
Circle all the **terminal** nodes that will be **pruned (NOT visited)**.





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Copy of Game Tree 3 Below



You can solve this question by trying an example. Assume that the terminal nodes have utilities 1 to 12. Start by assigning the utilities to the terminal nodes arbitrarily. Then, re-order the utility values to maximize pruning. We get the tree above.

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