$G=\{1,g,g^2,\ldots,g^{N-1}\},\quad g^N=1$ Given p, x and g

 $a = \log_g(x \mod p)$

Hard to compute backward

Easy to compute forward

 $x = g^a$

Given a and g