

# Project2 Phase1

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## 一. 安装虚拟机和Ubuntu 18.04 系统

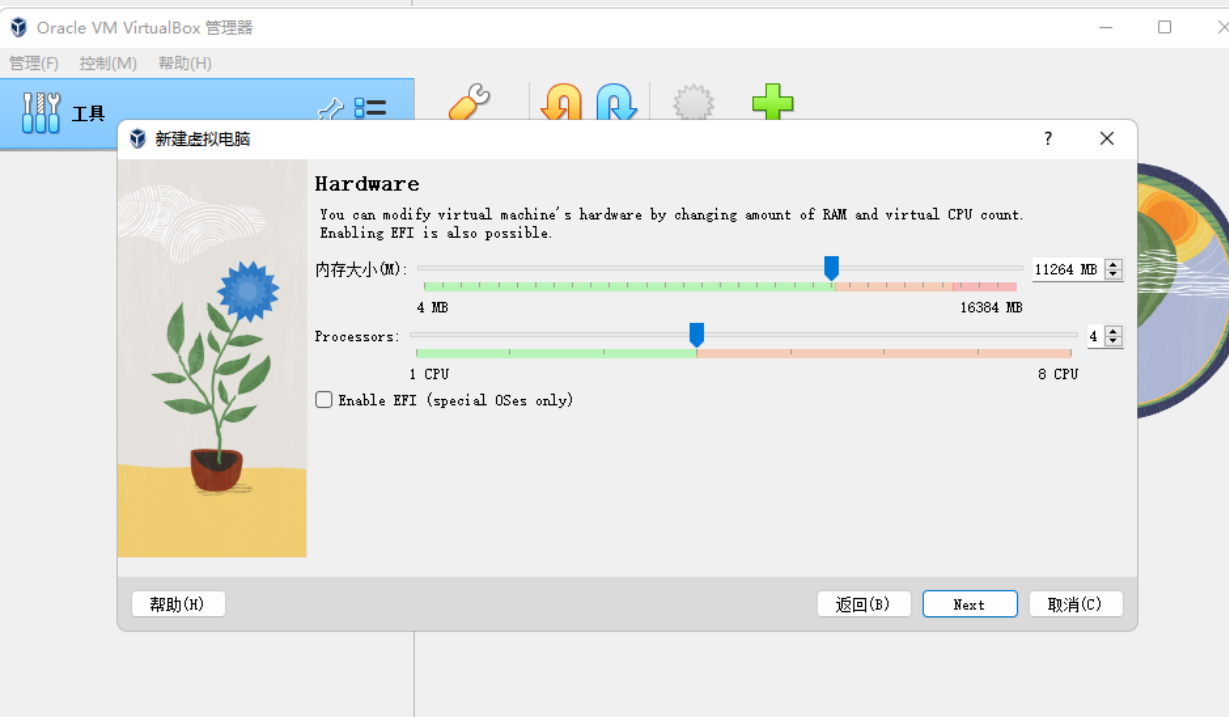
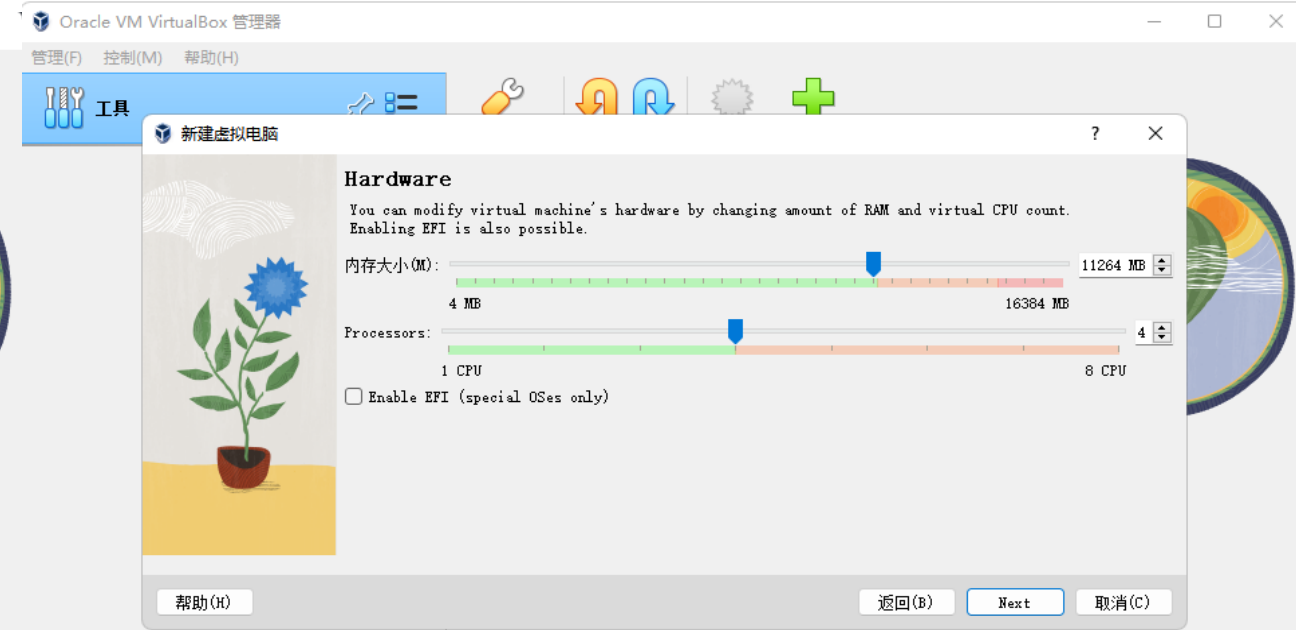
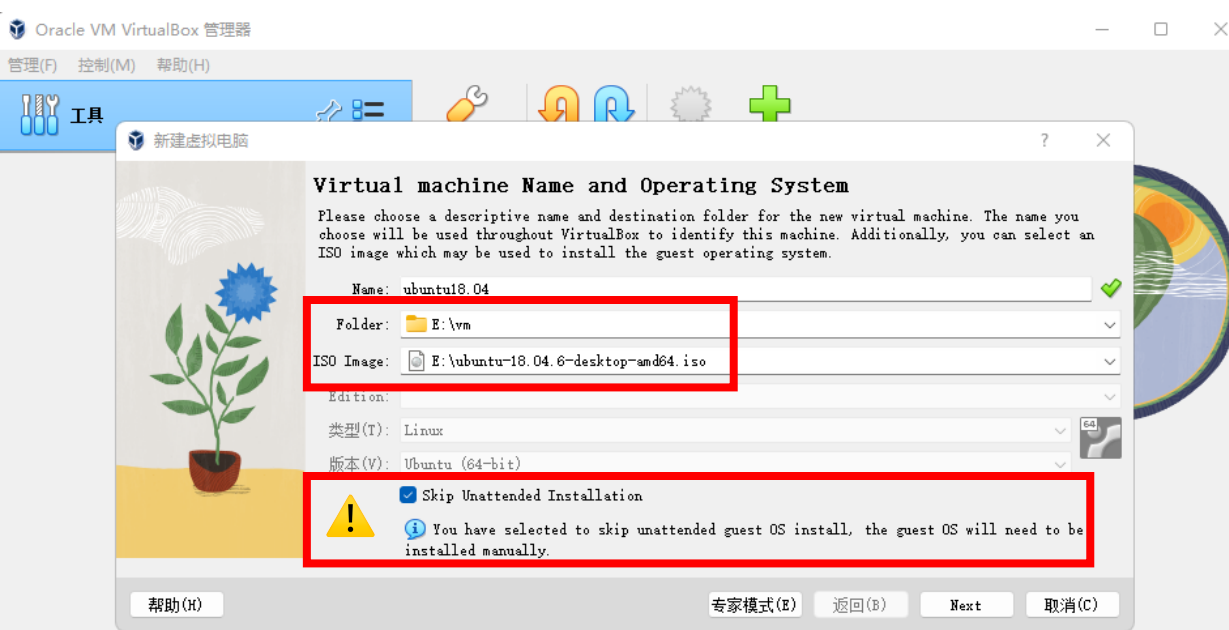


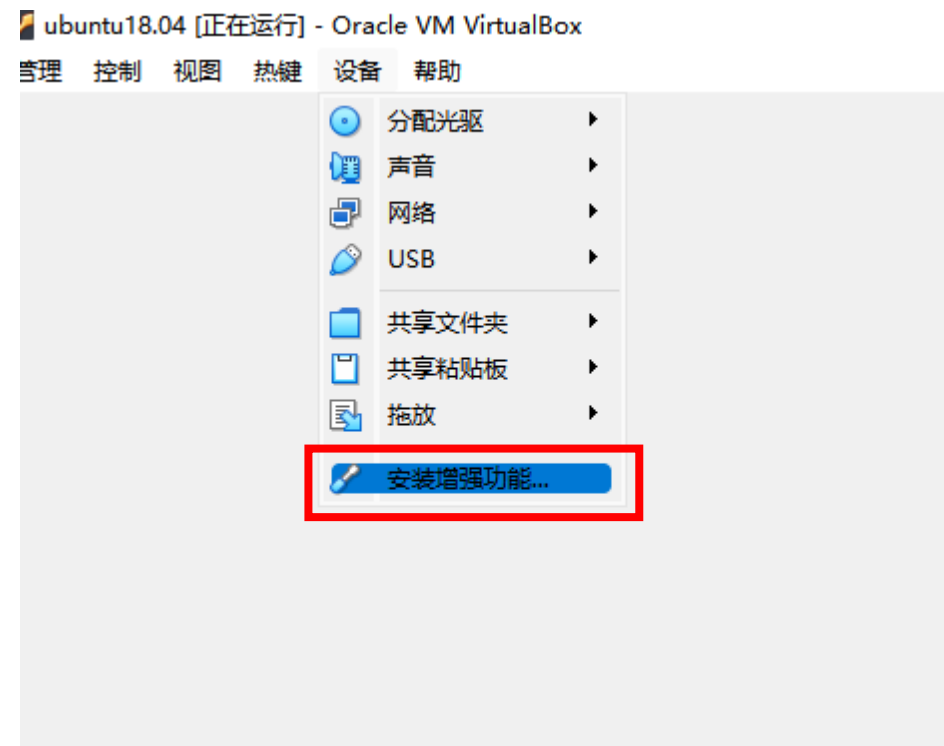
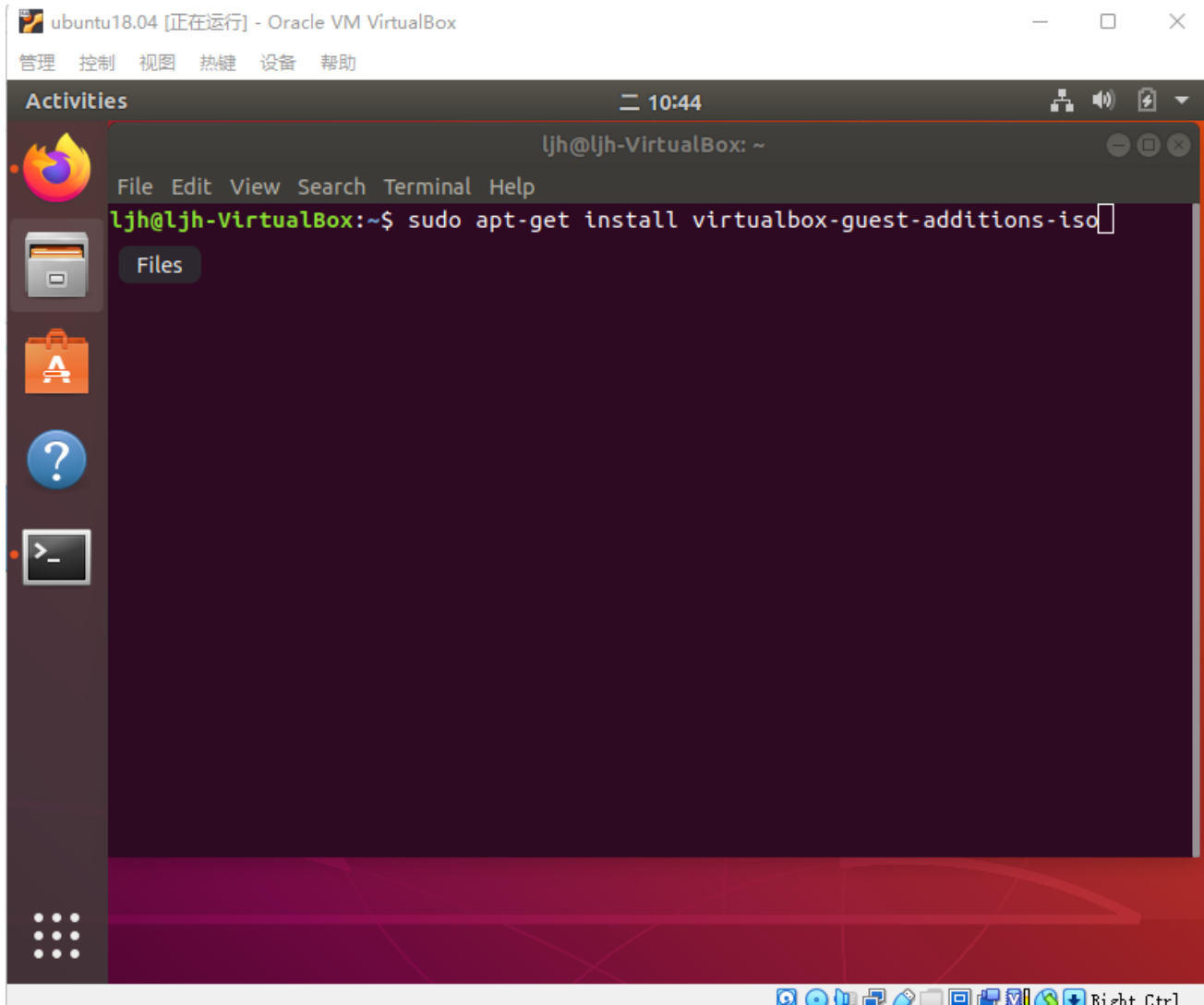
虚拟机的安装包和 Ubuntu18.04 的镜像文件会提供给大家

### 1. 安装教程

几个关键步骤：

⚠ 注意：Ubuntu 安装时的语言设置请选择英文，否则目录的名字会变成中文，不方便后续操作





解决虚拟机在安装后不能全屏的问题

## 2. 安装ROS系统

melodic

### ROS Melodic Morenia

ROS Melodic Morenia is the twelfth ROS distribution release. It was released on May 23rd, 2018.

#### Contents

1. ROS Melodic Morenia
  1. Platforms
  2. Installation
  3. Release Planning
  4. Changes



## 1. Platforms

ROS Melodic Morenia is primarily targeted at the Ubuntu 18.04 (Bionic) release, though other Linux systems as well as Mac OS X, Android, and Windows are supported to varying degrees. For more information on compatibility on other platforms, please see [REP 3: Target Platforms](#). It will also support Ubuntu 17.10 Artful and Debian Stretch.

⚠ 注意：ROS 安装时选择 melodic 版本，

安装方法见 ROS wiki，链接如下：

Link: <http://wiki.ros.org/melodic/Installation/Ubuntu>

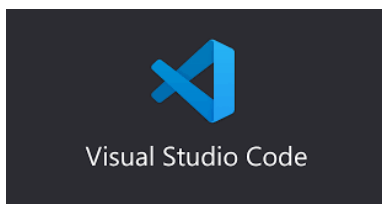
### 3. ROS 基础知识

- 请先跟着ROS wiki 上 <1.1初级教程 (中文)> 操作一遍，了解ROS的一些基本用法，链接如下：

Link: <http://wiki.ros.org/cn/ROS/Tutorials>

- 可以选择 VS code 编辑代码，安装方法见链接：

Link: <https://zhuanlan.zhihu.com/p/430939275>



#### 4. 编译 tag\_detector 的预先准备



**eigen** 

Project ID: 15462818 

## 二. 程序架构

```
97  /* THIS IS THE POSE ESTIMATION FUNCTION YOU NEED TO IMPLEMENT */
98  // pts_id: id of each point
99  // pts_3: 3D position (x, y, z) in world frame
100 // pts_2: 2D position (u, v) in image frame
101 void process(
102     const vector<int> &pts_id,
103     const vector<cv::Point3f> &pts_3,
104     const vector<cv::Point2f> &pts_2,
105     const ros::Time& frame_time)
106 {
```

```
106 {
107     /* Pose estimation using OpenCV's PnP function.
108      * THIS IS YOUR WORK
109      * The result will be used as reference. */
110     // Use cv::solvePnPRansac() and cv::Rodrigues().
```



## 1. 程序架构

```
126 // Apply undistortion if needed. Use cv::undistortPoints().
```

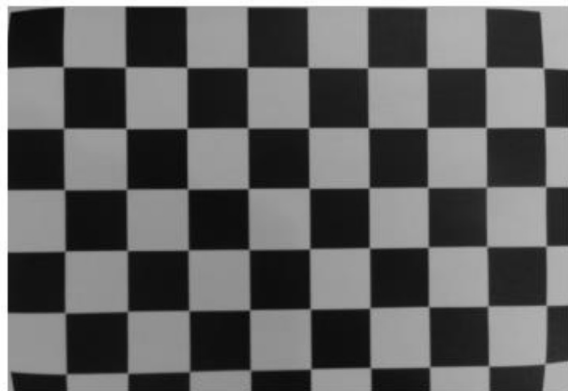
Lec5\_机器视觉



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### Radial Distortions

- Wide angle lenses have radial distortions
  - Straight lines become curves
- Formulation:
  - $r^2 = u^2 + v^2$
  - $u^{dist} = u(1 + k_1r + k_2r^2 + k_3r^3 + \dots)$
  - $v^{dist} = v(1 + k_1r + k_2r^2 + k_3r^3 + \dots)$



## 1. 程序架构

```
128 // Step 1: Work out the initial pose estimates using the linear solution.
```

- Suppose  $\mathbf{H} = \mathbf{K}(\mathbf{r}_1 \quad \mathbf{r}_2 \quad \mathbf{t})$

$\lambda \begin{pmatrix} u \\ v \\ 1 \end{pmatrix}$  • If the SVD of  $(\tilde{\mathbf{h}}_1 \quad \tilde{\mathbf{h}}_2 \quad \tilde{\mathbf{h}}_1 \times \tilde{\mathbf{h}}_2) = \mathbf{USV}^T$ , then the solution is

$$\mathbf{R} = \mathbf{UV}^T$$

$$\lambda u = h_{11}x + h_{12}y$$

$$\lambda v = h_{21}x + h_{22}y$$

$$\lambda = h_{31}x + h_{32}y$$

- To find the translation:

Given an obs  
of feature  $(x_i$

$$\mathbf{t} = \tilde{\mathbf{h}}_3 / \|\tilde{\mathbf{h}}_3\|$$

$$\begin{bmatrix} x_i & y_i & 1 & 0 & 0 & 0 & -x_i u_i & -y_i u_i & -u_i \\ 0 & 0 & 0 & x_i & y_i & 1 & -x_i v_i & -y_i v_i & -v_i \end{bmatrix} \begin{bmatrix} h_{13} \\ h_{21} \\ h_{22} \\ h_{23} \\ h_{31} \\ h_{32} \\ h_{33} \end{bmatrix} = 0$$

Solve this  $\mathbf{Ax} = 0$  problem using SVD

Stack pairs of observations

## 1. 程序架构

- If the SVD of  $(\tilde{\mathbf{h}}_1 \quad \tilde{\mathbf{h}}_2 \quad \tilde{\mathbf{h}}_1 \times \tilde{\mathbf{h}}_2) = \mathbf{U}\mathbf{S}\mathbf{V}^T$ , then the solution is

$$\mathbf{R} = \mathbf{U}\mathbf{V}^T$$

- To find the translation:

$$\mathbf{t} = \tilde{\mathbf{h}}_3 / \|\tilde{\mathbf{h}}_3\|$$

## 1. 程序架构

```
129
130 // Step 2: Refine the pose estimates using non-linear optimization
131
```



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## Nonlinear 3D-2D Pose Estimation

$\theta$ : Euler Angles  $\in R^3$      $t$ : Translation  $\in R^3$      $\pi(\cdot)$ : projection function

1) Nonlinear least square

$$\min_{\theta, t} \sum_i \left\| \begin{bmatrix} u_i \\ v_i \end{bmatrix} - \pi \left( K \cdot (R(\theta) \cdot \begin{bmatrix} x_i \\ y_i \\ z_i \end{bmatrix} + t) \right) \right\|^2 = \min_{\theta, t} \sum_i \|\gamma_i(\theta, t)\|^2$$

2) Linearization **Initial values**

$$\gamma_i(\theta, t) \approx \underbrace{\gamma_i(\theta_0, t_0)}_{2 \times 6 \text{ matrix}} + \underbrace{\frac{\partial \gamma_i}{\partial \theta_i, t_i} \big|_{\theta_0, t_0}}_{2 \times 6 \text{ matrix}} \cdot \begin{bmatrix} \delta \theta \\ \delta t \end{bmatrix} = \gamma_i(\theta_0, t_0) + J_i \begin{bmatrix} \delta \theta \\ \delta t \end{bmatrix}$$

The problem becomes:

$$\min_{\delta \theta, \delta t} \sum_i \left\| \gamma_i(\theta_0, t_0) + J_i \begin{bmatrix} \delta \theta \\ \delta t \end{bmatrix} \right\|^2$$



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## Nonlinear 3D-2D Pose Estimation

$\theta$ : Euler Angles  $\in R^3$      $t$ : Translation  $\in R^3$      $\pi(\cdot)$ : projection function

3) Take derivative and set it to zero

$$\sum_i J_i^T J_i \begin{bmatrix} \delta \theta \\ \delta t \end{bmatrix} + \sum_i J_i^T \gamma_i(\theta_0, t_0) = 0 \Rightarrow \underbrace{\sum_i J_i^T J_i}_{\mathbf{A}} \begin{bmatrix} \delta \theta \\ \delta t \end{bmatrix} = - \underbrace{\sum_i J_i^T \gamma_i(\theta_0, t_0)}_{\mathbf{b}}$$

4) Solve for the incremental states and update the optimization variables

$$\begin{bmatrix} \delta \theta \\ \delta t \end{bmatrix} = \mathbf{A}^{-1} \mathbf{b} \Rightarrow \begin{bmatrix} \theta \\ t \end{bmatrix} = \begin{bmatrix} \theta_0 \\ t_0 \end{bmatrix} + \begin{bmatrix} \delta \theta \\ \delta t \end{bmatrix}$$

5) Iterate from step 1)

## 2. C++ 求解SVD



**eigen** 

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使用Eigen 库：进行svd分解，形如  $A = U * S * V^T$ 。

```
JacobiSVD<MatrixXd> svd(J, ComputeThinU | ComputeThinV);
```

```
U = svd.matrixU();
```

```
V = svd.matrixV();
```

```
A = svd.singularValues();
```