Assignment Report

CSC 4005 Heat Distribution

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I. Introduction

This assignment is implementing a sequential program, a pthread program, an

CUDA program, an OpenMP program and an MPI program to simulate an two-

dimensional heat distribution problem.

A square metal sheet has known temperatures along each of its edges. Find the temperature distribution.

Dividing the area into a fine mesh of points, $h_{i,j}$. The temperature at an inside point can be taken to be the average of the temperatures of the four neighboring points.

Convenient to describe the edges by points adjacent to the interior points. The interior points of $h_{i,j}$ are where 0 < i < n, 0 < j < n $[(n-1) \times (n-1)$ interior points].

Temperature of each point by iterating the equation:

$$h_{i,j} = \frac{h_{i-1,j} + h_{i+1,j} + h_{i,j-1} + h_{i,j+1}}{4}$$

(0 < i < n, 0 < j < n) for a fixed number of iterations or until the difference between iterations of a point is less than some very small prescribed amount.

II. Design Approaches

1. Architecture

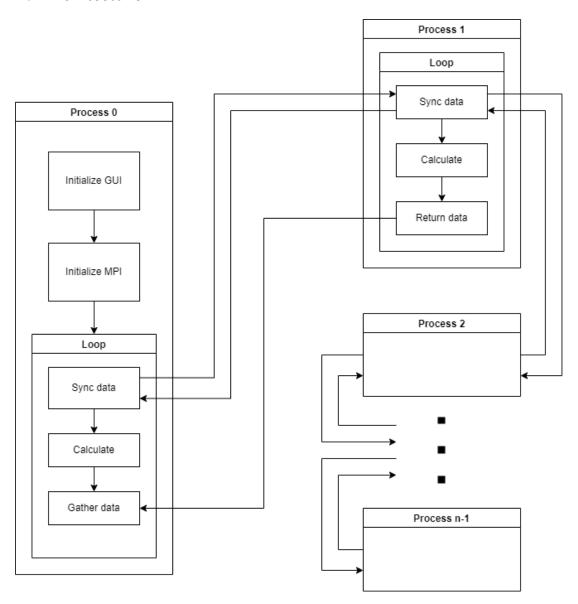


Figure 1. Architecture of the MPI version of the program

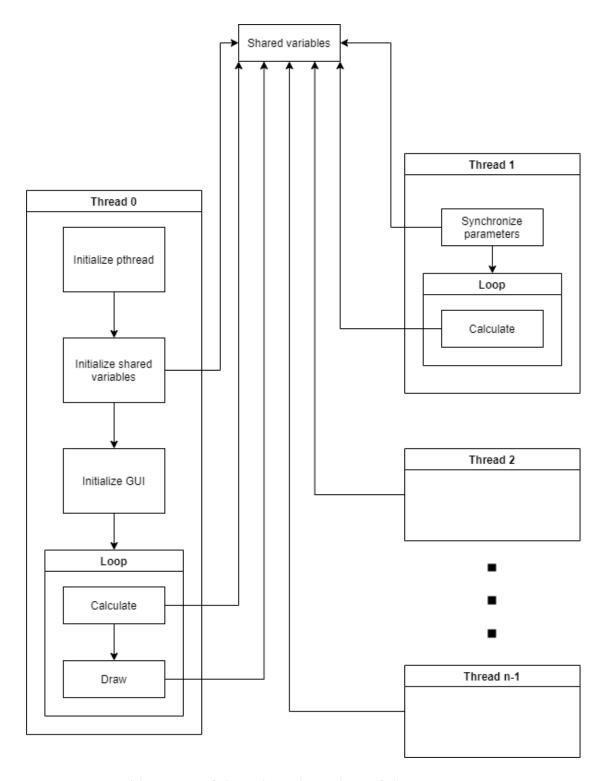


Figure 2. Architecture of the pthread version of the program

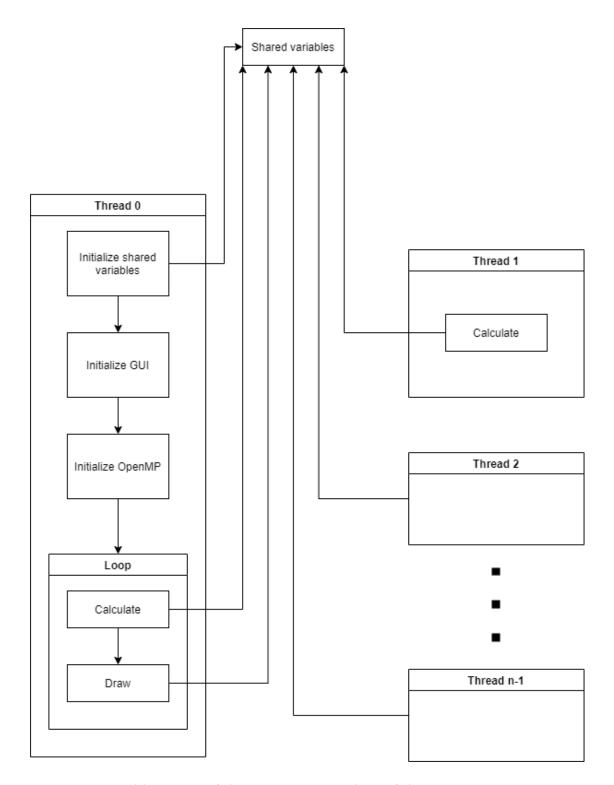


Figure 3. Architecture of the OpenMP version of the program

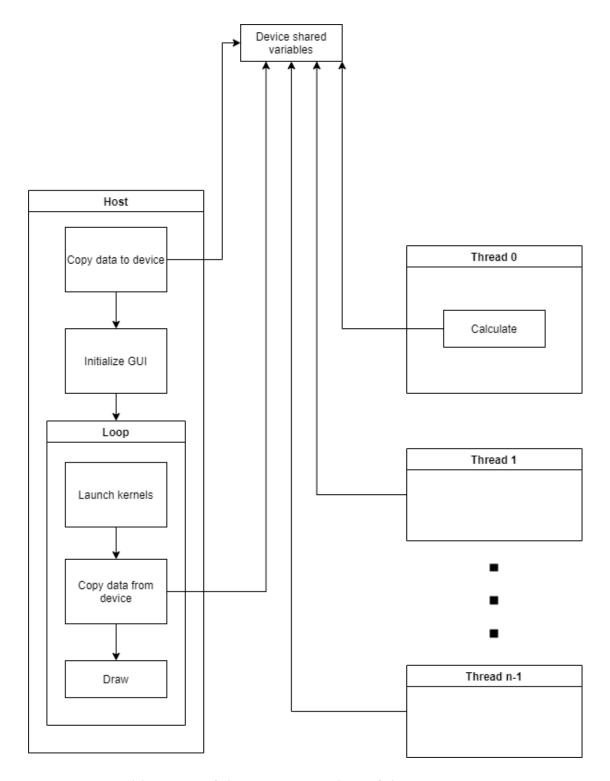


Figure 4. Architecture of the CUDA version of the program

III. Build And Run

1. MPI

To build the program, use the following commands on the server:

cd /path/to/project

mkdir build && cd build

cmake .. -DCMAKE_BUILD_TYPE=Release

make

cp ~/.Xauthority /pvfsmnt/\$(whoami)

export XAUTHORITY=/pvfsmnt/\$(whoami)/.Xauthority

(1) To run the program, use the following commands on the server:

mpirun csc4005 imgui (room size) (max iteration) (algorithm)

Examples:

- a. mpirun csc4005_imgui
- b. mpirun csc4005 imgui 300 100 0
- c. mpirun csc4005 imgui 300 100 1

2. pthread

To build the program, use the following commands on the server:

cd /path/to/project

mkdir build && cd build

cmake .. -DCMAKE_BUILD_TYPE=Release

make

```
cp ~/.Xauthority /pvfsmnt/$(whoami)
```

```
export XAUTHORITY=/pvfsmnt/$(whoami)/.Xauthority
```

(2) To run the program, use the following commands on the server:

```
mpirun csc4005 imgui num threads (room size) (max iteration) (algorithm)
```

Examples:

- a. srun -n1 csc4005_imgui 4
- b. srun -n1 csc4005_imgui 8 100 100
- c. srun -n1 csc4005_imgui 16 1000 100 1

3. OpenMP

To build the program, use the following commands on the server:

cd /path/to/project

mkdir build && cd build

cmake .. -DCMAKE_BUILD_TYPE=Release

make

cp ~/.Xauthority /pvfsmnt/\$(whoami)

export XAUTHORITY=/pvfsmnt/\$(whoami)/.Xauthority

(3) To run the program, use the following commands on the server:

mpirun csc4005_imgui num_threads (room_size) (max_iteration) (algorithm)

Examples:

- a. srun -n1 csc4005_imgui 4
- b. srun -n1 csc4005 imgui 8 100 100 0

4. CUDA

To build the program, use the following commands on the server:

cd /path/to/project

mkdir build && cd build

source scl_source enable devtoolset-10

CC=gcc CXX=g++ cmake ..

make -j12

cp ~/.Xauthority /pvfsmnt/\$(whoami)

export XAUTHORITY=/pvfsmnt/\$(whoami)/.Xauthority

(4) To run the program, use the following commands on the server:

mpirun csc4005 imgui num threads (room size) (max iteration) (algorithm)

Examples:

- c. srun -n1 csc4005_imgui 4
- d. srun -n1 csc4005_imgui 32 1000 100 1

IV. Performance Analysis

1. Test Results

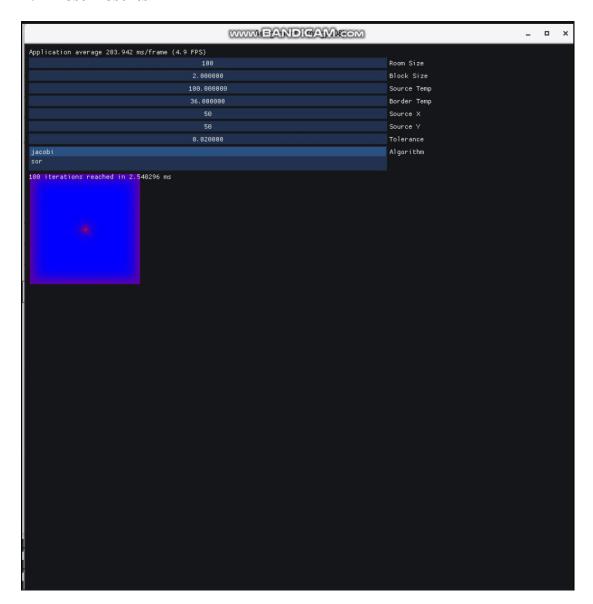


Figure 6. Test result with room_size = 100

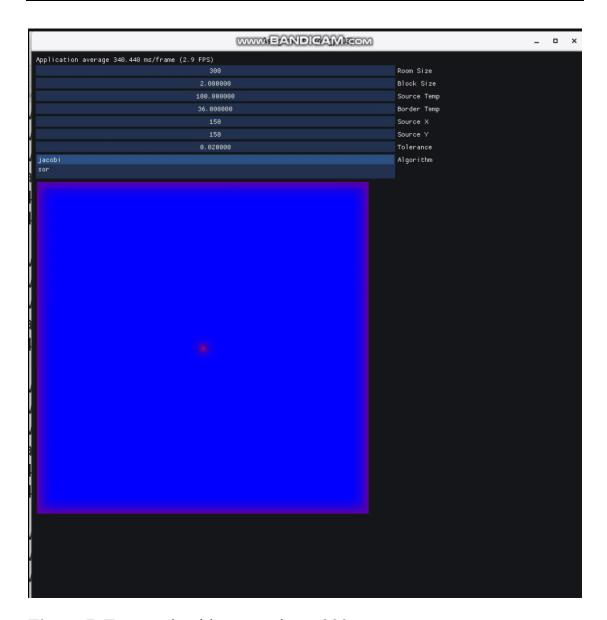


Figure 7. Test result with room_size = 300

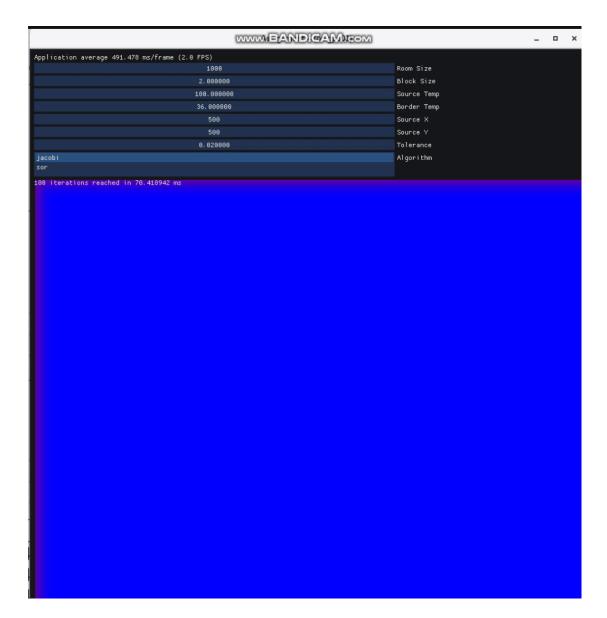


Figure 8. Test result with room_size = 1000

		N	lumber of pr	ocesses		
Φ		1	4	16	32	64
ı size	100	8.48	4.01	2.56	2.54	69.92
оот	300	75.35	21.89	7.67	6.13	38.66
5	1000	815.43	208.98	60.69	38.54	44.35

Table 1. Execution time (ms) of 100 iterations using the Jacobi algorithm of the MPI version of the program with respect to different room sizes and numbers of processes

		Νι	umber of pro	ocesses		
e U		1	4	16	32	64
ı size	100	11.99	5.59	3.29	3.33	84.28
тоо.	300	107.8	30.45	10.03	7.66	57.18
5	1000	1166.23	304.86	82.33	54.22	58.33

Table 2. Execution time (ms) of 100 iterations using the Sor algorithm of the MPI version of the program with respect to different room sizes and numbers of processes

		N	lumber of pro	ocesses		
മ		1	4	16	32	64
ı size	100	8.92	6.44	15.88	28.51	59.87
.00m	300	82.34	25.21	21.23	35.19	63.24
2	1000	842.19	219.42	73.74	67.94	96.13

Table 3. Execution time (ms) of 100 iterations using the Jacobi algorithm of the pthread version of the program with respect to different room sizes and numbers of processes

		Ν	umber of pr	ocesses		
Ð		1	4	16	32	64
ı size	100	13.32	10.11	32.71	68.95	140.7
шоо.	300	117.29	39.68	37.55	71.52	132.93
2	1000	1257.33	336.49	115.53	125.17	195.75

Table 4. Execution time (ms) of 100 iterations using the Sor algorithm of the pthread version of the program with respect to different room sizes and numbers of processes

	Number of processes							
Ф		1	4	16	32	64		
ı size	100	8.86	4.44	4.4	113.12	797.24		
moo.	300	79.49	23.27	9.65	69.99	1090.05		
2	1000	841.12	222.48	62.97	47.57	807.02		

Table 5. Execution time (ms) of 100 iterations using the Jacobi algorithm of the OpenMP version of the program with respect to different room sizes and numbers of processes

		Nı	umber of pr	ocesses		
Ф		1	4	16	32	64
ı size	100	14.09	6.89	7.49	117.46	892.84
moo.	300	118.34	35.03	15.9	119.22	739.98
2	1000	1279.02	329.07	104.59	164.05	1229.78

Table 6. Execution time (ms) of 100 iterations using the Sor algorithm of the OpenMP version of the program with respect to different room sizes and numbers of processes

			N	umber of pr	ocesses		
	ല		1	4	16	32	64
	size	100	535.43	142.86	49.75	33.95	22.35
9	.00L	300	4802.93	1240.65	346.13	219.93	122.63
2	2	1000	39326.86	10477.32	3870.53	2285.29	1292.92

Table 7. Execution time (ms) of 100 iterations using the Jacobi algorithm of the CUDA version of the program with respect to different room sizes and numbers of processes

9		1	4	16	32	64
ı size	100	988.32	372.58	142.99	52.49	29.52
Oom	300	8023.61	4269.45	1136.82	363.76	339.43
2	1000	74323.37	19468.78	9386.17	4005.14	2200.03

Table 8. Execution time (ms) of 100 iterations using the Sor algorithm of the CUDA version of the program with respect to different room sizes and numbers of processes

Note:

- a. All tests were conducted on 10.26.1.30.
- b. Each test was repeated for three times and averaged.

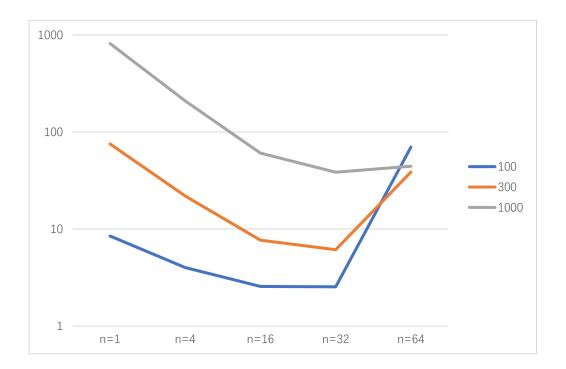


Figure 9. Execution time (ms) of 100 iterations using the Jacobi algorithm of the MPI version of the program with respect to different number of processes

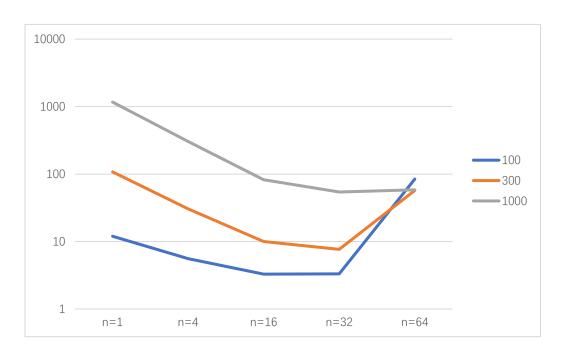


Figure 10. Execution time (ms) of 100 iterations using the Sor algorithm of the MPI version of the program with respect to different number of processes

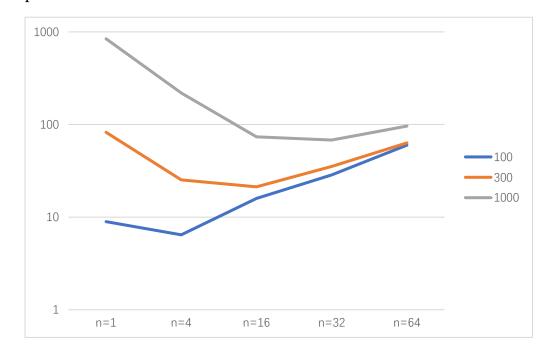


Figure 11. Execution time (ms) of 100 iterations using the Jacobi algorithm of the pthread version of the program with respect to different number of processes

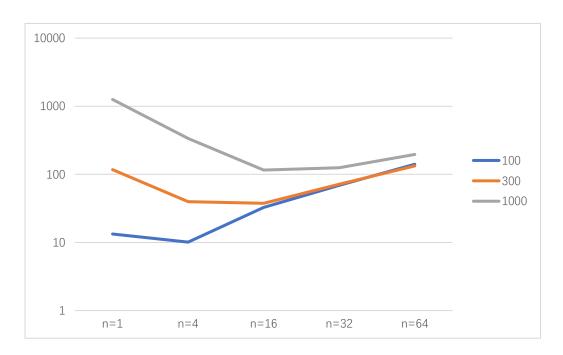


Figure 12. Execution time (ms) of 100 iterations using the Sor algorithm of the pthread version of the program with respect to different number of processes

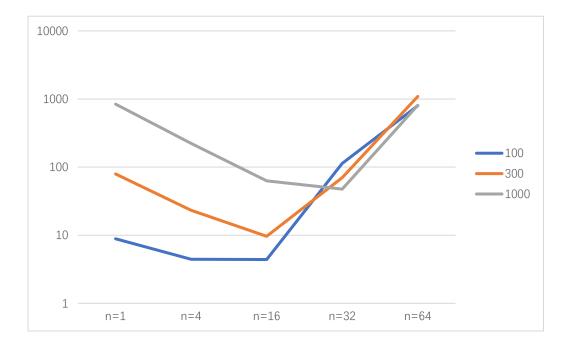


Figure 13. Execution time (ms) of 100 iterations using the Jacobi algorithm of the OpenMP version of the program with respect to different number of processes

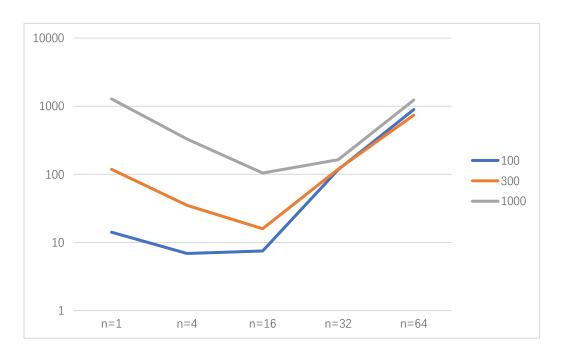


Figure 14. Execution time (ms) of 100 iterations using the Sor algorithm of the OpenMP version of the program with respect to different number of processes

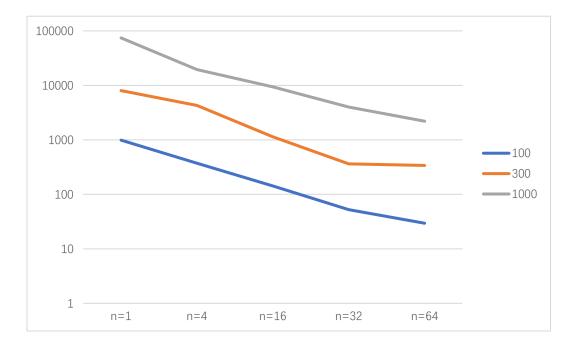


Figure 15. Execution time (ms) of 100 iterations using the Jacobi algorithm of the CUDA version of the program with respect to different number of processes

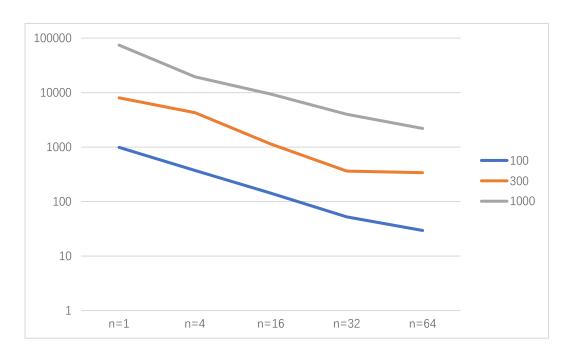


Figure 16. Execution time (ms) of 100 iterations using the Sor algorithm of the CUDA version of the program with respect to different number of processes

2. Analysis

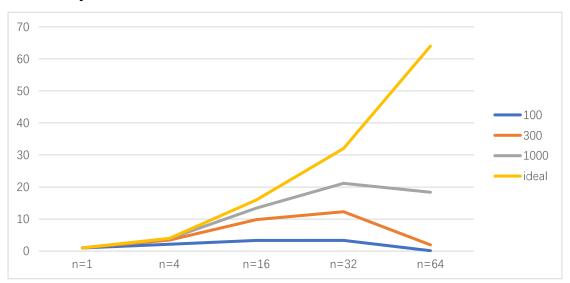


Figure 17. Speedup factor of the MPI version of the program using the Jacobi algorithm with respect to different number of processes

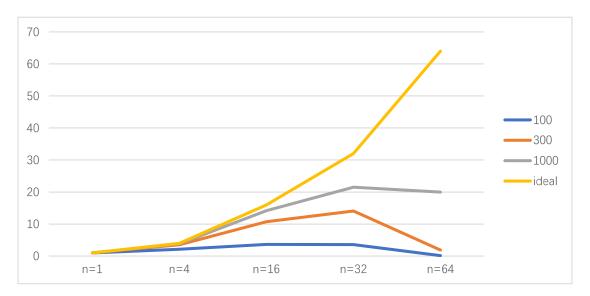


Figure 18. Speedup factor of the MPI version of the program using the Sor algorithm with respect to different number of processes

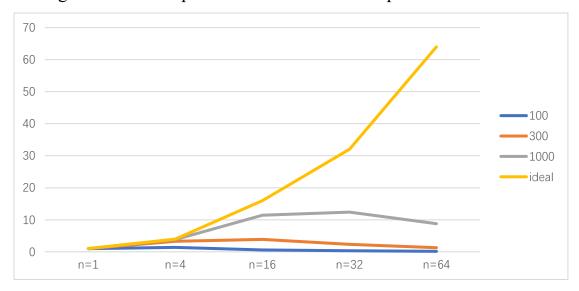


Figure 19. Speedup factor of the pthread version of the program using the Jacobi algorithm with respect to different number of processes

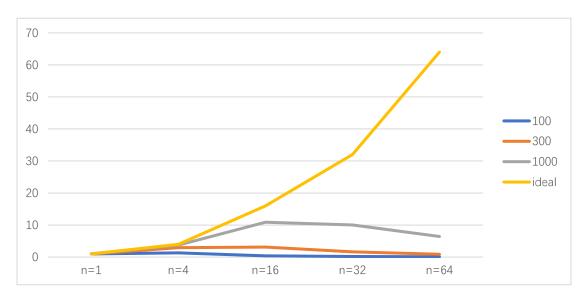


Figure 20. Speedup factor of the pthread version of the program using the Sor algorithm with respect to different number of processes

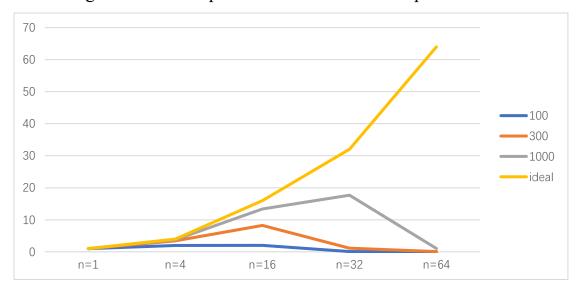


Figure 21. Speedup factor of the OpenMP version of the program using the Jacobi algorithm with respect to different number of processes

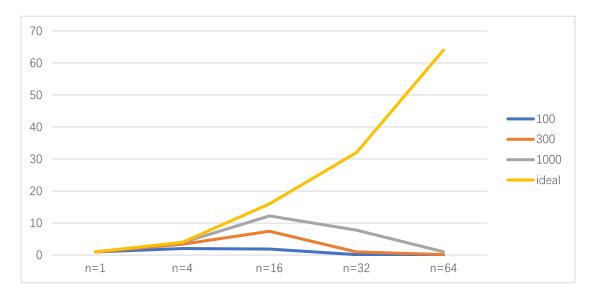


Figure 22. Speedup factor of the OpenMP version of the program using the Sor algorithm with respect to different number of processes

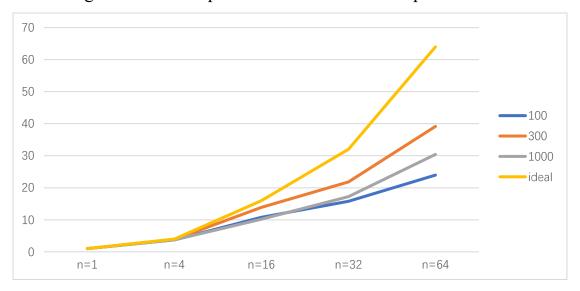


Figure 23. Speedup factor of the CUDA version of the program using the Jacobi algorithm with respect to different number of processes

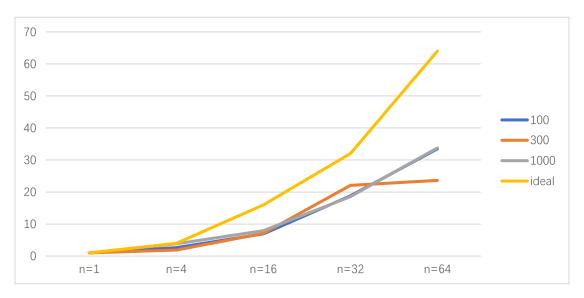


Figure 24. Speedup factor of the CUDA version of the program using the Sor algorithm with respect to different number of processes

As shown in Figure 17-24, when the room size is small (100) and the number of processes/threads is also small, the execution time does not decrease much as the number of processes/threads increases. When the number of processes/threads becomes larger, the execution time even soars due to the multiprocessing overhead, such as inter-process communication, shared memory access, mutual exclusive locks, etc.

Generally speaking, the speedup is better for larger room sizes. For MPI, pthread, OpenMP versions, when the number of processes/threads exceeds 32, which is the number of processor cores on a single node, the performance drops dramatically due to the context switching overhead. The graphics card has much more cores than the CPU. Therefore, when the number of processes/threads exceeds 32, the speedup is stable.

Note that in the OpenMP version of the program, the speedup drops

tremendously when the number of threads reaches 64. This might be related to the mutual exclusive locks to the global variable that indicates whether the program should terminate. When the number of threads exceeds the number of processor cores, the threads need to do time sharing. Therefore, active threads may need to wait for mutual exclusive locks obtained by inactive threads, which could be a huge waste of time.

Besides, the Jacobi algorithm has a higher performance than the Sor.

In terms of performance, the MPI version generally provides the best calculation speed. Notice that the CUDA version seems to be very slow. There are a few possible reasons. First, the timing function is executed on the CPU. Therefore, the measured calculation time may be much larger than the actual calculation time on the GPU. Second, a single CUDA core may be much slower than a CPU core.

Nevertheless, this does not necessarily mean that the MPI framework is superior than the others. There are many factors that may affect the performance. For example, my design and implementation of each version of the program. The choice of the parallel programming framework should depend on the specific usage (CPU-bound or IO-bound), algorithm, and hardware.

In all versions, it is obvious that as the number of processes increases, the speedup factor increases slower and even decreases for small input sizes, while the efficiency decreases.

V. Conclusion

In summary, this assignment explores two different heat distribution algorithm and implementations by different parallel computing frameworks, the concepts and implementation of parallel computing, the MPI, pthread, OpenMP, and CUDA framework, and the speedup and overhead of multiprocessing/multithreading. Due to the inter-process communication and/or the shared memory access overhead, when the number of processes becomes larger, the efficiency of multiprocessing/multithreading gets lower. For small input sizes, this overhead may even outweigh the speedup from parallelism when the number of processes/threads is large. However, for large input sizes, the impact of the multiprocessing/multithreading overhead is relatively smaller since the portion of computation is larger. Therefore, parallel computing is best suitable for large input sizes.

There exist some limitations in this assignment. First, since the maximum time of a single session of the cloud server is 10 minutes, it is not feasible to test the program for a long time to see whether the calculation speed is stable over time.

Second, since the maximum processor cores of a single node of the cloud server is 32, it is not feasible to test larger number of cores for the MPI, pthread, and OpenMP versions of the program. Nevertheless, from the existing experiment results, we can infer that when the input size is

large enough, the efficiency of multiprocessing will be close to 1. Also, we can infer that the multiprocessing overhead will become larger and larger as the number of processors increases, and finally slows down the execution.

VI. Source Code

1. MPI Version

```
#include <graphic/graphic.hpp>
#include <imgui_impl_sdl.h>
#include <cstring>
#include <chrono>
#include <hdist/hdist.hpp>
#include <mpi.h>
template<typename ...Args>
void UNUSED(Args &&... args [[maybe_unused]]) {}
ImColor temp_to_color(double temp) {
   auto value = static_cast<uint8_t>(temp / 100.0 * 255.0);
   return {value, 0, 255 - value};
int main(int argc, char **argv) {
   int size;
   int rank;
   MPI_Init(&argc, &argv);
   MPI Comm size(MPI COMM WORLD, &size);
   MPI_Comm_rank(MPI_COMM_WORLD, &rank);
   bool first = true;
   int finished = 0;
   int local finished = finished;
   static hdist::State current_state, last_state;
   int num_iteration = 0;
   int max_iteration = 100;
   if (argc >= 2) {
       current state.room size = atoi(argv[1]);
       current_state.source_x = current_state.room_size / 2;
       current_state.source_y = current_state.room_size / 2;
   if (argc >= 3) {
       max_iteration = atoi(argv[2]);
   if (argc >= 4) {
```

```
int algo = atoi(argv[3]);
       if (algo == 0) {
           current_state.algo = hdist::Algorithm::Jacobi;
       else {
           current_state.algo = hdist::Algorithm::Sor;
    int chunk = (current_state.room_size + size - 1) / size;
    int capacity = chunk * size;
   double* global_buffer;
    auto grid = hdist::Grid{
       static_cast<size_t>(current_state.room_size),
       static cast<size t>(capacity),
       current_state.border_temp,
       current_state.source_temp,
       static_cast<size_t>(current_state.source_x),
       static_cast<size_t>(current_state.source_y)};
   if (0 == rank) {
       static std::chrono::high resolution clock::time point begin,
end;
       static size t duration = 0;
       static const char* algo_list[2] = { "jacobi", "sor" };
       graphic::GraphicContext context{"Assignment 4"};
       context.run([&](graphic::GraphicContext *context
[[maybe_unused]], SDL_Window *) {
           auto io = ImGui::GetIO();
           ImGui::SetNextWindowPos(ImVec2(0.0f, 0.0f));
           ImGui::SetNextWindowSize(io.DisplaySize);
           ImGui::Begin("Assignment 4", nullptr,
                       ImGuiWindowFlags_NoMove
                       | ImGuiWindowFlags NoCollapse
                       │ ImGuiWindowFlags NoTitleBar
                       | ImGuiWindowFlags NoResize);
           ImDrawList *draw_list = ImGui::GetWindowDrawList();
           ImGui::Text("Application average %.3f ms/frame (%.1f FPS)",
1000.0f / ImGui::GetIO().Framerate,
                       ImGui::GetIO().Framerate);
           ImGui::DragInt("Room Size", &current_state.room_size, 10,
200, 1600, "%d");
```

```
ImGui::DragFloat("Block Size", &current_state.block_size,
0.01, 0.1, 10, "%f");
           ImGui::DragFloat("Source Temp", &current_state.source_temp,
0.1, 0, 100, "%f");
           ImGui::DragFloat("Border Temp", &current state.border temp,
0.1, 0, 100, "%f");
           ImGui::DragInt("Source X", &current_state.source_x, 1, 1,
current_state.room_size - 2, "%d");
           ImGui::DragInt("Source Y", &current state.source y, 1, 1,
current_state.room_size - 2, "%d");
           ImGui::DragFloat("Tolerance", &current_state.tolerance,
0.01, 0.01, 1, "%f");
           ImGui::ListBox("Algorithm", reinterpret_cast<int</pre>
*>(&current state.algo), algo list, 2);
           if (current state.algo == hdist::Algorithm::Sor) {
               ImGui::DragFloat("Sor Constant",
&current state.sor constant, 0.01, 0.0, 20.0, "%f");
           // GUI paramater adjustment is disbled
           // if (current state.room size != last state.room size) {
                  grid = hdist::Grid{
                          static cast<size t>(current state.room size),
                          current state.border temp,
                          current_state.source_temp,
                          static_cast<size_t>(current_state.source_x),
                          static_cast<size_t>(current_state.source_y)};
                  first = true;
           // if (current_state != last_state) {
                  last_state = current_state;
                  finished = false;
           if (first) {
               first = false;
               finished = 0;
           if (!finished) {
               if (num_iteration < max_iteration) {</pre>
```

```
begin = std::chrono::high_resolution_clock::now();
                   if (size > 1) {
                       // synchronize the points on the boarder
                       // communicate with the succeeding process
                       // even rank (0): send before receive
                       MPI_Send(grid.get_current_buffer().data() +
(chunk - 1) * current_state.room size,
                                  current_state.room_size, MPI_DOUBLE,
1, 0, MPI COMM WORLD);
                       MPI_Recv(grid.get_current_buffer().data() + chunk
 current_state.room_size,
                                  current_state.room_size, MPI_DOUBLE,
1, 0, MPI_COMM_WORLD, MPI_STATUS_IGNORE);
                      if (current state.algo == hdist::Algorithm::Sor)
                           MPI Send(grid.get alt buffer().data() +
(chunk - 1) * current_state.room_size,
                                      current_state.room_size,
MPI_DOUBLE, 1, 0, MPI_COMM_WORLD);
                           MPI_Recv(grid.get_alt_buffer().data() + chunk
* current_state.room_size,
                                      current_state.room_size,
MPI_DOUBLE, 1, 0, MPI_COMM_WORLD, MPI_STATUS_IGNORE);
                   local finished = (int)
hdist::calculate(current_state, grid, rank, chunk);
                   // synchronize the global status (finished or not)
                   MPI_Allreduce(&local_finished, &finished, 1,
MPI INT, MPI LAND, MPI COMM WORLD);
                   end = std::chrono::high_resolution_clock::now();
                   duration +=
duration_cast<std::chrono::nanoseconds>(end - begin).count();
                   // collect the results for drawing
                   global buffer = grid.get current buffer().data();
                   MPI_Gather(grid.get_current_buffer().data() + rank *
chunk * current_state.room_size,
                              chunk * current_state.room_size,
MPI_DOUBLE, global_buffer,
                              chunk * current_state.room_size,
MPI DOUBLE, 0, MPI_COMM_WORLD);
                   num iteration ++;
```

```
}
            }
            const ImVec2 p = ImGui::GetCursorScreenPos();
            float x = p.x + current_state.block_size, y = p.y +
current_state.block_size;
            for (size_t i = 0; i < current_state.room_size; ++i) {</pre>
                for (size t j = 0; j < current state.room size; ++j) {</pre>
                   auto temp = grid[{i, j}];
                   auto color = temp_to_color(temp);
                   draw_list->AddRectFilled(ImVec2(x, y), ImVec2(x +
current_state.block_size, y + current_state.block_size), color);
                   y += current state.block size;
               x += current_state.block_size;
               y = p.y + current_state.block_size;
            if (finished) {
                ImGui::Text("stabilized in %lf ms", (double) duration /
1'000'000);
           else if (num_iteration >= max_iteration) {
                ImGui::Text("%d iterations reached in %lf ms",
max_iteration, (double) duration / 1'000'000);
            ImGui::End();
        });
    else {
       while(num_iteration < max_iteration) {</pre>
            if (!finished) {
               // synchronize the points on the boarder
               // even rank: send before receive
               if (rank % 2 == 0) {
                   // communicate with the succeeding process
                   if (rank < size - 1) {</pre>
                       MPI_Send(grid.get_current_buffer().data() + (rank
* chunk + chunk - 1) * current_state.room_size,
                                   current_state.room_size, MPI_DOUBLE,
rank + 1, 0, MPI_COMM_WORLD);
```

```
MPI_Recv(grid.get_current_buffer().data() + (rank
* chunk + chunk) * current_state.room_size,
                                  current_state.room_size, MPI_DOUBLE,
rank + 1, 0, MPI COMM WORLD, MPI STATUS IGNORE);
                       if (current state.algo == hdist::Algorithm::Sor)
                           MPI_Send(grid.get_alt_buffer().data() + (rank
* chunk + chunk - 1) * current_state.room_size,
                                      current state.room size,
MPI_DOUBLE, rank + 1, 0, MPI_COMM_WORLD);
                          MPI_Recv(grid.get_alt_buffer().data() + (rank
* chunk + chunk) * current_state.room_size,
                                      current_state.room_size,
MPI DOUBLE, rank + 1, 0, MPI COMM WORLD, MPI STATUS IGNORE);
                   // communicate with the preceding process
                   MPI_Send(grid.get_current_buffer().data() + (rank *
chunk) * current_state.room_size,
                              current_state.room_size, MPI_DOUBLE, rank
- 1, 0, MPI COMM WORLD);
                   MPI_Recv(grid.get_current_buffer().data() + (rank *
chunk - 1) * current state.room size,
                              current_state.room_size, MPI DOUBLE, rank
- 1, 0, MPI_COMM_WORLD, MPI_STATUS_IGNORE);
                   if (current_state.algo == hdist::Algorithm::Sor) {
                       MPI_Send(grid.get_alt_buffer().data() + (rank *
chunk) * current_state.room_size,
                              current_state.room_size, MPI_DOUBLE, rank
- 1, 0, MPI COMM WORLD);
                       MPI_Recv(grid.get_alt_buffer().data() + (rank *
chunk - 1) * current_state.room_size,
                              current_state.room_size, MPI_DOUBLE, rank
 1, 0, MPI_COMM_WORLD, MPI_STATUS_IGNORE);
               // odd rank: receive before send
               else {
                   // communicate with the preceding process
                   MPI_Recv(grid.get_current_buffer().data() + (rank *
chunk - 1) * current_state.room_size,
                              current_state.room_size, MPI_DOUBLE, rank
- 1, 0, MPI_COMM_WORLD, MPI_STATUS_IGNORE);
```

```
MPI_Send(grid.get_current_buffer().data() + (rank *
chunk) * current_state.room_size,
                               current_state.room_size, MPI_DOUBLE, rank
- 1, 0, MPI COMM WORLD);
                   if (current state.algo == hdist::Algorithm::Sor) {
                       MPI_Recv(grid.get_alt_buffer().data() + (rank *
chunk - 1) * current state.room size,
                               current_state.room_size, MPI_DOUBLE, rank
- 1, 0, MPI_COMM_WORLD, MPI_STATUS_IGNORE);
                       MPI_Send(grid.get_alt_buffer().data() + (rank *
chunk) * current_state.room_size,
                               current_state.room_size, MPI_DOUBLE, rank
- 1, 0, MPI_COMM_WORLD);
                   // communicate with the succeeding process
                   if (rank < size - 1) {
                       MPI_Send(grid.get_current_buffer().data() + (rank
* chunk + chunk - 1) * current_state.room_size,
                                  current_state.room_size, MPI_DOUBLE,
rank + 1, 0, MPI_COMM_WORLD);
                       MPI Recv(grid.get current buffer().data() + (rank
* chunk + chunk) * current_state.room_size,
                                  current_state.room_size, MPI_DOUBLE,
rank + 1, 0, MPI_COMM_WORLD, MPI_STATUS_IGNORE);
                       if (current state.algo == hdist::Algorithm::Sor)
                           MPI_Send(grid.get_alt_buffer().data() + (rank
* chunk + chunk - 1) * current_state.room_size,
                                  current_state.room_size, MPI_DOUBLE,
rank + 1, 0, MPI COMM WORLD);
                           MPI_Recv(grid.get_alt_buffer().data() + (rank
* chunk + chunk) * current_state.room_size,
                                  current_state.room_size, MPI_DOUBLE,
rank + 1, 0, MPI_COMM_WORLD, MPI_STATUS_IGNORE);
                   }
               local_finished = (int) hdist::calculate(current_state,
grid, rank, chunk);
               MPI_Allreduce(&local_finished, &finished, 1, MPI_INT,
MPI LAND, MPI COMM WORLD);
               MPI_Gather(grid.get_current_buffer().data() + rank *
chunk * current_state.room_size,
```

2. Pthread Version

```
#include <graphic/graphic.hpp>
#include <imgui_impl_sdl.h>
#include <cstring>
#include <chrono>
#include <hdist/hdist.hpp>
template<typename ...Args>
void UNUSED(Args &&... args [[maybe_unused]]) {}
ImColor temp_to_color(double temp) {
   auto value = static_cast<uint8_t>(temp / 100.0 * 255.0);
   return {value, 0, 255 - value};
pthread_mutex_t mutex = PTHREAD_MUTEX_INITIALIZER;
pthread barrier t barrier;
hdist::Grid* grid;
bool first = true;
int finished = 0;
int local_finished = finished;
hdist::State current state, last state;
int max_iteration = 100;
int chunk = 0;
void* gui_loop(void* t) {
   int* int_ptr = (int *) t;
   int tid = *int_ptr;
```

```
int num_iteration = 0;
   if (0 == tid) {
       static std::chrono::high resolution clock::time point begin,
end;
       static size_t duration = 0;
       static const char* algo_list[2] = { "jacobi", "sor" };
       graphic::GraphicContext context{"Assignment 4"};
       context.run([&](graphic::GraphicContext *context
[[maybe_unused]], SDL_Window *) {
           auto io = ImGui::GetIO();
           ImGui::SetNextWindowPos(ImVec2(0.0f, 0.0f));
           ImGui::SetNextWindowSize(io.DisplaySize);
           ImGui::Begin("Assignment 4", nullptr,
                       ImGuiWindowFlags NoMove
                       | ImGuiWindowFlags NoCollapse
                       │ ImGuiWindowFlags_NoTitleBar
                       ImGuiWindowFlags_NoResize);
           ImDrawList *draw_list = ImGui::GetWindowDrawList();
           ImGui::Text("Application average %.3f ms/frame (%.1f FPS)",
1000.0f / ImGui::GetIO().Framerate,
                       ImGui::GetIO().Framerate);
           ImGui::DragInt("Room Size", &current_state.room_size, 10,
200, 1600, "%d");
           ImGui::DragFloat("Block Size", &current state.block size,
0.01, 0.1, 10, "%f");
           ImGui::DragFloat("Source Temp", &current_state.source_temp,
0.1, 0, 100, "%f");
           ImGui::DragFloat("Border Temp", &current_state.border_temp,
0.1, 0, 100, "%f");
           ImGui::DragInt("Source X", &current_state.source_x, 1, 1,
current_state.room_size - 2, "%d");
           ImGui::DragInt("Source Y", &current_state.source_y, 1, 1,
current_state.room_size - 2, "%d");
           ImGui::DragFloat("Tolerance", &current_state.tolerance,
0.01, 0.01, 1, "%f");
           ImGui::ListBox("Algorithm", reinterpret cast<int</pre>
*>(&current_state.algo), algo_list, 2);
           if (current state.algo == hdist::Algorithm::Sor) {
               ImGui::DragFloat("Sor Constant",
&current_state.sor_constant, 0.01, 0.0, 20.0, "%f");
           }
```

```
// GUI paramater adjustment is disbled
                  grid = hdist::Grid{
                          current_state.border_temp,
                          current_state.source_temp,
                          static cast<size t>(current state.source y)};
                  first = true;
                  last state = current state;
           if (first) {
               first = false;
               finished = 0;
           if (!finished) {
               if (num_iteration < max_iteration) {</pre>
                   begin = std::chrono::high_resolution_clock::now();
                   if (current_state.algo == hdist::Algorithm::Jacobi)
                       local_finished = (int)
hdist::calculate_jacobi(current_state, *grid, tid, chunk);
                   else if (current_state.algo ==
hdist::Algorithm::Sor) {
                       local_finished = (int)
hdist::calculate_sor(current_state, *grid, tid, chunk, 0);
                       // sync threads and switch buffer
                       pthread_barrier_wait(&barrier);
                       grid->switch buffer();
                       // acknowledge other threads that the buffer has
                       pthread_barrier_wait(&barrier);
                       local_finished = (int)
hdist::calculate_sor(current_state, *grid, tid, chunk, 1);
                   pthread_mutex_lock(&mutex);
```

```
// update the global status (finished or not)
                   finished &= local finished;
                   pthread_mutex_unlock(&mutex);
                   // sync threads and switch buffer
                   pthread barrier wait(&barrier);
                   grid->switch_buffer();
                   // acknowledge other threads that the buffer has
been switched
                   pthread barrier wait(&barrier);
                   // hence this does not count into the total time
                   end = std::chrono::high_resolution_clock::now();
                   duration +=
duration cast<std::chrono::nanoseconds>(end - begin).count();
                   num_iteration ++;
               }
           const ImVec2 p = ImGui::GetCursorScreenPos();
            float x = p.x + current_state.block_size, y = p.y +
current state.block size;
            for (size_t i = 0; i < current_state.room_size; ++i) {</pre>
               for (size_t j = 0; j < current_state.room_size; ++j) {</pre>
                   auto temp = (*grid)[{i, j}];
                   auto color = temp_to_color(temp);
                   draw_list->AddRectFilled(ImVec2(x, y), ImVec2(x +
current_state.block_size, y + current_state.block_size), color);
                   y += current_state.block_size;
               x += current_state.block_size;
               y = p.y + current_state.block_size;
           if (finished) {
               ImGui::Text("stabilized in %lf ms", (double) duration /
1'000'000);
           else if (num_iteration >= max_iteration) {
               ImGui::Text("%d iterations reached in %lf ms",
max_iteration, (double) duration / 1'000'000);
            }
           ImGui::End();
```

```
});
    }
   else {
       while (num_iteration < max_iteration) {</pre>
           if (!finished) {
               if (current_state.algo == hdist::Algorithm::Jacobi) {
                   local finished = (int)
hdist::calculate_jacobi(current_state, *grid, tid, chunk);
               else if (current_state.algo == hdist::Algorithm::Sor) {
                   local_finished = (int)
hdist::calculate_sor(current_state, *grid, tid, chunk, 0);
                   // sync threads for switching buffer
                   pthread barrier wait(&barrier);
                   pthread barrier wait(&barrier);
                   local_finished = (int)
hdist::calculate_sor(current_state, *grid, tid, chunk, 1);
               pthread_mutex_lock(&mutex);
               // update the global status (finished or not)
               finished &= local_finished;
               pthread_mutex_unlock(&mutex);
               // sync threads for switching buffer
               pthread barrier wait(&barrier);
               // wait thread 0 to switch buffer
               pthread_barrier_wait(&barrier);
           num_iteration ++;
   return nullptr;
int main(int argc, char **argv) {
    if (argc < 2) {
       exit(1);
    int num_threads = atoi(argv[1]);
   if (argc >= 3) {
       current_state.room_size = atoi(argv[2]);
       current_state.source_x = current_state.room_size / 2;
```

```
current_state.source_y = current_state.room_size / 2;
}
if (argc >= 4) {
   max_iteration = atoi(argv[3]);
if (argc >= 5) {
   int algo = atoi(argv[4]);
   if (algo == 0) {
       current state.algo = hdist::Algorithm::Jacobi;
   else {
        current_state.algo = hdist::Algorithm::Sor;
chunk = (current_state.room_size + num_threads - 1) / num_threads;
int capacity = chunk * num_threads;
grid = new hdist::Grid{
   static_cast<size_t>(current_state.room_size),
   static_cast<size_t>(capacity),
   current_state.border_temp,
   current_state.source_temp,
   static_cast<size_t>(current_state.source_x),
    static_cast<size_t>(current_state.source_y)};
pthread_barrier_init(&barrier, nullptr, num_threads);
pthread_t threads[num_threads];
int tids[num_threads];
for (int i = 0; i < num_threads; i++) {</pre>
   tids[i] = i;
   void* tid = (void*) &tids[i];
   pthread_create(&threads[i], NULL, gui_loop, tid);
for (auto &i : threads) {
   pthread_join(i, nullptr);
}
return 0;
```

3. OpenMP Version

```
#include <graphic/graphic.hpp>
#include <imgui_impl_sdl.h>
#include <cstring>
#include <chrono>
#include <hdist/hdist.hpp>
#include <omp.h>
template<typename ...Args>
void UNUSED(Args &&... args [[maybe_unused]]) {}
ImColor temp_to_color(double temp) {
   auto value = static_cast<uint8_t>(temp / 100.0 * 255.0);
   return {value, 0, 255 - value};
int main(int argc, char **argv) {
    if (argc < 2) {
       exit(1);
   int n_threads = atoi(argv[1]);
   hdist::State current_state, last_state;
   bool first = true;
   int finished = 0;
   int local_finished = finished;
   int max_iteration = 100;
    int chunk = 0;
   if (argc >= 3) {
       current_state.room_size = atoi(argv[2]);
       current_state.source_x = current_state.room_size / 2;
       current_state.source_y = current_state.room_size / 2;
   if (argc >= 4) {
       max_iteration = atoi(argv[3]);
   if (argc >= 5) {
       int algo = atoi(argv[4]);
       if (algo == 0) {
           current_state.algo = hdist::Algorithm::Jacobi;
```

```
else {
           current state.algo = hdist::Algorithm::Sor;
   chunk = (current_state.room_size + n_threads - 1) / n_threads;
   int capacity = chunk * n_threads;
   hdist::Grid grid(
       static_cast<size_t>(current_state.room_size),
       static_cast<size_t>(capacity),
       current_state.border_temp,
       current_state.source_temp,
       static cast<size t>(current state.source x),
       static_cast<size_t>(current_state.source_y));
   omp_lock_t lock;
   omp_init_lock(&lock);
   #pragma omp parallel num_threads(n_threads)
       long tid = omp_get_thread_num();
       int num_iteration = 0;
       if (0 == tid) {
           static std::chrono::high_resolution_clock::time_point begin,
end;
           static size_t duration = 0;
           static const char* algo_list[2] = { "jacobi", "sor" };
           graphic::GraphicContext context{"Assignment 4"};
           context.run([&](graphic::GraphicContext *context
[[maybe_unused]], SDL_Window *) {
               auto io = ImGui::GetIO();
               ImGui::SetNextWindowPos(ImVec2(0.0f, 0.0f));
               ImGui::SetNextWindowSize(io.DisplaySize);
               ImGui::Begin("Assignment 4", nullptr,
                           ImGuiWindowFlags NoMove
                           | ImGuiWindowFlags_NoCollapse
                           │ ImGuiWindowFlags_NoTitleBar
                           ImGuiWindowFlags_NoResize);
               ImDrawList *draw list = ImGui::GetWindowDrawList();
               ImGui::Text("Application average %.3f ms/frame (%.1f
FPS)", 1000.0f / ImGui::GetIO().Framerate,
                          ImGui::GetIO().Framerate);
```

```
ImGui::DragInt("Room Size", &current_state.room_size,
10, 200, 1600, "%d");
               ImGui::DragFloat("Block Size",
&current state.block size, 0.01, 0.1, 10, "%f");
               ImGui::DragFloat("Source Temp",
&current_state.source_temp, 0.1, 0, 100, "%f");
               ImGui::DragFloat("Border Temp",
&current_state.border_temp, 0.1, 0, 100, "%f");
               ImGui::DragInt("Source X", &current_state.source_x, 1,
1, current_state.room_size - 2, "%d");
               ImGui::DragInt("Source Y", &current_state.source_y, 1,
1, current_state.room_size - 2, "%d");
               ImGui::DragFloat("Tolerance", &current_state.tolerance,
0.01, 0.01, 1, "%f");
               ImGui::ListBox("Algorithm", reinterpret_cast<int</pre>
*>(&current_state.algo), algo_list, 2);
               if (current state.algo == hdist::Algorithm::Sor) {
                   ImGui::DragFloat("Sor Constant",
&current_state.sor_constant, 0.01, 0.0, 20.0, "%f");
               // GUI paramater adjustment is disbled
               // if (current state.room size != last state.room size)
                      grid = hdist::Grid{
                              static_cast<size_t>(current_state.room_siz
                              current state.border temp,
                              current_state.source_temp,
                              static_cast<size_t>(current_state.source_x
                              static_cast<size_t>(current_state.source_y
               // if (current_state != last_state) {
                      finished = false;
               if (first) {
```

```
first = false;
                   finished = 0;
               if (!finished) {
                   if (num_iteration < max_iteration) {</pre>
                       begin =
std::chrono::high_resolution_clock::now();
                       if (current_state.algo ==
hdist::Algorithm::Jacobi) {
                           local_finished = (int)
hdist::calculate_jacobi(current_state, grid, tid, chunk);
                       else if (current state.algo ==
hdist::Algorithm::Sor) {
                           local finished = (int)
hdist::calculate_sor(current_state, grid, tid, chunk, 0);
                           // sync threads and switch buffer
                           #pragma omp barrier
                           grid.switch_buffer();
has been switched
                           #pragma omp barrier
                           local_finished = (int)
hdist::calculate_sor(current_state, grid, tid, chunk, 1);
                       omp_set_lock(&lock);
                       // update the global status (finished or not)
                       finished &= local_finished;
                       omp unset lock(&lock);
                       #pragma omp barrier
                       grid.switch_buffer();
                       // acknowledge other threads that the buffer has
been switched
                       #pragma omp barrier
                       end = std::chrono::high_resolution_clock::now();
                       duration +=
duration_cast<std::chrono::nanoseconds>(end - begin).count();
                       num iteration ++;
```

```
const ImVec2 p = ImGui::GetCursorScreenPos();
               float x = p.x + current_state.block_size, y = p.y +
current state.block size;
               for (size_t i = 0; i < current_state.room_size; ++i) {</pre>
                   for (size_t j = 0; j < current_state.room_size; ++j)</pre>
                       auto temp = grid[{i, j}];
                       auto color = temp_to_color(temp);
                       draw_list->AddRectFilled(ImVec2(x, y), ImVec2(x +
current_state.block_size, y + current_state.block_size), color);
                       y += current_state.block_size;
                   x += current_state.block_size;
                   y = p.y + current_state.block_size;
               if (finished) {
                   ImGui::Text("stabilized in %lf ms", (double)
duration / 1'000'000);
               else if (num_iteration >= max_iteration) {
                   ImGui::Text("%d iterations reached in %lf ms",
max iteration, (double) duration / 1'000'000);
               ImGui::End();
            });
       else {
           while (num_iteration < max_iteration) {</pre>
               if (!finished) {
                   if (current_state.algo == hdist::Algorithm::Jacobi)
                       local finished = (int)
hdist::calculate jacobi(current state, grid, tid, chunk);
                   else if (current_state.algo ==
hdist::Algorithm::Sor) {
                       local_finished = (int)
hdist::calculate_sor(current_state, grid, tid, chunk, 0);
                       // sync threads for switching buffer
                       #pragma omp barrier
```

4. CUDA Version

```
#include <graphic/graphic.hpp>
#include <imgui_impl_sdl.h>
#include <cstring>
#include <chrono>
#include <hdist/hdist.hpp>
#include <cuda.h>
#include <cuda_runtime.h>
#include <device_launch_parameters.h>
#include <inttypes.h>

template<typename ...Args>
void UNUSED(Args &&... args [[maybe_unused]]) {}

ImColor temp_to_color(double temp) {
    auto value = static_cast<uint8_t>(temp / 100.0 * 255.0);
    return {value, 0, 255 - value};
}
```

```
global__ void calculate(hdist::Grid* grid,
                           hdist::State* current_state,
                           int* chunk,
                           bool* finished,
                           int* lock) {
   int tid = threadIdx.x;
   bool local finished = false;
   if (current_state->algo == hdist::Algorithm::Jacobi) {
       local finished = hdist::calculate jacobi(current state, grid,
tid, *chunk);
   else if (current_state->algo == hdist::Algorithm::Sor) {
       local_finished = hdist::calculate_sor(current_state, grid, tid,
*chunk, 0);
        __syncthreads();
       if (tid == 0) {
           grid->switch_buffer();
       syncthreads();
       local_finished = hdist::calculate_sor(current_state, grid, tid,
*chunk, 1);
   while (*lock != 0) {};
   *lock = 1;
   // update the global status (finished or not)
   *finished &= local_finished;
   *lock = 0;
   // sync threads and switch buffer
    __syncthreads();
   if (tid == 0) {
       grid->switch_buffer();
    }
int main(int argc, char **argv) {
   if (argc < 2) {
       exit(1);
   int num_threads = atoi(argv[1]);
   bool first = true;
```

```
bool finished = false;
hdist::State current_state; //, last_state;
int max_iteration = 100;
int chunk = 0;
int num iteration = 0;
if (argc >= 3) {
   current_state.room_size = atoi(argv[2]);
   current_state.source_x = current_state.room_size / 2;
   current_state.source_y = current_state.room_size / 2;
if (argc >= 4) {
   max_iteration = atoi(argv[3]);
if (argc >= 5) {
   int algo = atoi(argv[4]);
   if (algo == 0) {
       current_state.algo = hdist::Algorithm::Jacobi;
   else {
       current_state.algo = hdist::Algorithm::Sor;
chunk = (current state.room size + num threads - 1) / num threads;
int capacity = chunk * num_threads;
auto grid = hdist::Grid{
   static_cast<size_t>(current_state.room_size),
   static cast<size t>(capacity),
   current_state.border_temp,
   current_state.source_temp,
   static_cast<size_t>(current_state.source_x),
   static_cast<size_t>(current_state.source_y)};
cudaError_t cudaStatus;
hdist::Grid* cuda grid;
hdist::State* cuda_current_state;
int* cuda_chunk;
bool* cuda_finished;
int* cuda_lock;
double* cuda_data0;
double* cuda_data1;
```

```
size_t cuda_current_buffer;
   int array_size = current_state.room_size * capacity *
sizeof(double);
   cudaMallocManaged((void**) &cuda grid, sizeof(grid));
   cudaMemcpy(cuda_grid, &grid, sizeof(grid), cudaMemcpyHostToDevice);
   cudaMallocManaged((void**) &cuda_current_state,
sizeof(current_state));
    cudaMemcpy(cuda current state, &current state,
sizeof(current_state), cudaMemcpyHostToDevice);
   cudaMallocManaged((void**) &cuda_chunk, sizeof(int));
   cudaMemcpy(cuda_chunk, &chunk, sizeof(int), cudaMemcpyHostToDevice);
   cudaMallocManaged((void**) &cuda_finished, sizeof(bool));
   cudaMemcpy(cuda finished, &finished, sizeof(bool),
cudaMemcpyHostToDevice);
   cudaMallocManaged((void**) &cuda lock, sizeof(int));
   cudaMemset(cuda_lock, 0, sizeof(int));
   cudaMallocManaged((void**) &cuda_data0, array_size);
   cudaMallocManaged((void**) &cuda_data1, array_size);
   cuda_grid->data0 = cuda_data0;
   cuda grid->data1 = cuda data1;
   cudaMemcpy(cuda_grid->data0, grid.data0, array_size,
cudaMemcpyHostToDevice);
   cudaMemcpy(cuda_grid->data1, grid.data1, array_size,
cudaMemcpyHostToDevice);
   static std::chrono::high_resolution_clock::time_point begin, end;
   static size t duration = 0;
   static const char* algo_list[2] = { "jacobi", "sor" };
   graphic::GraphicContext context{"Assignment 4"};
   context.run([&](graphic::GraphicContext *context [[maybe_unused]],
SDL_Window *) {
       auto io = ImGui::GetIO();
       ImGui::SetNextWindowPos(ImVec2(0.0f, 0.0f));
       ImGui::SetNextWindowSize(io.DisplaySize);
       ImGui::Begin("Assignment 4", nullptr,
                   ImGuiWindowFlags NoMove
                   | ImGuiWindowFlags_NoCollapse
                   | ImGuiWindowFlags_NoTitleBar
                   ImGuiWindowFlags_NoResize);
       ImDrawList *draw list = ImGui::GetWindowDrawList();
       ImGui::Text("Application average %.3f ms/frame (%.1f FPS)",
1000.0f / ImGui::GetIO().Framerate,
                   ImGui::GetIO().Framerate);
```

```
ImGui::DragInt("Room Size", &current_state.room_size, 10, 200,
1600, "%d");
       ImGui::DragFloat("Block Size", &current_state.block_size, 0.01,
0.1, 10, "%f");
       ImGui::DragFloat("Source Temp", &current_state.source_temp, 0.1,
0, 100, "%f");
       ImGui::DragFloat("Border Temp", &current_state.border_temp, 0.1,
0, 100, "%f");
       ImGui::DragInt("Source X", &current state.source x, 1, 1,
current_state.room_size - 2, "%d");
       ImGui::DragInt("Source Y", &current_state.source_y, 1, 1,
current_state.room_size - 2, "%d");
       ImGui::DragFloat("Tolerance", &current_state.tolerance, 0.01,
0.01, 1, "%f");
       ImGui::ListBox("Algorithm", reinterpret_cast<int</pre>
*>(&current state.algo), algo list, 2);
       if (current state.algo == hdist::Algorithm::Sor) {
           ImGui::DragFloat("Sor Constant",
&current_state.sor_constant, 0.01, 0.0, 20.0, "%f");
       // GUI paramater adjustment is disbled
       // if (current state.room size != last state.room size) {
              grid = hdist::Grid{
                      static_cast<size_t>(current_state.room_size),
                      current_state.border_temp,
                      current_state.source_temp,
                      static cast<size t>(current state.source x),
                      static_cast<size_t>(current_state.source_y)};
              first = true;
       // if (current state != last state) {
       if (first) {
           first = false;
           finished = 0;
```

```
if (!finished) {
           if (num_iteration < max_iteration) {</pre>
               begin = std::chrono::high_resolution_clock::now();
               // Launch GPU kernel
               calculate<<<1, num_threads>>>(cuda_grid,
                                               cuda_current_state,
                                               cuda_chunk,
                                               cuda finished,
                                               cuda lock);
               // Wait GPU to complete calculation
               cudaDeviceSynchronize();
               cudaStatus = cudaGetLastError();
               if (cudaStatus != cudaSuccess) {
                   fprintf(stderr, "mykernel launch failed: %s\n",
                           cudaGetErrorString(cudaStatus));
                   return 0;
               // Get the finished status
               cudaMemcpy(&finished, cuda_finished, sizeof(bool),
cudaMemcpyDeviceToHost);
               end = std::chrono::high_resolution_clock::now();
               duration +=
std::chrono::duration_cast<std::chrono::nanoseconds>(end -
begin).count();
               num_iteration ++;
       const ImVec2 p = ImGui::GetCursorScreenPos();
       float x = p.x + current_state.block_size, y = p.y +
current_state.block_size;
       // Receive data from device
       cudaMemcpy(&cuda_current_buffer, &cuda_grid->current_buffer,
                   sizeof(size_t), cudaMemcpyDeviceToHost);
       if (cuda current buffer == 0)
       {
           cudaMemcpy(grid.get_current_buffer(), cuda_grid->data0,
                       array_size, cudaMemcpyDeviceToHost);
       }
       else {
           cudaMemcpy(grid.get_current_buffer(), cuda_grid->data1,
```

```
array_size, cudaMemcpyDeviceToHost);
       for (size_t i = 0; i < current_state.room_size; ++i) {</pre>
            for (size_t j = 0; j < current_state.room_size; ++j) {</pre>
               auto temp = grid[{i, j}];
               auto color = temp_to_color(temp);
               draw_list->AddRectFilled(ImVec2(x, y), ImVec2(x +
current_state.block_size, y + current_state.block_size), color);
               y += current_state.block_size;
           x += current_state.block_size;
           y = p.y + current_state.block_size;
       if (finished) {
           ImGui::Text("stabilized in %lf ms", (double) duration /
1'000'000);
       else if (num_iteration >= max_iteration) {
            ImGui::Text("%d iterations reached in %lf ms",
max_iteration, (double) duration / 1'000'000);
        ImGui::End();
    });
    return 0;
```