First show that Rayleigh Principle. H is Hermitian. $\min \langle Hu, u \rangle = \lambda n$ || U||=1 where In is the least eigenvalue of H H is Hermitian. The eigenvalues $\lambda_1 \geqslant \lambda_2 \geqslant -\lambda_n$ of H are real and we can find the corresponding orthonormal eignvectors u', u2, -- un. $\|u^i\| = \sqrt{\langle u^i, u^i \rangle} = 1$ $\langle u^{\lambda}, u^{\delta} \rangle = 0$ for $\lambda \neq j$ $< H u^i, u^i > = \lambda_i$ $< H u^i, u^i > = 0$ for $\lambda \neq i$ For every unit vector u can be written as the linear combination of u', u2 -- un $U = C_1 U' + C_2 U^2 + \cdots + C_n U^n$ Where |C1|2+ |C2|2+ ... + |Cn|2=1 $< HU, U> = < H(C_1U^1 + C_2U^2 + \dots + C_nU^n), U>$ $= \sum_{i} |C_{i}|^{2} \lambda_{i} ||\mathbf{u}^{i}||^{2} \geq \sum_{i} |C_{i}|^{2} \lambda_{n} = \lambda_{n}$ (In is the least eight value) Thus, Min < Hu, u > = 2n equality if u=v".

0 11 04) 1 6 2 6 7 1 2

Show that $\lambda_n = \min_{x \neq 0} \frac{\langle Hx, x \rangle}{\langle x, x \rangle}$ $x \neq 0$, $ut \quad u = \frac{x}{||x||}$ be a unit vector From D, Min < Hu. u> = 2n $\min_{X \neq 0} < H \frac{X}{\|X\|}, \frac{X}{\|X\|} > = \lambda_n$ $\frac{1}{2} \lim_{x \to 0} \frac{\langle H \chi, \chi \rangle}{\langle \chi, \chi \rangle} = \lambda_n$ $H = \begin{bmatrix} 1 & 2 & 3 \\ 2 & M & 4 \end{bmatrix}$ His a Fermitian mairix $\begin{bmatrix} 3 & 4 & 5 \end{bmatrix}$ If His positive definite } det([2 M]) >0 - 0 det ([1 2 3 /)) 0 - @ From O, M-4>0, M>4-0

5M+24+24-9N-16-2020

4M < 12, M < 3 - 9

From @

From (3), @ M>4 and M<3 Contradiction! There is no solution of M. $|X|_{\infty} = \max_{k} |X_{k}|$, $|X|_{k} = \sum_{k} |X_{k}|$ (U Show that Ixlow is a norm. Check - three properties. Q = X = C, $|X|_{\infty} = \max_{k} |X_k| = 0$ $X \neq 0$, $|X|_{\infty} = \max_{x} |X_{x}| \geq 0$ ② $\alpha \neq 0$, $|\alpha \times |_{\infty} = |\alpha \times |\alpha \times |_{\infty} = |\alpha| \cdot |\alpha| \cdot |\alpha \times |_{\infty} = |\alpha| \cdot |\alpha$ 3 $|X+Y|_{\infty} = \max_{k} |X_{k} + Y_{k}| \leq \max_{k} |X_{k}| + |Y_{k}| = |X_{\infty} + |Y_{\infty}|$ Hera. IXIO is a norm Show that IXI is a norm (2) - Check three properties. X=0, $X=\sum_{i} X_{i} X_{i} = 0$ Hace, IXI, is a norm

(3) Find the matrix norm for
$$[\times]_1$$

$$|\times|_1 = \sum_{i \in X_i} \{y_{i}\}, \quad |X_i|_1 = \sum_{i \in X_i} \{y_{i}\}, \quad |X_i|_1 = \sum_{i \in X_i} \{x_{i}\}, \quad |X_i|_1 = |X_i|_1 =$$

