

# Islington College



## MA4001NI Logic and Problem Solving Group Coursework (50% Weighted)

### Submitted By:

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## 1. Problem 1 Solution

When a taxing body, typically the government, puts a financial responsibility on its citizens or residents, it is referred to as taxation. Since ancient times, paying taxes to governments or officials has been a fundamental aspect of civilization.

The word "taxation" refers to all kinds of compulsory charges, including capital gains, income, and estate taxes. While taxes can be either verbs or nouns, they are typically described as acts, and the money that is collected as a result is known as "taxes." (Janssen, 1999)

Income:

Their overall earnings, including their salary and wages, investment returns, pension payouts, and other receipts, are referred to as their income. For businesses, income consists of the money they make from selling goods and services as well as any interest or dividends they get from their business-related cash accounts and reserves. It acts as the primary source when calculating taxes. (Janssen, 1999)

Tax deduction:

A deduction from taxes is an arrangement that lowers taxable income. One deduction at a set amount is known as a standard deduction. Higher-income taxpayers who frequently have large deductible expenses (Jr, 1937)

Income Tax Bracket:

The range of incomes taxed at specific rates—which usually vary based on filing status—is known as a tax bracket. Rates increase in line with income under a progressive individual or corporate income tax system. The federal corporation income tax structure is flat, but there are seven federal individual income tax bands. (Jr, 1937)

**Tax Slab:**

This is a representation of each income tax bracket's width. It is the range of earnings that each bracket covers. Each tax slab in this chart is worth 250,000 Indian rupees.

**Tax Rate:**

The percentage that an organization or person must pay in taxes on their income is known as their tax rate. When an individual's or company's taxable income rises, so does the tax rate that is charged. Higher income people pay more in taxes under a progressive system. (Janssen, 1999)

**Tax Amount:**

Based on the taxable income and tax rate, this is the actual tax amount. It is calculated if the yearly taxable income is less than or equal to the tax slab. The tax rate is multiplied by Yearly taxable income (tax rate multiplied by tax slab)

**Taxable Income Left:**

This is what's remaining after the total revenue is subtracted by the tax amount. in the event that (yearly taxable income less the tax slab, 0, yearly taxable income less the tax slab). It displays the remaining income for each tax bracket.

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H22 :  $=IF(I21<=F22,G22*I21,G22*F22)$

	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P
4																
5																
6																
7			Yearly Income	13,550,010												
8																
9			Deductions:													
10																
11			Citizen Investment Trust (CIT)	326362												
12			Provident Fund (PF)	112,245												
13			Life Insurance	68,000												
14																
15			Total Deductions:	506607												
16																
17			Total Taxable Income	13,043,403												
18																
19																
20																
21																
22																
23																
24																
25																
26																
27																
28																
29																
30																
31																
32																
33																
34																

Sheet1

Figure 1 Screen shots for tax Template.



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SUM :  $\text{=IF(D17<=F21,G21*D17,G21*G21)}$

	A	B	C	D	E	F	G	H	I	J
4										
5										
6										
7			Yearly Income	13,550,010						
8										
9			Deductions:							
10										
11			Citizen Investment Trust (CIT)	326362						
12			Provident Fund (PF)	112,245						
13			Life Insurance	68,000						
14										
15			Total Deductions:	506607						
16										
17			Total Taxable Income	13,043,403						
18										
19										
20										
				<b>Income Tax Bracket</b>	<b>Tax slab</b>	<b>Tax Rate</b>	<b>Tax Amount</b>	<b>Taxable Income left</b>		
21				0	250000	250000	0%	G21*G21	12793403	
22				250,000	500,000	250,000	5%	12500	12543403	
23				500,000	750,000	250,000	10%	25000	12293403	
24				750,000	1000000	250,000	15%	37500	12043403	
25				1000000	1250000	250,000	20%	50000	11793403	
26				1250000	1500000	250,000	25%	62500	11543403	
27				Above	15,00,000	#VALUE!	30%	3463020.9		
28										
29										
						<b>Total Yearly Tax</b>		3650520.9		

Figure 2 Screen shots for Formula of Taxable amount 1

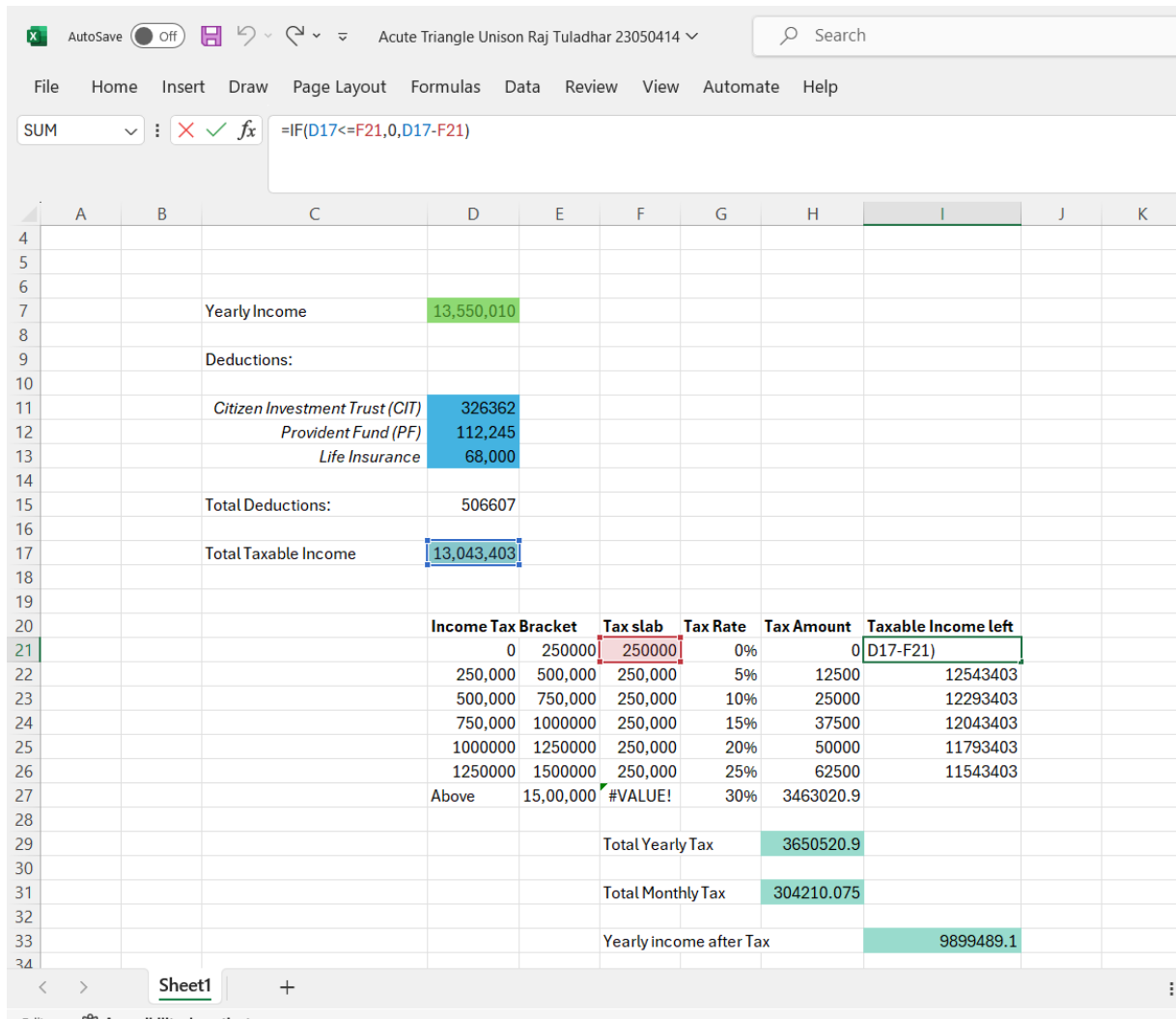


Figure 3 Screen shots for Formula of Taxable amount left 1.

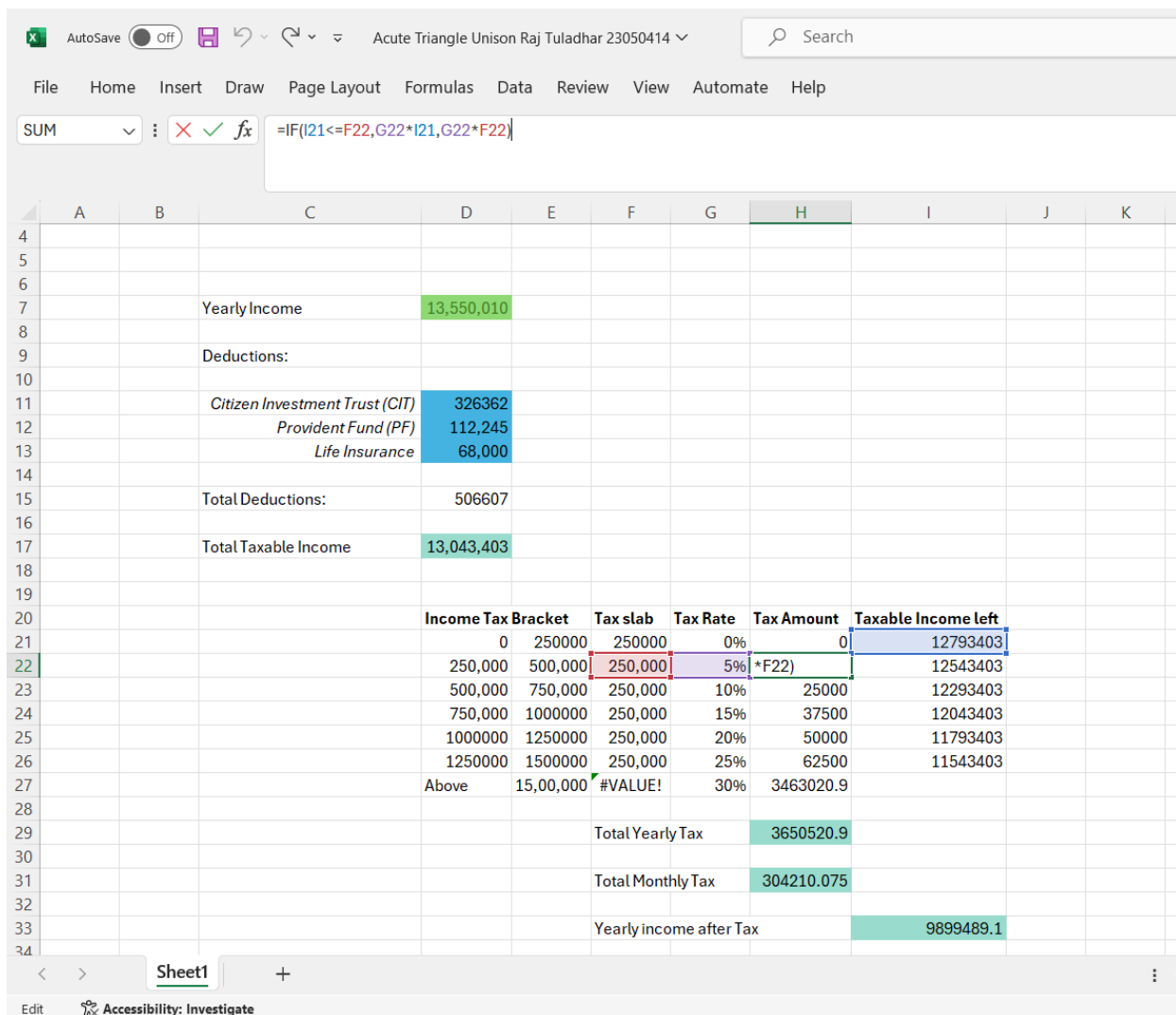


Figure 4 Screen shots for Formula of Tax amount 2.

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SUM :  $=IF(I21<=F22,0,I21-F22)$

	A	B	C	D	E	F	G	H	I	J	K
4											
5											
6											
7			Yearly Income	13,550,010							
8											
9			Deductions:								
10											
11			Citizen Investment Trust (CIT)	326362							
12			Provident Fund (PF)	112,245							
13			Life Insurance	68,000							
14											
15			Total Deductions:	506607							
16											
17			Total Taxable Income	13,043,403							
18											
19											
20				Income Tax Bracket	Tax slab	Tax Rate	Tax Amount	Taxable Income left			
21				0 250000	250000	0%	0	12793403			
22				250,000 500,000	250,000	5%	12500	F22)			
23				500,000 750,000	250,000	10%	25000	12293403			
24				750,000 1000000	250,000	15%	37500	12043403			
25				1000000 1250000	250,000	20%	50000	11793403			
26				1250000 1500000	250,000	25%	62500	11543403			
27				Above 15,00,000	#VALUE!	30%	3463020.9				
28											
29						Total Yearly Tax	3650520.9				
30											
31						Total Monthly Tax	304210.075				
32											
33						Yearly income after Tax		9899489.1			
34											

Sheet1 +

Figure 5 Screen shots for Formula of Taxable amount left 2.

The screenshot shows an Excel spreadsheet with the following data:

	A	B	C	D	E	F	G	H	I	J	K
4											
5											
6											
7			Yearly Income	13,550,010							
8			Deductions:								
9											
10											
11			Citizen Investment Trust (CIT)	326362							
12			Provident Fund (PF)	112,245							
13			Life Insurance	68,000							
14											
15			Total Deductions:	506607							
16											
17			Total Taxable Income	13,043,403							
18											
19											
20											
21											
22											
23											
24											
25											
26											
27											
28											
29											
30											
31											
32											
33											
34											

The formula bar shows:  $=I26*G27$

The tax bracket table is as follows:

Income Tax Bracket	Tax slab	Tax Rate	Tax Amount	Taxable Income left
0	250000	250000	0%	0
250,000	500,000	250,000	5%	12500
500,000	750,000	250,000	10%	25000
750,000	1000000	250,000	15%	37500
1000000	1250000	250,000	20%	50000
1250000	1500000	250,000	25%	62500
Above	15,00,000	#VALUE!	30%	=I26*G27

The final calculations are:

Total Yearly Tax		3650520.9
Total Monthly Tax		304210.075
Yearly income after Tax		9899489.1

Figure 6 Screen shots for Formula of for last income tax bracket.

Write a procedure, tax, to calculate (in Indian rupees, Rs.) the tax a person owes, depending on his/her income. Calculate the tax using this table:

Taxable income	Income tax rates ( in Percent)
0 to 250000	0%
250,000 to 500,000	5%
500,000 to 750000	10%
750,000 to 10,00,000	15%
10,00,000 to 12,50,000	20%
12,50,000 to 15,00,000	25%
15,00,000 and above	30%

The procedure should show.

- i) The salary,
- ii) The tax rate,
- iii) The amount of tax
- iv) The amount left after tax and
- v) Be able to deal with any input, valid or not.

Your tests of procedure should include the following values, which should be included in your final presentation.

a) tax (Rs. 4,005,000)

Deductions:

- Employees provident fund organization: (Rs. 415,330)

b) tax (Rs. 13,550,010)

Deductions:

- Employees provident fund organization: (Rs. 112,245)
- Life Insurance premium: (Rs. 68,000)

c) tax ( Rs. 620,000)

Deductions:

- Employees provident fund organization: (Rs. 17,007)
- Life Insurance premium: (Rs. 32,000)

d) tax ( Rs. 9,19,887)

Deductions:

Employees provident fund organization: (Rs. 92,224)

e) tax ( Rs. 18,009,000)

Deductions:

Employees provident fund organization: (114,221)

f) tax ( Rs. - 7,050,000)

Deductions:

Employees provident fund organization: (Rs. 88,526)

Soln:

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H21 :  $=IF(D17<=F21,G21*D17,G21*G21)$

	A	B	C	D	E	F	G	H	I	J	K	L	M
4													
5													
6													
7			Yearly Income	4,005,000									
8			Deductions:										
9													
10			Citizen Investment Trust (CIT)										
11			Provident Fund (PF)	415,330									
12			Life Insurance										
13													
14			Total Deductions:	415330									
15													
16			Total Taxable Income	3,589,670									
17													
18													
19													
20													
21													
22													
23													
24													
25													
26													
27													
28													
29													
30													
31													
32													
33													
34													

Sheet1

Ready Accessibility: Investigate

Figure 7: Screenshot for Test 1



The screenshot shows an Excel spreadsheet with the following data:

	A	B	C	D	E	F	G	H	I	J	K	L	M	N
4														
5														
6														
7			Yearly Income	13,550,010										
8														
9			Deductions:											
10														
11			Citizen Investment Trust (CIT)											
12			Employees provident fund organization	112,245										
13			Life Insurance premium	68,000										
14														
15			Total Deductions:	180,245										
16														
17			Total Taxable Income	13,369,765										
18														
19														
20														
21														
22														
23														
24														
25														
26														
27														
28														
29														
30														
31														
32														
33														
34														

	Income Tax Bracket	Tax slab	Tax Rate	Tax Amount	Taxable Income left
21	0 250000	250000	0%	0	13119765
22	250,000 500,000	250,000	5%	12500	12869765
23	500,000 750,000	250,000	10%	25000	12619765
24	750,000 1000000	250,000	15%	37500	12369765
25	1000000 1250000	250,000	20%	50000	12119765
26	1250000 1500000	250,000	25%	62500	11869765
27	Above 15,00,000	#VALUE!	30%	3560929.5	
29		Total Yearly Tax		3748429.5	
31		Total Monthly Tax		312369.125	
33		Yearly income after Tax			9801580.5

Figure 8 Screenshot for Test 2

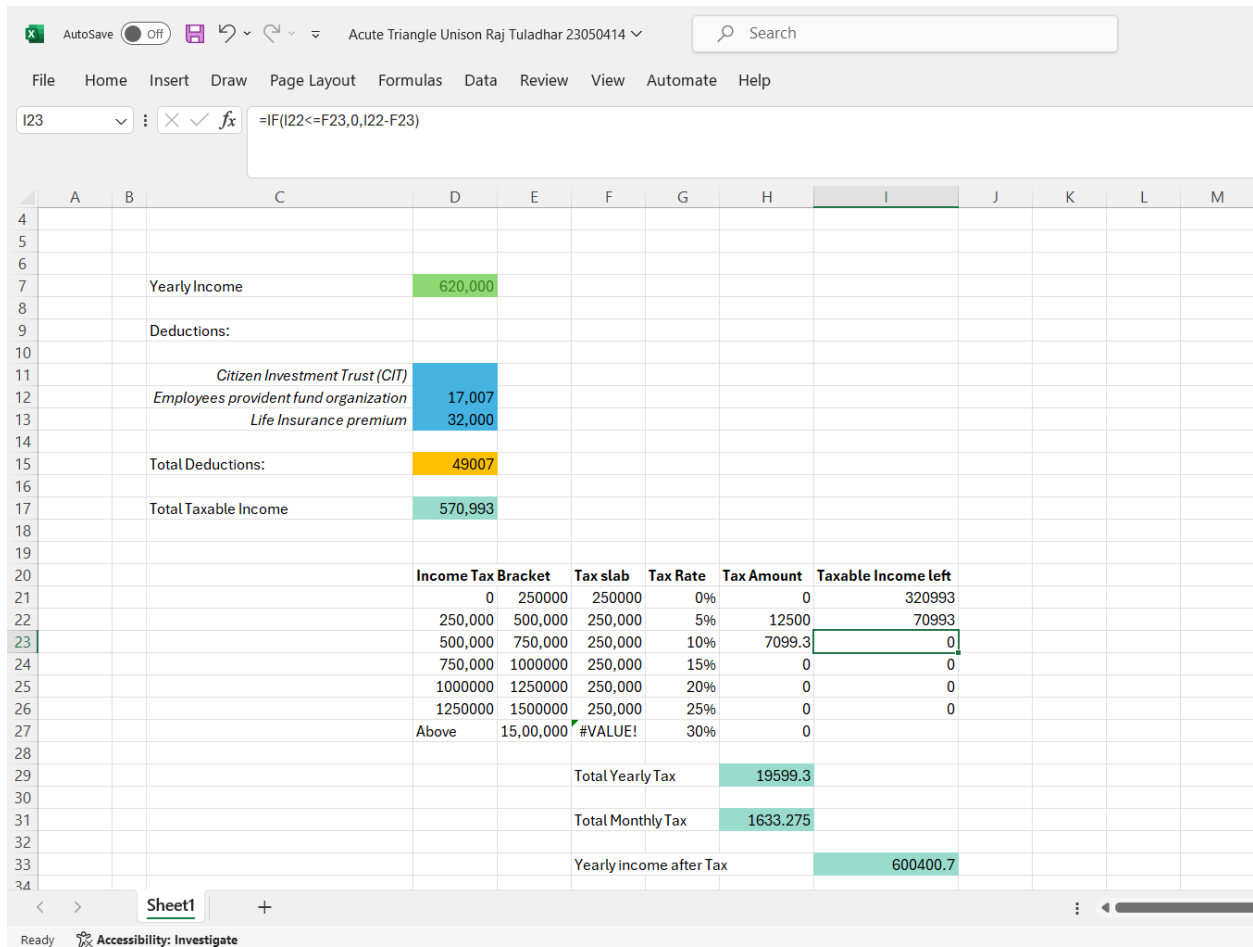


Figure 9 Screenshot for Test 3

<div> <div>AutoSave</div> <div>Off</div> <div>Acute Triangle Unison Raj Tuladhar 23050414</div> <div>Search</div> </div> <div> <div>File</div> <div>Home</div> <div>Insert</div> <div>Draw</div> <div>Page Layout</div> <div>Formulas</div> <div>Data</div> <div>Review</div> <div>View</div> <div>Automate</div> <div>Help</div> </div> <div> <div>I11</div> <div>fx</div> </div>													
	A	B	C	D	E	F	G	H	I	J	K	L	M
4													
5													
6													
7			Yearly Income	919,887									
8													
9			Deductions:										
10													
11			Citizen Investment Trust (CIT)										
12			Employees provident fund organization	92,224									
13			Life Insurance premium										
14													
15			Total Deductions:	92224									
16													
17			Total Taxable Income	827,663									
18													
19													
20				Income Tax Bracket	Tax slab	Tax Rate	Tax Amount	Taxable Income left					
21				0	250000	250000	0%	0	577663				
22				250,000	500,000	250,000	5%	12500	327663				
23				500,000	750,000	250,000	10%	25000	77663				
24				750,000	1000000	250,000	15%	11649.45	0				
25				1000000	1250000	250,000	20%	0	0				
26				1250000	1500000	250,000	25%	0	0				
27				Above	15,00,000	#VALUE!	30%	0					
28													
29							Total Yearly Tax	49149.45					
30													
31							Total Monthly Tax	4095.7875					
32													
33							Yearly income after Tax		870737.55				
34													

Figure 10 Screenshot for Test 4

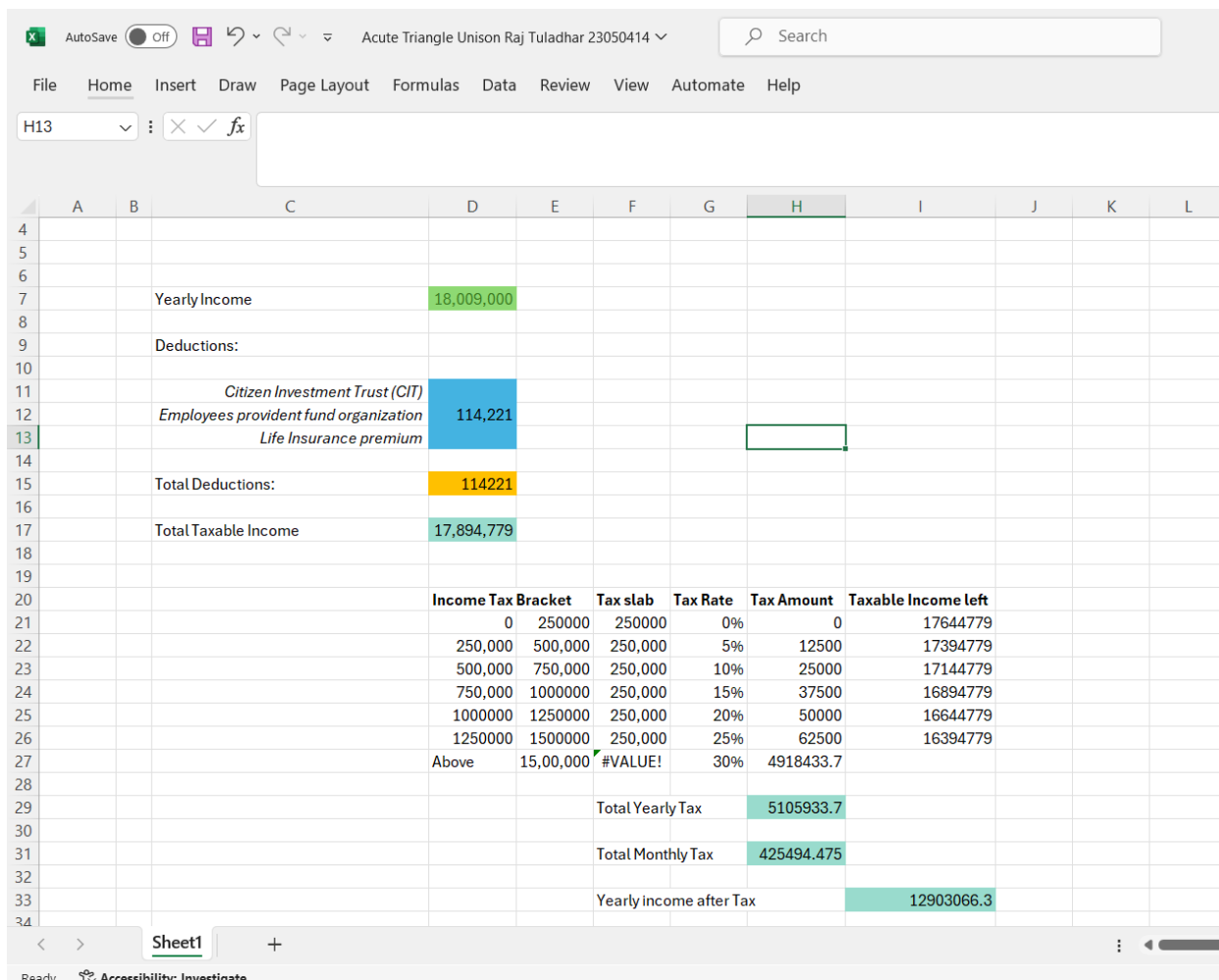


Figure 11 Screenshot for Test 5

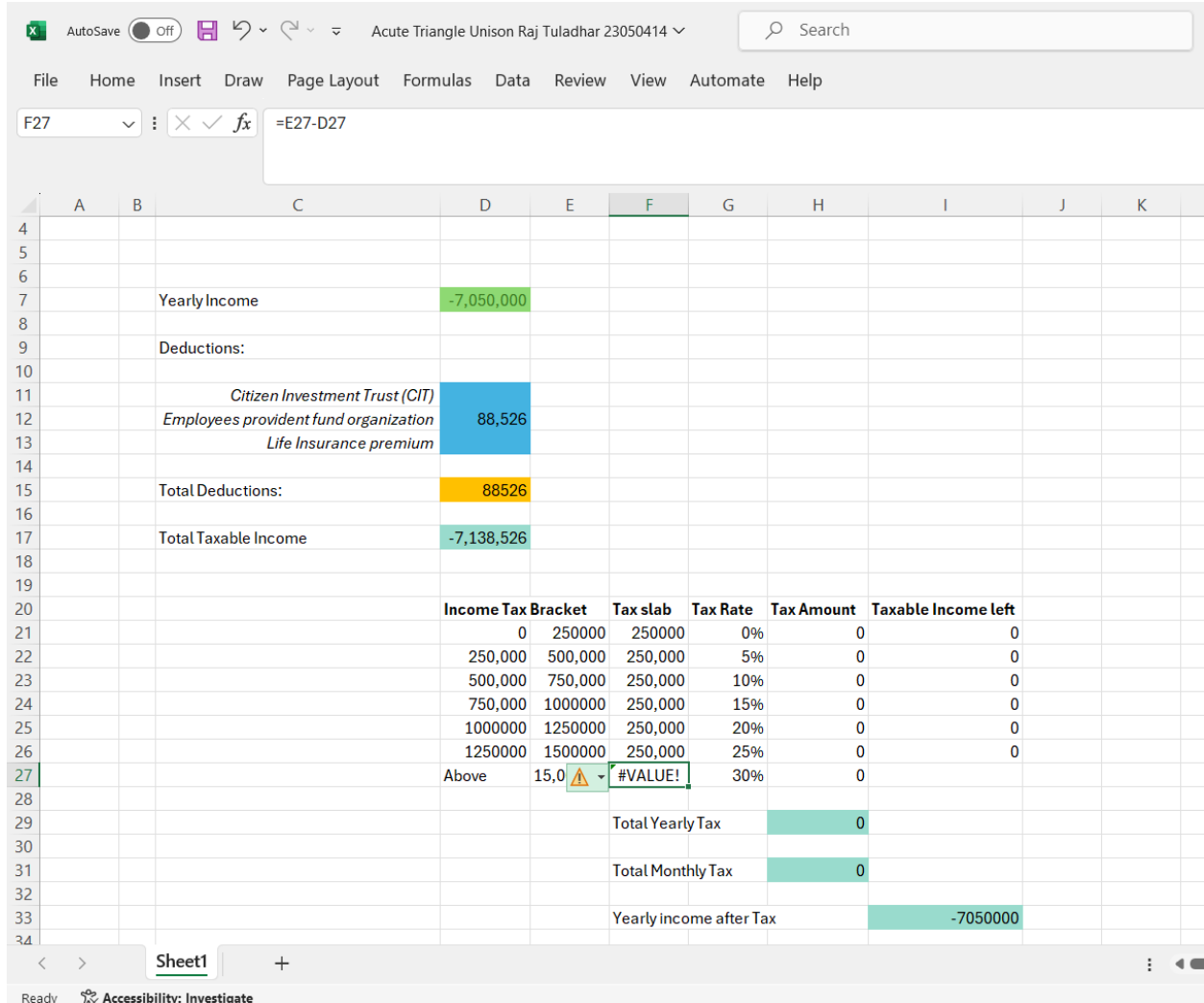


Figure 12 Screenshot for Test 6

## 2. Problem 2 Solution

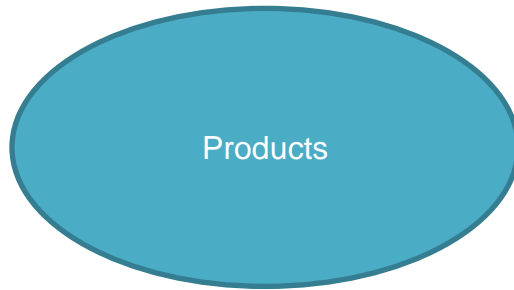
A) The Newcastle company manufactures three products: A, B and C. Their contribution to profit is \$3, \$5 and \$2 per unit respectively. The sales department currently has firm orders for 150 units of A and 100 units of C for the week which must be fulfilled. All three products must go through a bottleneck machine, which has only 80 hours of processing time available each week. The time requirements are 10, 10 and 5 minutes per unit for products A, B and C respectively.

### Questions

You should answer the following questions and incorporate your answers into a word-processed report to form part of your final pdf. The sections of your report should correspond to the individual questions following.

- a) Formulate the problem as a linear programming model, clearly defining the variables, the objective function, and the constraints.
- b) Solve the problem using Simplex method.
- c) Solve the problem using the Excel Solver and interpret the results.
- d) For the final part of your report, in your capacity as an Adviser, you should present a memorandum to the Newcastle Company. Describe your main conclusions in simple, non-technical English, i.e., do not use technical terms like variable, objective function, or dual price. Don't worry about repeating some or all the points that you have already made in answer to earlier questions. The aim is to communicate your conclusions clearly to someone who is knowledgeable about the combination of contents used in the production, but who knows nothing about the subject of linear programming. You may use tables and charts, if you wish.

A)



	A	B	C
Products	\$3	\$5	\$2
Time	10	10	5
Order in unit	150	-	100

Let X, Y, Z be the number of unit of A B and C respectively.

The maximum value of the function is  $(R) = 3x + 5y + 2z$

We have 80 hours of processing time which is converted into minutes.

$$10x + 10y + 5z \leq 4800$$

Other constraints are,

$$X = 150$$

$$Y = 100$$

Hence the final equations are

$$\text{Maximize}(Z) = 3x + 5y + 2z.$$

b) Soln

To maximize  $R = 3x + 5y + 2z$

Constraints,

$$x = 150$$

$$z = 100$$

$$10x + 10y + 5z \leq 4800$$

$$y \geq 0$$

Let  $A_1, A_2$  be the artificial variables &  $S_1$  be the slack variable.

$$x + A_1 = 150$$

$$z + A_2 = 100$$

$$10x + 10y + 5z + S_1 = 4800$$

$$x, y, z, A_1, A_2, S_1 \geq 0$$

Standard equation for the simplex table,

$$1.C - 3.x - 5.y - 2.z + 10A_1 + 10A_2 + 0.S_1 = 0$$

$$0.C + 1.x + 0.y + 0.z + 1.A_1 + 0.A_2 + 0.S_1 = 150$$

$$0.C + 0.x + 0.y + 1.z + 0.A_1 + 1.A_2 + 0.S_1 = 100$$

$$0.C + 10x + 10.y + 5.z + 0.A_1 + 0.A_2 + 1.S_1 = 4800$$

Simplex Table 1:

	R	$x$	$y$	$z$	$A_1$	$A_2$	$S_1$	Constant
$R_0$	1	-3	-5	-2	10	10	0	0
$R_1$	0	1	0	0	1	0	0	150
$R_2$	0	0	0	1	0	1	0	100
$R_3$	0	10	10	5	0	0	1	4800

$\therefore$  Since the artificial values are not zero So, we cannot convert it into zero



So,

$$\text{New } R_0 = \text{old } R_0 - 10x (R_1 + R_2 + R_3)$$

Old $R_0$	$-10x (R_1 + R_2 + R_3)$	New $R_0$
1	0	1
-3	-30	-33
-5	-20	-25
-2	-20	-22
10	-10	0
10	-10	0
0	-10	-10
0	-12100	-12100

Now,

Simple Table 2,

	R	$x$	$y$	$z$	$A_1$	$A_2$	$S_1$	Constant	Ratio
$R_0$	1	-33	-25	-22	0	0	-10	-12100	
$R_1$	0	1	0	0	1	0	0	150	$R_1 = 150$
$R_2$	0	0	0	1	0	1	0	100	$R_2 = \infty$
$R_3$	0	10	10	5	0	0	1	4800	$R_3 = 480$

Key column is  $x$ .

Key row is  $R_1$

Key element = 1

Here,

$R_1$  is the key row &  $x$  is the key column.

$$\text{New } R_1 = \frac{\text{Old } R_1}{\text{Key element}}$$

$$\therefore \text{New } R_1 = \frac{\text{Old } R_1}{1}$$

Updating  $R_1$   $R_2$  &  $R_3$  using formula

For  $R_0$

Old $R_0$	$- 33 \times \text{New } R_1$	New $R_0$
1	0	1
$- 33$	33	0
$- 25$	0	$-25$
$- 22$	0	$-22$
0	33	33
0	0	0
$-10$	0	$-10$
$-12100$	4950	$-7150$

$\therefore$  Since the value of  $R_2$  is subtracted by 0, So New  $R_2 = \text{Old } R_2$

For  $R_3$

Old $R_3$	$-2 \times \text{New } R_2$	New $R_3$
0	0	0
10	-2	0
10	0	2
5	0	1
0	-2	-2
0	0	0
1	0	1
4800	-300	660

Simplex Table 3:

	R	$x$	$y$	$z$	$A_1$	$A_2$	$S_1$	Constant	Ratio
$R_0$	1	0	-25	-22	33	0	-10	-7150	
$R_1$	0	1	0	0	1	0	0	150	$\infty$
$R_2$	0	0	0	1	0	1	0	100	$\infty$
$R_3$	0	0	2	1	-2	0	1	660	330

Key column =  $y$

Key row =  $R_3$

Key element = 2

Here,

$R_3$  is the key row so it must be updated first,

$$R_3 = \frac{\text{Old } R_2}{2}$$

$$\text{New } R_3 = 0, 0, 1, \frac{1}{2}, -1, 0, \frac{1}{2}, 330$$

Now,

For  $R_0, R_1, R_2$

$$\text{New } R_0 = \text{Old } R_0 - (-25) \times \text{New } R_3$$

$$\text{New } R_1 = \text{Old } R_1 - 0 \times \text{New } R_3$$

$$\text{New } R_2 = \text{Old } R_2 - 0 \times \text{New } R_3$$

For  $R_0$

Old $R_0$	$-33 \times \text{New } R_1$	New $R_0$
1	0	1
0	0	0
-25	25	0
-22	$\frac{25}{2}$	$-\frac{19}{2}$
33	-25	8
0	0	0
-10	$\frac{25}{2}$	$\frac{5}{2}$
-7150	8250	1100

Simplex Table 4

	R	$x$	$y$	$z$	$A_1$	$A_2$	$S_1$	Constant	Ratio
$R_0$	1	0	0	$-\frac{19}{2}$	8	0	$\frac{5}{2}$	1100	
$R_1$	0	1	0	0	1	0	0	150	$\infty$
$R_2$	0	0	0	1	0	1	0	100	100
$R_3$	0	0	1	1	-1	0	$\frac{1}{2}$	330	660

Key column =  $z$

Key row =  $R_3$

Key element = 1

Here,

$R_2$  is the key row so it must be updated.

First,

$$\text{New } R_2 = \frac{\text{Old } R_2}{1}$$

Similarly, For  $R_0, R_1, R_3$

$$\text{New } R_0 = \text{Old } R_0 - \left(-\frac{19}{2}\right) \times \text{New } R_2$$

$$\text{New } R_1 = \text{Old } R_1 - 0 \times \text{New } R_2$$

$$\text{New } R_3 = \text{Old } R_3 - \frac{1}{2} \times \text{New } R_2$$

For  $R_0$

Old $R_0$	$\pm \frac{19}{2} \times \text{New } R_2$	New $R_0$
1	0	1
0	0	0
0	0	0
$-\frac{19}{2}$	$\frac{19}{2}$	8
8	0	$\frac{19}{2}$
$\frac{5}{2}$	$\frac{19}{2}$	$\frac{5}{2}$
1100	950	2050

For  $R_2$

Old R <sub>3</sub>	$-\frac{1}{2} \times \text{New R}_2$	New R <sub>3</sub>
0	0	0
0	0	0
1	$-\frac{1}{2}$	1
$\frac{1}{2}$	0	0
-1	0	-1
0	$-\frac{1}{2}$	$-\frac{1}{2}$
$\frac{1}{2}$	0	$\frac{1}{2}$
330	-50	280

Simplex Table 5

	R	$x$	$y$	$z$	$A_1$	$A_2$	$S_1$	Constant
R <sub>0</sub>	1	0	0	0	8	$\frac{19}{2}$	$\frac{5}{2}$	2050
R <sub>1</sub>	0	1	0	0	1	0	0	150
R <sub>2</sub>	0	0	0	1	0	1	0	100
R <sub>3</sub>	0	0	1	0	-1	$-\frac{1}{2}$	$\frac{1}{2}$	330

Here all the constants of variables in R<sub>0</sub> is positive So this is the optimal condition.  $X = 150$ ,  $Y = 280$ ,  $Z = 100 \therefore R = 2050$

## B) Maximize and Minimize

$$z = 4x + 7y$$

Subjected to the constraints

$$2x + 3y \leq 60$$

$$x + y \geq 12$$

$$x \leq y$$

$$x \geq 0, y \geq 0$$

Sol<sup>n</sup>

Changing  $\leq, \geq$ , into =

$$2x + 3y = 60 \dots\dots\dots (i)$$

$$x + y = 12 \dots\dots\dots (ii)$$

$$x - y = 0 \dots\dots\dots (iii)$$

From eq<sup>n</sup> (i)  $2x + 3y \leq 60$

$x$	0	15	-30
$y$	20	10	40

From eq<sup>n</sup> (ii)  $x + y = 12$

$x$	6	-6	-30
$y$	6	18	42

From eq<sup>n</sup> (iii)  $x - y = 0$

$x$	0	15	15
$y$	0	10	15

Take (0,0) as a testing point,

$$2x + 3y = 60$$

$$2 \times 0 + 3 \times 0 \leq 60$$

$$0 \leq 60 \text{ [True]}$$

$\therefore$  It contains origin.

$$x + y \geq 12$$

$$0 + 0 \geq 12$$

$$0 \geq 12 \text{ [False]}$$

$\therefore$  It doesn't contains origin.

$$x - y \leq 0$$

$$0 - 0 \leq 0$$

$$0 \leq 0 \text{ [True]}$$

$\therefore$  It does contains origin.

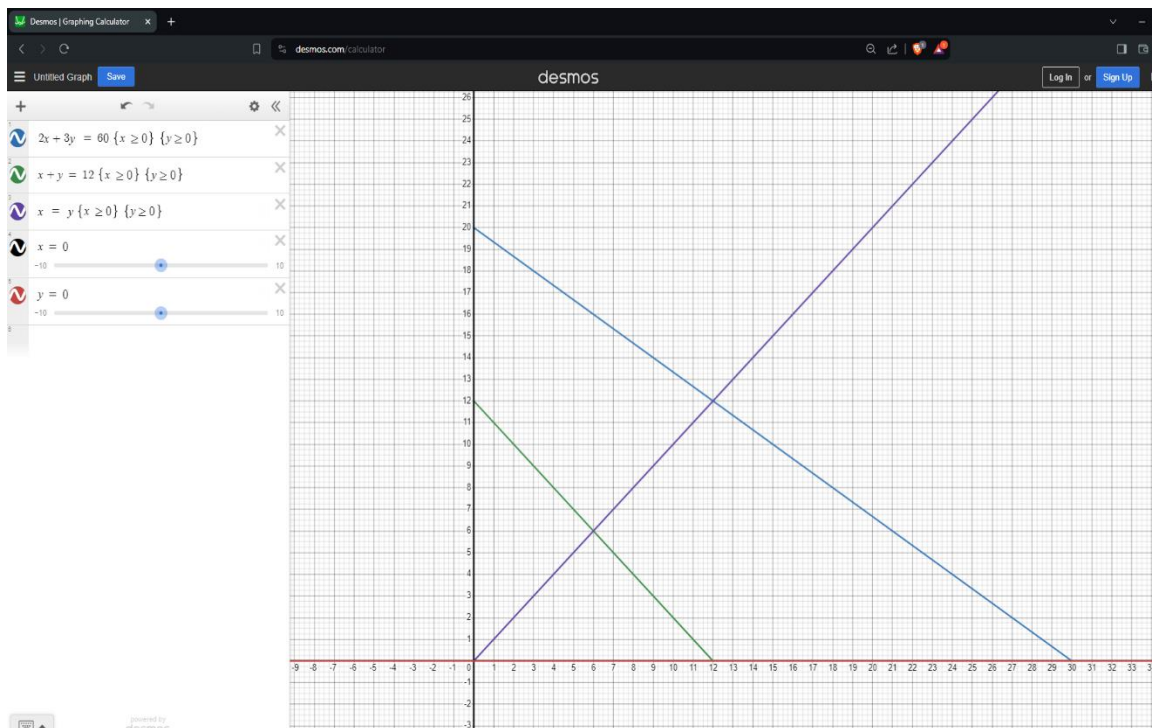


Figure 13: Screen shot for graph of question no 2.



The Feasible region is shaded and can be labelled as (0,20), (0,12), (6,6), (12,12).

Now,

Points	x	y	$Z = 4x + 7y$
(0,20)	0	20	140
(0,12)	0	12	84
(6,6)	6	6	66
(12,12)	12	12	132

Therefore, the maximum value is 140 when  $x = 0$  and  $y = 20$ .

Therefore, the minimum value is 66 when  $x = 6$  and  $y = 6$ .

## c) Excel solver and the interpret results

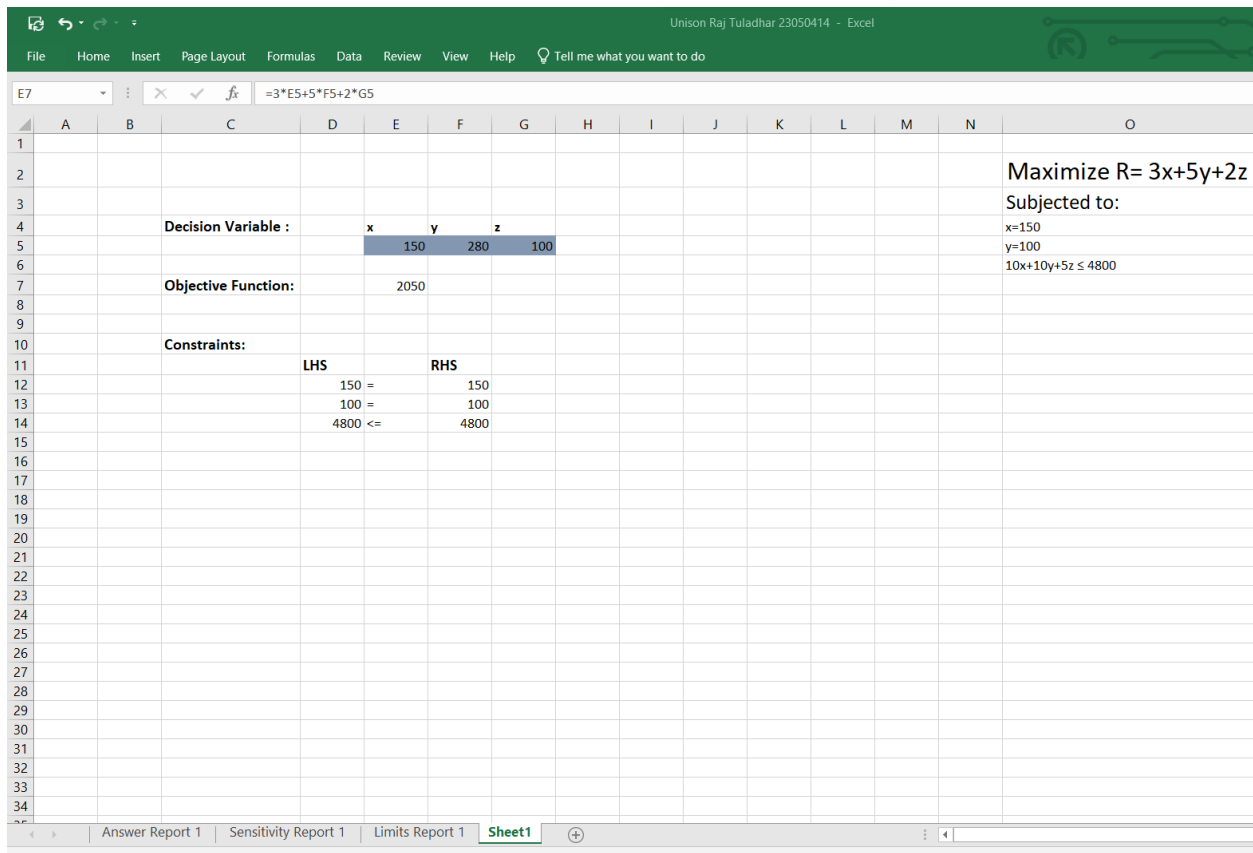


Figure 14: Solution of 2c using excel solver.

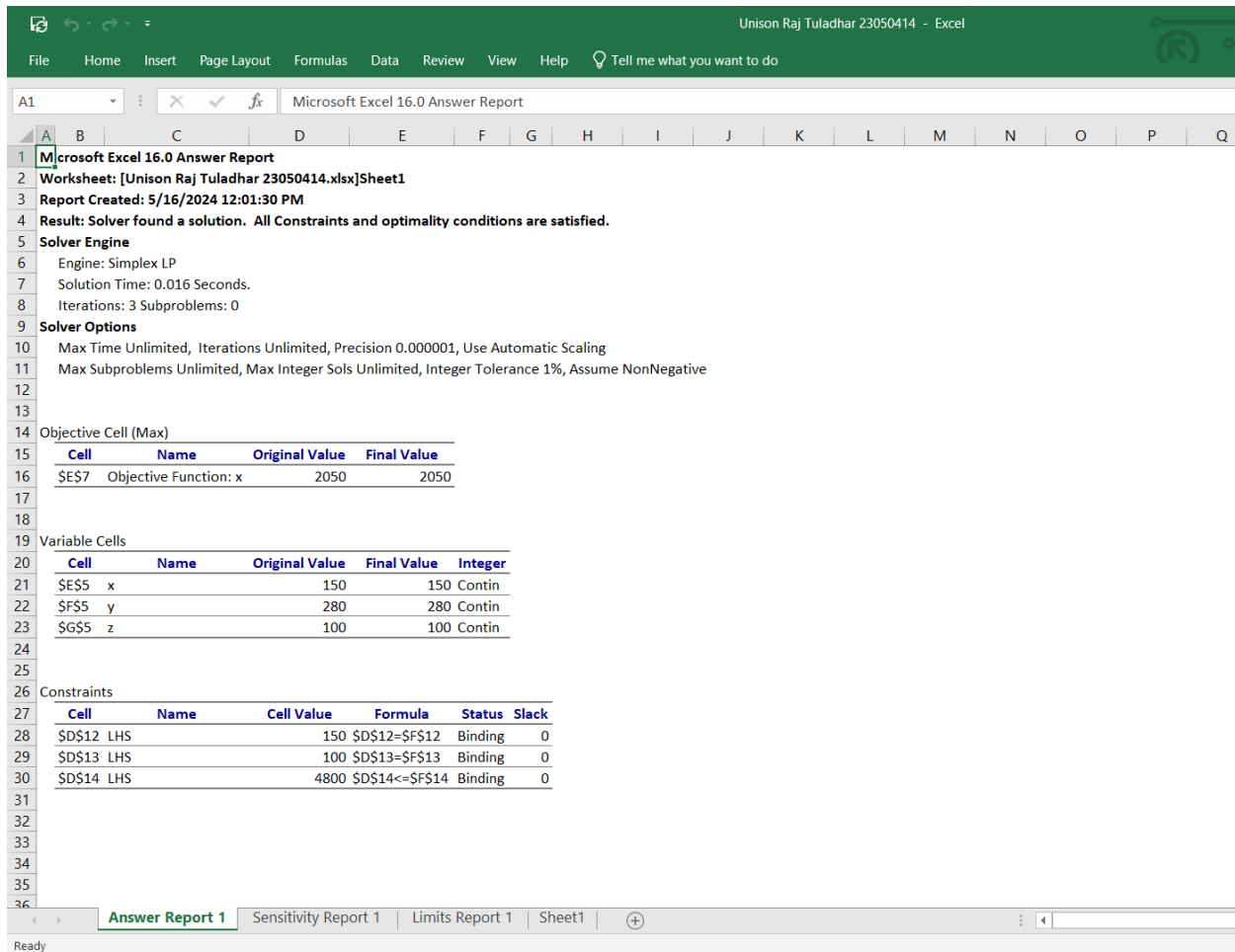


Figure 15: Solution of 2c using excel solver.



Microsoft Excel 16.0 Limits Report

Worksheet: [Unison Raj Tuladhar 23050414.xlsx]Sheet1

Report Created: 5/16/2024 12:01:30 PM

Objective		
Cell	Name	Value
\$E\$7	Objective Function: x	2050

Variable			Lower Limit	Objective Result	Upper Limit	Objective Result
Cell	Name	Value				
\$E\$5	x	150	150	2050	150	2050
\$F\$5	y	280	0	650	280	2050
\$G\$5	z	100	100	2050	100	2050

Figure 17: Solution of 2c using excel solver.

#### d) Memorandum

To: Newcastle Business

From: Math's Group,

Date: 15<sup>th</sup> May, 2024

Subject: Inferences and Suggestions

To Whom It May Concern,

After carefully examining everything, I discovered the following:

**Streamline Operations:** We can modify our resource allocation to ensure that we're getting the most out of what we have. This implies that we can produce more goods without increasing our costs.

**Save Money:** There are ways to reduce expenses without losing out on quality. By using more tactics, we can reduce costs without losing our income.

**Stay Ahead of the Curve:** It's critical to manufacture goods that consumers genuinely desire to purchase. We can prevent resource waste by keeping an eye on what is and is not selling.

**Make Plans for the Future:** We must plan ahead and consider what will make us successful in the long run. This could entail taking risks or getting ready for market shifts.

Product	Unit to profit	Time	Profit per unit	Total Profit
X	150	1500	3	450
Y	280	2800	5	1400
Z	100	500	2	200
				Total profit =2050

All things considered, we can strengthen and increase the success of the Newcastle Company by implementing some adjustments based on these concepts.

Let's talk more about how to put these concepts into practice.

Regards, Math's Group

### 3. Problem 3 Solution

In a survey of a research department, a company that produces certain type of spare parts has the price-demand function found to be  $p(x) = 3000 - 55x$ , where  $p(x)$  is the price per spare part in dollars at which number of spare parts can be sold. The company's fixed cost is \$3000, and the production cost per spare part is \$400. You should answer the following questions and incorporate your answers into a word-processed report. The sections of your report should correspond to the individual questions below.

- Find the cost function and the revenue function.
  - Find the break-even point.
  - Plot the break-even points in graph paper. Label the points accurately.
  - Find the output level that maximizes the profit and find the maximum profit.
- Round the answers in the nearest integer values.

Sol<sup>n</sup>

$p(x)$  = price per spare part

$x$  = number of spare parts can be sold

Price demand function  $p(x) = 3000 - 55x$

Fixed Cost = \$3000

Production per spare part = \$400

Now,

a) Cost function  $c(x) = 3000 + 400x$

Revenue function =  $p(x) \cdot x$

$$= 3000x - 55x^2$$

b) Breakeven Point,

Revenue = Cost

$$3000x - 55x^2 = 3000 + 400x$$

$$3000x - 55x^2 - 3000 - 400x = 0$$

$$55x^2 - 2600x + 3000 = 0 \dots\dots\dots (i)$$

Now,

Comparing eq<sup>n</sup> ( i ) with the formula  $a x^2 - b x + c = 0$

Where,

$$a = 55, b = - 2600, c = 3000$$

Putting value of a, b, c in the formula.

$$\begin{aligned} x &= \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \\ &= \frac{-(-2600) \pm \sqrt{(-2600)^2 - 4 \times 55 \times 3000}}{2 \times 55} \\ &= \frac{2600 \pm \sqrt{6100000}}{110} \end{aligned}$$

Taking +,

$$= 2600 + 6100000$$

$$= 46.08$$

Taking −,

$$= 2600 - 1610000$$

$$= 1.18$$

Again,

For the corresponding valves,

$$Y_1 = 3000 + (400 \times 46.08)$$

$$= 21432$$

&

$$Y_2 = 3000 + (400 \times 1.18)$$

$$= 3472$$



c) Graph

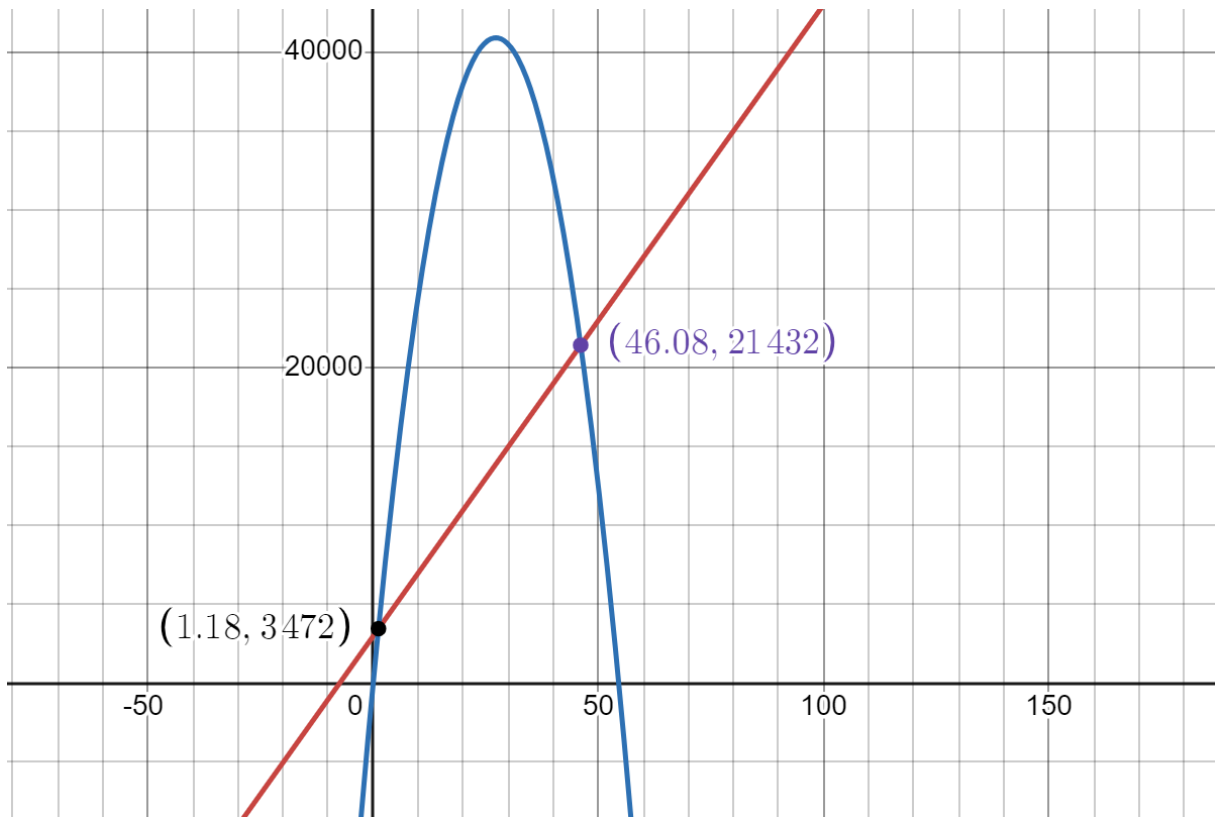


Figure 18: Screenshot for the graph of question 3.

$$\begin{aligned}
 \text{d) Profit} &= R(x) + C(x) \\
 &= 3000x - 55x^2 + 3000 + 400x \\
 &= -55x^2 + 2600x - 3000
 \end{aligned}$$

$$\begin{aligned}
 \text{Level of production } (x) &= \frac{-b}{2a} \\
 &= \frac{-2600}{2 \times -55} \\
 &= 23.63 \approx 24
 \end{aligned}$$

$$\begin{aligned}
 \text{Maximum profit } (y) &= c \cdot \frac{b^2}{4a} \\
 &= -3000 \frac{(2600)^2}{4 \times -55} \\
 &= 27727
 \end{aligned}$$

## 4. Conclusion

To sum out, this project provides an in-depth study of important mathematical ideas, strategies for solving problems, and real-world applications. We have explored topics including demand analysis, linear programming, and tax computation by working through three different problem sets. Our studies have improved our mathematical abilities while also explaining real-world situations, such as taxation plans, production efficiency, and market structure.

Our coursework has given us invaluable abilities for our future academic and professional activities, and we are appreciative of the chance to put our knowledge to use in real-world situations. It was also difficult to understand data, conduct equations correctly, and have technical software tool skill. We overcame these challenges by working together, being constant, and being open, and as a result, we were able to solve problems more effectively and learn mathematical ideas on deeper levels.

## 5. References

### References

Janssen, C. W. a. C., 1999. *Investopedia*. [Online]

Available at: <https://www.investopedia.com/terms/t/taxrate.asp>

[Accessed 14 may 2024].

Jr, A. P. S., 1937. *Tax Foundation*. [Online]

Available at: <https://taxfoundation.org/taxedu/glossary/tax-brackets/#:~:text=A%20tax%20bracket%20is%20the,rates%20rise%20as%20income%20increases.>




[20increases.](https://taxfoundation.org/taxedu/glossary/tax-brackets/#:~:text=A%20tax%20bracket%20is%20the,rates%20rise%20as%20income%20increases.)

[Accessed 14 may 2024].

## 6. Appendix: Logbook Entry Sheet



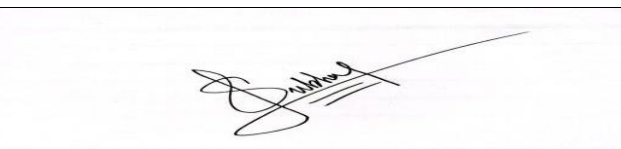
### 6.1 Entry sheet 1.

Table 1: Entry sheet 1

<b>Logbook Entry Sheet</b>	
<b>Meeting No: 1</b>	<b>Date: 6<sup>th</sup> May 2024</b>
Start Time: 11:00 pm	Finish Time: 12:00 pm
<p><b>Items Discussed:</b> Questions divided into sections for each group member.</p> <p><b>Achievements:</b> Questions is discussed and learnt new things.</p> <p><b>Problems (if any):</b> N/A</p> <p><b>Tasks for Next Meeting:</b> Show the task's progress.</p>	
<b>Student's Name</b>	<b>Student's Signature</b>
Unison Raj Tuladhar	
Sayun Rajkarnikar	
Subham Khoju Shrestha	

## 6.2 Entry sheet 2.

Table 2 : Entry sheet 2

<b>Logbook Entry Sheet</b>	
<b>Meeting No: 2</b>	<b>Date: 9<sup>th</sup> May 2024</b>
Start Time: 1:00 pm	Finish Time: 2:00 pm
<p><b>Items Discussed:</b> The amount of progress was shown and some problems regarding the question were discussed.</p> <p><b>Achievements:</b> Found the problem's basic reasoning and logic for the issue.</p> <p><b>Problems (if any):</b> N/A</p> <p><b>Tasks for Next Meeting:</b> check for further any problems</p>	
<b>Student's Name</b>	<b>Student's Signature</b>
Unison Raj Tuladhar	
Sayun Rajkarnikar	
Subham Khoju Shrestha	

## 6.3 Entry sheet 3.

Table 3: Entry sheet 3

## Logbook Entry Sheet

**Meeting No: 3****Date: 12<sup>th</sup> May 2024**

Start Time: 2:00 pm




Finish Time: 4:00 pm

**Items Discussed:** With the teacher's assistance, every issue was resolved, and now it was time to write the report.




**Achievements:** The issue was resolved, and report work was given out.

**Problems (if any):** N/A

**Tasks for Next Meeting:** Present the finished report and request feedback.

Student's Name	Student's Signature
Unison Raj Tuladhar	
Sayun Rajkarnikar	
Subham Khoju Shrestha	

**6.4 Entry sheet 4.***Table 4: Entry sheet 4*

<b>Logbook Entry Sheet</b>	
<b>Meeting No: 4</b>	<b>Date: 14<sup>th</sup> May 2024</b>
Start Time: 12:00 pm	Finish Time: 2:00 pm
<p><b>Items Discussed:</b> All the things were discussed with the group members and now time for submission.</p> <p><b>Achievements:</b> All the work was done and ready to submit.</p> <p><b>Problems (if any):</b> N/A</p> <p><b>Tasks for Next Meeting:</b> The final report was submitted by the group leader.</p>	
<b>Student's Name</b>	<b>Student's Signature</b>
Unison Raj Tuladhar	
Sayun Rajkarnikar	
Subham Khoju Shrestha	

## 7. Photo and Evidences

### 7.1 Photo of question number 2 a.

2a)  
Soln

To maximize  $R = 3x + 5y + 2z$   
 Constraints  
 $x = 150$   
 $z = 100$   
 $10x + 10y + 5z \leq 4800$

Let  $A_1, A_2$  be the artificial variables &  $S_1$  be the slack variable.

Now  
 $x + A_1 = 150$   
 $z + A_2 = 100$   
 $2x + 2y + z + S_1 = 960$   
 $x, y, z, A_1, A_2, S_1 \geq 0$

Standard equation for the simplex table.

$$1.C - 3x - 5y - 2z + 10A_1 + 10A_2 + 0.S_1 = 0$$

$$0.C + 1x + 0.y + 0.z + 1.A_1 + 0.A_2 + 0.S_1 = 150$$

$$0.C + 0.x + 0.y + 1.z + 0.A_1 + 1.A_2 + 0.S_1 = 100$$

$$0.C + 10x + 10y + 5z + 0.A_1 + 0.A_2 + 1.S_1 = 4800$$

Simplex Table 1:

	R	x	y	z	$A_1$	$A_2$	$S_1$	Constant
$R_0$	1	-3	-5	-2	10	10	0	0
$R_1$	0	1	0	0	1	0	0	150
$R_2$	0	0	0	1	0	1	0	100
$R_3$	0	10	10	5	0	0	1	4800

$\therefore$  Since the artificial values are not zero so, we cannot convert it into zero.

Figure 19: Solution of 2a part 1

50. New  $R_0 = \text{Old } R_0 - 10 \times (R_1 + R_2 + R_3)$

Old $R_0$	$-10 \times (R_1 + R_2 + R_3)$	New $R_0$
1	0	1
-3	-30	-33
-5	-50	-55
-2	-20	-22
10	-10	0
10	-10	0
0	-10	-10
0	-12100	-12100

Now Simplex Table 2:

	R	x	y	z	$A_1$	$A_2$	$S_1$	Constant
$R_0$	1	-33	-55	-22	0	0	-10	-12100
$R_1$	0	1	0	0	1	0	0	150
$R_2$	0	0	0	1	0	1	0	100
$R_3$	0	10	10	5	0	0	1	4800

Key column is  $x$ .  
 Key row is  $R_1$ .  
 Key element = 1.

Ratio  
 $R_1 = 150$   
 $R_2 = \infty$   
 $R_3 = 480$

Here,  $R_1$  is the key row &  $x$  is the key column.

New  $R_1 = \frac{\text{Old } R_1}{\text{key element}}$   
 $\therefore \text{New } R_1 = \frac{\text{Old } R_1}{1}$

Figure 20: Solution of 2a part 2



Updating  $R_0, R_1, R_2$  using formula

For  $R_0$

Old $R_0$	$+33 \times \text{New } R_1$	New $R_0$
1	0	1
-33	33	0
-25	0	-25
-22	0	-22
0	33	33
0	0	0
0	0	-10
-10	0	-10
-1200	4950	-7250

$\therefore$  Since the value of  $R_2$  is subtracted by 0, so  
New  $R_2 = \text{Old } R_2$

For  $R_2$

Old $R_2$	$-2 \times \text{New } R_1$	New $R_2$
0	0	0
10	-2	8
10	0	10
5	0	5
0	-2	-2
0	0	0
1	0	1
4800	-300	4500

Figure 21: Solution of 2a part 3

Simplex Table 3:

	$R_0$	$x$	$y$	$z$	$A_1$	$A_2$	$S_1$	Constant	Ratio
$R_0$	1	0	-25	-22	33	0	-10	-7250	
$R_1$	0	1	0	0	1	0	0	150	$\infty$
$R_2$	0	0	0	1	0	1	0	100	$\infty$
$R_3$	0	0	2	1	-2	0	1	660	330

Key column =  $y$   
Key row =  $R_3$   
Key element = 2

Now,  
 $R_3$  is the key row so it must be updated first,  
 $R_3 = \frac{\text{Old } R_3}{2}$

Now  $R_3 = 0, 0, 1, \frac{1}{2}, -\frac{1}{2}, 0, \frac{1}{2}, 330$

Now,  
For  $R_0, R_1, R_2$

New  $R_0 = \text{Old } R_0 - (-25) \times \text{New } R_3$   
New  $R_1 = \text{Old } R_1 - 0 \times \text{New } R_3$   
New  $R_2 = \text{Old } R_2 - 0 \times \text{New } R_3$

Figure 22: Solution of 2a part 4

For  $R_0$

Old $R_0$	$+25 \times \text{New } R_2$	New $R_0$
1	0	1
0	0	0
-25	25	0
-22	$25/2$	$-19/2$
33	-25	8
0	0	0
-10	$25/2$	$5/2$
-1150	8250	1100

Simplex Table 4

	R	x	y	z	$A_1$	$A_2$	$S_1$	Constant	Ratio
$R_0$	1	0	0	$-1/2$	8	0	$5/2$	1100	$\infty$
$R_1$	0	1	0	0	1	0	0	150	100
$R_2$	0	0	0	1	0	1	0	100	100
$R_3$	0	0	1	$1/2$	-1	0	$1/2$	330	660

Key column = 2  
 Key row =  $R_2$   
 Key element = 1

Here,  $R_2$  is the key row so it must be updated first.  
 $\text{New } R_2 = \text{Old } R_2$

Similarly, For  $R_0, R_1, R_3$

$$\begin{aligned} \text{New } R_0 &= \text{Old } R_0 - (-1/2) \times \text{New } R_2 \\ \text{New } R_1 &= \text{Old } R_1 - 0 \times \text{New } R_2 \\ \text{New } R_3 &= \text{Old } R_3 - 1/2 \times \text{New } R_2 \end{aligned}$$

Figure 23: Solution of 2a part 5

For  $R_0$

Old $R_0$	$+19/2 \times \text{New } R_2$	New $R_0$
0	0	0
0	0	0
-19/2	$19/2$	0
8	0	8
0	$19/2$	$13/2$
$5/2$	0	$5/2$
1100	950	2050

For  $R_3$

Old $R_3$	$-1/2 \times \text{New } R_2$	New $R_3$
0	0	0
0	0	0
1	0	1
$1/2$	$-1/2$	0
-1	0	-1
0	$-1/2$	$-1/2$
$1/2$	0	$1/2$
330	-50	280

Simplex Table 5

	R	x	y	z	$A_1$	$A_2$	$S_1$	Constant
$R_0$	1	0	0	0	8	$19/2$	$5/2$	2050
$R_1$	0	1	0	0	1	0	0	150
$R_2$	0	0	0	1	0	1	0	100
$R_3$	0	0	1	0	-1	$-1/2$	$1/2$	280

Here all the constants of variables in  $R_0$  is positive.  
 So this is the optimal condition  $x = 150, y = 280, z = 100$   
 $\therefore R = 2050$

Figure 24: Solution of 2a part 6

## 7.2 Photo of question number 2 b.

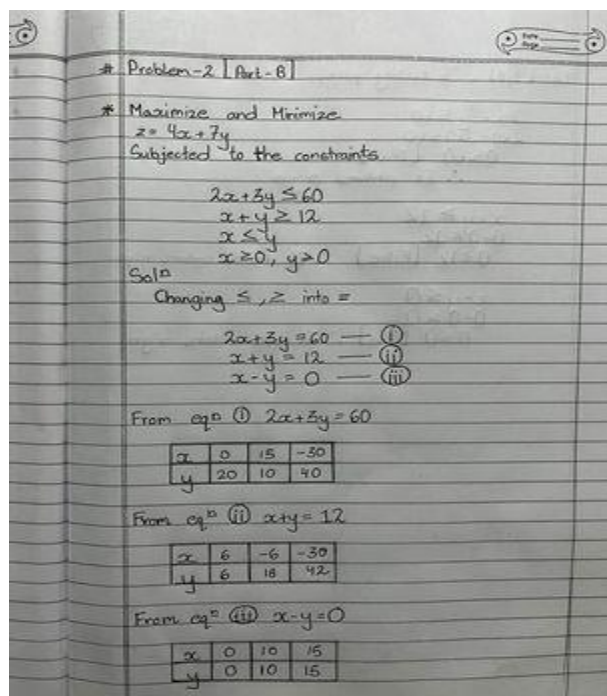


Figure 25: Question 2 solution1

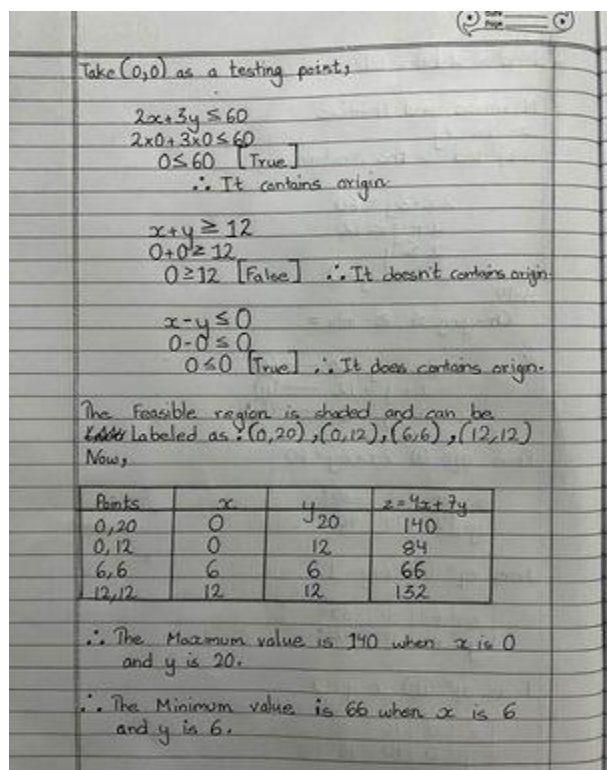


Figure 26: Question 2 solution2

## 7.2 Photo of question number 3.

Qm 3)

$p(x)$  = price per spare part  
 $x$  = number of spare part can be sold  
 Price demand function  $p(x) = 3000 - 55x$   
 Fixed cost = 3000  
 Production per spare part = 3400

Now

a) Cost function  $C(x) = 3000 + 400x$   
 Revenue function =  $p(x) \cdot x$   
 $= 3000x - 55x^2$

b) Break even point.  
 Revenue = Cost  
 $3000x - 55x^2 = 3000 + 400x$   
 $3000x - 55x^2 - 3000 - 400x = 0$   
 $55x^2 - 2600x + 3000 = 0 \quad \text{--- (1)}$

Now,  
 Comparing eq<sup>n</sup> (1) with the formula  $ax^2 + bx + c = 0$   
 Where,  $a = 55$ ,  $b = -2600$ ,  $c = 3000$

Putting value of a, b, c in the formula.

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$= \frac{-(-2600) \pm \sqrt{(-2600)^2 - 4 \times 55 \times 3000}}{2 \times 55}$$

$$= \frac{2600 \pm \sqrt{6100000}}{110}$$

Figure 27: Question 3 solution1

Taking +,  

$$\frac{2600 + \sqrt{6100000}}{2 \times 55} = 46.08$$

Taking -,  

$$\frac{2600 - \sqrt{6100000}}{2 \times 55} = 1.18$$

Again, for the corresponding values,  

$$y_1 = 3000 + (400 \times 46.08) = 21432$$

$$y_2 = 3000 + (400 \times 1.18) = 3472$$

d) Profit =  $R(x) + C(x)$   

$$= 3000x - 55x^2 + 3000 + 400x$$

$$= -55x^2 + 2600x + 3000$$

Level of production (x) =  $\frac{-b}{2a}$   

$$= \frac{-2600}{2 \times -55}$$

$$= 23.63 \approx 24$$

Maximum profit (y) =  $c - \frac{b^2}{4a}$   

$$= -3000 - \frac{(2600)^2}{4 \times -55}$$

$$= 27727$$

Figure 28: Question 3 solution2