
ASSIGNED: Feb. 21, 2013. **READ:** Sects. 4.4 & 5.1-5.2.

DUE DATE: Feb. 28, 2013. **TOPICS:** DTFT and DTFS.

Please box your answers. Show your work. Turn in all Matlab plots and Matlab code.

[20] 1. We are given $x[n] = \{\dots 18, 12, 6, 0, 6, 12, \underline{18}, 12, 6, 0, 6, 12, 18 \dots\}$ (a periodic signal).

[10] (a) Compute the Discrete-Time Fourier Series (DTFS) expansion of $x[n]$.

Hint: $x[n]$ has period=6, $x[n]$ is real-valued, and $x[n]$ is an even function.

[05] (b) Compute average power in the time domain. Your answer should agree with:

[05] (c) Compute average power in the frequency domain.

[20] 2. We are given DTFS coefficients $x_k = \cos(\pi k/4) + \sin(3\pi k/4)$.

Note that x_k is entirely real-valued, but it is *not* an even function.

[5] (a) Explain why $x[n]$ with these coefficients x_k has period=8.

[5] (b) Compute the *purely real* part of $x[n]$ from the *even* part of x_k .

[5] (c) Compute the *imaginary* part of $x[n]$ from the *odd* part of x_k .

[5] (d) Compute average powers in time and frequency domains. Confirm they agree.

Hint: One period of $x[n]$ has only two real and two imaginary nonzero values.

Hint: Read off $x[n]$ from $x_k = \sum_{n=0}^{N-1} \frac{x[n]}{N} e^{-j2\pi nk/N}$. Note $e^{-j2\pi nk/N} = e^{j2\pi(N-n)k/N}$.

[10] 3. Compute DTFTs of the following. Simplify to sums of sines and cosines.

[5] (a) $\{1, 1, \underline{1}, 1, 1\}$. [5] (b) $\{3, \underline{2}, 1\}$.

[10] 4. Use the inverse DTFT to evaluate the following integrals:

[5] (a) $\frac{1}{2\pi} \int_{-\pi}^{\pi} \frac{e^{j\omega} e^{j3\omega}}{e^{j\omega} - \frac{1}{2}} d\omega$. [5] (b) $\frac{1}{2\pi} \int_{-\pi}^{\pi} e^{j3\omega} 2 \cos(3\omega) d\omega$.

Hint: Replace $e^{j\omega}$ with z and compute Z^{-1} at a specific n .

[20] 5. $x[n] = \{1, 4, 3, 2, 5, 7, \underline{-45}, 7, 5, 2, 3, 4, 1\}$. Let $X(e^{j\omega}) = \text{DTFT}[x[n]]$. Compute:

[5] (a) $X(e^{j\pi})$. [5] (b) $\arg[X(e^{j\omega})]$. [5] (c) $\int_{-\pi}^{\pi} X(e^{j\omega}) d\omega$. [5] (d) $\int_{-\pi}^{\pi} |X(e^{j\omega})|^2 d\omega$.

Hint: Do *not* actually compute $X(e^{j\omega})$! Use some properties of the DTFT.

Note: $45 > 1+4+3+2+5+7+7+5+2+3+4+1$, so the phase is uniquely specified here.

[20] 6. Download `p5.mat`. In Matlab, type `>>load p5.mat` to get the sampled signal **X**.

[5] (a) Listen to **X** using `soundsc(X, 24000)`. Describe it. (It's not the same as before.)

[5] (b) Plot the spectrum of **X** using the Matlab command from problem set #1.

Compare carefully to the spectrum plot from problem set #1. What did I do?

[5] (c) Use `fftshift` somehow and `Y=real(ifft(FY))` to unscramble **X**.

[5] (d) Use the modulation property of the DTFT to unscramble **X** more easily.

Hint: Shifting discrete-time frequency by π does what in the time domain?

Note: This is the digital version of *voice scramblers* used in World War II.

Turn in plots of the spectrum of **X** and of its unscrambled version.

“A chicken is just an egg’s way of making another egg.”
