

EECS 451 FALL 2013 HW 9
DUE DECEMBER 10

After a genuine attempt to solve the homework problems by yourself, you are free to collaborate with your fellow students to find solutions to the homework problems. Regardless of whether you collaborate with other 451 students, you are required to write your own solutions to hand in. Copying homework solutions from another student or from existing solutions will be considered a violation of the honor code. Finally, if you choose to collaborate, you must include the names of your collaborators on your submitted homework. I haven't figured out yet how to track this, but I do look at it every once in awhile to see who's working with whom.

Please take advantage of the Piazza discussion forum on CTools and the professor's and GSI's office hours. This is a pretty easy one, though...

All HWs are worth 50 points. Each problem is worth 10 points.

1. Suppose the input-output relation of a system is given as

$$y[n] = \sum_{k=0}^M b_k x[n-k] + \sum_{k=1}^N a_k y[n-k] . \quad (0.1)$$

Show that the Z-transform of the impulse response $h[n]$ is equal to

$$H(z) = \frac{\sum_{k=0}^M b_k z^{-k}}{1 - \sum_{k=1}^N a_k z^{-k}} .$$

2. Suppose the input-output relation of a system is given as

$$y[n] = x[n] + ay[n-1] .$$

What is the Z-transform of the impulse response, $H(z)$? What is the impulse response $h[n]$? Is this system IIR or FIR?

3. Consider the IIR impulse response

$$h[n] = \left(\frac{3}{4}\right)^n u[n] .$$

- (a) What is the frequency response $H(\omega)$? Sketch $|H(\omega)|$.
- (b) Using Matlab, window this impulse response with a rectangular window of length $M = 10$ and a window of length $M = 50$. Qualitatively, how do the DFTs of these windowed impulse responses compare to one another?
- (c) Using Matlab, window the impulse response with a Hamming window, Bartlett window, and Hanning window, all of length $M = 50$. Their equations are found on p468 of the text. Qualitatively, how do the DFTs of these windowed impulse responses compare to one another? How do they compare to the rectangular window of length 50?

4. Using the `fdatool` in matlab, design FIR lowpass filters of order 20 using the windowing method. Set the cutoff frequency to 4000 Hz. Try the hamming, kaiser (with $\beta=5$), and rectangular window. Show the resulting plots. What are the qualitative differences?
5. A rare Jimi Hendrix recording was recently re-discovered at a recording studio. However, the (former) sound engineer did not protect against electromagnetic interference. Load the mat file at <http://web.eecs.umich.edu/~girasole/teaching/451/jimi.mat> and listen to this short excerpt from the recording (the sampling rate is 8000 Hz). If your headphones have adequate low-frequency response, you will hear an annoying 120 Hz hum.
 - (a) Design an IIR notch filter by putting zeros at $z = e^{\pm\omega_c}$ where $\omega_c = 2\pi 120/8000$ and poles at $re^{\pm\omega_c}$ where $r = 0.9$. What is the resulting difference equation (in the form of Equation 0.1 above)?
 - (b) Using the `filter` command in matlab, apply this filter to the hendrix clip. Submit your code.