Introduction to Information Retrieval

CS276: Information Retrieval and Web Search Christopher Manning and Pandu Nayak

Wildcard queries and Spelling Correction

WILD-CARD QUERIES

Wild-card queries: *

- mon*: find all docs containing any word beginning with "mon".
- Easy with binary tree (or B-tree) dictionary: retrieve all words in range: mon ≤ w < moo</p>
- *mon: find words ending in "mon": harder
 - Maintain an additional B-tree for terms backwards.

Can retrieve all words in range: *nom ≤ w < non*.

From this, how can we enumerate all terms meeting the wild-card query *pro*cent*?

Query processing

- At this point, we have an enumeration of all terms in the dictionary that match the wild-card query.
- We still have to look up the postings for each enumerated term.
- E.g., consider the query:

se*ate AND fil*er

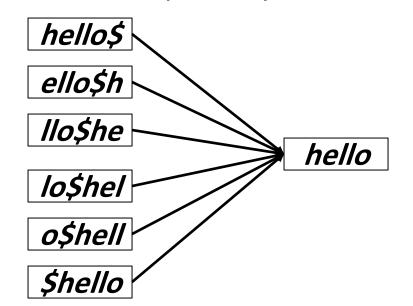
This may result in the execution of many Boolean *AND* queries.

B-trees handle *'s at the end of a query term

- How can we handle *'s in the middle of query term?
 - co*tion
- We could look up co*AND *tion in a B-tree and intersect the two term sets
 - Expensive
- The solution: transform wild-card queries so that the
 *'s occur at the end
- This gives rise to the Permuterm Index.

Permuterm index

- Add a \$\foatstartetest to the end of each term
- Rotate the resulting term and index them in a B-tree
- For term *hello*, index under:
 - hello\$, ello\$h, llo\$he, lo\$hel, o\$hell, \$hello
 where \$ is a special symbol.



Empirically, dictionary quadruples in size

Permuterm query processing

- (Add \$), rotate * to end, lookup in permuterm index
- Queries:

```
lookup on X$
                            hello$ for hello
■ X
                            $hel* for hel*
           lookup on $X*
■ X*
           lookup on X$*
                            llo$* for *llo
■ *X
           lookup on X* ell* for *ell*
■ *X*
X*Y
           lookup on Y$X*
                            lo$h for h*lo
          treat as a search for X*Z and post-filter
X*Y*Z
              For h*a*o, search for h*o by looking up o$h*
```

and post-filter *hello* and retain *halo*

Bigram (k-gram) indexes

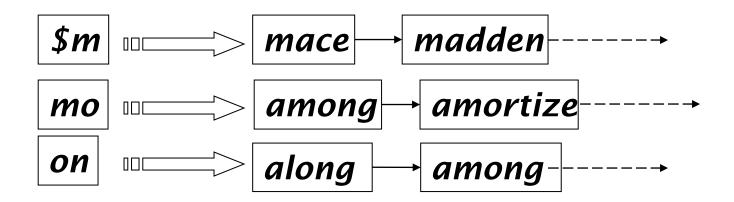
- Enumerate all k-grams (sequence of k chars)
 occurring in any term
- e.g., from text "April is the cruelest month" we get the 2-grams (bigrams)

```
$a,ap,pr,ri,il,l$,$i,is,s$,$t,th,he,e$,$c,cr,ru,
ue,el,le,es,st,t$, $m,mo,on,nt,h$
```

- \$ is a special word boundary symbol
- Maintain a <u>second</u> inverted index <u>from bigrams to</u> <u>dictionary terms</u> that match each bigram.

Bigram index example

 The k-gram index finds terms based on a query consisting of k-grams (here k=2).

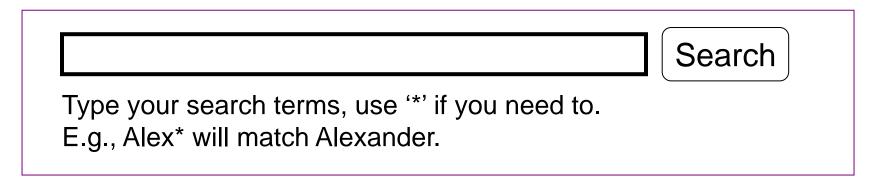


Processing wild-cards

- Query mon* can now be run as
 - \$m AND mo AND on
- Gets terms that match AND version of our wildcard query.
- But we'd enumerate moon.
- Must post-filter these terms against query.
- Surviving enumerated terms are then looked up in the term-document inverted index.
- Fast, space efficient (compared to permuterm).

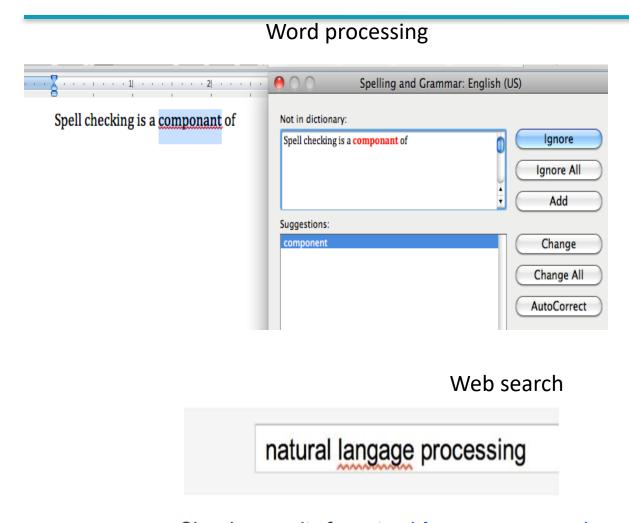
Processing wild-card queries

- As before, we must execute a Boolean query for each enumerated, filtered term.
- Wild-cards can result in expensive query execution (very large disjunctions...)
 - pyth* AND prog*
- If you encourage "laziness" people will respond!



SPELLING CORRECTION

Applications for spelling correction





Showing results for <u>natural language</u> processing Search instead for natural language processing

Rates of spelling errors

Depending on the application, ~1–20% error rates

26%: Web queries Wang *et al.* 2003

13%: Retyping, no backspace: Whitelaw et al. English&German

7%: Words corrected retyping on phone-sized organizer

2%: Words uncorrected on organizer Soukoreff & MacKenzie 2003

1-2%: Retyping: Kane and Wobbrock 2007, Gruden et al. 1983

Spelling Tasks

- Spelling Error Detection
- Spelling Error Correction:
 - Autocorrect
 - hte → the
 - Suggest a correction
 - Suggestion lists

Types of spelling errors

- Non-word Errors
 - graffe → giraffe
- Real-word Errors
 - Typographical errors
 - three \rightarrow there
 - Cognitive Errors (homophones)
 - piece → peace,
 - too → two
 - your → you're
- Non-word correction was historically mainly context insensitive
- Real-word correction almost needs to be context sensitive

Non-word spelling errors

- Non-word spelling error detection:
 - Any word not in a *dictionary* is an error
 - The larger the dictionary the better ... up to a point
 - (The Web is full of mis-spellings, so the Web isn't necessarily a great dictionary ...)
- Non-word spelling error correction:
 - Generate candidates: real words that are similar to error
 - Choose the one which is best:
 - Shortest weighted edit distance
 - Highest noisy channel probability

Real word & non-word spelling errors

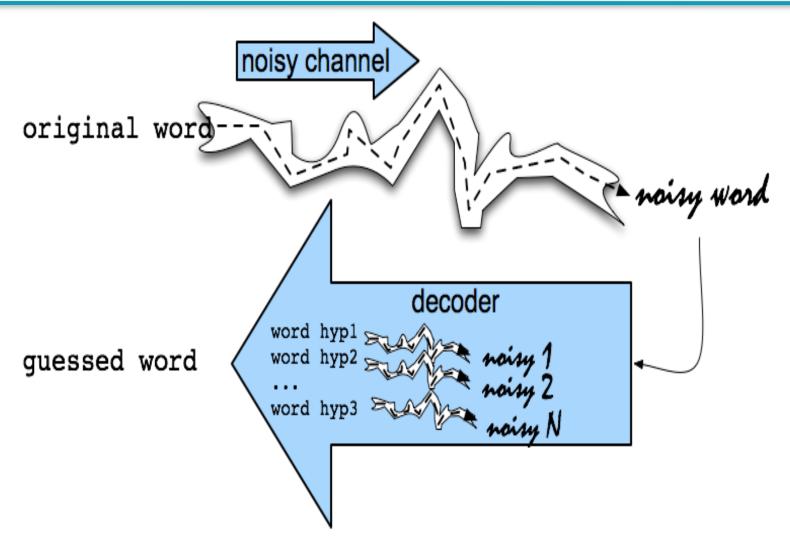
- For each word w, generate candidate set:
 - Find candidate words with similar pronunciations
 - Find candidate words with similar spellings
 - Include w in candidate set
- Choose best candidate
 - Noisy Channel view of spell errors
 - Context-sensitive so have to consider whether the surrounding words "make sense"
 - Flying <u>form</u> Heathrow to LAX → Flying <u>from</u> Heathrow to LAX

Terminology

- We just discussed <u>character bigrams and k-grams</u>:
 - st, pr, an ...
- We can also have <u>word bigrams and n-grams</u>:
 - palo alto, flying from, road repairs

The Noisy Channel Model of Spelling INDEPENDENT WORD SPELLING CORRECTION

Noisy Channel Intuition



Noisy Channel = Bayes' Rule

- We see an observation x of a misspelled word
- Find the correct word \hat{W}

$$\hat{w} = \underset{w \mid V}{\operatorname{argmax}} P(w \mid x)$$

$$= \underset{w \mid V}{\operatorname{argmax}} \frac{P(x \mid w)P(w)}{P(x)}$$

$$= \underset{w \mid V}{\operatorname{argmax}} P(x \mid w)P(w)$$

$$= \underset{w \mid V}{\operatorname{argmax}} P(x \mid w)P(w)$$
Noisy channel model

History: Noisy channel for spelling proposed around 1990

IBM

Mays, Eric, Fred J. Damerau and Robert L. Mercer. 1991.
 Context based spelling correction. *Information Processing and Management*, 23(5), 517–522

AT&T Bell Labs

Kernighan, Mark D., Kenneth W. Church, and William A.
 Gale. 1990. <u>A spelling correction program based on a noisy channel model</u>. Proceedings of COLING 1990, 205-210

Non-word spelling error example

acress

Candidate generation

- Words with similar spelling
 - Small <u>edit distance</u> to error
- Words with similar pronunciation
 - Small distance of pronunciation to error

Candidate Testing: Damerau-Levenshtein edit distance

- Minimal edit distance between two strings, where edits are:
 - Insertion
 - Deletion
 - Substitution
 - Transposition of two adjacent letters
- See //R sec 3.3.3 for edit distance

acress

acress

acress

acress

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acress

Mards within 1 of a area

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Error	Candidate	Correct	Error	Туре

ca

Correction

actress

cress

caress

access

across

acres

Letter Letter

a

ac

r

е

S

deletion

insertion

transposition

substitution

substitution

27

insertion

Candidate generation

- 80% of errors are within edit distance 1
- Almost all errors within edit distance 2

- Also allow insertion of space or hyphen
 - \blacksquare thisidea \rightarrow this idea
 - inlaw \rightarrow in-law
- Can also allow merging words
 - data base → database
 - For short texts like a query, can just regard whole string as one item from which to produce edits

How do you generate the candidates?

- Run through dictionary, check edit distance with each word
- 2. Generate all words within edit distance $\leq k$ (e.g., k = 1 or 2) and then intersect them with dictionary
- Use a character k-gram index and find dictionary words that share "most" k-grams with word (e.g., by Jaccard coefficient)
 - see //R sec 3.3.4
- 4. Compute them fast with a Levenshtein finite state transducer
- 5. Have a precomputed map of words to possible corrections

A paradigm ...

- We want the best spell corrections
- Instead of finding the very best, we
 - Find a subset of pretty good corrections
 - (say, edit distance at most 2)
 - Find the best amongst them
- These may not be the actual best
- This is a recurring paradigm in IR including finding the best docs for a query, best answers, best ads ...
 - Find a good candidate set
 - Find the top K amongst them and return them as the best

Let's say we've generated candidates: Now back to Bayes' Rule

- We see an observation x of a misspelled word
- Find the correct word \hat{w}

$$\hat{w} = \underset{w \mid V}{\operatorname{argmax}} P(w \mid x)$$

$$= \underset{w \mid V}{\operatorname{argmax}} \frac{P(x \mid w)P(w)}{P(x)}$$

= $\operatorname{argmax} P(x \mid w)P(w)$ What's P(w)? \widehat{w} \widehat{V}

Language Model

■ Take a big supply of words (your document collection with T tokens); let C(w) = # occurrences of w

$$P(w) = \frac{C(w)}{T}$$

 In other applications – you can take the supply to be typed queries (suitably filtered) – when a static dictionary is inadequate

Unigram Prior probability

Counts from 404,253,213 words in Corpus of Contemporary English (COCA)

word	Frequency of word	<i>P(w)</i>
actress	9,321	.0000230573
cress	220	.0000005442
caress	686	.0000016969
access	37,038	.0000916207
across	120,844	.0002989314
acres	12,874	.0000318463

Channel model probability

- Error model probability, Edit probability
- Kernighan, Church, Gale 1990

- Misspelled word $x = x_1, x_2, x_3... x_m$
- Correct word $w = w_1, w_2, w_3, ..., w_n$
- P(x/w) = probability of the edit
 - (deletion/insertion/substitution/transposition)

Computing error probability: confusion "matrix"

Insertion and deletion conditioned on previous character

Confusion matrix for substitution

cuhlX.	V 1 =	Substitution	of X	(incorrect)	for V	(correct)
SUDIA	1	- ԾԱՍԾԱԼԱԱՄՄ	VI A	THUMITULE	IUI I	COLICCI

X	Y (correct)																									
	a	b	С	d	e	f	g	h	i	j	k	_ 1	m	n	0	p	q	r	S	t	u	V	W	Х	у	Z
a	0	0	7	1	342	0	0	2	118	0	1	0	0	3	76	0	0	1	35	9	9	0	1	0	5	0
b	0	0	9	9	2	2	3	1	0	0	0	5	11	5	0	10	0	0	2	I	0	0	8	0	0	0
С	6	5	0	16	0	9	5	0	0	0	1	0	7	9	1	10	2	5	39	40	1	3	7	1	1	0
d	1	10	13	0	12	0	5	5	0	0	2	3	7	3	()	1	0	43	30	22	0	0	4	0	2	0
e	388	0	3	11	0	2	2	0	89	0	0	3	0	5	93	0	0	14	12	6	15	0	1	0	18	0
f	0	15	0	3	1	0	5	2	0	0	0	3	4	1	0	0	0	6	4	12	0	0	2	0	0	0
g	4	1	11	11	9	2	0	0	0	1	1	3	0	0	2	1	3	5	13	21	0	0	1	0	3	0
h	1	8	0	3	0	0	0	0	0	0	2	0	12	14	2	3	0	3	1	11	0	0	2	0	0	0
i	103	0	0	0	146	0	1	0	0	0	0	6	0	0	49	0	0	0	2	1	47	0	2	1	15	0
j	0	1	1	9	0	0	1	0	0	0	0	2	1	0	0	0	0	0	5	0	0	0	0	0	0	0
k	1	2	8	4	1	1	2	5	0	0	0	0	5	0	2	0	0	0	6	0	0	0	. 4	0	0	3
1	2	10	1	4	0	4	5	6	13	0	1	0	0	14	2	5	0	11	10	2	0	0	0	0	0	0
m	1	3	7	8	0	2	0	6	0	()	4	4	0	180	0	6	0	0	9	15	13	3	2	2	3	0
n	2	7	6	5	3	0	1	19	1	0	4	35	78	0	0	7	0	28	5	7	0	0	1	2	0	2
0	91	1	1	3	116	0	0	0	25	0	2	0	0	0	0	14	0	2	4	14	39	0	0	0	18	0
p	0	11	1	2	0	6	5	0	2	9	0	2	7	6	15	0	0	1	3	6	0	4	1	0	0	0
q	0	0	1	0	0	0	27	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
r	0	14	0	30	12	2	2	8	2	0	5	8	4	20	1	14	0	0	12	22	4	0	0	1	0	0
S	11	8	27	33	35	4	0	1	0	1	0	27	0	6	1	7	0	14	0	15	0	0	5	3	20	1
t	3	4	9	42	7	5	19	5	0	l	0	14	9	5	5	6	0	11	37	0	0	2	19	0	7	6
u	20	0	0	0	44	0	0	0	64	0	0	0	0	2	43	0	0	4	0	0	0	0	2	0	8	0
V	0	0	7	0	0	3	0	0	0	0	0	1	0	0	1	0	0	0	8	3	0	0	0	0	0	0
W	2	2	1	0	1	0	0	2	0	0	ı	0	0	0	0	7	0	6	3	3	ı	0	0	0	0	0
X	0	0	0	2	0	0	0	0	0	0	0	0	0	0	0	0	0	0	9	0	0	0	0	0	0	0
y	0	0	2	0	15	0	I	7	15	0	0	0	2 5	0	6	1	0	7	36	8	5	0	0	1	0	0
Z	0	0	0	7	0	0	0	0	0	0	0	7	3	0	0	0	0	2	21	3	0	0	0	0	3	0

Nearby keys



Generating the confusion matrix

- Peter Norvig's list of errors
- Peter Norvig's list of counts of single-edit errors
 - All Peter Norvig's ngrams data links: http://norvig.com/ngrams/

Channel model

Kernighan, Church, Gale 1990

$$P(x|w) = \begin{cases} \frac{\operatorname{del}[w_{i-1}, w_i]}{\operatorname{count}[w_{i-1}, x_i]}, & \text{if deletion} \\ \frac{\operatorname{ins}[w_{i-1}, x_i]}{\operatorname{count}[w_{i-1}]}, & \text{if insertion} \\ \frac{\operatorname{sub}[x_i, w_i]}{\operatorname{count}[w_i]}, & \text{if substitution} \\ \frac{\operatorname{trans}[w_i, w_{i+1}]}{\operatorname{count}[w_i w_{i+1}]}, & \text{if transposition} \end{cases}$$

Smoothing probabilities: Add-1 smoothing

- But if we use the confusion matrix example, unseen errors are impossible!
- They'll make the overall probability 0. That seems too harsh
 - e.g., in Kernighan's chart q→a and a→q are both 0, even though they're adjacent on the keyboard!
- A simple solution is to add 1 to all counts and then if there is a |A| character alphabet, to normalize appropriately:

If substitution,
$$P(x | w) = \frac{\text{sub}[x, w] + 1}{\text{count}[w] + A}$$

Channel model for acress

Candidate Correction		x/w	<i>P(x/w)</i>

actress

c|ct

.000117

cress

 \bigcirc

a | #

r | C

 $e \mid 0$

es | e

SSS

.0000321

.0000342

а ac

0

S

.00000144

caress ca

ac | ca

.00000164

41

access

.000000209 .0000093

across

.0000916 .019 .000000209 r|C access r .0000093 2.8 .000299 $e \mid 0$ 9 across 0

es | e

SSS

S

S

acres

acres

.0000321

.0000342

1.0

1.042

.0000318

.0000318

Candidate Correction	Correct Letter	Error Letter	x/w	P(x/w)	P(w)	10 ⁹ * <i>P(x/w)P(</i> <i>w)</i>
actress	t	_	c c t	.000117	.0000231	2.7
cress	_	a	a #	.00000144	.000000544	.00078
caress	са	ac	ac ca	.00000164	.00000170	.0028
access	С	r	r c	.000000209	.0000916	.019
across	0	е	elo	.0000093	.000299	2.8
acres	_	S	es e	.0000321	.0000318	1.0
acres	_	S	ss	.0000342	.0000318	1.043

Evaluation

- Some spelling error test sets
 - Wikipedia's list of common English misspelling
 - Aspell filtered version of that list
 - Birkbeck spelling error corpus
 - Peter Norvig's list of errors (includes Wikipedia and Birkbeck, for training or testing)

Context-Sensitive Spelling Correction

SPELLING CORRECTION WITH THE NOISY CHANNEL

Real-word spelling errors

- …leaving in about fifteen minuets to go to her house.
- The design an construction of the system...
- Can they *lave* him my messages?
- The study was conducted mainly be John Black.

25-40% of spelling errors are real words Kukich 1992

Context-sensitive spelling error fixing

- For each word in sentence (phrase, query ...)
 - Generate candidate set
 - the word itself
 - all single-letter edits that are English words
 - words that are homophones
 - (all of this can be pre-computed!)
- Choose best candidates
 - Noisy channel model

Noisy channel for real-word spell correction

- Given a sentence x₁,x₂,x₃,...,x_n
- Generate a set of candidates for each word x_i
 - Candidate(x_1) = { x_1 , w_1 , w'_1 , w''_1 ,...}
 - Candidate(x_2) = { x_2 , w_2 , w'_2 , w''_2 ,...}
 - Candidate(x_n) = { x_n , w_n , w'_n , w''_n ,...}
- Choose the sequence W that maximizes $P(W|x_1,...,x_n)$

$$\hat{w} = \underset{w \mid V}{\operatorname{argmax}} P(w \mid x)$$

$$= \underset{w \mid V}{\operatorname{argmax}} P(x \mid w) P(w)$$

Incorporating context words: Context-sensitive spelling correction

- Determining whether actress or across is appropriate will require looking at the context of use
- We can do this with a better language model
 - You learned/can learn a lot about language models in CS124 or CS224N
 - Here we present just enough to be dangerous/do the assignment
- A bigram language model conditions the probability of a word on (just) the previous word

$$P(w_1...w_n) = P(w_1)P(w_2 | w_1)...P(w_n | w_{n-1})$$

Incorporating context words

- For unigram counts, P(w) is always non-zero
 - if our dictionary is derived from the document collection
- This won't be true of $P(w_k | w_{k-1})$. We need to **smooth**
- We could use add-1 smoothing on this conditional distribution
- But here's a better way interpolate a unigram and a bigram:

$$P_{li}(w_k|w_{k-1}) = \lambda P_{uni}(w_k) + (1-\lambda)P_{bi}(w_k|w_{k-1})$$

$$P_{bi}(w_k|w_{k-1}) = C(w_{k-1}, w_k) / C(w_{k-1})$$

All the important fine points

- Note that we have several probability distributions for words
 - Keep them straight!
- You might want/need to work with log probabilities:
 - $\log P(w_1...w_n) = \log P(w_1) + \log P(w_2|w_1) + ... + \log P(w_n|w_{n-1})$
 - Otherwise, be very careful about floating point underflow
- Our query may be words anywhere in a document
 - We'll start the bigram estimate of a sequence with a unigram estimate
 - Often, people instead condition on a start-of-sequence symbol, but not good here
 - Because of this, the unigram and bigram counts have different totals – not a problem

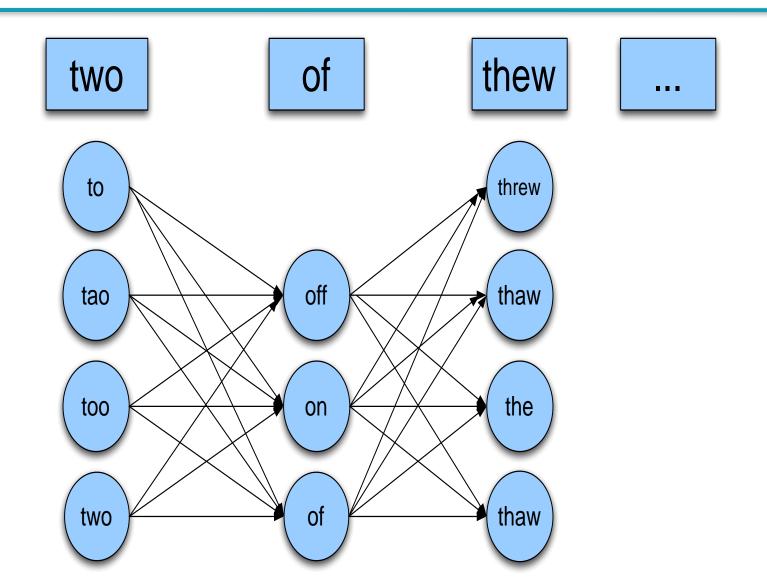
Using a bigram language model

- "a stellar and versatile acress whose combination of sass and glamour..."
- Counts from the Corpus of Contemporary American
 English with add-1 smoothing
- P(actress|versatile) = .000021 P(whose|actress) = .0010
 P(across|versatile) = .000021 P(whose|across) = .000006
- P("versatile actress whose") = $.000021*.0010 = 210 \times 10^{-10}$
- P("versatile across whose") = $.000021*.000006 = 1 \times 10^{-10}$

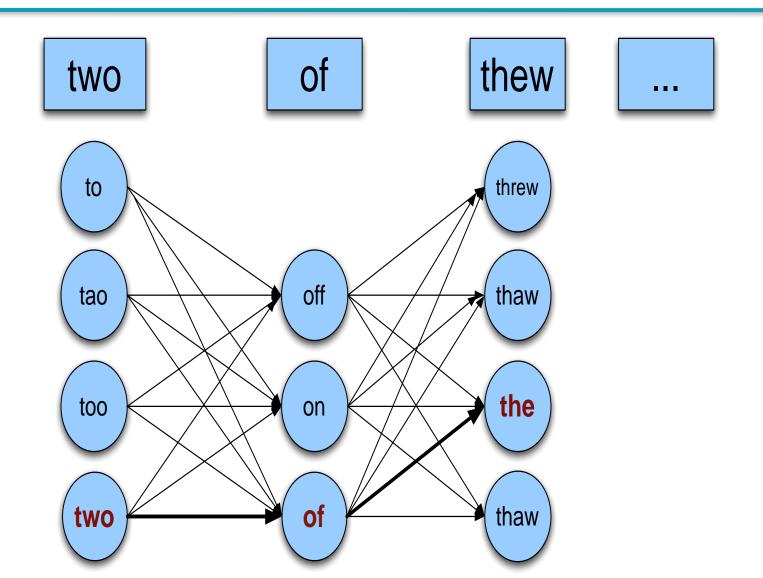
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Noisy channel for real-word spell correction



Noisy channel for real-word spell correction



Simplification: One error per sentence

Out of all possible sentences with one word replaced

```
    w<sub>1</sub>, w"<sub>2</sub>, w<sub>3</sub>, w<sub>4</sub> two off thew
    w<sub>1</sub>, w<sub>2</sub>, w'<sub>3</sub>, w<sub>4</sub> two of the
    w""<sub>1</sub>, w<sub>2</sub>, w<sub>3</sub>, w<sub>4</sub> too of thew
    ...
```

Choose the sequence W that maximizes P(W)

Where to get the probabilities

- Language model
 - Unigram
 - Bigram
 - etc.
- Channel model
 - Same as for non-word spelling correction
 - Plus need probability for no error, P(w/w)

Probability of no error

- What is the channel probability for a correctly typed word?
- P("the" | "the")
 - If you have a big corpus, you can estimate this percent correct
- But this value depends strongly on the application
 - .90 (1 error in 10 words)
 - .95 (1 error in 20 words)
 - .99 (1 error in 100 words)

Peter Norvig's "thew" example

X	W	x w	P(x w)	P(w)	10 ⁹ P(x w)P(w)
thew	the	ew e	0.00007	0.02	144
thew	thew		0.95	0.0000009	90
thew	thaw	e a	0.001	0.000007	0.7
thew	threw	h hr	0.00008	0.000004	0.03
thew	thwe	ew w e	0.00003	0.0000004	0.0001

State of the art noisy channel

- We never just multiply the prior and the error model
- Independence assumptions → probabilities not commensurate
- Instead: Weight them

$$\hat{w} = \underset{w \in V}{\operatorname{argmax}} P(x \mid w) P(w)^{\prime}$$

Learn λ from a development test set

Improvements to channel model

- Allow richer edits (Brill and Moore 2000)
 - ent → ant
 - ph→f
 - le → al
- Incorporate pronunciation into channel (Toutanova and Moore 2002)
- Incorporate device into channel
 - Not all Android phones need have the same error model
 - But spell correction may be done at the system level