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Atomic Structure

Mass Number and Atomic Number

Mass number of an element = No. of protons (Z) + No. of neutrons (n). Atomic Number (Z) = No. of Protons

Wave and its Characteristics (For emission/ Absorption of energy)

$$\overline{v} = \frac{1}{\lambda}$$
 $\overline{v} = \text{Wave Number}$

E = hv (v - Frequency of light)

 $E = \frac{hc}{\lambda}$ (c - speed of light)

Photoelectric Effect

 $hv = hv_0 + \frac{1}{2} m_e v^2$, where, $v_0 =$ Threshold frequency, V = Velocity of photoelectron

 ν = Incident Frequency

Bohr's Model of Atom

$$\Rightarrow \frac{mv^2}{r} = \frac{Ke^2Z}{r^2}$$

$$ightharpoonup mvr = \frac{nh}{2\pi}$$

$$r_n = 0.529 \times \frac{n^2}{Z} \text{ Å}$$

$$V = \frac{2\pi Z e^2 K}{nh}$$

$$> V_n = 2.18 \times 10^6 \times \frac{Z}{n} \text{ m/sec}$$

$$ightharpoonup T = \frac{2\pi r}{v}$$

$$\qquad f = \frac{v}{2\pi r}$$

$$T.E. = E_n = -\frac{2\pi^2 \text{ me}^4 \text{ k}^2}{\text{h}^2} \left(\frac{\text{z}^2}{\text{n}^2}\right)$$

$$E_n = -13.6 \frac{Z^2}{n^2} \text{ eV / atom}$$

$$\boldsymbol{r}_n = 0.529 \times \boldsymbol{n}^2$$

$$ightharpoonup$$
 T.E. = $\frac{1}{2}$ P.E.

$$V_n = \frac{V_1}{n}$$

$$\rightarrow$$
 E_n = -2.18 × 10⁻¹⁸ $\frac{Z^2}{n^2}$ J/atom

$$En = E_1/n^2$$

$$n = orbit no.$$

$$\rightarrow$$
 T.E. = - K.E.

Emission Spectrum of Hydrogen & H-like species.

$$\Delta E = hv = \frac{hC}{\lambda}$$
; h = Planck's Constant(h = 6.62 × 10⁻³⁴ JS)

C = Velocity of Light

 $\lambda = Wavelength$

 $R = Rydberg constant = 1.09678 \times 10^7 m^{-1}$

 $n_1 = Lower energy level$

 n_2 = Higher energy level

Number of different line produce = $\frac{\Delta n (\Delta n + 1)}{2}$, where $\Delta n = n_2 - n_1$.

 n_2 = higher energy orbit, n_1 = lower energy orbit.

For single isolated atom maximum number of spectral lines observed = (n - 1).

de-Broglie's Hypothesis

 $\lambda = de$ -Broglie wavelength

h = Planck's Constant

m = mass of particle

e = charge on particle

V = Accelerated Potential

$$ightharpoonup \lambda = \frac{h}{mv} = \frac{h}{p}$$
, $p = momentum$

$$\lambda = \frac{h}{\sqrt{2emV}}$$

Heisenberg's Uncertainty

$$\blacktriangleright \quad \Delta x \; . \; \Delta p \geq \frac{h}{4\pi} \; \; \text{or} \; \Delta x \; . \; (m\Delta v) \geq \; \frac{h}{4\pi}$$

$$ightharpoonup \Delta E.\Delta t \ge \frac{h}{4\pi}$$
; $\Delta x =$ change in position

 Δp = change in Momentum

 $P = \psi^2 dv$, P = probability of finding electron

where, ψ = wave function

Radial nodes =
$$n - \ell - 1$$
,

$$\triangleright$$
 Angular nodes = ℓ ,

$$\triangleright$$
 Total nodes = $n-1$

Quantum Numbers

- Number of subshell present in n^{th} shell = n.
- Number of orbitals present in n^{th} shell = n^2 .
- The maximum number of electrons in a principal energy shell = $2n^2$.
- Angular momentum of any orbit = $\frac{\text{nh}}{2\pi}$.
- ❖ Number of orbitals in a subshell = $2\ell + 1$
- ❖ Maximum number of electrons in particular subshell = $2 \times (2\ell + 1)$.

$$\label{eq:lambda} \mbox{\star} \quad L = \frac{h}{2\pi} \sqrt{\,\ell\,(\ell+1)} = \hbar \sqrt{\,\ell\,(\ell+1)} \Bigg\lceil \, \hbar = \frac{h}{2\pi} \, \Bigg\rceil \, .$$

- Orbitals present in a main energy level is 'n2'.
- * $\mu = \sqrt{n(n+2)}$ B.M., n = No. of unpaired electron.
- Spin angular momentum $=\frac{h}{2\pi}\sqrt{s(s+1)}$.
- ❖ Maximum spin of atom = $\frac{1}{2}$ × No. of unpaired electron.