

YAKEEN NEET 2.0

2026

Motion in a Plane

Physics

Lecture – 8

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Topics to be covered

1

#

✓ Relative motion in Motion under gravity →

2

✓ feel of 2-D Relative motⁿ.

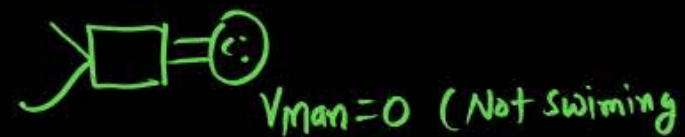
3

✓ Minimum sep^d

4

✓ Condition of collision

Case-1

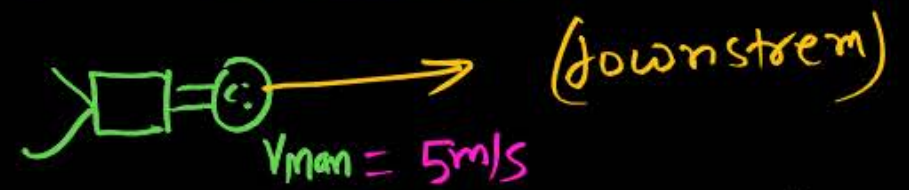


$V_r = \text{velocity of river}$
 $= 20 \text{ m/s}$ ✓

$$U_{man(river)} = 0$$

$$U_{man(ground)} = 0 + 20 \\ = 20 \text{ m/s}$$

Case-2



$V_r = 20 \text{ m/s}$

$$U_{man(river)} = 5 \text{ m/s}$$

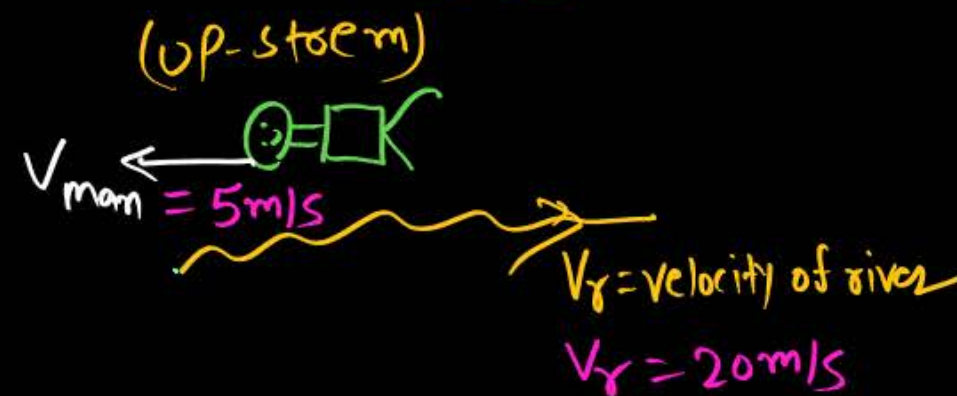
$$V_{man(ground)} = 25 \text{ m/s}$$

MR BOX

Velocity by which man can swim = velocity of man w.r.t river = velocity of man w.r.t still water.

Case-3

विरुद्ध धारा



$$U_{man(river)} = -5 \text{ m/s} \checkmark$$

$$V_{man(ground)} = 20 - 5 \\ = 15 \text{ m/s}$$

Question

Likho



A man boat travelled 30 km downstream in 3 hours and made the upstream trip in 5 hours. Find the speed of the boat in still water. ✓

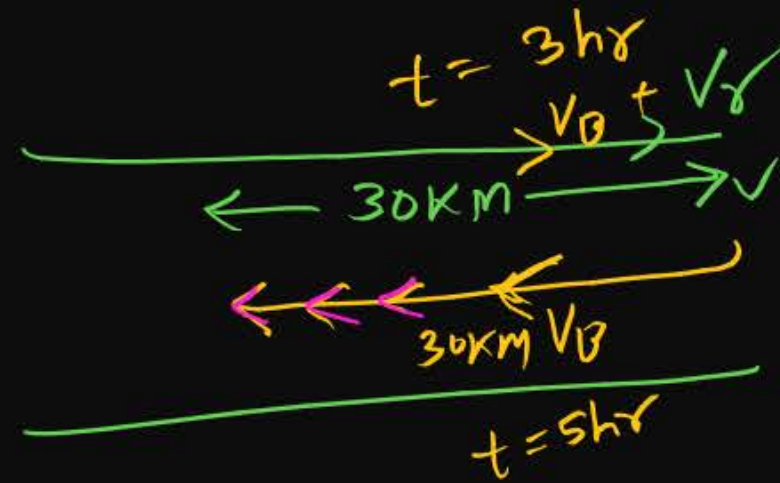
dirⁿ of flow of river

1 ✓✓ 8 km/hr

2 12 km/hr

3 6 km/hr

4 10 km/hr



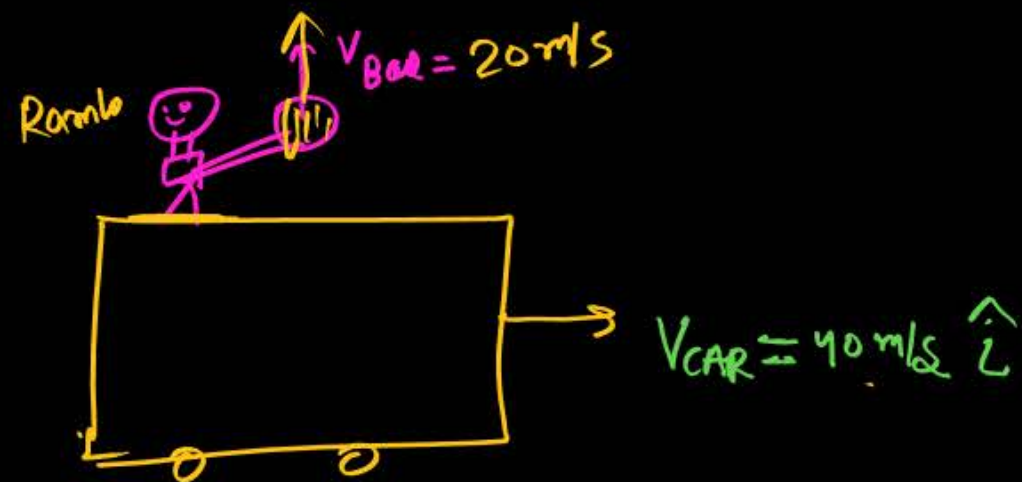
Backward motⁿ only possible ($V_B > V_r$)

$$\begin{aligned} \text{Case-1} \quad V_{\text{down}} &= V_B + V_r = \frac{30 \text{ km}}{3 \text{ hr}} \quad \text{--- (i)} \\ \text{Case-2} \quad V_B - V_r &= \frac{30 \text{ km}}{5 \text{ hr}} \quad \text{--- (ii)} \end{aligned}$$

$$2V_B = 10 + 6$$

$$2V_B = 16$$

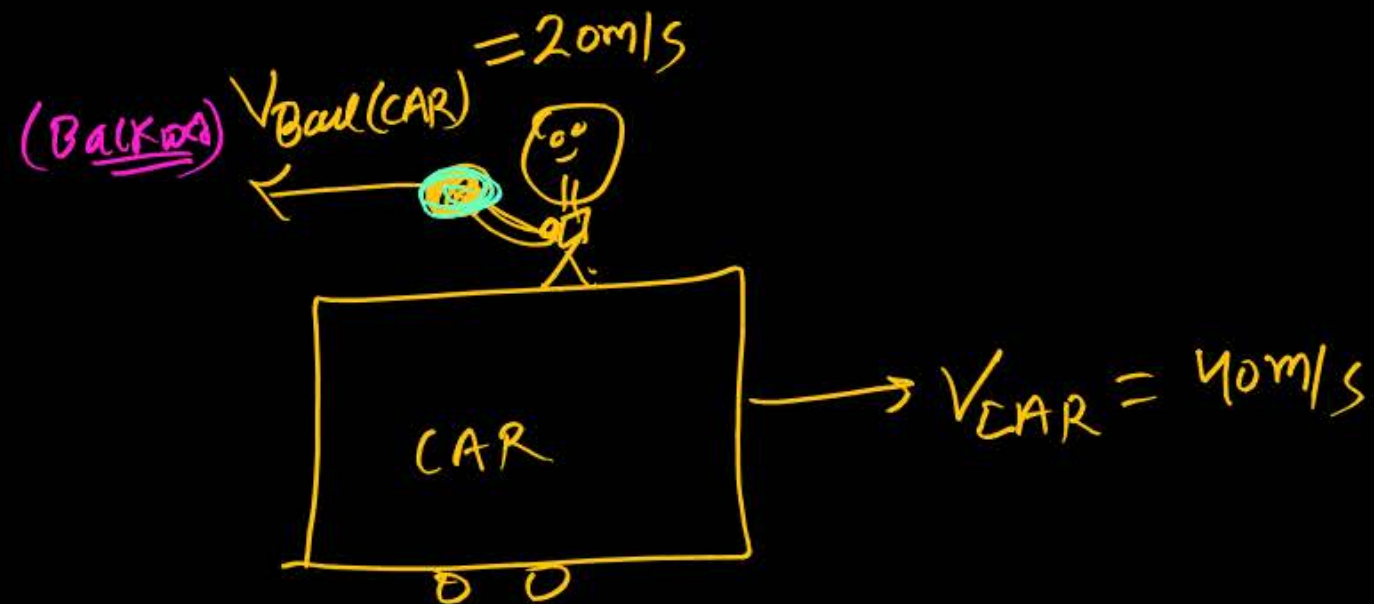
$$V_B = 8 \text{ km/hr}$$



$$U_{Ball/ground} = \underline{20\hat{j} + 40\hat{i}} \quad (60) \times \text{wrong}$$

$$\textcircled{\#} V_{Ball(CAR)} = 20 \text{ m/s } \hat{j} \quad (20) \checkmark$$

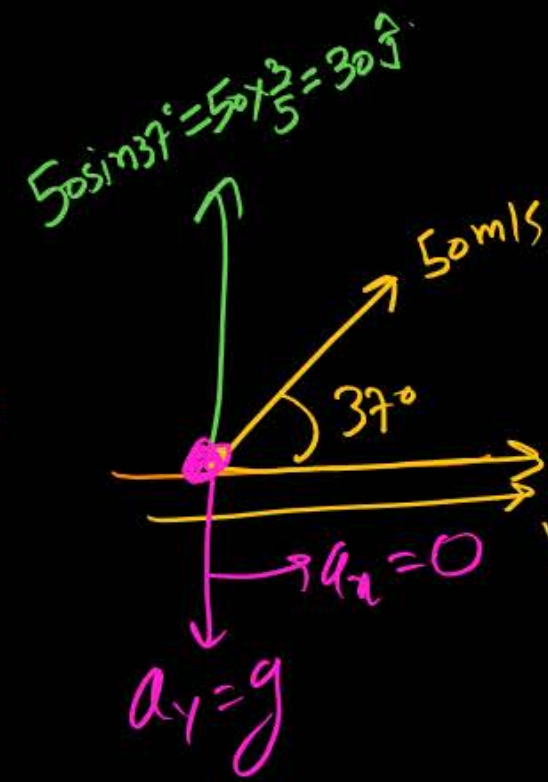
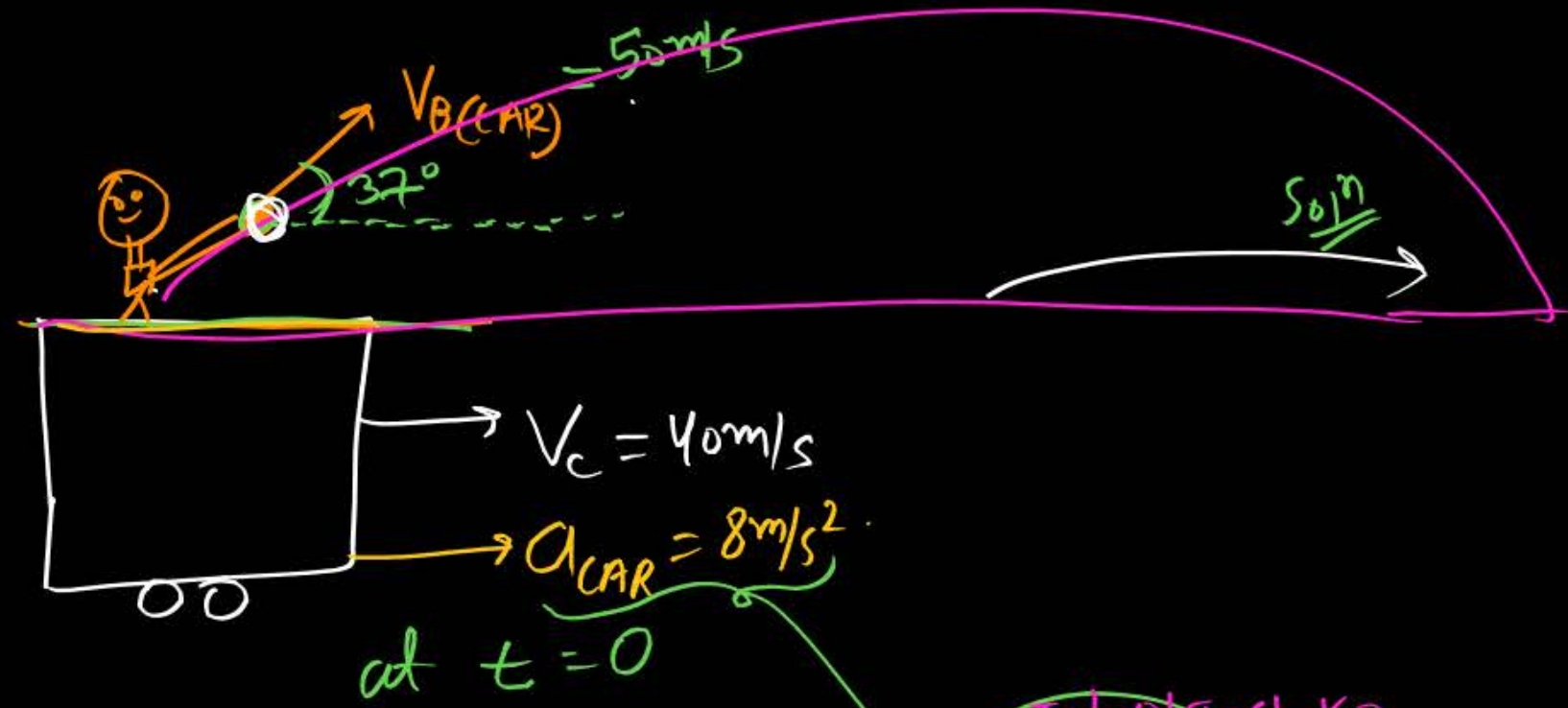
$\textcircled{\#}$ Path of Ball w.r.t (Ronaldo) or CAR is straight line
 " " " w.r.t ground = Parabola



$$U_{Ball(CAR)} = -20 \text{ m/s}$$

$$V_{Ball(ground)} = 40\hat{i} - 20\hat{i} = \underline{20\hat{i}} \quad \checkmark$$

Q



$$V_{\text{Ball Grw}} = 80 \text{ m/s } \hat{i} + 30 \hat{j}$$

find Range of Ball.

$$T_f = ??$$

$$H_{\text{max}} = ??$$

Height of CAR is negligible

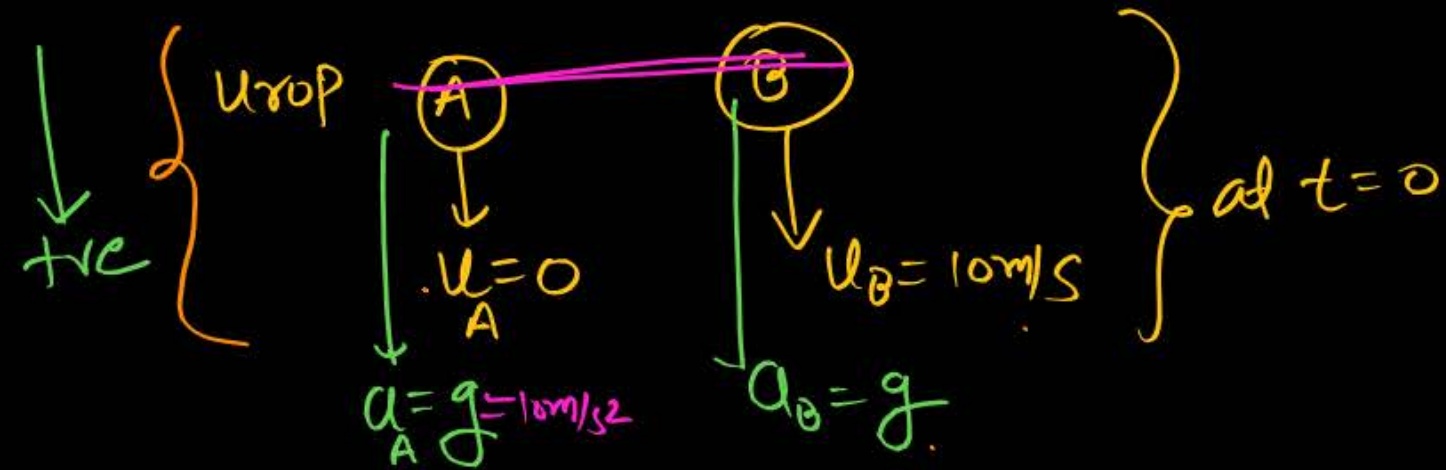
Jab object ko
Bahar thek denge.
frame ke
accⁿ object
Nahi leta
hai

$$T_f = \frac{2u_y}{g} = \frac{2 \times 30}{10} = 6 \text{ sec}$$

$$H = \frac{u_y^2}{2g} = 45 \text{ m}$$

$$R = \frac{2u_x u_y}{g} + u_x T_f = \frac{2 \times 40 \times 30}{10} + 40 \times 6 = 480 \text{ m}$$

Relative motion under gravity



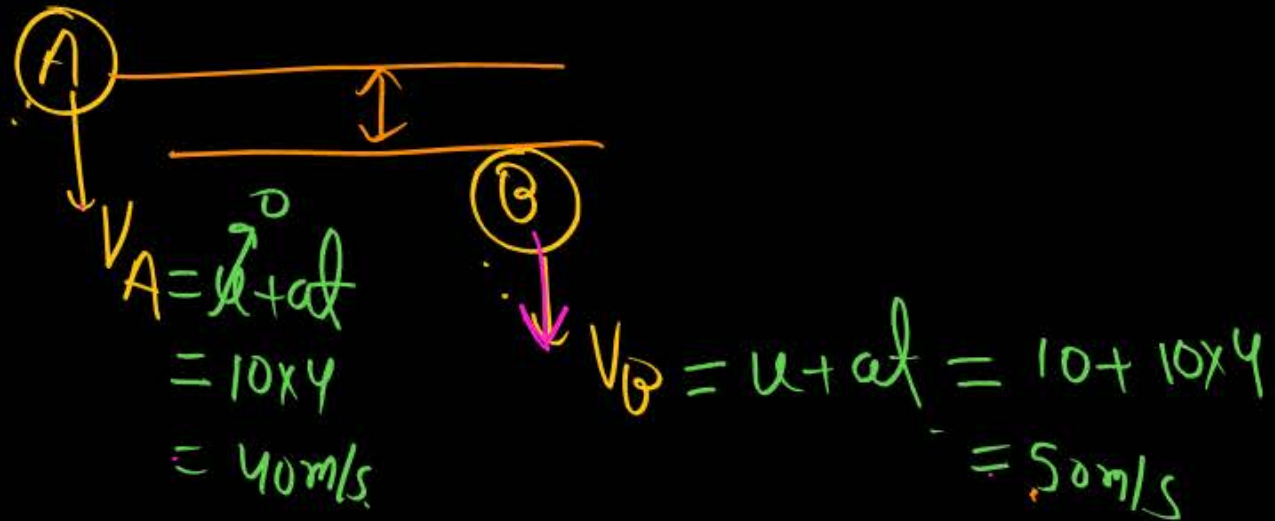
find velocity of B
w.r.t A at $t = 4 \text{ sec}$

at $t=0$

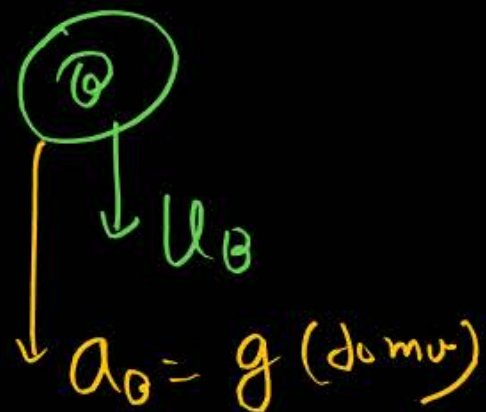
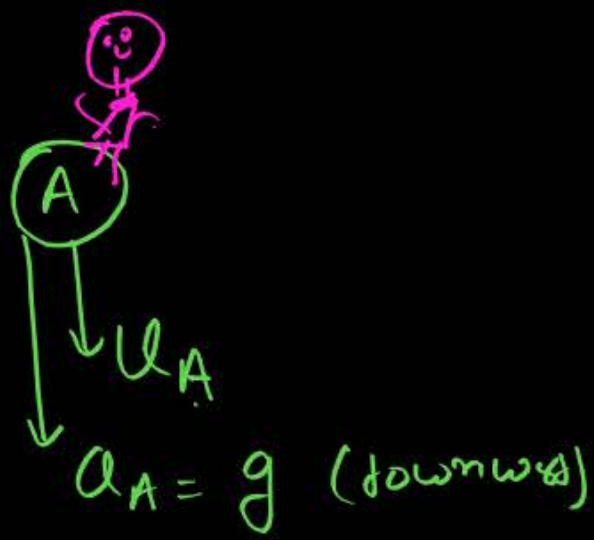
$$V_{BA} = V_B - V_A = 10 \text{ m/s}$$

Why relative velocity is constant here, velocity of A is increasing, velocity of B is increasing

at $t=4$



$$\begin{aligned} \vec{V}_{BA} &= \vec{V}_B - \vec{V}_A \\ &= 50 - 40 \\ &= 10 \text{ m/s} \end{aligned}$$



Relative motion under gravity:



$$\# \vec{a}_{BA} = g - g = 0 \quad (\text{relative acc}^n = 0)$$

$$\vec{u}_{BA} = \vec{u}_B - \vec{u}_A = \text{relative velocity} = \text{const}^n$$

relative motion uniform.

$$\vec{s}_{BA} = u_{BA}t + \frac{1}{2}a_{BA}t^2$$

$$\# \boxed{\vec{s}_{BA} = u_{BA}t}$$

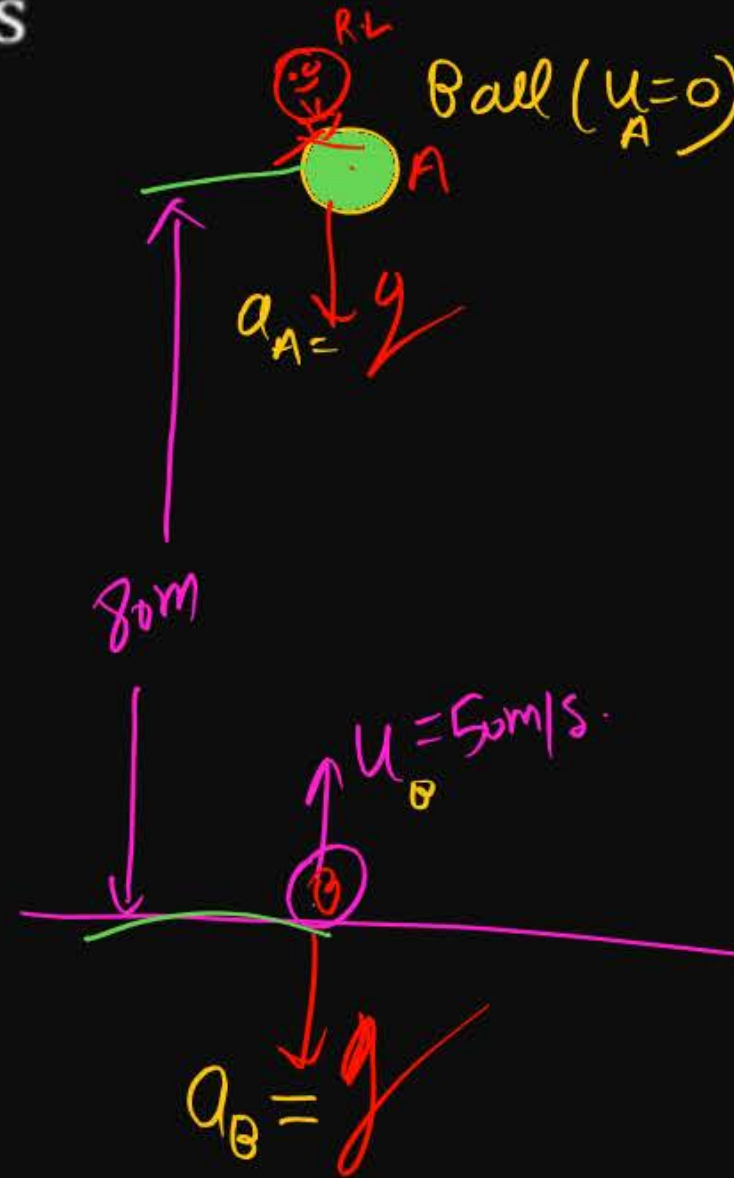
MR⁺ Box

Motion under gravity (free-fall) is non-uniform motion ($v = \text{variable}$) but motion under gravity of one object w.r.t. other object also in motion under gravity is uniform motion ($a_{AB} = 0$)

Question

A ball is dropped from the top of a building of height 80 m. At same instant another ball is thrown upwards with speed 50 m/s from the bottom of the building. The time at which balls will meet is

- 1 1.6 s ✓
- 2 5 s
- 3 8 s
- 4 10 s



$$a_{BA} = 0 \quad \checkmark$$

$$u_{BA} = 50 \text{ m/s} = u \quad \checkmark$$

$$S_{BA} = 80 \text{ m}$$

$$S_{BA} = v_{BA} t$$

$$80 = 50 t$$

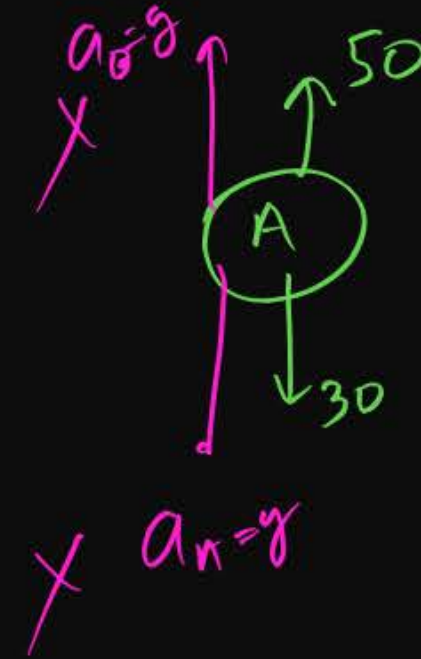
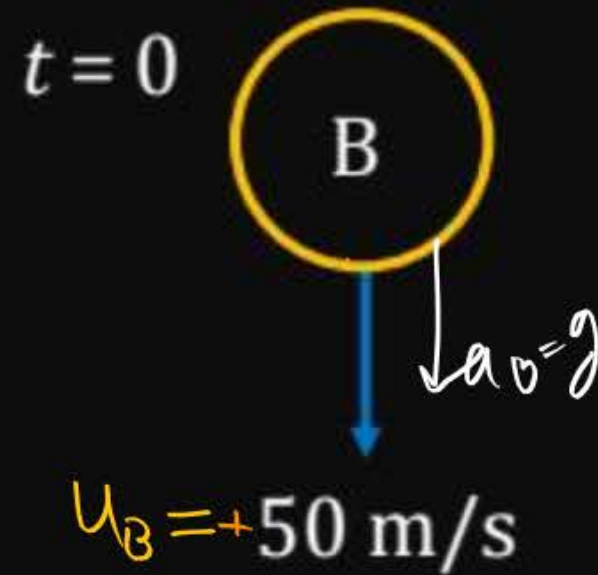
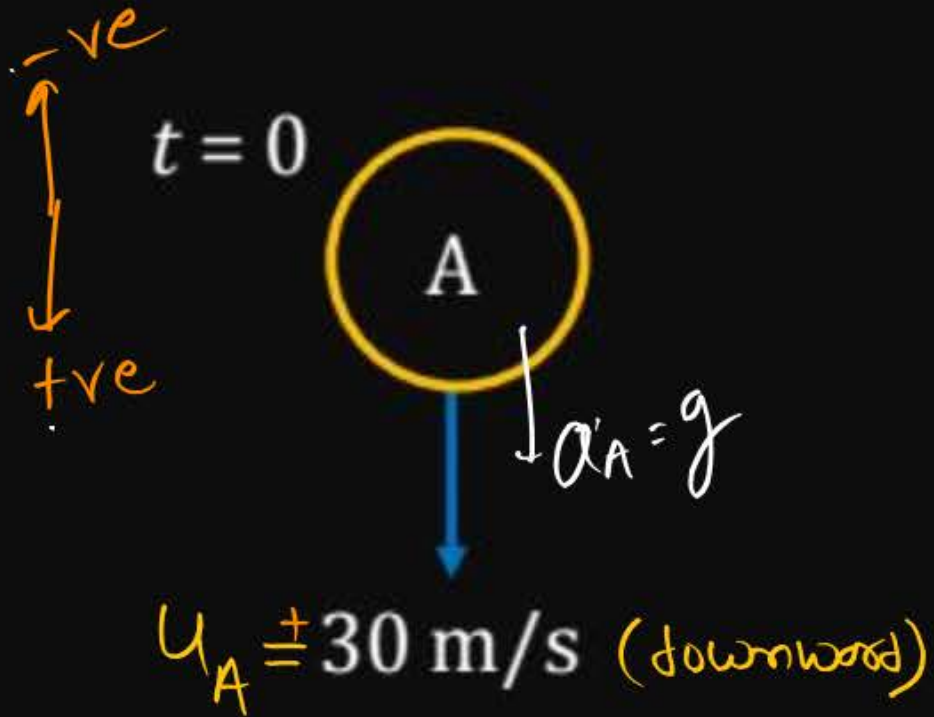
$$t = 1.6 \text{ sec}$$

Question

Likho

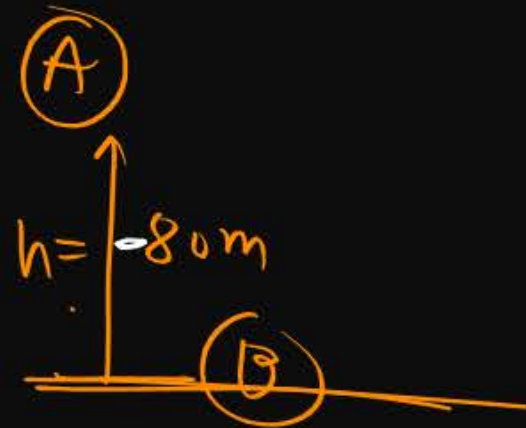


Find relative velocity of A w.r.t. B after 4 sec and distance between them.



$$\begin{aligned}\vec{u}_{AB} &= \vec{u}_A - \vec{u}_B \\ &= 30 - 50 \\ &= -20 \text{ m/s} \\ &\quad \text{(upward)}\end{aligned}$$

$$\begin{aligned}S_{AB} &= u_{AB} \times t \\ &= -20 \times 4 = -\underline{\underline{80 \text{ m}}}\end{aligned}$$



Question

A body is projected vertically up at $t = 0$ with a velocity of 98 m/s. Another body is projected from the same point with same velocity after 4 seconds. Both bodies will meet at $t =$

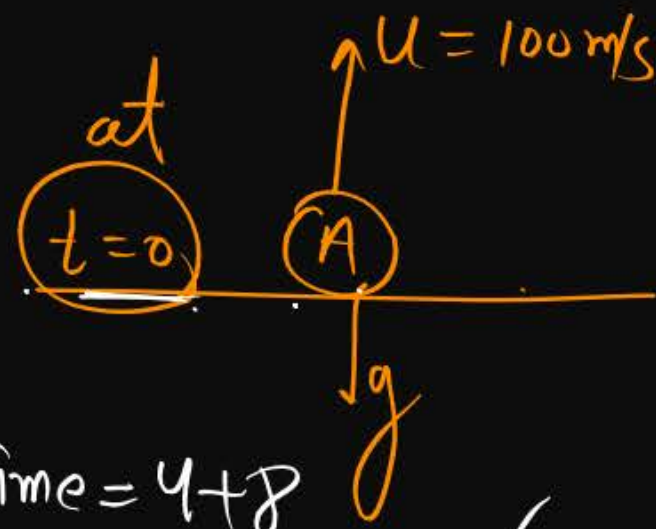
1 6 s

2 8 s

3 10 s

4 12 s

Final time = $4 + 8$
 $= 12 \text{ sec}$ ✓

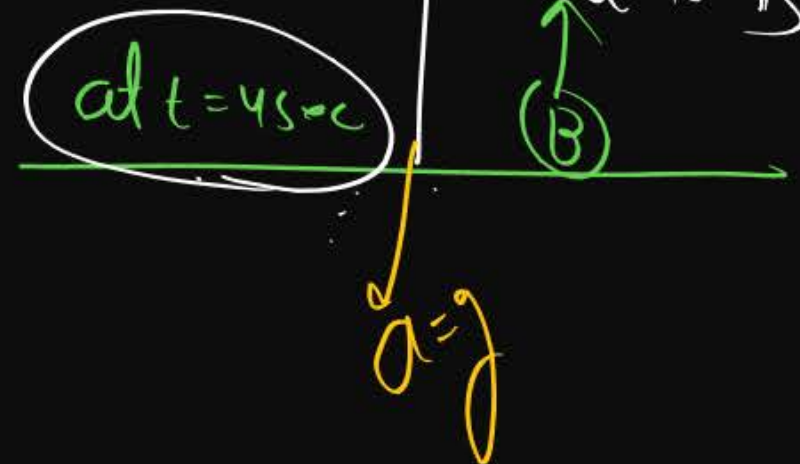


$$h = ut + \frac{1}{2} at^2$$

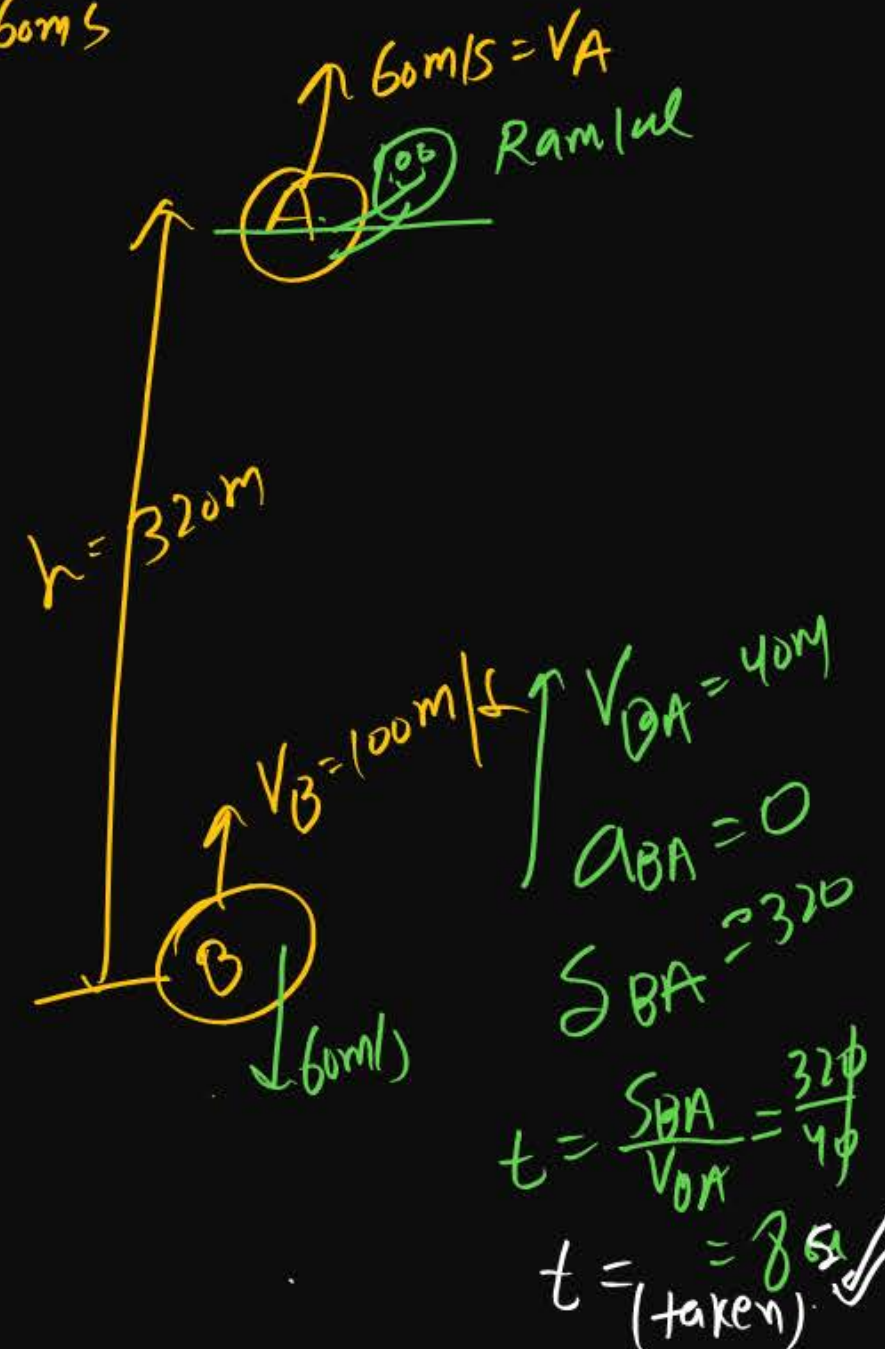
$$= 100 \times 4 - \frac{1}{2} \times 10 \times (4)^2$$

$$= 400 - 80$$

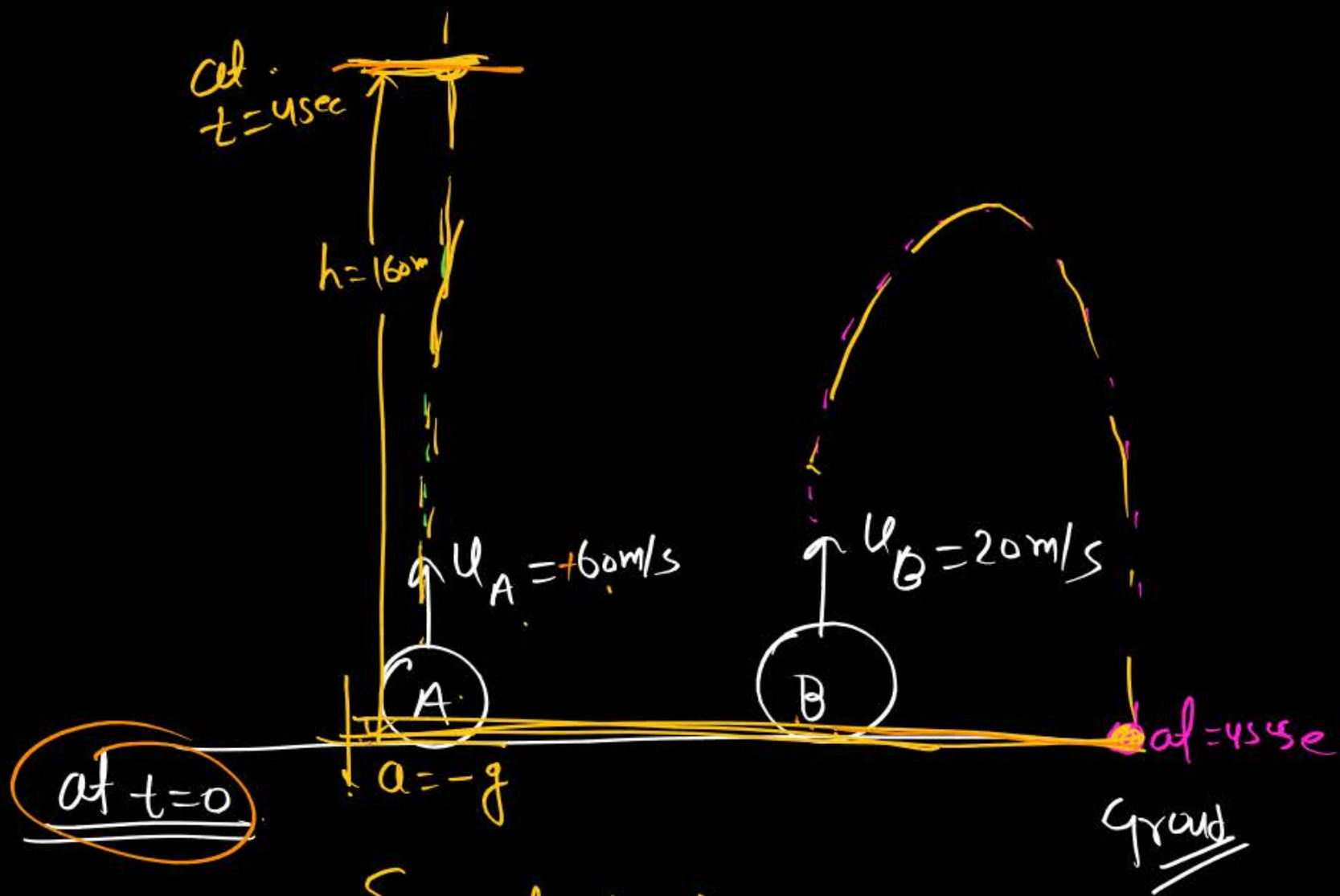
$$= 320 \text{ m}$$



$$V = u + at = 100 - 10 \times 4 = 60 \text{ m/s}$$



(easy)



$$\begin{aligned} S_A &= ut + \frac{1}{2}at^2 \\ &= 60 \times 4 - \frac{1}{2} \times 10 \times (4)^2 \\ &= 240 - 5 \times 16 \\ &= 240 - 80 = \underline{\underline{160\text{m}}} \end{aligned}$$

find distⁿ B/w them at $t=4\text{sec}$ ✓

direct relative

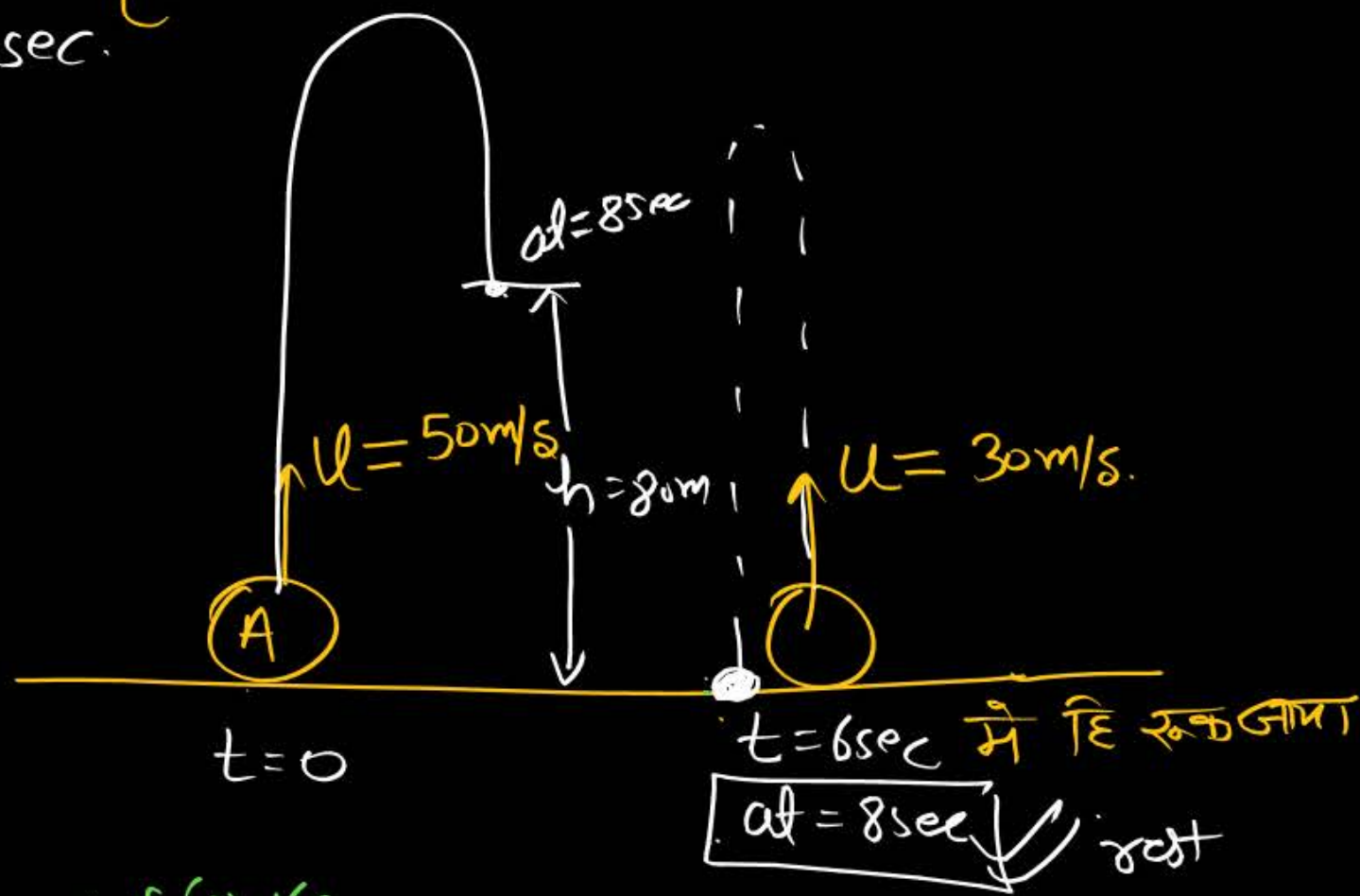
$$u_{AB} = 60 - 20 = 40\text{m/s.}$$

$$S_{AB} = u_{AB} \times t = 40 \times 4$$

$$= 160\text{m}$$

~~Beauty~~
Beauty

Q) distⁿ b/w them
at t = 8-sec. (level up)



sirif 'A' Ka

$$\begin{aligned}
 S_A &= ut + \frac{1}{2}at^2 \\
 &= 50 \times 8 - \frac{1}{2} \times 10 \times (8)^2 \\
 &= 400 - 64 \times 5 \\
 &= 400 - 320 \\
 &= \underline{80\text{m}}
 \end{aligned}$$

Solⁿ

$$u_{AB} = 50 - 30 = 20\text{m/s}$$

$$a_{AB} = 0$$

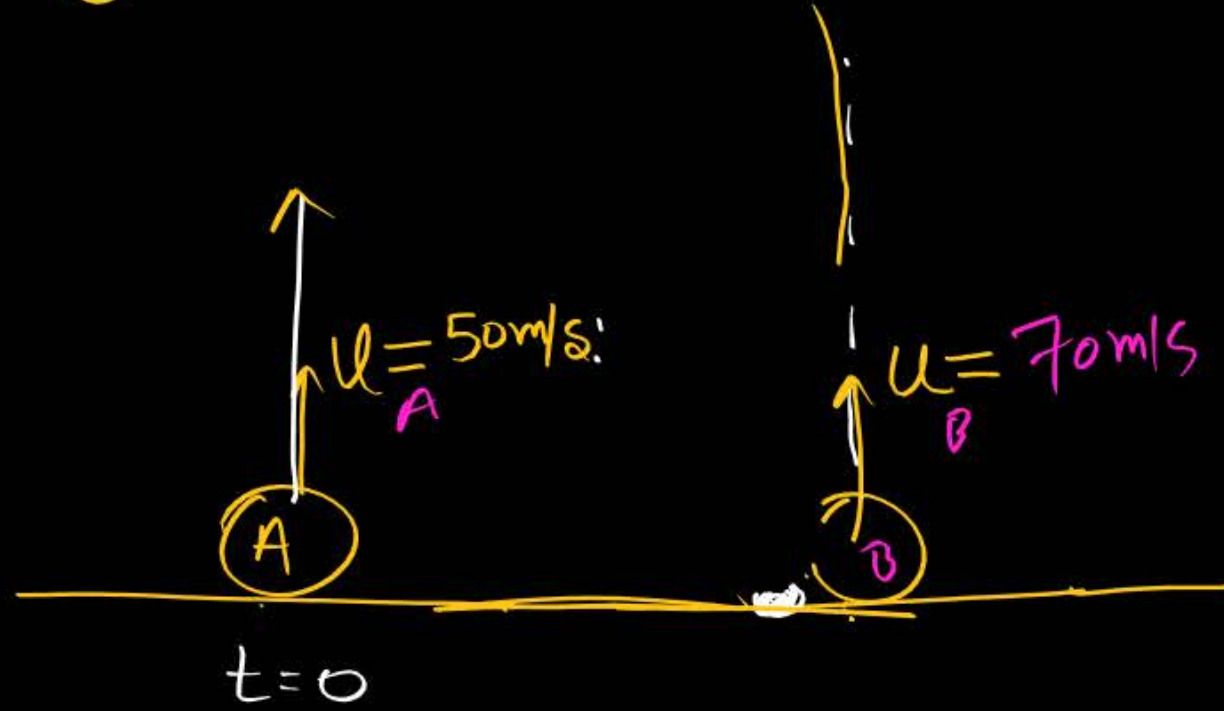
MR SCAM

$$\begin{aligned}
 S_{AB} &= u_{AB} \times t \\
 &= 20 \times 8 \\
 &= 160\text{m}
 \end{aligned}$$

Reason \rightarrow $t=0$ to $t=8\text{sec}$
tak relative a_{BA}
zero nahi hai

distⁿ = 80m
b/w them

Q) distⁿ b/w them
at t = 8-sec. (level up)



Solⁿ

$$u_{BA} = 70 - 50 \\ = 20 \text{ m/s}$$

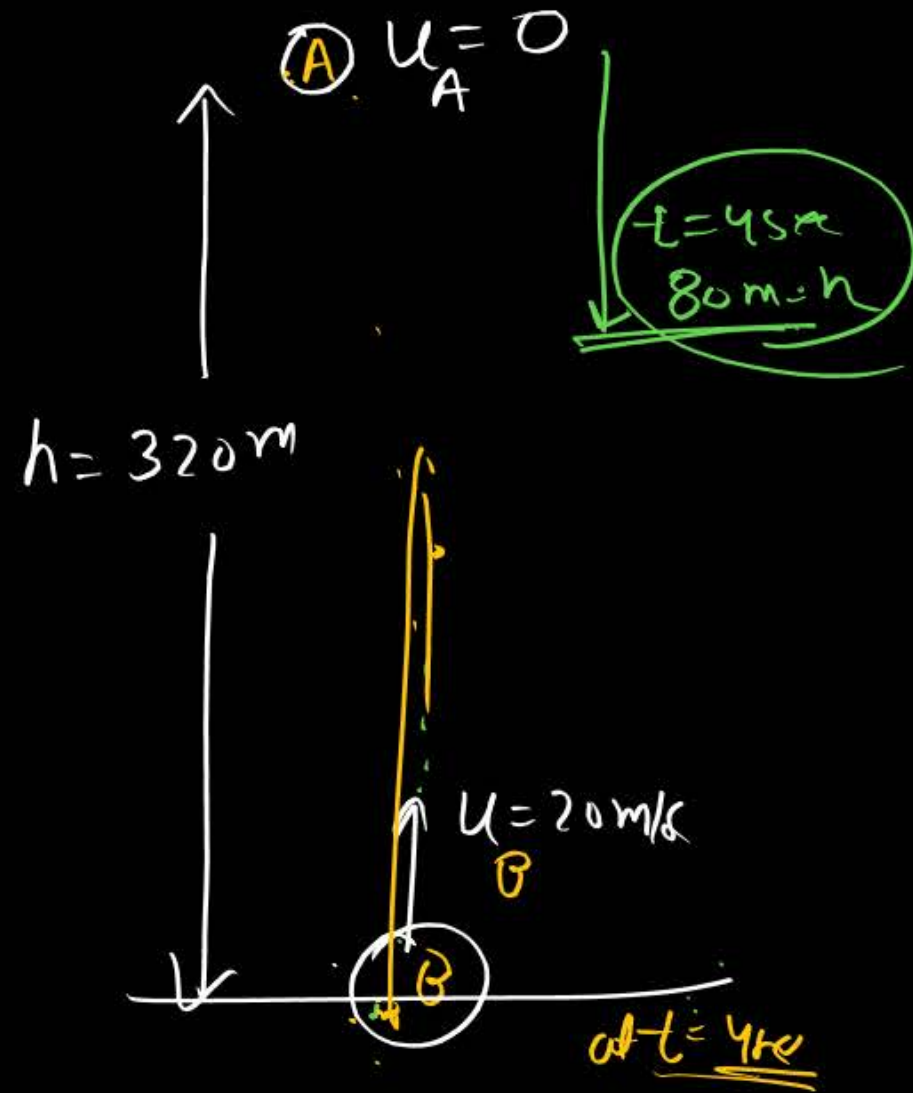
$$S_{BA} = u_{BA} t \\ = 20 \times 8 \\ = 160 \text{ m}$$

correct

IMP⁺ BOX

relative motⁿ tavi
lagega Tab question
me given time t dono
ke time of flight
se kam ho.

- ① Ball is dropped from height 320 m/s, other is projected up with 20 m/s.
then find time when it will collide in air.



use question
no option
se khelenge

Solⁿ

~~MR scam ✓~~

$a_{BA} = 0$

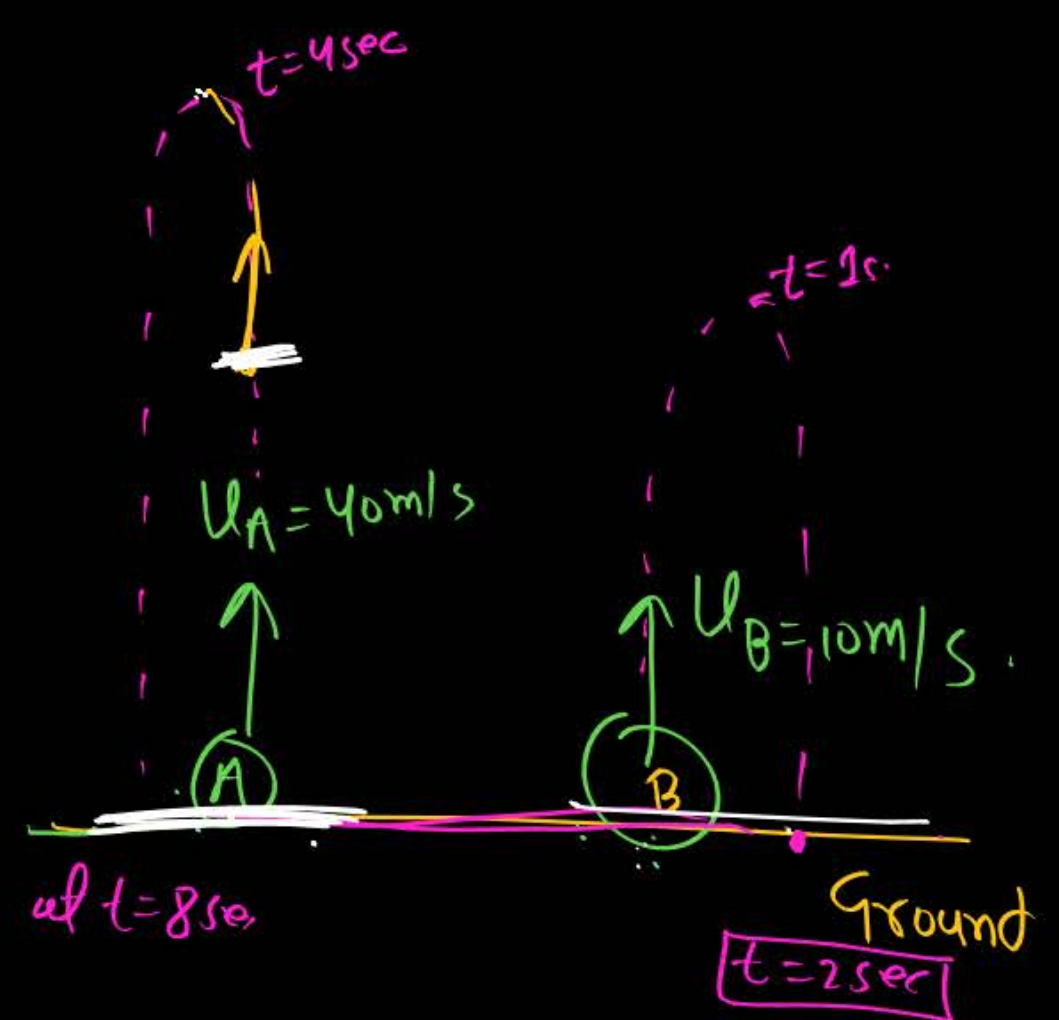
$u_{BA} = 20$

$t = \frac{h}{u_{BA}} = \frac{320}{20} = 16 \text{ sec}$

they will not collide in air

→ They can collide at ground at $t = 8 \text{ sec}$

JEE-Adv
 (8)

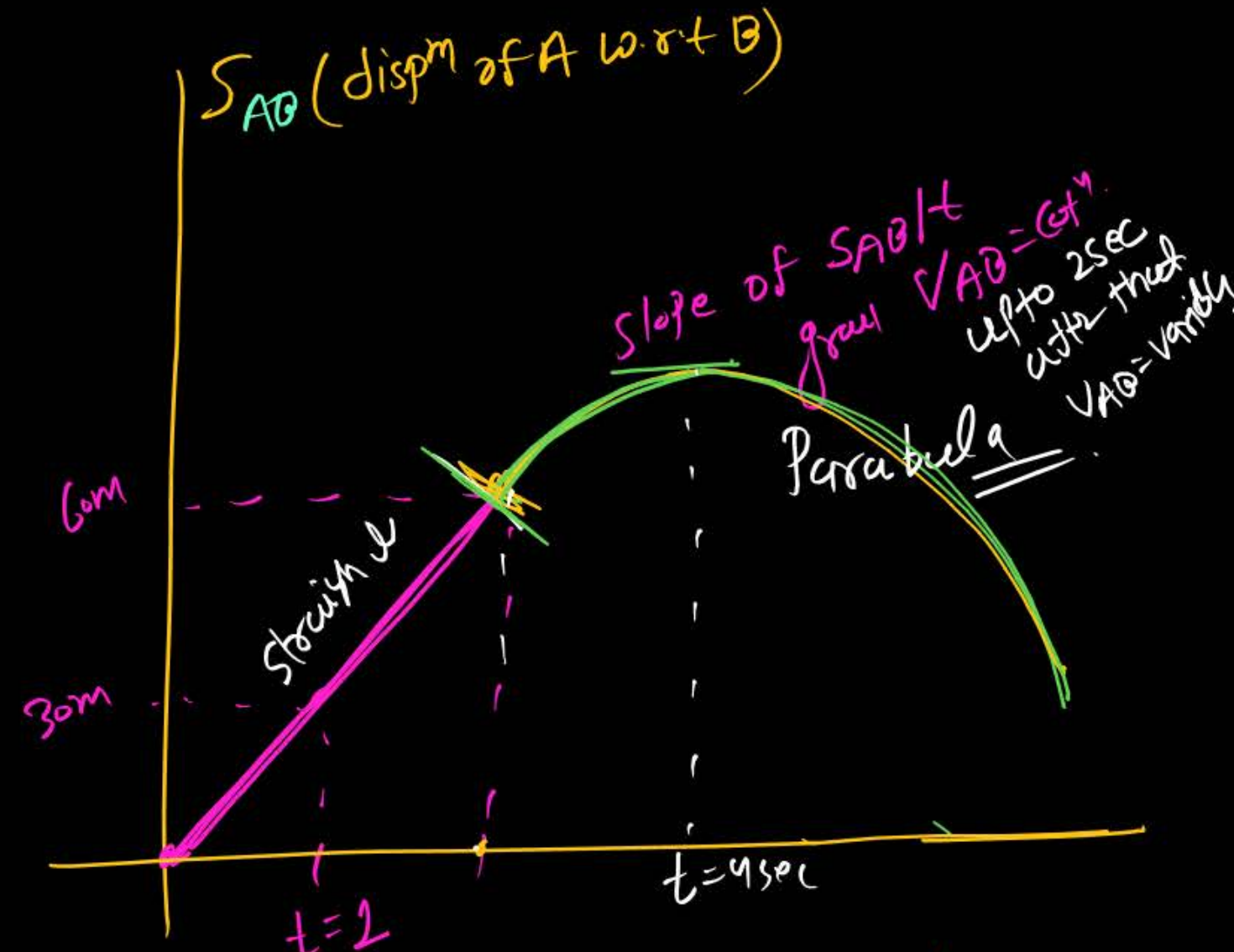


Solⁿ relative motion

$$a_{AB} = 0$$

$$u_{AB} = 40 - 10 = 30 \text{ m/s}$$

$$S_{AB} = u_{AB} \times t = 30t$$



at $t=2 \text{ sec}$ B comes to rest

$$\left. \begin{array}{l} u_B = 0 \\ a_B = 0 \end{array} \right\} \text{ \& \& no ke Bud.}$$

after $t=2 \text{ sec}$ only A is moving

$$u_A = +20 \text{ m/s} \quad a_{rel}^A = -g \text{ m/s}^2$$

Relative motion in 2-D (vector subtract)

(A) $\rightarrow 10 \text{ m/s } \hat{i}$ (east)

(B) $\uparrow 10 \text{ m/s } \hat{j}$ (North)

$\vec{v}_{AB} = ??$

$\vec{v}_{BA} = ??$

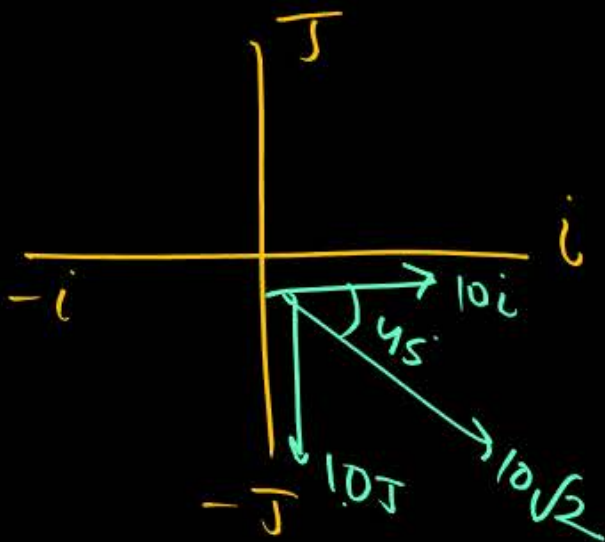
Soln

$$\vec{v}_{AB} = \vec{v}_A - \vec{v}_B$$

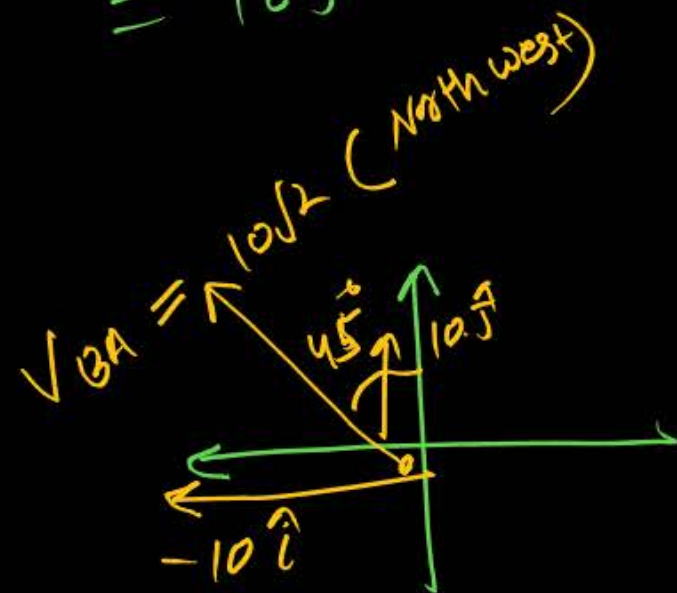
$$\vec{v}_{AB} = 10\hat{i} - 10\hat{j}$$

$$|\vec{v}_{AB}| = 10\sqrt{2}$$

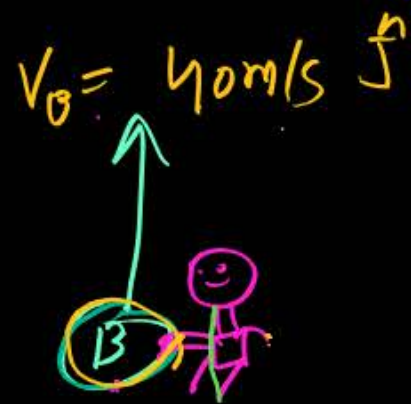
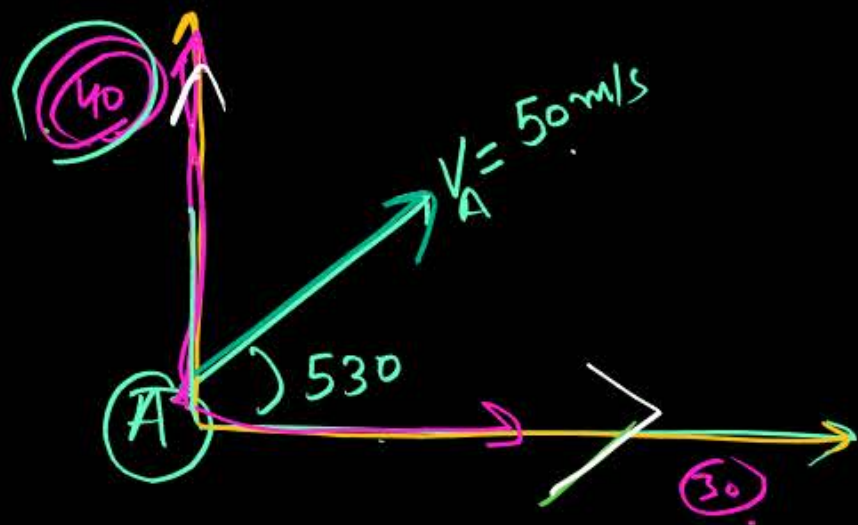
South East



$$\vec{v}_{BA} = \vec{v}_B - \vec{v}_A$$
$$= 10\hat{j} - 10\hat{i}$$



Q



find $V_{AB} = ??$

Soln

$$\vec{V}_A = V_A \cos 53^\circ \hat{i} + V_A \sin 53^\circ \hat{j}$$

$$= 50 \times \frac{3}{5} \hat{i} + 50 \times \frac{4}{5} \hat{j}$$

$$\vec{V}_A = 30\hat{i} + 40\hat{j}$$

$$\vec{V}_B = 40\hat{j}$$

$$\begin{aligned} \vec{V}_{AB} &= \vec{V}_A - \vec{V}_B \\ &= 30\hat{i} + 40\hat{j} - 40\hat{j} \end{aligned}$$

$$\vec{V}_{AB} = 30\hat{i}$$

Velocity of A w.r.t B

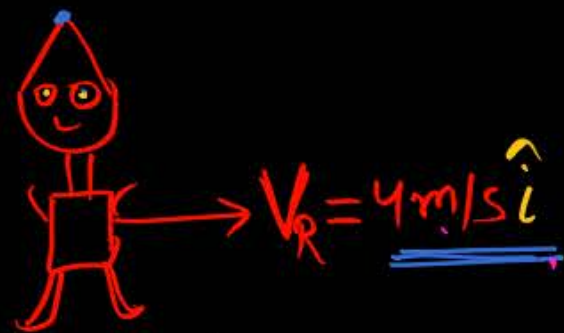
$$\vec{V}_{BA} = -\vec{V}_{AB} = -30\hat{i} \text{ m/s}$$

mpd



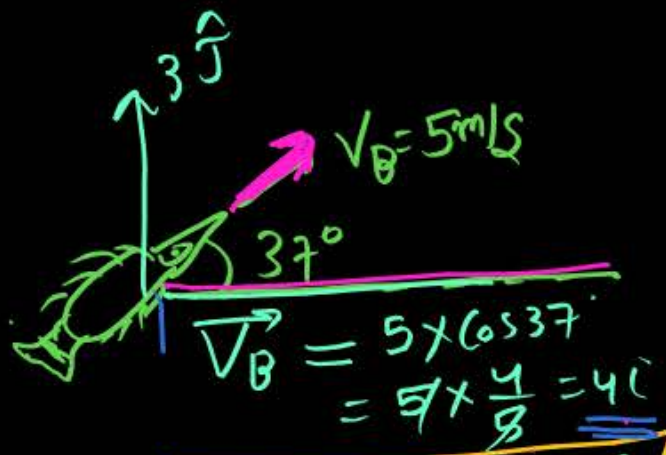
Sun

$$\vec{V}_B(\text{mp}) = 4\hat{i} + 3\hat{j}$$

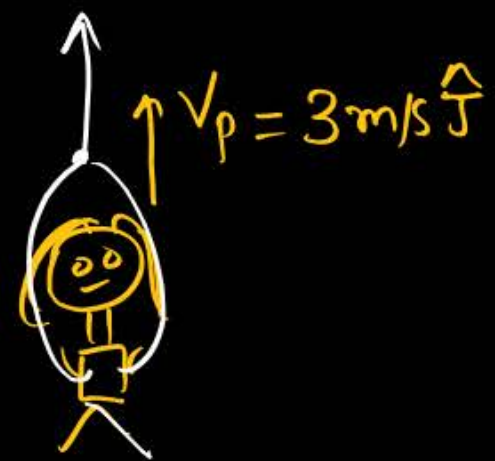


Ramlu

$$\vec{V}_{Rg} = 4\hat{i} + 0\hat{j}$$



$$\vec{V}_{\text{Bird Gr}} = 4\hat{i} + 3\hat{j}$$



$$\vec{V}_{Pg} = 0\hat{i} + 3\hat{j}$$

$$\vec{U}_{\text{Pinky w.r.t Bird}} = -4\hat{i}$$

$$\begin{aligned} \vec{U}_{B \text{ Ramlu}} &= \vec{V}_B - \vec{V}_R \\ &= 4\hat{i} + 3\hat{j} - 4\hat{i} \\ \vec{U}_B(\text{Ramlu}) &= 3\hat{j} \end{aligned}$$

\vec{V}_{BR} (upward arrow)

$$\vec{U}_{\text{Ramlu Bird}} = -3\hat{j}$$

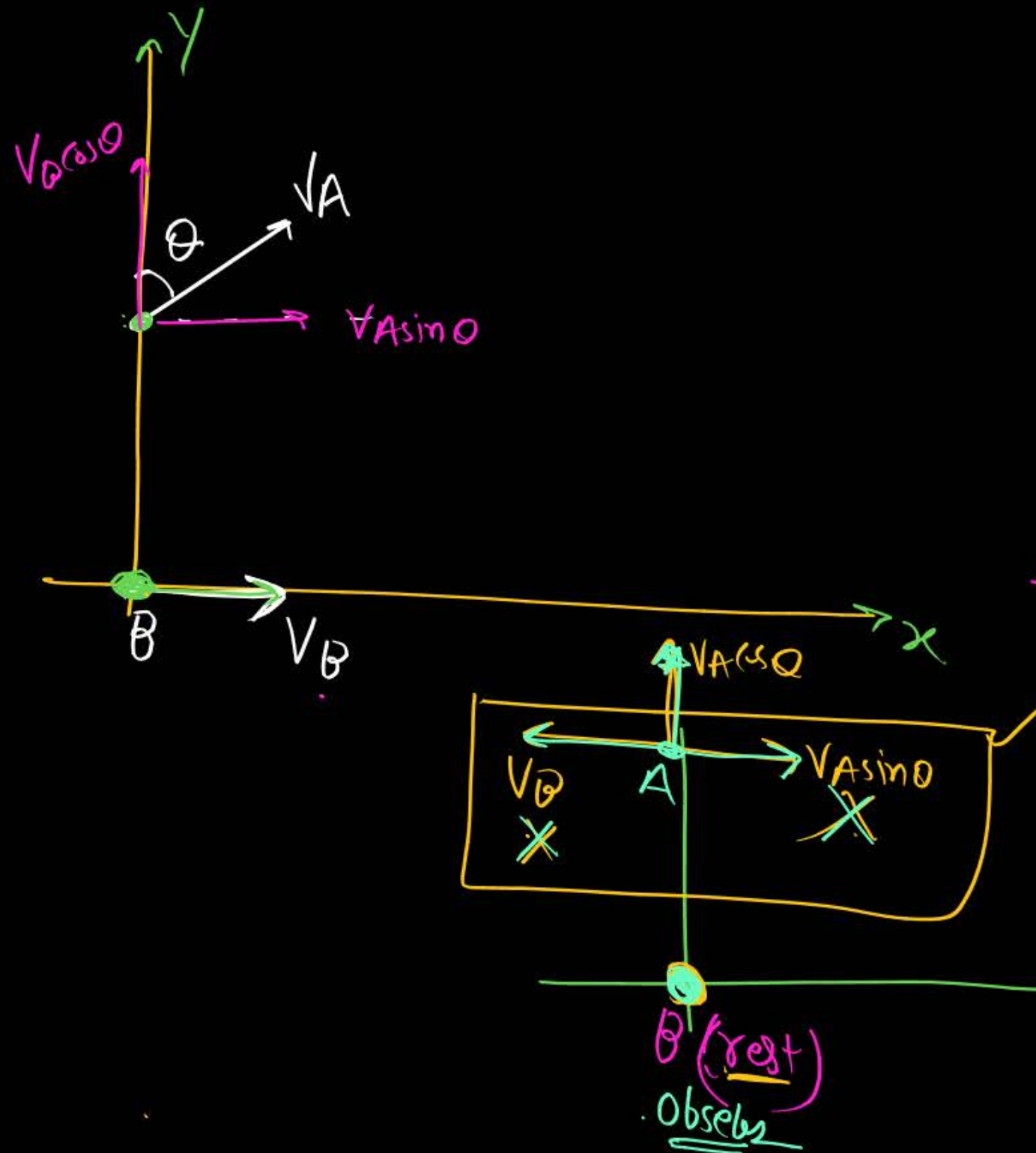
\vec{V}_{BR} (downward arrow)

$$\begin{aligned} \vec{U}_{B \text{ Pinky}} &= \vec{V}_B - \vec{V}_P \\ &= 4\hat{i} + 3\hat{j} - 3\hat{j} \end{aligned}$$

$$\vec{V}_{\text{Bird (Pinky)}} = 4\hat{i}$$

\vec{V}_{BP} (rightward arrow)

AIEEE (JEE Main)



Find $\frac{V_A}{V_B}$ so that
A appears to move
in vertical upward
w.r.t B

Soln

$$V_A \sin \theta = V_B$$

$$\frac{V_A}{V_B} = \left(\frac{1}{\sin \theta} \right) = \underline{\underline{\csc \theta}}$$

Question

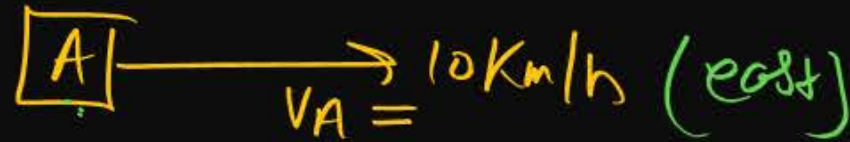
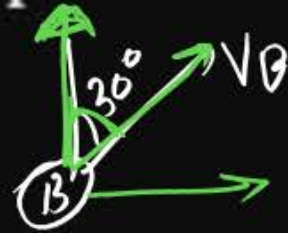
A ship is travelling due east at 10 km/h. ^{other} A ship heading 30° east of north is always due north from the first ship. The speed of the second ship in km/h is:

1 $20\sqrt{2}$

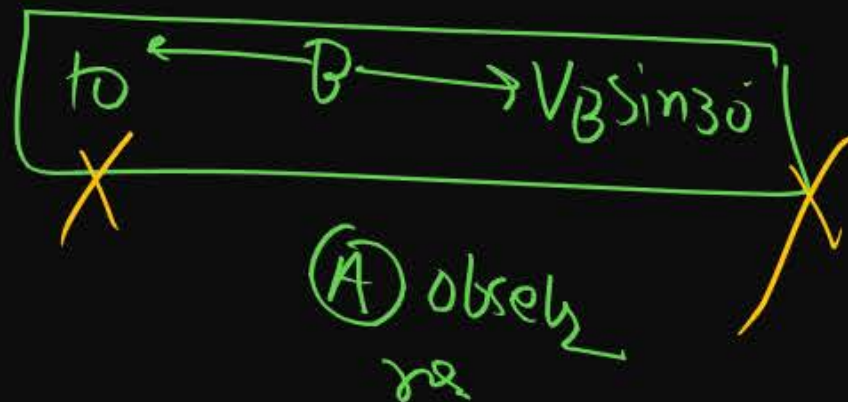
2 $20\sqrt{3/2}$

3 20

4 $20/\sqrt{2}$

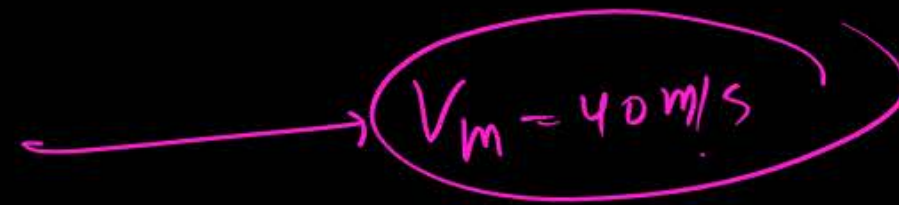
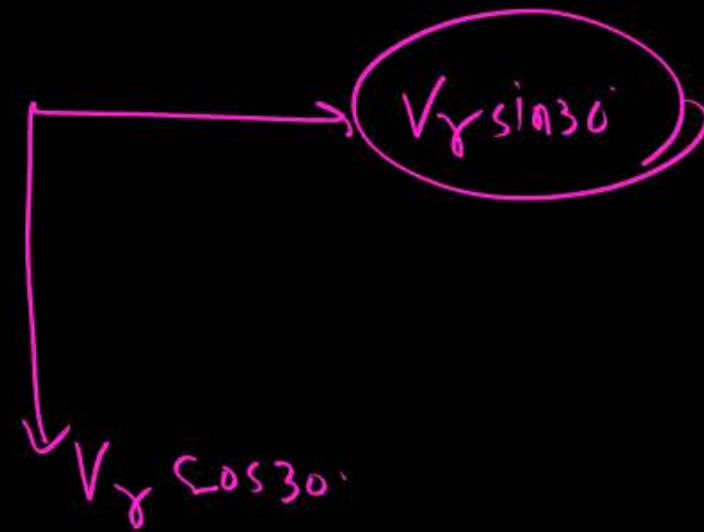
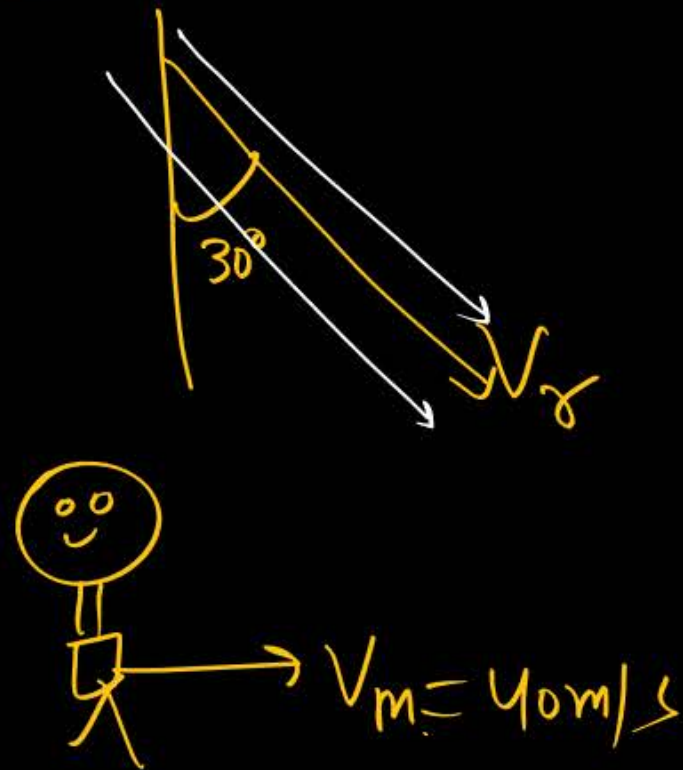


$(u_{BA}) = 0$ in east



$V_B \times \frac{1}{2} = 10$
 $V_B = 20 \text{ km/h}$

Rain man Probⁿ



rain falling at angle 30°
from vertical ✓ [as shown in fig ✓]
find V_r so that

rain falling vertical
downward w.r.t
man ✓

(rain appear to fall
vertically down
w.r.t man)

$$V_r \frac{1}{2} = 40$$

$$V_r = \underline{2 \times 40 = 80 \text{ m/s}}$$

Question



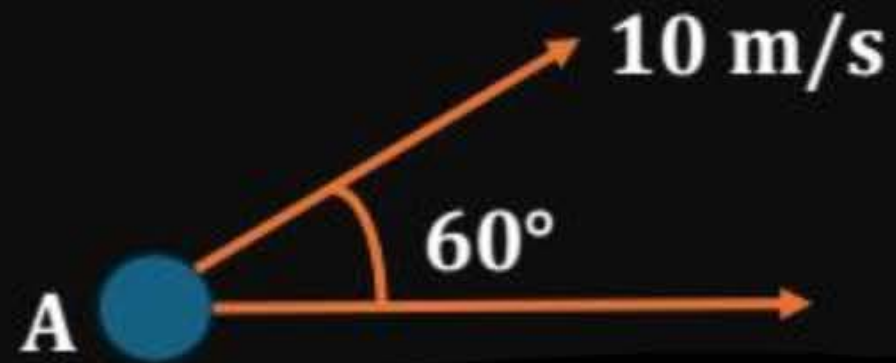
A bird is flying with a speed of 40 km/hr. in the north direction. A train is moving with a speed of 40 km/hr. in the west direction. A passenger sitting in the train will see the bird moving with velocity :-

H/w must
Try

- 1 40 km/hr in NE direction
- 2 $40\sqrt{2}$ km/hr in NE direction
- 3 40 km/hr in NW direction
- 4 $40\sqrt{2}$ km/hr in NW direction

Question

Find velocity of A with respect to B.



Must H/W

Question



Velocity of Ramlal $\vec{V}_R = -3\hat{i} + 4\hat{j}$ and velocity of Pinky $\vec{V}_P = 4\hat{i} + 3\hat{j}$ then find velocity of Ramlal with respect to Pinky.

H/w

Question



Car is moving with 30 m/s along east and truck is moving with speed 40 m/s at 30° N of E w.r.t. car then find velocity of truck.

H/W

Question



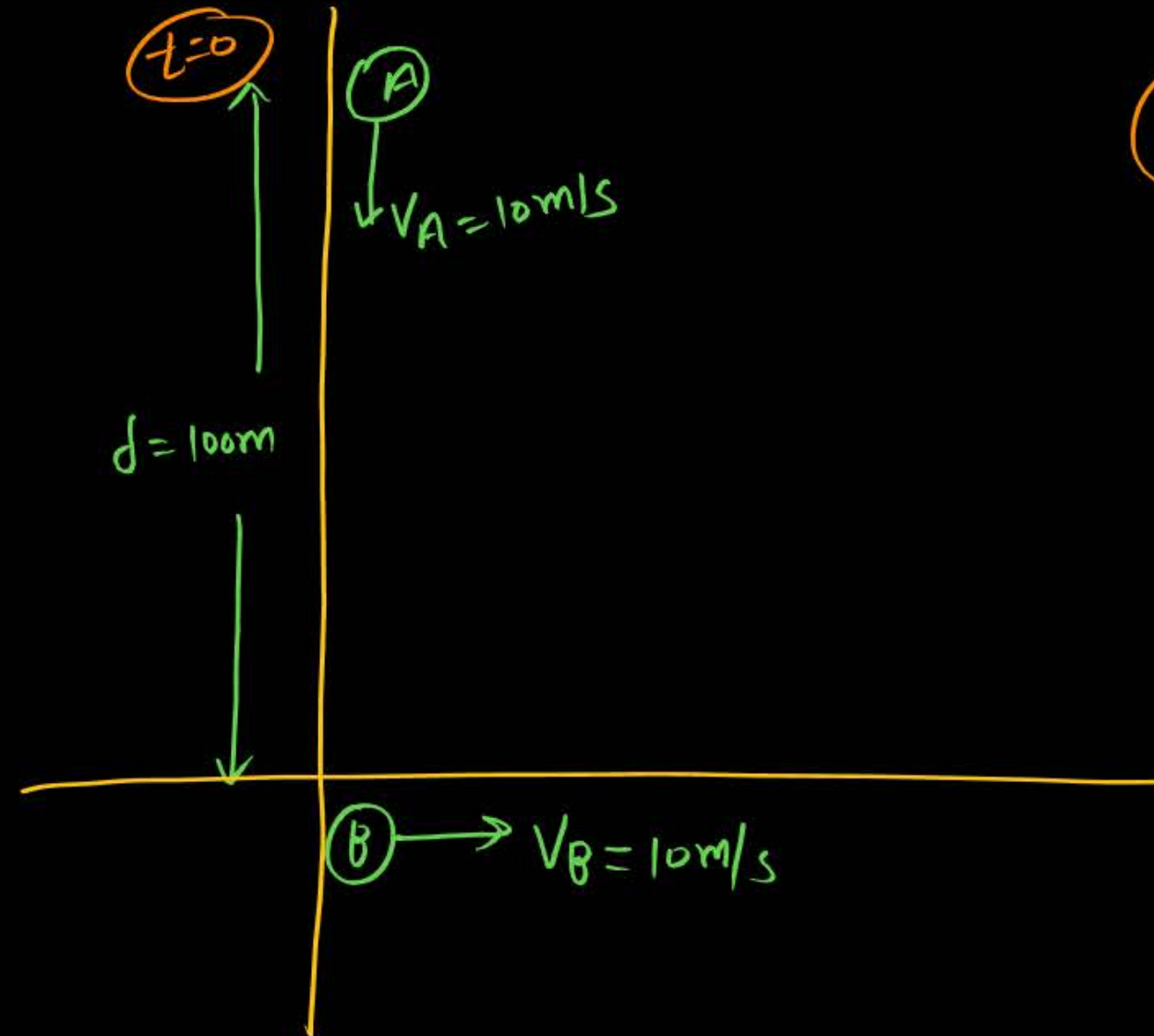
A man 'A' moves in the north direction with a speed 10 m/s and another man B moves in $E-30^\circ-N$ with 10 m/s . Find the relative velocity of B w.r.t. A.

H/w

Minimum separation

Position and velocity of A & B
at $t=0$ shown in fig.

then find minimum
separation b/w A & B



H/w

must Try

- Velocity of man with respect to river
- Velocity of man with respect to still water
- Velocity of man by which he can swim

All are same.

{MR* Boy}

THANK
YOU