Vectors

Assignment-02 By: M.R. Sir

1. Check which of the following is a unit vector:

(1)
$$\vec{A} = \frac{1}{\sqrt{3}}\hat{i} + \frac{1}{\sqrt{3}}\hat{j}$$

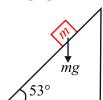
(2)
$$\vec{B} = \sin\theta \hat{i} - \cos\theta \hat{j}$$

(3)
$$\vec{C} = \frac{\hat{i}}{\sqrt{3}} - \frac{\hat{j}}{\sqrt{3}} + \frac{\hat{k}}{\sqrt{3}}$$

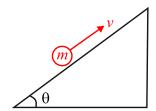
(4)
$$\vec{D} = 0.8\hat{i} - 0.6\hat{j}$$

(5)
$$\vec{E} = \frac{3}{5}\hat{i} + \frac{4}{5}\hat{j}$$

- **2.** Draw given vector in graphical representation: Force 10 N 30° North of East
- **3.** Find component of gravitational force along inclined plane and perpendicular to inclined plane.



4. Component of velocity along x and y-axis.



5. Find unit vector of given vector:

$$\vec{A} = 3\hat{i} + 4\hat{j}$$

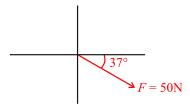
$$\vec{B} = -3\hat{i} + 4\hat{j} - 5\hat{k}$$

$$\vec{C} = 2\hat{i} + 3\hat{j} - \hat{k}$$

$$\vec{D} = \hat{i} + \hat{j} - 2\hat{k}$$

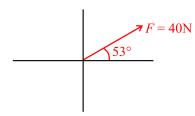
6. Following vector are given:

Then write it in vector form



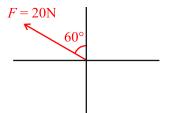
7. Following vector are given:

Then write it in vector form



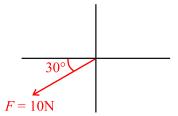
8. Following vector are given:

Then write it in vector form



9. Following vector are given:

Then write it in vector form



10. Draw given vector in graphical representation:

Object is moving with velocity 60 m/s at 60° South of west



- 11. Draw given vector in graphical representation: 30 N force at 53° North of West
- 12. Draw given vector in graphical representation: Force 40 N 53° South of East
- A null vector is defined as a vector having: 13.
 - (1) Zero Direction
 - (2) Zero magnitude and undefined direction
 - (3) Maximum magnitude and fixed direction
 - (4) Zero magnitude and fixed direction
- Which of the following sets can never represent a 14. system of collinear vectors?
 - (1) 2 N right, 3 N right, 5 N left
 - (2) 2 N up, 4 N up, 6 N down
 - (3) 2 N right, 3 N up, 4 N down
 - (4) 5 N left, 5 N right
- If $\vec{A} + \vec{B} = 0$, what is the value of $|\vec{A}| + |\vec{B}|$? 15.
 - (1) 0
- (3) 2|A|
- **16.** Which of the following sets of components gives a vector of zero magnitude?
 - (1) (0,0)
- (2) (3, -3)
- (3) (1,-1)
- (4) (2, 2)
- A vector \vec{A} has a magnitude of 5. You are told that 17. the x-component of this vector is also 5.

What can you conclude about the *y*-component?

- (1) It is zero
- (2) It is positive
- (3) It is imaginary
- (4) It is negative

- A vector \vec{V} has a magnitude of 1 and makes equal 18. angles with x, y and z axes. What is each component?

- 19. A person walks 1 m east, then 1 m north. What is the unit vector in the direction of net displacement?
 - (1) $\frac{1}{\sqrt{2}}(\hat{i} + \hat{j})$ (2) $\frac{1}{2}(\hat{i} + \hat{j})$
- - (3) $\left(\hat{i} + \hat{j}\right)$ (4) $\frac{1}{\sqrt{3}}\left(\hat{i} + \hat{j}\right)$
- Let $\vec{A} = a\hat{i} + b\hat{j}$ be a unit vector. If $a = \frac{3}{5}$, find b.

- 21. Assertion (A): The sum of two unit vectors can never be a unit vector.

Reason (R): The magnitude of the sum of two unit vectors is always greater than 1.

- (1) Both A and R are true, and R is the correct explanation of A.
- (2) Both A and R are true, but R is not the correct explanation of A.
- (3) A is false, but R is true.
- (4) Both A and R are false.
- 22. Three equal vectors are placed head to tail forming a triangle. What is the resultant vector?
 - (1) Equal to each vector
 - (2) 0
 - (3) Double of one vector
 - (4) Cannot be determined

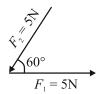


- **23.** Two vectors are added and the resultant is smaller than both. What must be the angle between them?
 - $(1) < 90^{\circ}$
- $(2) = 90^{\circ}$
- $(3) > 90^{\circ}$
- $(4) = 0^{\circ}$
- **24.** Vector addition is commutative.
 - (1) True
- (2) False
- **25.** Vector addition violates the triangle inequality.
 - (1) True
- (2) False
- **26.** Assertion (A): The direction of the vector $\vec{A} + \vec{B}$ lies between the directions of \vec{A} and \vec{B} .

Reason (R): Vector addition follows the triangle law or parallelogram law of vectors.

- (1) Both A and B are true, and R is the correct explanation of A.
- (2) Both A and R are true, but R is not the correct explanation of A.
- (3) A is false, but R is true
- (4) Both A and B are false
- **27.** Triangle law of vector addition holds when vectors are:
 - (1) Collinear
 - (2) Coplanar and in same direction
 - (3) Represented as two adjacent sides of a triangle taken in same order
 - (4) Draw from the same origin
- 28. A particle undergoes two displacements represented by vectors \vec{A} and \vec{B} , making an angle θ between them. If resultant displacement is less than both A and B, what can be said about θ ?
 - (1) $\theta = 0^{\circ}$
- (2) $\theta = 90^{\circ}$
- (3) $\theta > 90^{\circ}$
- (4) $\theta = 180^{\circ}$
- **29.** Two forces of magnitude 8 N and 15 N respectively act at a point. If the resultant forces is 17 N, the angle between the forces has to be
 - $(1) 60^{\circ}$
- (2) 45
- (3) 90°
- $(4) 30^{\circ}$

- **30.** Two $\vec{F}_1 = 5$ N due to east and $F_2 = 10$ N due north then resultant of these two force is
 - (1) $5\sqrt{5}$ N
- (2) 15 N
- (3) 5 N
- (4) $\sqrt{5}$ N
- **31.** Find net force = $(\vec{F_1} + \vec{F_2})$?



- **32.** Two forces of 10 N and 6 N act upon a body. The direction of the forces are unknow. The resultant forces on the body may be
 - (1) 15 N
- (2) 3 N
- (3) 17 N
- (4) 2 N
- 33. If $\vec{R} = \vec{A} + \vec{B}$ and R = A + B then angle between \vec{A} and \vec{B} must be
 - (1) 90°
- $(2) 60^{\circ}$
- $(3) 0^{\circ}$
- (4) 180°
- **34.** If $\vec{R} = \vec{A} + \vec{B}$ and $R^2 \pm A^2 + B^2$ then angle between \vec{A} and \vec{B} may be
 - (1) 90°
- (2) 60°
- (3) 120°
- $(4) 80^{\circ}$
- **35.** Two vector of magnitude 2 then resultant of these two vector may be?
 - (1) 2
- (2) 8
- (3) 5
- (4) 6
- **36.** Two force 5N and 2N acting on object then net force on object must not be:
 - (1) 2N
- (2) 1N
- (3) 6N
- (4) Both (1) and (2)

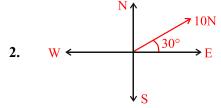


- 37. Vector \vec{A} is 2m long at 60° above the +x-axis and \vec{B} is 2m long at 60° below the +x-axis then resultant will be:
- **38.** If vector sum of two unit vector is a unit vector then:
- **39.** The ratio of maximum and minimum magnitude of resultant of two vectors \vec{a} and \vec{b} is 3:1, then $|\vec{a}|$ in term of |B|.
- **40.** Find angle between force 2P and $\sqrt{2}P$ act so that resultant force is $P\sqrt{10}$.

- 41. Two vector of magnitude 2 and 4 and resultant is $2\sqrt{3}$ find angle between vectors.
- 42. The sum of the magnitude of two force is 18 and magnitude of their resultant is 12. If resultant is at 90° with the force of smaller magnitude, then what is magnitude of force
- **43.** Which of the combination of three force can give zero resultant.
 - (1) (2, 4, 7)
- (2) (3, 1, 5)
- (3) (2, 8, 11)
- (4) (3, 4, 2)

ANSWER KEY

1. (2, 3, 4, 5)



3.
$$\frac{4}{5}mg$$

4.
$$v_x = v \cos \theta$$
 $v_y = v \sin \theta$

5.
$$\vec{A} = \frac{3}{5}\hat{i} + \frac{4}{5}\hat{j}$$

$$\vec{B} = \frac{-3}{5\sqrt{2}}\hat{i} + \frac{4}{5\sqrt{2}}\hat{j} - \frac{1}{\sqrt{2}}\hat{k}$$

$$\vec{C} = \frac{2}{\sqrt{14}}\hat{i} + \frac{3}{\sqrt{14}}\hat{j} - \frac{1}{\sqrt{14}}\hat{k}$$

$$\vec{D} = \frac{1}{\sqrt{6}}\hat{i} + \frac{1}{\sqrt{6}}\hat{j} - \frac{2}{\sqrt{6}}2\hat{k}$$

6. Magnitude: 50N

Direction: N 37° S or 37° South of North

7. Magnitude: 40N

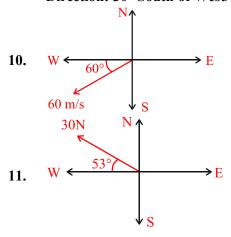
Direction: 53° North of East/37° East of North

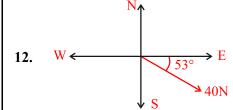
8. Magnitude: 20N

Direction: 60° West of North/30° North of West

9. Magnitude: 10N

Direction: 30° South of West/60° West of South





- **13. (2)**
- 14. **(3)**
- **15. (3)**
- **16. (1)**
- **17. (1)**
- 18. **(1)**
- 19. **(1)**
- 20. **(1)**
- 21. **(3)**
- 22. **(2)**
- 23. **(3)**
- 24. **(1)**
- 25. **(2)**
- **26. (1)**
- 27. **(3)**
- 28. **(3) 29.**
- 0 **30.**
- **(A)** 31.
- 5 N
- 32. **(1)**
- 33. **(3)** 34. **(1)**
- 35.
- **(1) 36. (4)**
- 37.
- 38. Angle between them must be 120°
- $|\vec{Q}| = 2|\vec{b}|$ 39.
- 45° **40.**
- 120° 41.
- 42. 5 N, 13 N
- 43. **(4)**

