

# YAKEEN NEET 2.0

**2026**

**Motion in a plane**

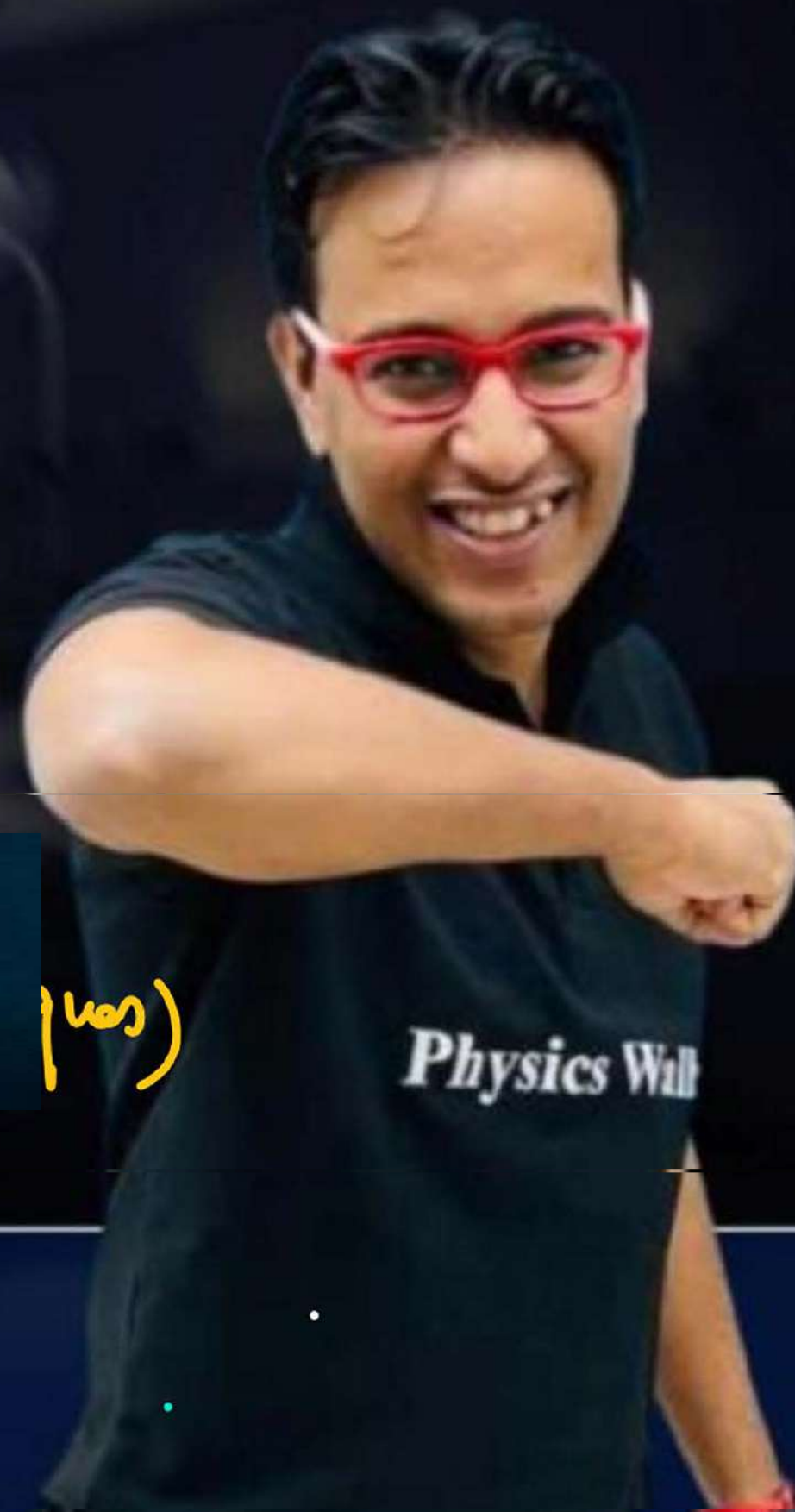
**Microlecture**

(ues)

**PHYSICS**

**Lecture -04**

**By – Saleem Ahmed Sir**



Diff & Integration based ques.



Q  $\vec{r} = 3t^2\hat{i} - t^3\hat{j} + 2t^2\hat{k}$

position vector

① find  $\vec{v}$

Sol<sup>n</sup> ①  $\vec{v} = \frac{d\vec{r}}{dt} = 6t\hat{i} - 3t^2\hat{j} + 4t\hat{k}$

② Find  $\vec{a}$

②  $\vec{a} = \frac{d\vec{v}}{dt} = 6\hat{i} - 6t\hat{j} + 4\hat{k}$

③  $t=2$ ,  $\vec{v}$ ,  $\vec{a}$

③  $t=2$ ,  $\vec{v} = 12\hat{i} - 12\hat{j} + 8\hat{k}$   
 $\vec{a} = 6\hat{i} - 12\hat{j} + 4\hat{k}$

④ Find  $\langle \vec{v} \rangle$  &  $\langle \vec{a} \rangle$   
 from  $t=1 \rightarrow t=2$

④  $\langle \vec{v} \rangle = \frac{\vec{r}_f - \vec{r}_i}{t_2 - t_1} = \frac{9\hat{i} - 7\hat{j} + 6\hat{k}}{2-1}$

$t=1$ ,  $\vec{r}_i = (3, -1, 2)$

$t=2$ ,  $\vec{r}_f = (12, -8, 8)$

$\langle \vec{a} \rangle = \frac{\vec{v}_2 - \vec{v}_1}{t_2 - t_1} = \frac{(12, -12, 8) - (6, -3, 4)}{2-1} = \frac{6\hat{i} - 9\hat{j} + 4\hat{k}}{1}$

$$Q \quad x = 6t \longrightarrow \frac{dx}{dt} = v_x = 6 \longrightarrow a_x = 0$$

$$y = 3t - 5t^2 \longrightarrow v_y = 3 - 10t \longrightarrow a_y = -10$$

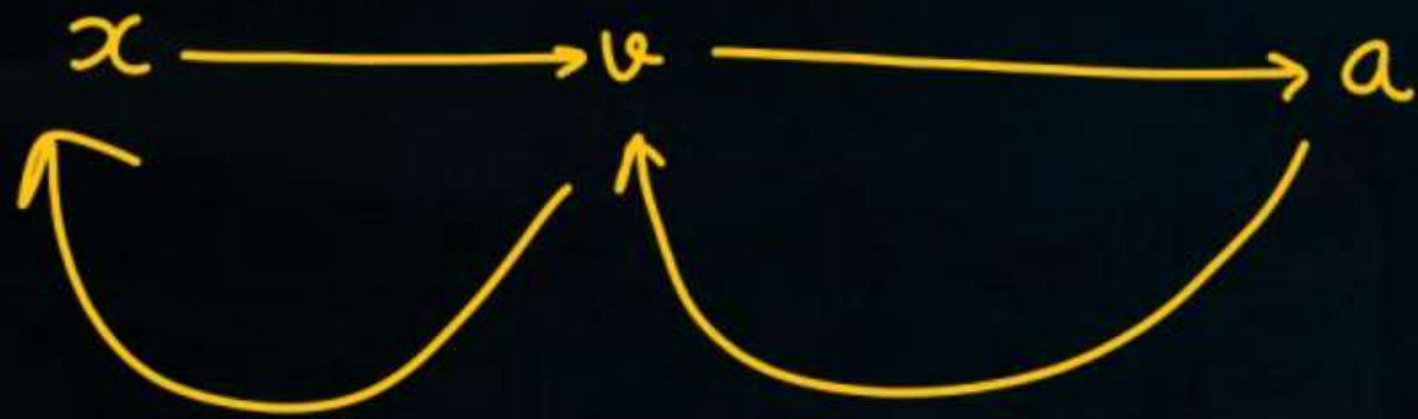
$$\vec{r} = 6t\hat{i} + (3t - 5t^2)\hat{j}$$

$$\vec{v} = 6\hat{i} + (3 - 10t)\hat{j}$$

$$\vec{a} = -10\hat{j}$$

$$\vec{v} = 6\hat{i} + (3 - 10t)\hat{j}$$

$$\vec{a} = 0 + -10\hat{j}$$





Q A particle start motion from rest at  $t=0$   
from origin ( $x=0$ ), on the  $x$ -Axis

$$v = 3t^2$$

find location of particle at  $t=3$  sec.

Sol

(1D)

$$v = 3t^2$$

$$\frac{dx}{dt} = 3t^2$$

$$dx = 3t^2 dt$$

$$\int_0^x dx = \int_0^3 3t^2 dt$$

$$x \Big|_0^x = 3 \frac{t^3}{3} \Big|_0^3$$

$$x - 0 = 3^3 = 27$$

Definite

Indefinite

$$\int dx = \int 3t^2 dt$$

$$x = t^3 + c$$

$$\text{At } t=0, x=0$$

$$0 = 0 + c$$

$$c = 0$$

$$x = t^3$$

$$\text{At } t=3, x = 3^3 = 27$$

from  $t=0$   
^

Q A particle start motion from  $x=-10$  with initial velocity  $5\text{m/s}$  from origin s.t.

$$V = 3t^2 + 5$$

find location of particle at  $t=3\text{ sec.}$

Sol<sup>n</sup>  $\frac{dx}{dt} = 3t^2 + 5$

$$\int dx = \int (3t^2 + 5) dt$$

$$x = t^3 + 5t + C$$

At  $t=0, x=-10$

$$-10 = 0 + 0 + C$$

$$\boxed{C = -10}$$

$$x = t^3 + 5t - 10$$

At  $t=3$

$$x = 27 + 15 - 10$$

$$x = 32$$

$$\frac{dx}{dt} = 3t^2 + 5$$

$$\int_{-10}^x dx = \int_0^3 (3t^2 + 5) dt$$

$$x \Big|_{-10}^x = (t^3 + 5t) \Big|_0^3$$

$$x - (-10) = 3^3 + 5 \times 3 - 0$$

$$x + 10 = 27 + 15$$

$$\boxed{x = 32}$$



Q A particle start motion from origin from rest at  $t=0$ , s.t.  $a_x = 6t$ . find

①  $v = f(t)$

②  $x = f(t)$

③  $v$  &  $x$  at  $t=2\text{sec}$ .

Sol<sup>n</sup>

$$a = 6t$$

$$\frac{dv}{dt} = 6t$$

$$\int_0^v dv = \int_0^t 6t dt$$

$$v - 0 = 6 \frac{t^2}{2} \Big|_0^t = 3t^2$$

$$\boxed{v = 3t^2}$$

$$v = 3t^2$$

$$\frac{dx}{dt} = 3t^2$$

$$\int_0^x dx = \int_0^t 3t^2 dt$$

$$x - 0 = t^3 - 0$$

$$\boxed{x = t^3}$$

At  $t=2$ ,  $v=12$   
 $a=8$



m-2

$$\Delta v = \int a dt$$

$$v_f - v_i = \int_0^t 6t dt$$

$$v - 0 = 3t^2$$

$$v = 3t^2$$

$$x_f - x_i = \int 3t^2 dt$$

$$x_f - 0 = t^3$$

$$\frac{dv}{dt} = a$$

$$\int_{v_1}^{v_2} dv = \int_{t_1}^{t_2} a dt$$

$$v_2 - v_1 = \int_{t_1}^{t_2} a dt$$

Q Particle start motion at  $t=0$  from  $x=+10$  s.t.

$$V = 4t^3 + 3t^2 + 2t$$

Find location of particle at  $t=1$  sec.

Sol<sup>n</sup>

$$\frac{dx}{dt} = 4t^3 + 3t^2 + 2t$$

$$\int_{10}^x dx = \int_0^1 (4t^3 + 3t^2 + 2t) dt$$

$$x - 10 = t^4 + t^3 + t^2 \Big|_0^1$$

$$x - 10 = 3 - 0$$

$$\boxed{x = 13}$$

or

$$x_f - x_i = \int_0^1 v dt$$

$$x_f - 10 = t^4 + t^3 + t^2 \Big|_0^1$$

$$x_f - 10 = 3 - 0$$

$$\underline{x_f = 13}$$



## Question



A particle start motion at  $t=0$  having initial velocity  $v=+10$  and  
such that  $a=24t^2$  initial location at  $x=20$

find ①  $v, x$  (location) at  $t=2\text{sec}$

②  $v = f(t)$

$x = f(t)$

Ans : ( $v = 74, x = 72$ )

## Question



A particle start motion at  $t=0$  having initial velocity  $v=+10$  and initial location at  $x=20$  such that  $a=24t^2$

find  $v, x$  (location), at  $t=2\text{sec}$

Sol<sup>n</sup>

$$a = 24t^2$$

$$\frac{dv}{dt} = 24t^2$$

$$\int_{10}^v dv = \int_0^t 24t^2 dt$$

$$v - 10 = 24 \left. \frac{t^3}{3} \right|_0^t$$

$$\boxed{v = 8t^3 + 10}$$

$$v = 8t^3 + 10$$

$$\frac{dx}{dt} = 8t^3 + 10$$

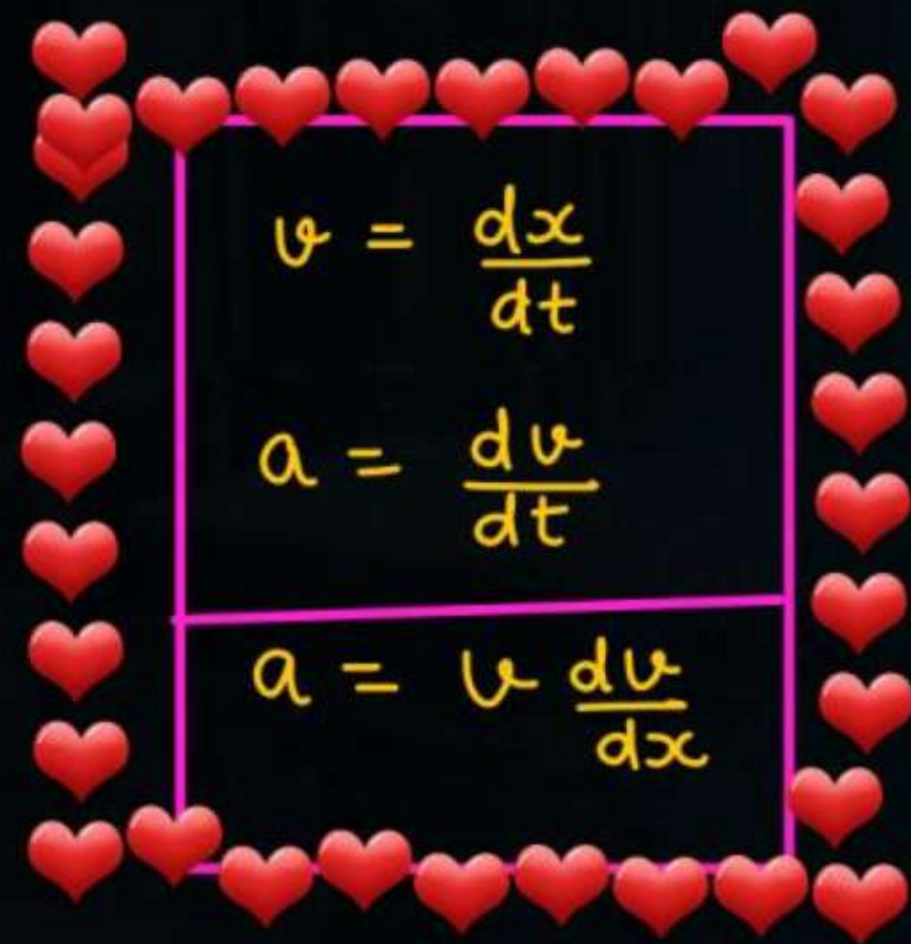
$$\int_{20}^x dx = \int_0^t (8t^3 + 10) dt$$

$$x - 20 = \left( 8 \frac{t^4}{4} + 10t \right) \Big|_0^t$$

$$\boxed{x = 20 + 2t^4 + 10t}$$

Ans : ( $v = 74, x = 72$ )




$$v = \frac{dx}{dt}$$
$$a = \frac{dv}{dt}$$
$$a = v \frac{dv}{dx}$$

$$a = v \frac{dv}{dx}$$

Q  $v = x^2 + 8x$

find acc. at  $x=2$

Sol  $\frac{dv}{dx} = 2x + 8$

$$a = v \frac{dv}{dx} = (x^2 + 8x)(2x + 8)$$

At  $x=2$ ,  $a = (4+16)(4+8)$   
 $a = \checkmark$

$$\left\{ \begin{array}{l} v = \frac{dx}{dt} \\ a = \frac{dv}{dt} \\ a = v \frac{dv}{dx} \end{array} \right\}$$



A particle is moving on x-axis such that its acc is given by  $a = \frac{3}{v}$ . At  $t = 0$  its velocity is 1 m/s. Find velocity at  $t = 40$  sec.

$v, t$

Sol<sup>n</sup>

$$a = \frac{3}{v}$$

$$\frac{dv}{dt} = \frac{3}{v}$$

$$\int_1^v v dv = \int_0^{40} 3 dt$$

$$\frac{v^2}{2} \Big|_1^v = 3t \Big|_0^{40}$$

$$\frac{v^2}{2} - \frac{1}{2} = 3 \times (40 - 0)$$

$$\frac{v^2 - 1}{2} = 120$$

$$v = \sqrt{241}$$

Ans :  $(v = \sqrt{241})$

SKC

ye dekhien ki  
Diya kya hai  
or pucha kya hai



## Question



Acceleration of a particle moving on x-axis having initial speed  $v_0$  with distance from origin is given by  $a = \sqrt{x}$ . Distance covered by particle where its speed become thrice that of initial speed.

$$a = \sqrt{x}$$

$$v \frac{dv}{dx} = \sqrt{x}$$
$$\int_{v_0}^{3v_0} v dv = \int_0^x x^{\frac{1}{2}} dx$$

$$\frac{v^2}{2} \Big|_{v_0}^{3v_0} = \frac{x^{3/2}}{3/2}$$

$$\frac{1}{2} \left[ (3v_0)^2 - v_0^2 \right] = \frac{2}{3} x^{3/2}$$

$$4v_0^2 = \frac{2}{3} x^{3/2}$$

$$x = (6v_0^2)^{2/3}$$

Ans:

$$x = \left( \frac{2}{3} v_0^2 \right)^{\frac{4}{3}}$$

## Question



$v, x$

A particle is projected with velocity  $v_0 = 4 \text{ m/s}$  along +x-axis from origin and acc. is  $a = -3x^2$ . Find where particle will come to at rest

$$a = -3x^2$$

$$v \frac{dv}{dx} = -3x^2$$

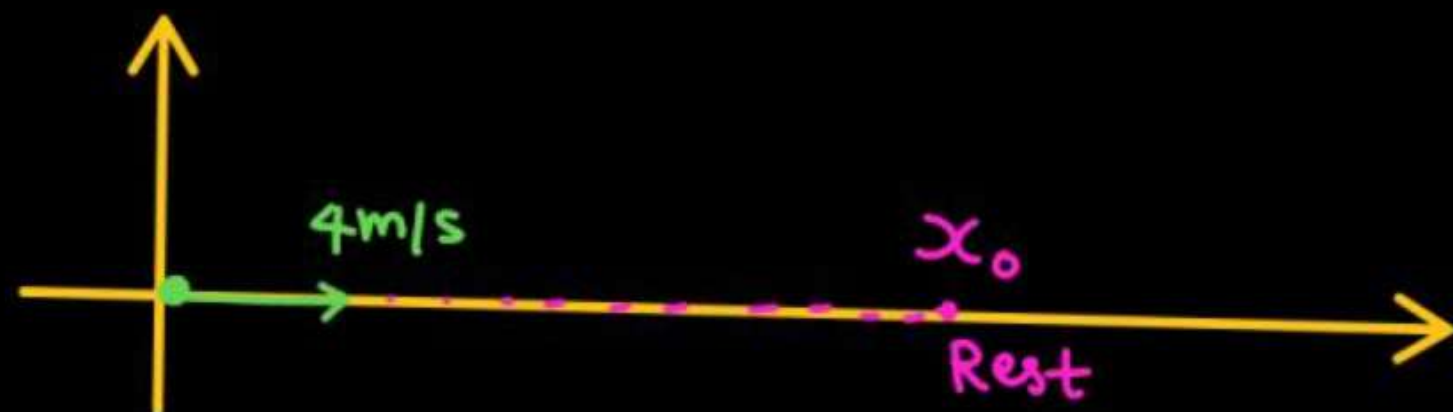
$$\int_4^0 v dv = \int_0^{x_0} -3x^2 dx$$

$$\left. \frac{v^2}{2} \right|_4^0 = -3 \cdot \left. \frac{x^3}{3} \right|_0^{x_0}$$

$$0 - \frac{4^2}{2} = -x_0^3$$

$$8 = x_0^3$$

$$\boxed{x_0 = 2}$$



$$a = -3x^2$$

When rest  $x = 2$

$$a = -3 \times 2^2 = -12$$

Ans :  $x_f = 2, a = -12$



## Question



The retardation of a car when its engine is shut off depends on its velocity as  $a = -\alpha v$  where  $\alpha$  is positive constant. Find the total distance travelled by the car if its initial velocity is 20 m/s and  $\alpha = 0.5/\text{s}$ .



Sol<sup>n</sup>

$$a = -\alpha v$$

$$v \frac{dv}{dx} = -\alpha v$$
$$\int_{20}^0 dv = \int_0^{x_0} -\alpha dx$$

$$0 - 20 = -\alpha x_0$$

$$20 = \frac{1}{2} x_0$$

$$x_0 = 40$$

Ans : (d = 40 m)



find

## Question



Acceleration of particle moving rectilinearly is  $a = 4 - 2x$  (where  $x$  is position in metre and  $a$  in  $\text{m/s}^2$ ). It is at rest at  $x = 0$ . At what position  $x$  (in metre) will the particle again come to instantaneous rest?

$u, x$

$$a = 4 - 2x$$

$$u \frac{du}{dx} = 4 - 2x$$

$$\int_0^0 u \, du = \int_0^{x_0} (4 - 2x) \, dx$$

$$0 = (4x - x^2) \Big|_0^{x_0}$$

$$(4x_0 - x_0^2) - 0 = 0$$

$$4x_0 - x_0^2 = 0$$

$$x_0(4 - x_0) = 0$$

$$\begin{aligned} x_0 &= 0 \\ x_0 &= 4 \end{aligned}$$

Ans :  $(x = 0, 4)$

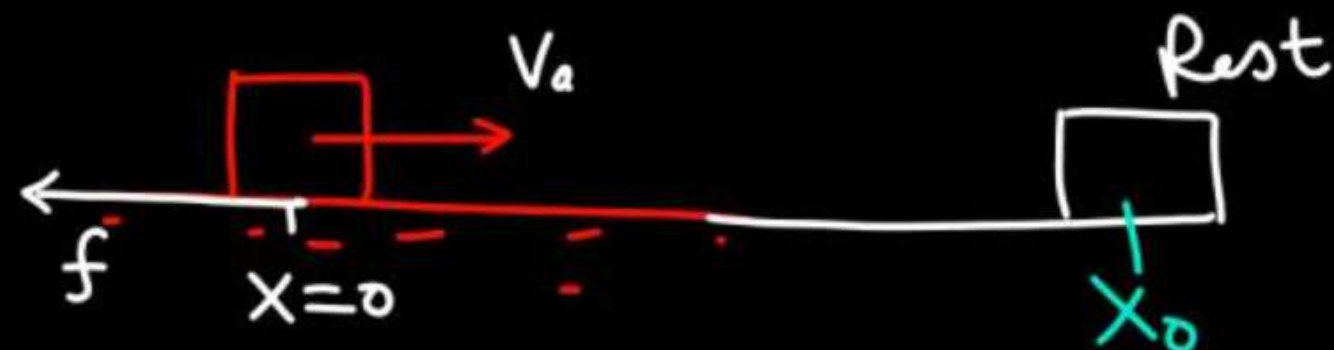


## Question

Copy X



A block of mass  $m$  is fired horizontally along a level surface that is lubricated with oil. The oil provides a viscous resistance <sup>force</sup> that varies as the  $3/2$  power of the speed. If the initial speed of the block is  $v_0$  at  $x = 0$ , find the maximum distance reached by the block. Assume no resistance to motion other than that provided by the oil.



$$2\sqrt{v_0} = \frac{x_0}{m}$$

$$x_0 = 2m\sqrt{v_0}$$

$$F = -v^{3/2}$$

$$ma = -v^{3/2}$$

$$a = -\frac{v^{3/2}}{m}$$

$$v \frac{dv}{dx} = -\frac{v^{3/2}}{m}$$

$$\int_{v_0}^0 v^{-1/2} dv = -\frac{1}{m} \int_0^{x_0} dx$$

$$\frac{v_0^{1/2}}{1/2} = \frac{1}{m} (x_0 - 0)$$

Ans : (\*)



## Question



The deceleration experienced by a moving motor boat, after its engine is cut-off is given by  $dv/dt = -kv^3$ , where  $k$  is constant. If  $v_0$  is the magnitude of the velocity at cut-off, the magnitude of the velocity at a time  $t$  after the cut-off is

- (1)  $v_0/2$                       (2)  $v$   
(3)  $v_0 e^{-kt}$                 (4)  $\frac{v_0}{\sqrt{2v_0^2 kt + 1}}$

$$\frac{dv}{dt} = -kv^3$$
$$\int_{v_0}^v \frac{dv}{v^3} = \int_0^t -k dt$$

Ans : (4)

An object, moving with a speed of 6.25 m/s, is decelerated at a rate given by

$$\frac{dv}{dt} = -2.5\sqrt{v}$$

where  $v$  is the instantaneous speed. The time taken by the object, to come to rest, would be :-

6.25 m/s की चाल से गतिशील एक वस्तु के मन्दन की दर इससे दी जाती है।

$$\frac{dv}{dt} = -2.5\sqrt{v} \quad \int_{6.25}^0 \frac{dv}{\sqrt{v}} = - \int_0^t 2.5 dt$$

जहाँ  $v$  तात्क्षणिक चाल है। वस्तु को विराम अवस्था में आने में लगा समय है :-

[AIEEE-2011]

(1) 4 s

(2) 8 s

(3) 1 s

(4) 2 s

Ans. (4)

A particle is projected with velocity  $v_0$  along x-axis. The deceleration on the particle is proportional to the square of the distance from the origin i.e.,  $a = -\alpha x^2$ . The distance at which the particle stops is:—  
 एक कण x अक्ष के अनुदिश  $v_0$  वेग से प्रक्षेपित किया जाता है। कण का मंदन, मूल बिन्दु से इसकी दूरी के वर्ग के समानुपाती है अर्थात्  $a = -\alpha x^2$  है। किस दूरी पर कण रूक जायेगा ?

- (A)  $\sqrt{\frac{3v_0}{2\alpha}}$       (B)  $\left(\frac{3v_0}{2\alpha}\right)^{\frac{1}{3}}$       (C)  $\sqrt{\frac{3v_0^2}{2\alpha}}$       (D)  $\left(\frac{3v_0^2}{2\alpha}\right)^{\frac{1}{3}}$

Ans. (D)

Sol<sup>n</sup>

$$u \frac{du}{dx} = -\alpha x^2$$

$$\int_{v_0}^0 u \, du = -\int_0^{x_0} \alpha x^2 \, dx$$



The acceleration vector along x-axis of a particle having initial speed  $v_0$  changes with distance as  $a = \sqrt{x}$ . The distance covered by the particle, when its speed becomes twice that of initial speed is:-

प्रारम्भिक चाल  $v_0$  वाले एक कण का x- अक्ष के अनुदिश त्वरण सदिश, दूरी के साथ  $a = \sqrt{x}$  के अनुसार परिवर्तित होता है। जब कण की चाल प्रारम्भिक चाल की दुगुनी हो जाये उस समय कण द्वारा तय की गई दूरी होगी:-

- (A)  $\left(\frac{9}{4}v_0\right)^{\frac{4}{3}}$       (B)  $\left(\frac{3}{2}v_0\right)^{\frac{4}{3}}$       (C)  $\left(\frac{2}{3}v_0\right)^{\frac{4}{3}}$       (D)  $2v_0$

**Ans. (B)**

$$v \frac{dv}{dx} = x^{\frac{1}{2}}$$

(copy)

Q

A particle has an initial velocity of  $3\hat{i} + 4\hat{j}$  and an acceleration of  $0.4\hat{i} + 0.3\hat{j}$ . Its speed after 10s is:-  
[AIEEE-2009]

(1) 7 units

(2) 8.5 units

(3) 10 units

(4)  $7\sqrt{2}$  units

$$\vec{v} = \vec{u} + \vec{a}t$$

$$\vec{v} = (3\hat{i} + 4\hat{j}) + (0.4\hat{i} + 0.3\hat{j}) \times 10$$

magnitude

## Question



A particle is moving along the  $x$ -axis whose instantaneous speed is given by  $v^2 = 108 - 9x^2$ . The acceleration of the particle is

(1)  $-9x \text{ m s}^{-2}$

(2)  $-18x \text{ m s}^{-2}$

(3)  $\frac{-9x}{2} \text{ m s}^{-2}$

(4) None of these

$v^2 = 108 - 9x^2$   
Diff wrt  $x$

$$2v \frac{dv}{dx} = 0 - 9 \times 2x$$

$$2a = -18x$$

$$a = -9x$$

$m^2$

$$2v \frac{dv}{dt} = 0 - 9 \times 2x \cdot \frac{dx}{dt}$$

$$2v/a = -18x$$

$$a = -9x$$

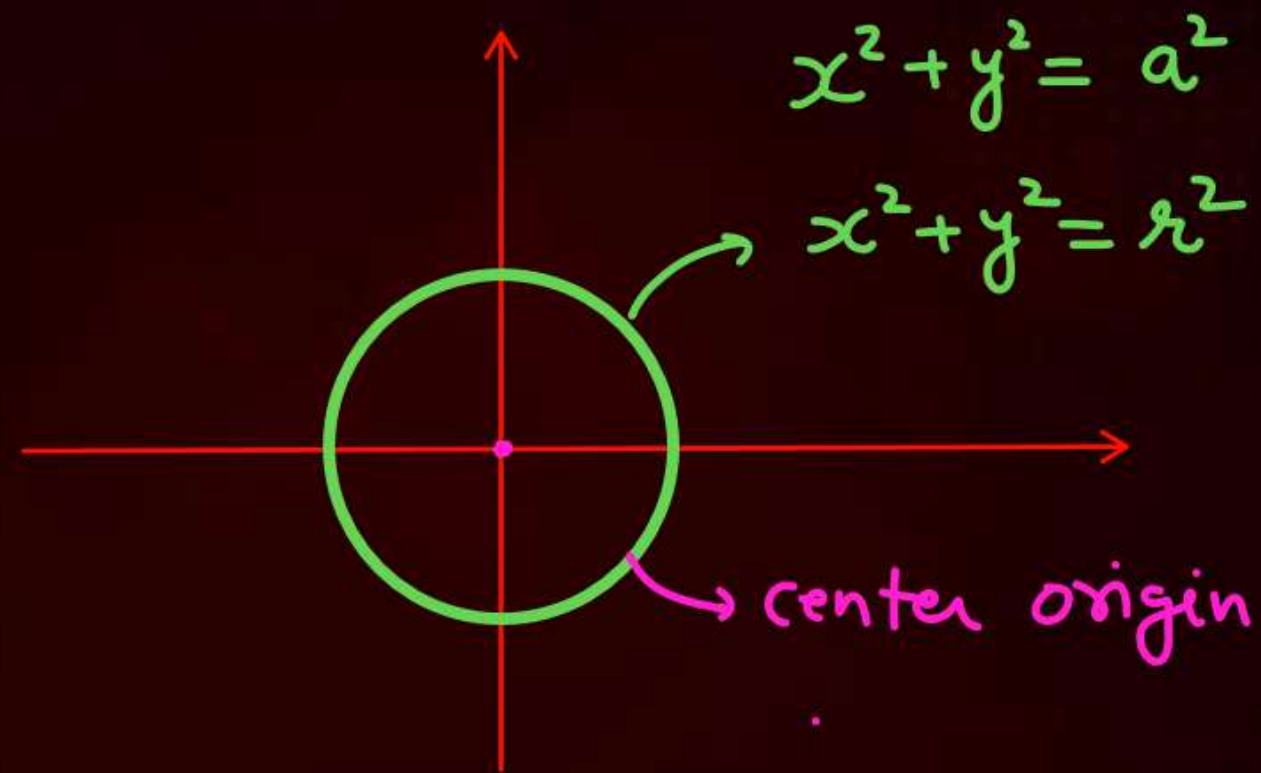
Ans : (1)



① St. line  $\longrightarrow y = mx + c$

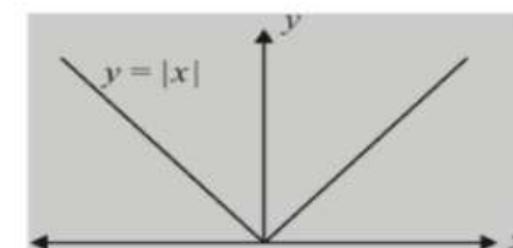
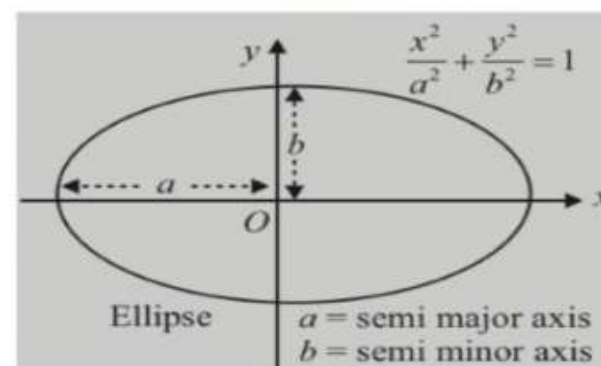
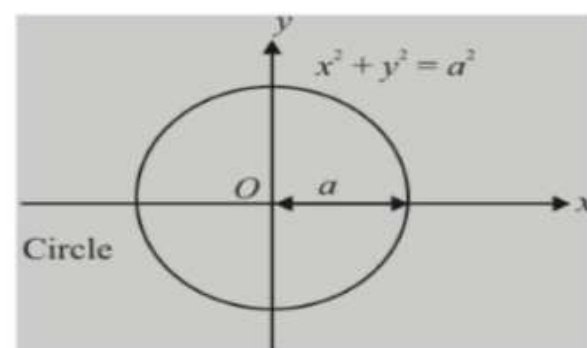
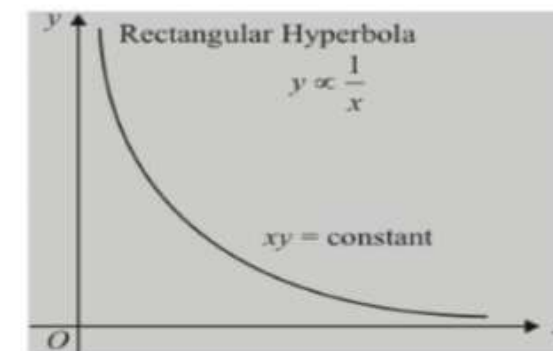
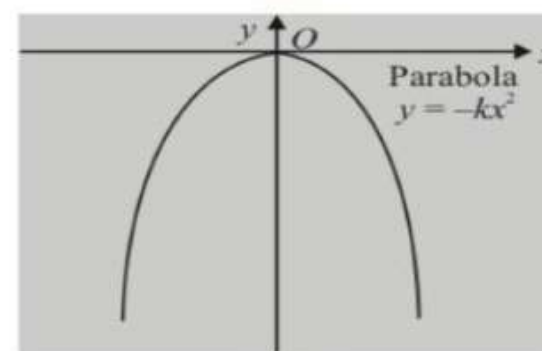
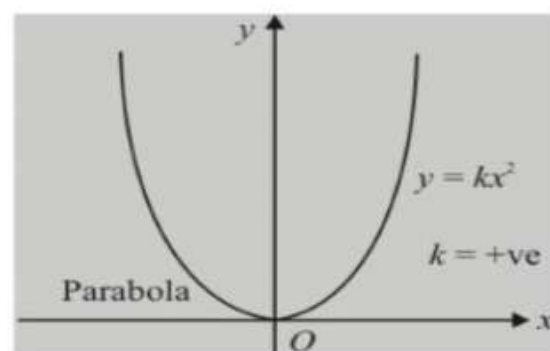
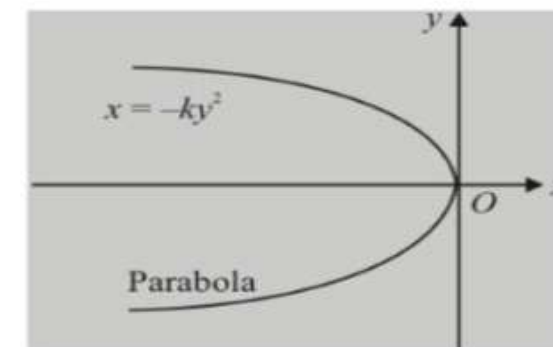
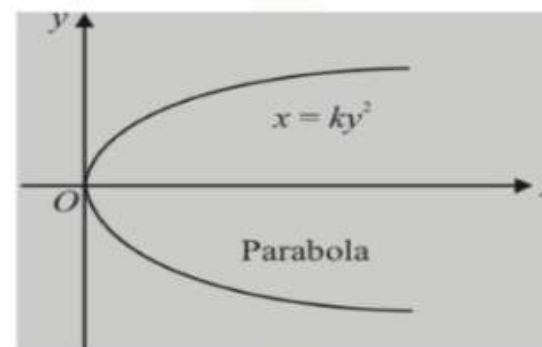
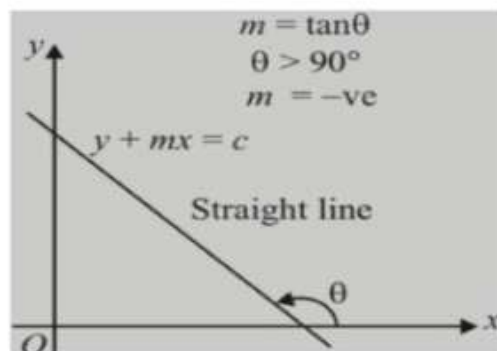
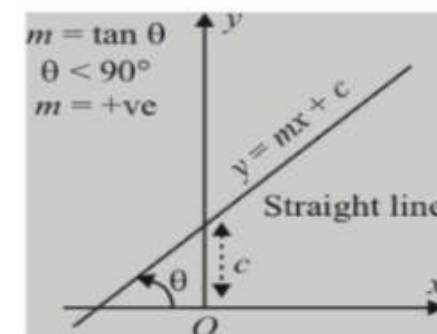
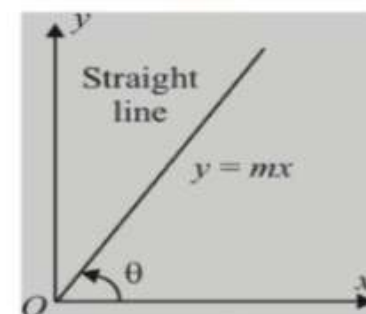
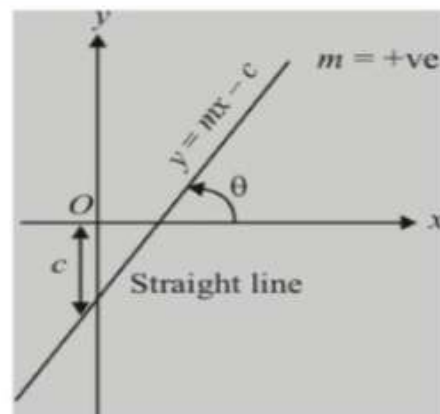
② parabola  $y^2 = x$   
 $y = x^2$

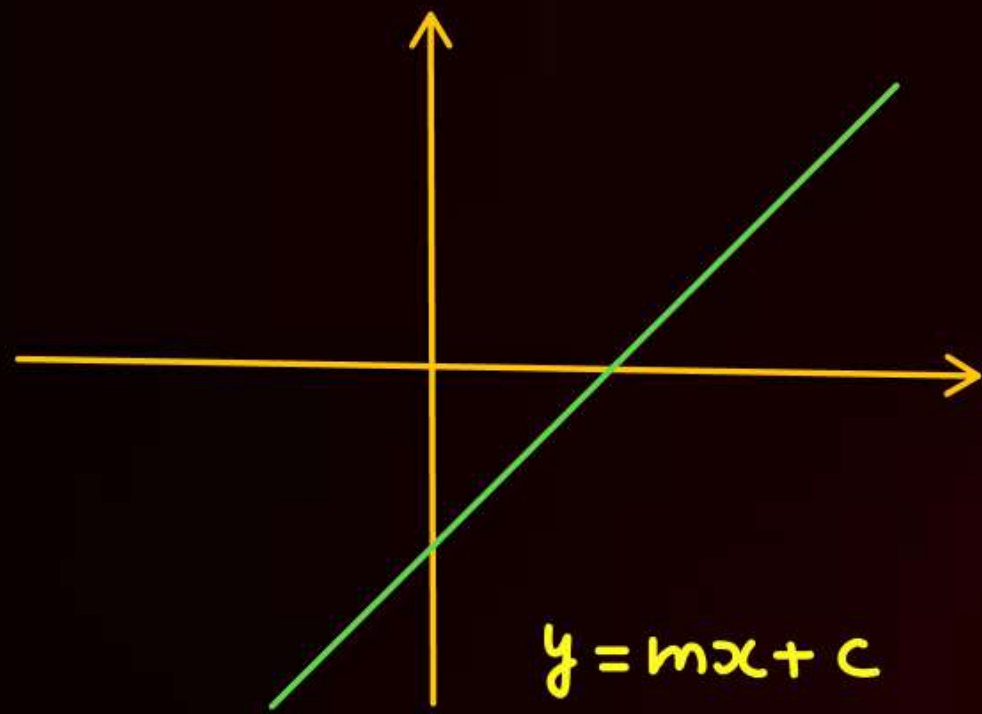
③ Circle  
 $x^2 + y^2 = r^2$



$$(x - x_1)^2 + (y - y_1)^2 = r^2$$

Center  $(x_1, y_1)$

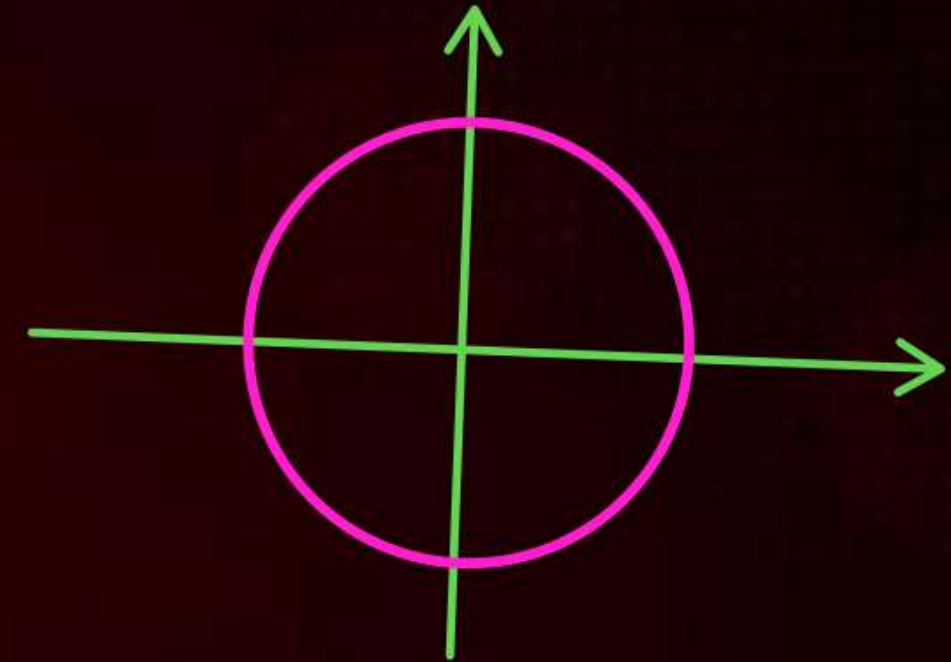




parabola

$$y = x^2$$

$$y^2 = x$$

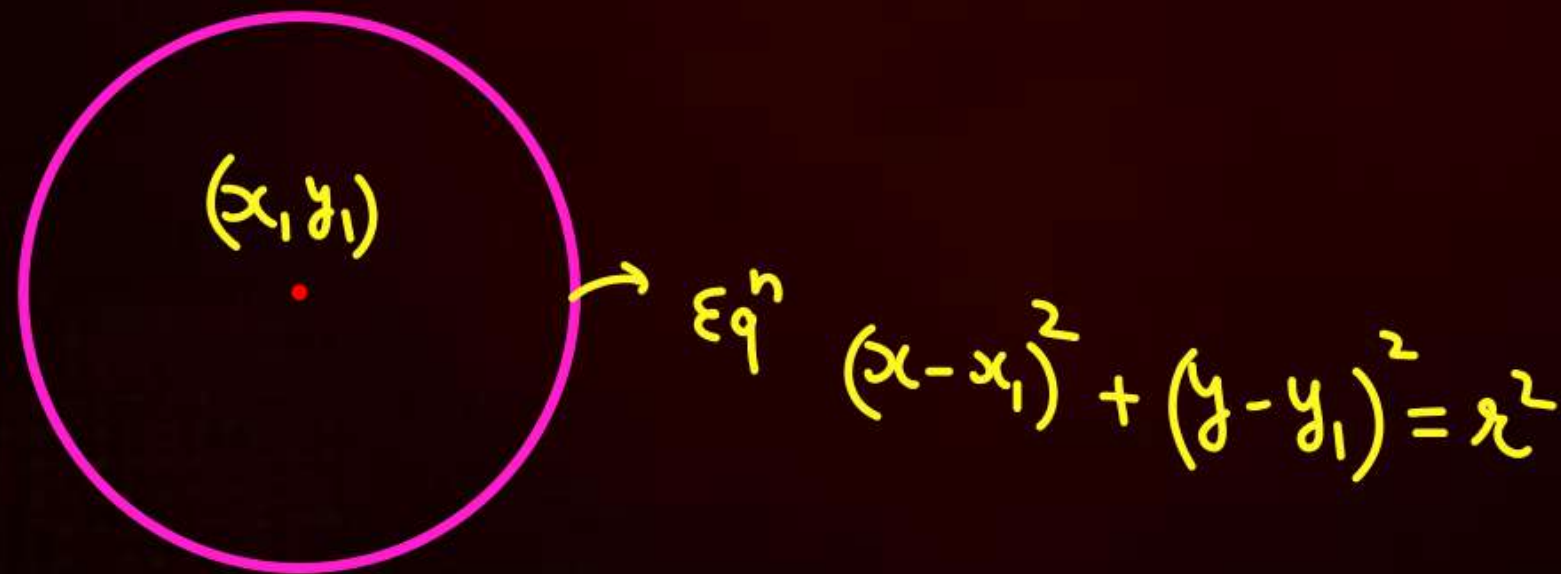


$$x^2 + y^2 = r^2$$

or

$$x^2 + y^2 = a^2$$

Equation of  
circle  
of center  $(0,0)$   
& radius  $r$

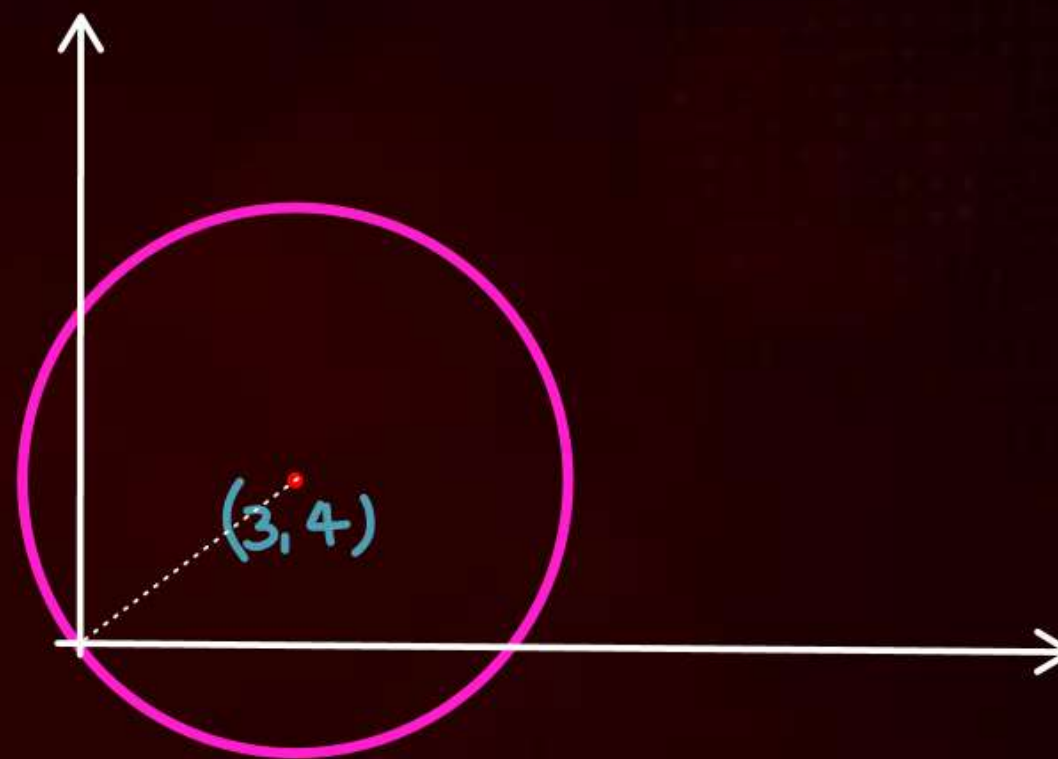


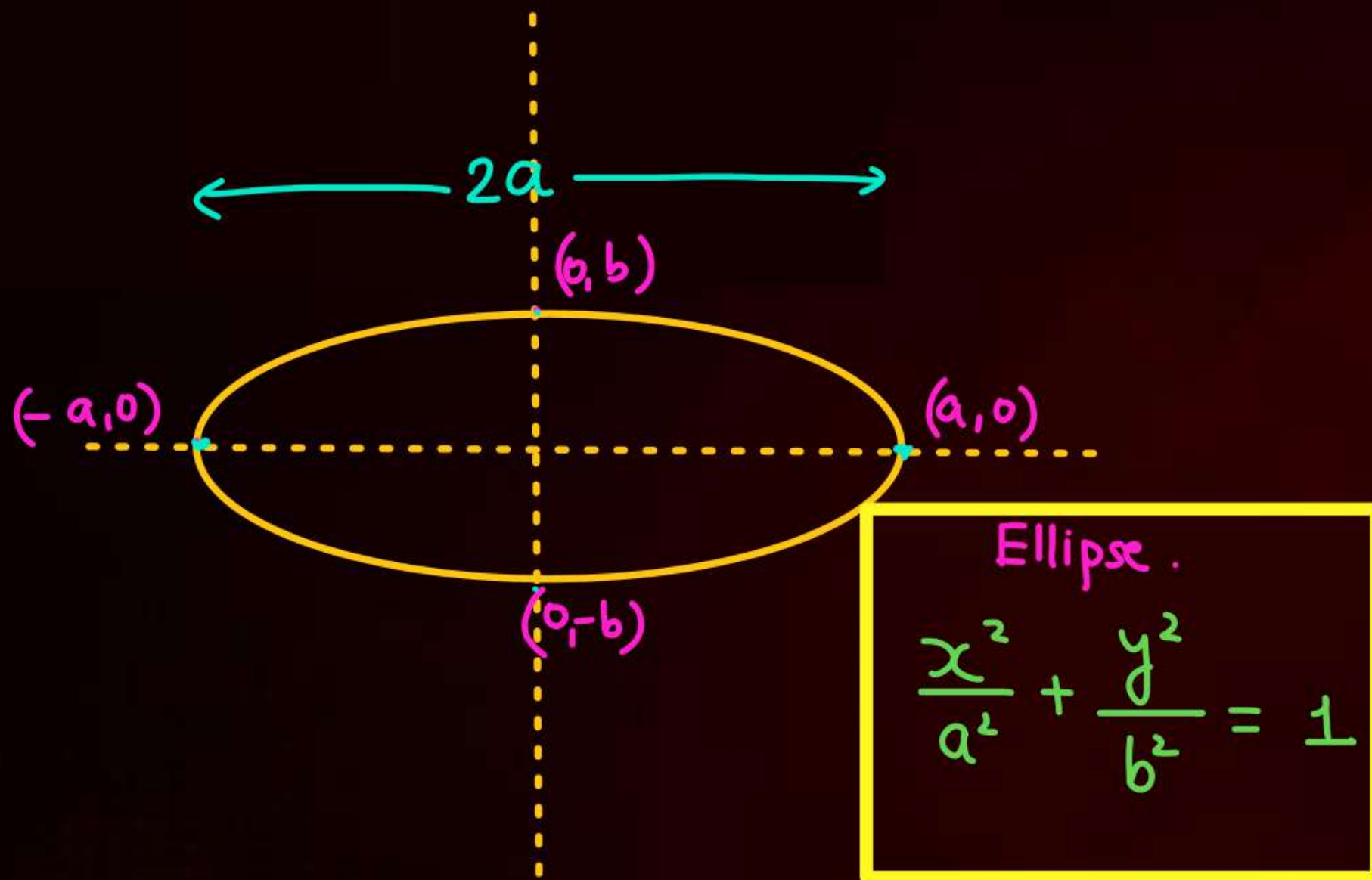


Q  $(x-3)^2 + (y-4)^2 = 25$

Center  $\rightarrow (3, 4)$

radius  $\rightarrow \sqrt{25} = 5$





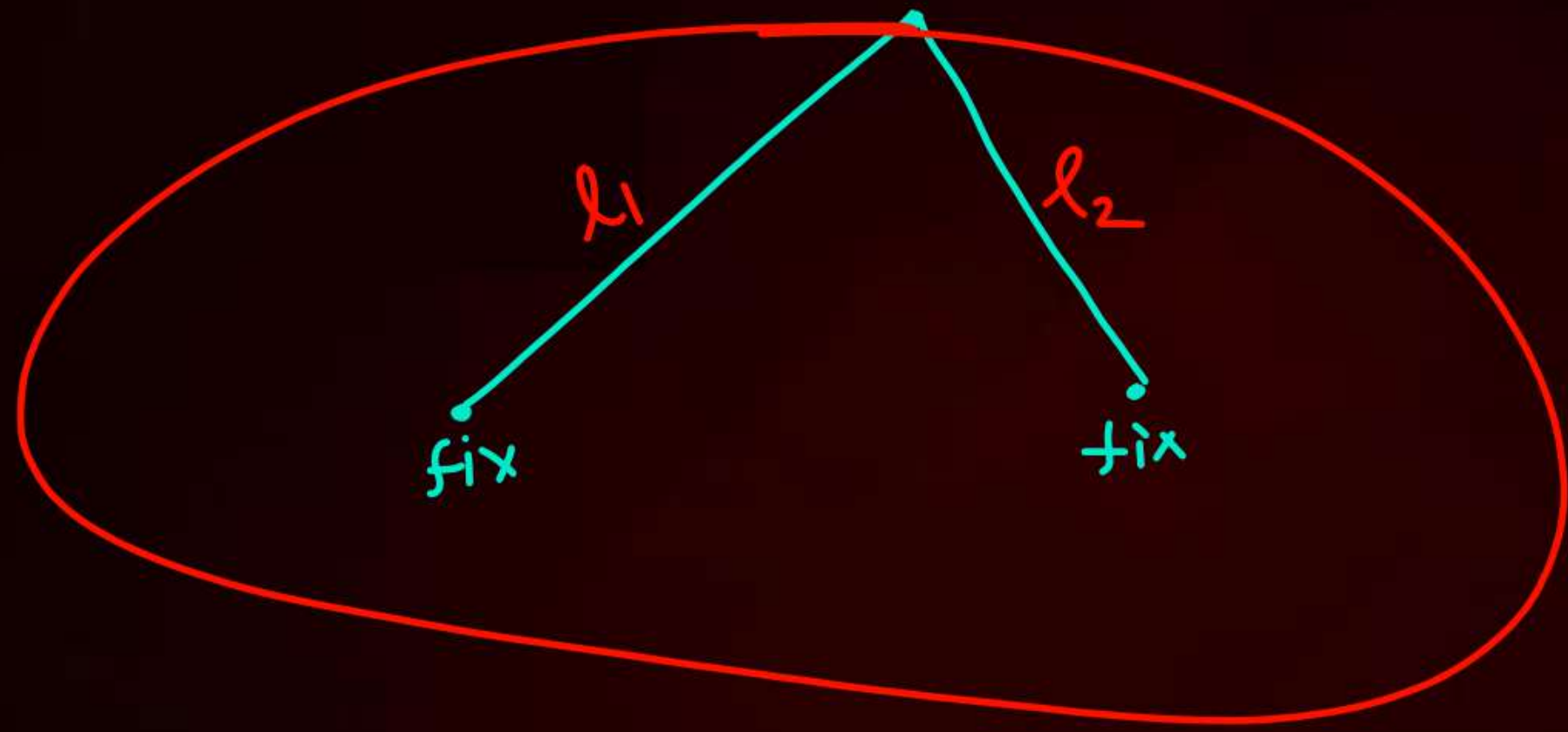
If  $a=b \Rightarrow$  circle

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$$

put,  $y=0$

$$x^2 = a^2$$

$$x = \pm a$$





Find eq<sup>n</sup> of trajectory

①  $x = 2t$   
 $y = 4t$

Sol<sup>n</sup>  $t = \frac{x}{2}$

$$y = 4 \cdot \frac{x}{2}$$

$$\boxed{y = 2x}$$

St. line, (1D)

②  $x = 2t$   
 $y = 4t^2$

Sol<sup>n</sup>  $t = \frac{x}{2}$

$$y = 4 \left( \frac{x}{2} \right)^2$$

$$y = 4 \frac{x^2}{4} = x^2$$

$$y = x^2$$

(parabola), (2D)

③  $x = A \sin \omega t$   
 $y = A \cos \omega t$

Sol<sup>n</sup>

$$\sin^2 \omega t + \cos^2 \omega t = 1$$

$$\left( \frac{x}{A} \right)^2 + \left( \frac{y}{A} \right)^2 = 1$$

$$x^2 + y^2 = A^2$$

(circular), 2D



@SALEEMSIR\_PW

**THANK**  
**YOU**