

YAKEEN NEET 2.0

2026

Vectors

PHYSICS

Lecture – 06

By – Saleem Ahmed Sir





Today's Goal

- magnitude of vector
- Unit vector & application

(copy)

Q $|\vec{A}| = |\vec{B}| = x$

angle between \vec{A} & \vec{B} is θ

① Find $|\vec{A} + \vec{B}|$

\Rightarrow solⁿ $\vec{A} + \vec{B} = \vec{C}$

$$|\vec{A} + \vec{B}| = |\vec{C}| = C$$

$$C = \sqrt{A^2 + B^2 + 2AB \cos \theta}$$

$$C = \sqrt{x^2 + x^2 + 2x \cdot x \cos \theta}$$

$$= \sqrt{2x^2(1 + \cos \theta)} = \sqrt{2x^2 \left(1 + 2\cos^2 \frac{\theta}{2} - 1\right)}$$

$$C = 2x \cos \frac{\theta}{2}$$

② $|\vec{A} - \vec{B}| = D$

$$D = \sqrt{A^2 + B^2 - 2AB \cos \theta}$$

$$C = \sqrt{x^2 + x^2 - 2x \cdot x \cos \theta} = \sqrt{2x^2(1 - \cos \theta)}$$

$$C = \sqrt{2x^2 \left[1 - \left(1 - 2\sin^2 \frac{\theta}{2}\right)\right]} = 2x \sin \frac{\theta}{2}$$

$$|\vec{A}| = |\vec{B}| = x \text{ (Equal magnitude)}$$

Angle b/w \vec{A} & \vec{B} is θ

$$|\vec{A} + \vec{B}| = 2x \cos \frac{\theta}{2}$$

$$|\vec{A} - \vec{B}| = 2x \sin \frac{\theta}{2}$$





magnitude of a vector

$$\textcircled{1} \quad \vec{A} = 2\hat{i} + 3\hat{j} + 4\hat{k}$$

$$|\vec{A}| = A = \sqrt{2^2 + 3^2 + 4^2} = \sqrt{29}$$

$$\textcircled{2} \quad \vec{A} = 3\hat{i} + 4\hat{j} + 5\hat{k}$$

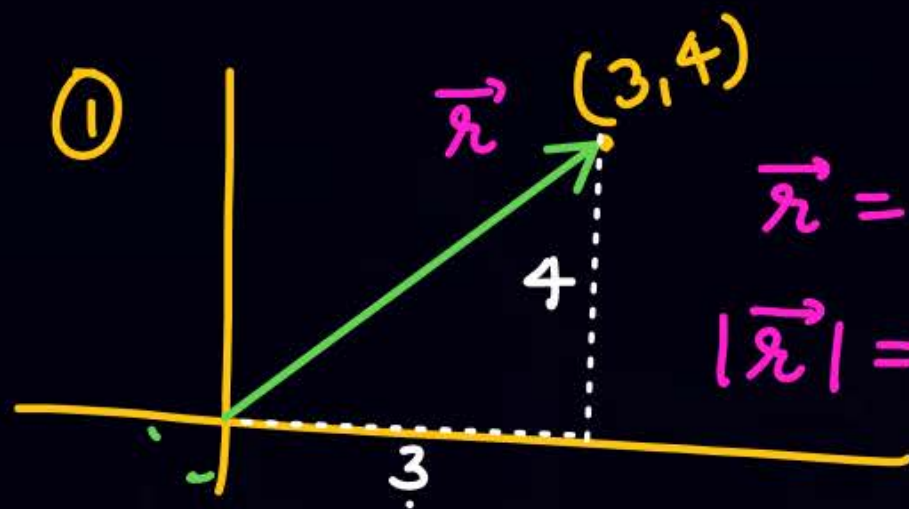
$$|\vec{A}| = \sqrt{3^2 + 4^2 + 5^2} = 5\sqrt{2}$$

$$\textcircled{3} \quad \vec{A} = 3\hat{i} - 4\hat{j} - 5\hat{k}$$

$$|\vec{A}| = \sqrt{3^2 - 4^2 - 5^2}$$

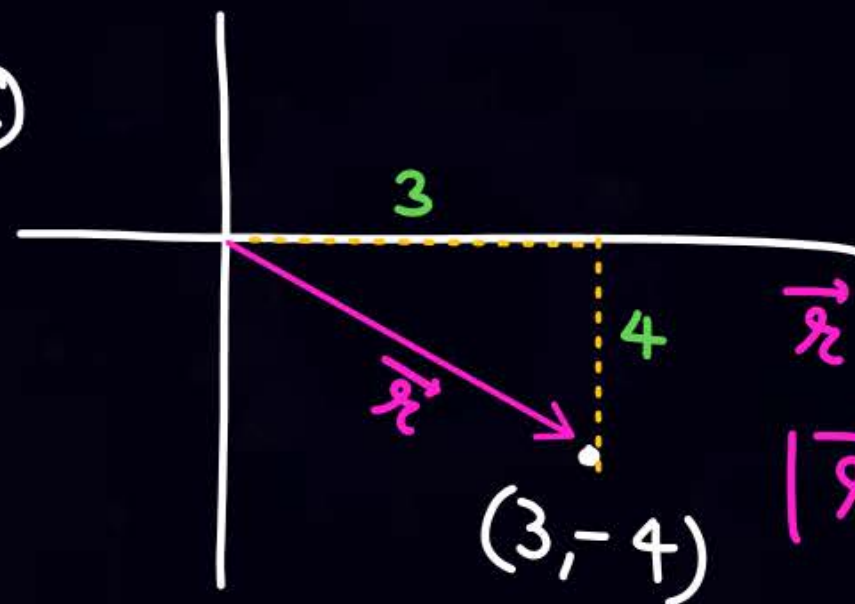
$$|\vec{A}| = \sqrt{3^2 + 4^2 + 5^2}$$

X



$$\vec{r} = 3\hat{i} + 4\hat{j}$$
$$|\vec{r}| = \sqrt{3^2 + 4^2} = 5$$

②



$$\vec{r} = 3\hat{i} - 4\hat{j}$$
$$|\vec{r}| = \sqrt{3^2 + 4^2}$$



$$\textcircled{4} \quad \vec{A} = 3\hat{i} - 4\hat{j} + 5\hat{k}$$

$$A = \sqrt{3^2 + 4^2 + 5^2} = 5\sqrt{2}$$

$$\textcircled{5} \quad \vec{A} = \hat{i} + \hat{j} + \hat{k}$$

$$A = \sqrt{1^2 + 1^2 + 1^2} = \sqrt{3}$$

$$\textcircled{6} \quad \vec{A} = \hat{i} - \hat{j} - \hat{k}$$

$$A = \sqrt{1^2 + 1^2 + 1^2} = \sqrt{3}$$

$$\textcircled{7} \quad \vec{A} = \hat{i} + \hat{j}$$

$$A = \sqrt{1^2 + 1^2} = \sqrt{2}$$

$$\textcircled{8} \quad \vec{A} = \hat{i} - \hat{j}$$

$$A = \sqrt{1^2 + 1^2} = \sqrt{2}$$

$$\textcircled{9} \quad \vec{A} = 3\hat{j} + 4\hat{k} \Rightarrow A = \sqrt{0^2 + 3^2 + 4^2}$$

$$A = 5$$

$$\textcircled{10} \quad \vec{A} = \frac{\hat{i}}{\sqrt{2}} - \frac{\hat{j}}{\sqrt{2}} \Rightarrow A = \sqrt{\left(\frac{1}{\sqrt{2}}\right)^2 + \left(\frac{1}{\sqrt{2}}\right)^2} = 1$$

Unit vector

$$\textcircled{11} \quad \vec{A} = \frac{\hat{i}}{\sqrt{3}} + \frac{\hat{j}}{\sqrt{3}} + \frac{\hat{k}}{\sqrt{3}} \quad A = \sqrt{\left(\frac{1}{\sqrt{3}}\right)^2 + \left(\frac{1}{\sqrt{3}}\right)^2 + \left(\frac{1}{\sqrt{3}}\right)^2}$$

$$A = 1$$

$$\textcircled{12} \quad \vec{A} = \frac{\hat{i}}{\sqrt{3}} - \frac{\hat{j}}{\sqrt{3}} - \frac{\hat{k}}{\sqrt{3}}$$

Unit Vector

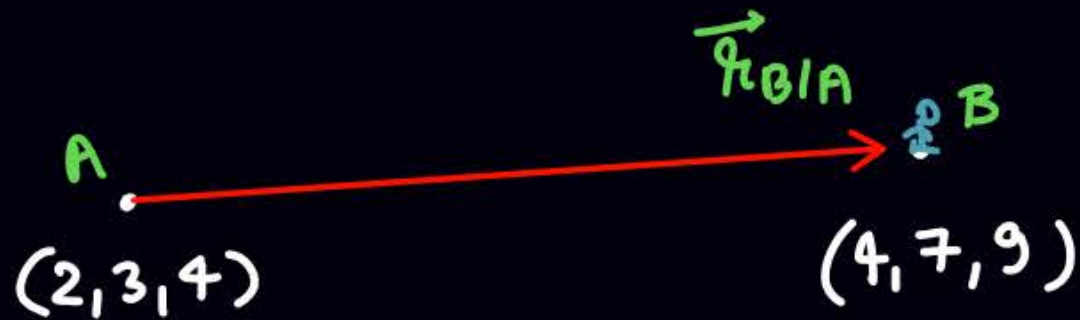
$$A = 1$$

$$\textcircled{13} \quad \vec{A} = -5\hat{i}$$

$$A = 5$$



#



$$\vec{r}_{B/A} = (4-2)\hat{i} + (7-3)\hat{j} + (9-4)\hat{k}$$

$$\vec{r}_{B/A} = 2\hat{i} + 4\hat{j} + 5\hat{k} =$$

$$|\vec{r}_{B/A}| = \sqrt{2^2 + 4^2 + 5^2} = \sqrt{45}$$

$$|\vec{r}_{B/A}| = \sqrt{(4-2)^2 + (7-3)^2 + (9-4)^2}$$

$$AB = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}$$

$$AB = \sqrt{(4-2)^2 + (7-3)^2 + (9-4)^2}$$

$$AB = \sqrt{2^2 + 4^2 + 5^2} = \sqrt{45}$$

$$* \vec{A} = (\text{magnitude}) (\text{Direction})$$

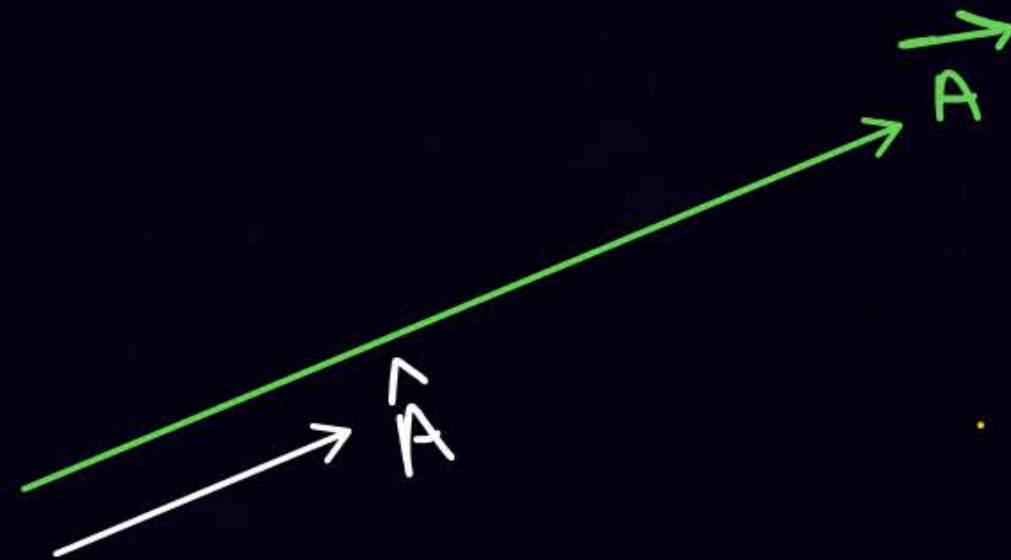
$$\vec{A} = |\vec{A}| \hat{A}$$

$$\hat{A} = \frac{\vec{A}}{|\vec{A}|} = \frac{\vec{A}}{(\text{magnitude})}$$

$$\textcircled{1} \vec{A} = 3\hat{i} + 4\hat{j}$$

$$|\vec{A}| = \sqrt{3^2 + 4^2} = 5$$

$$\hat{A} = \frac{\vec{A}}{|\vec{A}|} = \frac{3\hat{i} + 4\hat{j}}{5} = \frac{3}{5}\hat{i} + \frac{4}{5}\hat{j}$$



find \hat{A} (Unit vector along \vec{A})

$$\textcircled{1} \quad \vec{A} = 3\hat{i} + 4\hat{j} + 5\hat{k}$$

$$\hat{A} = \frac{3\hat{i} + 4\hat{j} + 5\hat{k}}{5\sqrt{2}}$$

$$\textcircled{2} \quad \vec{A} = 3\hat{i} - 4\hat{j} + 5\hat{k}$$

$$\hat{A} = \frac{3\hat{i} - 4\hat{j} + 5\hat{k}}{5\sqrt{2}}$$

$$\textcircled{3} \quad \vec{A} = \hat{i} + \hat{j} - \hat{k}$$

$$\hat{A} = \frac{\hat{i} + \hat{j} - \hat{k}}{\sqrt{3}}$$

$$\textcircled{4} \quad \vec{A} = \hat{j} - \hat{k}$$

$$\hat{A} = (\hat{j} - \hat{k})/\sqrt{2}$$

$$\textcircled{5} \quad \vec{A} = \hat{i} + \hat{j}$$

$$\hat{A} = (\hat{i} + \hat{j})/\sqrt{2}$$

$$\textcircled{6} \quad \vec{A} = \hat{i} - \hat{j} + \hat{k}$$

$$\hat{A} = \frac{\hat{i} - \hat{j} + \hat{k}}{\sqrt{3}}$$

Q A bird is flying with speed 10m/s along $\vec{A} = 3\hat{i} + 4\hat{j}$
Find its velocity

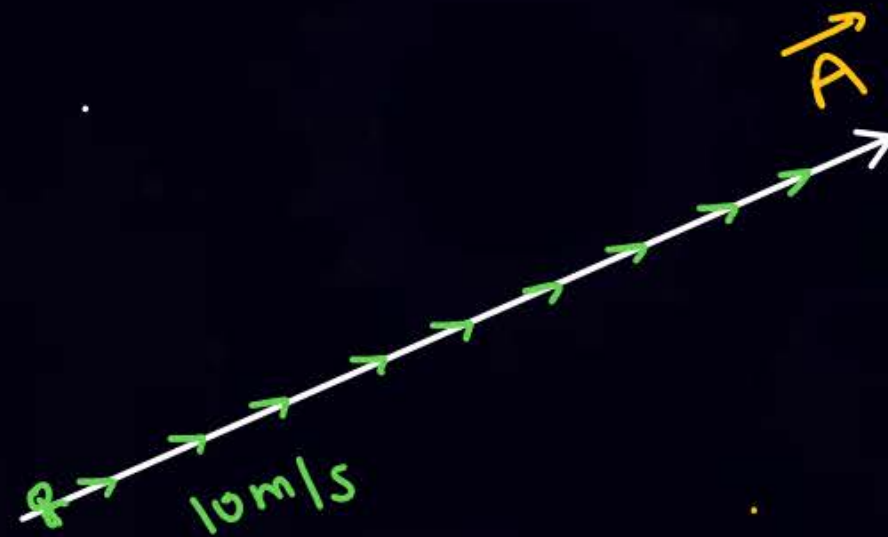
A bird is flying with speed 10m/s parallel to $\vec{A} = 3\hat{i} + 4\hat{j}$
Find its velocity

Sol $\vec{v} = (\text{magnitude})(\text{Direction})$

$$\vec{v} = (10\text{m/s}) \hat{A}$$

$$\vec{v} = 10 \times \left(\frac{3\hat{i} + 4\hat{j}}{5} \right)$$

$$\boxed{\vec{v} = 6\hat{i} + 8\hat{j}}$$



$$\hat{A} = \frac{3\hat{i} + 4\hat{j}}{5}$$



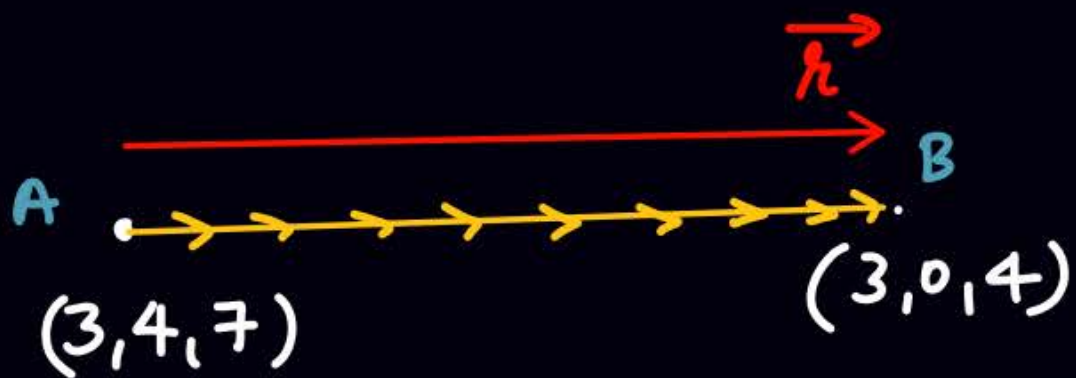
Q Find a vector of magnitude 20 N whose direction is parallel to $\vec{A} = 3\hat{i} - 4\hat{j}$

Solⁿ $\vec{B} = 20 \hat{A} = 20 \left(\frac{3\hat{i} - 4\hat{j}}{5} \right) = 12\hat{i} - 16\hat{j}$

Q Find a vector of magnitude 20 N whose direction is opposite to $\vec{A} = 3\hat{i} - 4\hat{j}$.

Solⁿ $\vec{B} = 20 (-\hat{A}) = -20 \left(\frac{3\hat{i} - 4\hat{j}}{5} \right) = -12\hat{i} + 16\hat{j}$

Q



A bird is flying with speed 50 m/s from point A directly to point B
find its velocity.

Sol

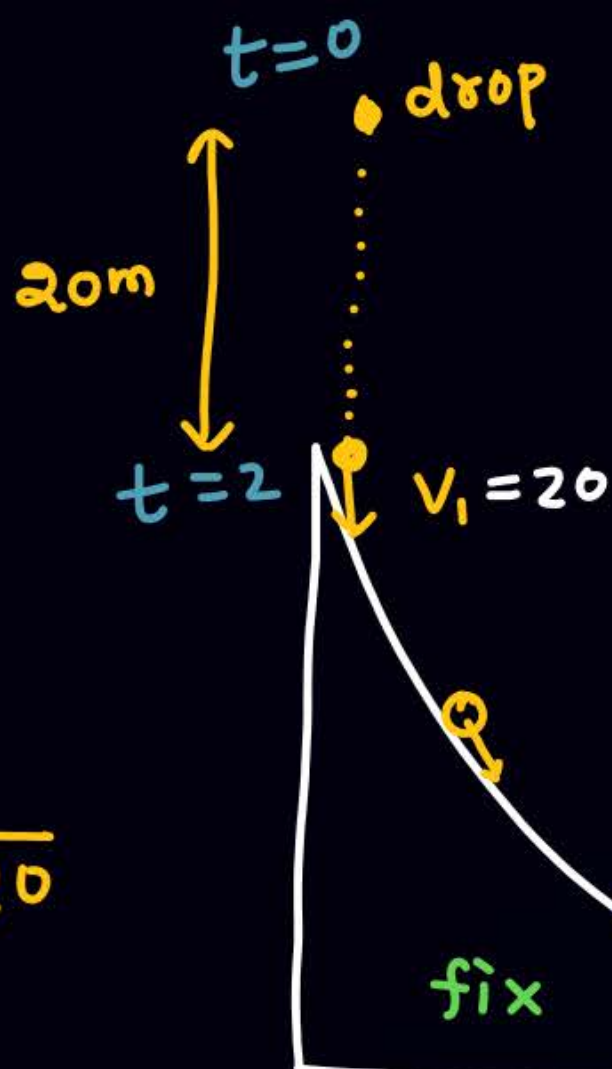
$$\vec{v} = 50 \times \hat{r}$$

$$\vec{r} = -4\hat{j} - 3\hat{k}$$

$$= 50 \left(\frac{-4\hat{j} - 3\hat{k}}{5} \right) = -40\hat{j} - 30\hat{k}$$



SSSR
Q



$$v_i = \sqrt{2gh}$$

$$v_i = \sqrt{2 \times 10 \times 20}$$

$$v_i = 20$$

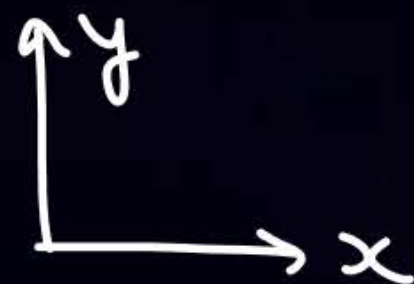
$$t=2 \longrightarrow t=10\text{sec}$$

$$\text{change in speed} = 30 - 20 = 10$$

$$\text{change in velocity} = \vec{v}_f - \vec{v}_i = 30\hat{i} - (-20\hat{j})$$

$$\Delta \vec{v} = 30\hat{i} + 20\hat{j}$$

$$|\Delta \vec{v}| = \sqrt{(30)^2 + (20)^2} = 10\sqrt{13}$$



$$\text{Avg. Acc.} = \frac{\text{Change in Velocity}}{\text{time}} = \frac{10\sqrt{13}}{8}$$

$$\begin{aligned} Q \quad \vec{A} &= 3\hat{i} + 7\hat{j} + 6\hat{k} \\ \vec{B} &= 2\hat{i} + 3\hat{j} + 5\hat{k} \end{aligned}$$

$$\vec{A} + \vec{B} = 5\hat{i} + 10\hat{j} + 11\hat{k}$$

$$\vec{A} - \vec{B} = \hat{i} + 4\hat{j} + \hat{k}$$

$$\begin{aligned} Q \quad \vec{A} &= 5\hat{i} - 6\hat{j} + 8\hat{k} \\ \vec{B} &= -2\hat{i} + 3\hat{j} - 2\hat{k} \end{aligned}$$

$$\vec{A} + \vec{B} = 3\hat{i} - 3\hat{j} + 6\hat{k}$$

$$|\vec{A} + \vec{B}| = \sqrt{3^2 + 3^2 + 6^2} = \sqrt{54}$$

$$Q \quad \vec{A} = 5\hat{i} - 6\hat{j} + 8\hat{k}$$

$$\vec{B} = -2\hat{i} + 3\hat{j} - 2\hat{k}$$

$$\vec{A} - \vec{B} = 7\hat{i} - 9\hat{j} + 10\hat{k}$$

$$|\vec{A} - \vec{B}| = \sqrt{7^2 + 9^2 + 10^2} = \sqrt{170}$$

$$Q \quad \vec{A} = 3\hat{i} + 4\hat{j} + 5\hat{k}$$

$$3\vec{A} = 9\hat{i} + 12\hat{j} + 15\hat{k}$$

$$Q \quad \vec{A} = 3\hat{i} - 2\hat{j} + 4\hat{k}$$

$$2\vec{A} = 6\hat{i} - 4\hat{j} + 8\hat{k}$$

$$-3\vec{A} = -9\hat{i} + 6\hat{j} - 12\hat{k}$$

$$3\vec{A} \Rightarrow (6, 9, 12)$$

$$2\vec{B} \Rightarrow (6, 8, 12)$$

$$\underline{Q} \quad \vec{A} = 2\hat{i} + 3\hat{j} + 4\hat{k}$$

$$\vec{B} = 3\hat{i} + 4\hat{j} + 6\hat{k}$$

$$\textcircled{1} \quad 3\vec{A} + 2\vec{B} = 12\hat{i} + 17\hat{j} + 24\hat{k}$$

$$\textcircled{2} \quad |3\vec{A} + 2\vec{B}| = \sqrt{12^2 + 17^2 + 24^2}$$

$$\textcircled{3} \quad 3\vec{A} - 2\vec{B} = \hat{j}$$

$$\textcircled{4} \quad |3\vec{A} - 2\vec{B}| = 1$$

~~Q~~

$\textcircled{5}$ If a bird start flying with speed 10m/s in the direction of $3\vec{A} - 2\vec{B}$ find its velocity.

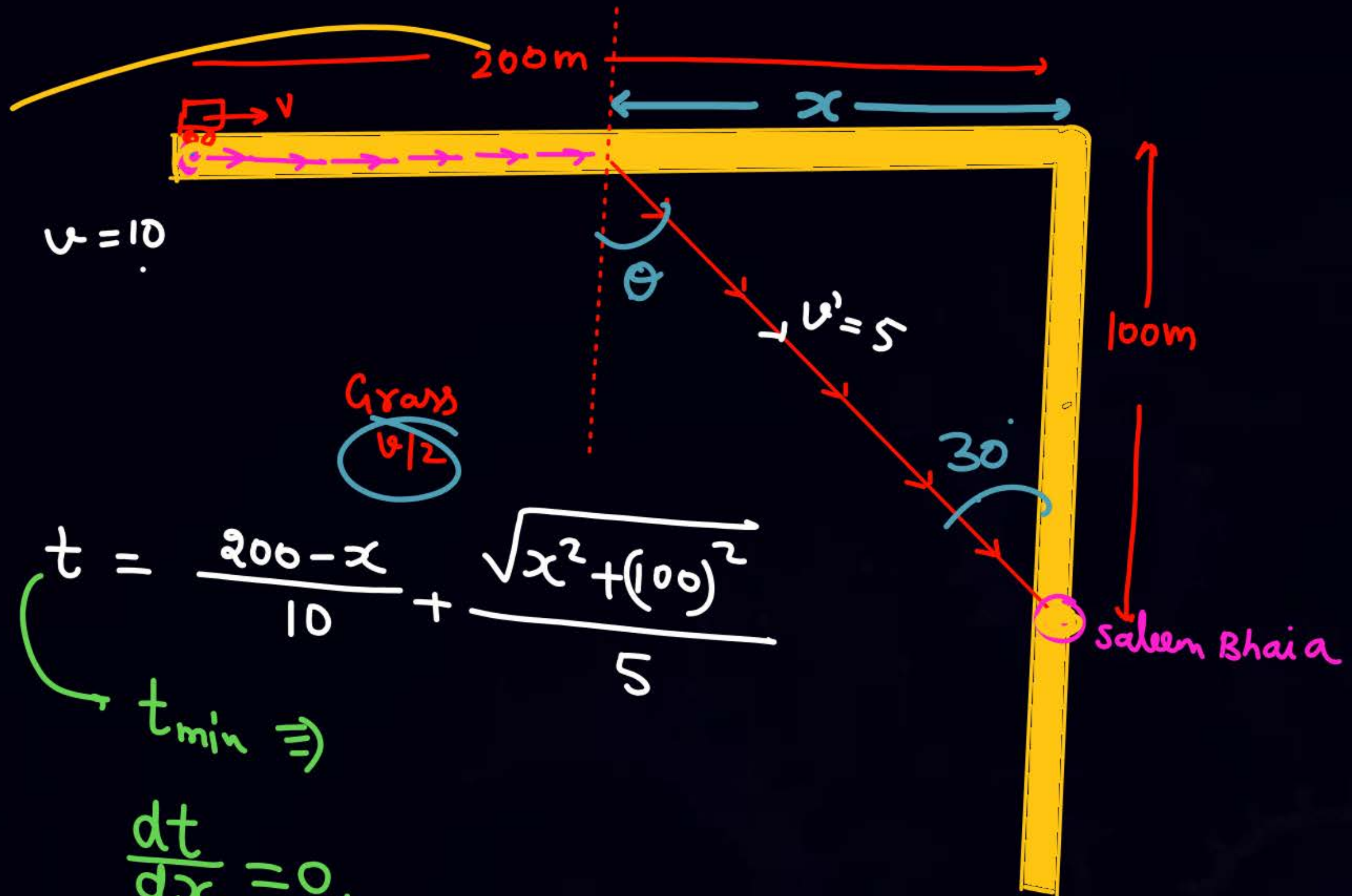
$$\vec{v} = 10\hat{j}$$

$\textcircled{6}$ If a bird start flying with speed 10m/s in the direction of $3\vec{A} + 2\vec{B}$ find its velocity.

$$\vec{v} = 10 \times \frac{12\hat{i} + 17\hat{j} + 24\hat{k}}{\sqrt{12^2 + 17^2 + 24^2}}$$



Beast mode



Grass $v/2$

$$t = \frac{200-x}{10} + \frac{\sqrt{x^2 + (100)^2}}{5}$$

$t_{\min} \Rightarrow$

$$\frac{dt}{dx} = 0,$$

$$t = \frac{200-x}{10} + \frac{(x^2 + (100)^2)^{\frac{1}{2}}}{5}$$

$$\frac{1}{2} - 1$$

$$\frac{dt}{dx} = \frac{1}{10}(0-1) + \frac{1}{5} \left[\frac{1}{2} \times [x^2 + (100)^2]^{\frac{1}{2}-1} \times 2x \right] = 0$$

$$3x^2 = (100)^2$$

$$x = \frac{100}{\sqrt{3}}$$

$$\frac{1}{\sqrt{x^2 + 10000}} \times 2x = 1$$

$$\sqrt{x^2 + 10000} = 2x$$

$$x^2 + (100)^2 = 4x^2$$

$$\cos 2\theta = \cos^2 \theta - \sin^2 \theta = 2\cos^2 \theta - 1 = 1 - 2\sin^2 \theta$$

Diagram illustrating the double-angle formula for cosine. The angle 2θ is circled in pink, with a pink arrow pointing to it labeled 40° . The angles θ and θ are each labeled with a pink arrow pointing to them labeled 20° . The angles 2θ and 2θ are each labeled with a pink arrow pointing to them labeled 20° . The angle 2θ is labeled with a pink arrow pointing to it labeled 20° .

$$\cos \theta = \cos^2 \frac{\theta}{2} - \sin^2 \frac{\theta}{2} = 2\cos^2 \frac{\theta}{2} - 1 = 1 - 2\sin^2 \frac{\theta}{2}$$

join it



Homework

- KPP - 69

- DPP

module page 114 (motion in plane)

Aanambh \rightarrow 1, 2, 4,

Prarambh \rightarrow (1-7)

Thank
You