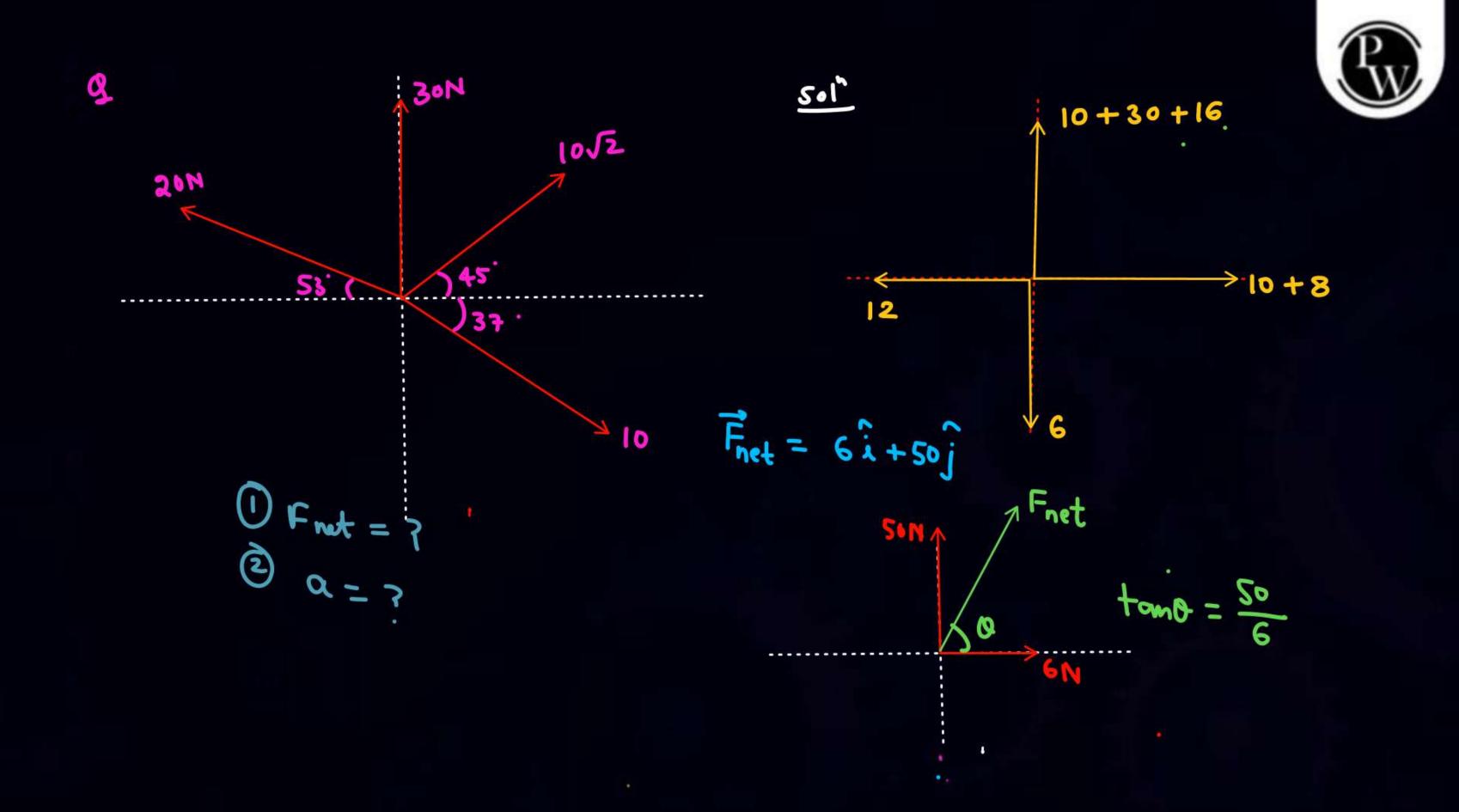
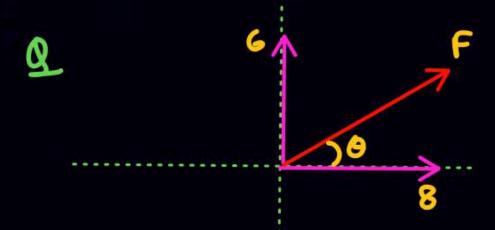


Todays Goal

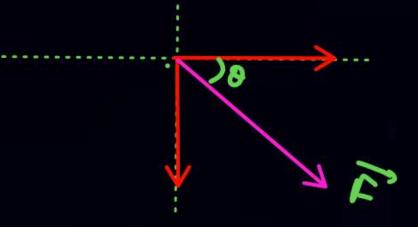












$$tamo = \frac{8}{8} = 1$$

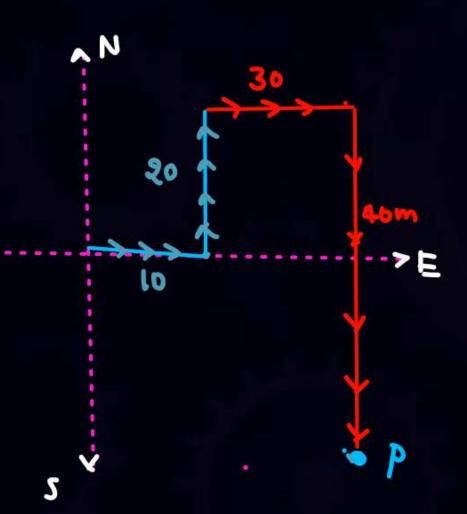
Pu

a A boy start moving from origin and he travel 10m along east

and then he tuen to left side and move 20 m along north eith that he tuen to right end cown a distance of 30 m, after that again he tuen right and travel 40 m and reaches the point P. If at P he goes inside to earth 10 m in a well

Distance = 10+20+30+40+10 = 110

Displacement = 10î+20j+30î-40j-10k 5



$$\vec{A} = A_x \hat{i} + A_y \hat{j} + A_z \hat{k}$$

Direction Cosine

$$\cos \alpha = \frac{Ax}{A}$$

=> Direction cosine.



$$\overrightarrow{A} = 3\hat{\lambda} + 4\hat{j} + 5\hat{k}$$

(2) Component of
$$\overrightarrow{A}$$
 along x -Axis = 3 i

1)

1)

1)

1)

2-Axis = 5 \widehat{K}



4) Find direction cosine cosa, cos B, cos V = ?

Anglemade by vector with x-Axis

$$\cos \alpha = \frac{Ax}{A} = \frac{3}{5\sqrt{2}}$$

$$Cos \beta = \frac{Ay}{A} = \frac{4}{5\sqrt{2}}$$

$$Ce_{5}Y = \frac{A_{2}}{A} = \frac{5}{5\sqrt{2}} = \frac{1}{\sqrt{2}}$$

 $\cos^2 x + \cos^2 \beta + \cos^2 Y = \frac{9}{49} + \frac{4}{45} + \frac{36}{49}$



Find direction cosine cosa, cos B, cos V = ?

Anglemade by vector with x-Axis

$$Cos x = \frac{Ax}{A} = \frac{3}{3}$$

$$Cos \beta = \frac{Ay}{A} = \frac{3}{4}$$

$$\frac{Cosy - Az}{A} = \frac{6}{7}$$

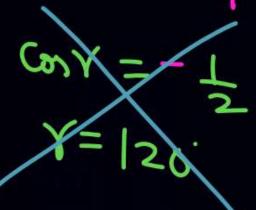
If A make angle 45, 60 Pw with X-Axis & y-Axis. Find angle made by A with 2 Axis Sol" x= 45, B= 60, Y=? COSTX + COSTS + COSTY = 1 Cus 45 + Cos 60 + Cos Y = 1 2+4+ cos r=1 $Cos^2 Y = \frac{1}{4} \qquad Cos Y = \pm \frac{1}{2}$ _ . Y=60,120

$$(8)$$
 $Q = 45$, $B = 30$, $Y = ?$

$$\frac{1}{2} + \frac{3}{4} + \cos^2 y = 1$$

$$\cos^2 Y = 1 - \frac{1}{2} - \frac{3}{4} = \frac{4 - 2 - 3}{4}$$

4 (Not possible)





Dot product

magnitude of B

0 → Angle b/w A & B.

10 Unit & 20 Unit are at angle 60. find their dot produc

Sol
$$\overrightarrow{A} \cdot \overrightarrow{B} = AB \cos \theta$$

$$= 10 \times 20 \times \cos 60$$

$$= 10 \times 20 \times \frac{1}{2} = 10 \times 10$$

$$= 100$$

$$\overrightarrow{A} \cdot \overrightarrow{B} = AB \cos \theta$$

$$\widehat{A} \cdot \widehat{A} = 1 \times 1 \times \cos \theta$$

$$\begin{array}{ccc}
\mathbf{A} & = & \mathbf{i} \\
\mathbf{B}' & = & \mathbf{j}
\end{array}$$

$$\mathbf{A} \cdot \mathbf{B}' = \mathbf{A} \mathbf{G} \cos \theta$$

$$\mathbf{i} \cdot \mathbf{j} & = \mathbf{I} \times \mathbf{I} \times \cos \theta$$

$$\mathbf{i} \cdot \mathbf{j} & = \mathbf{0}$$

$$2.\hat{j} = \hat{j}.\hat{j} = \hat{k}.\hat{k} = 1$$

$$2.\hat{j} = \hat{j}.\hat{k} = \hat{k}.\hat{k} = 0$$



$$\vec{B} = 3\hat{i} + 4\hat{j}$$

$$\vec{B} = 2\hat{i} + 6\hat{j}$$

$$\vec{A} \cdot \vec{B}' = 3x2 + 4x6$$

= $6 + 24 = 30$

$$\vec{A}' = 3\hat{\lambda} + 4\hat{j} + 5\hat{k}$$

$$\vec{B}' = 2\hat{\lambda} - 3\hat{j} - 4\hat{k}$$

$$\vec{A} \cdot \vec{B}' = 6 - 12 - 20 = -26$$

$$\vec{A} = 3\hat{1} + 4\hat{j}$$
 $\vec{B} = -4\hat{1} + 3\hat{j}$
 $\vec{A} \cdot \vec{B} = -12 + 12 = 0$

Find A: B

$$\overrightarrow{A} = 4\hat{\lambda} + 3\hat{j}$$

$$\overrightarrow{B} = \hat{\lambda} + \hat{j}$$

$$\overrightarrow{AB} = 4 + 3 = 7$$

3
$$\vec{A} = 4\hat{\lambda} - 3\hat{j}$$
 $\vec{B}' = \hat{\lambda} + \hat{j}$
 $\vec{A} \cdot \vec{B} = 4 - 3 - 1$

(3)
$$\vec{A} = 3\hat{i} - 4\hat{j} + 5\hat{k}$$

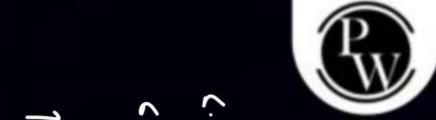
 $\vec{B} = \hat{i} - 2\hat{j} - 3\hat{k}$
 $\vec{A} \cdot \vec{B} = 3 + 8 - 15 = -4$

$$\frac{A}{A} = -3\hat{\lambda} - 4\hat{j} + 6\hat{k}$$

$$\frac{B}{B} = 2\hat{\lambda} + 6\hat{j} + 5\hat{k}$$

$$\frac{A}{B} = -6 - 24 + 30 = 0$$

$$\frac{A}{B} = 0 \quad A \perp B$$



$$\overrightarrow{A} = \widehat{\lambda} - \widehat{j}$$

$$\overrightarrow{B} = \widehat{j} + 3\widehat{k}$$

$$\overrightarrow{A} = \widehat{\lambda} - \widehat{j} + 3\widehat{k}$$

$$\overrightarrow{A} = 0 + \widehat{j} + 3\widehat{k}$$

$$\overrightarrow{A} = 0 + \widehat{j} + 0 = -1$$

$$\mathbf{Q} \quad \overrightarrow{A} = 3\hat{i} + 4\hat{j}$$

$$\mathbf{B} = .\hat{i} + \hat{j}$$

$$\overrightarrow{A} = 4\widehat{\lambda} - 3\widehat{j}$$
 $\overrightarrow{B} = \widehat{\lambda} + \widehat{j}$
find angle blw $\overrightarrow{A} \ge \widehat{B}$

$$\overrightarrow{A} \cdot \overrightarrow{B} = AB \cos \theta$$

$$4-3 = 5 \times \sqrt{2} \cos \theta$$

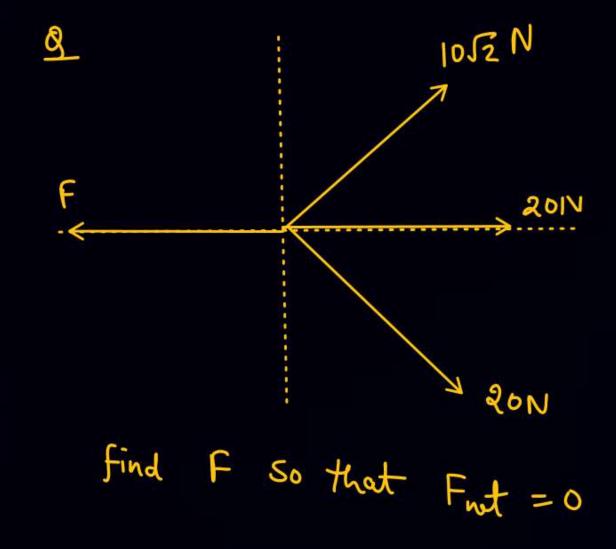
Cono = 1 5/2



$$Q \overrightarrow{A} = 2\hat{\lambda} - 3\hat{j} + 6\hat{k}$$

$$\overrightarrow{B} = \hat{\lambda} + \hat{j} + \hat{k}$$
Angle blu $\overrightarrow{A} \ge B$





Q11 The unit vector parallel to the resultant of the

vectors
$$ec{A}=4\hat{i}\,+3\hat{j}\,+6\hat{k}$$
 and

$$ec{B}=-\hat{i}\,+3\hat{j}-8\hat{k}$$
 is

(A)
$$\frac{1}{7}(3\hat{i}+6\hat{j}-2\hat{k})$$

(B)
$$\frac{1}{7}(3\hat{i} + 6\hat{j} + 2\hat{k})$$

(C)
$$rac{1}{49}(3\hat{i} + 6\hat{j} - 2\hat{k})$$

(D)
$$rac{1}{49}(3\hat{i} - 6\hat{j} + 2\hat{k})$$



Match List I with List II.

Choose the correct answer from the options given below:

- (a) \rightarrow (iv), (b) \rightarrow (i), (c) \rightarrow (iii), (d) \rightarrow (ii)
- (2) (a) \rightarrow (iv), (b) \rightarrow (iii), (c) \rightarrow (i), (d) \rightarrow (ii)
- (3) (a) \rightarrow (iii), (b) \rightarrow (ii), (c) \rightarrow (iv), (d) \rightarrow (i)
- (a) \rightarrow (i), (b) \rightarrow (iv), (c) \rightarrow (ii), (d) \rightarrow (iii)

[JEE Main-2021]

List I		List II	List II	
(a)	$\vec{C} - \vec{A} - \vec{B} = 0$	(i) Ā	B	
(b)	$\vec{A} - \vec{C} - \vec{B} = 0$	(ii) C	B	
(c)	$\vec{B} - \vec{A} - \vec{C} = 0$	(iii) A	B	
(d)	$\vec{A} + \vec{B} = -\vec{C}$	(iv) \tilde{C}	B	

Ans: (2)



Which of the following relation is true for two unit vectors \hat{A} and \hat{B} making an angle θ to each other?

[JEE Main-2022]

$$|\hat{A} + \hat{B}| = |\hat{A} - \hat{B}| \tan \frac{\theta}{2}$$

$$|\hat{A} - \hat{B}| = |\hat{A} + \hat{B}|\tan\frac{\theta}{2}$$

$$|\hat{A} + \hat{B}| = |\hat{A} - \hat{B}|\cos\frac{\theta}{2}$$

$$|\hat{A} - \hat{B}| = |\hat{A} + \hat{B}|\cos\frac{\theta}{2}$$



When vector $\vec{A} = 2\hat{i} + 3\hat{j} + 2\hat{k}$ is subtracted from vector \vec{B} , it gives a vector equal to $2\hat{j}$. Then the magnitude of vector \vec{B} will be: [11 April 2023 - Shift 2]

- **1** √5
- **2** 3
- **3** √6
- **4** √33



Two forces having magnitude A and $\frac{A}{2}$ are perpendicular to each other. The magnitude of their resultant is: [08 April 2023 - Shift 1]

- $\begin{array}{c}
 \sqrt{5} A \\
 4
 \end{array}$
- $2 \frac{\sqrt{5}A}{2}$
- $3 \frac{5A}{2}$
- $4 \frac{\sqrt{5}A^2}{2}$



If two vectors \vec{A} and \vec{B} having equal magnitude R are inclined at an angle θ , then [31 Jan. 2024 - Shift 2]

$$|\vec{A} - \vec{B}| = \sqrt{2}R \sin\left(\frac{\theta}{2}\right)$$

$$|\vec{A} + \vec{B}| = 2R \sin\left(\frac{\theta}{2}\right)$$

$$|\vec{A} + \vec{B}| = 2R \cos\left(\frac{\theta}{2}\right)$$

$$|\vec{A} - \vec{B}| = 2R \cos\left(\frac{\theta}{2}\right)$$



A vector in x-y plane makes an angle of 30° with y-axis. The magnitude of y-component of vector is $2\sqrt{3}$. The magnitude of x-component of the vector will be:

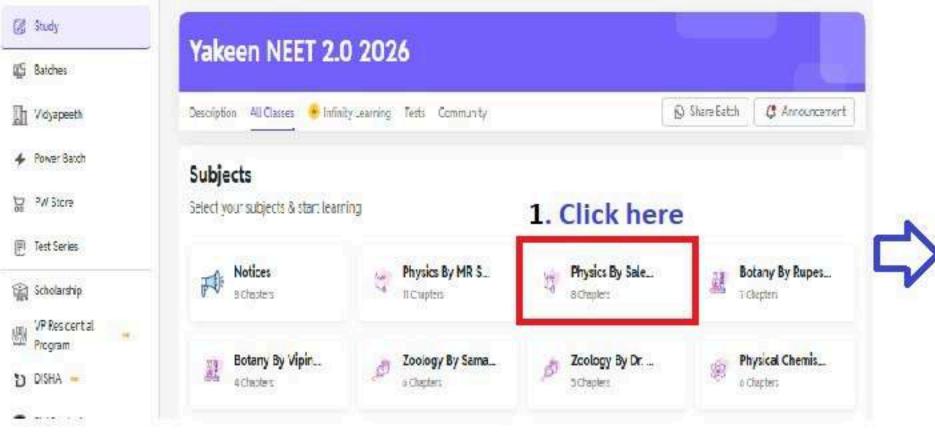
[15 April 2023 - Shift 1]

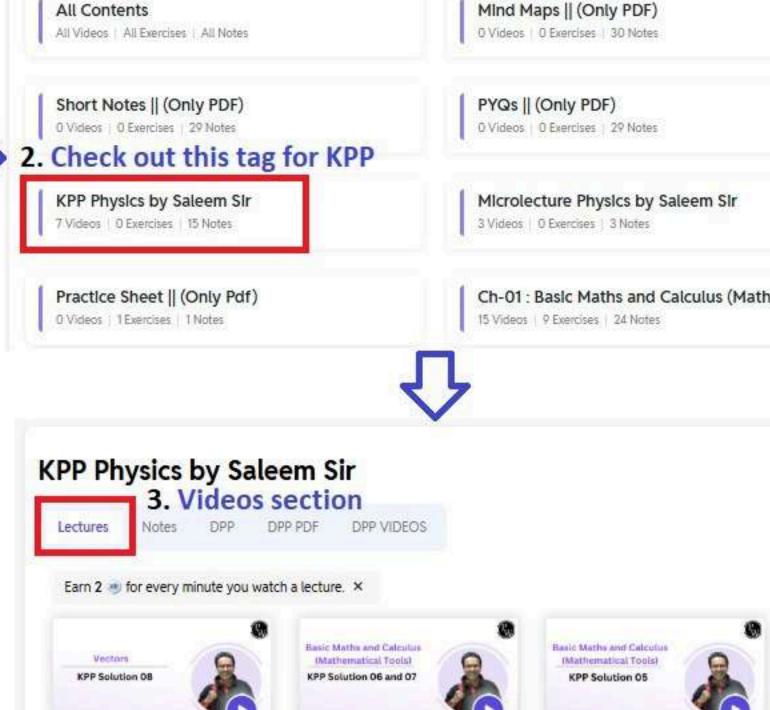
- $\boxed{1} \quad \frac{1}{\sqrt{3}}$
- **2** 6
- 3 2
- 4 √3



The resultant of two vectors \vec{A} and \vec{B} is perpendicular to \vec{A} and its magnitude is half that of \vec{B} . The angle between vectors \vec{A} and \vec{B} is _____°. [09 Apr. 2024 - Shift 2]

Ans: (150)





By Saleem Ahmad Sir

Basic Maths and Calculus

(Mathematical Tools): KPP Solution...

June 6, 2025

By Saleem Ahmad Sir

Basic Maths and Calculus

(Mathematical Tools): KPP Solution...

(3) 00:58:30

May 31, 2025

(i) 01:55:24

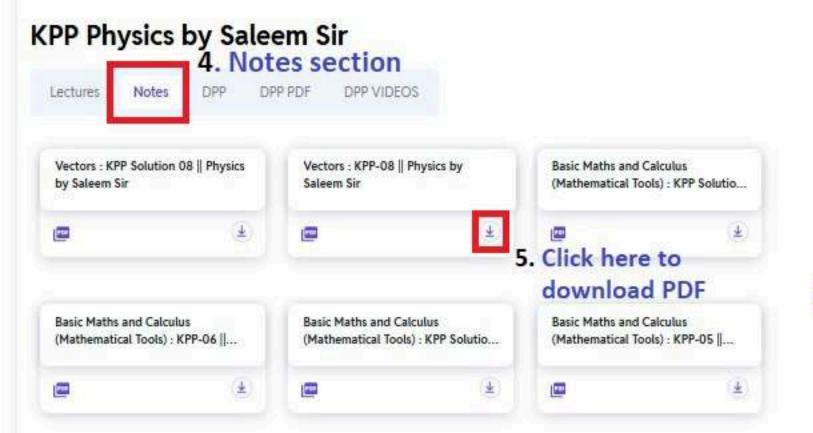
Physics by Saleem Sir

By Saleem Ahmad Sir

Vectors: KPP Solution 08

③ 01:07:43

June 9, 2025







Home work

-Revise All notes (will be up loaded

- KPP 10

DPP

even.



Thank You