

# YAKEEN NEET 2.0

2026

Vectors

PHYSICS

Lecture - 03

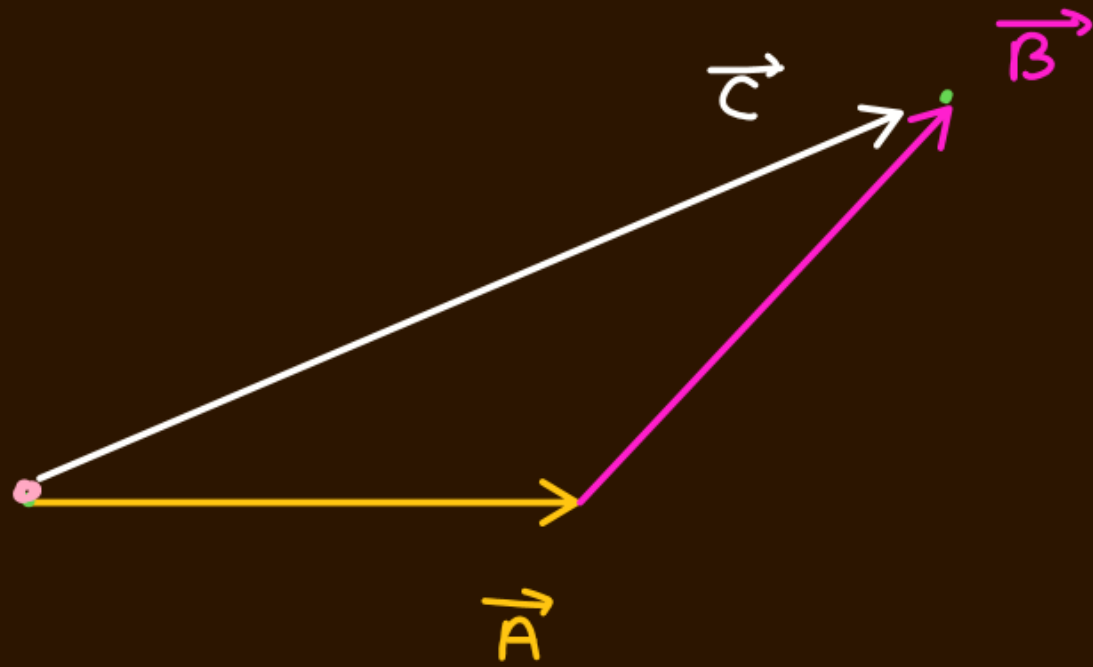
By - Saleem Ahmed Sir



## Today's Goal

- Triangle Law of Vector addition
- magnitude of resultant of two forces.

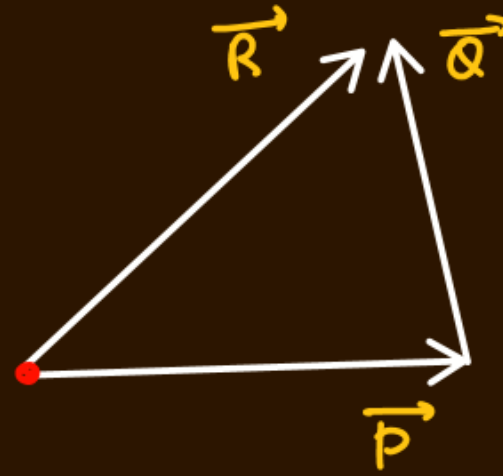
## Triangle Law of vector addition



$$\vec{A} + \vec{B} = \vec{C}$$

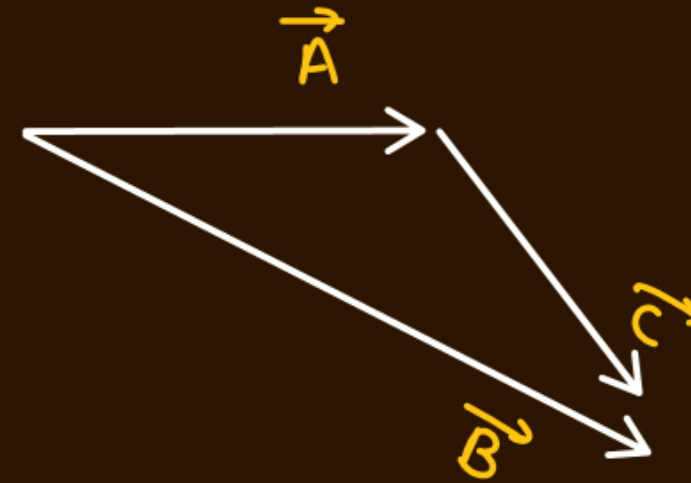
tail of  $\vec{B}$  = start

①



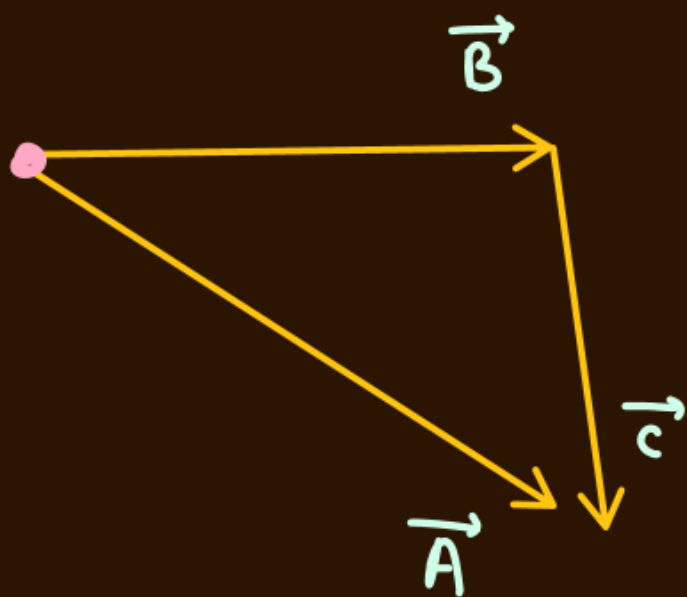
$$\vec{P} + \vec{Q} = \vec{R}$$

②



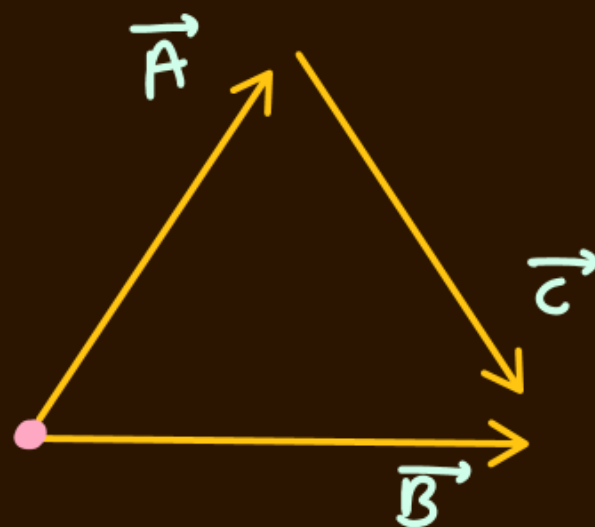
$$\vec{A} + \vec{C} = \vec{B}$$

③



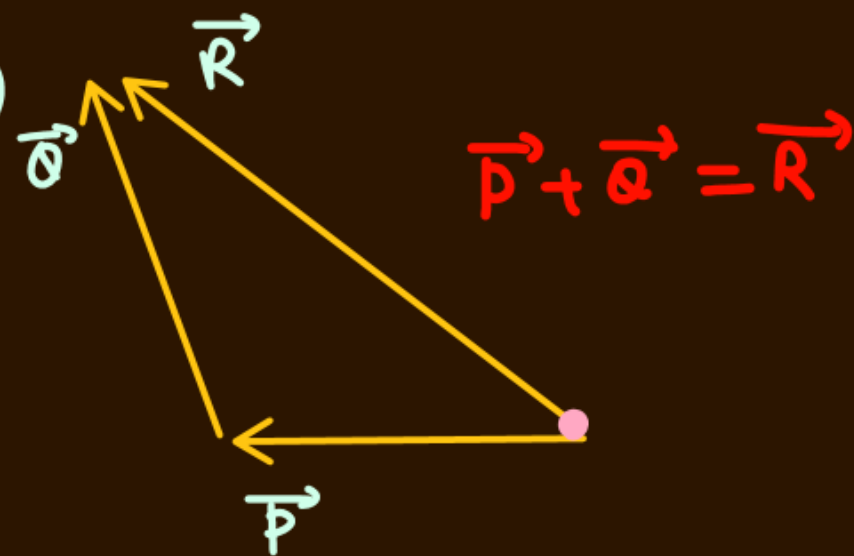
$$\vec{B} + \vec{C} = \vec{A}$$

④



$$\vec{A} + \vec{C} = \vec{B}$$

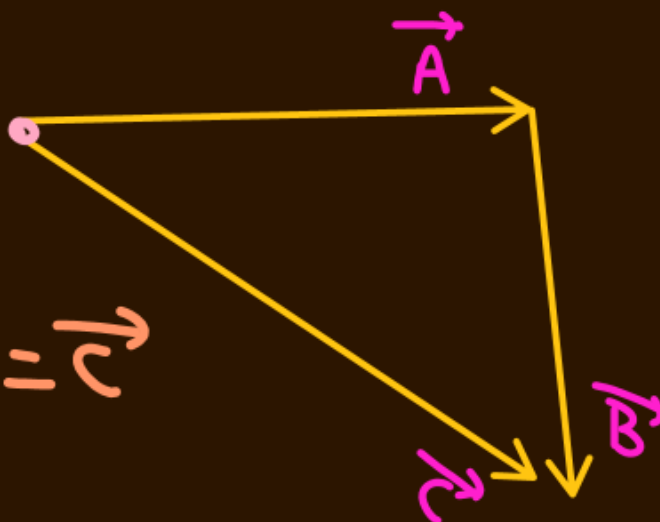
⑤



$$\vec{P} + \vec{Q} = \vec{R}$$

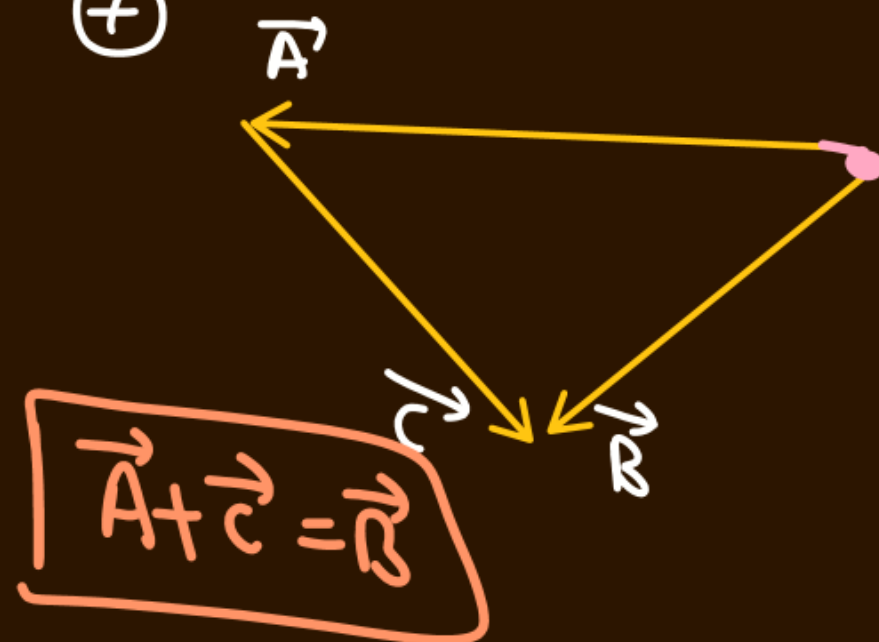
SKC

⑥



$$\vec{A} + \vec{B} = \vec{C}$$

⑦



$$\vec{A} + \vec{C} = \vec{B}$$



# ① Magnitude of resultant of $\vec{A}$ & $\vec{B}$

$$\Rightarrow \vec{A} + \vec{B} = \vec{C}$$

magnitude of  $\vec{A} = |\vec{A}| = A$

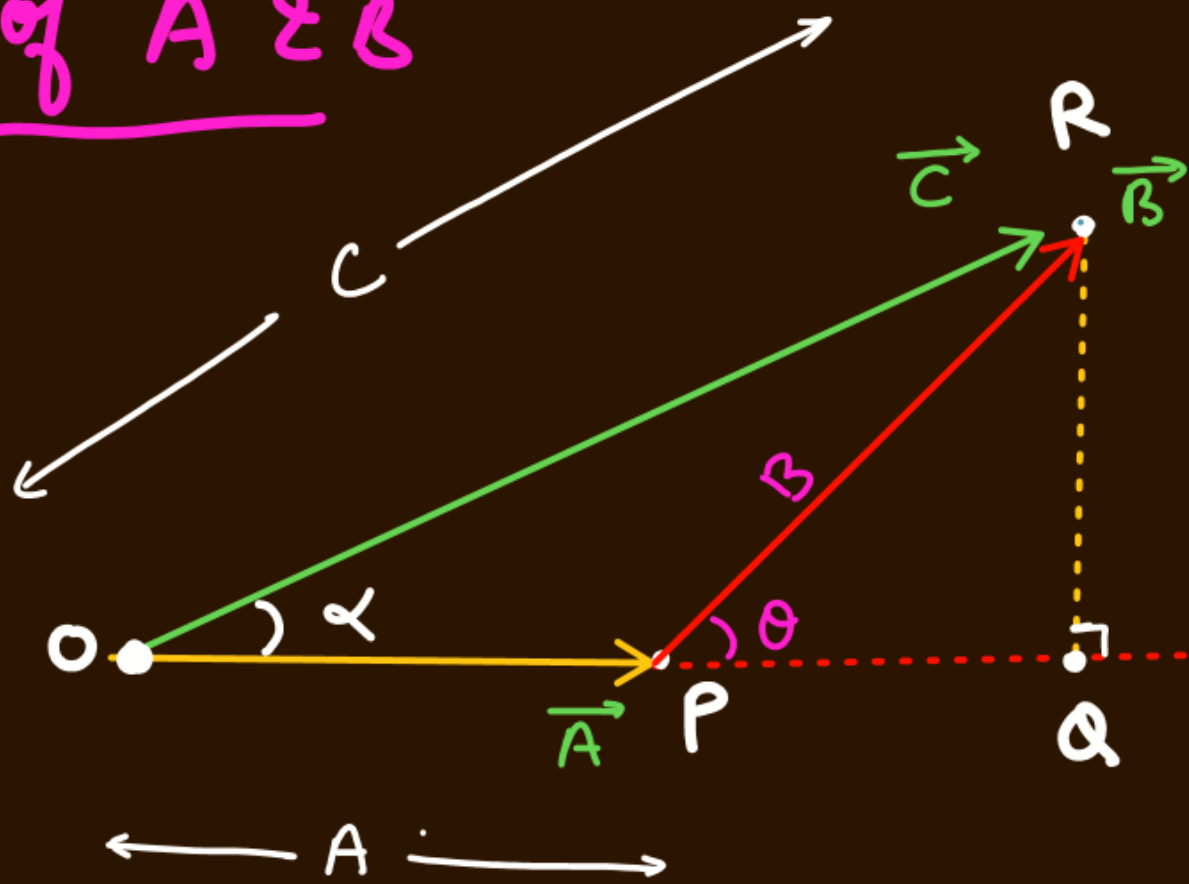
magnitude of  $\vec{B} = |\vec{B}| = B$

magnitude of  $\vec{C} = |\vec{C}| = C$

$\theta \rightarrow$  Angle between  $\vec{A}$  &  $\vec{B}$ .

$$\tan \alpha = \frac{B \sin \theta}{A + B \cos \theta}$$

$\alpha \equiv$  Angle made by  $\vec{C}$  with  $\vec{A}$



$$\cos \theta = \frac{PQ}{B}$$

$$PQ = B \cos \theta$$

$$\sin \theta = \frac{RQ}{B}$$

$$RQ = B \sin \theta$$

$\triangle ORQ$

$$(OQ)^2 + (QR)^2 = (OR)^2 \quad (\text{Pytho. -})$$

$$(A + B \cos \theta)^2 + (B \sin \theta)^2 = C^2$$

2

$$(A + B \cos \theta)^2 + (B \sin \theta)^2 = C^2$$

$$A^2 + B^2 \cos^2 \theta + 2AB \cos \theta + B^2 \sin^2 \theta = C^2$$

$$A^2 + B^2 \cos^2 \theta + B^2 \sin^2 \theta + 2AB \cos \theta = C^2$$

$$A^2 + B^2 (\cos^2 \theta + \sin^2 \theta) + 2AB \cos \theta = C^2$$

$$C = \sqrt{A^2 + B^2 + 2AB \cos \theta}$$

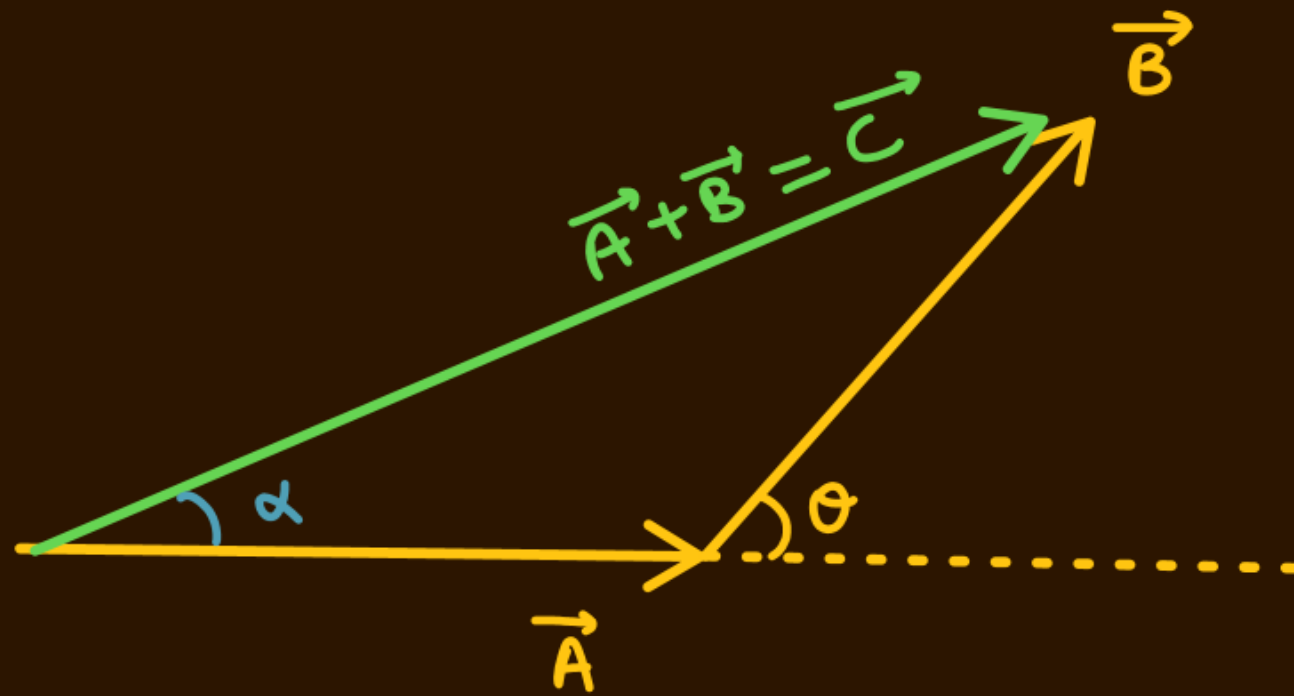
③

Resultant of  $\vec{A}$  &  $\vec{B} = \vec{A} + \vec{B} = \vec{C}$

Addition of  $\vec{A}$  &  $\vec{B} = \vec{A} + \vec{B} = \vec{C}$

$$C = \sqrt{A^2 + B^2 + 2AB \cos \theta}$$

$$\tan \alpha = \frac{B \sin \theta}{A + B \cos \theta}$$



$A, B, C \rightarrow$  magnitude, (+ve)

~~✗d~~

SXC

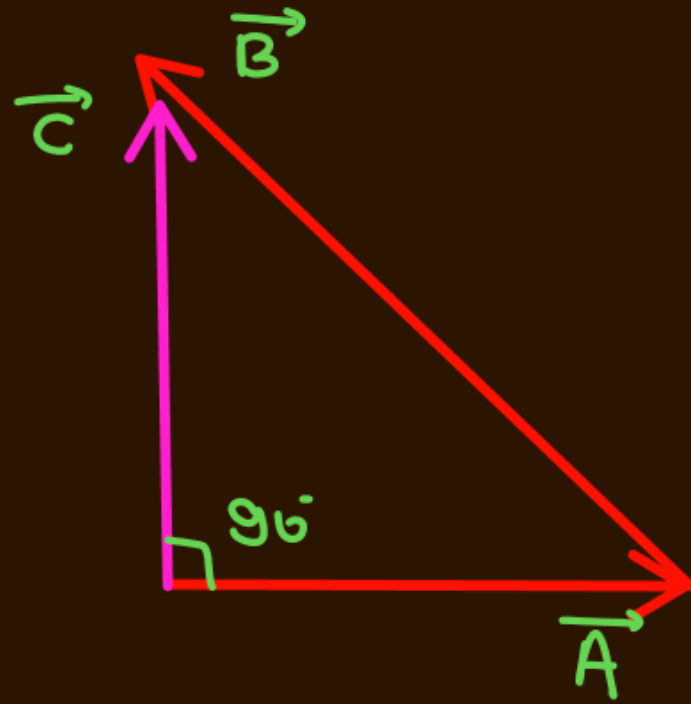
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#

Resultant of  $\vec{A}$  &  $\vec{B}$  is perpendicular to  $\vec{A}$

Draw Daigran

$\alpha = 90^\circ$



note

$$\vec{A} + \vec{B} = \vec{C}$$

orthogonal



③

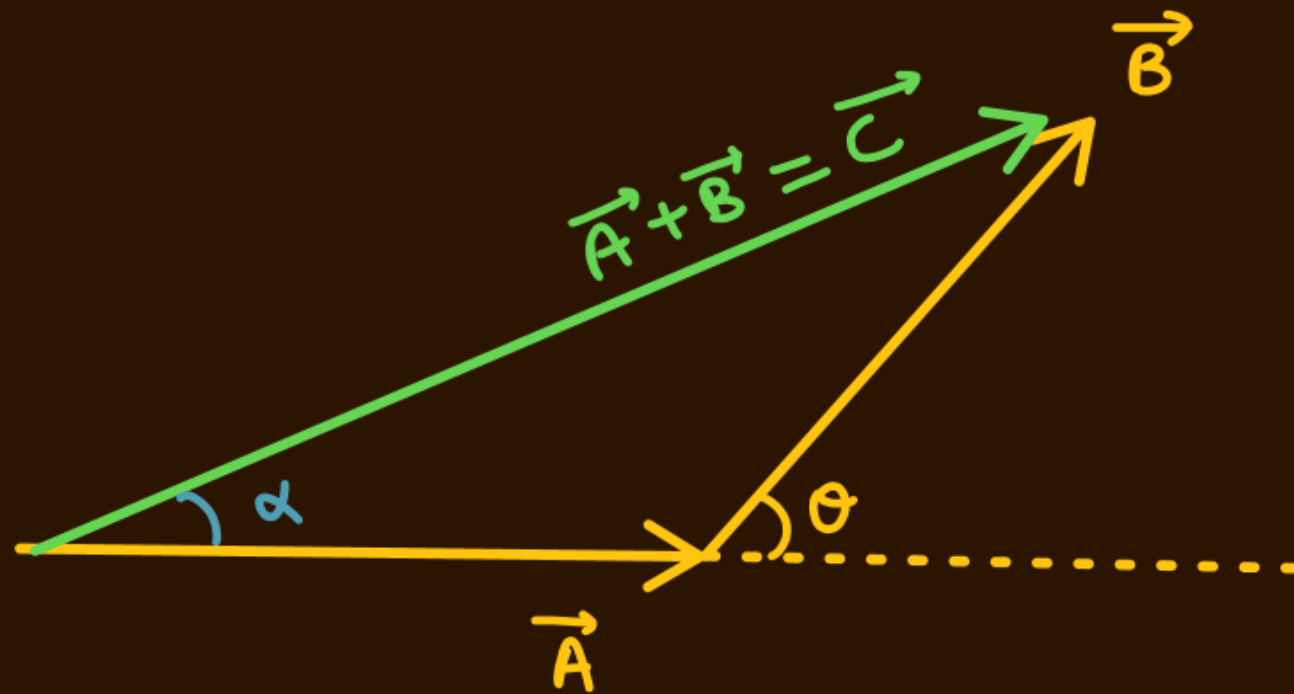
Resultant of  $\vec{A}$  &  $\vec{B} = \vec{A} + \vec{B} = \vec{C}$

Addition of  $\vec{A}$  &  $\vec{B} = \vec{A} + \vec{B} = \vec{C}$

$$C = \sqrt{A^2 + B^2 + 2AB \cos \theta}$$

$$\tan \alpha = \frac{B \sin \theta}{A + B \cos \theta}$$

$\theta \rightarrow$  Angle b/w  $\vec{A}$  &  $\vec{B}$

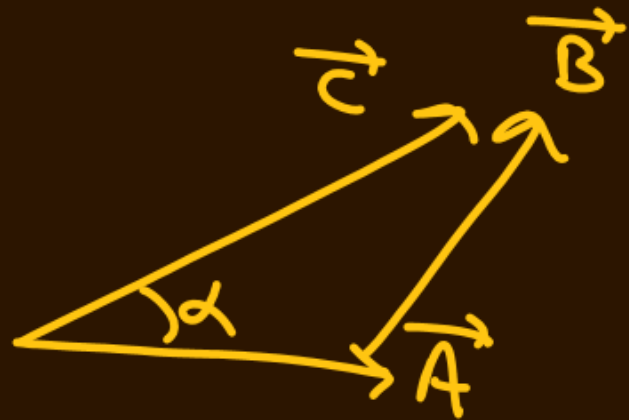


$A, B, C \rightarrow$  magnitude, (+ve)

Q If two vector of magnitude 10N and 20N are such that angle between them is  $60^\circ$ . Find magnitude of their resultant. and angle made by resultant with smaller vector.

Sol (a)  $A = 10$   
 $B = 20$   
 $\theta = 60^\circ$

$$\vec{A} + \vec{B} = \vec{C}$$



$$C = \sqrt{A^2 + B^2 + 2AB \cos \theta}$$

$$C = \sqrt{(10)^2 + (20)^2 + 2 \times 10 \times 20 \times \cos 60^\circ}$$

$$C = \sqrt{100 + 400 + 200} = \sqrt{700}$$
$$C = 10\sqrt{7}$$

$$\tan \alpha = \frac{B \sin \theta}{A + B \cos \theta}$$

$$\tan \alpha = \frac{20 \sin 60^\circ}{10 + 20 \cos 60^\circ}$$
$$= \frac{20 \sqrt{3}/2}{10 + 20 \times \frac{1}{2}}$$

$$\tan \alpha = \frac{\sqrt{3}}{2}$$

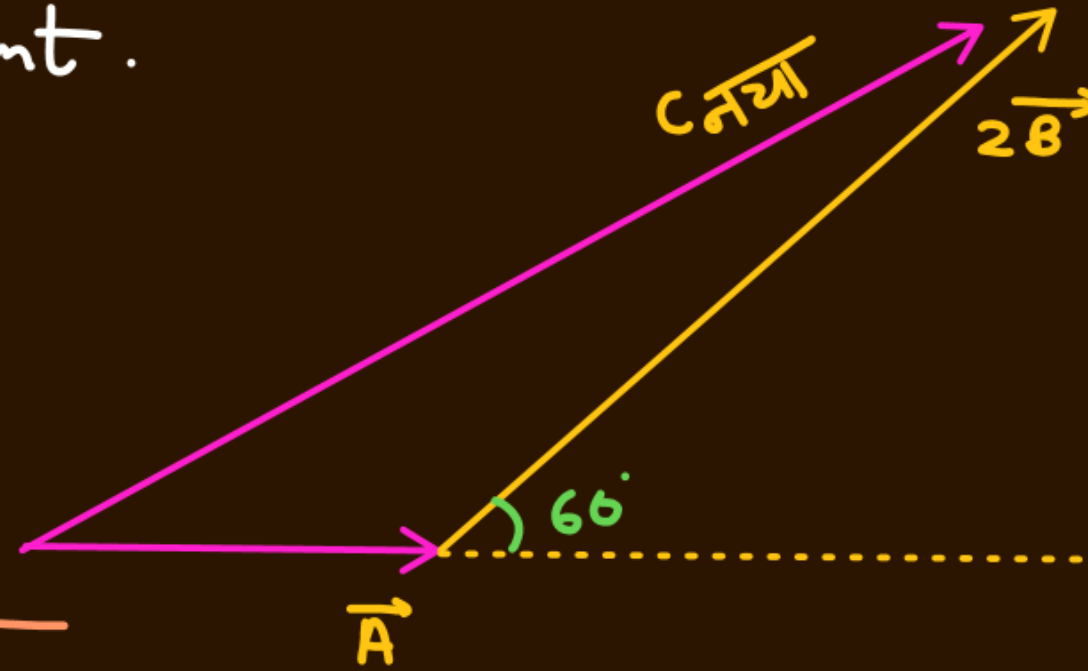
- ⑥ In above part ( $A=10$ ,  $B=20$ ,  $\theta=60^\circ$ ) if  $\vec{B}$  become twice and added to  $\vec{A}$  find magnitude of new resultant.

Sol<sup>n</sup>

$$A_{\text{new}} = 10$$

$$B_{\text{new}} = 40$$

$$C_{\text{new}} = \sqrt{(10)^2 + (40)^2 + 2 \times 10 \times 40 \times \cos 60^\circ}$$
$$= 10\sqrt{21}$$



Q magnitude of resultant of two forces  $\vec{A}$  &  $\vec{B}$  is 5 Newton. If magnitude of A is  $5\sqrt{3}$  N and magnitude of  $\vec{B}$  is 5 N then angle between  $\vec{A}$  &  $\vec{B}$ .

~~(A)  $\theta = 60$~~

(B)  $\theta = -60$

☒ (C)  $\theta = 150$

(d)  $\theta = 120$

$$C = \sqrt{A^2 + B^2 + 2AB \cos \theta}$$

$$5 = \sqrt{(5\sqrt{3})^2 + (5)^2 + 2 \times 5\sqrt{3} \times 5 \cos \theta}$$

$$25 = 75 + 25 + 50\sqrt{3} \cos \theta$$

$$-75 = 50\sqrt{3} \cos \theta$$

$$\cos \theta = \frac{-75}{50\sqrt{3}} = -\frac{3}{2\sqrt{3}} = -\frac{\sqrt{3}}{2}$$

$$\cos \theta = -\frac{\sqrt{3}}{2}$$

2<sup>nd</sup> quad.

$$\cos(180 - 30) = -\frac{\sqrt{3}}{2}$$

$$\theta = 150$$

Q If two vector  $\vec{A}$  and  $\vec{B}$  have same magnitude  $x$ .  
find magnitude of their resultant if angle between is  $\theta$

(a)  $\theta = 0^\circ$

$$C = \sqrt{x^2 + x^2 + 2 \cdot x \cdot x \cdot \cos 0^\circ} = 2x$$

(b)  $\theta = 60^\circ$

$$C = \sqrt{x^2 + x^2 + 2 \cdot x \cdot x \cdot \cos 60^\circ} = x\sqrt{3}$$

(c)  $\theta = 90^\circ$

$$C = \sqrt{x^2 + x^2 + 2 \cdot x \cdot x \cdot \cos 90^\circ} = x\sqrt{2}$$

(d)  $\theta = 120^\circ$

$$C = \sqrt{x^2 + x^2 + 2 \cdot x \cdot x \cdot \cos 120^\circ}$$

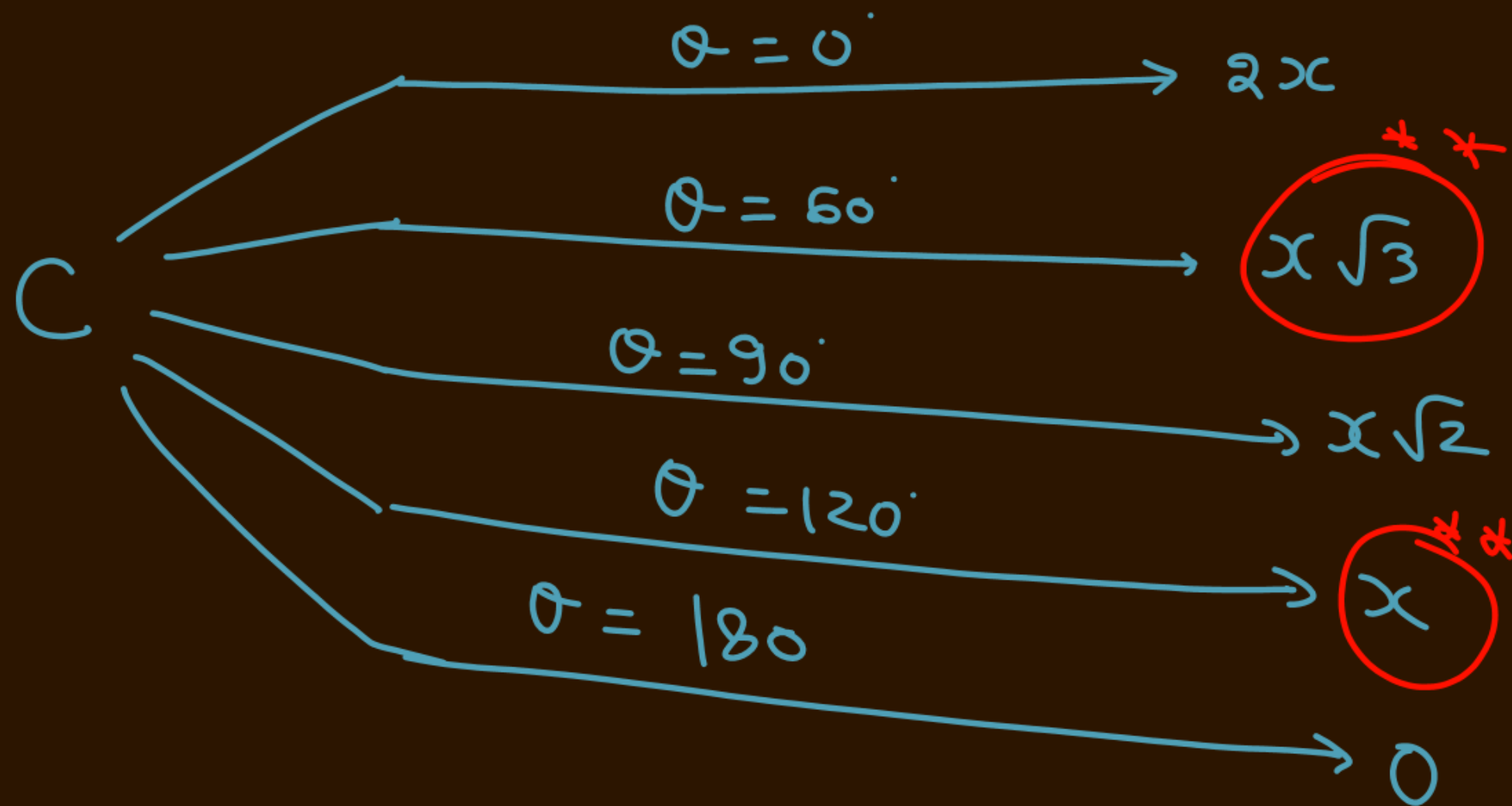
$$C = \sqrt{x^2 + x^2 - 2x^2 \cdot \frac{1}{2}} = x$$

(e)  $\theta = 180^\circ$

$$C = \sqrt{x^2 + x^2 + 2 \cdot x \cdot x \cdot \cos 180^\circ} = 0$$

note

If two vector of same magnitude  $x$  are acting.





(\*)

Q Two vector  $\vec{A}$  &  $\vec{B}$  have the same magnitude 'a' and resultant has magnitude 'R'.

Now  $\vec{B}$  is doubled and added to  $\vec{A}$ , and new resultant become  $a\sqrt{3}$

Find angle between  $\vec{A}$  &  $\vec{B}$ .

Sol  $R = \sqrt{a^2 + a^2 + 2 \cdot a \cdot a \cdot \cos \theta}$

Use ही नहीं हुआ

$$R_{\text{new}} = a\sqrt{3} = \sqrt{a^2 + (2a)^2 + 2 \cdot a \cdot 2a \cos \theta}$$

$$3a^2 = a^2 + 4a^2 + 4a^2 \cos \theta$$

$$3 = 5 + 4 \cos \theta$$

$$3 - 5 = 4 \cos \theta$$

$$\cos \theta = -\frac{1}{2}$$

$$\theta = 120^\circ$$

(b)  $\frac{R_{\text{new}}}{R_{\text{old}}} = \checkmark$

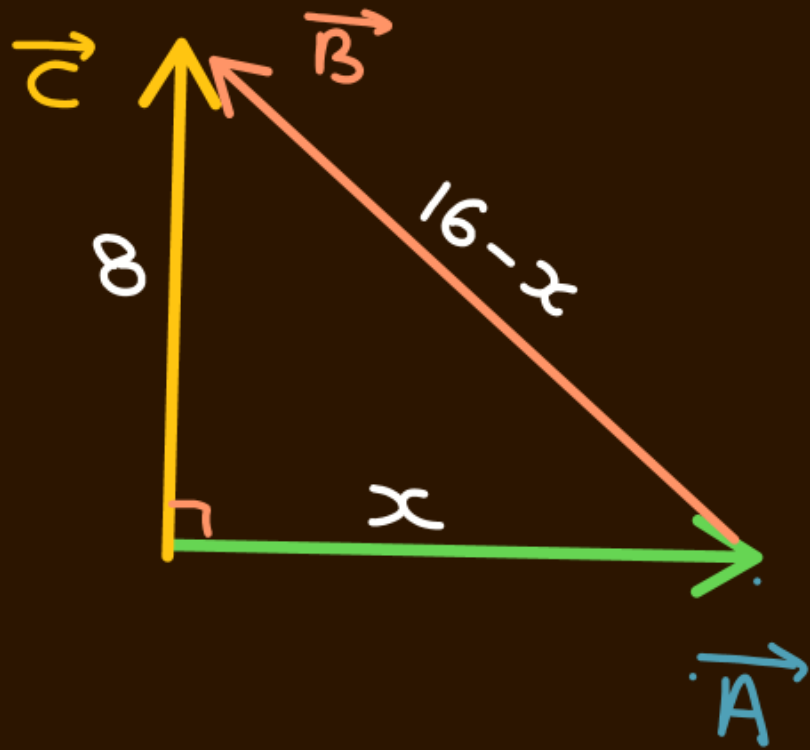
EXPT NEET

\*\*\* (Salem Sir Special ques) SSSQ.

Q

Sum of the magnitude of  $\vec{A}$  &  $\vec{B}$  is 16N. If magnitude of resultant of  $\vec{A}$  &  $\vec{B}$  is 8N such that resultant is perpendicular to the  $\vec{A}$ . Find magnitude of  $\vec{A}$  &  $\vec{B}$ . Also find  $\frac{A}{B}$ .

Sol<sup>n</sup>



$$\vec{A} + \vec{B} = \vec{C}$$

$$8^2 + x^2 = (16-x)^2$$

$$\text{Solve } x = 6$$

$$A = 6$$

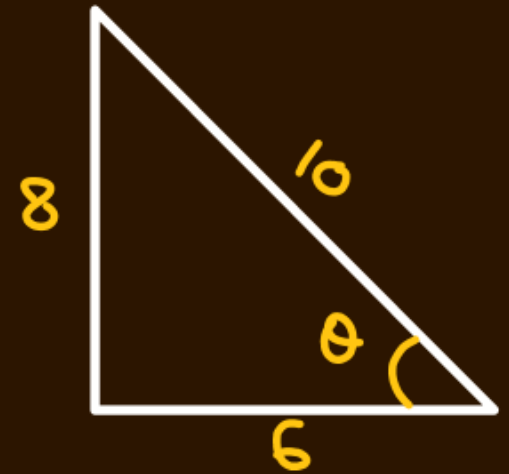
$$B = 16-x = 10$$

⑤ find angle b/w  $\vec{A}$  &  $\vec{B}$

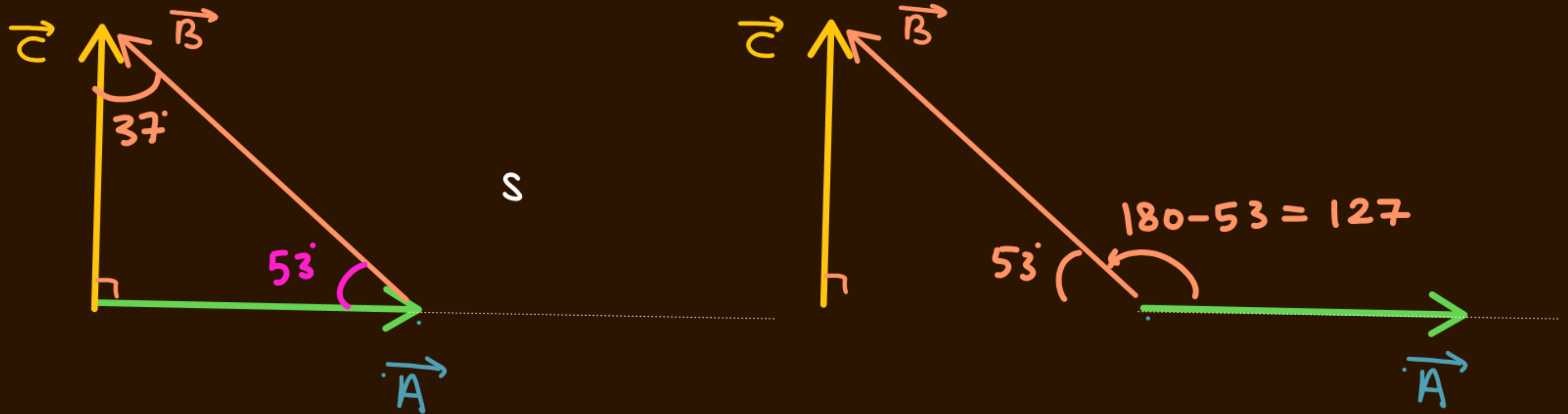
$$\tan \theta = \frac{8}{6}$$

$$\tan \theta = \frac{4}{3}$$

$$\theta = 53^\circ$$



$$\underline{\text{Ans}} = 180 - 53 = \underline{127}$$



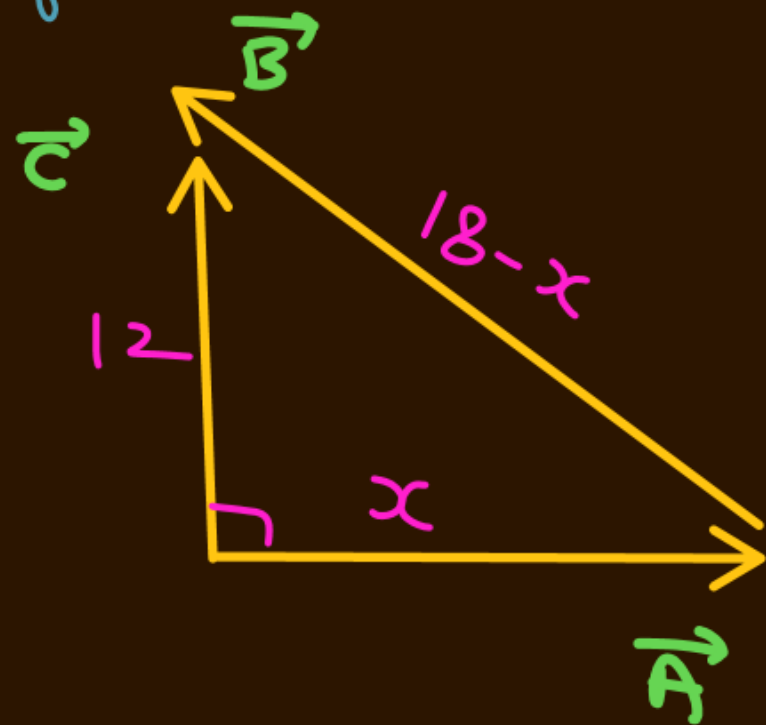
$$\text{Angle b/w } \vec{A} \text{ \& } \vec{B} = 180 - 53 = 127^\circ$$

$$\text{Angle b/w } \vec{A} \text{ \& } \vec{C} = 90^\circ$$

$$\text{" " } \vec{B} \text{ \& } \vec{C} = 37^\circ$$

Q Sum of the magnitude of  $\vec{A}$  &  $\vec{B}$  is  $18\text{N}$ . If magnitude of resultant of  $\vec{A}$  &  $\vec{B}$  is  $12\text{N}$ . Such that resultant is perpendicular to the  $\vec{A}$ . Find magnitude of  $\vec{A}$  &  $\vec{B}$ . Also find  $\frac{A}{B}$ .

Sol<sup>n</sup>



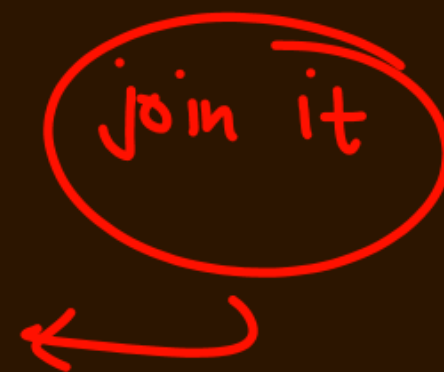
$$(12)^2 + x^2 = (18 - x)^2$$

$$x = 5$$

$$A = 5$$
$$B = 13$$

$$12^2 + 5^2 = 13^2$$

- KPP-08 (vector)  
Under making  
if i upload  
solve it on Sunday



**THANK**  
**YOU**