

By - Saleem Ahmed Sir



KPP Vector Pya Discussion



If
$$\vec{A} = (2\hat{\imath} + 3\hat{\jmath} - \hat{k})$$
m and $\vec{B} = (\hat{\imath} + 3\hat{\jmath} + 2\hat{k})$ m.

The magnitude of component of vector \vec{A} along vector \vec{B} will be $\underline{2}$ m.

[JEE Main 2022]

Aceso
$$\Rightarrow \frac{\vec{A} \cdot \vec{B}}{\vec{B}} = \frac{2 + 9 - 2}{\sqrt{1+}} = \frac{9}{\sqrt{14}} = \frac{9}{3.8} \approx 2.36$$



If the projection of
$$2\hat{i} + 4\hat{j} - 2\hat{k}$$
 on $\hat{i} + 2\hat{j} + \alpha\hat{k}$ is zero. Then, the value of α will be.

[JEE Main 2022]

(Pw)

Which of the following relation is true for two unit vectors \hat{A} and \hat{B} making an angle θ to each other?

[JEE Main 2022]

(1)
$$|\hat{A} + \hat{B}| = |\hat{A} - \hat{B}| \tan \frac{\theta}{2}$$

(2)
$$|\hat{A} - \hat{B}| = |\hat{A} + \hat{B}| \tan \frac{\theta}{2}$$

(3)
$$|\hat{A} + \hat{B}| = |\hat{A} - \hat{B}| \cos \frac{\theta}{2}$$

(4)
$$|\hat{A} - \hat{B}| = |\hat{A} + \hat{B}| \cos \frac{\theta}{2}$$



Two vectors \vec{A} and \vec{B} have equal magnitude. If magnitude of $\vec{A} + \vec{B}$ is equal to two times the magnitude of $\vec{A} - \vec{B}$, then the angle between \vec{A} and \vec{B} will be:

[JEE Main 2022]

$$(1) \quad \sin^{-1}\left(\frac{3}{5}\right)$$

$$(2) \quad \sin^{-1}\left(\frac{1}{3}\right)$$

(3)
$$\cos^{-1}\left(\frac{3}{5}\right)$$

(4)
$$\cos^{-1}\left(\frac{1}{3}\right)$$

$$A = B = X$$

$$|A + B| = 2|A - B|$$

$$A^{2} + B^{2} + 2 AB \cos \theta$$

$$X^{2} + 3C^{2} + 2 X^{2} \cos \theta = 4(X^{2} + X^{2} - 2 X^{2} \cos \theta)$$

$$2 + 2 \cos \theta = 4(2 - 2 \cos \theta)$$

$$10 \cos \theta = 6$$

$$\cos \theta = \frac{C}{10} = \frac{3}{10}$$



Vectors $a\hat{i} + b\hat{j} + \hat{k}$ and $2\hat{i} - 3\hat{j} + 4\hat{k}$ are perpendicular to each other when 3a + 2b = 7, the ratio of a to b is x/2. The value of x is

$$2a - 3b + 4 = 0$$

$$2a - 3b + 4 = 0$$

$$2a - 3b + 4 = -4$$

$$6a - 9b = -12$$

$$-6a + 4b = -14$$

$$-13b = -26$$

$$x = 1$$



 \vec{A} is a vector quantity such that $|\vec{A}| = \text{non zero}$ constant. Which of the following expression is true for \vec{A} ?

[JEE Main 2022]

$$\vec{A} \cdot \vec{A} = 0$$

$$\vec{A} \times \vec{A} < 0$$

$$(3) \vec{A} \times \vec{A} = 0$$

$$(4) \vec{A} \times \vec{A} > 0$$



If two vectors
$$\vec{P} = \hat{i} + 2m\hat{j} + m\hat{k}$$
 and

$$\vec{Q} = 4\hat{i} - 2\hat{j} + m\hat{k}$$
 are perpendicular to each other.

Then, the value of m will be:

[24 January 2023 - Shift 2]

$$(1)$$
 1

$$(2) -1$$

$$(3) -3$$

$$(4)$$
 2



If
$$\vec{P} = 3\hat{i} + \sqrt{3}\hat{j} + 2\hat{k}$$
 and $\vec{Q} = 4\hat{i} + \sqrt{3}\hat{j} + 2.5\hat{k}$
then, The unit vector in the direction of $\vec{P} \times \vec{Q}$ is $\left(\sqrt{3}\hat{i} + \hat{j} - 2\sqrt{3}\hat{k}\right)$. The value of x is:

[25 January 2023 - Shift 1]

$$\overrightarrow{P} \times \overrightarrow{B} = \sqrt{=}$$

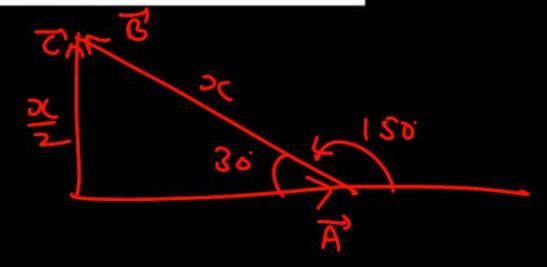
$$\Rightarrow \sqrt{3+1+12} = \sqrt{16} = 4$$



The resultant of two vectors \vec{A} and \vec{B} is perpendicular to \vec{A} and its magnitude is half that of \vec{B} . The angle between vectors \vec{A} and \vec{B} is



[09 April 2024 - Shift 2]





What will be the projection of vector $\vec{A} = \hat{i} + \hat{j} + \hat{k}$ on vector $\vec{B} = \hat{i} + \hat{j}$?

[JEE Main 2021]

(1)
$$\sqrt{2(\hat{i}+\hat{j}+\hat{k})}$$
 (2) $2(\hat{i}+\hat{j}+\hat{k})$



Two forces having magnitude A and A/2 are perpendicular to each other. The magnitude of their resultant is:

[08 April 2023 - Shift 1]

$$(1) \quad \frac{\sqrt{5}A}{4}$$

$$(2) \quad \frac{\sqrt{5} A}{2}$$

(3)
$$\frac{5A}{2}$$

(4)
$$\frac{\sqrt{5} A^2}{2}$$

$$\sqrt{\left(A\right)^{2}+\left(\frac{A}{2}\right)^{2}}$$



When vector $\vec{A} = 2\hat{\imath} + 3\hat{\jmath} + 2\hat{k}$ is subtracted from vector \vec{B} , it gives a vector equal to $2\hat{\jmath}$. Then the magnitude of vector \vec{B} will be:

(1)
$$\sqrt{5}$$

$$(2)$$
 3

(3)
$$\sqrt{6}$$

[11 April 2023 - Shift 2]

$$B - (2i + 3j + 2k) = 2i$$
 $B = 2i + 5j + 2k$



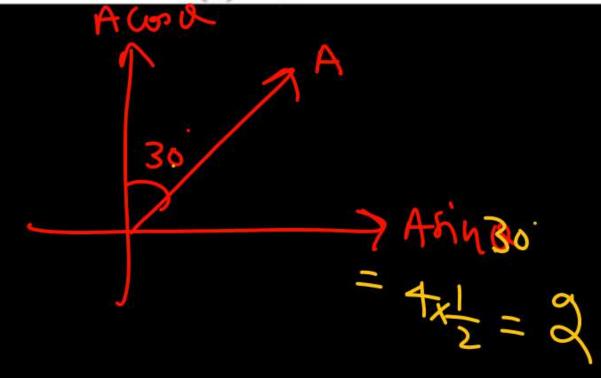
A vector in x - y plane makes an angle of 30° with y-axis. The magnitude of y-component of vector is $2\sqrt{3}$. The magnitude of x-component of the vector will be:

[15 April 2023 - Shift 1]

(1)
$$1/\sqrt{3}$$

$$(2)$$
 6

$$(4) \sqrt{3}$$



$$A \cos \theta = 2\sqrt{3}$$
 $A \cos 30 = 2\sqrt{3}$
 $A \int_{2}^{3} = 2\sqrt{3}$
 $A = 4$



If two vectors \vec{A} and \vec{B} having equal magnitude R are inclined at an angle θ , then.

[31 January 2024 - Shift 2]

$$(1) \quad |\vec{A} - \vec{B}| = \sqrt{2R} \sin\left(\frac{\theta}{2}\right)$$

$$(2) \quad |\vec{A} + \vec{B}| = 2R \sin\left(\frac{\theta}{2}\right)$$

$$(3) \quad |\vec{A} + \vec{B}| = 2R \cos\left(\frac{\theta}{2}\right)$$

$$(4) \quad |\vec{A} - \vec{B}| = 2R \cos\left(\frac{\theta}{2}\right)$$



A vector has magnitude same as that of $\vec{A} = 3\hat{i} + 4\hat{j}$ and is parallel to $\vec{B} = 4\hat{i} + 3\hat{j}$. The x and y components of this vector in first quadrant are x and 3 respectively where $x = \underline{4}$.

[30 January 2024 - Shift 2]

$$\overrightarrow{P} = 5 \cdot \widehat{B} = 5 \left(\frac{4\widehat{\lambda} + 3\widehat{1}}{5} \right)$$

$$\overrightarrow{P} = 4\widehat{\lambda} + 3\widehat{1}$$

$$\lambda = 4$$



Two forces $\vec{F_1}$ and $\vec{F_2}$ are acting on a body. One force has magnitude thrice that of the other force and the resultant of the two forces is equal to the force of larger magnitude. The angle between $\vec{F_1}$

and
$$\vec{F}_2$$
 is $\cos^{-1}\left(\frac{1}{n}\right)$. The value of $|n|$ is _____.

[04 April 2024 - Shift 1]

$$x, 3x, 3x$$

$$C = \sqrt{A^2 + B^2 + 2 A B CON B}$$

$$-x^2 = 6x^2 CON B$$

$$Con b = -\frac{1}{6}$$



The angle between vector \vec{Q} and the resultant of

$$(2\vec{Q}+2\vec{P})$$
 and $(2\vec{Q}-2\vec{P})$ is: [05 April 2024 - Shift 1]

(1)
$$\tan^{-1} \frac{(2\vec{Q} - 2\vec{P})}{2\vec{Q} + 2\vec{P}}$$

- (3) $tan^{-1}(P/Q)$
- (4) $tan^{-1}(2Q/P)$



If
$$\vec{a}$$
 and \vec{b} makes an angle $\cos^{-1}\left(\frac{5}{9}\right)$ with each other, then $|\vec{a}+\vec{b}|=\sqrt{2}\,|\vec{a}-\vec{b}|$ for $|\vec{a}|=n\,|\vec{b}|$. The integer value of n is 3 . $\alpha=n\,|\vec{b}|$ [09 April 2024 - Shift 1]

$$a^{2}+b^{2}+aab con a = 2 (a^{2}+b^{2}-2ab con a)$$
 $n^{2}b^{2}+b^{2}+2n.b^{2} cos a = 2 (n^{2}b^{2}+b^{2}-2nb^{2} cos a)$
 $\frac{h^{2}+1}{9}+2h\frac{5}{9}=2h^{2}+2-4h\frac{5}{9}$

$$n^{2}+1-\frac{30}{9}n=0$$

$$9n^{2}-30n+9=0$$

$$3n^{2}-10n+3=0$$

$$3n^{2}-9n-n+3=0$$

$$3n(n-3)-1(n-3)=0$$

$$n=3, n=\frac{1}{3}$$



Three forces $F_1 = 10 \text{ N}$ $F_2 = 8 \text{ N}$, $F_3 = 6 \text{ N}$ are acting on a particle of mass 5 kg. The forces F_2 and F_3 are applied perpendicularly so that particle remains at rest. If the force F_1 is removed, then the acceleration of the particle is:

[12 April 2023 - Shift 1]

- (1) 7 ms^{-2} (2) 0.5 ms^{-2}
- (3) 4.8 ms^{-2} (4) 2 ms^{-2}

$$\alpha = \frac{F_{not}}{m}$$



Two particles are located at equal distance from origin. The position vectors of those are represented by $\overline{A} = 2\hat{i} + 3n\hat{j} + 2\hat{k}$ and $\overline{B} = 2\hat{i} - 2\hat{j} + 4p\hat{k}$, respectively. If both the vectors are at right angle to each other, the value of n^{-1} is _____.

[23 Jan. 2025 - Shift 1]



Match List I with List II.

[JEE Main 2021]

List I		List II.	
(a)	$\vec{C} - \vec{A} - \vec{B} = 0$ $\vec{C} = \vec{A} + \vec{B}$	(i)	\overrightarrow{A} \overrightarrow{C} \overrightarrow{B} \overrightarrow{A} \overrightarrow{C} \overrightarrow{B}
(b)	$\vec{A} - \vec{C} - \vec{B} = 0$ $\vec{A} = \vec{C} + \vec{E}$	(ii)	\overrightarrow{C} \overrightarrow{B} $\overrightarrow{A} + \overrightarrow{B} + \overrightarrow{C} = 0$
(c)	$\vec{B} - \vec{A} - \vec{C} = 0$	(iii)	\vec{A} \vec{C} \vec{B} \vec{B} \vec{A} \vec{B} \vec{A}
(d)	$\vec{A} + \vec{B} = -\vec{C}$	(iv)	\vec{C} \vec{B} \vec{A} \vec{A} \vec{A}

Choose the correct answer from the options given below:

(1) (a)
$$\rightarrow$$
(iv), (b) \rightarrow (i), (c) \rightarrow (iii), (d) \rightarrow (ii)

(2) (a)
$$\rightarrow$$
(iv), (b) \rightarrow (iii), (c) \rightarrow (i), (d) \rightarrow (ii)

$$()$$
 (a) \rightarrow (iii), (b) \rightarrow (ii), (c) \rightarrow (iv), (d) \rightarrow (i)

(4)
$$(a)\rightarrow(i), (b)\rightarrow(iv), (c)\rightarrow(ii), (d)\rightarrow(iii)$$

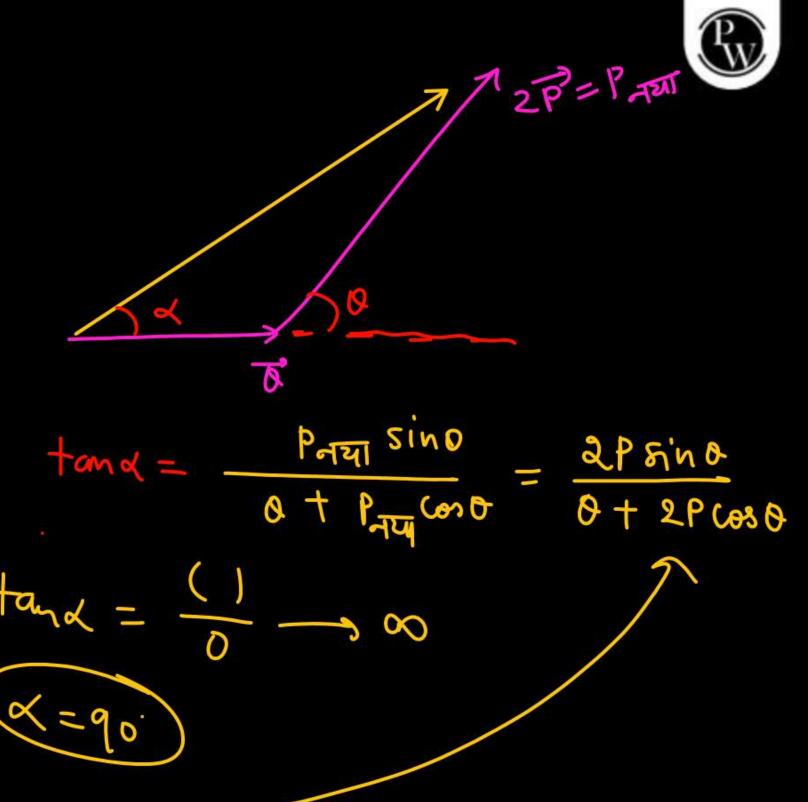
The sum of two \vec{P} and \vec{Q} is \vec{R} such that $|\vec{R}| = |\vec{P}|$. The angle θ (in degree) that the resultant of $2\vec{P}$ and \vec{Q} will make \vec{Q} is:

$$P + 0 = R$$

$$R = \sqrt{P^2 + 0^2 + 2 \cdot 90 \cdot 000} = P$$

$$0^2 + 2 \cdot 90 \cdot 000 = 0$$

$$0 + 2 \cdot 90 \cdot 000 = 0$$



Ans: (90)



If \vec{A} and \vec{B} are two vectors satisfying the relation $\vec{A} \cdot \vec{B} = |\vec{A} \times \vec{B}|$. Then the value of $|\vec{A} - \vec{B}|$ will be:

[JEE Main 2021]

(1)
$$\sqrt{A^2 + B^2}$$

(2)
$$\sqrt{A^2 + B^2} + \sqrt{2}AB$$

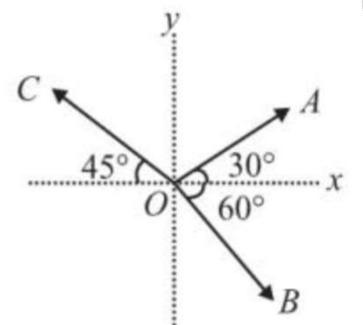
(3)
$$\sqrt{A^2 + B^2 + 2AB}$$

(4)
$$\sqrt{A^2 + B^2} - \sqrt{2}AB$$



The magnitude of vectors \overrightarrow{OA} , \overrightarrow{OB} and \overrightarrow{OC} in the given figure are equal. The direction of $\overrightarrow{OA} + \overrightarrow{OB} - \overrightarrow{OC}$ with x-axis will be:

[JEE Main 2021]



$$\tan^{-1}\frac{\left(1-\sqrt{3}-\sqrt{2}\right)}{\left(1+\sqrt{3}+\sqrt{2}\right)}$$

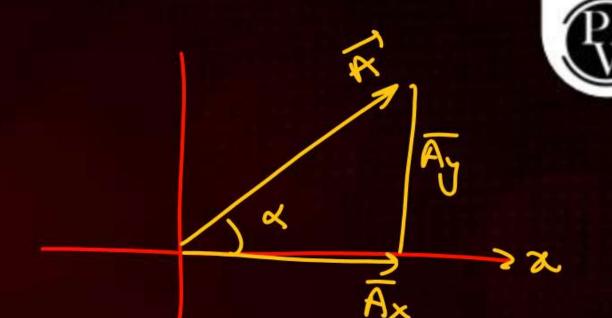
(2)
$$\tan^{-1} \frac{\left(\sqrt{3} - 1 + \sqrt{2}\right)}{\left(1 + \sqrt{3} - \sqrt{2}\right)}$$

(3)
$$\tan^{-1} \frac{\left(\sqrt{3} - 1 + \sqrt{2}\right)}{\left(1 - \sqrt{3} + \sqrt{2}\right)}$$

(4)
$$\tan^{-1} \frac{\left(1 + \sqrt{3} - \sqrt{2}\right)}{\left(1 - \sqrt{3} - \sqrt{2}\right)}$$

$$\frac{\partial \vec{A} + \partial \vec{B}^2 - \partial \vec{C}}{= \alpha \left(\frac{\sqrt{3}}{2} + \frac{1}{2} + \frac{\sqrt{2}}{2} \right) \hat{\lambda}}$$

$$+ \alpha \left(\frac{1}{2} - \frac{\sqrt{3}}{2} - \frac{\sqrt{3}}{2} \right) \hat{\lambda}$$



- A = Axi + Ayj

XI-Axis & the argle of =) tand = Ax

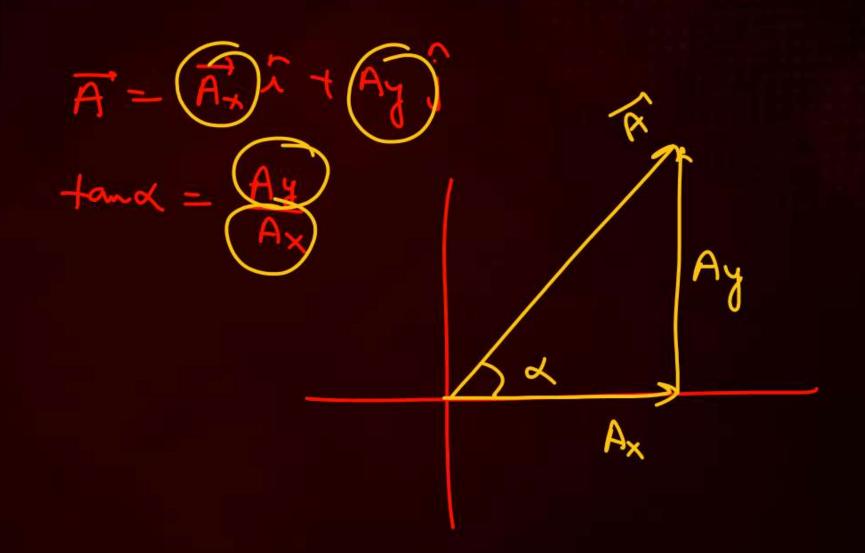
tand = Ay

 $x \cos \alpha = \frac{Ax}{\sqrt{A^2 + A^2}}$



$$\overline{A} = 3\overline{\lambda} + 4\overline{j}$$

$$\tan \alpha = \frac{4}{5}$$





$$A = 10$$
 $B = 6$
 $C = 3$
 $A + B - C$
 $b + 6 - 3$



Two vectors \vec{P} and \vec{Q} have equal magnitudes. If the magnitude of $\vec{P} + \vec{Q}$ is *n* times the magnitude of

 $\vec{P} - \vec{Q}$, then angle between \vec{P} and \vec{Q} is:

(JEE Main 2021)

$$(1) \quad \sin^{-1}\left(\frac{n-1}{n+1}\right)$$

$$(2) \quad \cos^{-1}\left(\frac{n-1}{n+1}\right)$$

(3)
$$\sin^{-1}\left(\frac{n^2-1}{n^2+1}\right)$$

(3)
$$\sin^{-1}\left(\frac{n^2-1}{n^2+1}\right)$$
 (4) $\cos^{-1}\left(\frac{n^2-1}{n^2+1}\right)$

$$\int P^{2}+a^{2}+2pa\omega = n \int P^{2}+a^{2}-2pa\omega = n^{2} \left(x^{2}+x^{2}+2x^{2}\omega + n^{2}\right)$$



Two vectors \vec{X} and \vec{Y} have equal magnitude. The magnitude of $(\vec{X} - \vec{Y})$ is n times the magnitude of $(\vec{X} + \vec{Y})$. The angle between \vec{X} and \vec{Y} is:

JEE Main 2021

(1)
$$\cos^{-1}\left(\frac{-n^2-1}{n^2-1}\right)$$
 (2) $\cos^{-1}\left(\frac{n^2-1}{-n^2-1}\right)$

(3)
$$\cos^{-1}\left(\frac{n^2+1}{-n^2-1}\right)$$
 (4) $\cos^{-1}\left(\frac{n^2+1}{n^2-1}\right)$

$$\int x_{1}^{2} + x_{2}^{2} - 3xx\cos\theta = u_{3}(3+3\cos\theta)$$

$$1 - \cos\theta = u_{3}(1+\cos\theta)$$

$$1 - \cos\theta = u_{5}(1+\cos\theta)$$

$$1 - \cos\theta = u_{5}(1+\cos\theta)$$

$$1 - \cos\theta = u_{5}(1+\cos\theta)$$



The angle between vector (\vec{A}) and $(\vec{A} - \vec{B})$ is:

[JEE Main 2021]

$$(1) \quad \tan^{-1} \left(\frac{-\frac{B}{2}}{A - B\frac{\sqrt{3}}{2}} \right)$$

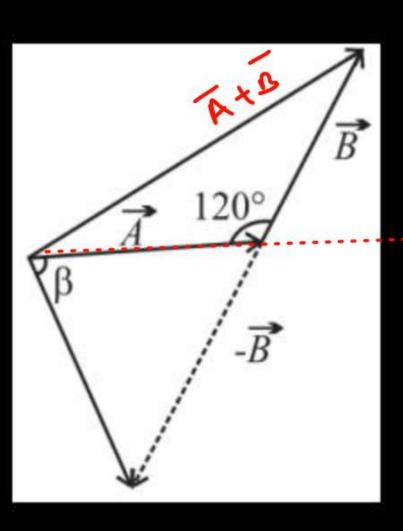
(2)
$$\tan^{-1}\left(\frac{A}{0.7B}\right)$$

(3)
$$\tan^{-1} \left(\frac{\sqrt{3}B}{2A - B} \right)$$

(4)
$$\tan^{-1} \left(\frac{B \cos \theta}{2 - B \sin \theta} \right)$$

$$\overrightarrow{R} = \overrightarrow{A} - \overrightarrow{B}$$
 ते वीय Ayla =) 60 $\overrightarrow{R} = \overrightarrow{A} - \overrightarrow{B}$

$$= \frac{BJ_3}{2A-R}$$

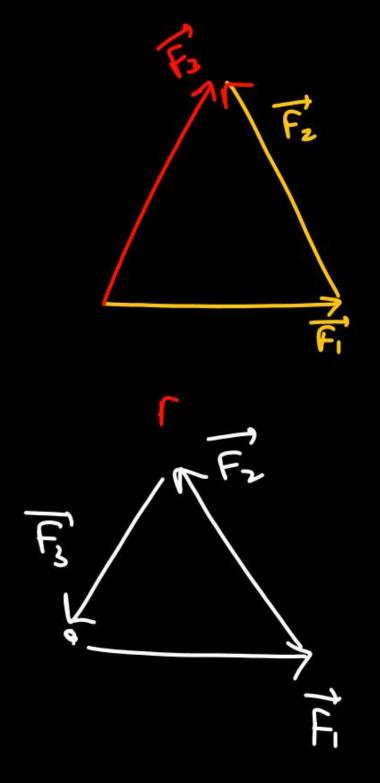


Statement I: If three forces $\vec{F_1}$, $\vec{F_2}$ and $\vec{F_3}$ are represented by three sides of a triangle and $\vec{F_1} + \vec{F_2} = \vec{F_3}$, then these three forces are concurrent forces and satisfy the condition for equilibrium.

Statement II: A triangle made up of three forces \vec{F}_1 , \vec{F}_2 and \vec{F}_3 as its sides taken in the same order, satisfy the condition for translatory equilibrium. In the light of the above statements, choose the most appropriate answer from the options given below:

[JEE Main 2021]

- (1) Statement-I is false but Statement-II is true
- (2) Statement-I is true but Statement-II is false
- (3) Both Statement-I and Statement-II are false
- (4) Both Statement-I and Statement-II are true











- correction

Fi+F2 = -F3



Statement I: If three forces \vec{F}_1 , \vec{F}_2 and \vec{F}_3 are represented by three sides of a triangle and $\vec{F}_1 + \vec{F}_2 = \vec{F}_3$, then these three forces are concurrent forces and satisfy the condition for equilibrium.

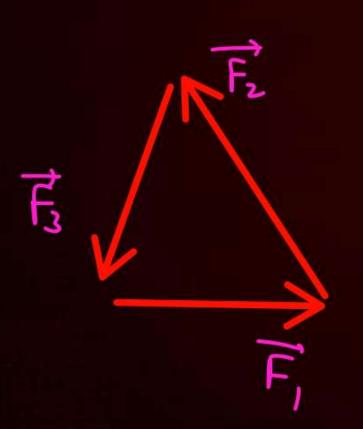
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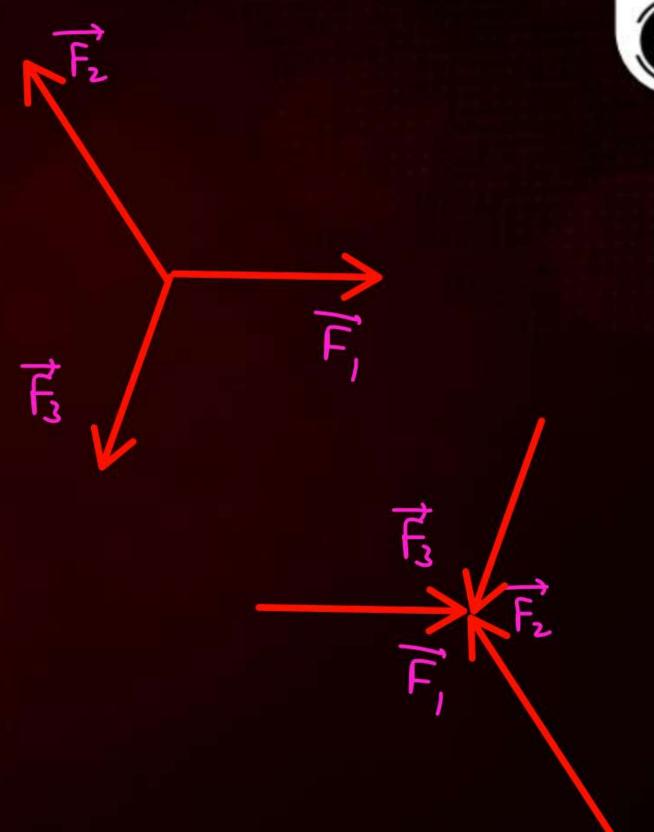
[JEE Main 2021]

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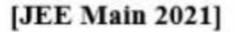


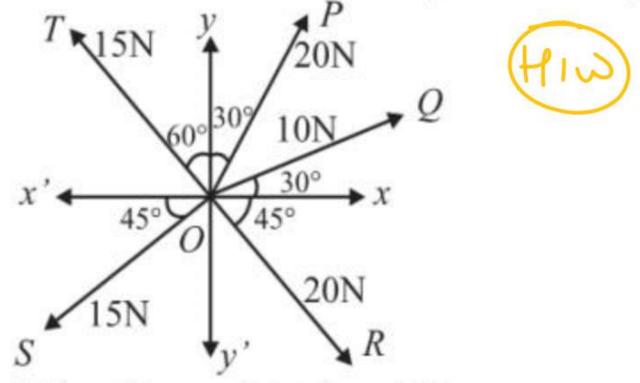




The resultant of these forces \overrightarrow{OP} , \overrightarrow{OQ} , \overrightarrow{OR} , \overrightarrow{OS} and \overrightarrow{OT} is approximately N.

[Take $\sqrt{3} = 1.7$, $\sqrt{2} = 1.4$ Given $\hat{\imath}$ and $\hat{\jmath}$ unit vectors along x, y axis].



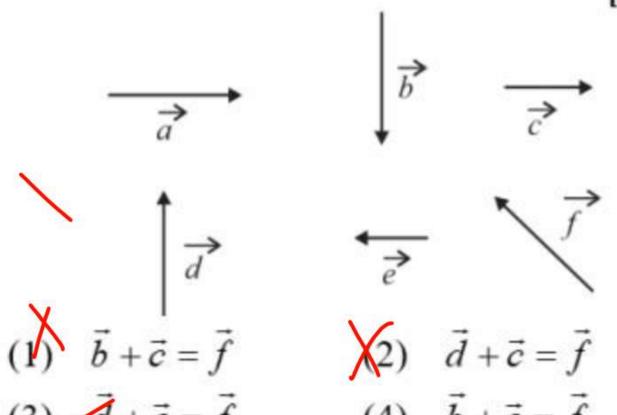


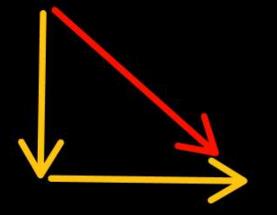
- (1) $9.25\hat{\imath} + 5\hat{\jmath}$
- (2) $3\hat{\imath} + 15\hat{\jmath}$
- (3) $2.5\hat{i} 14.5\hat{j}$
- (4) $-1.5\hat{\imath} 15.5\hat{\jmath}$



Six vectors, \vec{a} through \vec{f} fhave the magnitudes and directions indicated in the figure. Which of the following statements is true?

[NEET - 2010]



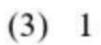




If a unit vector is represented by $0.5\hat{i} - 0.8\hat{j} + c\hat{k}$ then the value of c is:

[NEET - 1999]

(1)
$$\sqrt{0.01}$$



$$(4) \sqrt{0.39}$$

$$\sqrt{(s)^2+(8)^2+(c)^2}=1$$



If the magnitude of sum of two vectors is equal to the magnitude of difference of the two vectors, the angle between these vectors is:

[NEET-I, 2016]

45°

(2) 180°

(3) 0°

(4) 90°



The vectors \vec{A} and \vec{B} are such that $|\vec{A} + \vec{B}| = |\vec{A} - \vec{B}|$. The angle between the two vectors is:

NEET - 2006, 1996, 1991]

- (1) 45° (2) 90°
- (3) 60° (4) 75°



If $|\vec{A} + \vec{B}| = |\vec{A}| + |\vec{B}|$ then angle between A and B will be:

[NEET - 2001]

90°

(2) 120°

(3) 0°

(4) 60°

$$A^2 + B^2 + 2 AB CORO = A^2 + B$$

$$CORO = 1$$

$$CORO = 1$$



The magnitude of vectors \vec{A} , \vec{B} and \vec{C} are 3, 4 and 5 units respectively. If $\vec{A} + \vec{B} = \vec{C}$, the angle between \vec{A} and \vec{B} is:

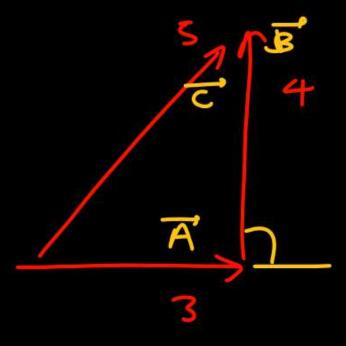
[NEET - 1988]

(1) $\pi/2$

(2) $\cos^{-1}(0.6)$

(3) $tan^{-1}(7/5)$

(4) $\pi/4$





A particle starting from the origin (0, 0) moves in a straight line in the (x, y) plane. Its coordinates at a later time are $(\sqrt{3}, 3)$. The path of the particle makes with the x-axis an angle of

[NEET - 2007]

(0,0) Slope =
$$\frac{\sqrt{3}-0}{3-0}$$
= $\sqrt{3}$



