



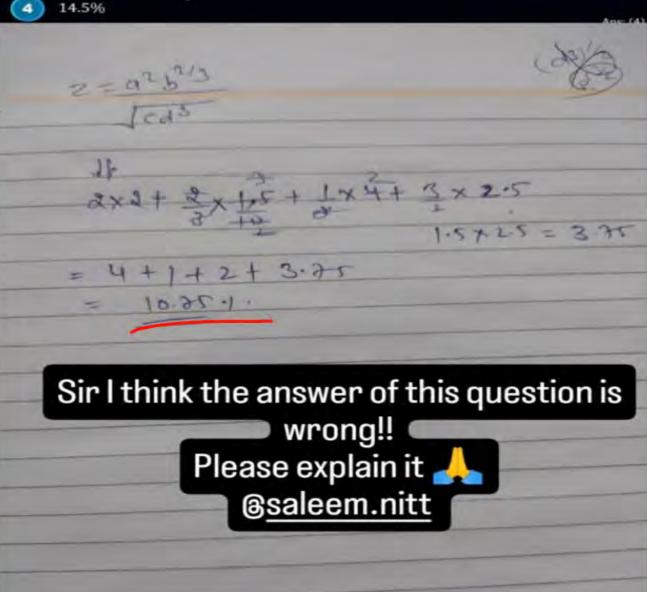
# Todays Goal

### Error Questions Practice

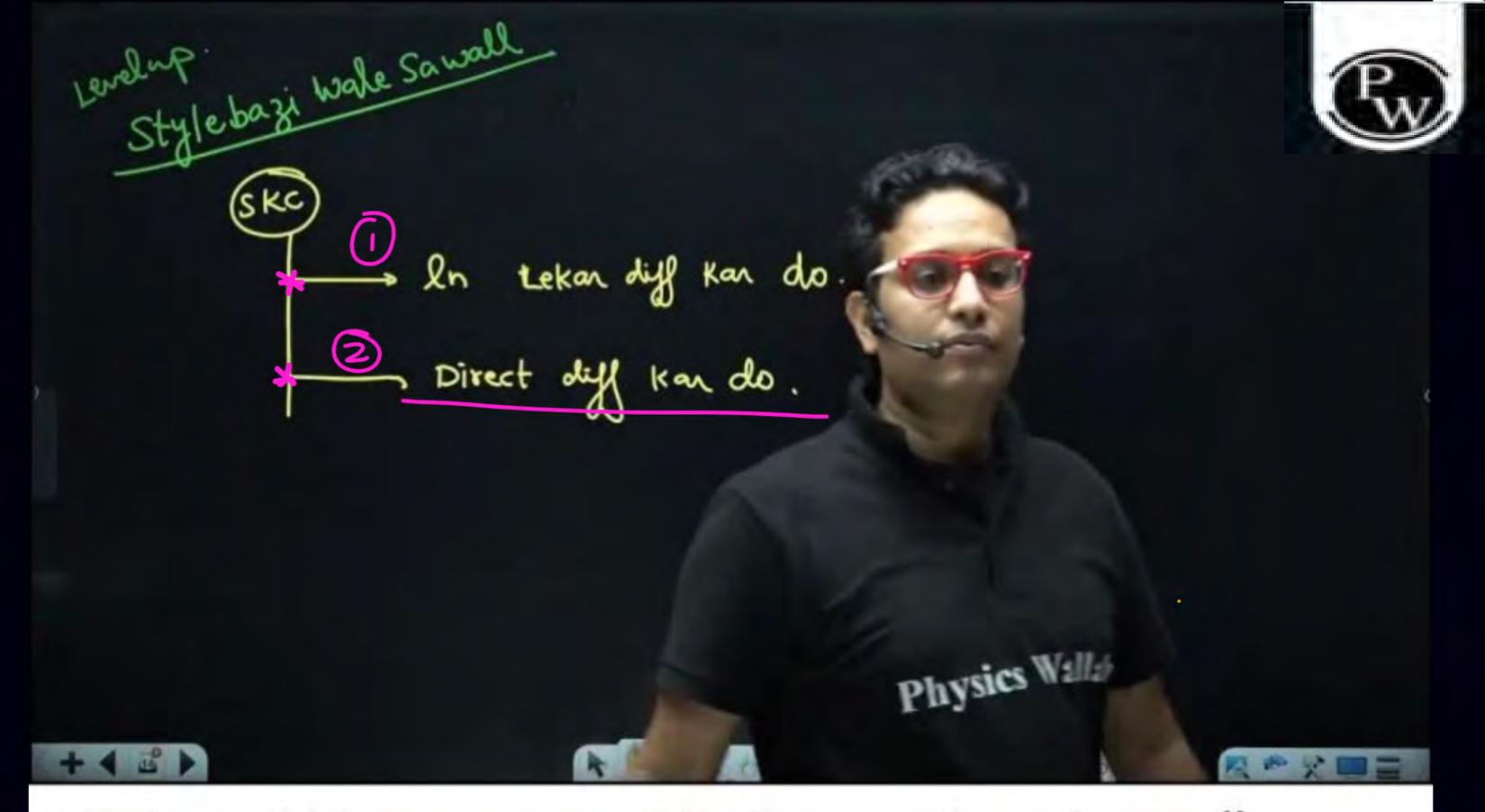


A physical quantity z depends on four observables a, b, c and d, as  $z = \frac{a^2b^3}{\sqrt{c}a^3}$ percentages of error in the measurement of a, b, c and d are 2%, 1.5%, 1% and 2.5% respectively. The percentage of error in z is: [Main Sep. 05, 2020 (I)]

- 12.25%
- 16.5%
- 13.5%
- 14.5%







Units and Measurements 09 : Propagation of error

Levelup. Stylebazi wale Sawall Lekan digf Kan do... Kan do. Direct



### distance - speed x time



B A particle is moving on a straight line with speed (100 ± .1) m/s

find distance brawl by the particle.

$$\frac{501}{t = 100}$$
 $x = 0 + 1000$ 

$$x = (1000 \pm 51)$$

$$x = vt$$

$$\frac{1000}{1000} = \frac{1}{100} + \frac{5}{10} = \frac{1}{1000} + \frac{5}{100}$$

$$\Delta x = 1 + \frac{5000}{100} = 51$$

\* sobse pahle error ko bhool jao. & solve

\* Fix error pan attack

$$y = \frac{3b^{3}}{5t^{3}}$$

$$\frac{34}{3} = \frac{30b}{3} + 40c$$

+ 307

& A particle is moving in a straight line path & travel

find its velocity.

$$v = \frac{s}{t}$$

$$\frac{\Delta v}{v} = \frac{\Delta s}{s} + \frac{\Delta t}{t}$$

$$\frac{\sqrt{2}}{\sqrt{2}} = \frac{10}{2}$$

Relative error in 
$$V = \frac{3V}{V} = \frac{3}{10}$$

$$Q = \frac{a^2b^3}{c^4}$$

$$b = 20 \pm \cdot 3$$

$$C = 10 \pm .4$$

$$= 2x \frac{-1}{10} + 3x \frac{-3}{20} + 4x \frac{-4}{10}$$

$$= \frac{2}{100} + \frac{9}{200} + \frac{16}{100}$$

$$\frac{\Delta x}{x} = \frac{45}{200} = Relative error.$$

$$\frac{\Delta x}{31} \times 100 - \frac{45}{2} = 22.5 \%$$





$$Q \qquad x = \frac{a^2 b^3}{c^4}$$

$$x = \frac{10^2 \times (20)^3}{(10)^4} = \frac{800000}{10000} = 80$$

$$C = lo \pm \cdot 4$$

$$x = (80 \pm \Delta x)$$

$$\frac{5x}{5c} = \frac{25a}{a} + \frac{345}{5} + \frac{45c}{c}$$

$$\frac{\Delta x}{80} = 2\left(\frac{-1}{10}\right) + 3\left(\frac{-3}{20}\right) + 4\left(\frac{-4}{10}\right)$$

$$\frac{\Delta \chi}{80} = \frac{45}{200} \qquad \Delta \chi = 18$$

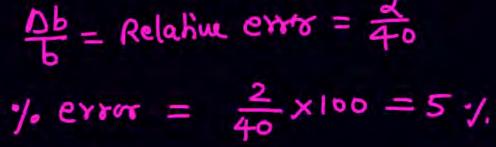
$$y = \frac{ab^2}{C^3}$$

$$= \frac{ab^2}{C^3}$$

### where

- 1) Find 1/0 error in a  $\frac{501}{10} \times \frac{1}{10} \times 100 = \frac{1}{1}$
- 2) Find relative error in a  $\frac{\Delta a}{a} = \frac{1}{10} = \frac{1}{100}$

# 3) Find relative error à percentage error in b





$$\frac{\Delta C}{C} = \frac{.4}{40}$$
 % error in  $C' = \frac{.4}{20} \times 100 = 2\%$ 

\*\*\*

4) Find relative error and 1/0 error in y

$$\frac{5y}{y} = \frac{1}{10} + 2x \frac{2}{40} + 3x \cdot \frac{4}{20} = \frac{17}{100}$$



$$y = \frac{ab^2}{C^3}$$

# (5) find value of y in proper error limit



soi crrer Bhod jaw

where

$$y = \frac{10 \times (40)^{2}}{(20)^{3}} = \frac{16000}{8000} = 2$$

Any

$$\frac{\Delta y}{2} = \frac{1}{10} + 2x \frac{2}{40} + 3x \cdot \frac{4}{20} = .17$$

$$Q = \frac{a^2 \sqrt{b}}{c^3}$$

$$a = 10 \pm .1$$
 $b = 100 \pm .4$ 
 $c = 10 \pm .2$ 

find Value of y in proper limit



$$\frac{Sol}{y} = \frac{100 \times \sqrt{100}}{(10)^3} = 1$$



$$\frac{\Delta y}{y} = \frac{2}{100} \times \frac{1}{10} + \frac{1}{2} \cdot \frac{4}{100} + \frac{3}{2} \times \frac{2}{10}$$

$$\Delta y = \frac{82}{1000} = .08 - .1$$

Q 
$$R_{1}=(30\pm .2)\Lambda$$
  
 $R_{2}=(60\pm .5)\Lambda$ 

1) find Reg when resistance one in series.

Soi Req = 
$$R_1+R_2=90$$
  
 $Req = (90 \pm 07)$ 

(b) when R, & R, one in parallel.

$$\frac{1}{Req} = \frac{1}{R_1} + \frac{1}{R_2}$$

$$-\frac{1}{R_{eq}^2}$$
 dReq =  $-\frac{1}{R_1^2}$  dR,  $-\frac{1}{R_2^2}$  dR,

$$\frac{\Delta Req}{R_{eq}^2} = \frac{\Delta R_1}{R_1^2} + \frac{\Delta R_2}{R_2^2}$$

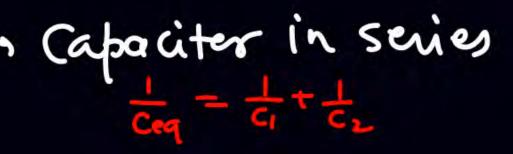


Kam Ka debba

$$\frac{1}{3^2} d3 = \frac{1}{x^2} dx + \frac{1}{y^2} dy$$

$$\frac{\Delta 3}{3^2} = \frac{\Delta x}{x^2} + \frac{\Delta y}{y^2}$$

Resis. in parallel



$$\frac{1}{Req} \Delta Req = \frac{1}{R_1^2} \Delta R_1 + \frac{1}{R_2^2} \Delta R_2$$

$$\frac{\Delta Reg}{(7.5)^2} = \frac{\cdot 1}{100} + \frac{\cdot 2}{900}$$

$$\frac{dy}{dy} = x^2$$

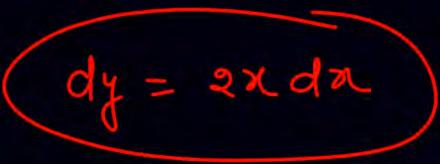
$$\frac{dy}{dy} = 2x dx$$

$$82 \quad 3 = x^{6}$$

$$dy = 6x^{5} dx$$

$$y = x^2$$

$$\frac{dx}{dx} = 2x$$





$$y = e^{x}$$
 $dy = e^{x} dx$ 

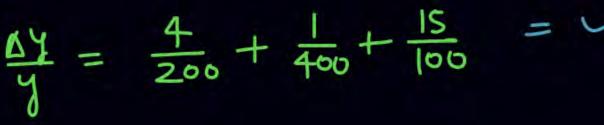
$$y = \frac{a^2b}{c^3}$$

Find relative error

$$\frac{\Delta y}{y} = \frac{2 \Delta \alpha}{a} + \frac{1}{4} + \frac{3 \Delta c}{b}$$

$$\frac{\Delta y}{y} = \frac{2 \times \cdot 2}{20} + \frac{\cdot 1}{40} + \frac{3 \times \cdot 5}{10}$$

$$\frac{47}{9} = \frac{4}{200} + \frac{15}{100} = \frac{15}{100}$$





$$\frac{\Delta y}{y} = \frac{2 \times 2}{20} + \frac{1}{40} + \frac{3 \times 5}{10}$$

$$\frac{\Delta y}{y} \times 100 = \frac{4}{2} + \frac{1}{4} + \frac{15}{5} = \sqrt{\frac{1}{2}}$$





A physical quantity z depends on four observables a, b, c and d, as  $z = \frac{a^2b^{\frac{3}{3}}}{\sqrt{c}d^3}$ . The percentages of error in the measurement of a, b, c and d are 2%, 1.5%, 4% and 2.5% respectively. The percentage of error in z is:

[Main Sep. 05, 2020 (I)]

$$\frac{ab}{\sqrt{c}d^{3}} = 2xxx + \frac{2}{3}x^{\frac{3}{2}} + \frac{1}{2}x4 + \frac{3}{2}x2.5 = \frac{10.75}{1}$$

$$\frac{a^{2}b^{2}|_{3}}{\sqrt{c}d^{3}} = 2x^{2} + \frac{2}{3}x^{2} + \frac{1}{2}x^{4} + 3x^{2}s$$

$$= 4 + 1 + 2 + 7 \cdot 5 - 14 \cdot 5$$

20. The energy of a system as a function of time t is given as E(t) = A<sup>2</sup>exp (-αt), where α = 0.2s<sup>-1</sup>. The measurement of A has an error of 1.25%. If the error in the measurement of time is 1.50%, the percentage error in the value of E(t) at t = 5 s is.

[JEE-Advance 2015]

एक निकाय की समय t पर ऊर्जा E(t) = A<sup>2</sup>exp (-αt) फलन द्वारा दी जाती है, जहाँ α = 0.2s<sup>-1</sup> है। A के मापन में

1.25% की प्रतिशत त्रुटि है। यदि समय के मान में 1.50% की त्रुटि है तब t = 5s पर E(t) के मान में प्रतिशत त्रुटि होगी।

Ans. 4

26. Two resistance are measured in ohm and is given

$$R_1 = 3\Omega \pm 1\%$$

$$R_2 = 6\Omega \pm 2\%$$

When they are connected in parallel, the percentage error in equivalent resistance is

- (1) 3% (2) 4.5%
- (3) 0.67% (4) 1.33%

Ans. (4)

6.

HIN

In an experiment, the percentage of error occurred in the measurement of physical quantities A, B, Cand D are 1%, 2%, 3% and 4% respectively. Then the maximum percentage of error in the

measurement of X, where  $X = \frac{A^2 B^{1/2}}{C^{1/3} D^3}$  will be:

NEET [2019]

1) 10% (2) 
$$\left(\frac{3}{13}\right)\%$$
  
3) 16% (4) -10%

$$(4) -10\%$$

7. In an experiment, four quantities a, b, c and d are measured with percentage error 1%, 2%, 3% and

4% respectively. Quantity P is calculated as

follows 
$$p = \frac{a^3b^2}{cd}$$
. % error in *P* is:

NEET [2013]

- (1) 7% (2) 4%
- (3) 14% (4) 10%

9. If the error in the measurement of radius of a sphere is 2%, then the error in the determination of volume of the sphere will be:

NEET [2008]

- (1) 8% (2) 2%
- (3) 4% (4) 6%

A metal wire has mass  $(0.4 \pm 0.002)$  g, radius  $(0.3 \pm 0.001)$  mm and length  $(5 \pm 0.02)$  cm. The maximum possible percentage error in the measurement of density will nearly be:

NEET [2023]

- (1) 1.6% (2) 1.4%
- (3) 1.2% (4) 1.3%

11. Taking into account of the significant figures, what is the value of 9.99 m - 0.0099 m?

NEET [2020]

- (1) 9.9801 m (2) 9.98 m
- (3) 9.980 m (4) 9.9 m

10. The area of a rectangular field (in m<sup>2</sup>) of length 55.3 m and breadth 25 m after rounding off the value for correct significant digits is:

NEET [2022]

- (1)  $138 \times 10^1$  (2) 1382
- (3) 1382.5 (4)  $14 \times 10^2$

The resistance R = V/i, where  $V = 100 \pm 5$  V and  $i = 10 \pm 0.2$  A. What is the total error in R?

Aug 77.

$$R = 10 \pm .7$$

$$R = \frac{V}{i} = \frac{100}{10} = 10$$

In Ohm's law experiment, the potential drop across a resistance was measured as V = 5.0 V and the current was measured as i = 2.00 A. Find the maximum permissible error in resistance.

The distance covered by a body in time  $(5.0 \pm 0.6)$  s is  $(40.0 \pm 0.4)$  m. Calculate the speed of the body. Also determine the percentage error in the speed.

(8.0 ± 1.04), 137.

13. Two resistance R<sub>1</sub> and R<sub>2</sub> are connected in (i) series and (ii) parallel. What is the equivalent resistance

Two resistance  $R_1$  and  $R_2$  are connected in (i) series and (ii) parallel. What is the equivalent resistance with limit of possible percentage error in each case of  $R_1 = 5.0 \pm 0.2 \Omega$  and  $R_2 = 10.0 \pm 0.1 \Omega$ .

And (15 ± 2%. (2) 3.3 1 ± 3%.



$$\infty = (2 \pm .2)$$

$$0 = (53 + 2^{\circ})$$

find value of 5 in proper limit.

Error ko bhool jao - -

$$\frac{1}{S} \Delta S = \frac{1}{x} \Delta X - \frac{1}{Coso} x sin \theta \Delta \theta$$

$$\infty = (2 \pm \cdot 2)$$

$$0 = (53 + 2^{\circ})$$

find value of 5 in proper limit.

Error ko bhool jao - -

$$ds = \infty (-\sin \theta) d\theta + (\cos \theta) dx$$



- X Simple pendulum base ques. = 15 min
- \* Vernier Calliper 1:30 hou
- & Somew guge 45 min
- \* Accuracy/Prink\_ smin

Before next sunday



· Co-ordinate Likhner

\* Dot product.

$$(2,3,4)$$
 $(7,8,9)$ 
 $(7,8,9)$ 
 $(7,8,9)$ 
 $(7,8,9)$ 
 $(7,8,9)$ 
 $(7,8,9)$ 

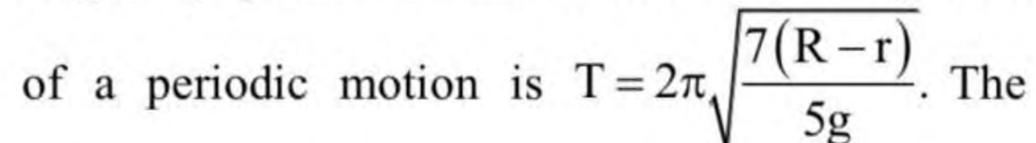
2. The edge of a cube is  $a = 1.2 \times 10^{-2}$  m. Then its volume will be recorded as : [JEE 2003] किसी घन की भुजा  $a = 1.2 \times 10^{-2}$  m है तो इसका आयतन होगा:- [JEE 2003] (A)  $1.7 \times 10^{-6}$  m<sup>3</sup> (C)  $1.70 \times 10^{-7}$  m<sup>3</sup> (D)  $1.78 \times 10^{-6}$  m<sup>3</sup>

The percentage errors in the measurement of mass and speed are 2% and 3%, respectively. How much will be the maximum error in the estimation of KE obtained by measuring mass and speed?

$$\frac{Sol}{E} = \frac{1}{2}mv^2$$

$$\frac{\Delta k}{E} = \frac{1}{2}mv^2$$

20. In an experiment to determine the acceleration due to gravity g, the formula used for the time period



values of R and r are measured to be  $(60 \pm 1)$  mm and  $(10 \pm 1)$  mm, respectively. In five successive measurements, the time period is found to be 0.52 s, 0.56 s, 0.57s, 0.54 s and 0.59 s. The least count of the watch used for the measurement of time period is 0.01 s. Which of the following statement(s) is(are) true? [JEE-Advance 2016]

- (1) The error in the measurement of r is 10%
- The error in the measurement of T is 3.57 %
- The error in the measurement of T is 2%
- (4) The error in the determined value of g is 11%

(1, 2, 4)Ans.

Q.12

A single slit diffraction experiment is performed to determine the slit width using the equation,  $\frac{bd}{D} = m\lambda$ , where b is the slit width, D the shortest distance between the slit and the screen, d the distance between the  $m^{th}$  diffraction maximum and the central maximum, and  $\lambda$  is the wavelength. D and d are measured with scales of least count of 1 cm and 1 mm, respectively. The values of  $\lambda$  and m are known precisely to be 600 nm and 3, respectively. The absolute error (in  $\mu$ m) in the value of b estimated using the diffraction maximum that occurs for m = 3 with d = 5 mm and D = 1 m is m = 3

 $\Delta D = 1 cm$ Answer. [75 to 79] 1d = 1mm 2- const 6 Kival b= 1x3x 600x10

Noxio

A wire has a mass  $0.3 \pm 0.003$  g, radius  $0.5 \pm 0.005$  mm and length  $6 \pm 0.06$  cm. The maximum percentage error in the measurement of its density is:-

एक तार का द्रव्यमान  $(0.3 \pm 0.003)$ g, त्रिज्या  $(0.5 \pm 0.005)$  mm तथा लम्बाई  $(6 \pm 0.06)$  cm है। इसके घनत्व के

मापन में अधिकतम प्रतिशत त्रुटि होगी-

(A) 1

(B) 2

(C) 3

[JEE 2004]

Ane (D)

$$\frac{3}{3} = \frac{m}{\pi^{\frac{3}{2}}}$$

$$\frac{4y}{y} = \frac{4m}{m} + \frac{34y}{x} + \frac{34}{x}$$

$$= \frac{-003}{3} + \frac{32 \times 005}{5} + \frac{06}{5}$$

Using the expression  $2d \sin \theta = \lambda$ , one calculates the values of d by measuring the corresponding angles  $\theta$  in the range 0 to 90°. The wavelength  $\lambda$  is exactly known and the error in  $\theta$  is constant for all values of  $\theta$ . As  $\theta$  increases from 0°:-

(A) the absolute error in d remains constant (B)

(B) the absolute error in d increases

(C) the fractional error in d remains constant

(D) the fractional error in d decreases

व्यंजक  $2d \sin \theta = \lambda$  का उपयोग करते हुए हम  $\theta$  को माप कर d का मान जानना चाहते हैं।  $\theta$  का मान  $\theta$  व  $\theta$ 0° के बीच में है। तरंग दैर्ध्य का मान हमें परिशुद्धत: ज्ञात है तथा  $\theta$  के मापन में त्रुटि  $\theta$  के सभी मानों के लिए समान है। जैसे  $\theta$  का मान  $\theta$ 0° के समान है। जैसे  $\theta$  का मान  $\theta$ 0° के समान है।  $\theta$ 1.

0° से बढ़ता है तब

[JEE-Advance 2013]

(A) d में निरपेक्ष त्रुटि स्थिर रहती है।

(B) d में निरपेक्ष त्रुटि बढ़ती है।

(C) d में भिन्नात्मक त्रुटि स्थिर रहती है।

(D) d में भिन्नात्मक त्रुटि घटती है।

Ans. (D)

Δf

In an experiment for determination of the focal length of a thin convex lens, the distance of the object from the lens is  $10 \pm 0.1$  cm and the distance of its real image from the lens is  $20 \pm 0.2$  cm. The error in the determination of focal length of the lens is n %. The value of n is

X100

2027 JEE Adv. 2023

いこしナー V= 20 土·2

Sol 
$$u = 10 \pm .1$$
 (1) Ever Ko Avol jao  
 $V = 20 \pm .2$   $u = -10$ ,  $u = +20$   
 $\frac{1}{V^2} \Delta V + \frac{1}{V^2} \Delta U = \frac{1}{f^2} \Delta f$   $\frac{1}{20} - \frac{1}{-10} = \frac{1}{f}$   
 $\frac{.2}{400} + \frac{.1}{100} = (\Delta f) \times \frac{1}{f}$ 

$$\frac{1}{4} = \frac{1}{4}$$
 $\frac{1}{4} = \frac{1}{4}$ 
 $\frac{1}{4} = \frac{1}{4}$ 
 $\frac{1}{4} = \frac{1}{4}$ 

Consider the ratio  $r = \frac{(1-a)}{(1+a)}$  to be determined by measuring



dimensionless quantity a. If the error in the measurement of  $\Delta a$  ( $\Delta a/a \ll 1$ ), then what is the error  $\Delta r$  in determining r?

C-34.7 W-33.81 UA-31.49 (JEE Adv. 2018

(a) 
$$\frac{\Delta a}{(1+a)^2}$$
 (b)  $\frac{2\Delta a}{(1+a)^2}$  (c)  $\frac{2\Delta a}{(1-a)^2}$  (d)  $\frac{2a\Delta a}{(1-a^2)}$ 

JEE ANV. 2018

$$\mathcal{L} = \frac{1-\alpha}{1+\alpha}$$

find DR

501

Notes

$$k = \frac{1-a}{1+a} + 1 - \frac{1}{a}$$

$$x = \frac{2}{1+a} - 1$$

$$\frac{dx}{da} = -\frac{2}{(1+a)^2}$$

$$dR = -\frac{2}{(1+\alpha)^2}d\alpha$$



Thoda dimag Lagro...yar

Gadho wali mehnat Nahi

Ha...ha.

Try to think seyond internet soi



## Homework



- Revise all notes (Error)
- KPP (pyo) will be provided 500n...
- module (Except Vernier Calliper & Screw grage you can solve.



