

YAKEEN NEET 2.0

11

2026

Basic Maths and Calculus (Mathematical Tools)

PHYSICS

Lecture - 02

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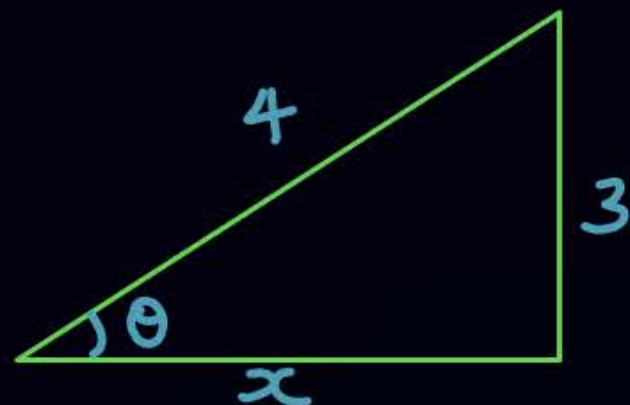
Topics to be covered



Basic trigonometry approximation & identity

Q

$$\sin \theta = \frac{3}{4}$$



$$3^2 + x^2 = 4^2$$

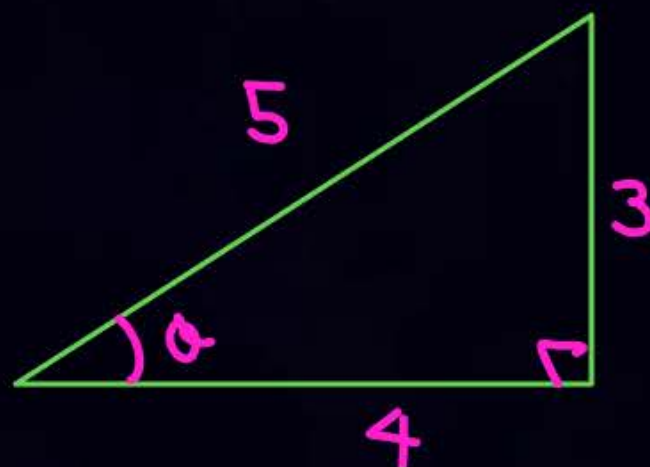
$$9 + x^2 = 16$$

$$x^2 = 7$$

$$x = +\sqrt{7}$$

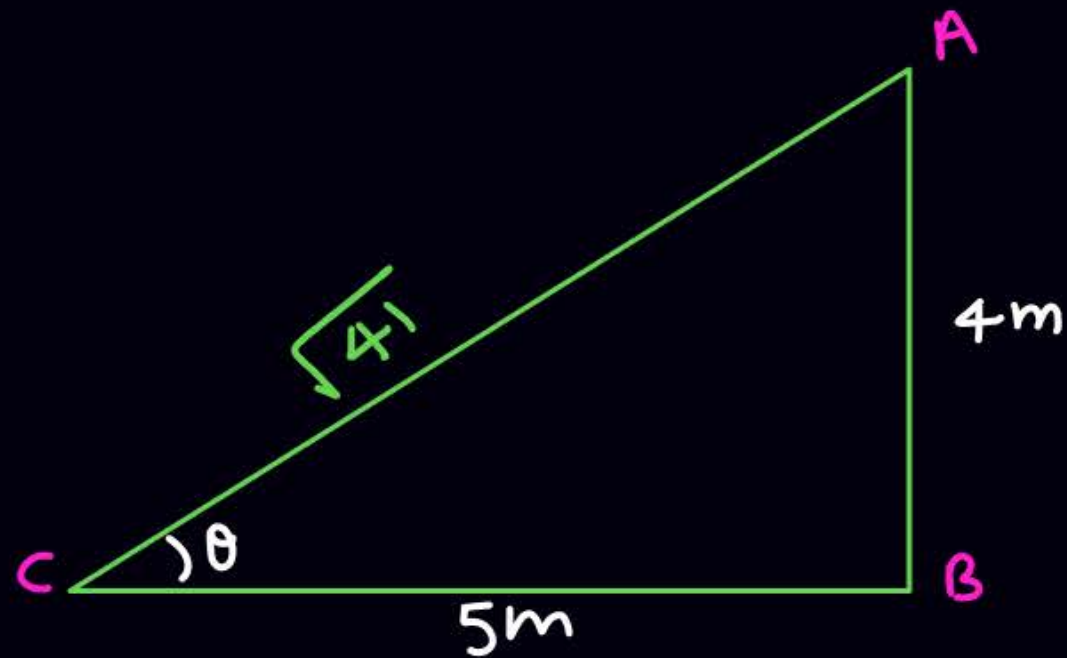
$$\tan \theta = \frac{3}{\sqrt{7}}$$

$$\cos \theta = \frac{\sqrt{7}}{4}$$



$$3^2 + 4^2 = 9 + 16 = 25 = 5^2$$

Q



$$AC = \sqrt{4^2 + 5^2} = \sqrt{16 + 25} = \sqrt{41}$$

$$\sin \theta = \frac{4}{\sqrt{41}}$$

$$\cos \theta = \frac{5}{\sqrt{41}}$$

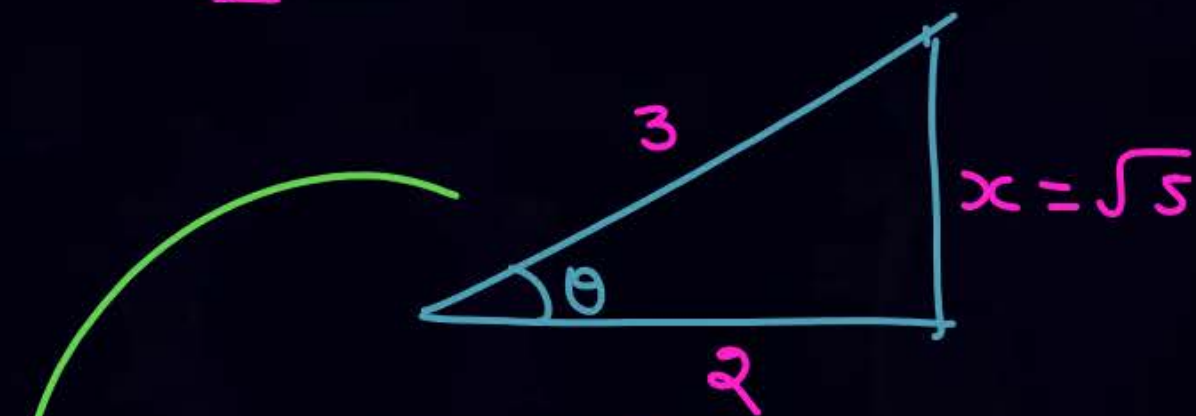
$$\tan \theta = \frac{4}{5}$$

Q

$$\cos \theta = \frac{2}{3}$$

$$\sin \theta = \frac{\sqrt{5}}{3}$$

$$\tan \theta = \frac{\sqrt{5}}{2}$$



$$x = \sqrt{3^2 - 2^2} = \sqrt{5}$$

$$2^2 + x^2 = 3^2$$

$$4 + x^2 = 9$$

$$x = \sqrt{5}$$

Small angle approximation

* $\sin \theta \approx \theta$ if θ is very small
 \downarrow
rad. $\theta < 5^\circ$
 $\theta < 10^\circ$

* $\tan \theta \approx \theta$ (if θ is very small)
 \downarrow
rad. $\theta < 10^\circ$

* If θ is very small ($\theta < 10^\circ$)

$$\sin \theta \approx \tan \theta \approx \theta$$

-03489



$$\textcircled{1} \sin 2^\circ = \sin 2 \cdot \frac{\pi}{180} \approx \frac{2\pi}{180} = \frac{\pi}{90}$$

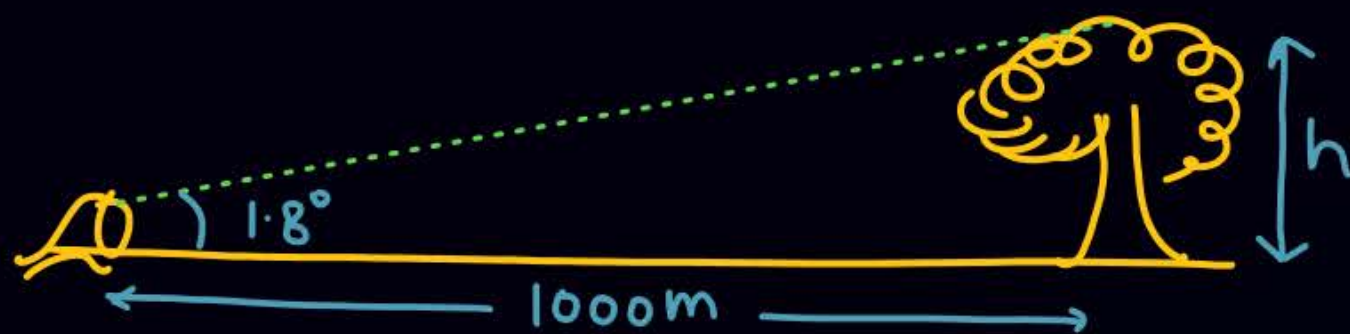
$$\textcircled{2} \tan 2^\circ = \tan \frac{2\pi}{180} \approx \frac{2\pi}{180} \approx \frac{\pi}{90}$$

$$\textcircled{3} \tan 6^\circ \approx \frac{6\pi}{180}$$

$$\textcircled{4} \sin 8^\circ \approx 8 \times \pi / 180$$

$$\textcircled{5} \tan 0^\circ = 0$$

Q find height of tree



$$\tan 1.8^\circ = \frac{h}{1000}$$

$$1.8 \times \frac{\pi}{180} = \frac{h}{1000}$$

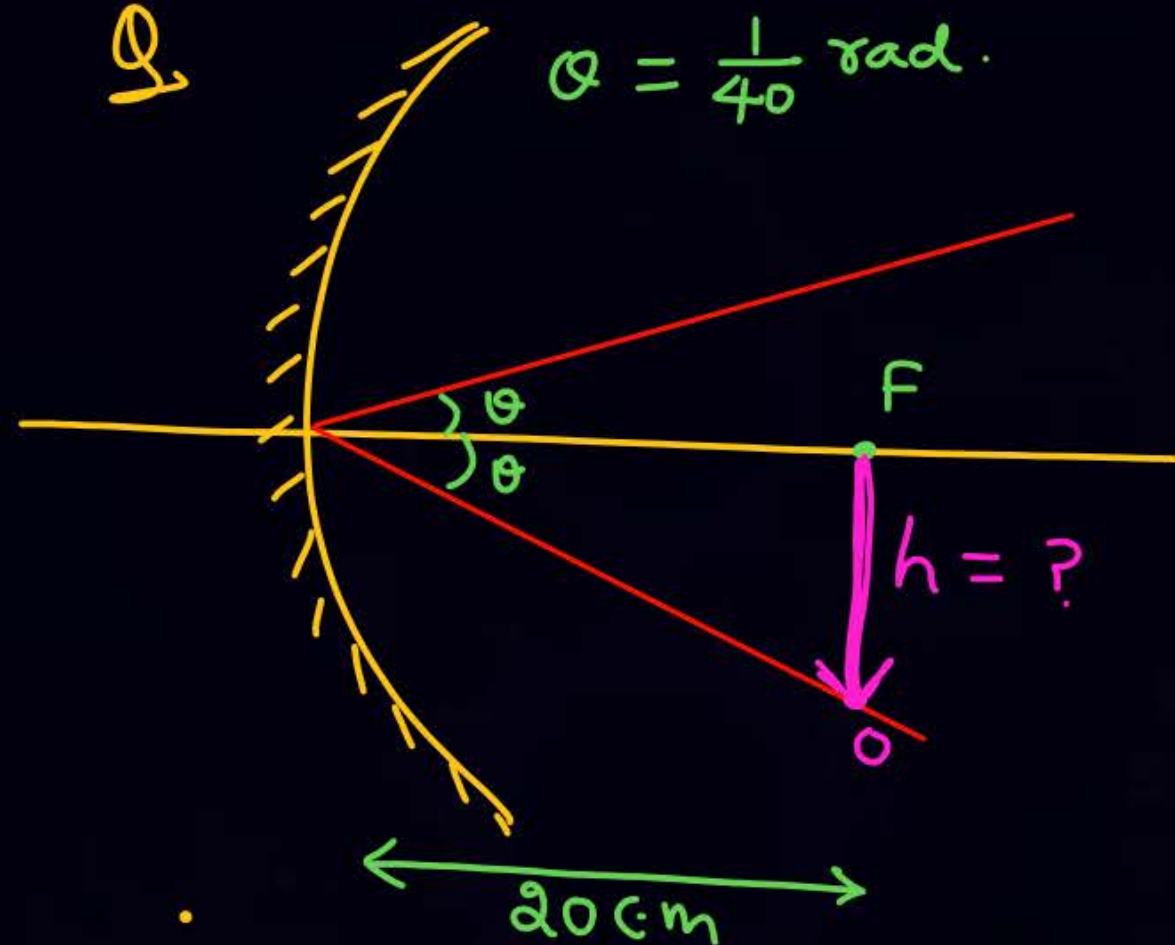
$$h = \frac{1.8 \times 3.14 \times 1000}{180} = 31.4 \text{ m}$$

optional

Q

$$f = 20 \text{ cm}$$

$$\theta = \frac{1}{40} \text{ rad.}$$



$$\tan \theta = \frac{h}{20}$$

$$\tan \frac{1}{40} = \frac{h}{20}$$

$$\frac{1}{40} = \frac{h}{20}$$

$$h = \frac{1}{2} \text{ cm}$$



Few important trigonometry ident. (8 days)

$$* \sin^2 \theta + \cos^2 \theta = 1$$

$$* \sin(A+B) = \sin A \cos B + \cos A \sin B$$

$$* \sin(A-B) = \sin A \cos B - \cos A \sin B$$

$$* \cos(A+B) = \cos A \cos B - \sin A \sin B$$

$$* \cos(A-B) = \cos A \cos B + \sin A \sin B$$

$$* \tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$$

$$* \tan(A-B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

$$* 1 + \tan^2 \theta = \sec^2 \theta$$

$$* 1 + \cot^2 \theta = \operatorname{cosec}^2 \theta \text{ (rarely)}$$

$$* \sin 2\theta = 2 \sin \theta \cos \theta$$

$$\begin{aligned} ** \cos 2\theta &= \cos^2 \theta - \sin^2 \theta \\ &= 1 - 2 \sin^2 \theta \\ &= 2 \cos^2 \theta - 1 \end{aligned}$$

* If θ is very small ($\theta < 10^\circ$)

$$*** \Rightarrow \sin \theta \approx \tan \theta \approx \theta$$

$$\Rightarrow \cos \theta = \sqrt{1 - \sin^2 \theta}$$

$$\cos \theta \approx \sqrt{1 - \theta^2}$$

$$\text{bcz } \cos^2 \theta = 1 - \sin^2 \theta$$

your choice (CKL)

If θ is very small

$$\sin^2 \theta + \cos^2 \theta = 1$$

$$\cos^2 \theta = 1 - \sin^2 \theta$$

$$\cos \theta = \sqrt{1 - \sin^2 \theta} \approx \sqrt{1 - \theta^2}$$

If θ is very small $\sin \theta \approx \theta$

$$\sin^2 \theta = \sin \theta \times \sin \theta \approx \theta \times \theta = \theta^2$$

Least priority



$$\begin{aligned} * \sin 75^\circ &= \sin (45^\circ + 30^\circ) = \sin 45^\circ \cos 30^\circ + \cos 45^\circ \sin 30^\circ = \frac{1}{\sqrt{2}} \frac{\sqrt{3}}{2} + \frac{1}{\sqrt{2}} \times \frac{1}{2} \\ &= \frac{\sqrt{3}}{2\sqrt{2}} + \frac{1}{2\sqrt{2}} = \frac{\sqrt{3} + 1}{2\sqrt{2}} \end{aligned}$$

$$\begin{aligned} * \sin 15^\circ &= \sin (45^\circ - 30^\circ) = \sin 45^\circ \cos 30^\circ - \cos 45^\circ \sin 30^\circ = \frac{1}{\sqrt{2}} \frac{\sqrt{3}}{2} - \frac{1}{\sqrt{2}} \times \frac{1}{2} \\ &= \frac{\sqrt{3} - 1}{2\sqrt{2}} \end{aligned}$$

(H/w ³ 2011 last slide 44)



$$\sin(A+B) = \sin A \cos B + \cos A \sin B$$

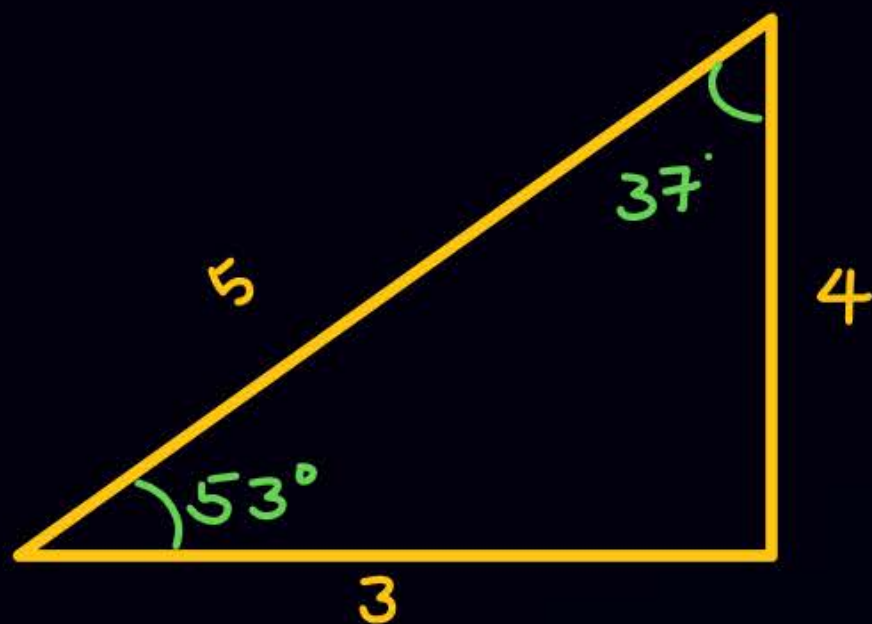
$$\cos(A+B) = \cos A \cos B - \sin A \sin B$$

$$\textcircled{1} \quad \sin 105^\circ = \sin(60+45) = \sin 60 \cos 45 + \cos 60 \sin 45 = \frac{\sqrt{3}}{2} \cdot \frac{1}{\sqrt{2}} + \frac{1}{2} \cdot \frac{1}{\sqrt{2}}$$

$$= \frac{\sqrt{3} + 1}{2\sqrt{2}}$$

$$\textcircled{2} \quad \tan 105^\circ = \tan(60+45) = \frac{\sqrt{3} + 1}{1 - \sqrt{3} \times 1} = \frac{\sqrt{3} + 1}{1 - \sqrt{3}}$$

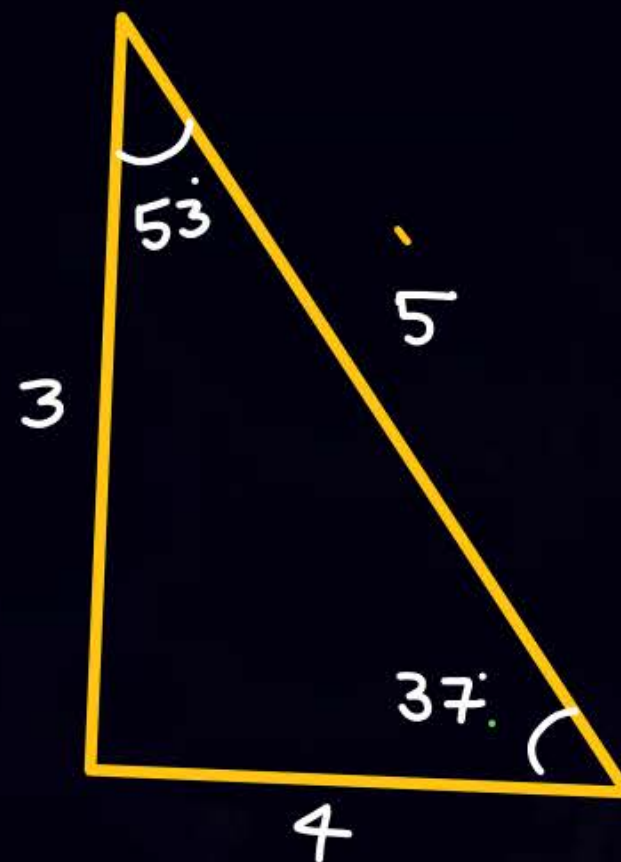
$$\textcircled{3} \quad \cos 105^\circ = \cos(60+45) = \cos 60 \cos 45 - \sin 60 \sin 45$$
$$= \frac{1}{2} \times \frac{1}{\sqrt{2}} - \frac{\sqrt{3}}{2} \cdot \frac{1}{\sqrt{2}} = \frac{1 - \sqrt{3}}{2\sqrt{2}}$$



$$\sin 53^\circ = \frac{4}{5}$$

$$\cos 53^\circ = \frac{3}{5}$$

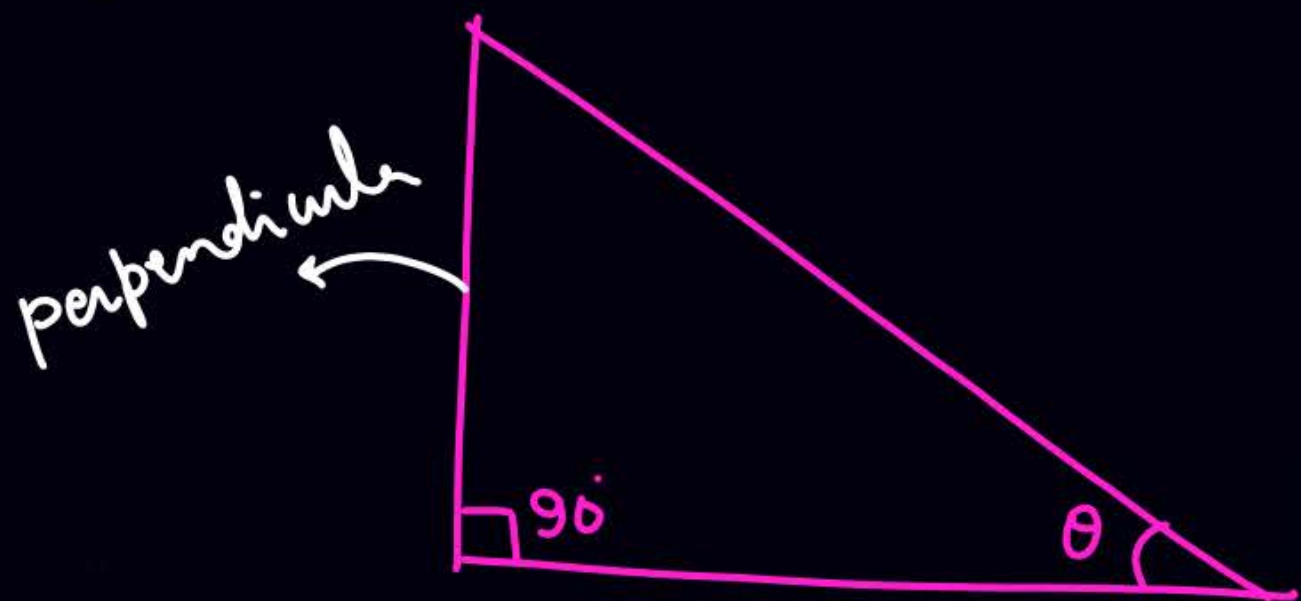
$$\tan 53^\circ = \frac{4}{3}$$



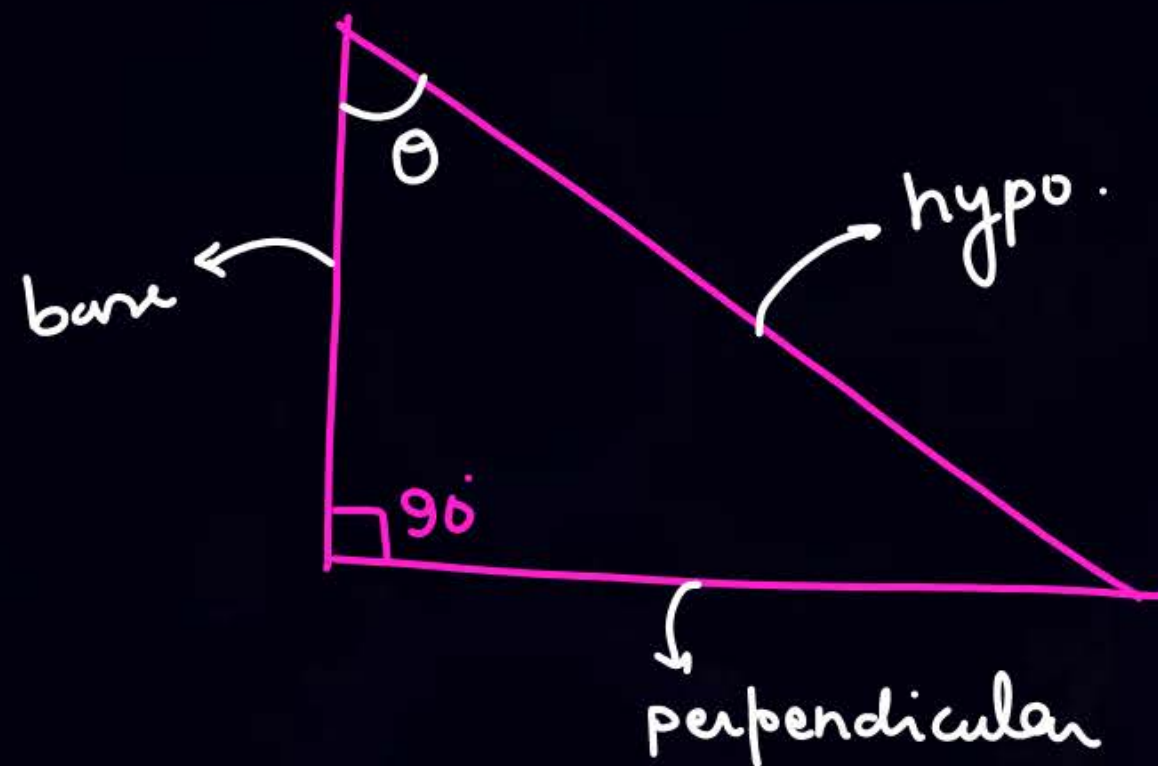
$$\cos 37^\circ = \frac{4}{5}$$

$$\sin 37^\circ = \frac{3}{5}$$

$$\tan 37^\circ = \frac{3}{4}$$



θ के सामने वाली side perpendicular है







Home Work

- Revise all formula
- KPP-01 (will be uploaded at evening)
- DPP-01

THANK
YOU