



Bayesian Network Fundamentals

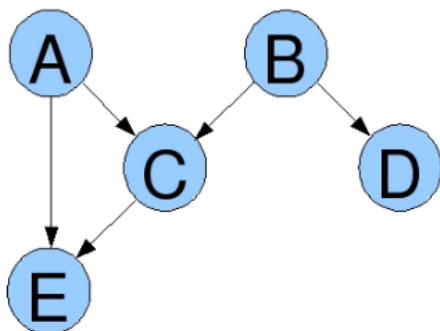
测验, 3 个问题

✔ 恭喜！您通过了！

下一项

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1.

Factorization.Given the same model as above, which of these is an appropriate decomposition of the joint distribution $P(A, B, C, E)$?

- ☐ $P(A, B, C, E) = P(A)P(B)P(C|A)P(C|B)P(E|A)P(E|C)$
- ☐ $P(A, B, C, E) = P(A)P(B)P(C)P(E)$
- ☐ $P(A, B, C, E) = P(A)P(B)P(A, B|C)P(A, C|E)$
- ☒ $P(A, B, C, E) = P(A)P(B)P(C|A, B)P(E|A, C)$

正确

We can read off the appropriate factorization from the graph by examining the parents of each variable in the graph: A and B have no parents, while C is a child of A, B and E is a child of A, C .

This gives us $P(A, B, C, E) = P(A)P(B)P(C|A, B)P(E|A, C)$.

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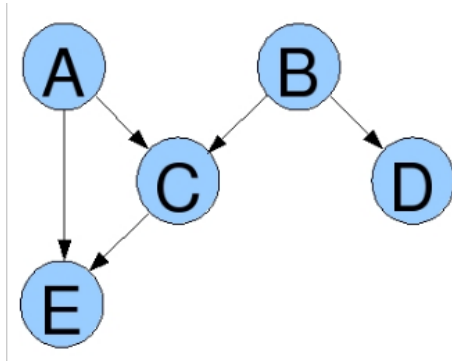
2.

Independent parameters.



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How many independent parameters are required to uniquely define the CPD of E (the conditional probability distribution associated with the variable E) in the same graphical model as above, if A, B, and D are binary, and C and E have three values each?



If you haven't come across the term before, here's a brief explanation: A multinomial distribution over m possibilities x_1, \dots, x_m has m parameters, but $m - 1$ independent parameters, because we have the constraint that all parameters must sum to 1, so that if you specify $m - 1$ of the parameters, the final one is fixed. In a CPD $P(X|Y)$, if X has m values and Y has k values, then we have k distinct multinomial distributions, one for each value of Y , and we have $m - 1$ independent parameters in each of them, for a total of $k(m - 1)$. More generally, in a CPD $P(X|Y_1, \dots, Y_r)$, if each Y_i has k_i values, we have a total of $k_1 \times \dots \times k_r \times (m - 1)$ independent parameters.

Example: Let's say we have a graphical model that just had $X \rightarrow Y$, where both variables are binary. In this scenario, we need 1 parameter to define the CPD of X . The CPD of X contains two entries $P(X = 0)$ and $P(X = 1)$. Since the sum of these two entries has to be equal to 1, we only need one parameter to define the CPD.

Now we look at Y . The CPD for Y contains 4 entries which correspond to:

$P(Y = 0|X = 0)$, $P(Y = 1|X = 0)$, $P(Y = 0|X = 1)$, $P(Y = 1|X = 1)$. Note that $P(Y = 0|X = 0)$ and $P(Y = 1|X = 0)$ should sum to one, so we need 1 independent parameter to describe those two entries; likewise, $P(Y = 0|X = 1)$ and $P(Y = 1|X = 1)$ should also sum to 1, so we need 1 independent parameter for those two entries.

Therefore, we need 1 independent parameter to define the CPD of X and 2 independent parameters to define the CPD of Y .

- ☐ 3
- ☐ 18
- ☐ 8
- ☐ 17
- ☐ 11
- ☐ 6
- ☒ 12

正确

In a Bayesian network, the conditional probability distribution associated with a variable is the conditional probability distribution of that variable given its parents. There are 6 possibilities for the values of E's parents (A is binary and C takes on 3 values). For each of these possibilities, there are 3 possible values for E, which corresponds to 2 free parameters (since the 3 numbers have to sum to 1). So there are $6 \times 2 = 12$ total free parameters.

1 / 1
分数

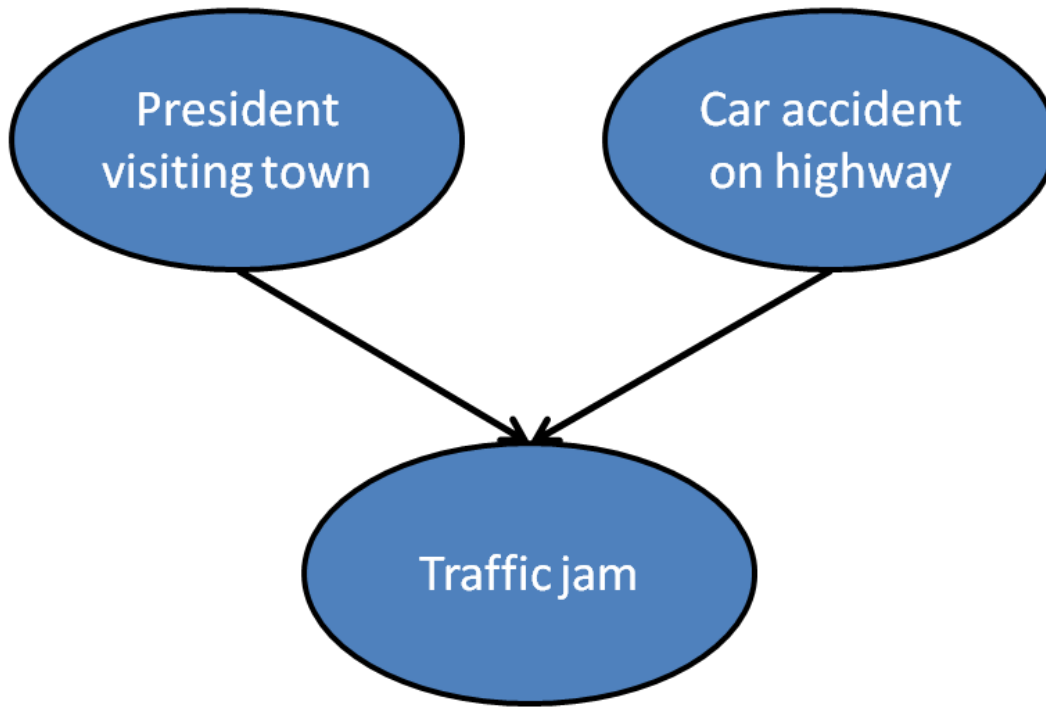
3.

*Inter-causal reasoning.

Consider the following model for traffic jams in a small town, which we assume can be caused by a car accident, or by a visit from the president (and the accompanying security motorcade).

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$P(\text{Accident} = 1) = 0.1$



$$P(\text{Traffic} = 1 \mid \text{President} = 0, \text{Accident} = 0) = 0.1$$

$$P(\text{Traffic} = 1 \mid \text{President} = 0, \text{Accident} = 1) = 0.5$$

$$P(\text{Traffic} = 1 \mid \text{President} = 1, \text{Accident} = 0) = 0.6$$

$$P(\text{Traffic} = 1 \mid \text{President} = 1, \text{Accident} = 1) = 0.9$$

Calculate $P(\text{Accident} = 1 \mid \text{Traffic} = 1)$ and $P(\text{Accident} = 1 \mid \text{Traffic} = 1, \text{President} = 1)$. Separate your answers with a space, e.g., an answer of

0.15 0.25

means that $P(\text{Accident} = 1 \mid \text{Traffic} = 1) = 0.15$ and $P(\text{Accident} = 1 \mid \text{Traffic} = 1, \text{President} = 1) = 0.25$. Round your answers to two decimal places and write a leading zero, like in the example above.

0.35 0.14

正确答案

To calculate the required values, we can apply Bayes' rule. For instance,

$$\begin{aligned}
 P(A = 1 \mid T = 1, P = 1) &= \frac{P(A = 1, T = 1, P = 1)}{P(T = 1, P = 1)} \\
 &= \frac{P(A = 1, T = 1, P = 1)}{P(A = 0, T = 1, P = 1) + P(A = 1, T = 1, P = 1)}.
 \end{aligned}$$

We can then use the chain rule of Bayesian networks to substitute the correct values in, e.g.,

$$P(A = 1, T = 1, P = 1) = P(P = 1) \times P(A = 1) \times P(T = 1 \mid P = 1, A = 1)$$

This example of inter-causal reasoning meshes well with common sense: if we see a traffic jam, the probability that there was a car accident is relatively high. However, if we also see that the president is visiting town, we can reason that the president's visit is the cause of the traffic jam; the probability that there was a car accident therefore drops correspondingly.



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