## Q-10.13.3.10

## Yash Patil - EE22BTECH11058

**Question:** Eight coins are tossed together. The probability of getting exactly 3 heads is

- 1)  $\frac{1}{256}$
- 2)  $\frac{7}{32}$
- 3)  $\frac{3}{32}$

Solution: Defining variables:

Parameter	Value	Description
n	8	Number of coins tossed
p	0.5	probability of getting heads
$\mu = np$	4	mean of the distribution
$\sigma^2 = np(1-p)$	2	variance of the distribution
Y	0-8	denotes number of heads obtained

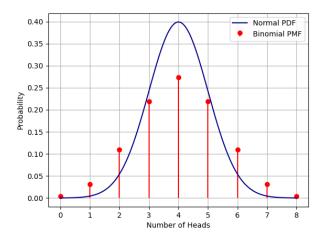


Fig. 1. Binomial vs Guassian

## **Gaussian Distribution:**

The gaussian distribution for Y is

$$P_Y(x) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{\frac{-(x-\mu)^2}{2\sigma^2}}$$
 (1)

For getting 3 exactly heads

$$Y = 3 \tag{2}$$

Substituting in equation (1), probability for getting exactly 3 heads is

$$Y = 3 \tag{3}$$

$$P_Y(3) = \frac{1}{\sqrt{2\pi \times 2}} e^{\frac{-(3-4)^2}{2\times 2}} \tag{4}$$

$$= 0.35206$$
 (5)

And, by binomial distribution, the probability of getting exactly 3 heads is

$$= \binom{8}{3} \times 0.5^3 \times 0.5^5 \tag{6}$$

$$= 0.21875$$
 (7)

: option 2 is correct.

Comparing Binomial and Gaussian distribution: