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## Q-10.13.3.10

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**Question:** A lot of 100 watches is known to have 10 defective watches. If 8 watches are selected (one by one with replacement) at random, what is the probability that there will be at least one defective watch? **Solution:** 

Parameter	Value	Description
$X_1 - X_8$	0,1	0-Defective watch, 1-Good watch and $X_i$ denotes $i^{th}$ selection
Y	$\sum_{i=1}^{8} X_i$	Represents number of defective watches selected in 8 selections

pmf of  $X_1 - X_8$ :

$$p_{X_i}(k) = \begin{cases} \frac{1}{10}, & k = 0\\ \frac{9}{10}, & k = 1 \end{cases} \quad \forall \quad 1 \le i \le 8$$
 (1)

pmf of Y is given by:

$$p_Y(k) = \binom{8}{k} \times (0.1)^k \times (0.9)^{8-k} \quad \forall \quad 0 \le k \le 8$$
 (2)

(3)

CDF of Y:

$$F_Y(k) = \sum_{i=0}^k {8 \choose i} \times (0.1)^i \times (0.9)^{8-i} \quad \forall \quad 0 \le k \le 8$$
 (4)

(5)

: probability of choosing atleast one defective watch in 8 selections

$$= F_Y(8) - F_Y(0) \tag{6}$$

$$=1 - \binom{8}{0} \times (0.1)^0 \times (0.9)^8 \tag{7}$$

$$= 1 - 0.430467 \tag{8}$$

$$= 0.569533$$
 (9)