## 1

## Q-10.13.3.10

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Question: All the jacks, queens and kings are removed from a deck of 52 playing cards. The remaining cards are well shuffled and then one card is drawn at random. Giving ace a value 1 similar value for other cards, find the probability that the card has a value

- 1) 7
- 2) greater than 7
- 3) less than 7

**Solution:** Number of cards left after removing all jacks, queens and kings(=N)

$$= 52 - 4 \times 3 \tag{1}$$

$$=40$$

Parameter	Value	Description
X	1-10	Represents the value of the card picked

Finding pmf:

$$p_X(k) = \Pr(X = k); 1 \le k \le 10$$
 (3)

$$=\frac{4\times1}{40}\tag{4}$$

$$=\frac{1}{10}\tag{5}$$

$$= \frac{4 \times 1}{40}$$

$$= \frac{1}{10}$$

$$\therefore p_X(k) = \begin{cases} \frac{1}{10} & 1 \le k \le 10\\ 0 & otherwise \end{cases}$$

$$(4)$$

$$(5)$$

CDF for the following pmf is:

$$F_X(k) = \sum_{m=0}^k p_X(m); 1 \le k \le 10$$
 (7)

$$= k \times \frac{1}{10} \tag{8}$$

$$=\frac{k}{10}\tag{9}$$

$$\therefore F_X(k) = \begin{cases} 0 & k \le 0 \\ \frac{k}{10} & 1 \le k \le 10 \\ 1 & k > 10 \end{cases}$$
 (10)

1) Probability that card has value equal to 7:

$$= p_X(k); k = 7$$
 (11)

$$= 1 \times \frac{1}{10} = \frac{1}{10} \tag{12}$$

2) Probability that card has value greater than 7

$$= F_X(10) - F_X(7) \tag{13}$$

$$=1-\frac{7}{10}=\frac{3}{10}\tag{14}$$

3) Probability that card has value less than 7

$$=F_X(6); (15)$$

$$=\frac{6}{10}\tag{16}$$