# UoA CP Lecture 3 Sorting and Brute Force

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# April 17, 2020

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# 1 How to sort

# 1.1 Quicksort

The main idea of this method is:

- 1. Choose a pivot, randomly.
- 2. Divide the numbers into three sub-arrays: smaller than pivot, equal to pivot, larger than pivot.
- 3. Recursively sort the sub-arrays.
- 4. Merge the sub-arrays.

```
vector<int> my_sort(vector<int> nums) {
        if(nums.size() <= 1) {
2
            return nums;
       } else {
            // 1. Randomly choose a pivot
            int pivot_index = rand() % nums.size();
            auto pivot = nums[pivot_index];
            // 2. Divide the numbers into three sub-arrays
            vector<int> small, equal, large;
10
            for(auto v:nums) {
                if(v < pivot)small.push_back(v);</pre>
12
                else if(v == pivot)equal.push_back(v);
13
                else if(v > pivot)large.push_back(v);
            }
15
16
            // 3. Recursively sort the sub-arrays
17
            small = my_sort(small);
            //equal = my_sort(equal);
19
            large = my_sort(large);
21
            // 4. Merge the sub-arrays
23
            vector<int> result;
            result.insert(result.end(), small.begin(), small.end());
25
            result.insert(result.end(), equal.begin(), equal.end());
            result.insert(result.end(), large.begin(), large.end());
27
            return result;
       }
29
   }
```

## 1.2 std::sort

# 1.2.1 Basic Usage

```
int main() {
        vector\langle int \rangle v = {4, 2, 5, 3, 5, 8, 3};
2
        // small -> large
        sort(v.begin(), v.end());
        // large -> small
        sort(v.rbegin(), v.rend());
        // sort an C-style array
        int n = 7; // array size
        int a[] = {4, 2, 5, 3, 5, 8, 3};
11
        sort(a, a + n);
13
14
        // sort a string
15
        string s = "monkey";
16
        sort(s.begin(), s.end());
17
18
        return 0;
19
  }
20
```

## 1.2.2 User-defined struct and Customized Comparison Functions

```
struct P {
        int x, y;
2
        bool operator<(const P &p) const {</pre>
             if(x != p.x) {
                 return x < p.x;
            } else {
                 return y < p.y;</pre>
            }
        }
10
   };
11
12
    bool cmp(const P &a, const P &b) {
13
        if(a.y != b.y) {
14
            return a.y < b.y;</pre>
15
        } else {
16
            return a.x < b.x;
17
        }
18
   }
19
20
   int main() {
21
        vector<P> v;
22
        v.push_back({1, 2});
        v.push_back({2, 1});
24
        // small -> large
        sort(v.begin(), v.end());
26
        // {(1,2), (2,1)}
        sort(v.begin(), v.end(), cmp);
28
        // {(2,1), (1,2)}
29
        return 0;
30
   }
31
```

# 2 Sorted, so what?

# 2.1 Binary Search - Sum of Two Values

```
#include <bits/stdc++.h>
   using namespace std;
   int main() {
        int n, target;
        cin >> n >> target;
        vector<pair<int, int>> v(n);
        int cnt = 1;
        for(auto &i:v) {
            cin >> i.first;
            i.second = cnt++;
11
        }
12
        sort(begin(v), end(v));
13
        for(auto itr = begin(v); itr != end(v); itr++) {
            auto itr2 = lower_bound(begin(v), itr, make_pair(target - itr->first, 0));
            if(itr2 != itr and itr2->first + itr->first == target) {
16
                cout << itr->second << " " << itr2->second << endl;</pre>
17
                return 0;
18
            }
20
        cout << "IMPOSSIBLE" << endl;</pre>
        return 0;
22
   }
23
```

# 2.2 Stick Lengths

```
#include <bits/stdc++.h>
   using namespace std;
    typedef long long 11;
    int main() {
        11 n;
        cin >> n;
        vector<ll> v(n);
9
        for(auto &i:v)
10
             cin >> i;
11
12
        sort(begin(v), end(v));
14
15
        //find the median
16
        11 \text{ opt} = v[n / 2];
17
        11 \text{ ans} = 0;
18
        for(int i = 0; i < n; i++)</pre>
19
            ans += abs(v[i] - opt);
20
        cout << ans;</pre>
21
22
23 }
```

# 3 Just brute force it

## 3.1 for loop - UVa 725

```
#include <bits/stdc++.h>
   using namespace std;
    void solve(int n) {
        bool found = false;
        for(int a = 0; a < 10; a++) {
5
            for(int b = 0; b < 10; b++) {
                for(int c = 0; c < 10; c++) {
                     for(int d = 0; d < 10; d++) {
                         for(int e = 0; e < 10; e++) {
9
                             int numerator = a * 10000 + b * 1000 + c * 100 + d * 10 + e;
10
                             if(numerator % n == 0) {
11
                                  int denominator = numerator / n;
12
                                  string nu = to_string(numerator), de = to_string(denominator);
13
                                  while(nu.size() < 5)nu = "0" + nu;
14
                                  while(de.size() < 5)de = "0" + de;
                                  set<char>s;
16
                                  for(auto i:nu)s.insert(i);
17
                                  for(auto i:de)s.insert(i);
18
                                  if(s.size() == 10){
                                      found = true;
20
                                      cout<<nu<<" / "<<de<<" = "<<n<<endl;
21
                                  }
22
                             }
                         }
24
                    }
                }
26
            }
28
        if(!found) cout << "There are no solutions for " << n << "." << endl;</pre>
29
30
    int main() {
31
        int n; bool first = true;
32
        while(cin >> n) {
33
            if(n == 0) {
34
                return 0;
35
            } else {
36
                if(first) first = false;
37
                else cout << endl;</pre>
                solve(n);
39
            }
40
        }
41
   }
42
```

# 3.2 Depth-First Search(DFS)

# 3.2.1 Generating Subset - Apple Division

```
#include <bits/stdc++.h>
   using namespace std;
    typedef long long 11;
   11 ans = LLONG_MAX, num[20], sum = 0;
    int n;
    void dfs(int step, ll sub_sum) {
9
        if(step == n) {
10
            ans = min(ans, abs(sub_sum - (sum - sub_sum)));
11
        } else {
            // choose
13
            dfs(step + 1, sub_sum + num[step]);
14
15
            // not choose
16
            dfs(step + 1, sub_sum + 0);
17
        }
18
   }
19
20
    int main() {
^{21}
        cin >> n;
22
        for(int i = 0; i < n; i++) {
            cin >> num[i];
24
            sum += num[i];
25
26
        dfs(0,0);
        cout<<ans<<endl;</pre>
28
        return 0;
30
   }
```

# 3.2.2 Backtrack - Chessboard and Queens

```
#include <bits/stdc++.h>
   using namespace std;
    const int n = 8;
    string maze[n];
    int pos[n];
    int ans = 0;
9
    void dfs(int row = 0) {
10
        if(row == n)
11
            ans++;
12
        else {
13
             for(pos[row] = 0; pos[row] < 8; pos[row]++) {</pre>
14
                 bool ok = true;
15
                 if(maze[row][pos[row]] == '*')ok = false;
16
                 for(int past = 0; past < row; past++) {</pre>
                      if(pos[past] == pos[row])ok = false;
18
                     if(pos[past] - pos[row] == past - row)ok = false;
19
                      if(pos[row] - pos[past] == past - row)ok = false;
20
                 }
                 if(ok) {
22
                     dfs(row + 1);
                 }
24
            }
        }
26
   }
27
28
29
    int main() {
30
        for(int i = 0; i < n; i++) {</pre>
31
             cin >> maze[i];
32
        }
33
        dfs();
34
        cout << ans << endl;</pre>
35
        return 0;
36
37
```

#### 3.2.3 Meet in the middle - Codeforces 888E

```
#include <bits/stdc++.h>
   using namespace std;
   int n, m;
   void dfs(vector<int> &num, vector<int> &result, int sum = 0, int cur = 0) {
        if(cur == num.size()) {
            result.push_back(sum);
       } else {
7
            // not choose
            dfs(num, result, (sum + num[cur]) % m, cur + 1);
            // choose
11
            dfs(num, result, sum, cur + 1);
        }
13
   }
14
   int main() {
15
        cin >> n >> m;
16
       vector<int> result[2], num[2];
17
        for(int i = 0; i < n; i++) {
18
            int v;
19
            cin >> v;
20
            if(i \% 2 == 0) {
                num[0].push_back(v);
22
            } else {
                num[1].push_back(v);
24
        }
26
        for(int i = 0; i < 2; i++) {
            dfs(num[i], result[i]);
28
            sort(begin(result[i]), end(result[i]));
29
        }
30
        int ans = 0;
31
        for(auto a: result[0]) {
            auto iterator = lower_bound(begin(result[1]), end(result[1]), m - a);
33
            if(iterator != begin(result[1])) {
34
                --iterator;
35
                ans = max(ans, a + (*iterator));
            }
37
            ans = max(ans, (a + result[1].back()) \% m);
        }
39
        cout << ans << endl;</pre>
        return 0;
41
   }
42
```

## 3.3 Bitmask

## 3.3.1 Generating Subset - Apple Division

```
#include <bits/stdc++.h>
   using namespace std;
    typedef long long 11;
   11 ans = LLONG_MAX, num[20], sum = 0;
    int n;
9
    int main() {
        cin >> n;
11
        for(int i = 0; i < n; i++) {
            cin >> num[i];
13
            sum += num[i];
14
        }
15
        for(int mask = 0; mask < (1 << n); mask++) {</pre>
16
            11 sub_sum = 0;
17
            for(int bit = 0; bit < n; bit++) {</pre>
18
                 if((1 << bit) & mask)
                     sub_sum += num[bit];
20
            }
21
            ans = min(ans, abs(sub_sum - (sum - sub_sum)));
22
        }
24
        cout << ans << endl;</pre>
26
        return 0;
28
   }
```