# A MULTI-BERNOULLI GAUSSIAN FILTER FOR TRACK-BEFORE-DETECT



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# **BACKGROUND & AIMS**

#### **PROJECT INFORMATION**

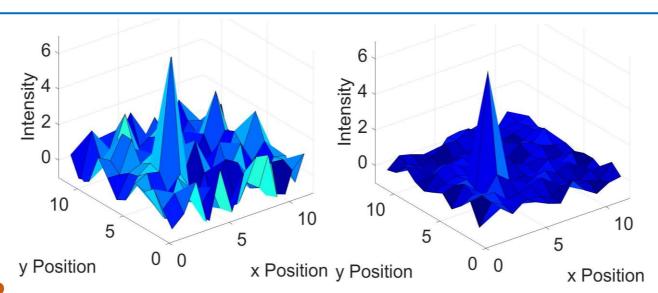
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The project focuses on using Track
Before-Detect to track objects from noisy measurement data.

## WHY A DIFFERENT APPROACH?

Typical methods work by **thresholding** measurement data to find **detections**. This becomes problematic in scenarios with **Low Signal-to-noise ratios**.



#### **MULTI-BERNOULLI FILTER?**

The Multi-Bernoulli Filter identifies potential targets that may be present in the surveillance region. For this filter it is required to predict each potential target's probability of existence. Each potential target is modelled with a Bernoulli probability [1].

$$f_{k|k-1}^{l}(X_{k|k-1}^{l})$$

$$=\begin{cases} 1 - r_{k|k-1}^{l}, & X_{k|k-1}^{l} = \emptyset \\ r_{k|k-1}^{l}p(x), & X_{k|k-1}^{l} = \{x\} \end{cases}$$

# DEALING WITH MULTIPLE OBJECTS

The filter can be extended for multiple objects with auxiliary variables [2]. The filter predicts the contribution of each potential target to the measurement likelihood. Each potential target then undergoes independent prediction and update steps.

# **ONGOING WORK**

#### **SENSOR NETWORK**

A multi-sensor environment is used in which the surveillance region is made up of cells with a sensor positioned at the midpoint of every cell. This results in a non-linear measurement function.

#### **SIGMA-POINT KALMAN FILTER**

A sigma-point Kalman filter is used to provide a mapping between the state-space and the measurements. Sigma-points are used to predict the expected measurement vector of each potential target, the corresponding measurement covariance and cross covariance with the target's state-space. Currently an Unscented Kalman filter is used.

#### **OBJECTS IN CLOSE PROXIMITY**

A challenging scenario is when there are multiple objects in close proximity. In this project a bias term and additional noise are introduced to account for any other potential targets.

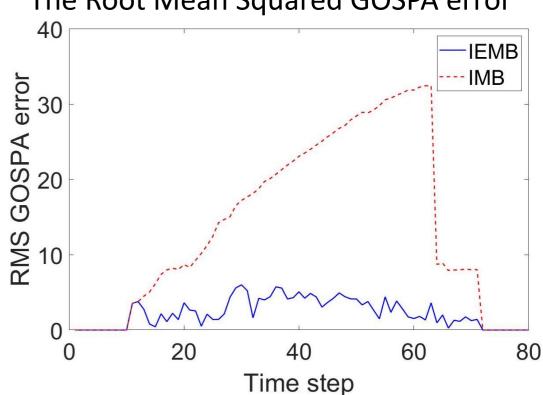
$$p(z_k) \approx N(z_k; h(x^u) + \tilde{z}_{corr}^u, R + S_{corr}^u)$$

#### **CONDITIONAL MOMENTS**

Each target's expected measurement vector and measurement covariance is weighted using its probability of existence to give its likelihood contribution. The bias term and additional noise are found by summing contributions from all other targets.

# PRELIMINARY RESULTS

The Root Mean Squared GOSPA error



In this approach (IEMB), compared to methods which ignore other targets (IMB), the number of false targets is greatly reduced. This produces a lower RMS GOSPA error [3].

## **FUTURE WORK**

- Parallelisation of the filter where the recursions for the independent potential targets operate on separate processors.
- Implement alternatives to the Unscented Kalman filter including particle filters or the iterated posterior linearisation filter.
- Investigate the possibility of switching auxiliary variables between **Bernoullis** at each time step.
- ☐ To test filter using data **real data** collected from sensor.

# **CONCLUSION**

This project will create a filter that works in noisy environments where there is a **low signal-to-noise ratio**. It should be capable of tracking **multiple objects** in **close proximity** to each other **simultaneously**. The use of **parallel computing** techniques means the potential of **highly accurate** results while maintaining desirable **run-times**.

# **REFERENCES**

[1] B. Ristic, B.-T. Vo, B.-N. Vo, and A. Farina, "A Tutorial on Bernoulli Filters: Theory, Implementation and Applications," IEEE Transactions on Signal Processing, vol. 61, no. 13, pp. 3406–3430, Jul. 2013.
[2] Á. F. García-Fernández, L. Svensson, J. L. Williams, Y. Xia, and K. Granström, "Trajectory Poisson multi-Bernoulli filters," in IEEE Transactions on Signal Processing, vol. 68, pp. 4933-4945, Mar. 2020.
[3] A. S. Rahmathullah, A. F. García-Fernández, and L. Svensson, "Generalized optimal sub-pattern assignment metric," in 20th International Conference on Information Fusion, 2017, pp. 1–8.





