## RoboScene to CSP Translation Rules

Holly Hendry June 24, 2024

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\llbracket \mathsf{lifeline} : \mathsf{Actor}; \; \mathsf{ins}, \mathsf{outs} : \mathsf{LifelineEvents}; \; \mathsf{vars} : \mathsf{VarsList} \rrbracket_{LS}
        \ \widehat{=} \ \ \left[\!\left[\mathsf{outs}\right]\!\right]_{OS} \ \left[\!\left[\mathsf{ins}\right]\!\right]_{IS} \ \left[\!\left[\mathsf{vars}\right]\!\right]_{VS}
[\![(\underline{\mathrm{out}}\ \mathtt{event}->\mathtt{actor}):\ \mathtt{LifelineEvents}]\!]_O\ \widehat{=}\ \mathit{channel}\ \mathtt{event}: \underline{\mathrm{InOut}}
 [(\underline{\text{out}} \text{ event} : \mathsf{Type} - > \mathsf{actor}) : \mathsf{LifelineEvents}]_Q
        \hat{=} \ oldsymbol{channel} \ 	ext{event} : \llbracket \mathsf{Type}, \mathsf{event} 
Vert 
Vert_{TO}
 \llbracket (\operatorname{\underline{in}} \mathsf{event} < -\mathsf{actor}) : \mathtt{LifelineEvents} 
Vert_I \; \widehat{=} \; \mathit{channel} \; \mathsf{event} : \underline{\mathtt{InOut}} \;
 \llbracket (\operatorname{\underline{in}} \operatorname{event} : \mathsf{Type} < -\operatorname{actor}) : \operatorname{LifelineEvents} 
rbracket_I
        \hat{=} channel event : \llbracket \mathsf{Type}, \mathsf{event} \rrbracket_{\mathit{TI}}
[(var : Type) : VariableList]]_V \stackrel{\widehat{=}}{=}
       channel set_var: Type
       {\it channel}\ {\it get\_}{\it var} : Type
       Memory\_var(var) = get\_var!var \rightarrow Memory\_var(var)
               \square set\_var?x \rightarrow Memory\_var(x)
               \Box terminate \rightarrow Skip
       Memory = ( || var \bullet \{terminate\} \circ Memory\_var(var) )
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[name: EString; trait: EString; actors: Actor; sequences: Sequence]_{SD}
                \ \widehat{=}\ \ \| \mathsf{actors} \|_A \ \| \mathsf{sequences} \|_{SS}
 \begin{split} & \left[ \left[ \operatorname{def} \right] \right]_{SS} \ \widehat{=} \ \left[ \left[ \operatorname{def} \right] \right]_{S} \\ & \left[ \left[ \operatorname{def} \operatorname{defS} \right] \right]_{SS} \ \widehat{=} \ \left[ \left[ \operatorname{def} \right] \right]_{S} \\ & \left[ \left[ \operatorname{defS} \right] \right]_{SS} \end{split} 
[\![ \textbf{actors} : \texttt{Actor}; \ \textbf{vars} : \texttt{VarsList}; \ \textbf{frags} : \texttt{InteractionFragment}]\!]_S \ \widehat{=} \ [\![ \textbf{frags} ]\!]_{FS}
             ((((\parallel a : \mathsf{actors}(a_1, ..., a_n) \bullet \mathsf{alpha}(a) \circ \mathsf{lifeline}(a))
               [str, par, terminate] [control(parFrags, strFrags))
               | [ {alt, opt, loop, guard, terminate} ] | Guard(altFrags, loopFrags, optFrags))
               ||[sharedVars \cup \{terminate\}]||Memory) \setminus \{alt, opt, loop, guard, str, par\}||
              alpha(a) = (\alpha(a_x, frags) \cap \alpha(a_{x+1}, frags)
             \frac{\boxed{\text{lifeline(a)}}}{Control(\text{parFrags}, \text{strFrags})} = \begin{bmatrix} \text{frags}_n \end{bmatrix}_{(a)}^{\vec{F}} \dots \ \S \ \begin{bmatrix} \text{frags}_n \end{bmatrix}_{(a)}^{\vec{F}} \\ = Parallel(\text{parFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{terminate\} \ ] \mid \ Strict(\text{strFrags}) \mid [ \ \{ter
              channel alt: IDs.Int
              channel opt: IDs.Int
              channel loop: IDs.Int
              channel par: IDs.Int
              {\it channel}\ str:\ IDs.Int
              channel guard: IDs.Int.Int.Bool
              datatype \; IDs \; = \; ID\_ALT \; | \; ID\_OPT \; | \; ID\_LOOP \; | \; ID\_PAR \; | \; ID\_STR
              \begin{split} & \| \mathsf{frags} \|_{FS} \ \widehat{=} \ \| \mathsf{frag} \|_F \\ & \| \mathsf{frag } \ \mathsf{frags} \|_{FS} \ \widehat{=} \ \| \mathsf{frag} \|_F \ \| \mathsf{frags} \|_{FS} \end{split} 
 \left[\!\!\left[ \underbrace{(\mathrm{wait}(\mathsf{x}) \ \mathrm{on} \ \mathrm{a})} : \mathtt{Wait} \mathtt{Occurrence} \right]\!\!\right]_F = Wait(\mathsf{x}) 
\overline{[\![(\mathrm{wait}([\mathsf{v},\mathsf{y}])\ \mathrm{on}\ \mathrm{a}): \mathtt{Wait}\mathtt{Occurrence}]\!]_{\scriptscriptstyle F}}\ =\ (\sqcap\ x:\{\mathsf{v}..\mathsf{y}\}\bullet\mathit{wait}(x))
[(\text{deadline}(x) b) : \text{DeadlineFragment}]_F = Deadline(b, x)
[\![(\text{destroy on a}): \text{DestroyOccurrence}]\!]_F = \textit{terminate} \rightarrow \textit{Skip}
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Guard(altFrags, loopFrags, optFrags) =
    (Evaluation(altFrags, loopFrags, optFrags) \mid [alphaCounters \cup \{terminate\}] \mid Counters)
     \ \ \ \ alpha Counters
    channel getCount: ID.Int.Int
    channel setCount: ID.Int.Int
    alphaCounters = \{getCount, setCount\}
    Counter\_ID\_x(count) = getCount.ID.x!count \rightarrow Counter\_ID\_x(count)
         \Box setCount.ID.x?y \rightarrow Counter\_ID\_x(y)
         \Box terminate \rightarrow Skip
    Counters = (\parallel \mathsf{ID} : IDs, \mathsf{x} : \{0..n\} \bullet \{terminate\} \circ Counter\_\mathsf{ID}\_\mathsf{x}(0))
    Evaluation(altFrags, loopFrags, optFrags) =
         reset_counters a guards_response(altFrags, loopFrags, optFrags)
    reset\_counters = {}_{\S} \mathsf{ID} : IDs, \mathsf{x} : \{0..n\} \bullet setCount. \mathsf{ID}. \mathsf{x} ! 0 \rightarrow Skip
    guards_response(altFrags, loopFrags, optFrags) =
          (\mathrm{id} = \mathrm{id}(\mathrm{altFrag})) \& (\mathrm{alt\_eval}([\![\mathsf{altFrag}]\!]_{\mathrm{AF}}))) \ \ \S \ \ \mathit{guards\_response}
         \Box opt?ID\_OPT.id \rightarrow (\llbracket \mathsf{optFrag} : \mathsf{OptFragment} \rrbracket_{\mathsf{OF}} : \mathsf{optFrags} \bullet
              (id = id(optFrag))\&(opt\_eval([optFrag]_{OF}))) \  guards\_response
          \label{eq:loop} $$\square$ $\overline{loop?ID\_LOOP.id} \to ([[\mathsf{loopFrag}: \texttt{LoopFragment}]]_{\mathrm{LF}}: \mathsf{loopFrags} \bullet $
              (\mathrm{id} = \mathrm{id}(\mathsf{loopFrag})) \& (\mathrm{loop\_eval}([\![\mathsf{loopFrag}]\!]_{\mathrm{LF}}))) \ \S \ \mathit{guards\_response}
         \Box \overline{terminate \rightarrow Skip}
    alt_eval(altFrag) =
         (variable : getFragmentGuardVariables([[altFrag]]_{AF}) \bullet 
         (\text{get}_{\text{variable}}) \rightarrow) (\text{[[altFrag]]}_{\text{C}})
    alt_{-}(a, x) = [altFrag]_{AF}
    opt_{eval}((optFrag) =
         (variable : getFragmentGuardVariables([optFrag]]_{OF}) \bullet
         (get_{variable} \rightarrow)) ([optFrag]_{G})
    opt_{-}(a, x) = [optFrag]_{OF}
    loop_eval((loopFrag) ≘
         \overline{\text{(variable : getFragmentGuardVariables([[loopFrag]]_{LF})}} \bullet
         (\text{get}_{\text{variable}} \rightarrow)) ([[loopFrag]]_{G}))
    loop_{-}(\mathbf{a}, \mathbf{x}) = [[loopFrag]]_{LF}
```

```
\begin{split} & [[\mathsf{altFrag}: \mathsf{XAltFragment}]]_F = \mathit{alt.ID\_ALT}.\underline{\mathrm{id}}(\mathsf{altFrag}) \to \mathit{Skip} \\ & [[\mathsf{optFrag}: \mathsf{OptFragment}]]_F = \mathit{opt.ID\_OPT}.\underline{\mathrm{id}}(\mathsf{optFrag}) \to \mathit{Skip} \\ & [[\mathsf{loopFrag}: \mathsf{LoopFragment}]]_F = \mathit{loop.ID\_LOOP}.\underline{\mathrm{id}}(\mathsf{loopFrag}) \to \mathit{Skip} \\ & [[\mathsf{strFrag}: \mathsf{StrFragment}]]_F = \mathit{str.ID\_STR}.\underline{\mathrm{id}}(\mathsf{strFrag}) \to \mathit{Skip} \\ & [[\mathsf{parFrag}: \mathsf{ParFragment}]]_F = \mathit{par.ID\_PAR}.\underline{\mathrm{id}}(\mathsf{parFrag}) \to \mathit{Skip} \end{split}
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```
[[loopFrag:LoopFragment]]_G =
    not(condition)\&
    (setCount.ID\_LOOP.id(loopFrag)!0 \rightarrow
    guard.ID\_LOOP.id(loopFrag).1! false \rightarrow Skip)
    ((count < min) and condition) &
    (setCount.ID\_LOOP.id(loopFrag)!(count + 1) \rightarrow
    guard.ID\_LOOP.id(loopFrag).1!true \rightarrow Skip)
    (count == max)\&
    (setCount.ID\_LOOP.id(loopFrag)!0 \rightarrow
    guard.ID\_LOOP.id(loopFrag).1!false \rightarrow Skip)
     (not(count < min) \ and \ not(count >= max) and \ condition) \&
    (setCount.ID\_LOOP.id(loopFrag)!(count + 1) \rightarrow
    guard.ID\_LOOP.id(loopFrag).1!true \rightarrow Skip)
    ((count >= min) \ and \ (count < max) \ and \ condition)\&
    ((setCount.ID\_LOOP.id(loopFrag)!(count + 1) \rightarrow
    guard.ID\_LOOP.id(loopFrag).1!true \rightarrow Skip) \sqcap
    (setCount.ID\_LOOP.id(\overline{\mathsf{loopFrag}})!0 \rightarrow
    guard.ID\_LOOP.id(loopFrag).1! false \rightarrow Skip))),
\underline{\mathrm{if}}\ \mathsf{loopFrag} \in \llbracket (\mathrm{loop}(\mathsf{min},\mathsf{max})[\mathsf{condition}]) : \mathtt{LoopFragment} \rrbracket_{\mathit{LF}}
[\![ \mathsf{loopFrag} : \mathtt{LoopFragment} ]\!]_G =
    getCount.ID\_LOOP.id(loopFrag)?count \rightarrow (
    (count < min)&
    (setCount.ID\_LOOP.id(loopFrag)!(count + 1) \rightarrow
    guard.ID\_LOOP.id(loopFrag).1!true \rightarrow Skip)
     (count == defaultMax)\&
    (setCount.ID\_LOOP.id(loopFrag)!0 \rightarrow
    guard.ID\_LOOP.id(loopFrag).1! false \rightarrow Skip)
    (not(count < min) \ and \ not(count >= defaultMax))\&
    (setCount.ID\_LOOP.id(loopFrag)!(count + 1) \rightarrow
    guard.ID\_LOOP.id(loopFrag).1!true \rightarrow Skip)
    (count > = min \ and \ count < \underline{defaultMax})\&
    ((setCount.ID\_LOOP.id(loopFrag)!(count + 1) \rightarrow
    guard.ID\_LOOP.id(loopFrag).1!true \rightarrow Skip) \sqcap
    (setCount.ID\_LOOP.id(loopFrag)!0 \rightarrow
    guard.ID\_LOOP.id(loopFrag).1! false \rightarrow Skip))),
\underline{\mathrm{if}}\;\mathsf{loopFrag} \in \llbracket (\mathrm{loop}(\overline{\mathsf{min}})) : \mathtt{LoopFragment} \rrbracket_{\mathit{LF}}
```

```
[\![ \mathsf{loopFrag} : \mathtt{LoopFragment} ]\!]_G =
    getCount.ID\_LOOP.id(loopFrag)?count \rightarrow (
    not(condition)\&
    (setCount.ID\_LOOP.\mathrm{id}(\mathsf{loopFrag})!0 \rightarrow
    guard.ID\_LOOP.id(loopFrag).1!false \rightarrow Skip)
    (count == \underline{defaultMax})\&
    (setCount.ID\_LOOP.id(loopFrag)!0 \rightarrow
    guard.ID\_LOOP.id(loopFrag).1!false \rightarrow Skip)
    (not(count >= \underline{defaultMax}) \ and \ condition == true) \&
    (setCount.ID\_LOOP.id(loopFrag)!(count + 1) \rightarrow
    guard.ID\_LOOP.id(loopFrag).1!true \rightarrow Skip)),
\underline{if} \ \mathsf{loopFrag} \in \llbracket (\mathsf{loop}[\mathsf{condition}]) : \mathsf{LoopFragment} \rrbracket_{IF}
[[loopFrag:LoopFragment]]_G =
    getCount.ID\_LOOP.id(loopFrag)?count \rightarrow (
    not(condition)\&
    (setCount.ID\_LOOP.id(loopFrag)!0 \rightarrow
    guard.ID\_LOOP.id(loopFrag).1! false \rightarrow Skip)
    ((count < min) and condition) &
    (setCount.ID\_LOOP.id(loopFrag)!(count + 1) \rightarrow
    guard.ID\_LOOP.id(loopFrag).1!true \rightarrow Skip)
     (count == defaultMax)\&
    (setCount.ID\_LOOP.id(loopFrag)!0 \rightarrow
    guard.ID\_LOOP.id(loopFrag).1!false \rightarrow Skip)
    (not(count < min) \ and \ not(count >= defaultMax) \ and \ condition)\&
    (setCount.ID\_LOOP.id(loopFrag)!(count + 1) \rightarrow
    guard.ID\_LOOP.\mathrm{id}(\mathsf{loopFrag}).1!true \to \mathbf{Skip})
     ((count >= min) \ and \ (count < defaultMax) \ and \ condition)\&
    ((setCount.ID\_LOOP.id(loopFrag)!(count + 1) \rightarrow
    guard.ID\_LOOP.id(loopFrag).1!true \rightarrow Skip) \sqcap
    (setCount.ID\_LOOP.id(loopFrag)!0 \rightarrow
    guard.ID\_LOOP.id(loopFrag).1!false \rightarrow Skip))),
\underline{\mathrm{if}}\ \mathsf{loopFrag} \in \llbracket (\mathsf{loop}(\mathsf{min})[\mathsf{condition}]) : \mathtt{LoopFragment} \rrbracket_{LF}
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```
[[loopFrag:LoopFragment]]_G =
    getCount.ID\_LOOP.id(loopFrag)?count \rightarrow (
    (count < min)\&
    (setCount.ID\_LOOP.id(loopFrag)!(count + 1) \rightarrow
    guard.ID\_LOOP.id(loopFrag).1!true \rightarrow Skip)
    (count == max)\&
    (setCount.ID\_LOOP.id(loopFrag)!0 \rightarrow
    guard.ID\_LOOP.id(loopFrag).1!false \rightarrow Skip)
    (not(count < min) \ and \ not(count >= max))\&
    (setCount.ID\_LOOP.id(loopFrag)!(count + 1) \rightarrow
    guard.ID\_LOOP.id(loopFrag).1!true \rightarrow Skip)
    (count >= min \ and \ count < max)\&
    ((setCount.ID\_LOOP.id(loopFrag)!(count + 1) \rightarrow
    guard.ID\_LOOP.id(loopFrag).1!true \rightarrow Skip) \sqcap
    (setCount.ID\_LO\overline{OP.id}(\mathsf{loopFrag})!0) \rightarrow
    guard.ID\_LOOP.id(loopFrag).1! false \rightarrow Skip))),
\underline{\mathrm{if}}\ \mathsf{loopFrag} \in \llbracket (\mathsf{loop}(\overline{\mathsf{min}}, \mathsf{max})) : \mathtt{LoopFragment} \rrbracket_{LF}
[[loopFrag:LoopFragment]]_G =
    getCount.ID\_LOOP.id(loopFrag)?count \rightarrow (
    (count < \underline{defaultMin})&
    (setCount.ID\_LOOP.id(loopFrag)!(count + 1) \rightarrow
    guard.ID\_LOOP.id(loopFrag).1!true \rightarrow Skip)
    (count == \underline{defaultMax})\&
    (setCount.ID\_LOOP.id(loopFrag)!0 \rightarrow
    guard.ID\_LOOP.id(loopFrag).1! false \rightarrow Skip)
    (not(count < defaultMin) and not(count >= defaultMax))\&
    (setCount.ID\_LOOP.id(loopFrag)!(count + 1) \rightarrow
    guard.ID\_LOOP.id(loopFrag).1!true \rightarrow Skip)
    (count > = \underline{defaultMin} \ and \ count < \underline{defaultMax})\&
    (setCount.ID\_LOOP.id(loopFrag)!(count + 1) \rightarrow
    guard.ID\_LOOP.\mathrm{id}(\mathsf{loopFrag}).1!true \to \mathbf{Skip})),
\underline{\text{if loopFrag}} \in \llbracket (\text{loop}) : \texttt{LoopFragment} \rrbracket_{LF}
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not((g_1_0\&g_1_1\&...\&g_1_n))\&
       (guard.ID\_OPT.id(optFrag).1!false)
\underline{\mathrm{if}} \ \mathsf{optFrag} \in \llbracket (\mathrm{opt} \ [\mathsf{g_0} \& \mathsf{g_1} \& ... \& \mathsf{g_n}] \ \mathsf{x_1} \ \mathsf{end}) : \mathsf{OptFragment} \rrbracket_{\mathit{OF}}
[altFrag:AltFragment]_G =
        (guard.ID\_ALT.id(altFrag).1?true \rightarrow guard.ID\_ALT.id(altFrag).2?false \rightarrow
       \dots \rightarrow guard.ID\_ALT.id(altFrag).n!false)
        П
       (\textit{guard}.\textit{ID\_ALT}.\text{id}(\mathsf{altFrag}).1? \textit{false} \ \rightarrow \ \textit{guard}.\textit{ID\_ALT}.\text{id}(\mathsf{altFrag}).2? \textit{true} \ \rightarrow \ \textit{guard}.
       \dots \rightarrow guard.ID\_ALT.id(altFrag).n!false)
        П
        (guard.ID\_ALT.id(altFrag).1?false \rightarrow guard.ID\_ALT.id(altFrag).2?false \rightarrow
        \dots \rightarrow guard.ID\_ALT.id(altFrag).n!true)
       (guard.ID\_ALT.id(altFrag).1?false \rightarrow guard.ID\_ALT.id(altFrag).2?false \rightarrow
        \dots \rightarrow guard.ID\_ALT.id(altFrag).n!false),
\underline{\text{if}} \text{ altFrag} \in [(\text{alt } x_1 \text{ else } x_2 \text{ else } ... \text{ } x_n \text{ end}) : \text{AltFragment}]_{A.F.}
[[altFrag:AltFragment]]_G =
        (g_0\&g_1\&...\&g_n)\&(guard.ID\_ALT.id(altFrag).1!true)
        not((g_0\&g_1\&...\&g_n))\&
        (guard.ID\_ALT\_id([[altFrag]]_{AF}).1!false),
\underline{\mathrm{if}} \ \mathsf{altFrag} \in \llbracket (\mathrm{alt} \ [\mathsf{g_0} \& \mathsf{g_1} \& ... \& \mathsf{g_n}] \ \mathrm{x_1} \ \mathrm{end}) : \mathsf{AltFragment} \rrbracket_{\mathit{AF}}
[[altFrag:AltFragment]]_G =
        (\mathsf{g}\_1_0\&\mathsf{g}\_1_1\&...\&\mathsf{g}\_1_\mathsf{n}) \& (\mathit{guard}.\mathit{ID}\_\mathit{ALT}.\mathrm{id}(\mathsf{altFrag}).1!\mathit{true})
        not((g_{-1_0}\&g_{-1_1}\&...\&g_{-1_n}))\&
        (guard.ID_ALT.id(altFrag).1!false),
\underline{\mathrm{if}} \ \mathsf{altFrag} \in \llbracket (\mathrm{alt} \ [\mathsf{g\_1}_0 \& \mathsf{g\_1}_1 \& ... \& \mathsf{g\_1}_\mathsf{n}] \ \mathrm{x_1} \ \mathrm{else} \ \mathrm{x_2} \ \mathrm{end}) : \mathsf{AltFragment} \rrbracket_{A.F.}
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 $(\mathsf{g}\_1_0\&\mathsf{g}\_1_1\&...\&\mathsf{g}\_1_\mathsf{n})\&(\mathit{guard}.\mathit{ID}\_\mathit{OPT}.\mathrm{id}(\mathsf{optFrag}).1!\mathit{true})$ 

 $[\![\mathsf{optFrag}: \mathsf{OptFragment}]\!]_G \ = \$ 

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[\![\mathsf{altFrag}: \mathsf{AltFragment}]\!]_G \ = \ 
     (g\_1_0\&g\_1_1\&...\&g\_1_n)\&(\mathit{guard}.\mathit{ID\_ALT}.\mathrm{id}(\mathsf{altFrag}).1!\mathit{true} \ \to \ ...
      \rightarrow guard.ID\_ALT.id(altFrag).n!false)
      (g_n_0\&g_n_1\&...\&g_n_n)\&(guard.ID\_ALT.id(altFrag).1!false \rightarrow ...
      \rightarrow guard.ID\_ALT.id(altFrag).n!true)
     not((g_{-1_0}\&g_{-1_1}\&...\&g_{-1_n}) \ or \ ... \ or \ (g_{-n_0}\&g_{-n_1}\&...\&g_{-n_n}))\&
     (guard.ID\_ALT.id(altFrag).1!false \rightarrow ...
      \rightarrow guard.ID\_ALT.id(altFrag).n!true),
\underline{\mathrm{if}} altFrag \in [(\mathrm{alt}\ [g\_1_0\&g\_1_1\&...\&g\_1_n]\ x_1\ \mathrm{else}\ ...\ \mathrm{else}
     [g\_n_0\&g\_n_1\&...\&g\_\overline{n_n}] \ x_n \ \mathrm{end}) : \texttt{AltFragment}]]_{\mathit{AF}}
[[altFrag:AltFragment]]_G =
     (g_{-1_0}\&g_{-1_1}\&...\&g_{-1_n})\&(guard.ID\_ALT.id(altFrag).1!true \rightarrow ...
      \rightarrow guard.ID\_ALT.id(altFrag).n!false)
      ...
     (g_n_0\&g_n_1\&...\&g_n_n)\&(guard.ID\_ALT.id(altFrag).1!false \rightarrow ...
      \rightarrow guard.ID\_ALT.id(altFrag).n!true)
     not((g_{-1_0}\&g_{-1_1}\&...\&g_{-1_n}) \ or \ ... \ or \ (g_{-n_0}\&g_{-n_1}\&...\&g_{-n_n}))\&
     (guard.ID\_ALT.id(altFrag).1!false \rightarrow ... \rightarrow
     guard.ID\_ALT.id(altFrag).n!true),
\underline{\mathrm{if}} \ \mathsf{altFrag} \in [\![ (\mathrm{alt} \ [g\_1_0\&g\_1_1\&...\&g\_1_n] \ \mathrm{x_1} \ \mathrm{else} \ ... \ \mathrm{else}
     [g_n_0\&g_n_1\&...\&g_n_n] x_n \text{ else } x_m \text{ end}): AltFragment]_{AF}
[\![ \mathsf{loopFrag} : \mathtt{LoopFragment} ]\!]_{LF} \; = \;
     loop.ID\_LOOP.\mathrm{id}(\mathsf{loopFrag}) \ \rightarrow \ guard.ID\_LOOP.\mathrm{id}(\mathsf{loopFrag}).1?id1 \ \rightarrow
           (id1\&(\llbracket x_1 \rrbracket_P) \ \Box \ not(id1)\&(\mathbf{Skip}))
\underline{\text{if}} \ \mathsf{loopFrag} \in \llbracket \mathsf{LoopFragment} \rrbracket_{LF}
[optFrag: OptFragment]_{OF} =
     opt.ID\_OPT.id(\mathsf{optFrag}) \rightarrow guard.ID\_OPT.id(\mathsf{optFrag}).1?id1 \rightarrow
          (id1\&(\llbracket x_1 \rrbracket_P) \ \Box \ not(id1)\&(\mathbf{Skip}))
\underline{if} \ \mathsf{optFrag} \in [\![\mathsf{OptFragment}]\!]_{OF}
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[[\mathsf{altFrag}: \mathsf{AltFragment}]]_{AF} =
      alt.ID\_ALT\_\{id\} \rightarrow guard.ID\_ALT\_\{id\}\_\{1\}?id1 \rightarrow
             guard.ID\_ALT\_\{id\}\_\{2\}?id2 \ \rightarrow \ \dots \ guard.ID\_ALT\_\{id\}\_\{n\}?idn
              \rightarrow (id1\&(\llbracket x_1 \rrbracket_P) \ \Box \ id2\&(\llbracket x_2 \rrbracket_P) \ \Box \ \dots \ idn\&(\llbracket x_n \rrbracket_P))
\underline{\mathrm{if}} altFrag \in \llbracket (\mathrm{alt} \ \mathsf{x}_1 \ \mathrm{else} \ \mathsf{x}_2 \ \mathrm{else} \ ... \ \mathsf{x}_n \ \mathrm{end}) : \mathtt{AltFragment} 
bracket{}_{A.F.}
[[\mathsf{altFrag}:\mathsf{OptFragment}]]_{AF} =
      alt.ID\_ALT.\{id\} \rightarrow guard.ID\_ALT.\{id\}.1?id1
              \rightarrow (id1\&([x_1]]_P) \square not(id1)\&(Skip))
\underline{\mathrm{if}} altFrag \in \llbracket (\mathrm{alt} \ [\mathrm{g}_0 \& \mathrm{g}_1 \& ... \& \mathrm{g}_\mathrm{n}] \ \mathsf{x}_1 \ \mathrm{end}) : \mathsf{OptFragment} 
bracket_{\mathit{AF}}
[[altFrag:AltFragment]]_{AF} =
      alt.ID\_ALT.\{id\} \rightarrow guard.ID\_ALT.\{id\}.1?id1
              \rightarrow (id1\&(\llbracket x_1 \rrbracket_P) \ \Box \ not(id1)\&(\llbracket x_2 \rrbracket_P))
\underline{\mathrm{if}} \ \mathsf{altFrag} \in \llbracket (\mathrm{alt} \ [\mathrm{g}\_1_0 \& \mathrm{g}\_1_1 \& ... \& \mathrm{g}\_1_\mathrm{n}] \ \mathsf{x_1} \ \mathrm{else} \ \underline{\mathsf{x_2}} \ \mathrm{end}) : \mathsf{AltFragment} \rrbracket_{AF}
[[altFrag:AltFragment]]_{AF} =
      alt.ID\_ALT.\{id\} \rightarrow guard.ID\_ALT.\{id\}.1?id1 \rightarrow ...
              \rightarrow guard.ID\_ALT.\{id\}.n?idn
              \rightarrow (id1\&(\llbracket x_1 \rrbracket_P) \square ... idn\&(\llbracket x_n \rrbracket_P)
              \square not(id1 or ... or idn)&(Skip))
\underline{if} altFrag \in [(alt [g_1_0\&g_1_1\&...\&g_1_n] x_1 else ... else
      [g_n_0\&g_n_1\&...\&g_n_n] \times_n end: AltFragment_{AF}
[[altFrag:AltFragment]]_{AF} =
      alt.ID\_ALT.\{id\} \rightarrow guard.ID\_ALT.\{id\}.1?id1 \rightarrow \dots
              \rightarrow guard.ID\_ALT.\{id\}.n?idn
              \rightarrow (id1\&(\llbracket \mathsf{x_1} \rrbracket_P) \ \Box \ \dots \ idn\&(\llbracket \mathsf{x_n} \rrbracket_P)
              \square not(id1 \ or \dots \ or \ idn)\&(\llbracket x_{\mathsf{m}} \rrbracket_P))
\underline{if} altFrag \in [(alt [g_1_0\&g_1_1\&...\&g_1_n] x_1 else ... else
      [g_n_0\&g_n_1\&...\&g_n_n] \times_n else \times_m end): AltFragment_{AF}
```

```
Parallel(parFrags) = \Box parFrag : parFrags \bullet
      (par.\overline{ID\_PAR}.\mathrm{id}(\llbracket \mathtt{parFrag} : \mathtt{ParFragment} \rrbracket_{\mathtt{PF}}) 	o
       \| \text{thread} : \text{parFrag}.\underline{\text{threads}} \bullet parallel\_(id([[parFrag]]_{PF}), id(varsthread))) \|
      parallel\_(id, threadID) = || actor : [[parFrag]]_{PF}.threadID.actors] \bullet
            parallel\_(\mathsf{actor}, \mathsf{id}, \mathsf{threadID})
      parallel\_(a, id, threadID) = \S frag : [[parFrag]]_{PF}.threadID.interactionFragments \bullet [[frag]]_{(a)}^{F}
Strict(\mathsf{strFrags}) = \square \ \mathsf{strFrag} : \mathsf{strFrags} \bullet
      (\mathit{str}.ID\_\overline{\mathit{STR}}.\mathrm{id}(\llbracket \mathsf{strFrag} : \mathtt{StrFragment} \rrbracket_{\mathrm{SF}}) \to \mathit{strict}\_(\mathrm{id}(\llbracket \mathsf{strFrag} \rrbracket_{\mathrm{SF}}))
      strict\_(id) = 3 interactionFrags : [strFrag]]_{SF}.interactionFragments
[(a_1 -> a_2: mID!var): InteractionFragment]]_F \stackrel{\widehat{=}}{=}
      \mathsf{a}_1 = \mathsf{mID!}\mathsf{var} \, 	o \, \mathit{Skip}
      \mathsf{a_2} = \mathsf{mID}?\mathsf{var} \, 	o \, \mathit{set}\_\mathsf{var}!\mathsf{var} \, 	o \, \mathit{Skip}
[(a_1 -> a_2: mID?var): InteractionFragment]]_F \stackrel{\widehat{=}}{=}
      \mathsf{a}_1 \ = \ \mathsf{mID} ? \mathsf{var} \ \to \ \mathit{set}\_\mathsf{var} ! \mathsf{var} \ \to \ \mathit{Skip}
      \mathsf{a_2} \ = \ \mathsf{mID!}\mathsf{var} \ 	o \ \mathit{Skip}
[(a_1 -> a_1: mID?var): InteractionFragment]_F \stackrel{\widehat{=}}{=}
      \mathsf{a}_1 = \mathsf{mID}?\mathsf{var} \, 	o \, \mathit{set}\_\mathsf{var}!\mathsf{var} \, 	o \, \mathit{Skip}
[(a_1 -> a_2: mID): InteractionFragment]_F \stackrel{\widehat{=}}{=}
     \mathsf{a}_1 \; = \; \mathsf{mID} \; 	o \; \mathit{Skip}
      \mathsf{a}_2 \ = \ \mathsf{mID} \ \to \ \textit{Skip}
```

```
Key
[]]_D - > RoboHumansDocument
[\![\!]\!]_{\mathit{CS}}-> Capabilities
[]]_{SDS}-> SequenceDiagramGroup
[]]_{SD}->An\ instance\ of\ {\tt SequenceDiagramGroup}
[]]_{CO} - > Constants
[\![\!]]_{LS}-> LifelineBlock
[]]_{TU}^{-}> TimeUnit
[]]_{CONS} - > ConstAssignment
[\![\!]]_{CON}->An\ instance\ of\ {\it ConstAssignment}
\parallel \parallel_{OS} -> Out
[\![]\!]_O - > An \ instance \ of \ {\rm Out}
[\hspace{-0.05cm}]]_{IS}-> In
[\![]\!]_I - > An \ instance \ of \ {\rm In}
[\![\!]]_{\mathit{VS}}-> VarsList
[\![\!]\!]_V - > An\ instance\ of\ {\it VarsList}
|||_{TO} - > An Out LifelineEvent instance with a type
\parallel \parallel_{TI} - > An In LifelineEvent instance with a type
[[]]_{SS}-> Sequence
[]]_S - > An instance of Sequence
[\![]\!]_A -> \mathsf{Actor}
[]]_{FS}-> InteractionFragment
[]]_F - > An instance of InteractionFragment
\iiint_{(a)}^{F} - > An \ instance \ of \ InteractionFragment \ for \ Actor \ a
\prod_{G} - > The \ body \ of \ the \ evaluation \ for \ an \ Interaction Fragment \ with \ a \ Guard
[]]_{AF} - > An AltFragment
[]]_{OF} - > An OptFragment
[\![\!]]_{LF}->A LoopFragment
[]]_{PF}->A ParFragment
[]]_{SF} -> A StrFragment
|||_{P} -> An operand inside an InteractionFragment with a Guard
```