

Catlab Overview

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What is Catlab?

- Catlab is a categorical computing platform
- Catlab is based on the programming language Julia, and exploits Julia's features for domain specific languages and type-based specialization
- Catlab provides the foundation for the AlgebraicJulia ecosystem
- Catlab offers abstractions for many categorical concepts
- The core of Catlab is based on Gatlab

GATLab: Generalized Algebraic Theories & Models Thereof

- Supports diverse doctrines (ThCategory, ThSchema, ThMonoid, ThGroupoid, ThCopresheaf, ThPresheaf, FreeSymmetricMonoidalCategory, ThPointedSetCategory, etc.)
- Can create a theory within a doctrine
- Can create models of these theories that adhere to the propertiiies

Example Categorical Abstractions in Catlab

- Categories (Objects, morphisms, relations)
- Presentations of categories
- C-Sets (copresheaves)
- ACSets (attributed C-Sets)
- Slice categories
- Functors
- Natural transformations between ACSets (ACSetTransformations)
- Various set-like categories (FinSet, SkelFinSet, FinRel, ...)
- Various universal constructions (product, coproduct, pullbacks, pushouts, equalizers, coequalizers, etc.)
- Preorders
- Lattices
- Undirected & directed wiring diagrams
- Semi-simplicial sets & complexes
- Monoidal categories & symmetric monoidal categories
- Structured cospans
- Functorial data migrations

Example Categorical Operations in Catlab

- Composing morphisms
- Computing homomorphisms
- Computing representables
- Taking category of elements
- Computing universal constructions (product, coproduct, pullbacks, pushouts, equalizers, coequalizers, etc.)
- Performing categorical rewriting
- Assessing whether a morphism is monic, epic, etc.
- Assessing whether a transformation is natural

Catlab Resources

- Catlab GitHub site: <https://github.com/AlgebraicJulia/Catlab.jl>
- Catlab documentation: <https://algebraicjulia.github.io/Catlab.jl/dev/>
- AlgebraicJulia Repo <https://github.com/AlgebraicJulia>
- AlgebraicJulia information (a bit dated): <https://www.algebraicjulia.org/>
- Testing code for different structures e.g.,
 - <https://github.com/AlgebraicJulia/Catlab.jl/blob/d07b6fc4f8c95feb52b9cc16febd49e714acb540/test/theories/Category.jl>
 - <https://github.com/AlgebraicJulia/Catlab.jl/blob/d07b6fc4f8c95feb52b9cc16febd49e714acb540/test/theories/Schema.jl>
- Catlab channel of Julia zulip <https://julialang.zulipchat.com/>
- Category Theory zulip <https://categorytheory.zulipchat.com/>
- Fortnightly Catlab/AlgebraicJulia community meeting (jacobszelko@gmail.com)

Some AlgebraicJulia Projects

- AlgebraicRewriting.jl
- AlgebraicDynamics.jl
- StockFlow.jl
- Statecharts.jl
- Decapodes.jl
- ACSets.jl
- CombinatorialSpaces.jl
- SemiringFactorizations.jl
- DiagrammaticEquations.jl
- AlgebraicABMs.jl*
- AlgebraicPetri.jl*