$$C^{i-1} \xrightarrow{k} \operatorname{im} \delta_C^{i-1}$$