$$F \xrightarrow{\exists i} P \\ \downarrow 1_{P} \\ \downarrow P \\ \longrightarrow 0$$