$$\operatorname{Hom}(P,I) \longleftarrow \operatorname{Hom}(A,I)$$

$$\uparrow$$
 $\operatorname{Hom}(P,B)$