

# Convolutional Neural Networks

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Reference: Ming Li's notes



#### Introduction

 Fukushima (1980) – Neo-Cognitron; LeCun (1998) – Convolutional Neural Networks (CNN, or ConvNet);...

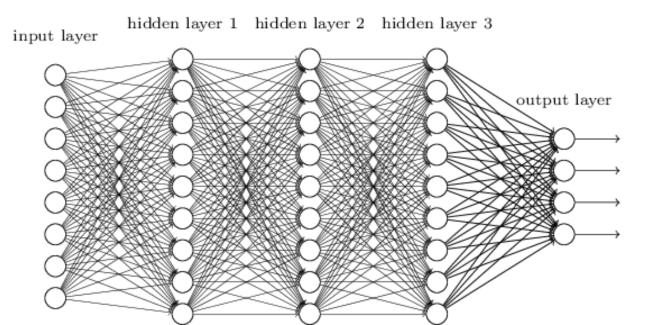
#### **Motivation:**

Images typically have 1000<sup>2</sup> pixels, which give rise to 1000<sup>2</sup> data points or features, leading to an intractably high dimension of the weight space. However, not all of them are essential due to the spatial patterns. Many of them have shared properties. Therefore, the weight space dimension can be dramatically reduced if an appropriate pre-processing of the image data is carried out to analyze or extract spatial correlations or patterns in images.



### Motivation

- We know it is good to learn a small model.
- From this fully connected model, do we really need all the edges?
- Can some of these be shared?



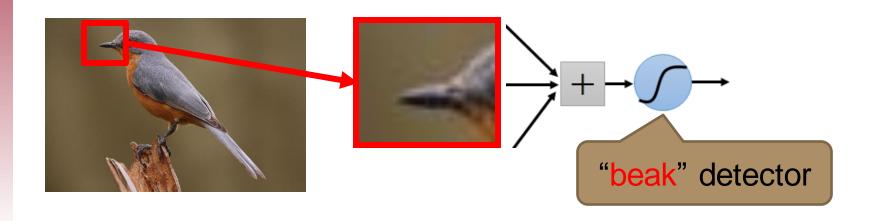


#### Motivation

Consider learning an image:

Some patterns are much smaller than the whole image

Can represent a small region with fewer parameters

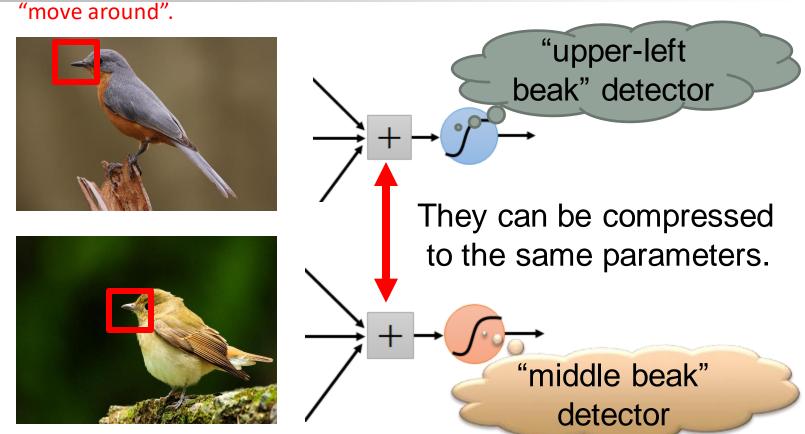




Same pattern appears in different places:

They can be compressed!

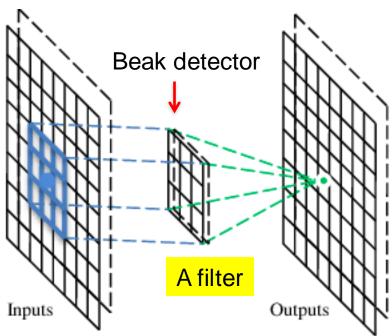
What about training a lot of such "small" detectors and each detector must





# A Convolutional Layer

A CNN is a neural network with some convolutional layers (and some other layers). A convolutional layer has a number of filters that does convolutional operation.





# Convolution These are the network

parameters to be learned.

1	0	0	0	0	1
0	1	0	0	1	0
0	0	1	1	0	0
1	0	0	0	1	0
0	1	0	0	1	0
0	0	1	0	1	0

1	-1	-1
-1	1	-1
-1	-1	1

Filter 1

-1	1	-1
-1	1	-1
-1	1	-1

Filter 2

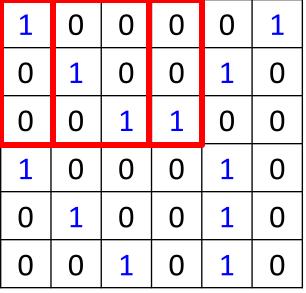
6 x 6 image

Each filter detects a small pattern (3 x 3).



## Convolution

stride=1



Dot product 3 -1

1	-1	-1
-1	1	-1
-1	-1	1

Filter 1

6 x 6 image



## Convolution

If stride=2

1	0	0	0	0	1
0	1	0	0	1	0
0	0	1	1	0	0
1	0	0	0	1	0
		U	0		U
0	1	0	0	1	0

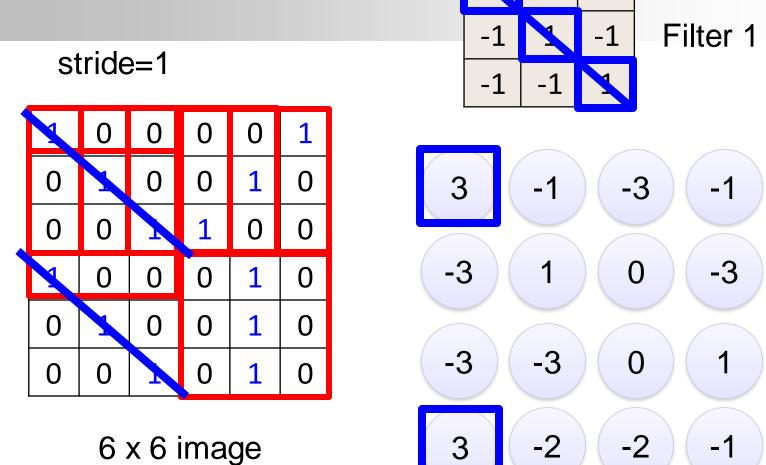
3 -3

1	-1	-1
-1	1	-1
-1	-1	1

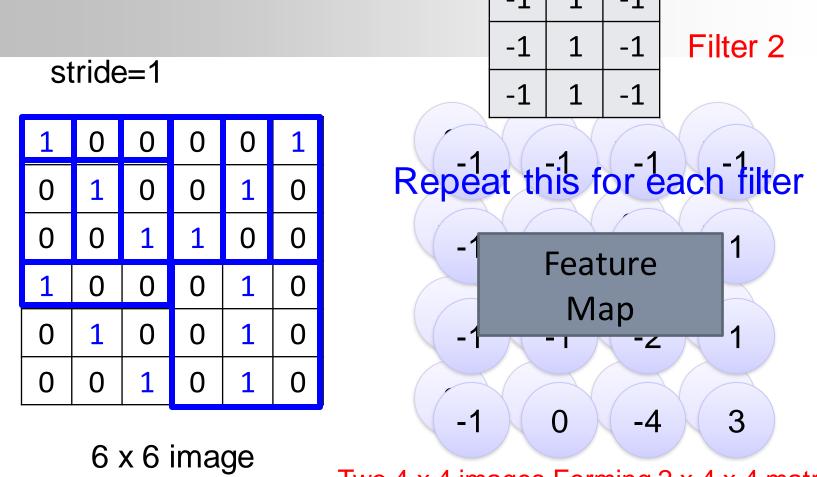
Filter 1

6 x 6 image



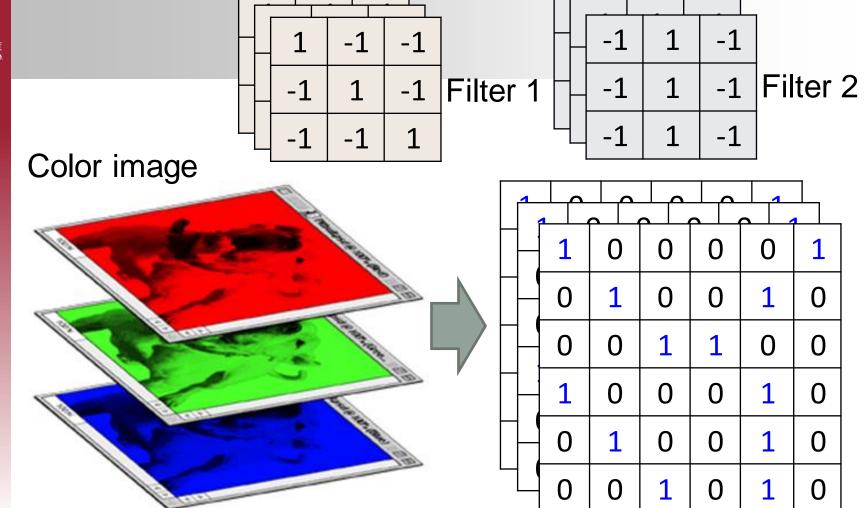




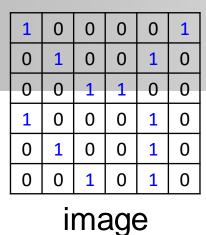


Two 4 x 4 images Forming 2 x 4 x 4 matrix









convolution

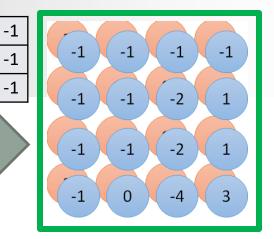
-1

-1

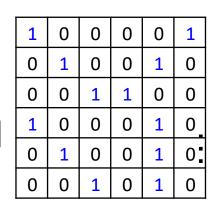
1

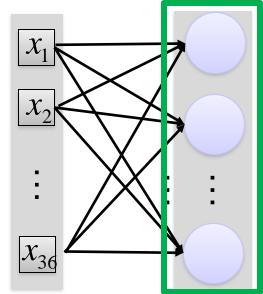
-1

-1

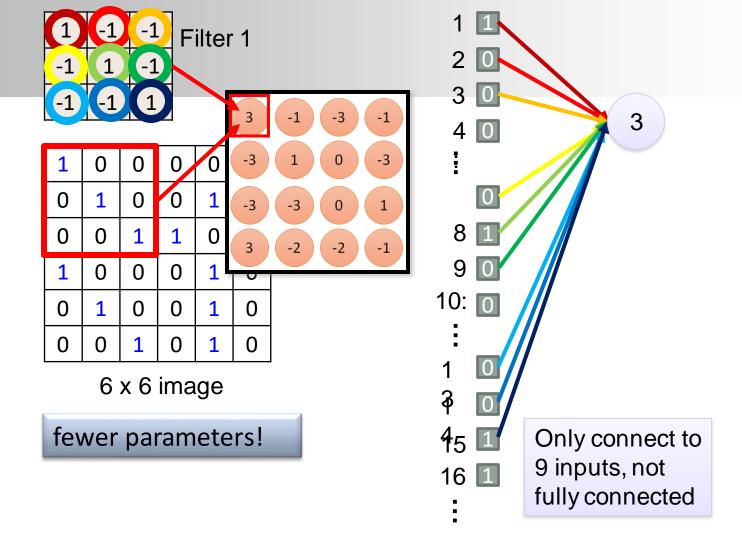


Fullyconnected

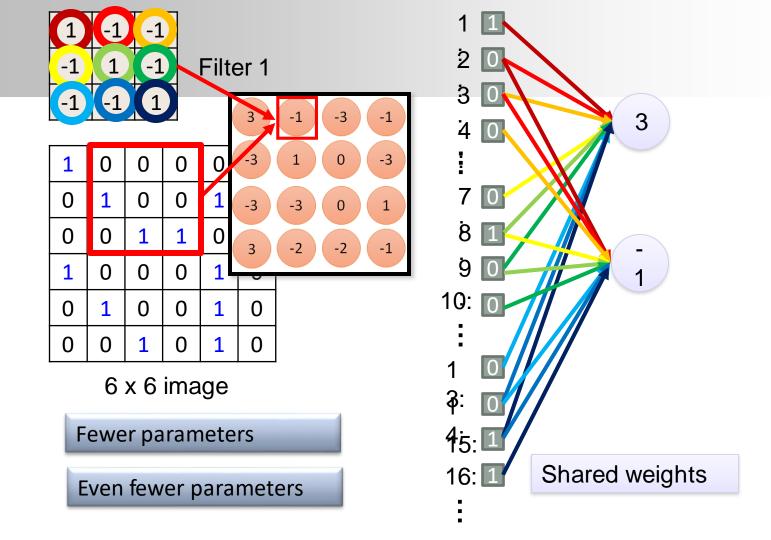






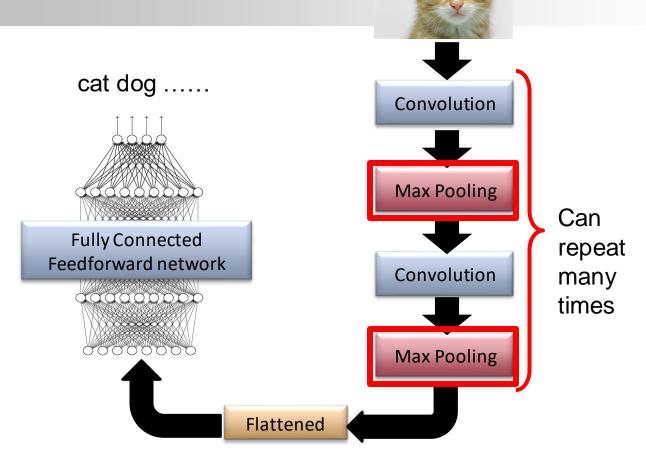






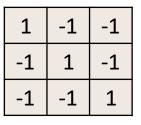


# The whole CNN





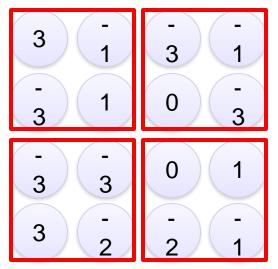
# **Max Pooling**

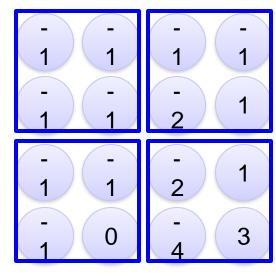


Filter 1

-1	1	-1
-1	1	-1
-1	1	-1

Filter 2







# Why Pooling

Subsampling pixels will not change the object bird



We can subsample the pixels to make image fewer parameters to characterize the image

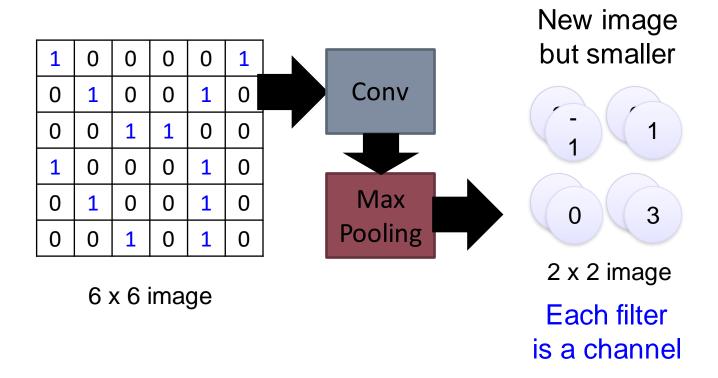


# A CNN compresses a fully connected network in two ways:

- Reducing number of connections
- Shared weights on the edges
- Max pooling further reduces the complexity



# **Max Pooling**





## The whole CNN



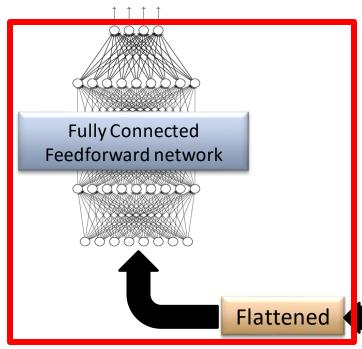
The number of channels is the number of filters

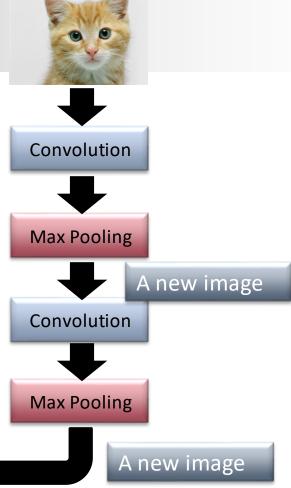
Can repeat many times



# The whole CNN

cat dog .....

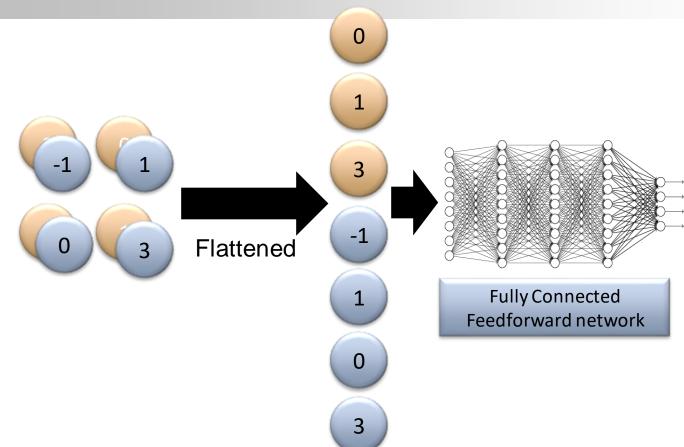






# Flattening

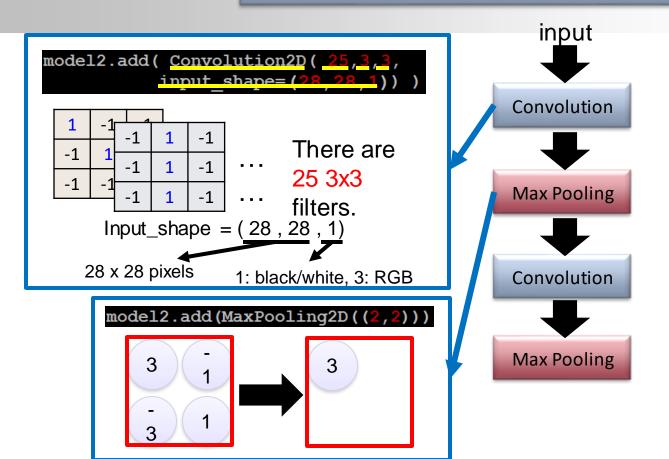
3





#### **CNN** in Keras

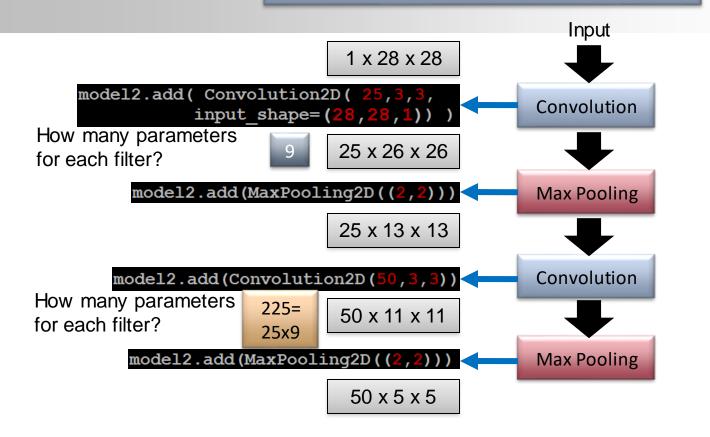
Only modified the *network structure* and *input* format (vector -> 3-D tensor)





#### **CNN** in Keras

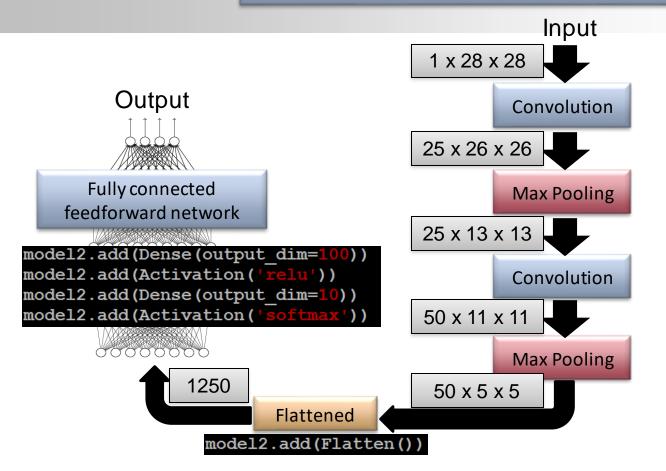
Only modified the *network structure* and *input* format (vector -> 3-D array)





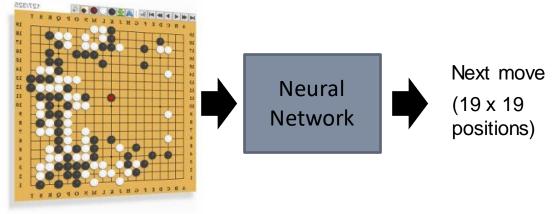
#### **CNN** in Keras

Only modified the *network structure* and *input* format (vector -> 3-D array)





# AlphaGo



19 x 19 matrix

Black: 1

white: -1

none: 0

Fully-connected feedforward network can be used

But CNN performs much better



# AlphaGo's policy network

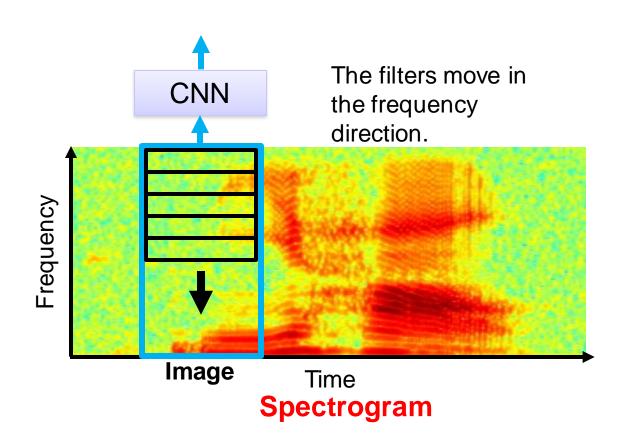
The following is quotation from their Nature article:

Note: AlphaGo does not use Max Pooling.

**Neural network architecture.** The input to the policy network is a  $\underline{19 \times 19 \times 48}$ <u>image</u> stack consisting of 48 feature planes. The first hidden layer <u>zero pads the</u> input into a 23  $\times$  23 image, then convolves k filters of kernel size 5  $\times$  5 with stride 1 with the input image and applies a <u>rectifier nonlinearity</u>. Each of the subsequent hidden layers 2 to 12 zero pads the respective previous hidden layer into a  $21 \times 21$ image, then convolves k filters of kernel size  $3 \times 3$  with stride 1, again followed by a rectifier nonlinearity. The final layer convolves 1 filter of kernel size  $1 \times 1$ with stride 1, with a different bias for each position, and applies a softmax function. The match version of AlphaGo used k = 192 filters; Fig. 2b and Extended Data Table 3 additionally show the results of training with k = 128, 256 and 384 filters.



# CNN in speech recognition





## CNN in text classification

