



Faculty of Engineering

**ECE 142: Electronic Circuits**

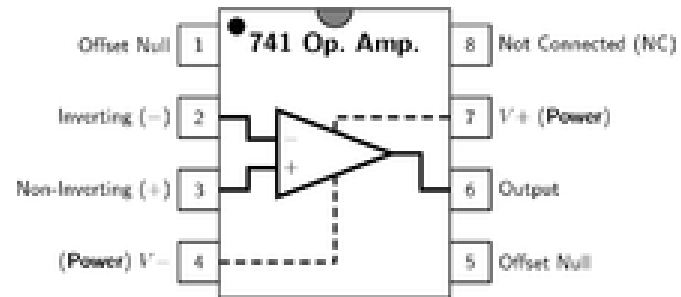
# **Lecture 17: OpAmp Circuits**

# What is an Op-Amp? – The Surface

- An Operational Amplifier (Op-Amp) is an integrated circuit that uses external voltage to amplify the input through a very high gain.
- We recognize an Op-Amp as a mass-produced component found in countless electronics.



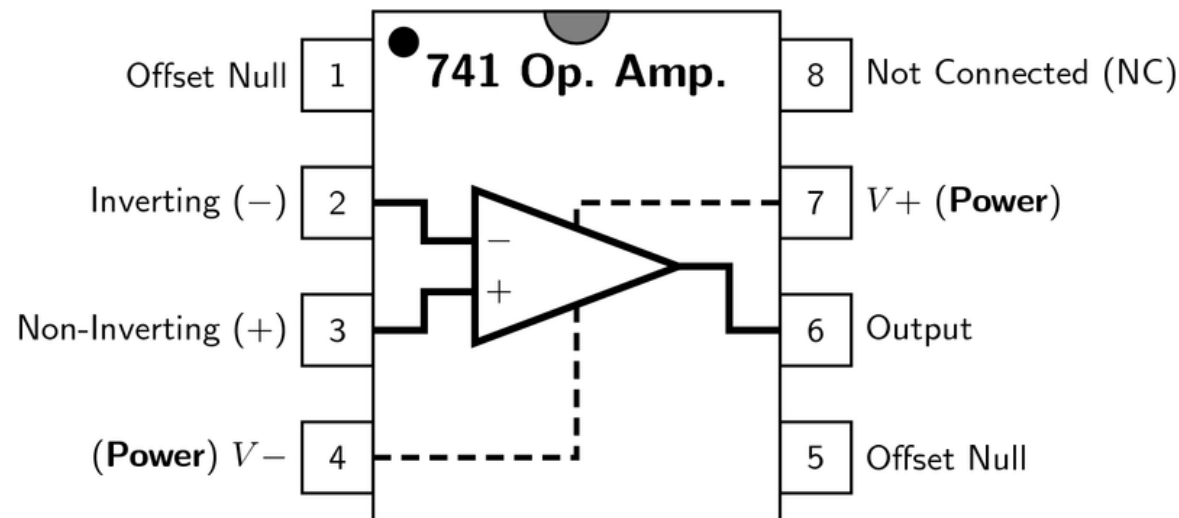
What an Op-Amp looks like to a lay-person



What an Op-Amp looks like to an engineer

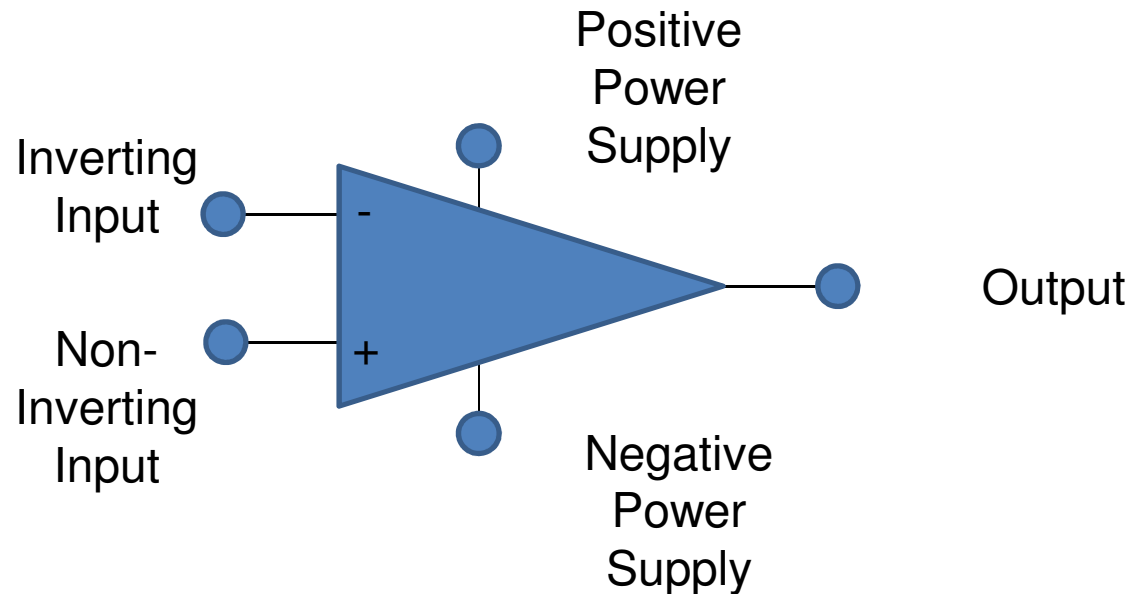
# What is an Op-Amp? – The Layout

- There are 8 pins in a common Op-Amp, like the 741 which is used in many instructional courses.



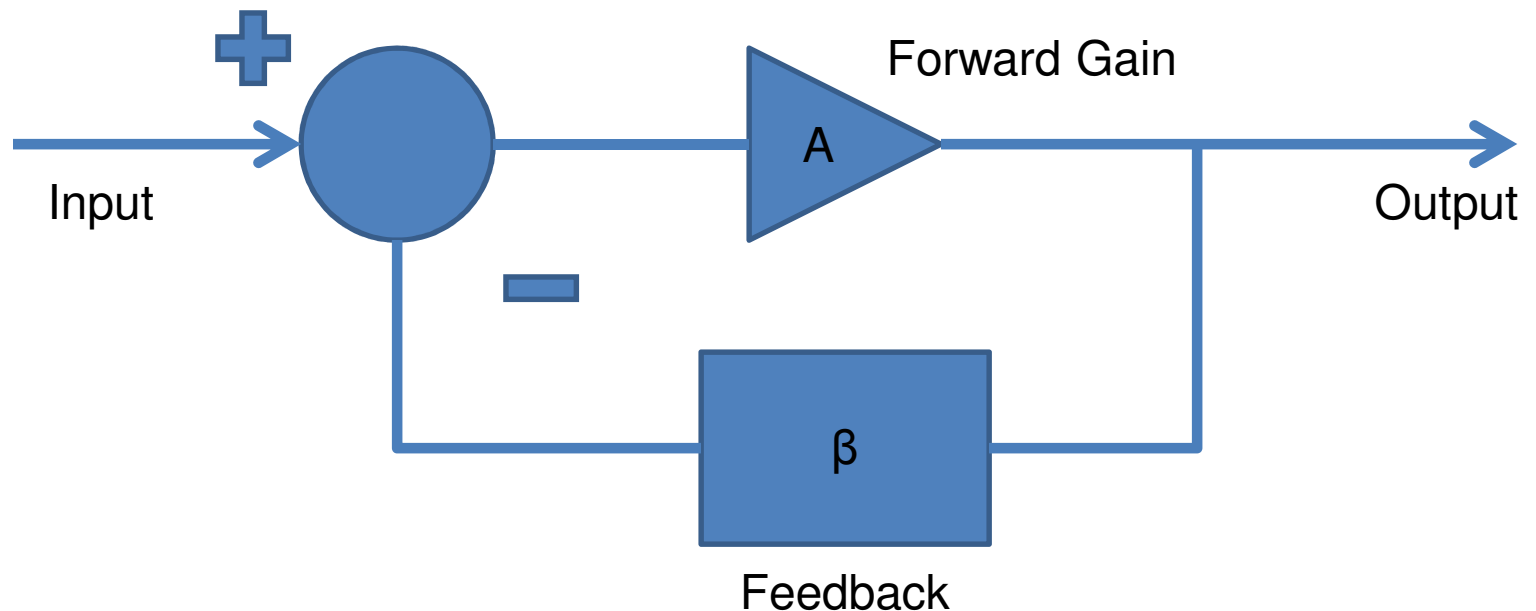
# What is an Op-Amp? – The Inside

- The actual count varies, but an Op-Amp contains several Transistors, Resistors, and a few Capacitors and Diodes.
- For simplicity, an Op-Amp is often depicted as this:



# History of the Op-Amp – The Dawn

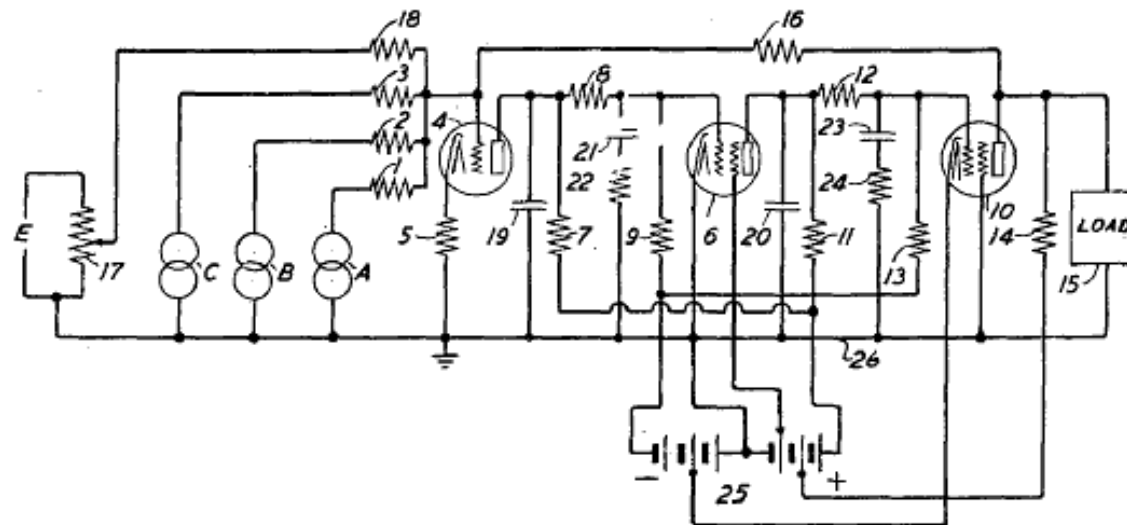
- Before the Op-Amp: Harold S. Black develops the feedback amplifier for the Western Electric Company (1920-1930)



# History of the Op-Amp – The Dawn

- **The Vacuum Tube Age**

- The First Op-Amp: (1930 – 1940) Designed by Karl Swartzel for the Bell Labs M9 gun director
- Uses 3 vacuum tubes, only one input, and  $\pm 350$  V to attain a gain of 90 dB
- Loebe Julie then develops an Op-Amp with two inputs: Inverting and Non-inverting



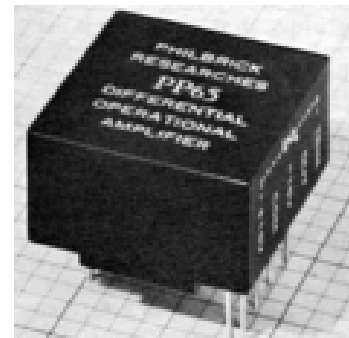
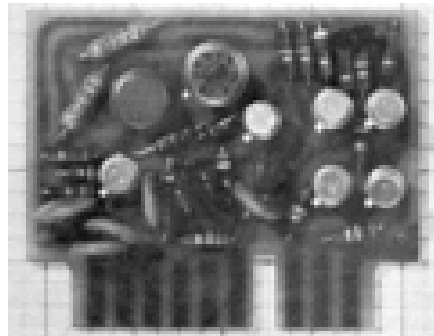
# History of the Op-Amp – The Shift

- The end of Vacuum Tubes was built up during the 1950's-1960's to the advent of solid-state electronics

1. The Transistor
2. The Integrated Circuit
3. The Planar Process

# History of the Op-Amp – The Shift

- 1960s: beginning of the Solid State Op-Amp
- Example: GAP/R P45 (1961 – 1971)
  - Runs on  $\pm 15$  V, but costs \$118 for 1 – 4
- The GAP/R PP65 (1962) makes the Op-Amp into a circuit component as a potted module





# History of the Op-Amp – The Evolution

- The solid-state decade saw a proliferation of Op-Amps
  - Model 121, High Speed FET family, etc.
- Robert J. Widlar develops the  $\mu$ A702 Monolithic IC Op-Amp (1963) and shortly after the  $\mu$ A709
- Fairchild Semiconductor vs. National Semiconductor
  - National: The LM101 (1967) and then the LM101A (1968) (both by Widlar)
  - Fairchild: The “famous”  $\mu$ A741 (by Dave Fullager 1968) and then the  $\mu$ A748 (1969)

# Mathematics of the Op-Amp

- The gain of the Op-Amp itself is calculated as:

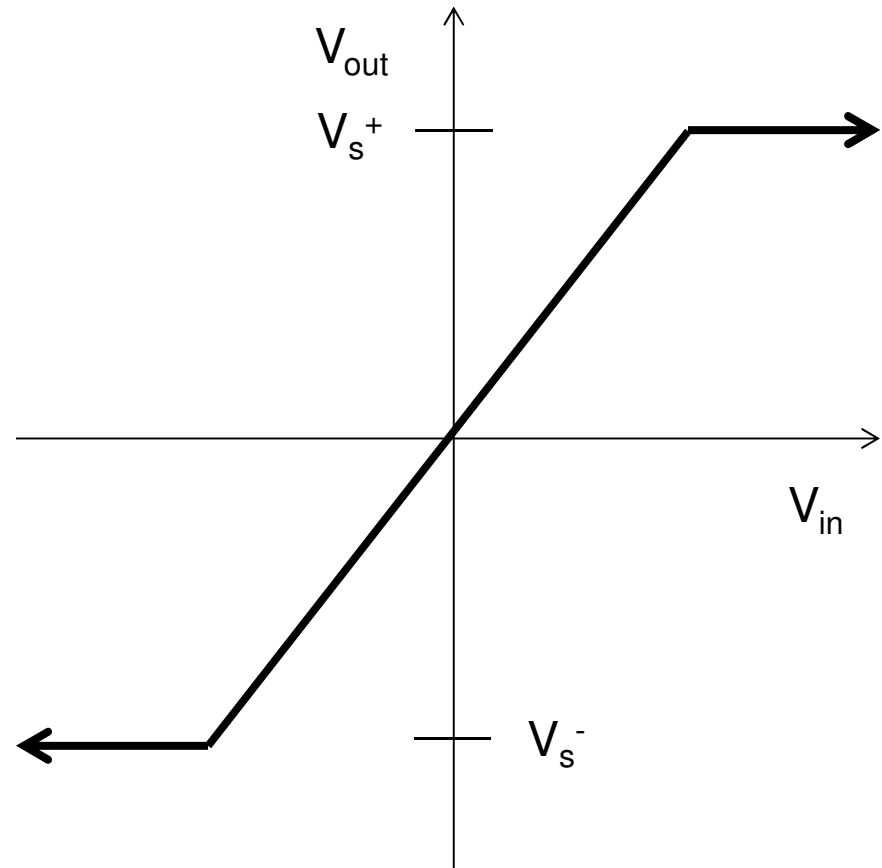
$$G = V_{\text{out}} / (V_{+} - V_{-})$$

- The maximum output is the power supply voltage
- When used in a circuit, the gain of the circuit (as opposed to the op-amp component) is:

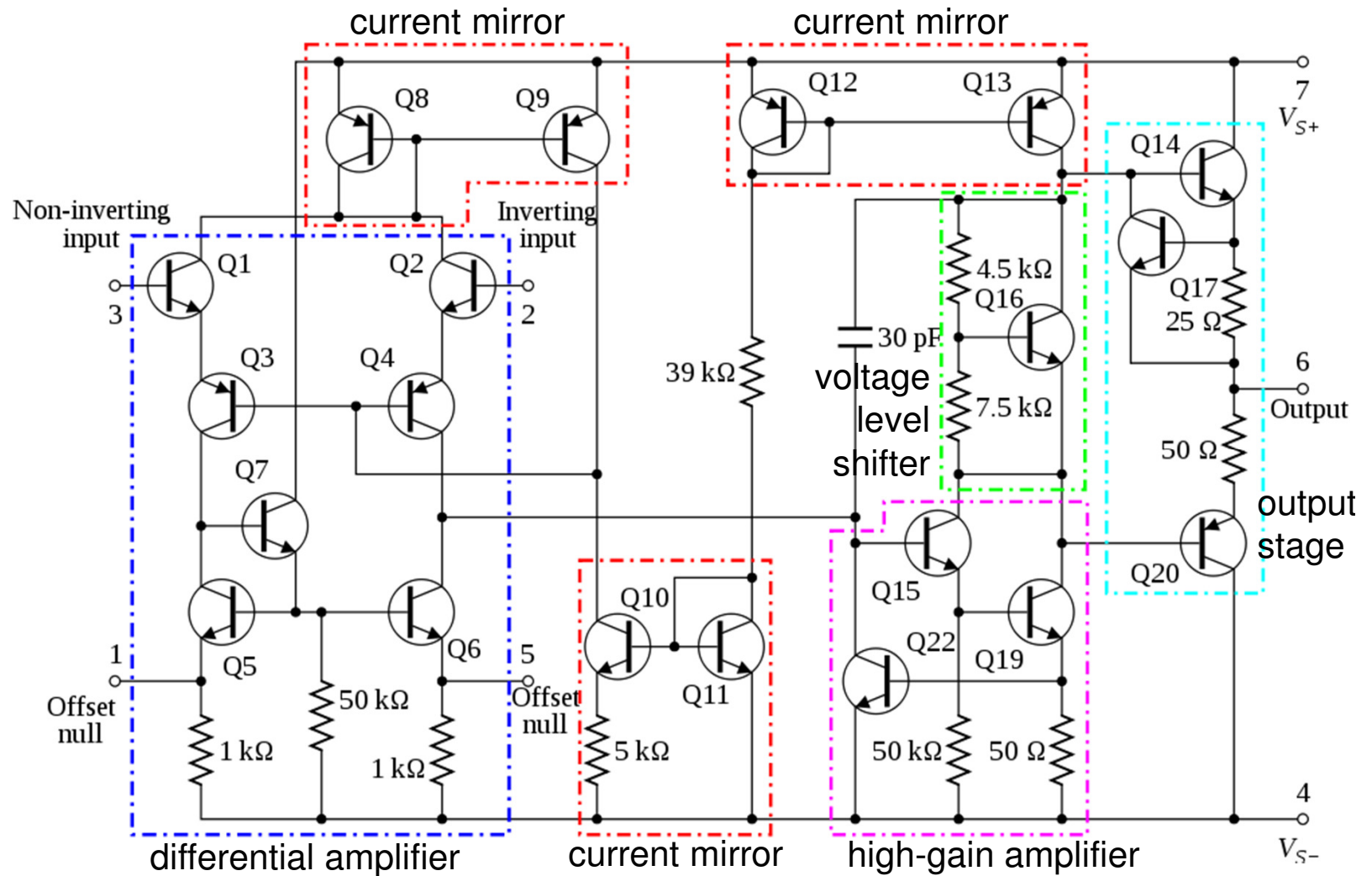
$$A_v = V_{\text{out}} / V_{\text{in}}$$

# Op-Amp Saturation

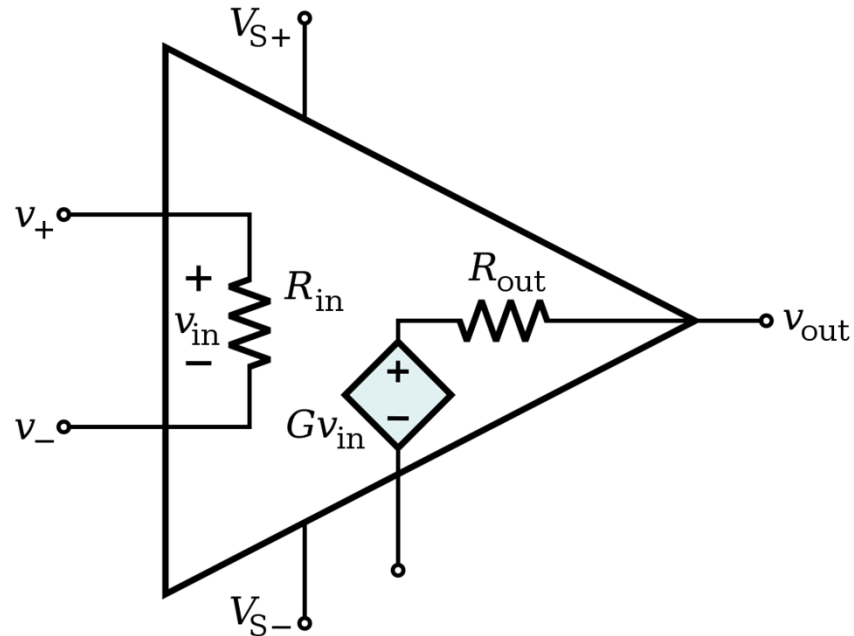
- As mentioned earlier, the maximum output value is the **supply voltage**, positive and negative.
- The gain ( $G$ ) is the slope between saturation points.



# 741 Op-Amp Schematic

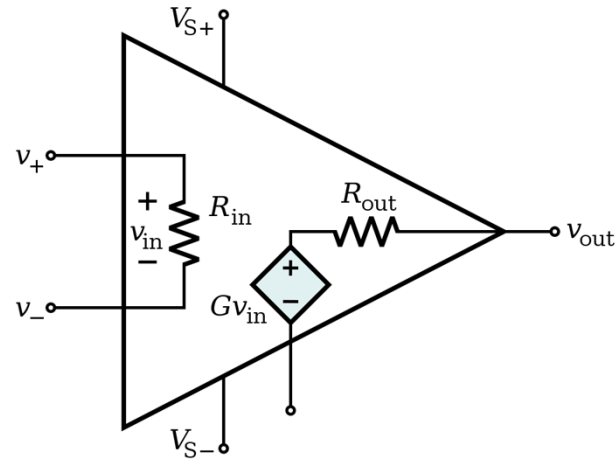


# Op-Amp Characteristics



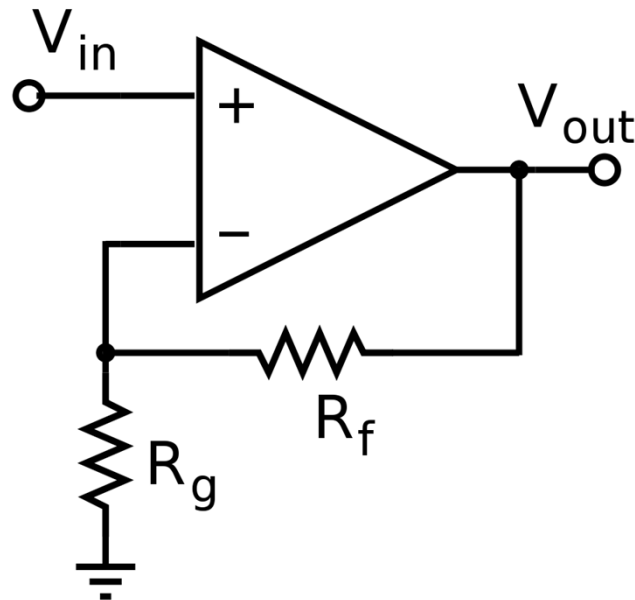
- Open-loop gain  $G$  is typically over 9000
  - But closed-loop gain is much smaller
- $R_{in}$  is very large ( $M\Omega$  or larger)
- $R_{out}$  is small ( $75\Omega$  or smaller)
  - Effective output impedance in closed loop is very small

# Ideal Op-Amp Characteristics



- Open-loop gain  $G$  is infinite
- $R_{in}$  is infinite
  - Zero input current
- $R_{out}$  is zero

# Ideal Op-Amp Analysis



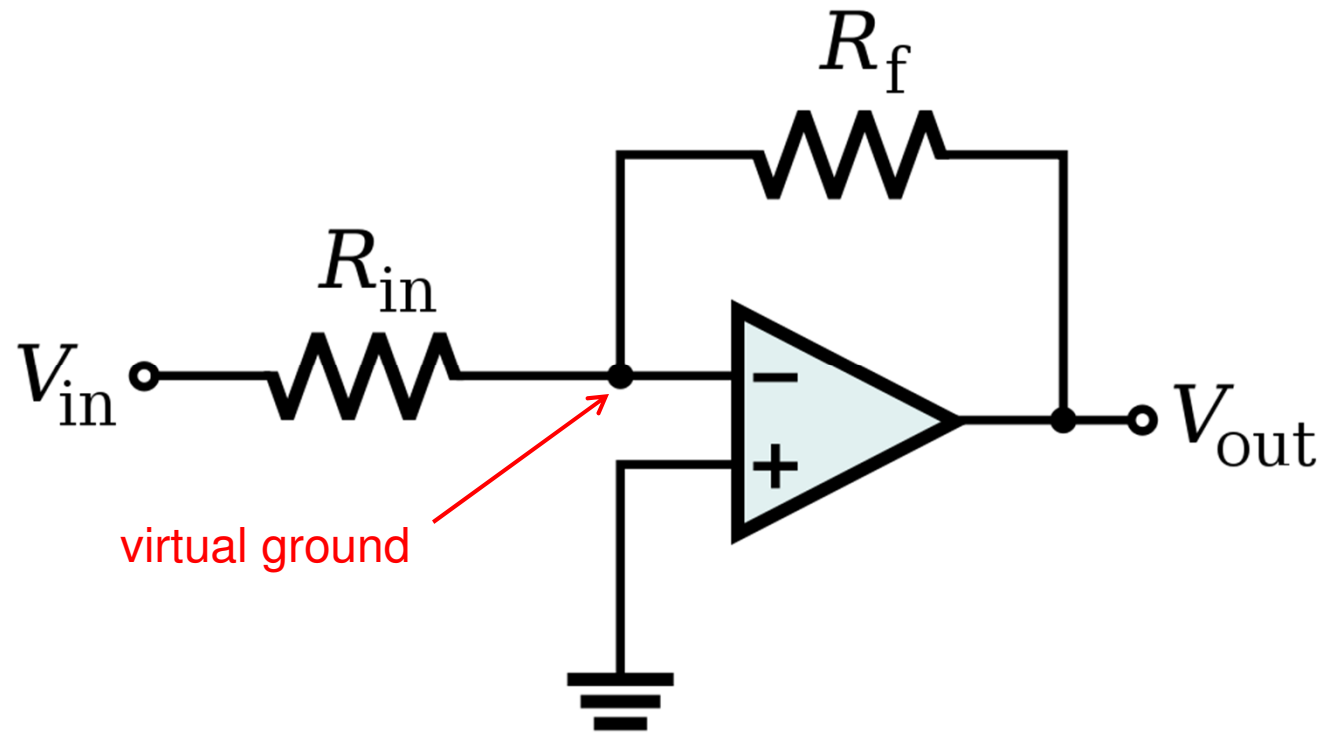
To analyze an op-amp feedback circuit:

- Assume no current flows into either input terminal
- Assume no current flows out of the output terminal
- Constrain:  $V_+ = V_-$

# **Operational Amplifiers Circuits**

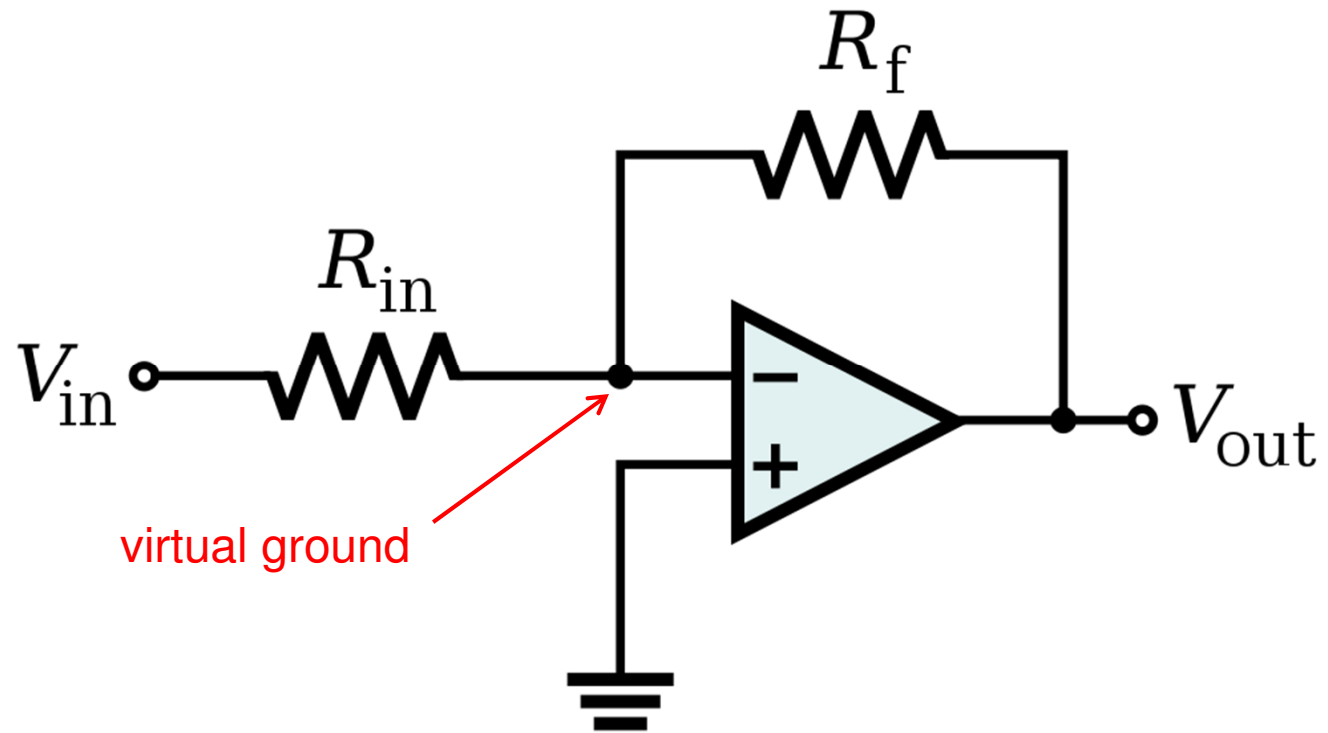


# Inverting Amplifier Analysis



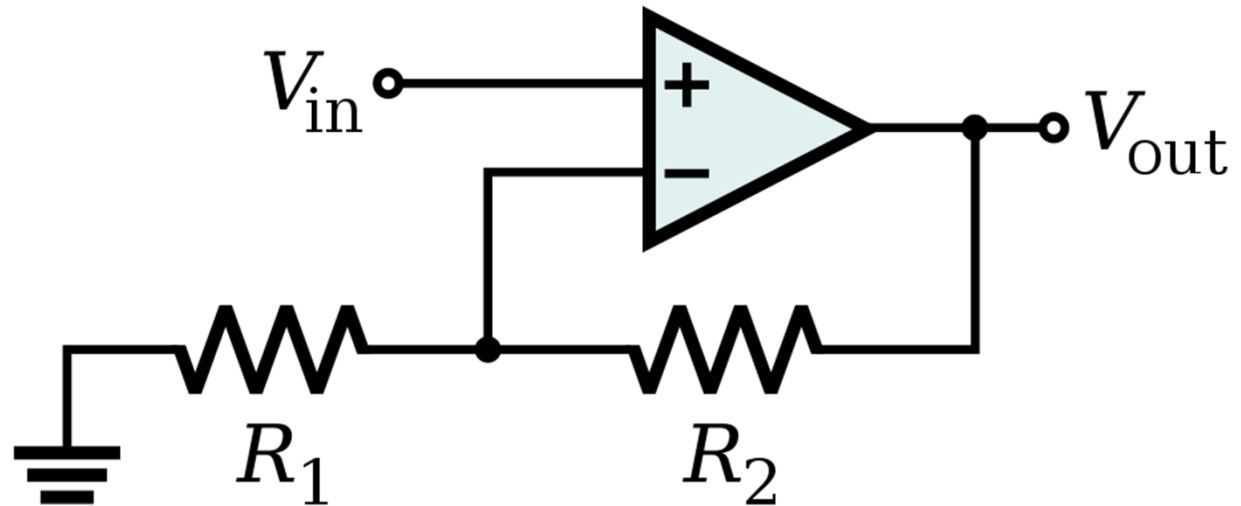
$$V_{out} = -\frac{R_f}{R_{in}} V_{in}$$

# Inverting Amplifier Analysis



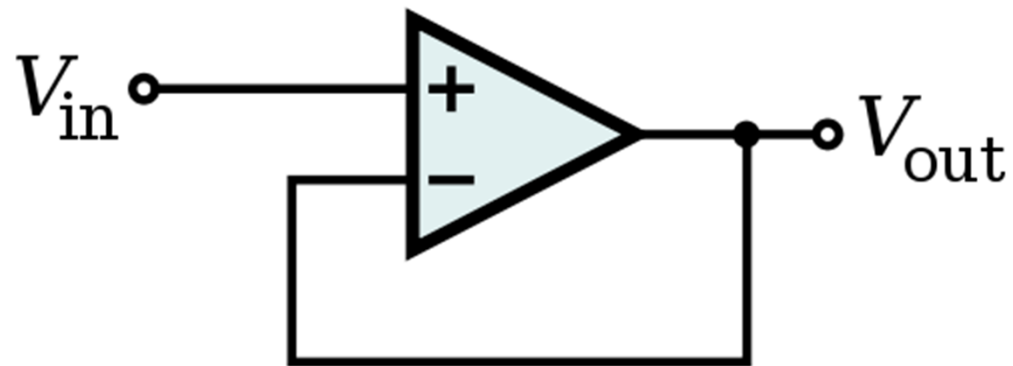
$$V_{out} = -\frac{R_f}{R_{in}} V_{in}$$

# Non-Inverting Amplifier Analysis

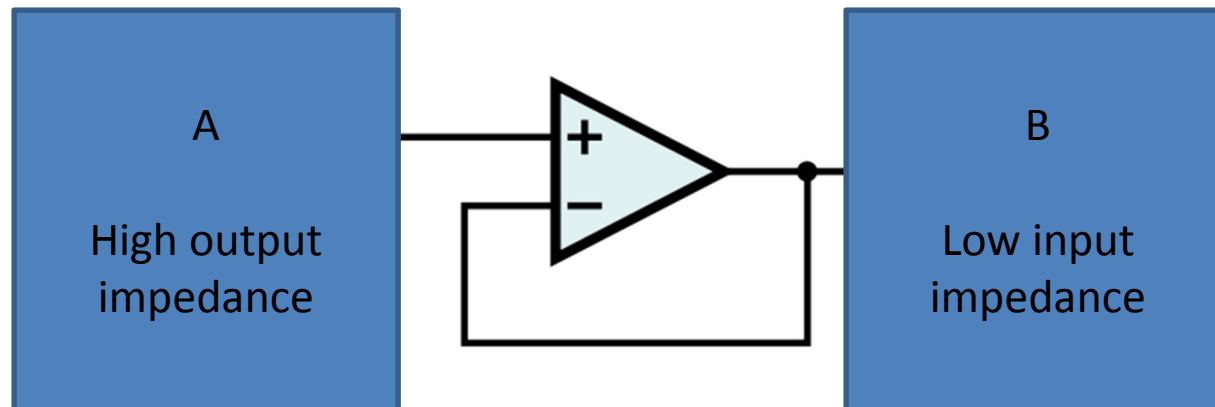


$$V_{out} = V_{in} \left( 1 + \frac{R_2}{R_1} \right)$$

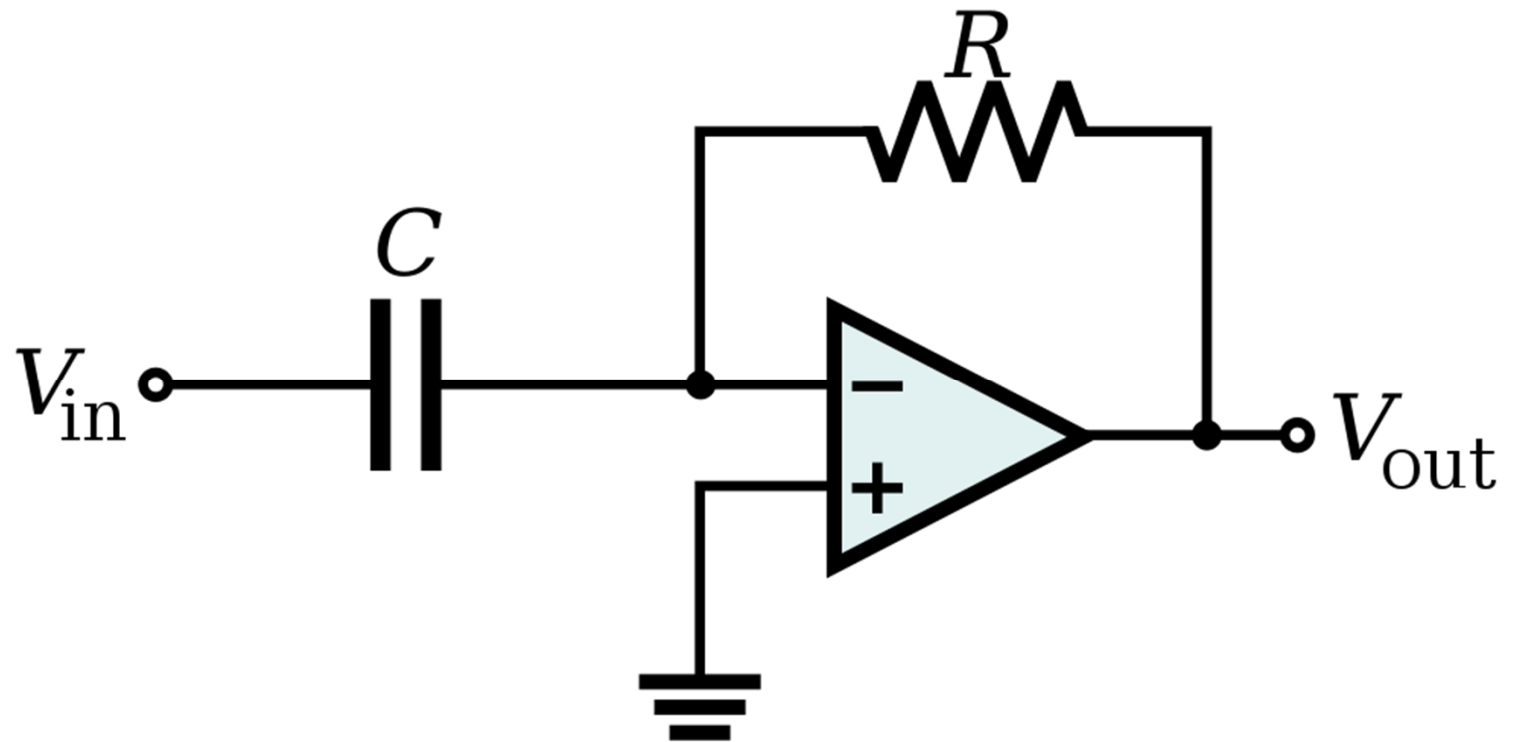
# Op-Amp Buffer



$V_{out} = V_{in}$   
Isolates loading effects

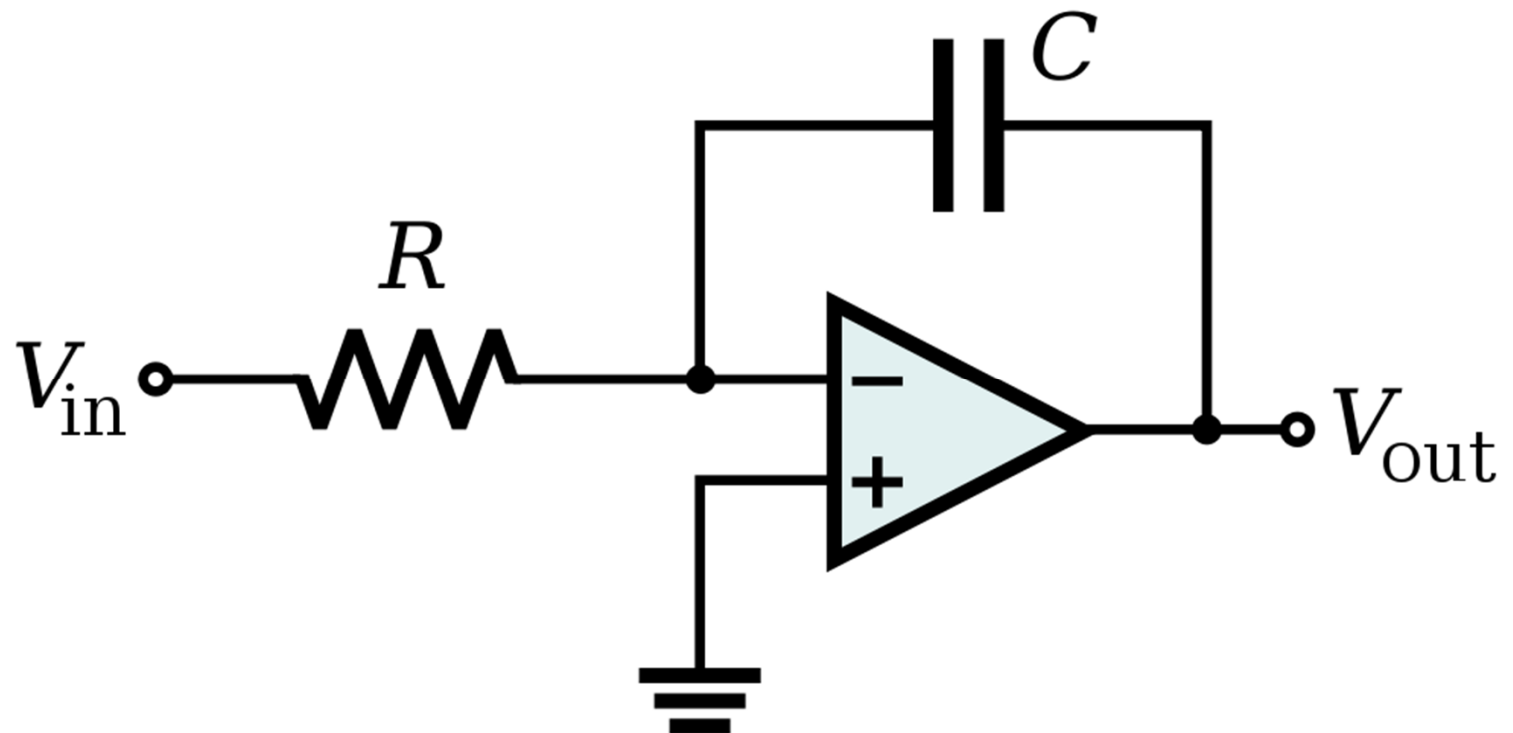


# Op-Amp Differentiator



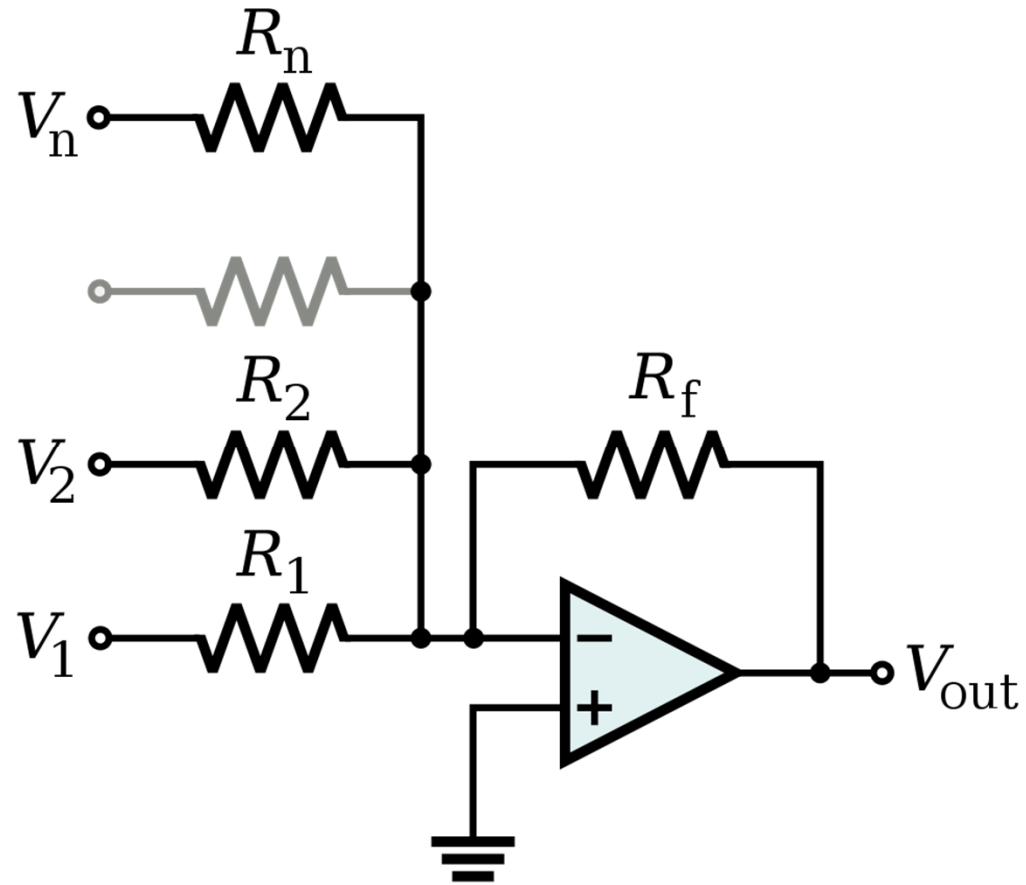
$$V_{out} = -RC \frac{dV_{in}}{dt}$$

# Op-Amp Integrator



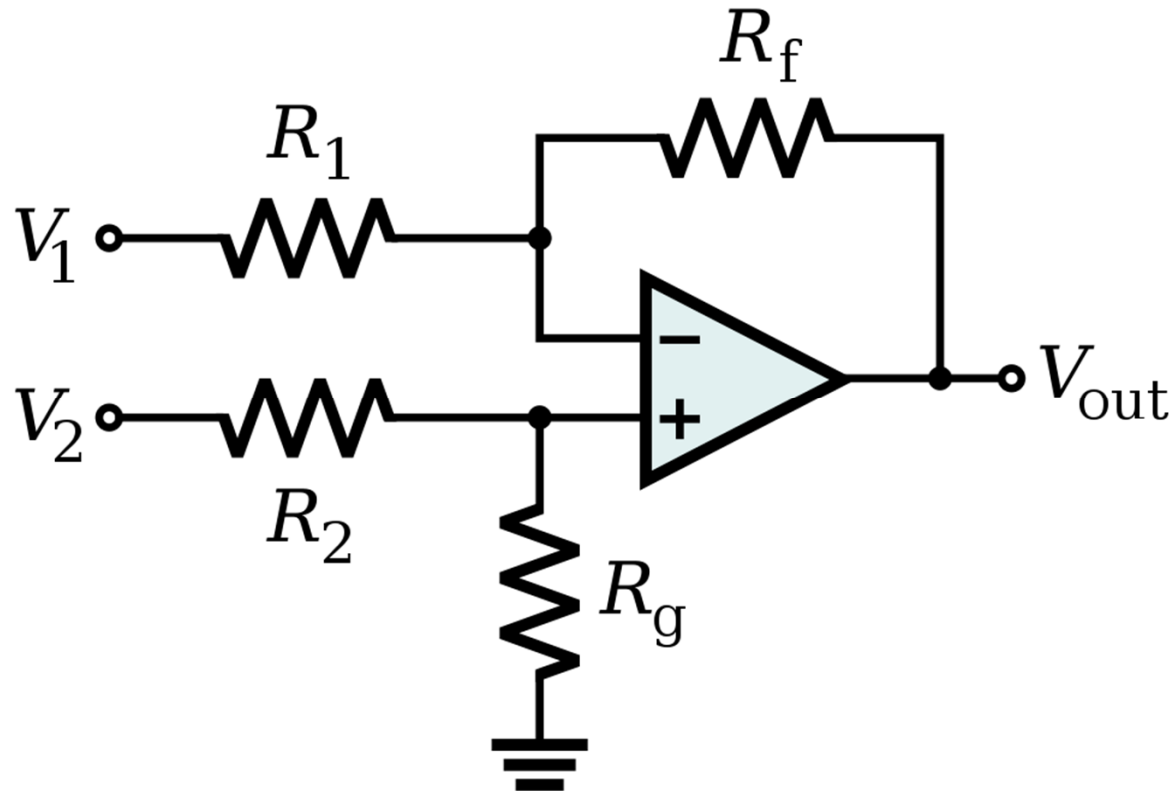
$$V_{out} = - \int_0^t \frac{V_{in}}{RC} dt + V_{initial}$$

# Op-Amp Summing Amplifier



$$V_{out} = -R_f \left( \frac{V_1}{R_1} + \frac{V_2}{R_2} + \cdots + \frac{V_n}{R_n} \right)$$

# Op-Amp Differential Amplifier



$$V_{out} = \frac{(R_f + R_1) R_g}{(R_g + R_2) R_1} V_2 - \frac{R_f}{R_1} V_1$$

If  $R_1 = R_2$  and  $R_f = R_g$ : 
$$V_{out} = \frac{R_f}{R_1} (V_2 - V_1)$$



# Applications of Op-Amps

## Filters

### Types:

- Low pass filter
- High pass filter
- Band pass filter
- Cascading (2 or more filters connected together)

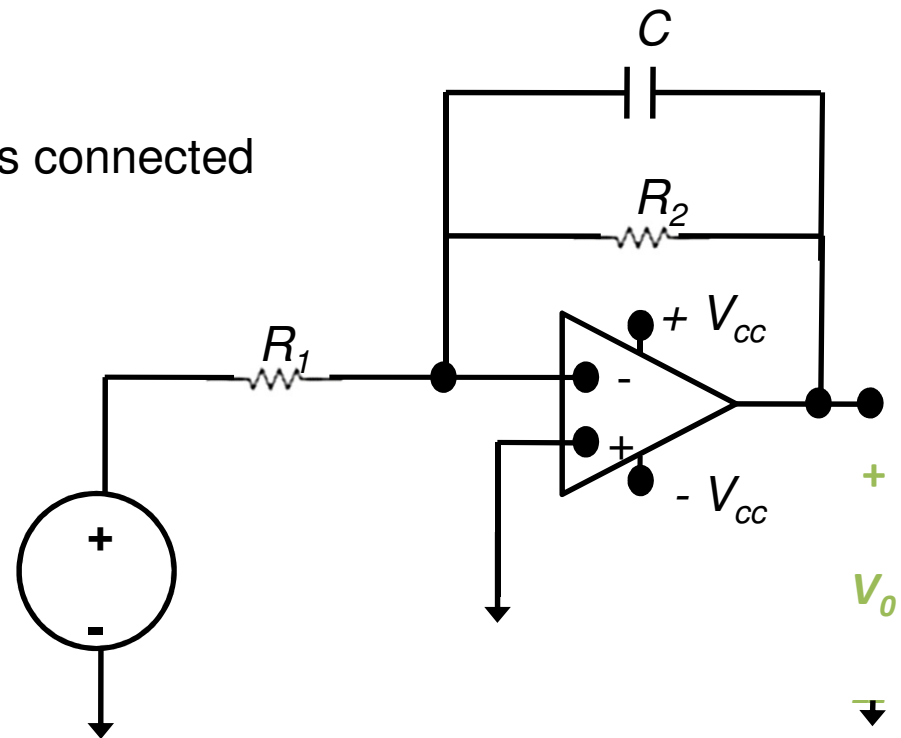
Low pass filter transfer function →

$$H(s) = \frac{-R_2 \omega_c}{sR_1 + R_1 \omega_c}$$

Low pass filter Cutoff frequency →

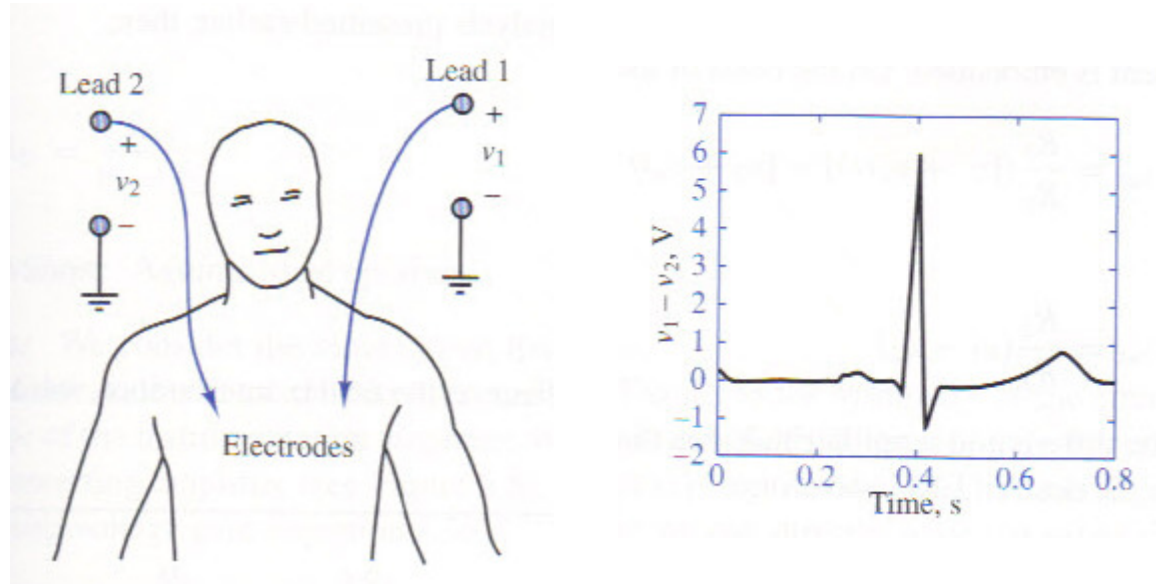
$$\omega_c = \frac{1}{R_2 C}$$

Low pass filter



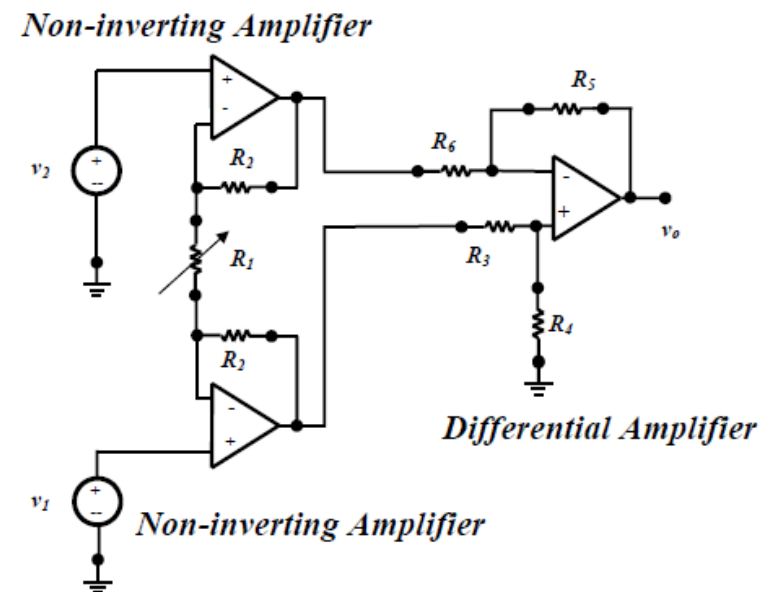
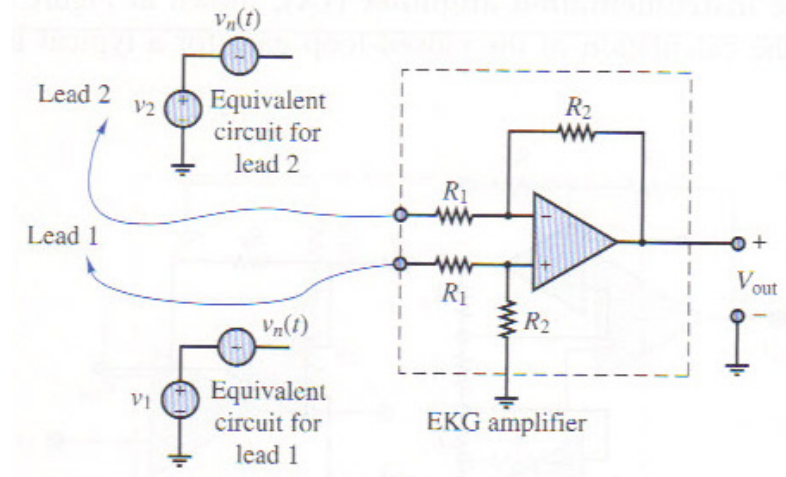
# Applications of Op-Amps

- Electrocardiogram (EKG) Amplification
  - Need to measure difference in voltage from lead 1 and lead 2
  - 60 Hz interference from electrical equipment

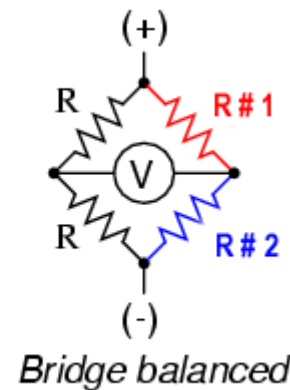
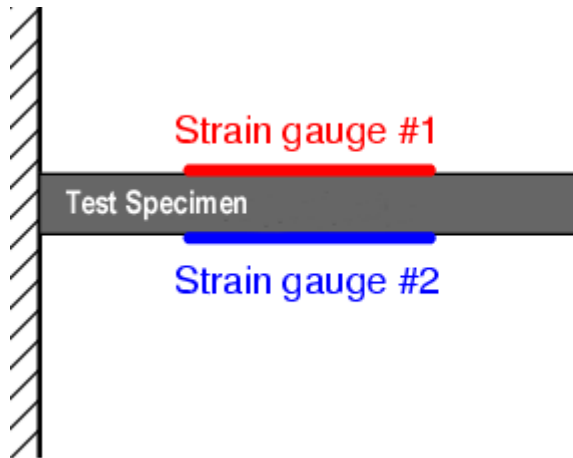


# Applications of Op-Amps

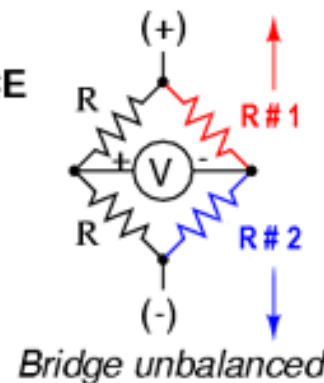
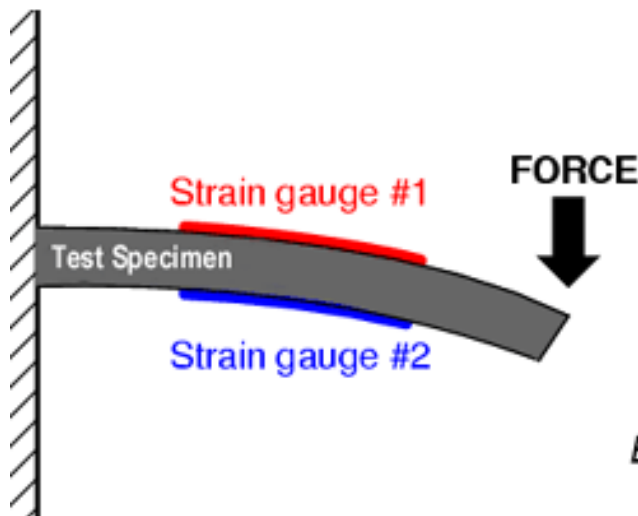
- Simple EKG circuit
  - Uses differential amplifier to cancel common mode signal and amplify differential mode signal
- Realistic EKG circuit
  - Uses two non-inverting amplifiers to first amplify voltage from each lead, followed by differential amplifier
  - Forms an “instrumentation amplifier”



# Strain Gauge



Use a Wheatstone bridge to determine the strain of an element by measuring the change in resistance of a strain gauge



(No strain) Balanced Bridge

$$R \#1 = R \#2$$

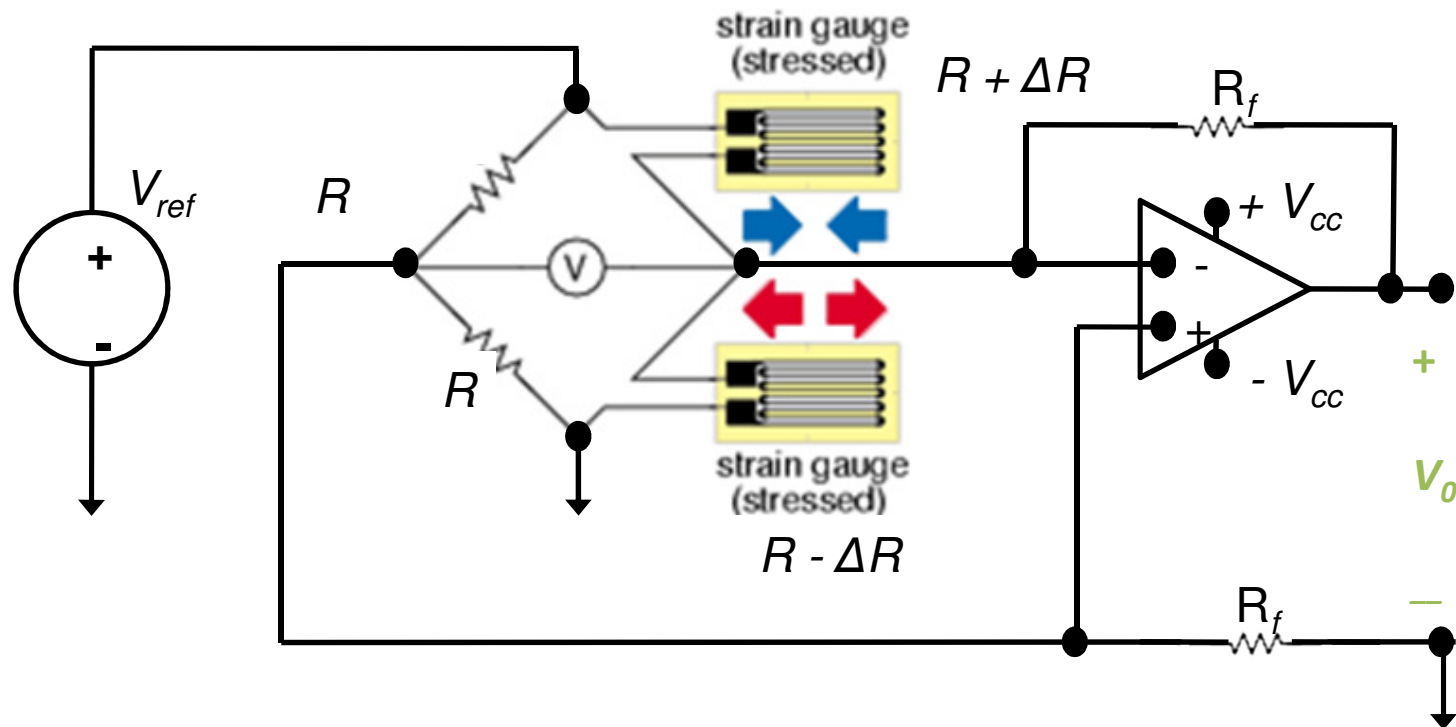
(Strain) Unbalanced Bridge

$$R \#1 \neq R \#2$$

# Strain Gauge

## Half-Bridge Arrangement

Op amp used to amplify output from strain gauge

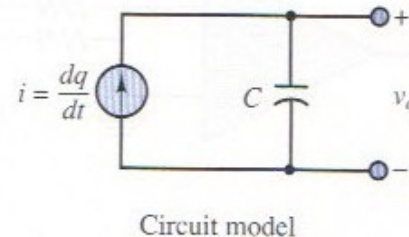
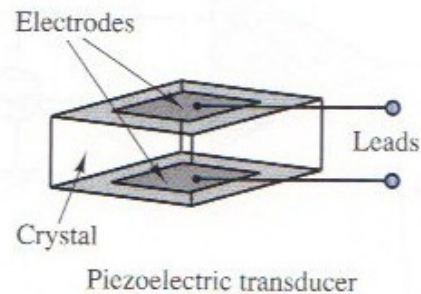


Using KCL at the inverting and non-inverting terminals of the op amp we find that →

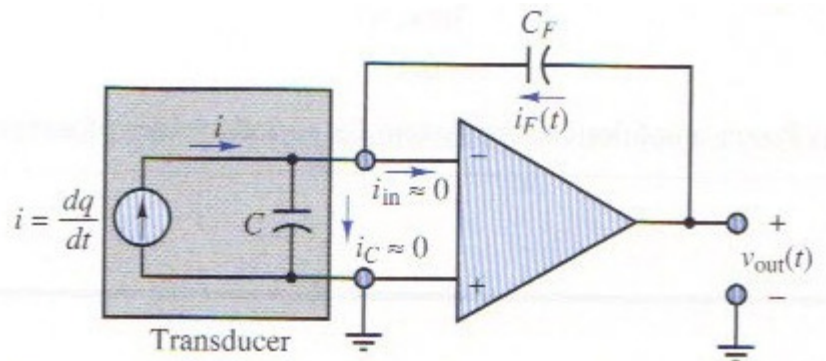
$$\epsilon \sim V_o = 2\Delta R(R_f/R^2)$$

# Applications of Op-Amps

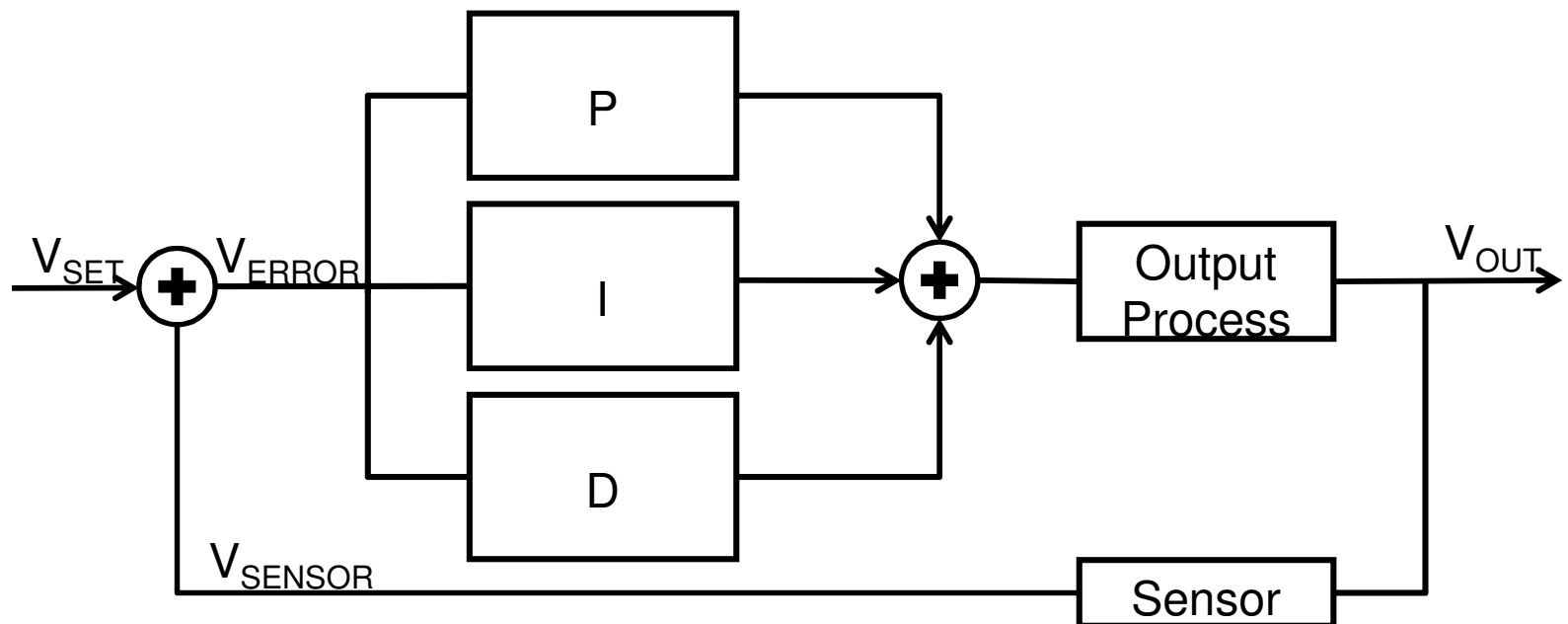
- Piezoelectric Transducer
  - Used to measure force, pressure, acceleration
  - Piezoelectric crystal generates an electric charge in response to deformation



- Use Charge Amplifier
  - Just an integrator op-amp circuit



# PID Controller – System Block Diagram



- Goal is to have  $V_{SET} = V_{OUT}$
- Remember that  $V_{ERROR} = V_{SET} - V_{SENSOR}$
- Output Process uses  $V_{ERROR}$  from the PID controller to adjust  $V_{out}$  such that it is  $\sim V_{SET}$

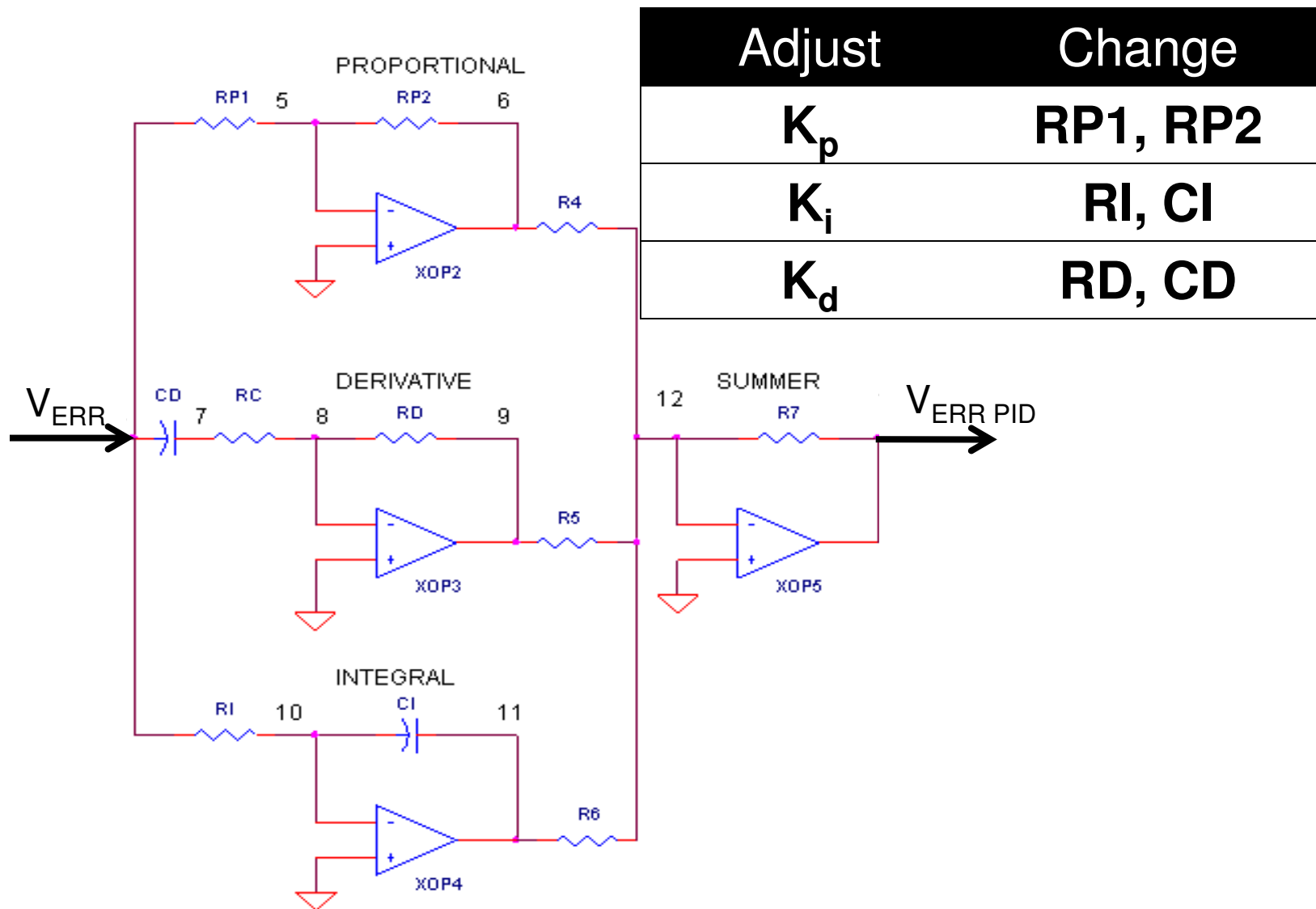
## PID Controller – System Circuit Diagram





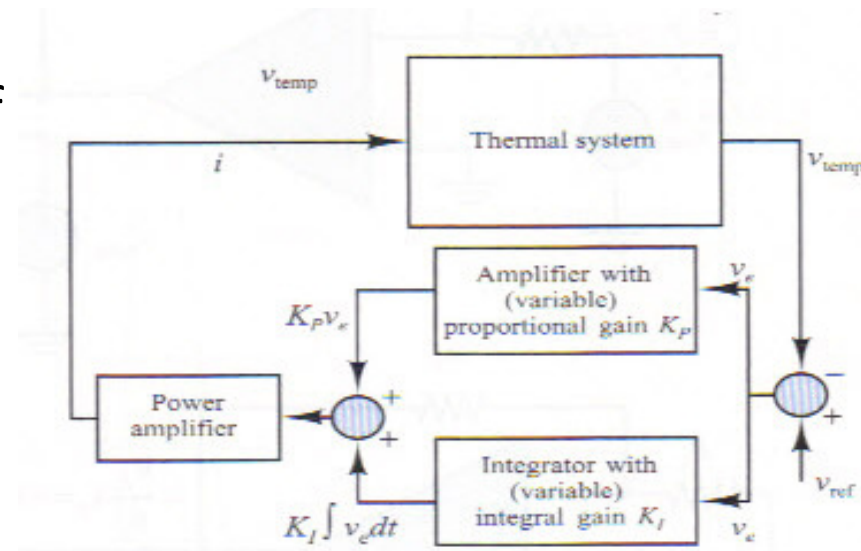
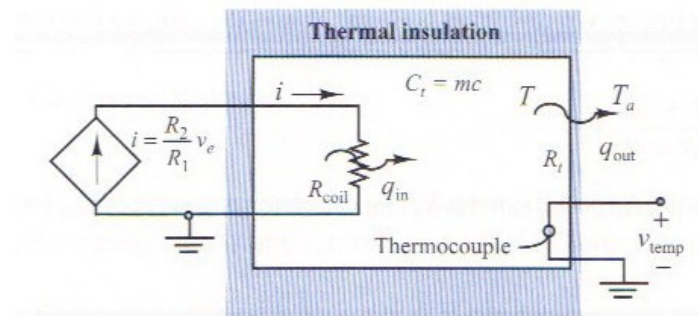
# Applications

## PID Controller – PID Controller Circuit Diagram



# Applications of Op-Amps

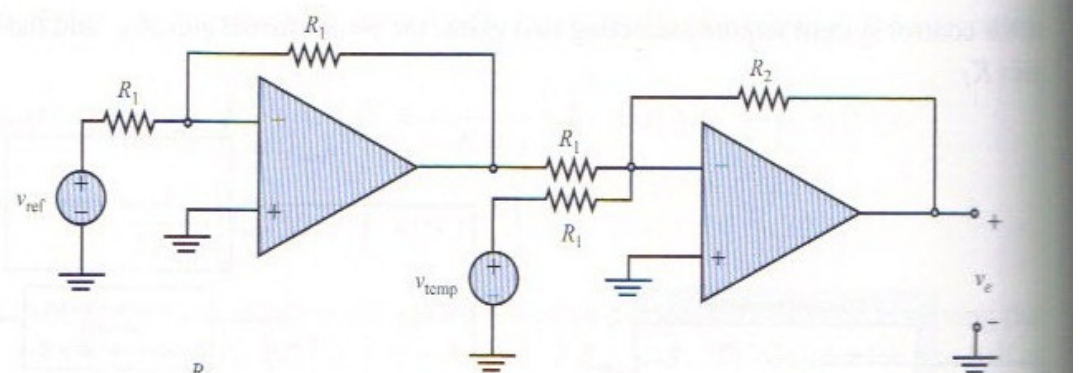
- Example of PI Control:  
Temperature Control
- Thermal System we wish to automatically control the temperature of:
- Block Diagram of Control System:



# Applications of Op-Amps

- Example of PI Control: Temperature Control

- Voltage Error Circuit:



- Proportional-Integral Control Circuit:

