

# Introduction to Massive MIMO technology

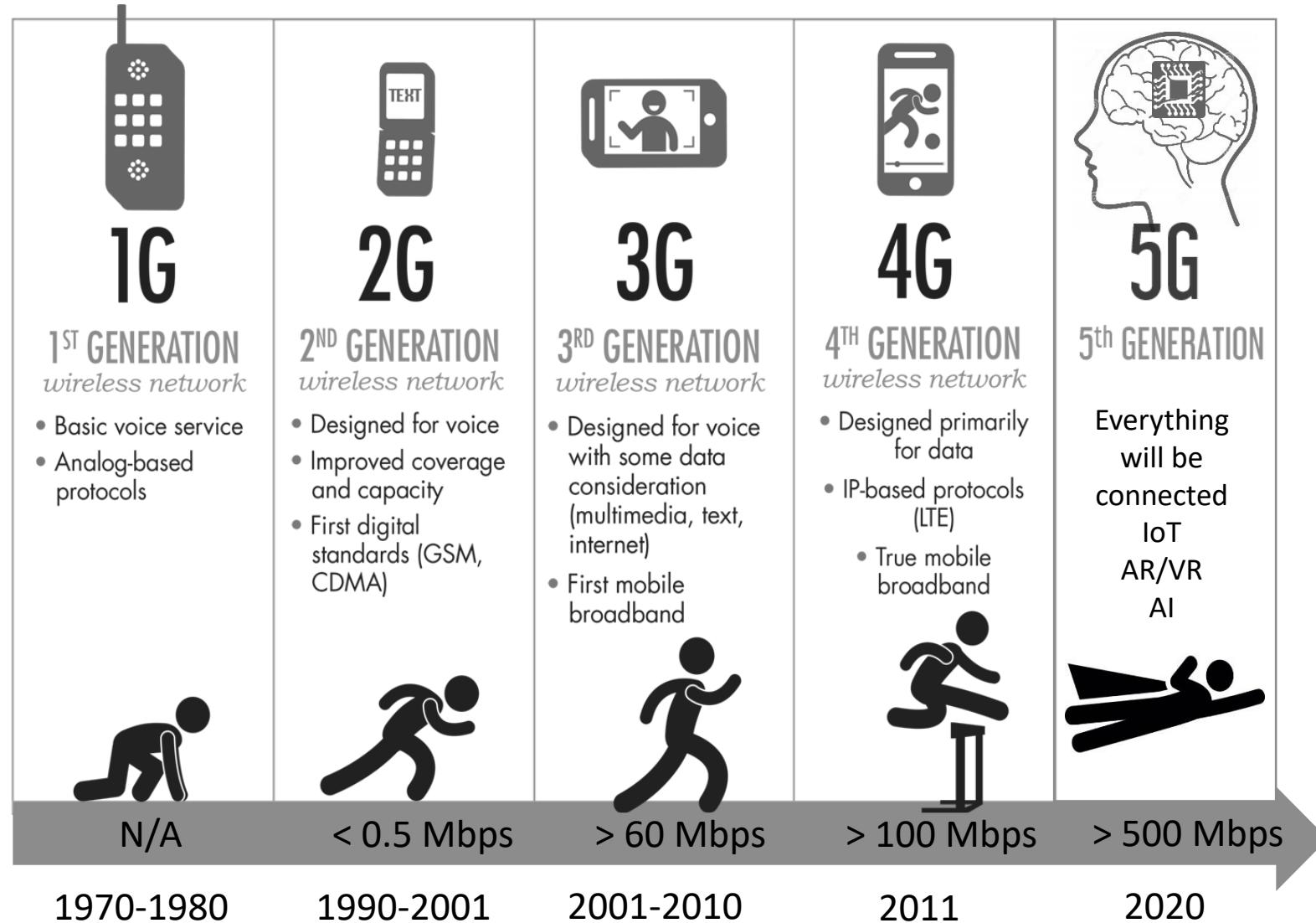
Aleksei Fedorov

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University of Otago

# Outline

- History of mobile communication
- Physical aspects of radio signals
- Introduction to LTE/4G
- Massive MIMO approach
- What we do

# History of mobile communication



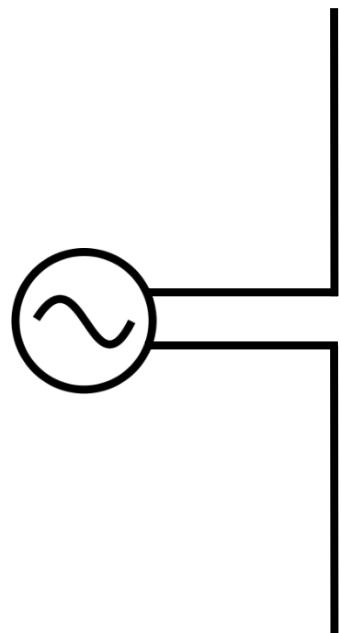
# Physical aspects of radio signals

- What is a radio signal

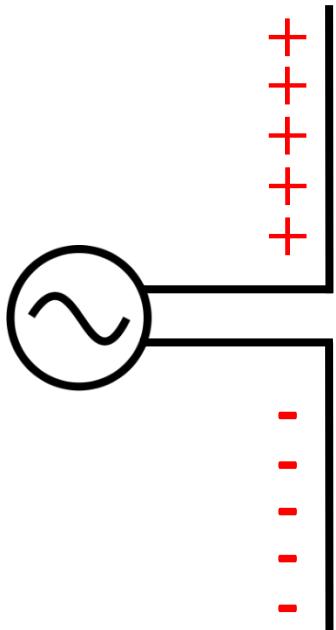
Radio signal is an electromagnetic wave travelling through air

- How is it generated?

# Generation of EM wave

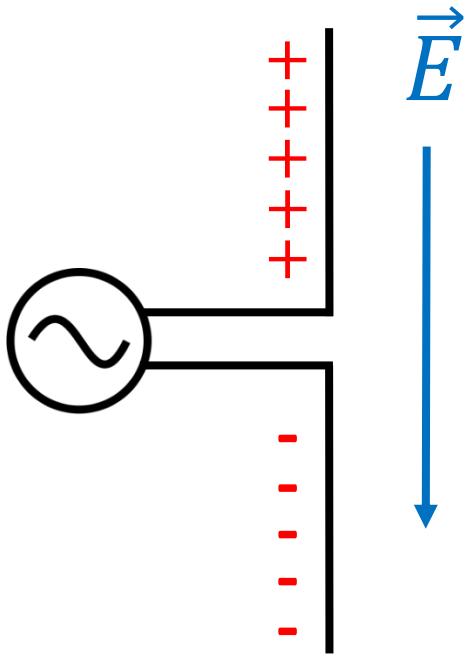


# Generation of EM wave



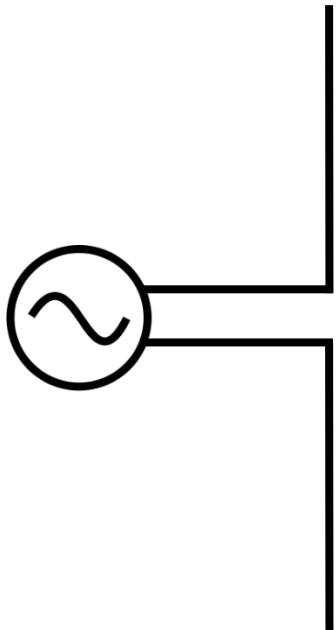
$t_0$

# Generation of EM wave



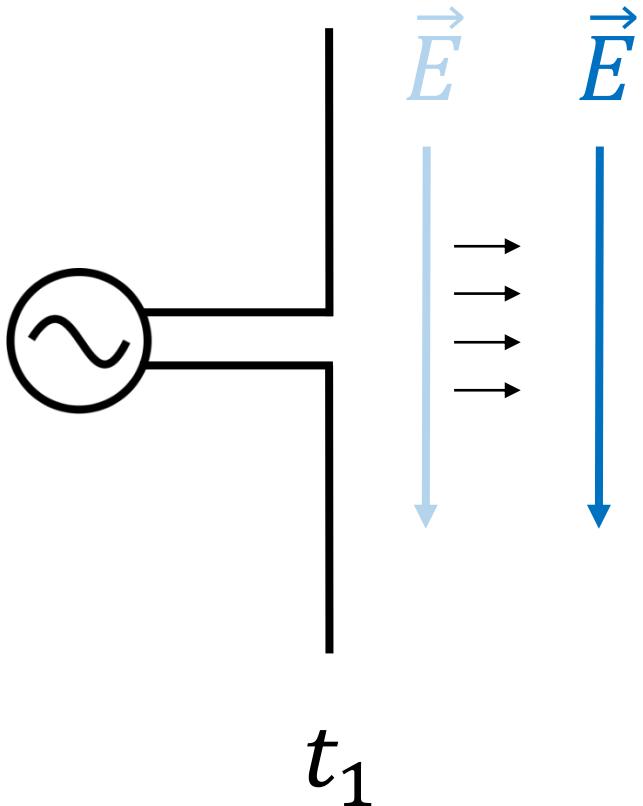
$t_0$

# Generation of EM wave

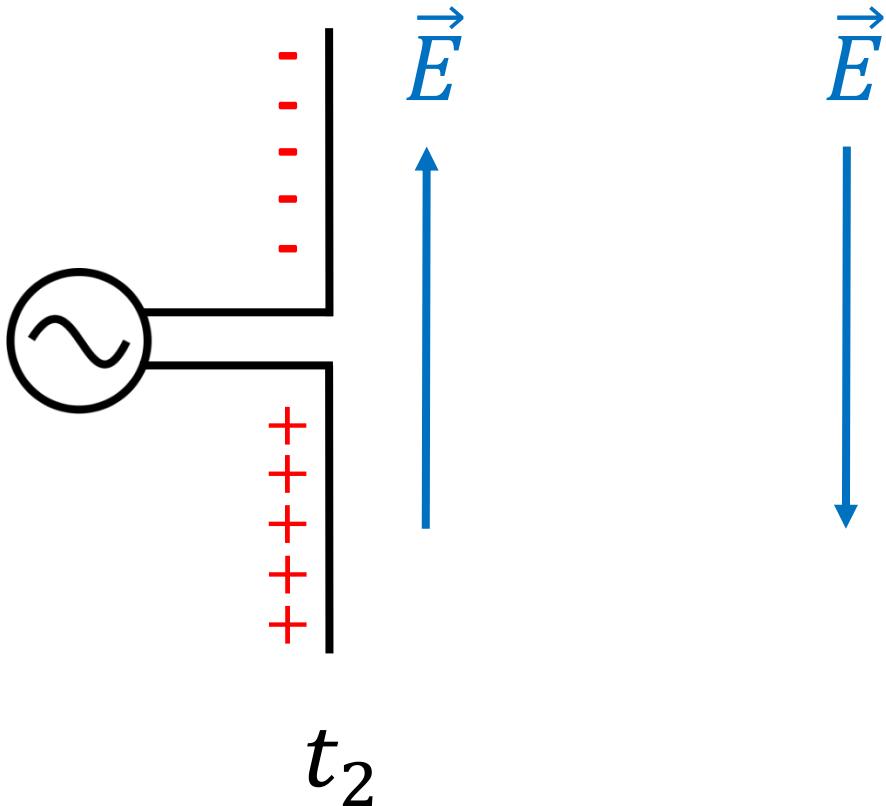


$t_1$

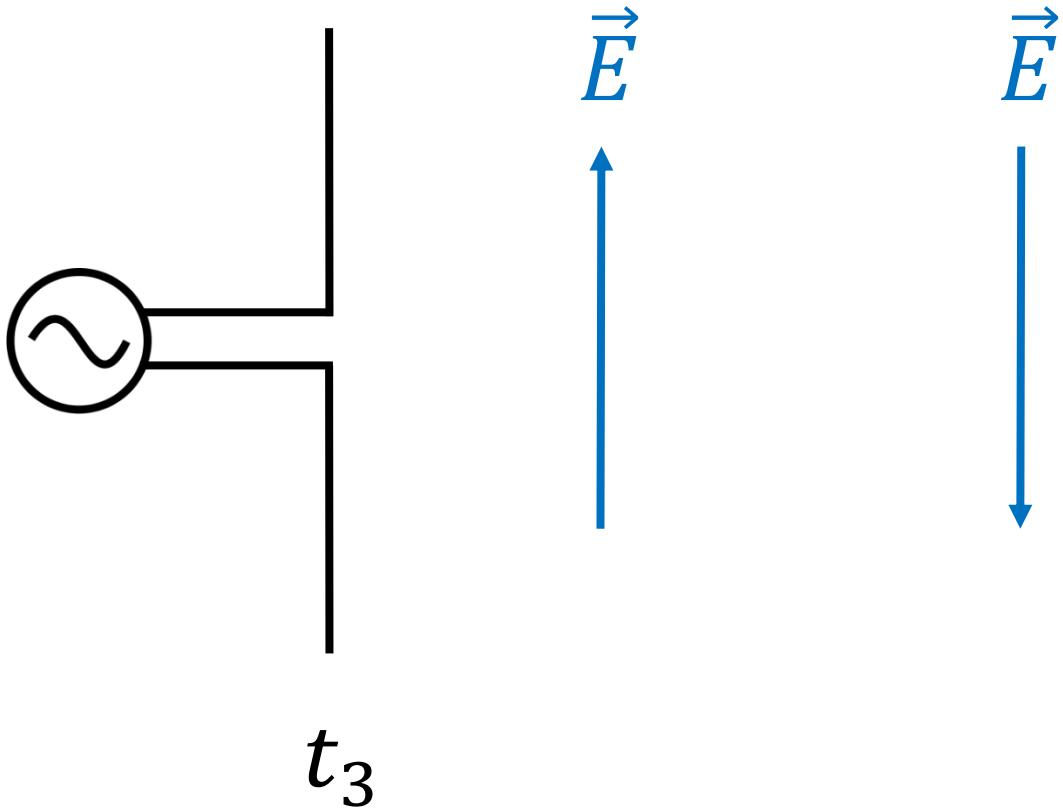
# Generation of EM wave



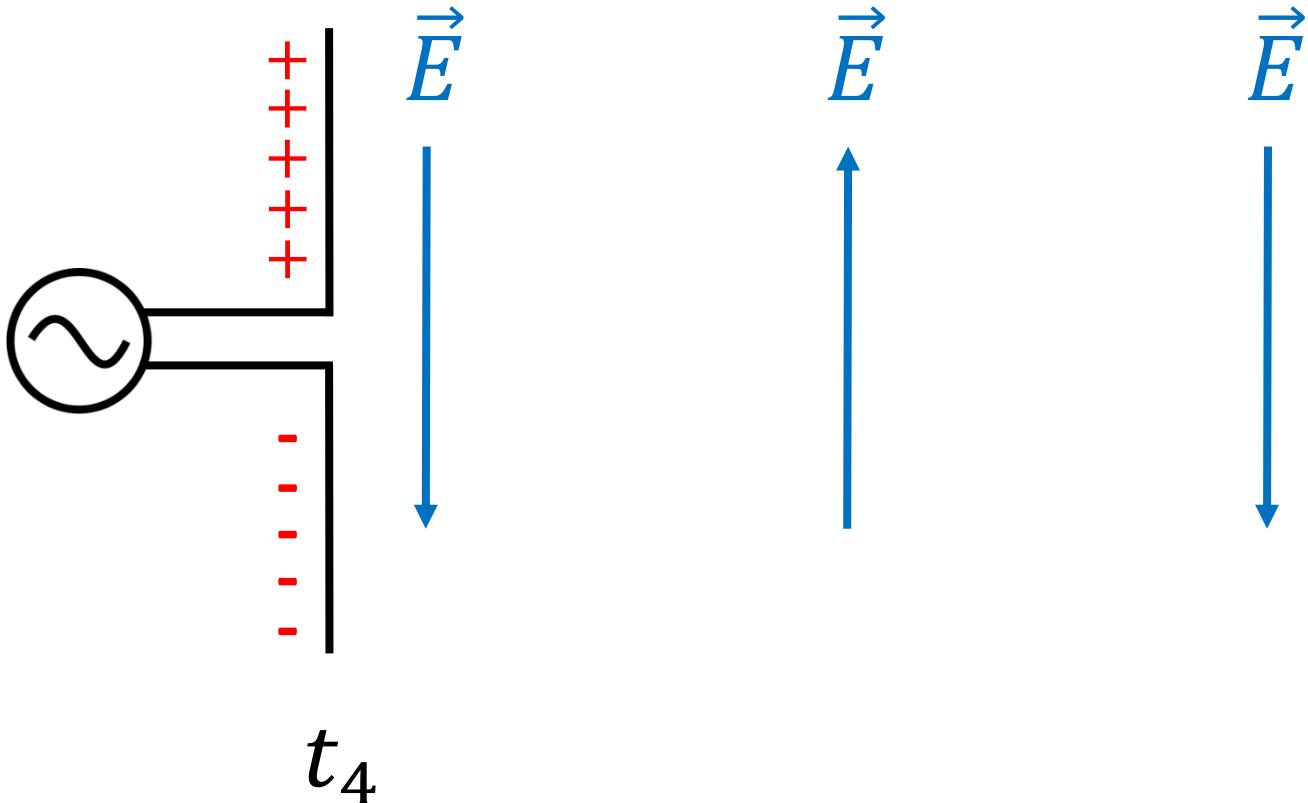
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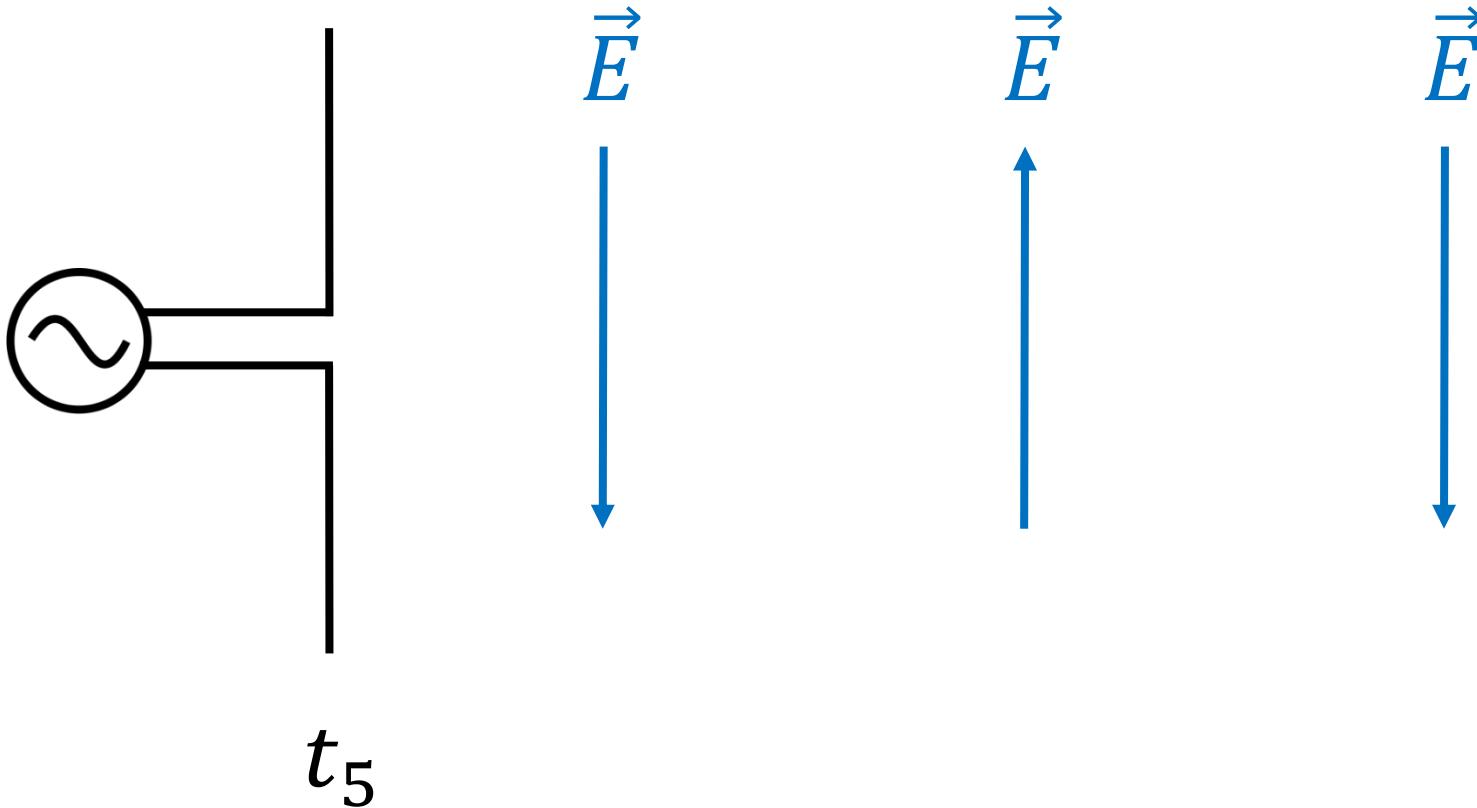
# Generation of EM wave



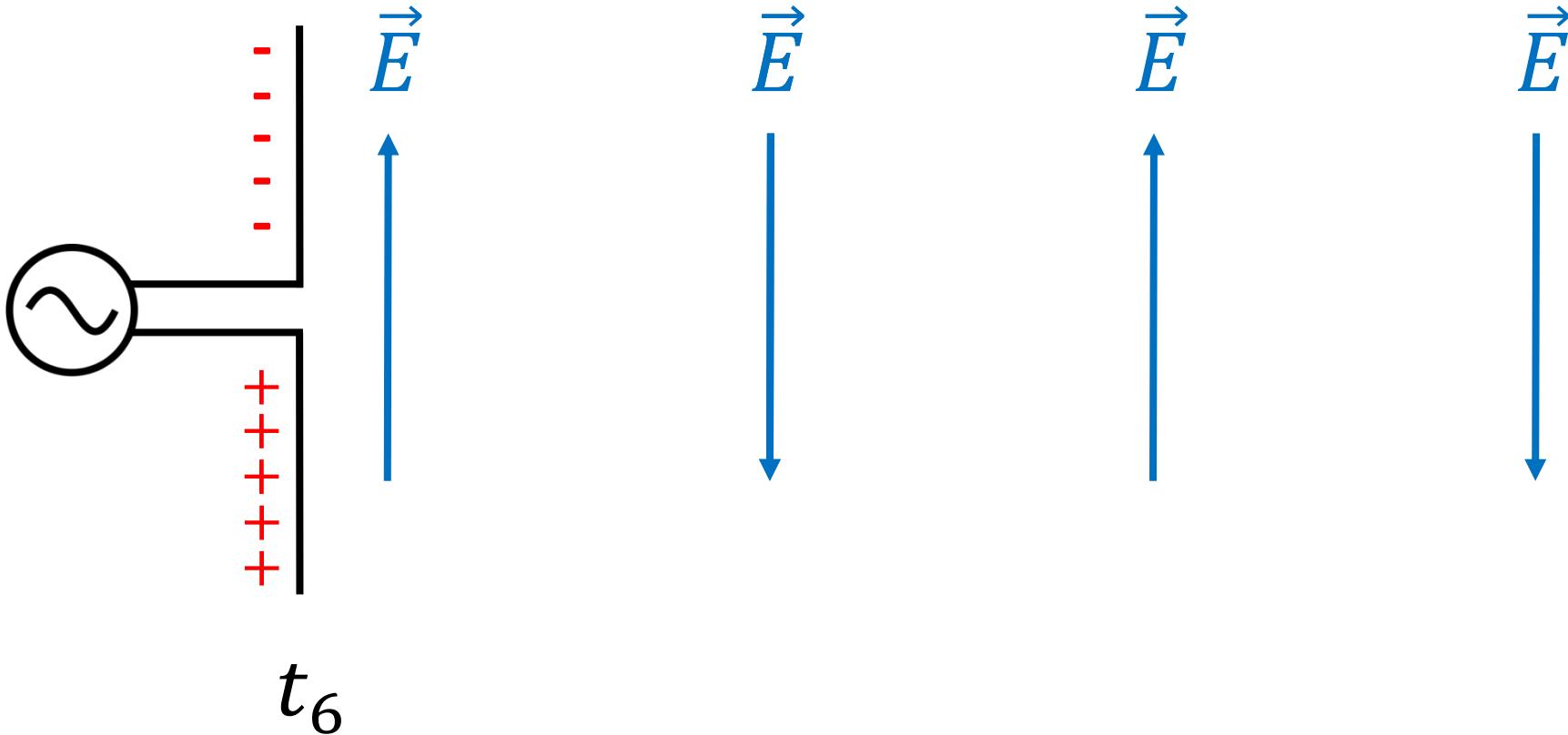
# Generation of EM wave



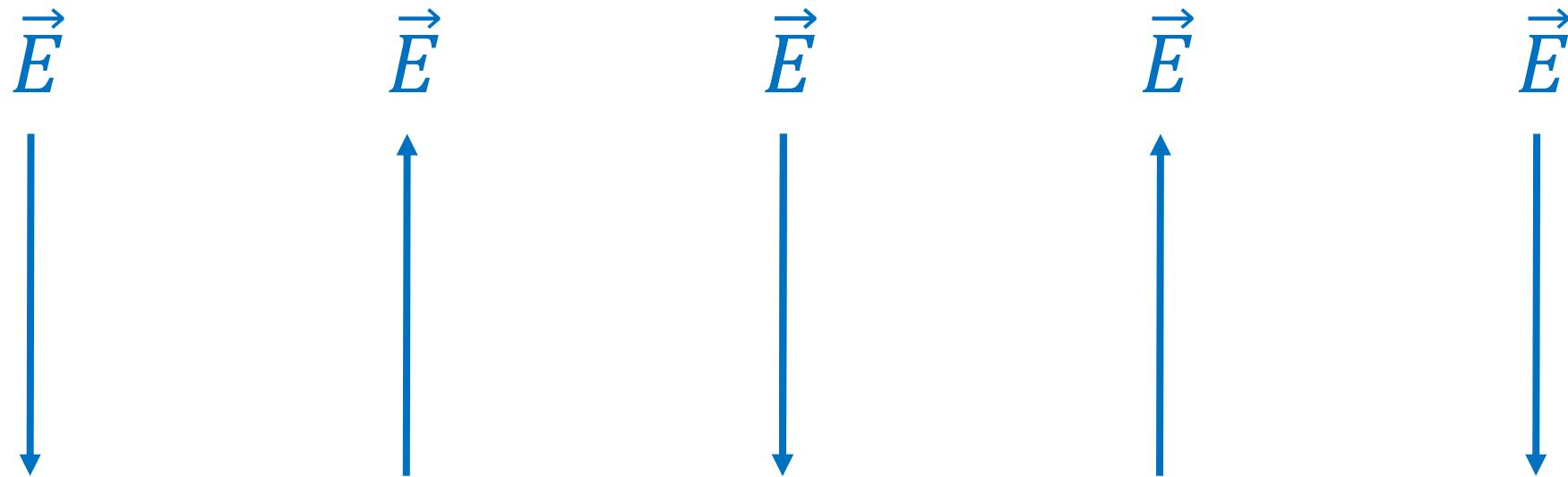
# Generation of EM wave



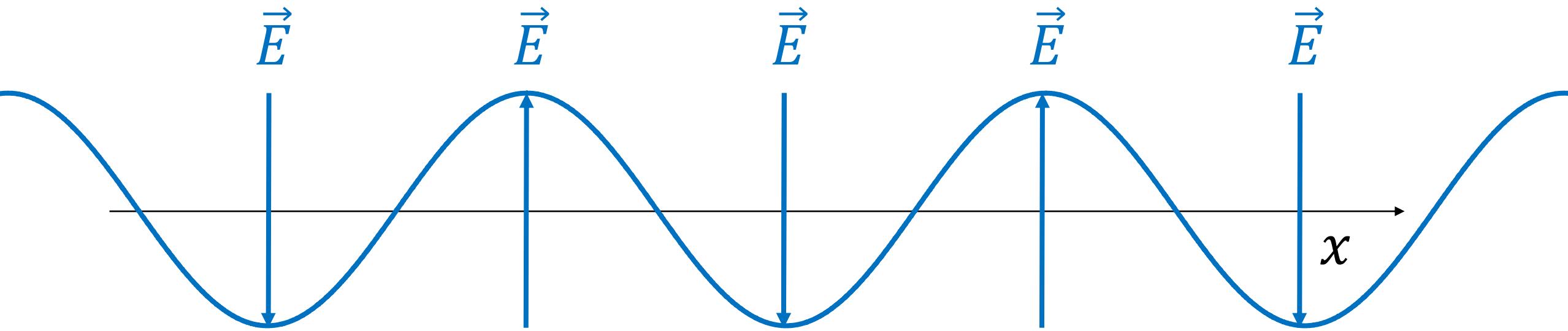
# Generation of EM wave



# Generation of EM wave

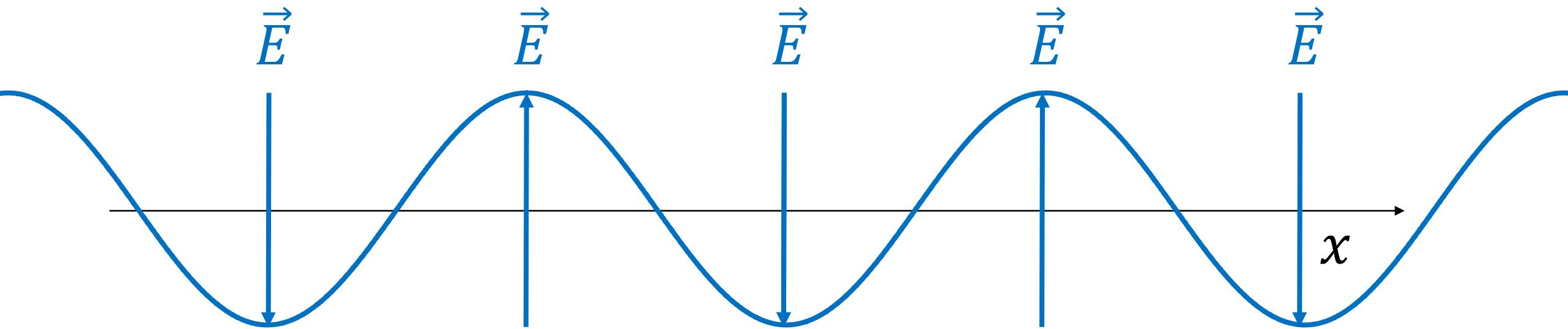


# Generation of EM wave



$$\vec{E}(t) = \vec{E}_0 \cdot \exp(j(2\pi \omega t - \varphi))$$

# Generation of EM wave



$$\vec{E}(t) = \overrightarrow{E_0} \cdot \exp(j(2\pi \omega t - \varphi))$$

# Physical aspects of radio signals

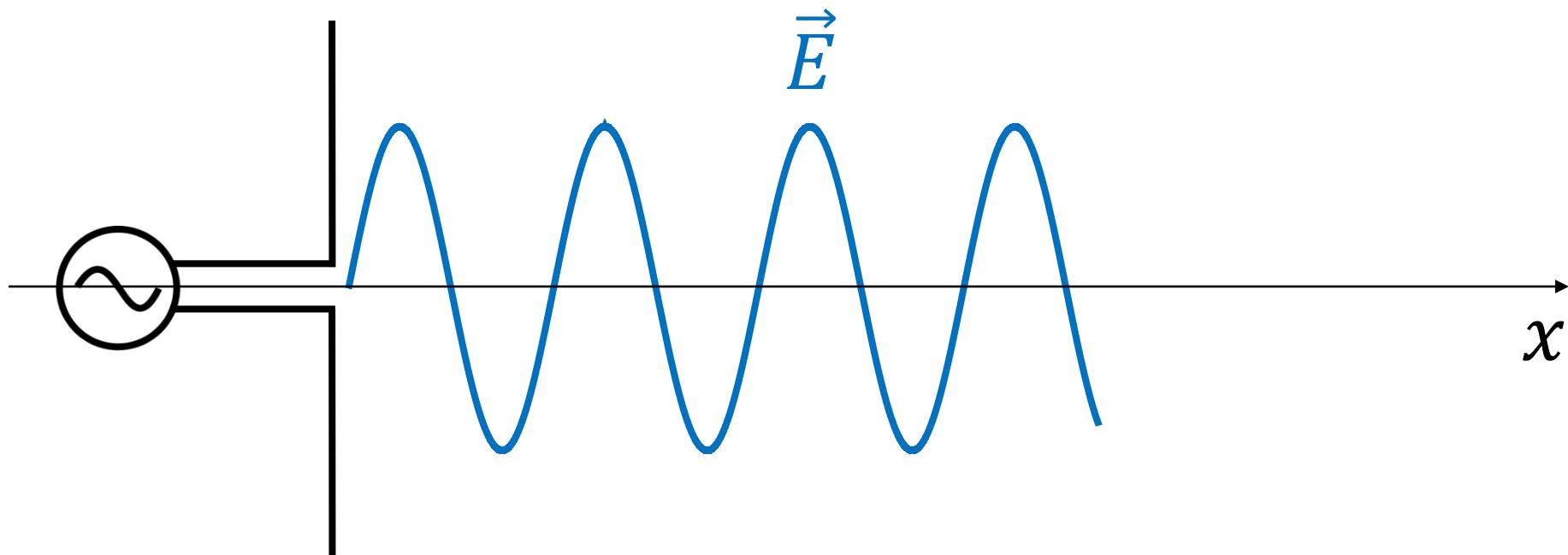
- What is a radio signal

Radio signal is an electromagnetic wave travelling through air

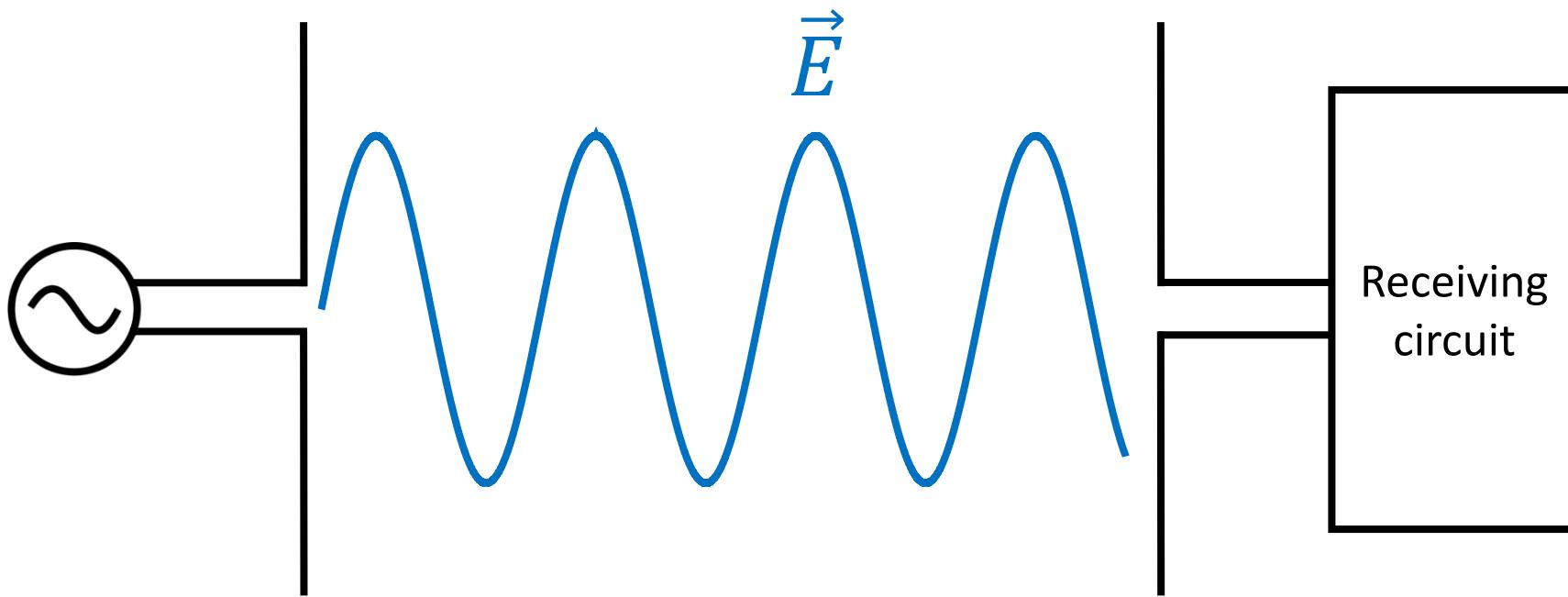
- How is it generated?

- How is it received?

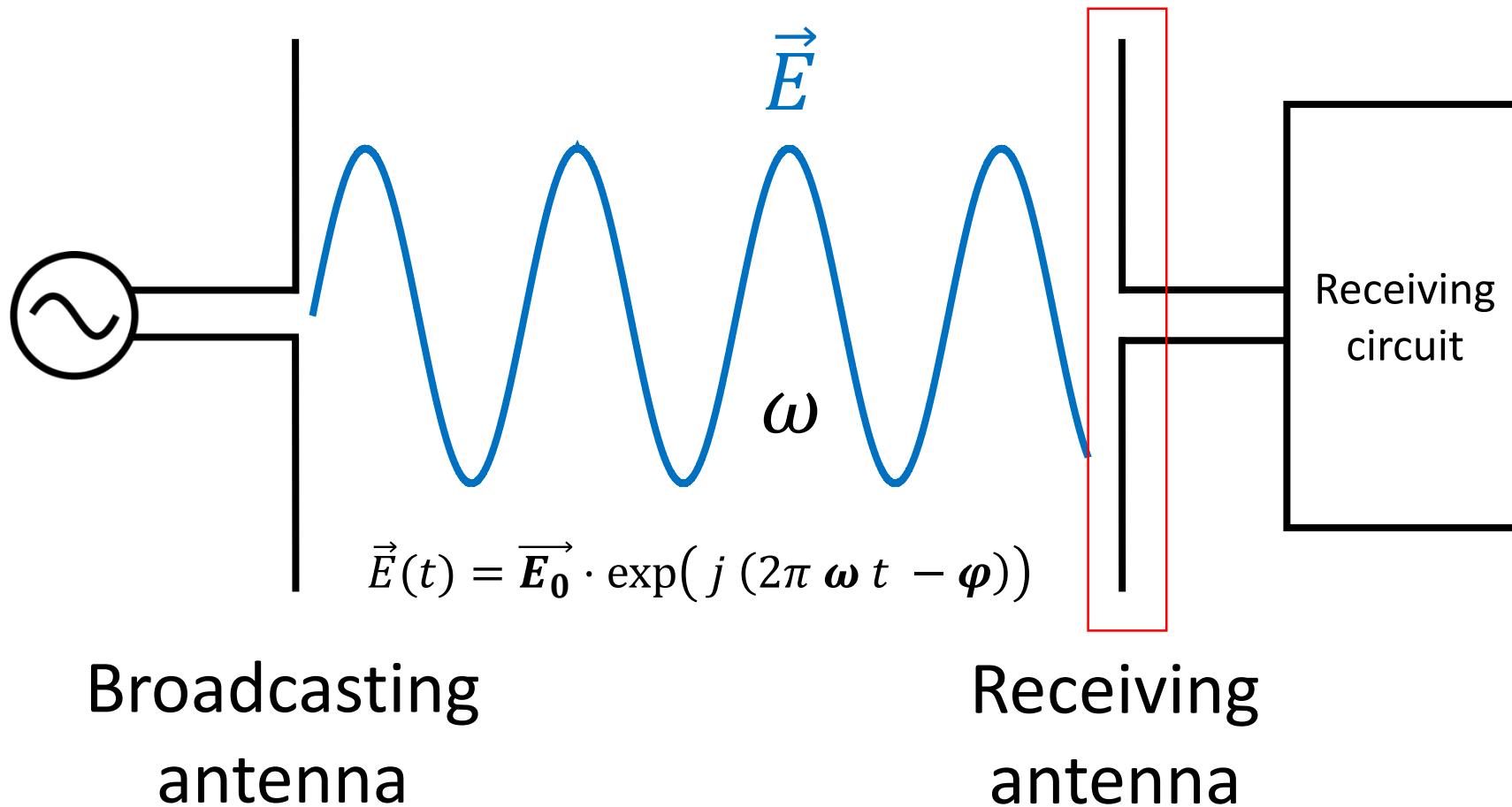
# Reception of EM wave

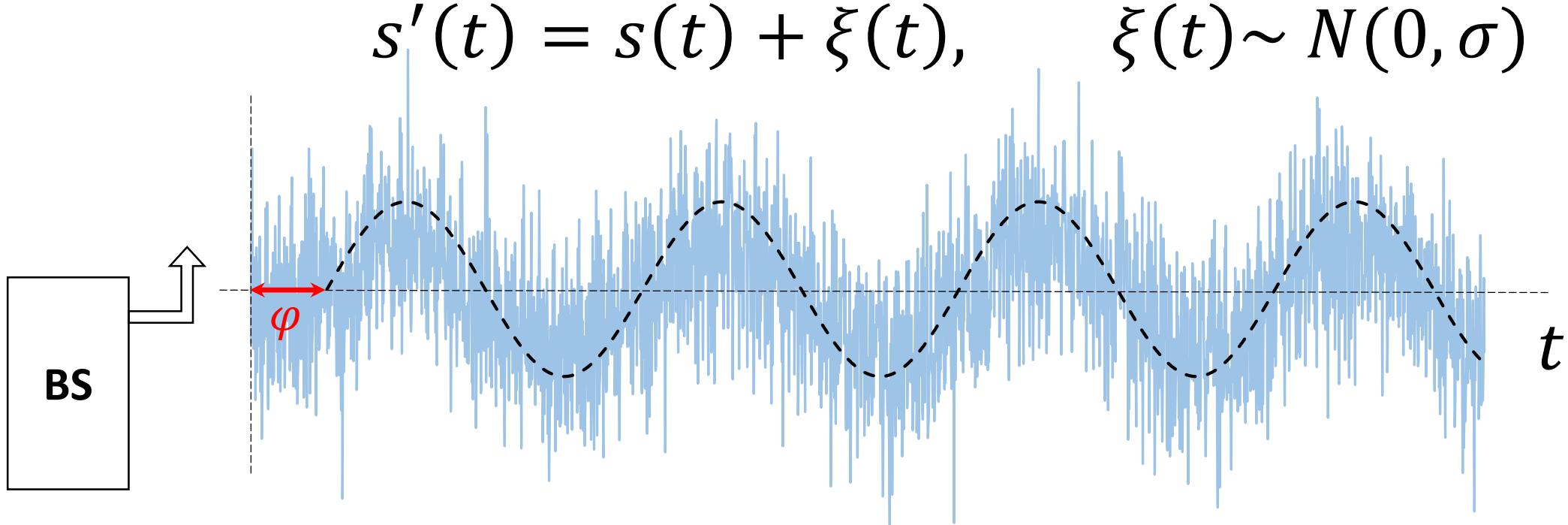
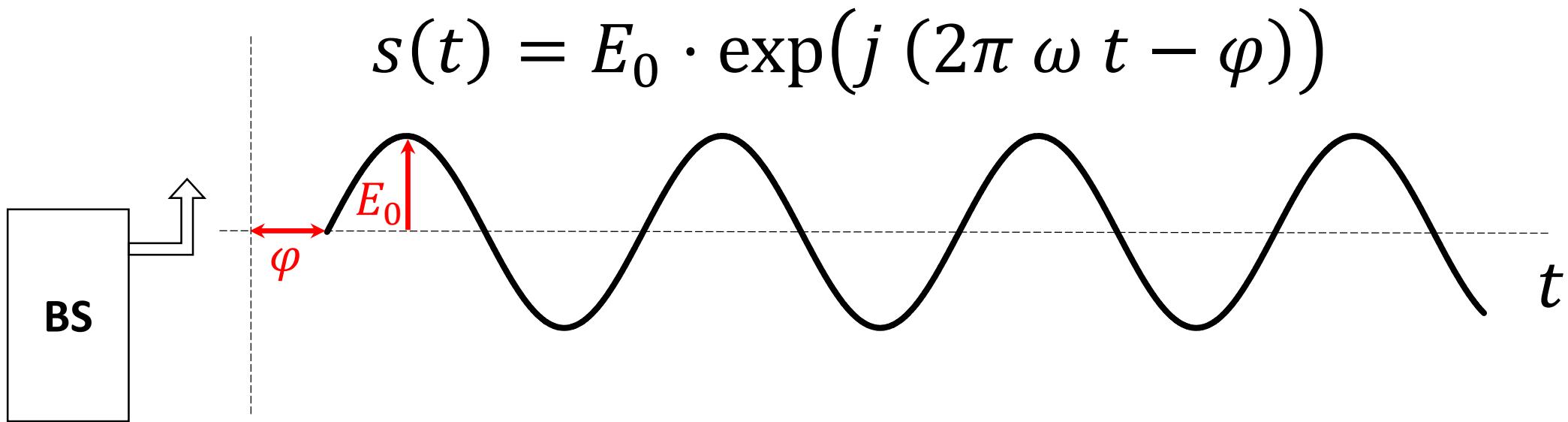


# Reception of EM wave

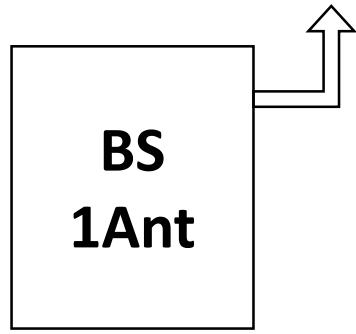


# Reception of EM wave



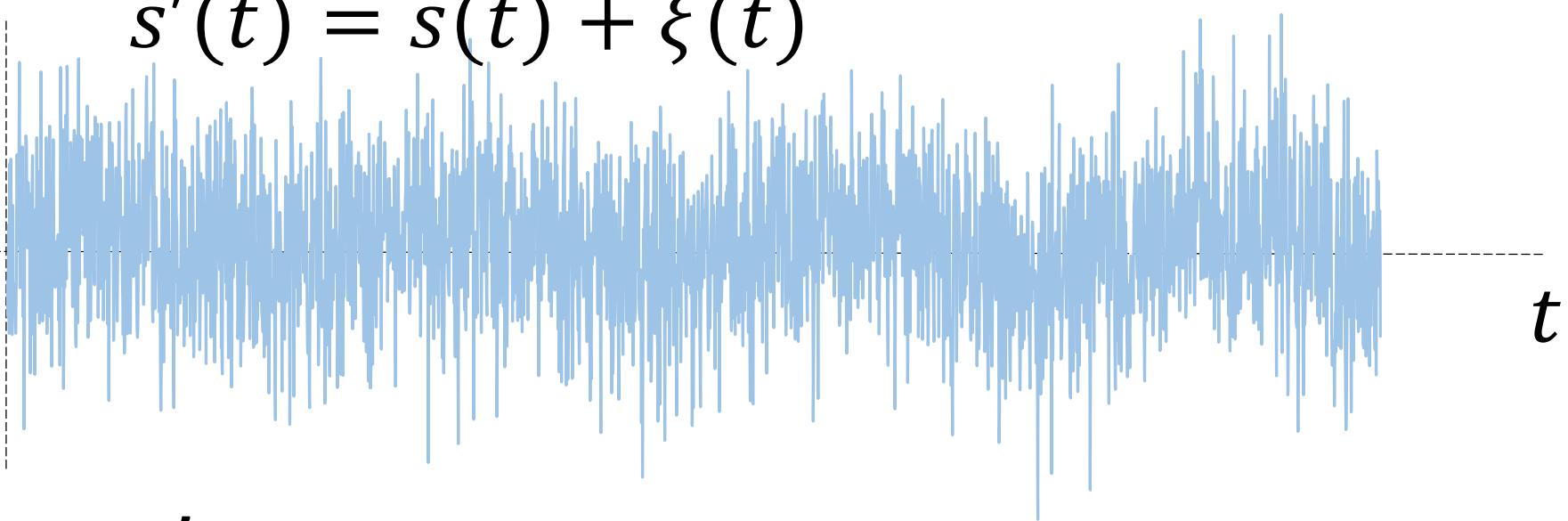
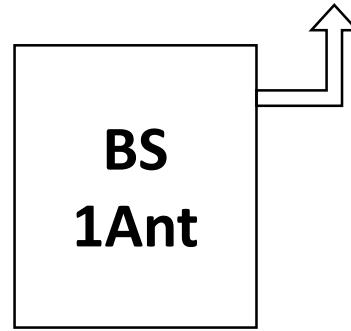


$$s'(t) = s(t) + \xi(t)$$

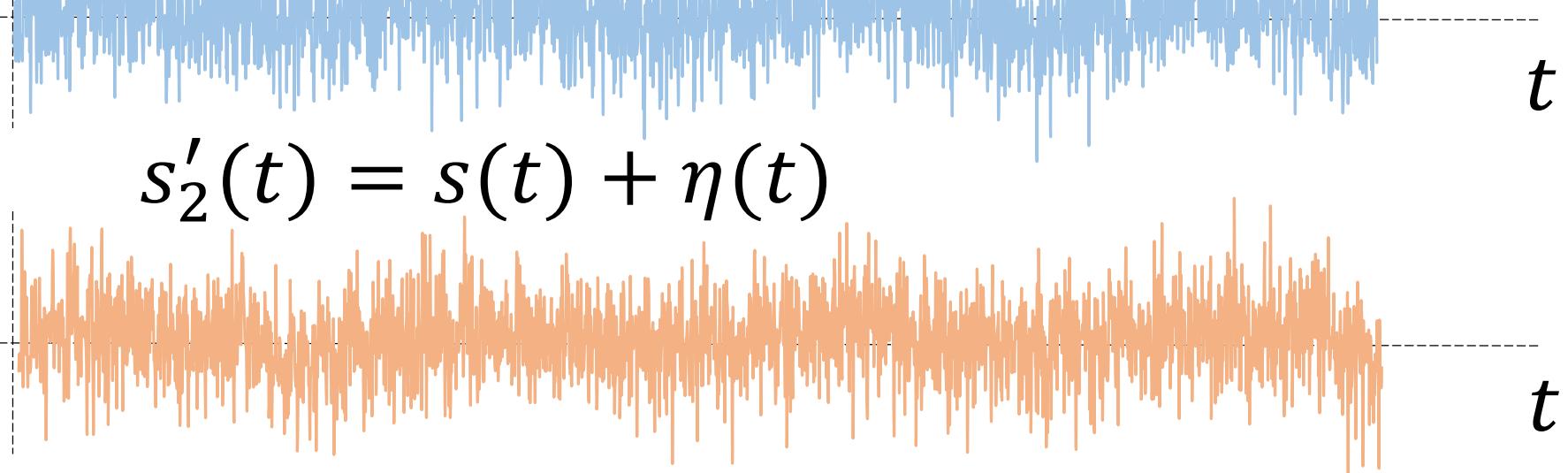
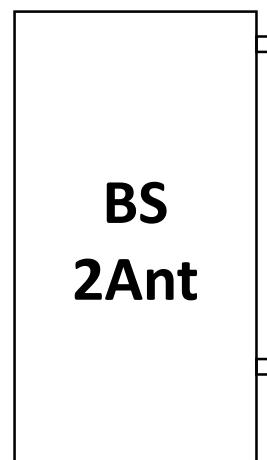


*t*

$$s'(t) = s(t) + \xi(t)$$

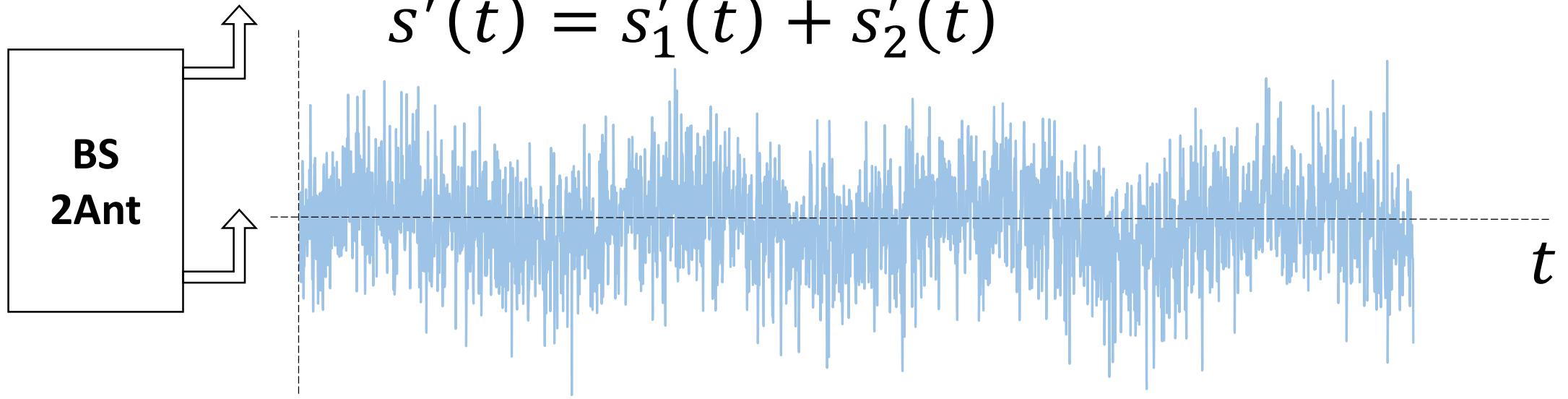


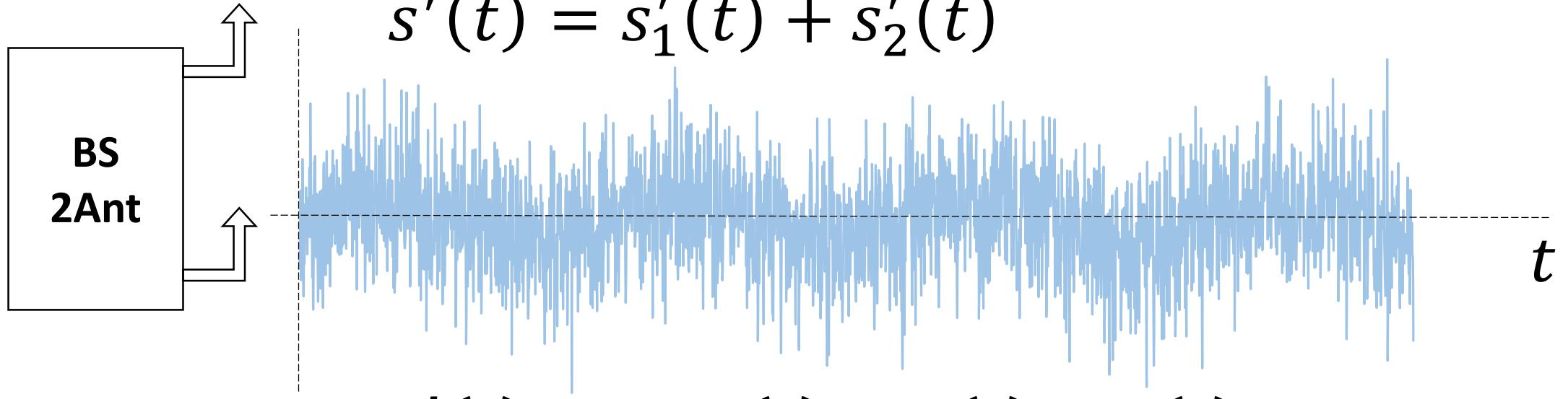
$$s'_1(t) = s(t) + \xi(t)$$



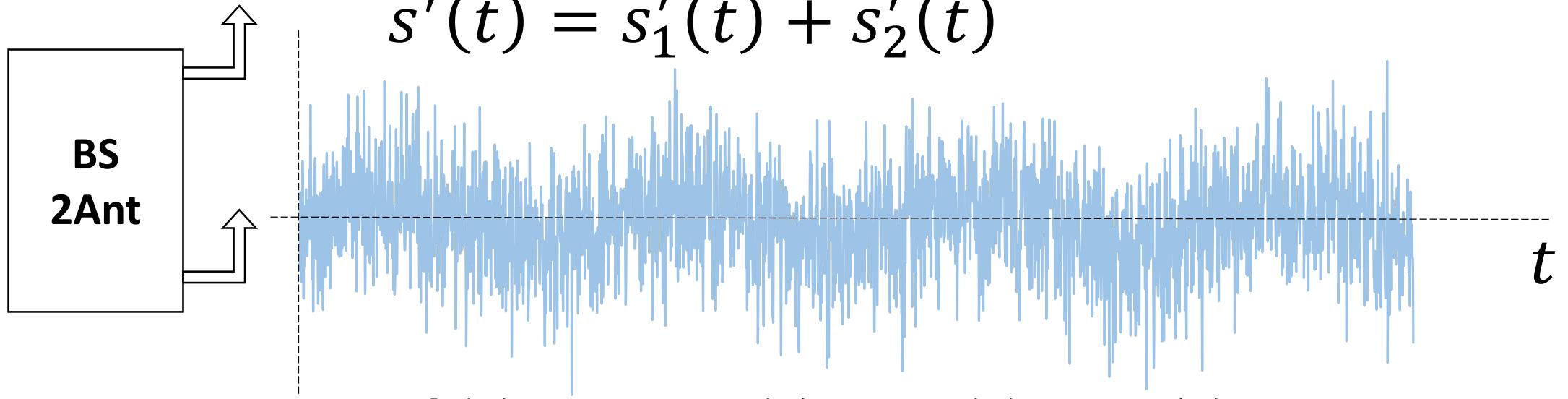
$$s'_2(t) = s(t) + \eta(t)$$



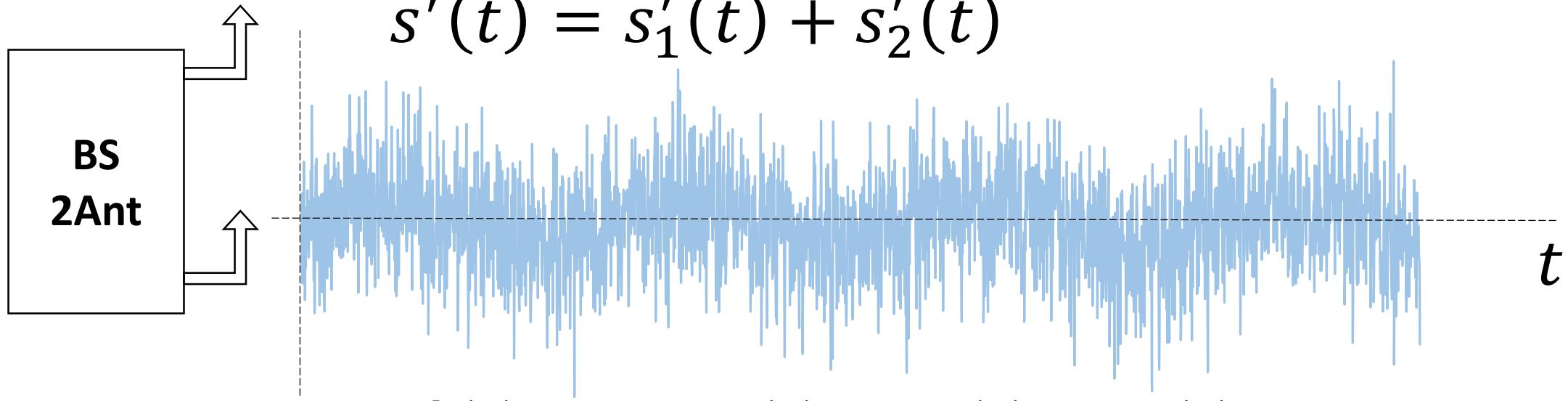




$$s'(t) = 2 \cdot s(t) + \eta(t) + \xi(t)$$

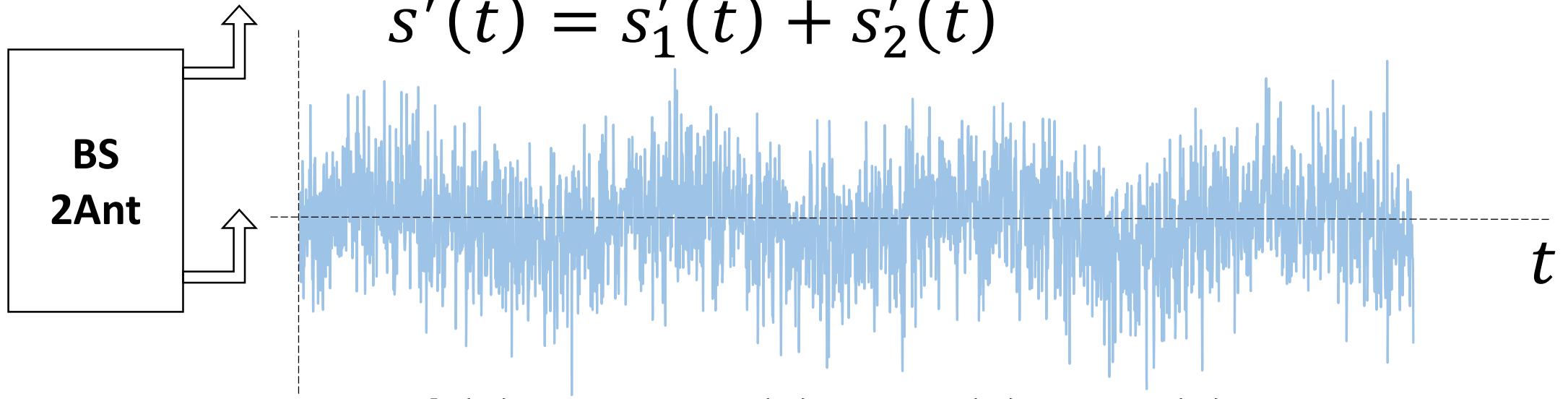


Noises  $\eta(t)$  and  $\xi(t)$  are independent



$$s'(t) = 2 \cdot s(t) + \eta(t) + \xi(t)$$

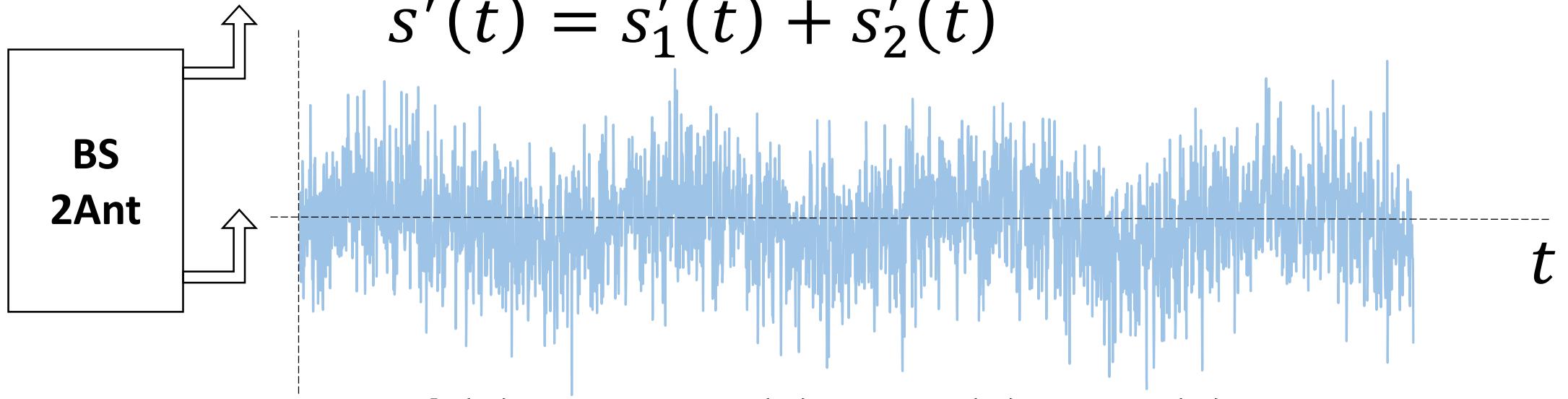
Noises  $\eta(t)$  and  $\xi(t)$  are independent  $E[\xi \eta] = 0$



$$s'(t) = 2 \cdot s(t) + \eta(t) + \xi(t)$$

Noises  $\eta(t)$  and  $\xi(t)$  are independent  $E[\xi \eta] = 0$

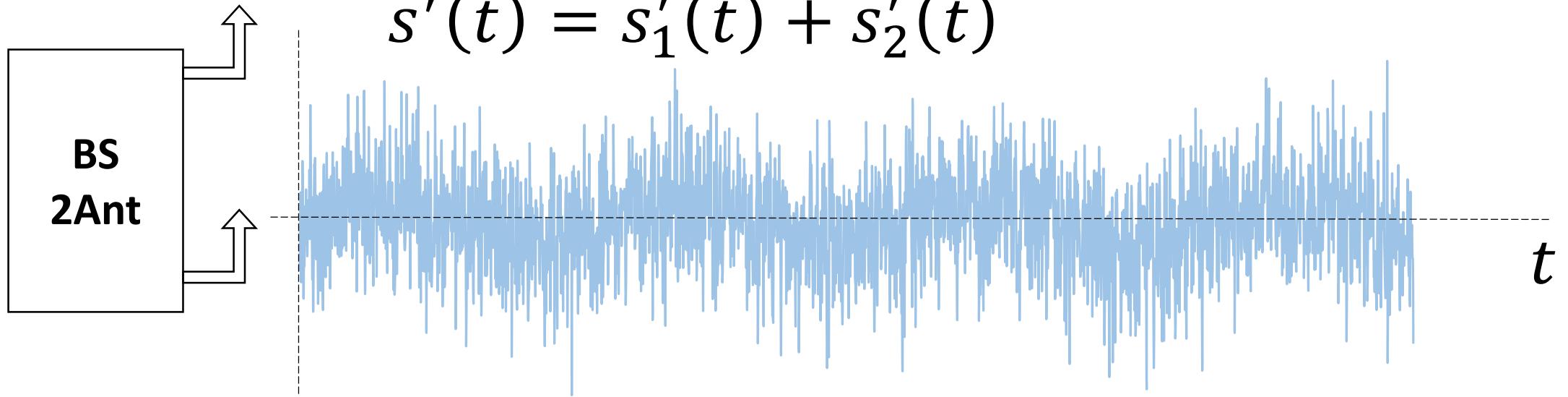
$$E[\xi] = E[\eta] = 0 \quad E[\xi^2] = E[\eta^2] = \sigma^2$$



$$s'(t) = 2 \cdot s(t) + \eta(t) + \xi(t)$$

Noises  $\eta(t)$  and  $\xi(t)$  are independent  $E[\xi \eta] = 0$

$$\xi(t) \sim N(0, \sigma) \quad \eta(t) \sim N(0, \sigma)$$

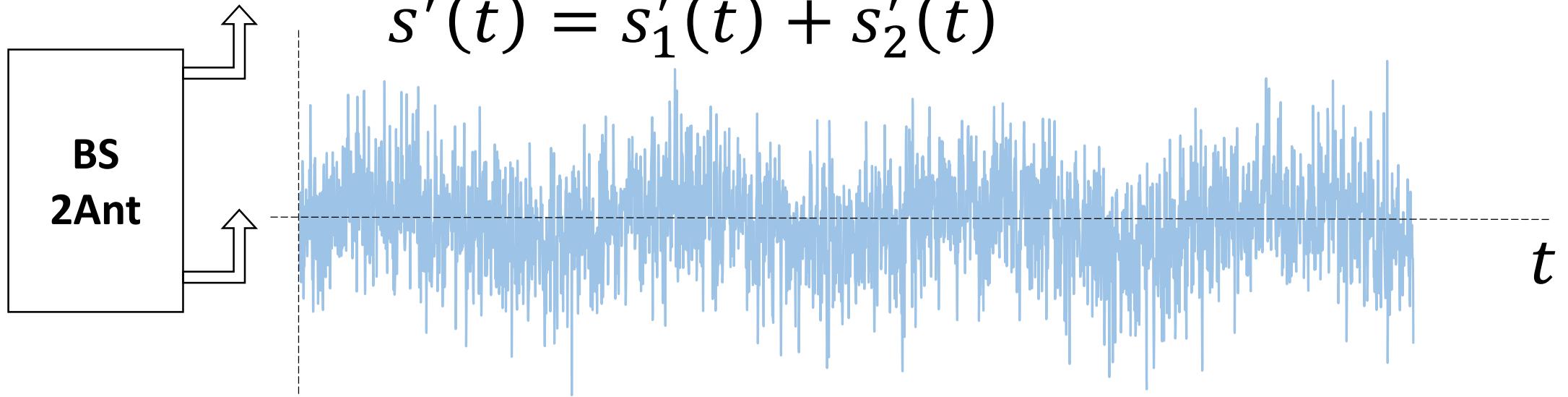


$$s'(t) = 2 \cdot s(t) + \eta(t) + \xi(t)$$

Noises  $\eta(t)$  and  $\xi(t)$  are independent  $E[\xi \eta] = 0$

$$E[\xi] = E[\eta] = 0 \quad E[\xi^2] = E[\eta^2] = \sigma^2$$

$$\zeta = \xi + \eta$$

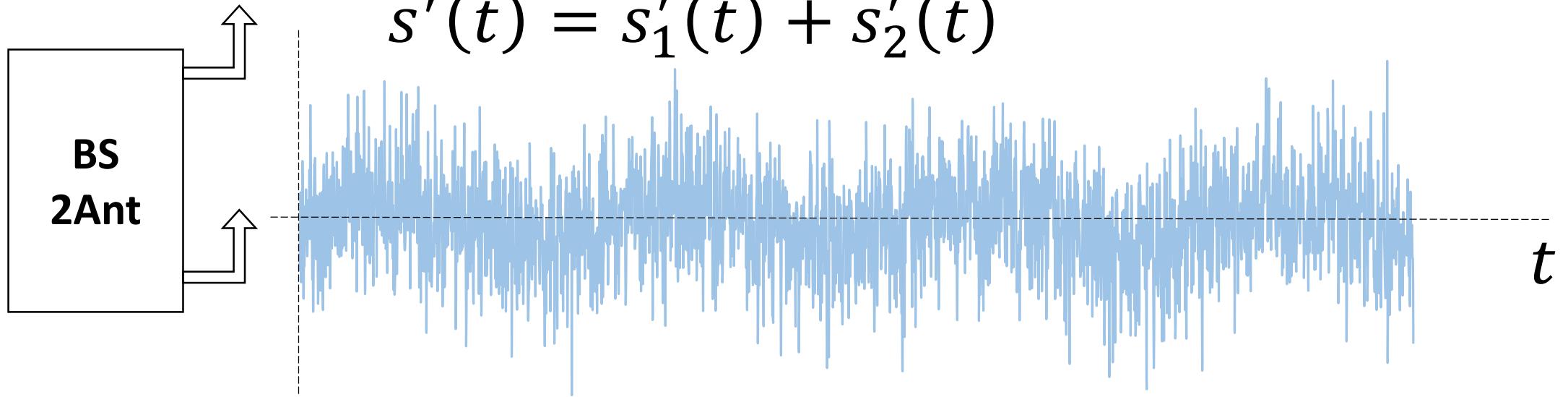


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Noises  $\eta(t)$  and  $\xi(t)$  are independent  $E[\xi \eta] = 0$

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$$\zeta = \xi + \eta \quad E[\zeta] = E[\xi + \eta] = E[\xi] + E[\eta] = 0$$

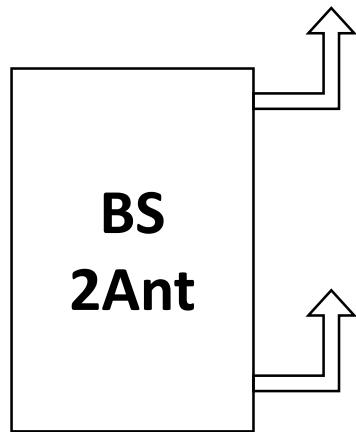


$$s'(t) = 2 \cdot s(t) + \eta(t) + \xi(t)$$

Noises  $\eta(t)$  and  $\xi(t)$  are independent  $E[\xi \eta] = 0$

$$E[\xi] = E[\eta] = 0 \quad E[\xi^2] = E[\eta^2] = \sigma^2$$

$$E[\zeta^2] = E[(\xi + \eta)^2] = E[\xi^2] + 2E[\xi \eta] + E[\eta^2] = ?$$



$$s'(t) = s'_1(t) + s'_2(t)$$

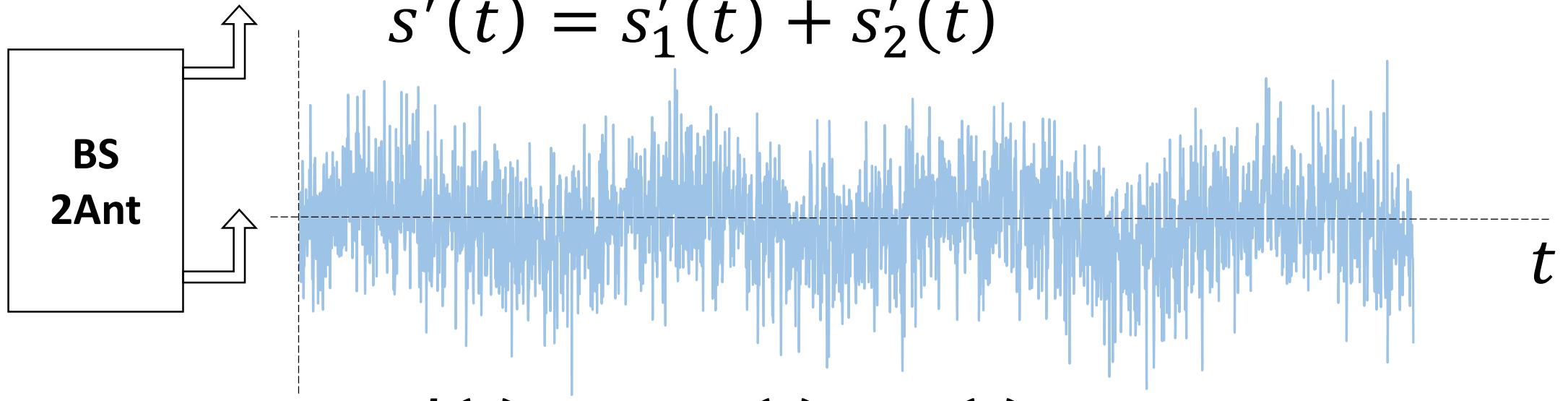
$t$

$$s'(t) = 2 \cdot s(t) + \eta(t) + \xi(t)$$

Noises  $\eta(t)$  and  $\xi(t)$  are independent  $E[\xi \eta] = 0$

$$E[\xi] = E[\eta] = 0 \quad E[\xi^2] = E[\eta^2] = \sigma^2$$

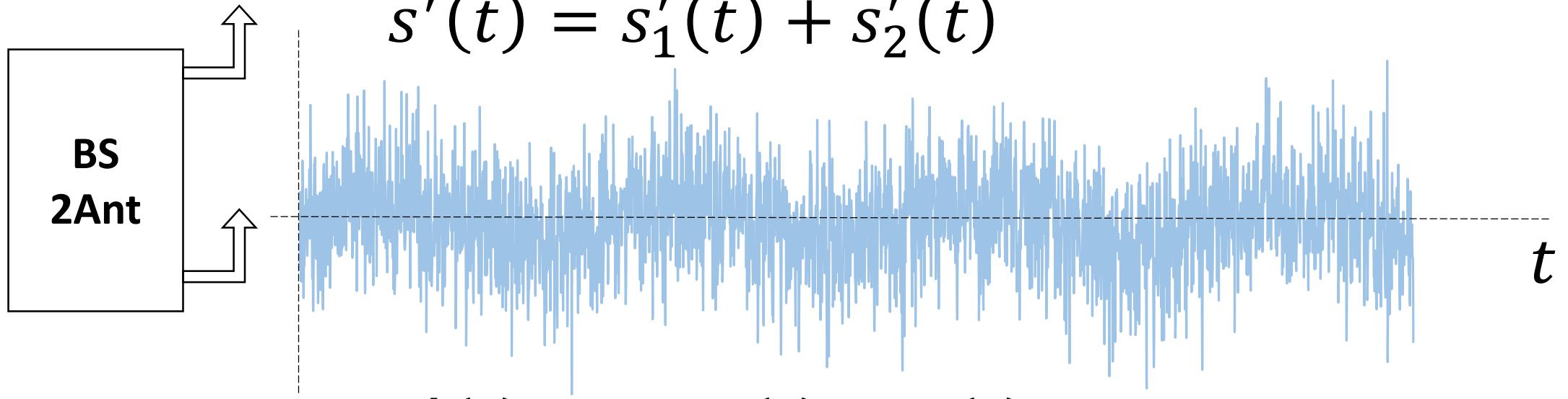
$$E[\zeta^2] = E[(\xi + \eta)^2] = E[\underset{\|}{\xi^2}] + 2E[\underset{\|}{\xi \eta}] + E[\underset{\|}{\eta^2}] = 2\sigma^2$$



$$s'(t) = s'_1(t) + s'_2(t)$$

$$E[\zeta] = 0$$

$$E[\zeta^2] = 2\sigma^2$$

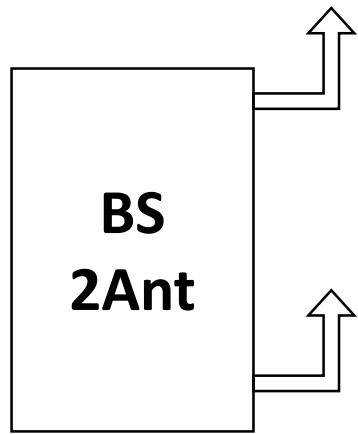


$$s'(t) = 2 \cdot s(t) + \zeta(t)$$

$$E[\zeta] = 0$$

$$\zeta(t) \sim N(0, \sqrt{2} \sigma)$$

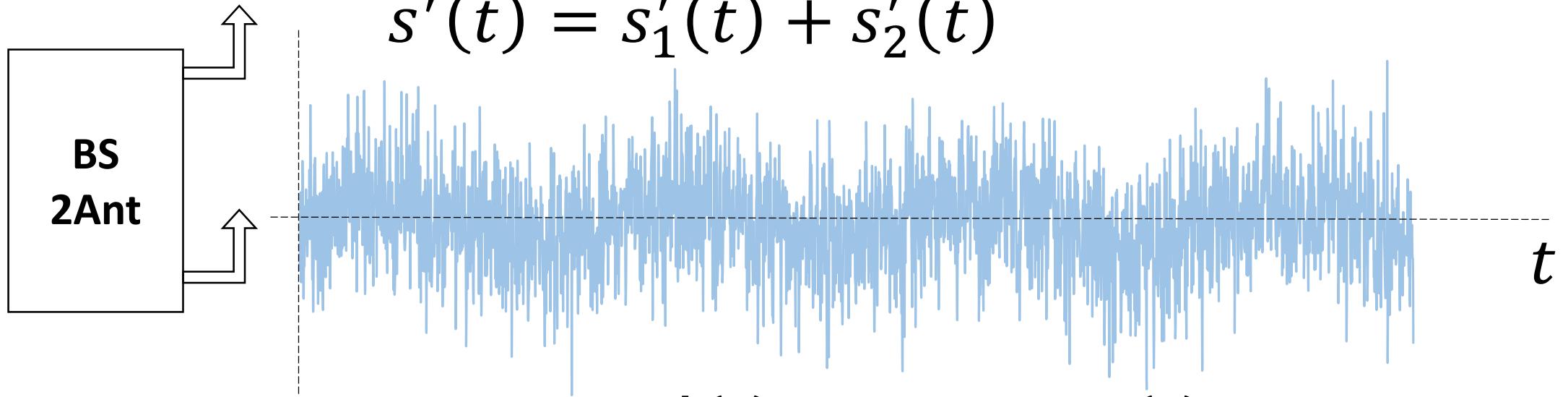
$$E[\zeta^2] = 2\sigma^2$$



$$s'(t) = s'_1(t) + s'_2(t)$$

*t*

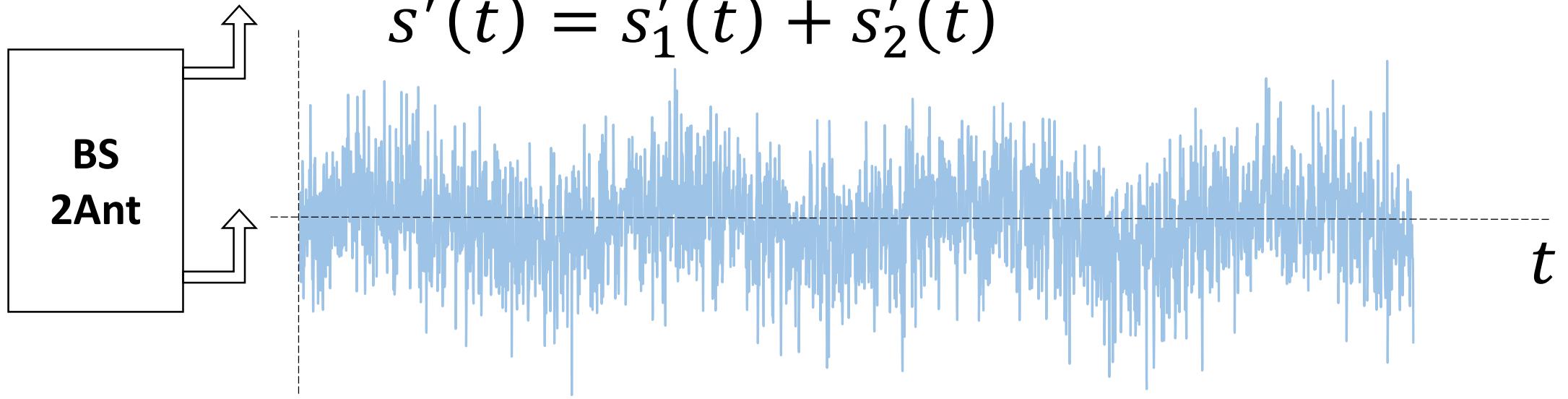
$$s''(t) = \frac{s'(t)}{2} = s(t) + \frac{\zeta(t)}{2} = s(t) + \zeta(t)$$



$$s''(t) = \frac{s'(t)}{2} = s(t) + \frac{\zeta(t)}{2} = s(t) + \zeta(t)$$

$$E[\zeta] = E\left[\frac{\zeta}{2}\right] = \frac{E[\zeta]}{2} = 0$$

$$E[\zeta^2] = E\left[\left(\frac{\zeta}{2}\right)^2\right] = \frac{E[\zeta^2]}{4} = \frac{2\sigma^2}{4} = \frac{\sigma^2}{2}$$



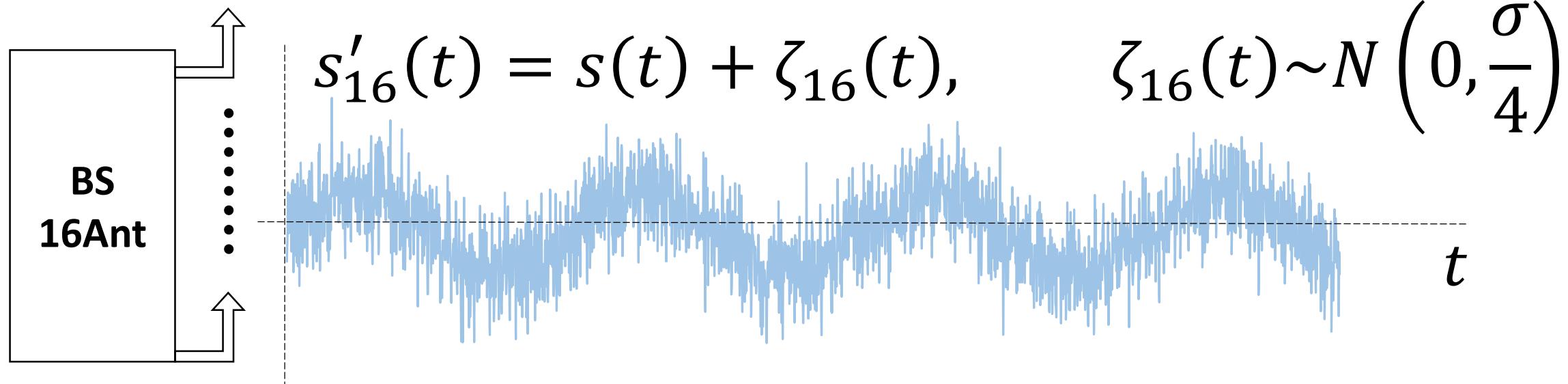
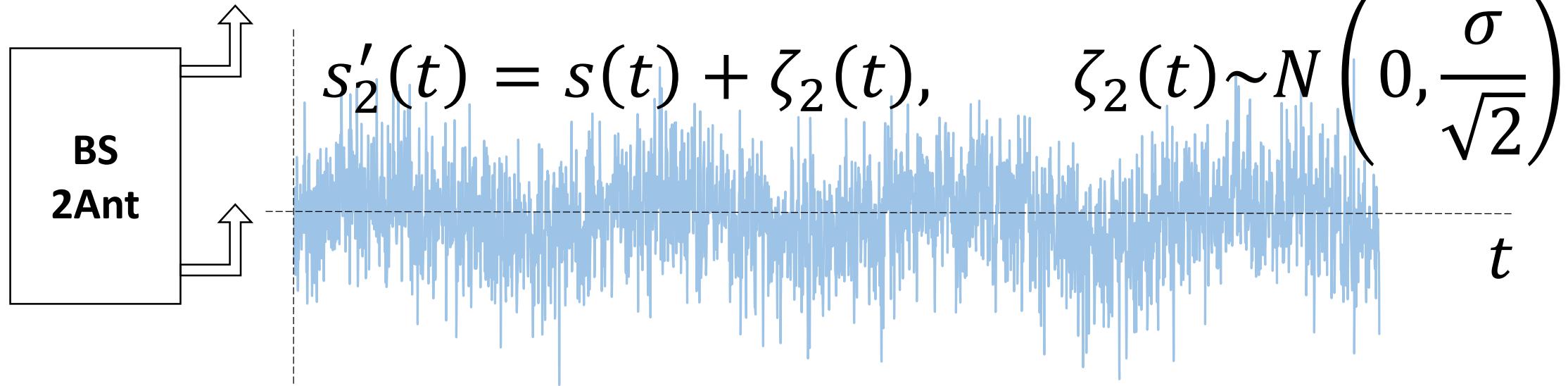
$$s''(t) = s(t) + \zeta(t)$$

$$E[\zeta] = 0$$

$$E[\zeta^2] = \frac{\sigma^2}{2}$$

$$\zeta(t) \sim N\left(0, \frac{\sigma}{\sqrt{2}}\right)$$

$$s'_1(t) = s(t) + \xi(t) \quad \xi(t) \sim N(0, \sigma)$$



# The number of antennas makes difference

- Theoretically, the more antennas we have, the better reception we obtain

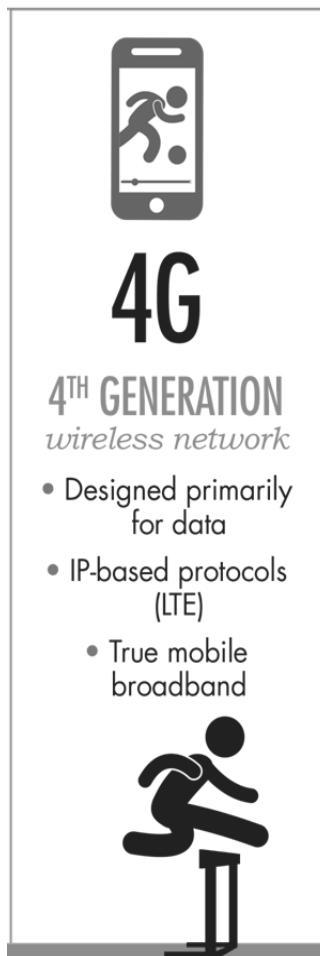
$$s'_{N_{ant}}(t) = s(t) + \zeta_{N_{ant}}(t)$$

$$\zeta_{N_{ant}}(t) \sim N\left(0, \frac{\sigma}{\sqrt{N_{ant}}}\right)$$

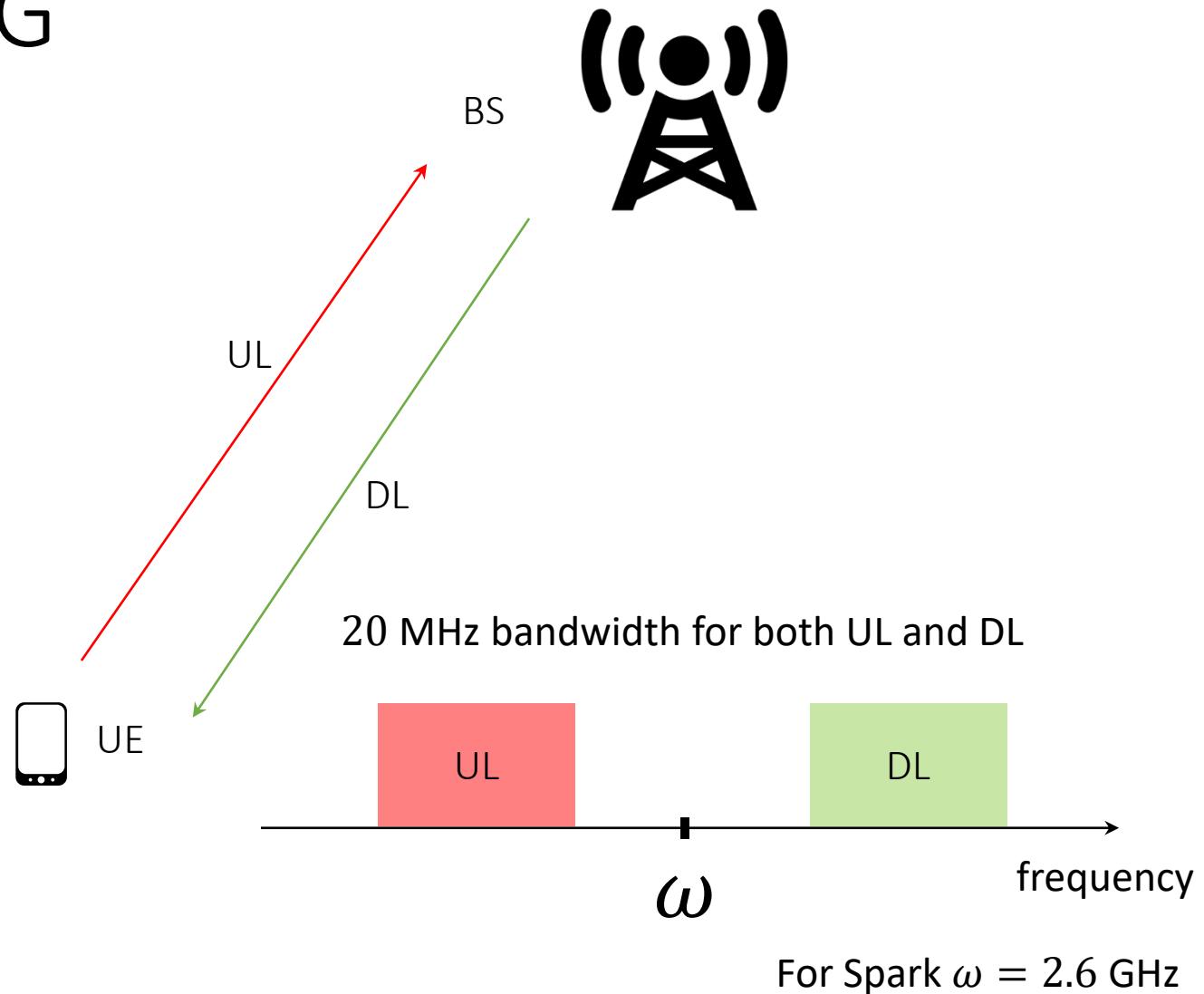
# Outline

- History of mobile communication
- Physical aspects of radio signals
- **Introduction to LTE/4G**
- Massive MIMO approach
- What we do

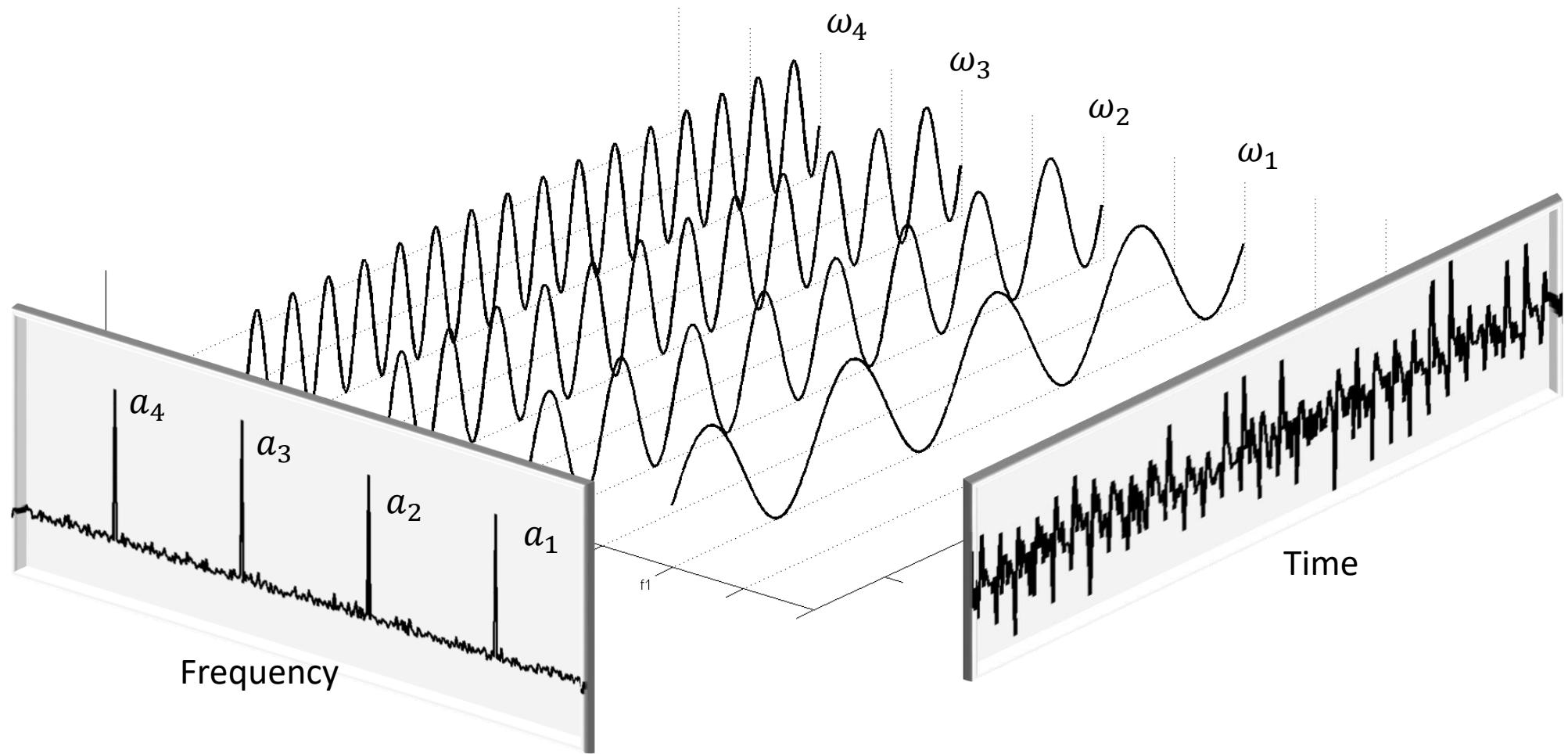
# Introduction to LTE/4G



> 100 Mbps  
2011



# LTE uses OFDM

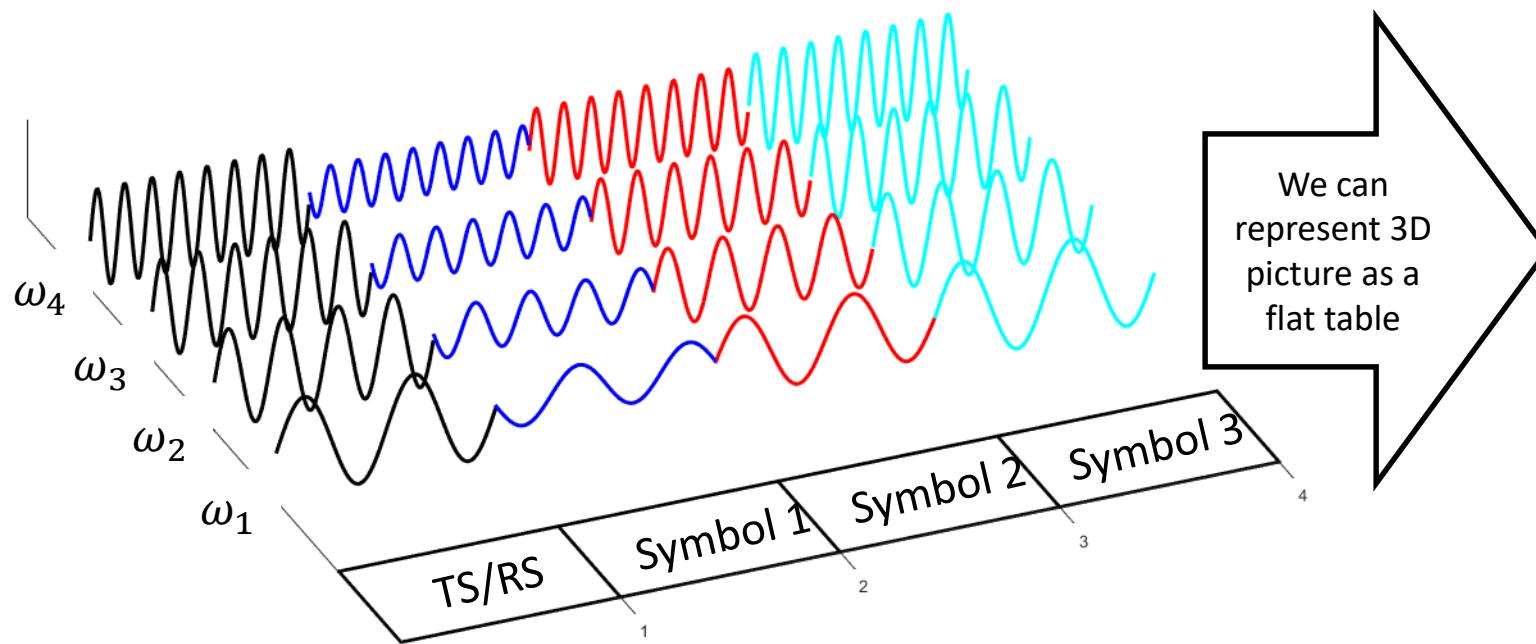


Orthogonal channels (subcarriers) can be shared among up to four users, or can be used by one user. Flexible approach for resource allocating

# LTE uses OFDM

- OFDM – Orthogonal Frequency Division Multiplexing is a technique, which allows to increase a transmission rate without increasing the sampling rate of a communication system.
- The technique utilizes a number of orthogonal subcarriers (sine waves) to transmit data in a parallel manner

# LTE Signal at Physical Layer



Reference Symbol

Symbol 1

Symbol 2

Symbol 3

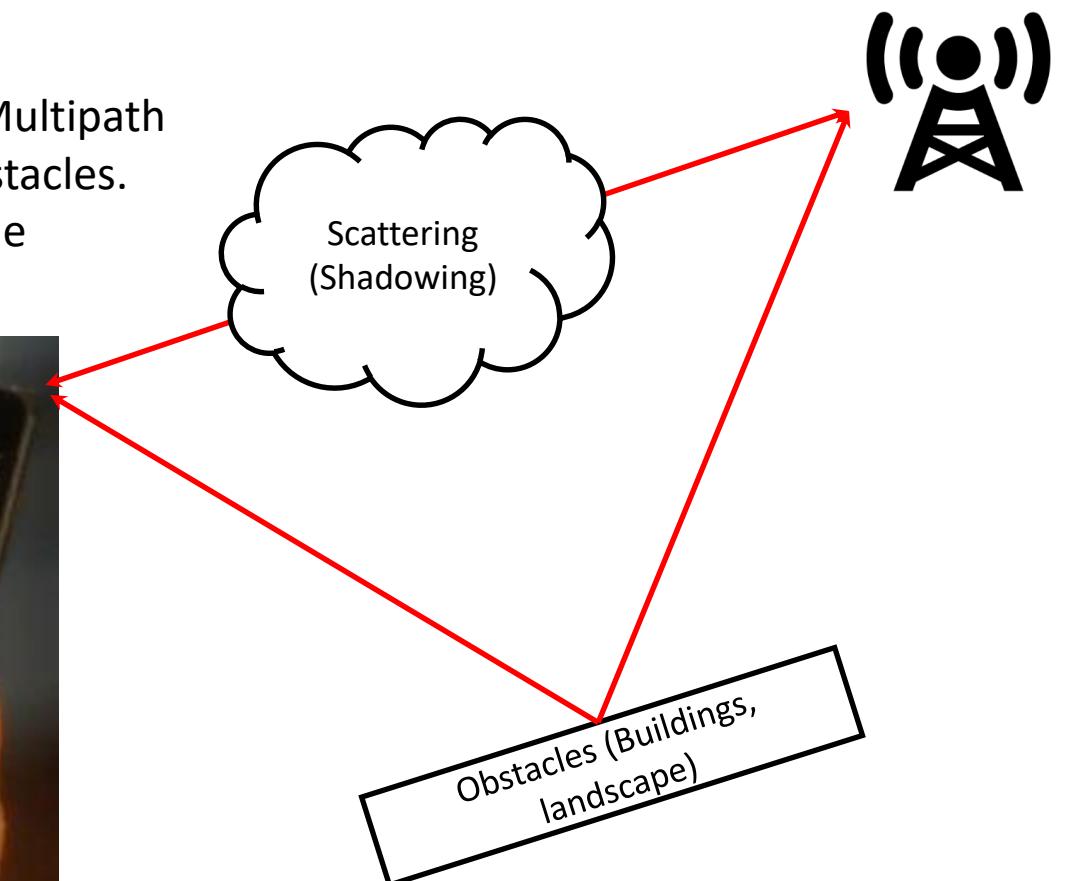
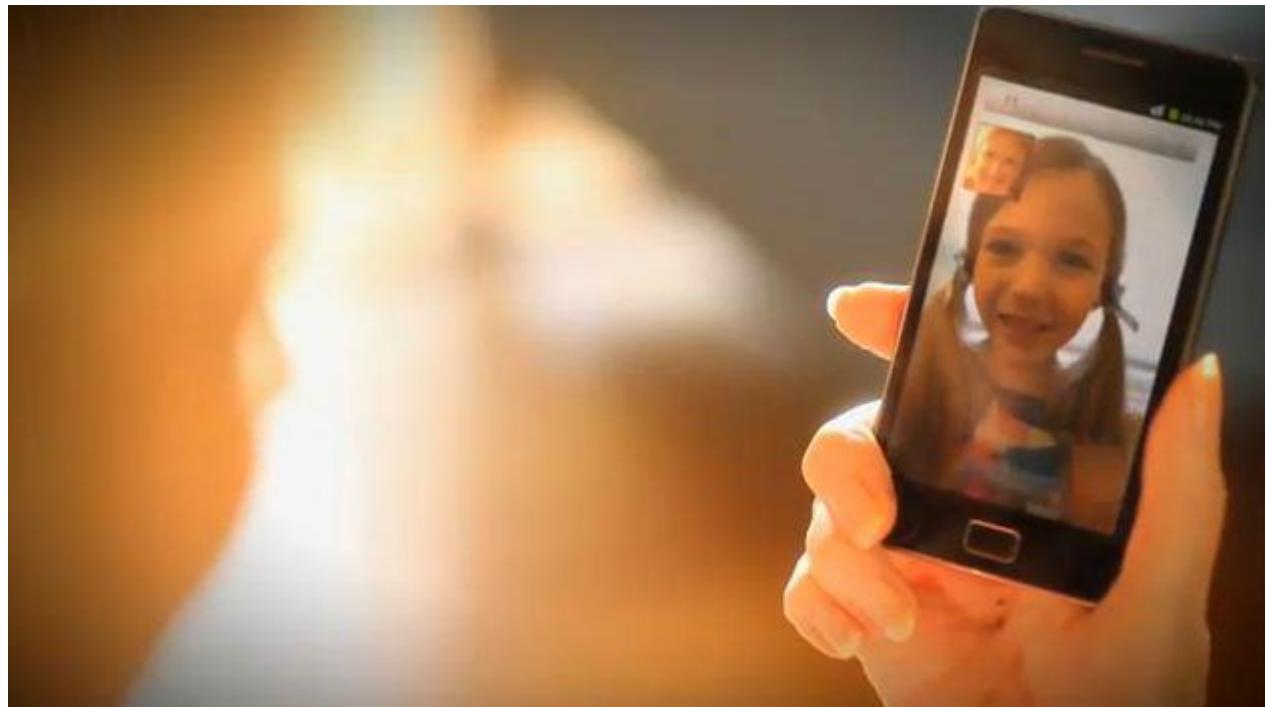
RS1	$a_1$	$a_5$	$a_9$
RS2	$a_2$	$a_6$	$a_{10}$
RS3	$a_3$	$a_7$	$a_{11}$
RS3	$a_4$	$a_8$	$a_{12}$

Such a spreadsheet is called as Resource Block (RB)

Reference Symbols are used to estimate the channel through which signals are transmitted

# What is Multipath Propagation Channel?

Multipath effects occur in a wireless channel, which is called Multipath channel, where a transmitted signal reflects from different obstacles. Instead of one signal, the receiver receives several copies of the transmitted signal.



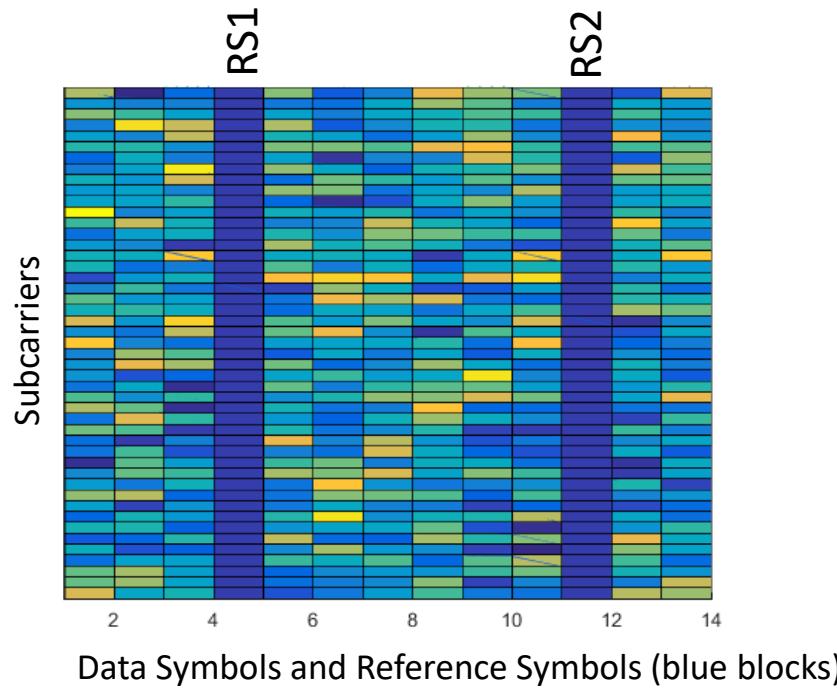
Video Call is loading channel in both sides  
High network capacity must be performed in both sides

# Channel estimation stage

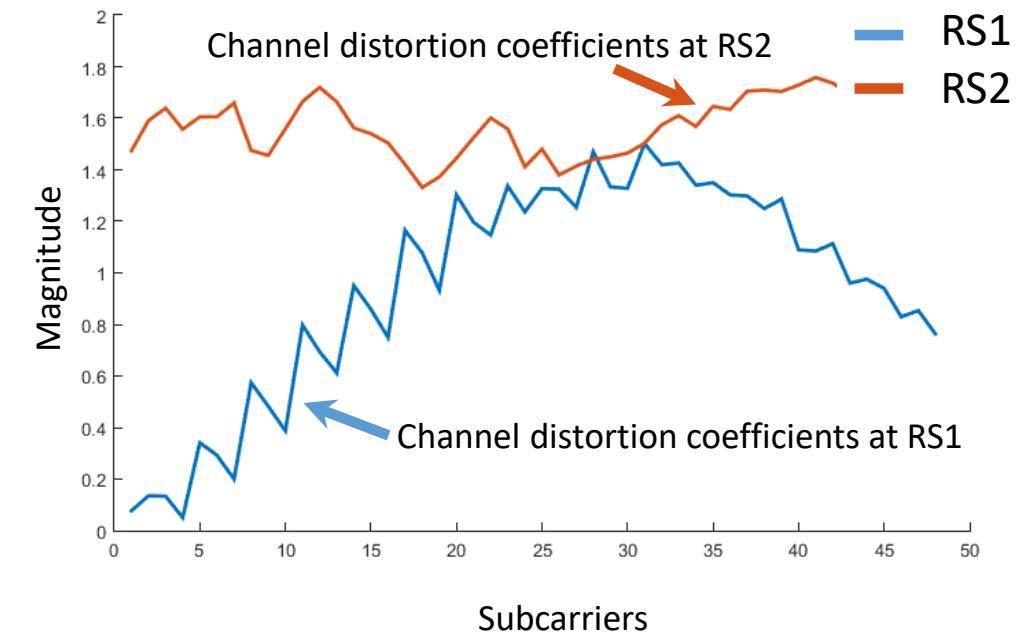
Resource Block from example

RS	Symbol 1	Symbol 2	Symbol 3
RS1	$a_1$	$a_5$	$a_9$
RS2	$a_2$	$a_6$	$a_{10}$
RS3	$a_3$	$a_7$	$a_{11}$
RS3	$a_4$	$a_8$	$a_{12}$

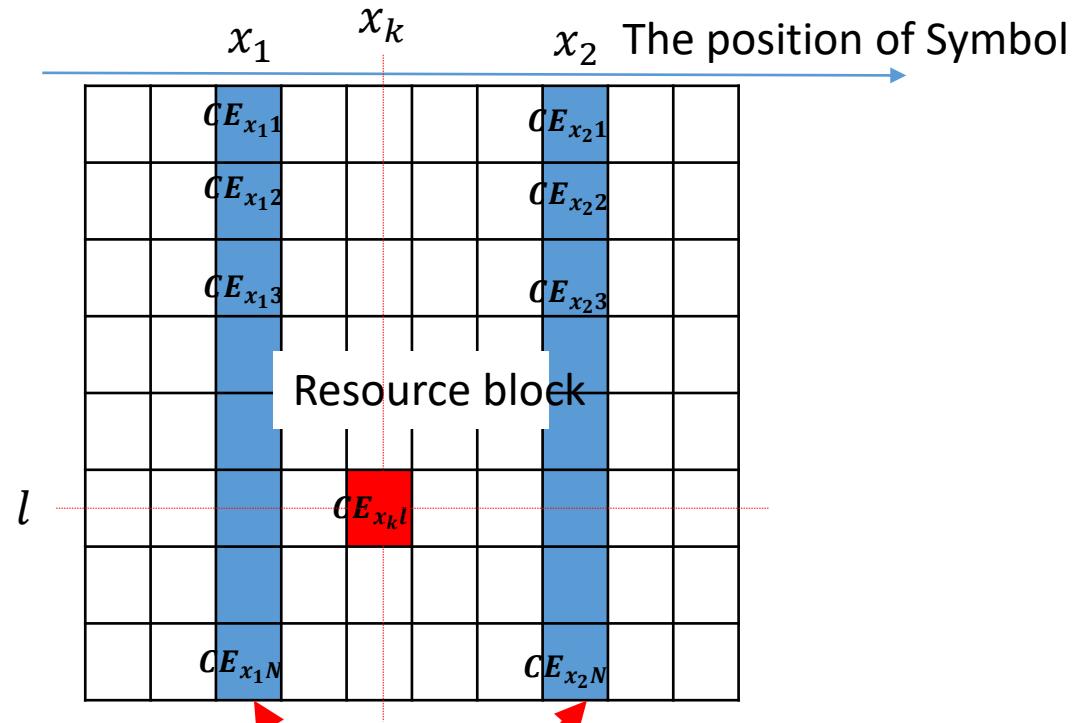
Typical Resource Block in LTE



Channel estimation is performed by using RSSs



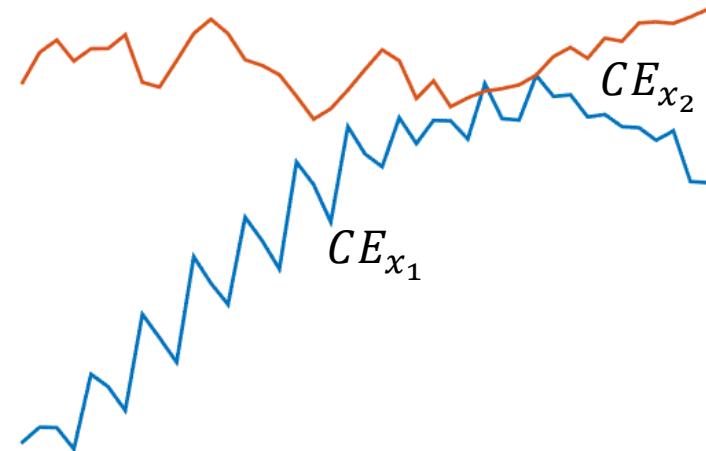
# The main weak place in CE is approximation



We estimated the channel at these places

Linear approximation

$$CE_{x_kl} = \frac{CE_{x_2l} - CE_{x_1l}}{x_2 - x_1} (x_k - x_1) + CE_{x_1l}$$



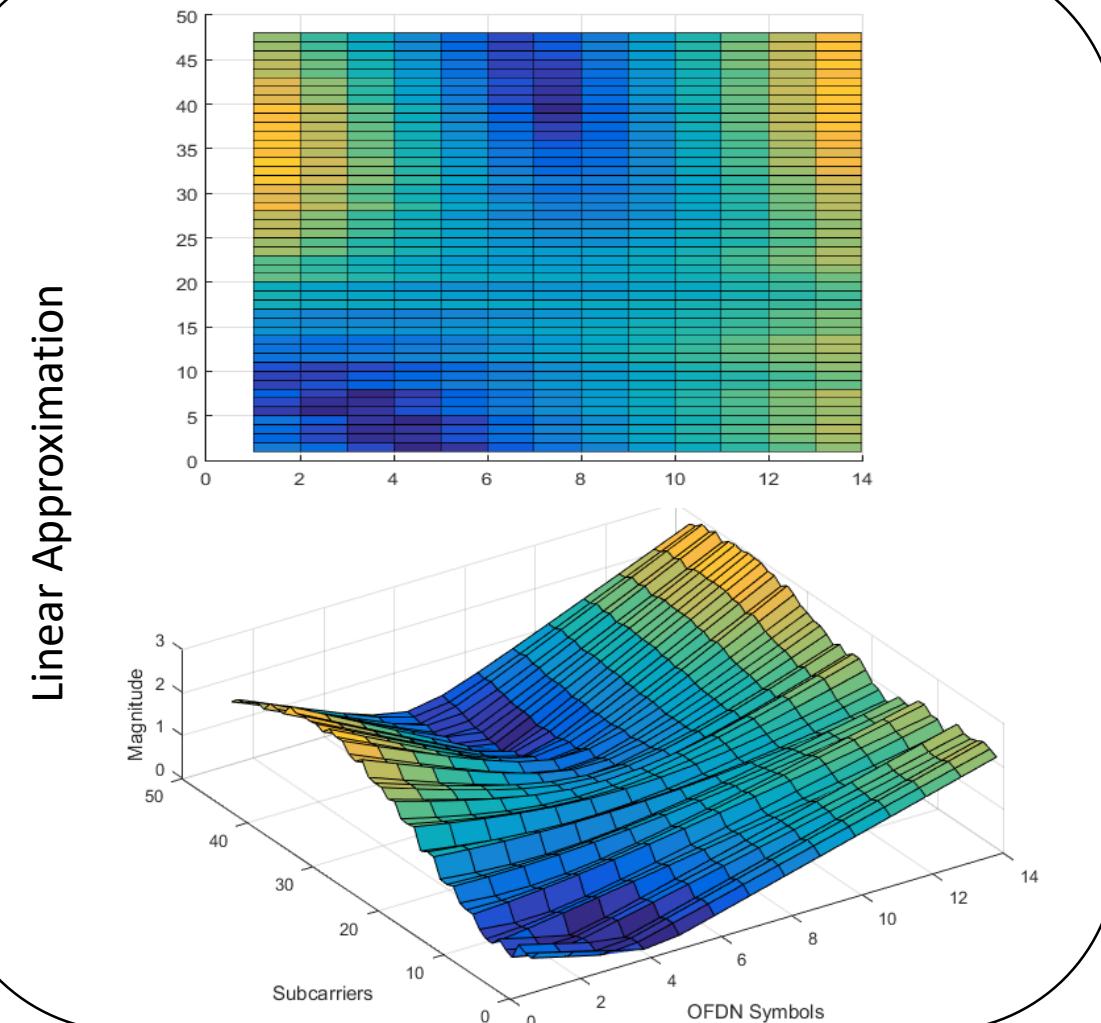
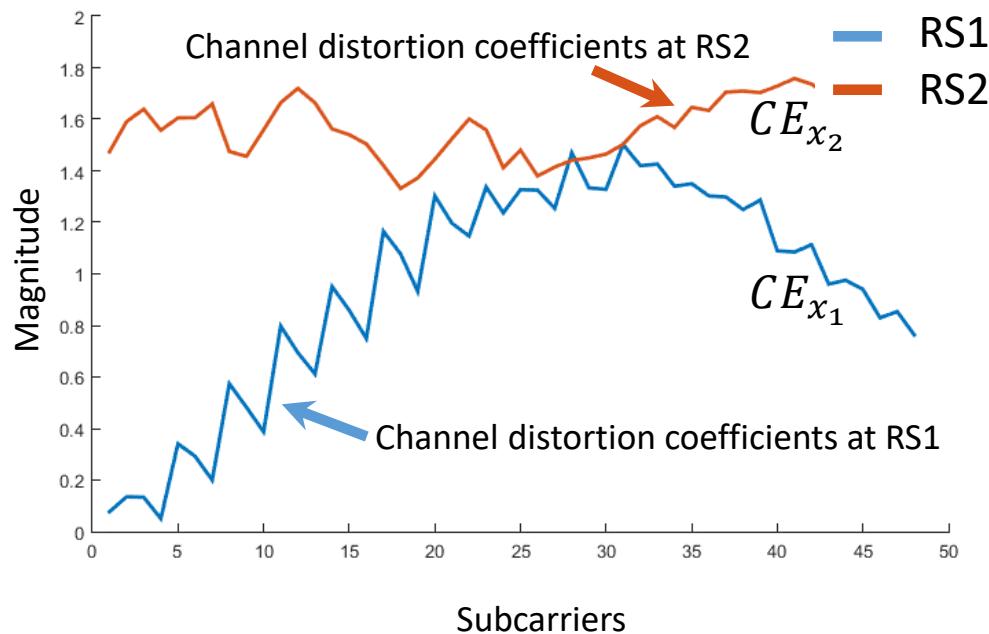
There are a lot of approaches in channel approximation, we will consider the easiest one: linear approximation

# Linear approximation results

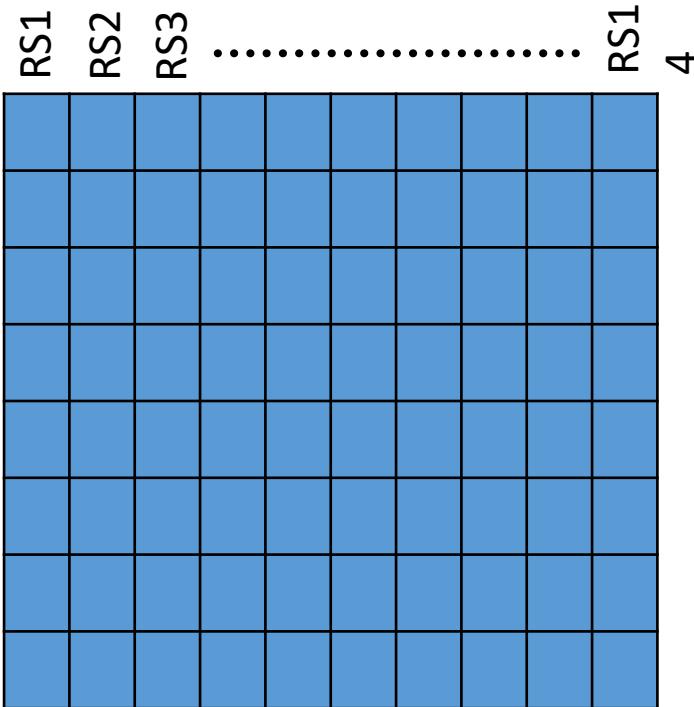
Linear approximation

$$CE_{x_kl} = \frac{CE_{x_2l} - CE_{x_1l}}{x_2 - x_1} (x_k - x_1) + CE_{x_1l}$$

Channel estimation is performed by using RSs

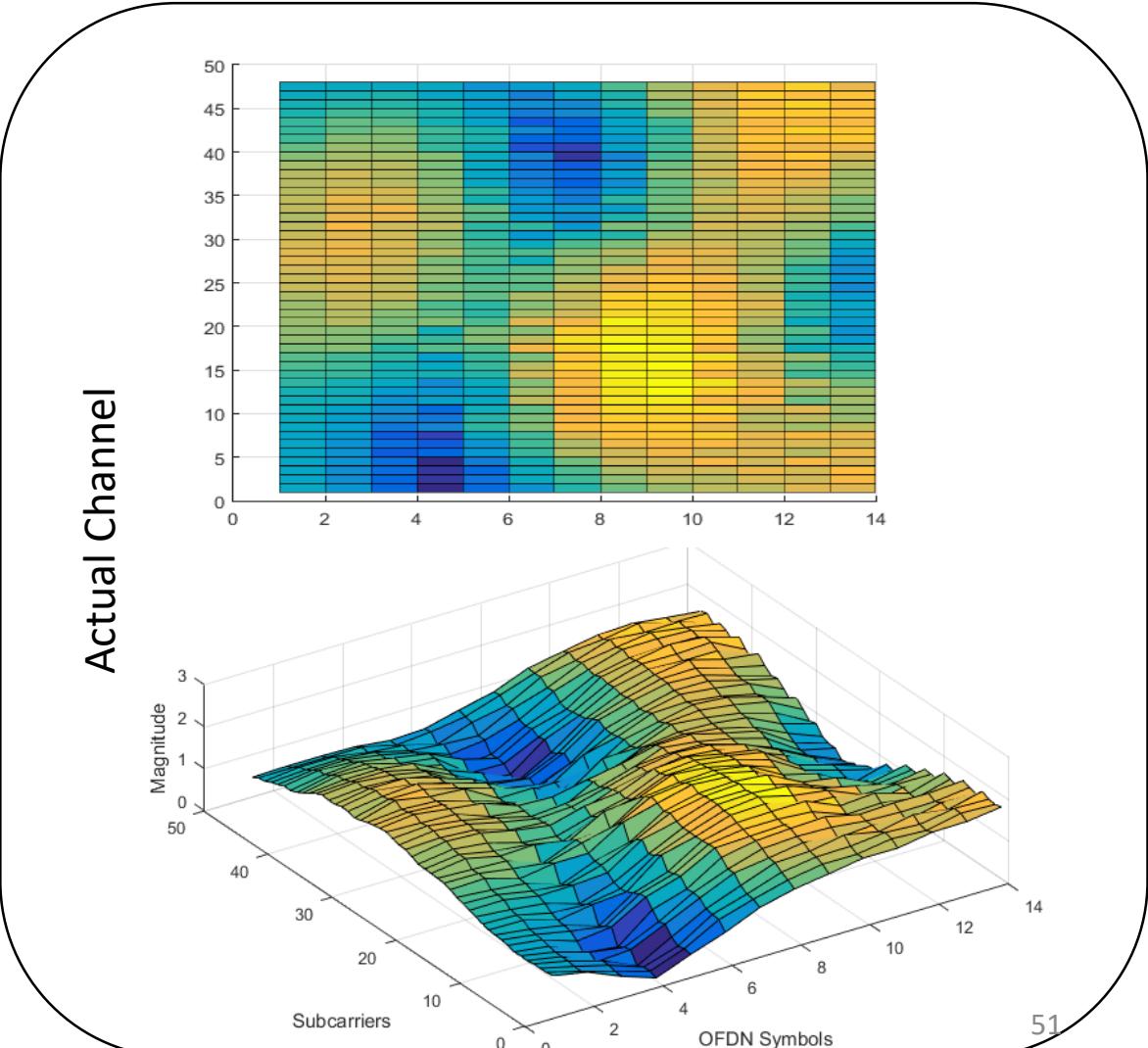


# Calculation of actual channel



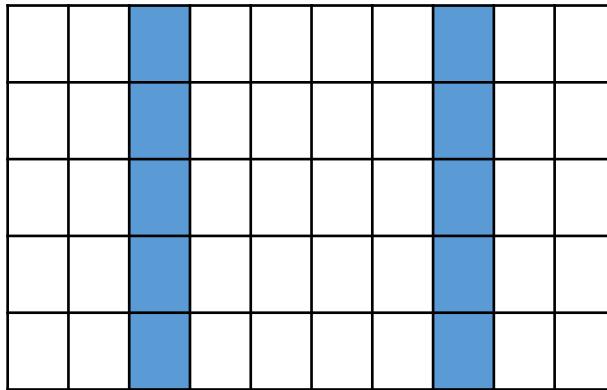
Whole resource block is fill by reference symbols

$$CE_{kl} = \frac{RS'_{kl}}{RS_{kl}}$$



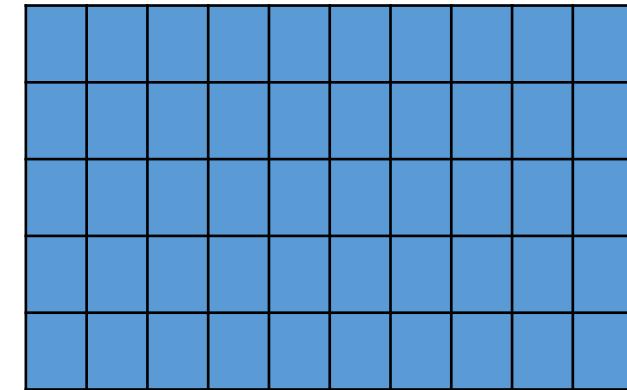
# Comparison of Estimated Channel and Actual Channel

Two RSs among Symbols

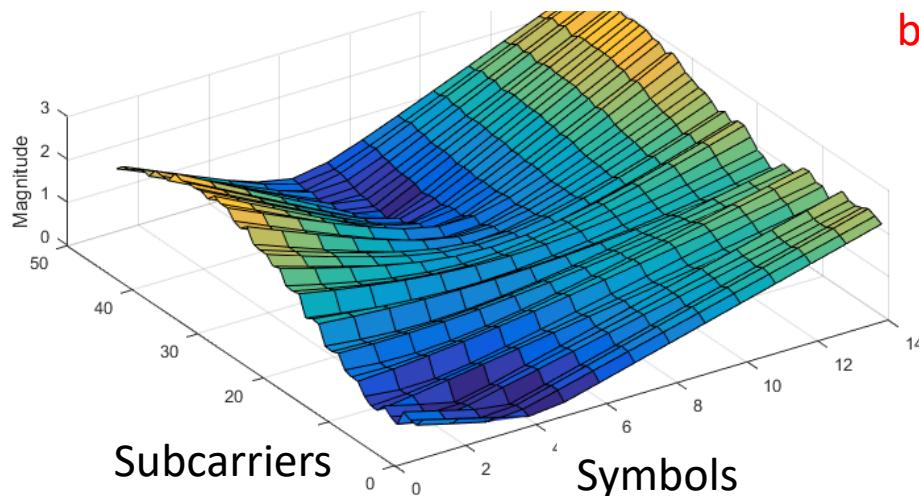


Multipath Channel is complicated object in wireless communication area, which must be accurately estimated for further correct data receiving  
(ref. page 10)

All Symbols are RS

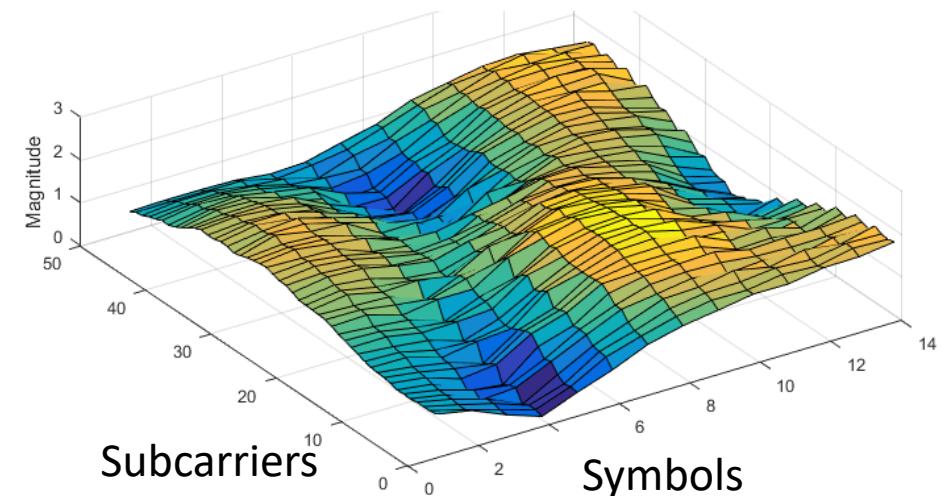


Not accurate estimation



There is trade off between accuracy of CE and the amount of transmitted data

Accurate estimation

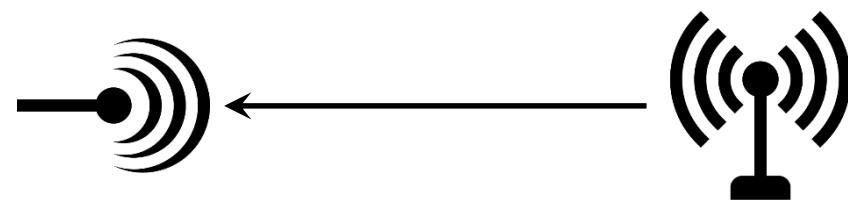


Can we eliminate CE  
or  
decrease its complexity?

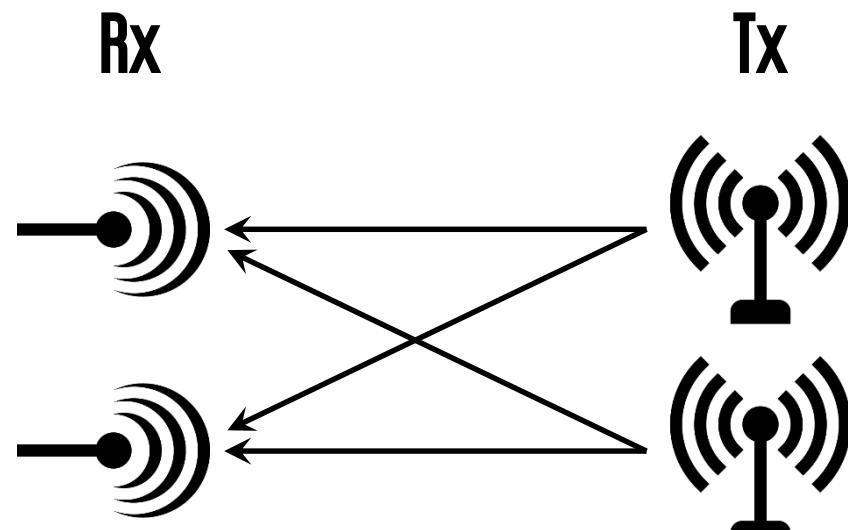
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# Massive MIMO and big antenna arrays?



SISO – Single Input Single Output

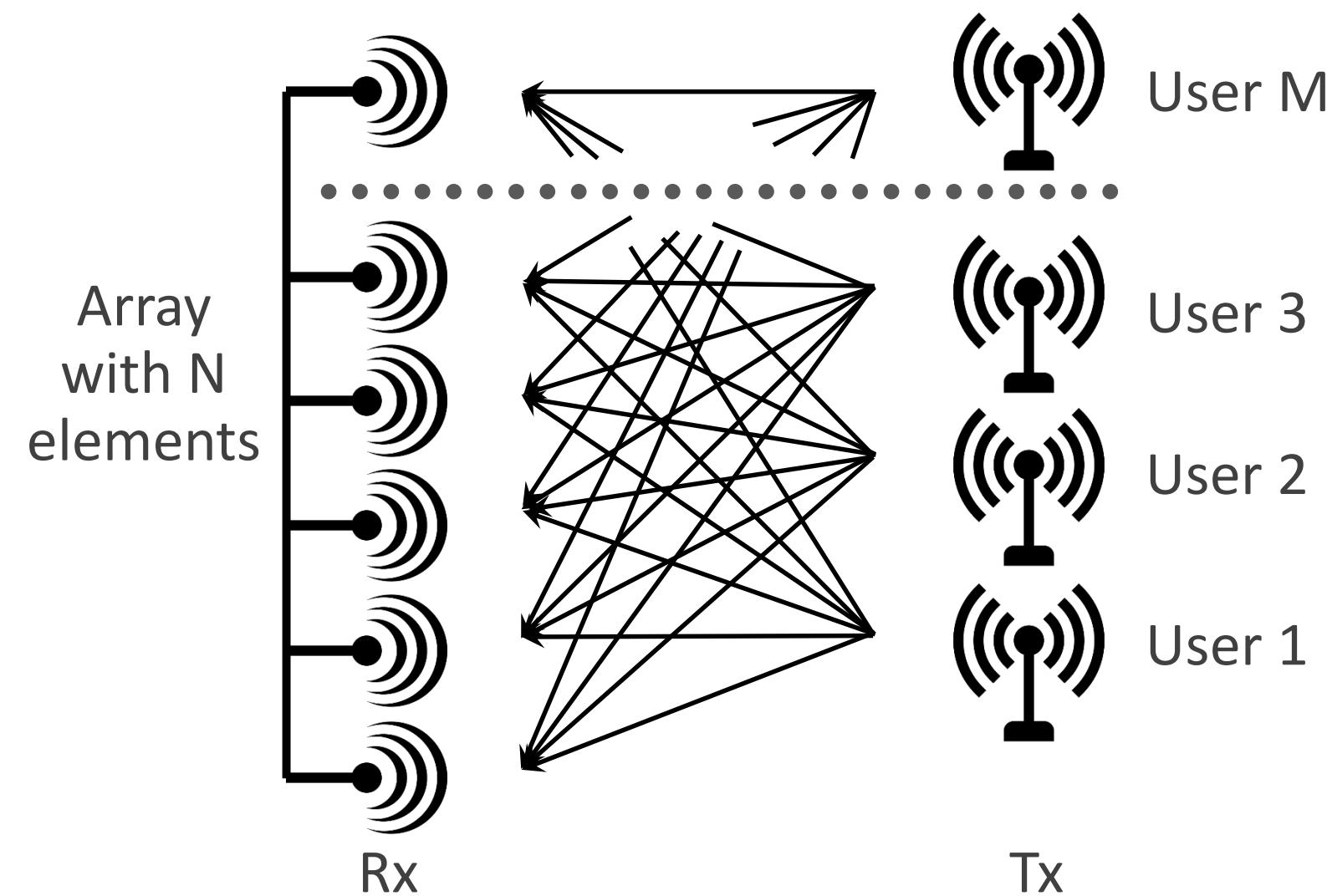


2x2 MIMO

MIMO – Multiple Input Multiple Output

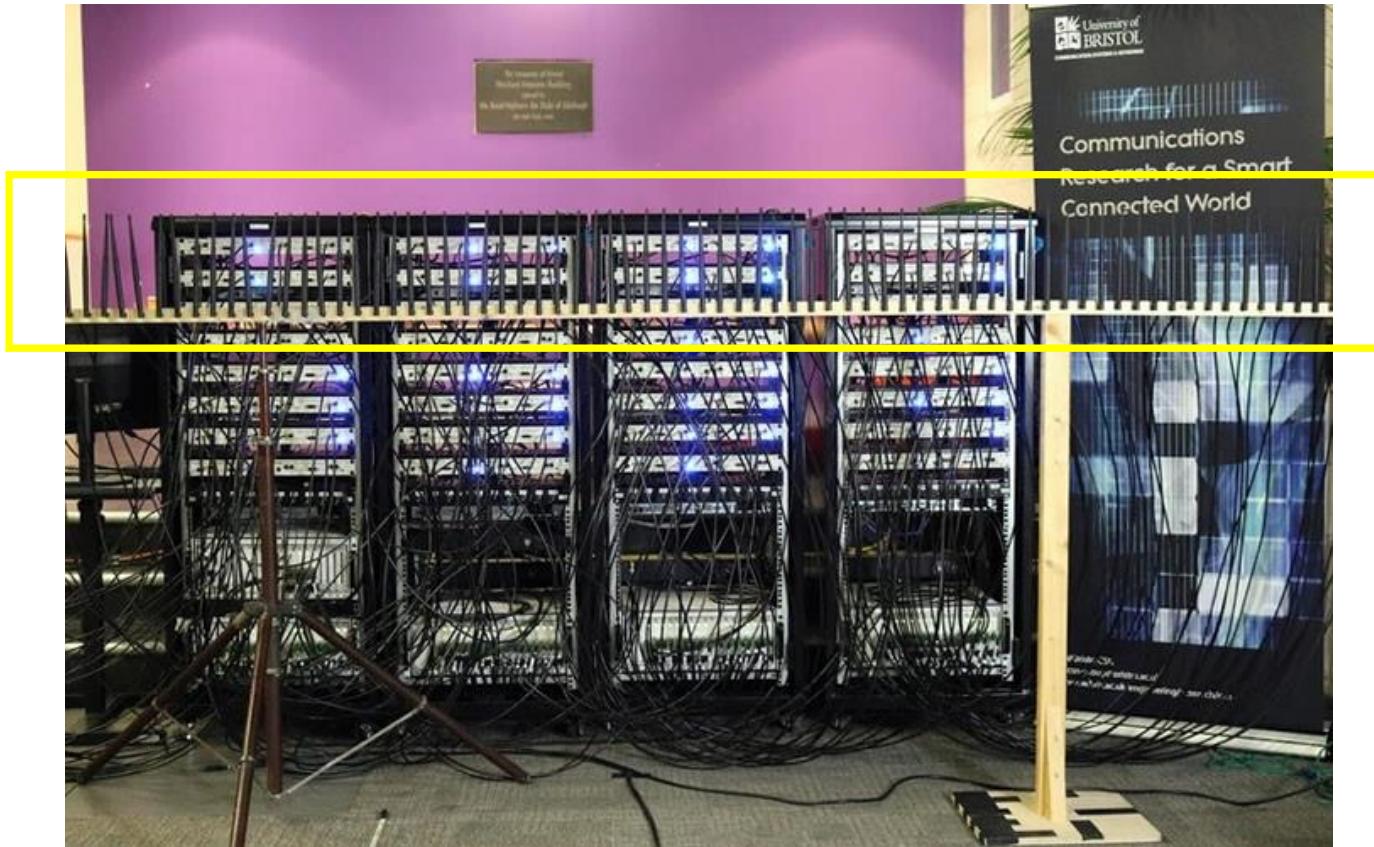
4x4 MIMO 8x2 MIMO 8x8 MIMO

# What is massive MIMO and big antenna arrays?



**Massive MIMO** when the system has a really big amount of Users and a big antenna array.

# Existing massive MIMO prototypes

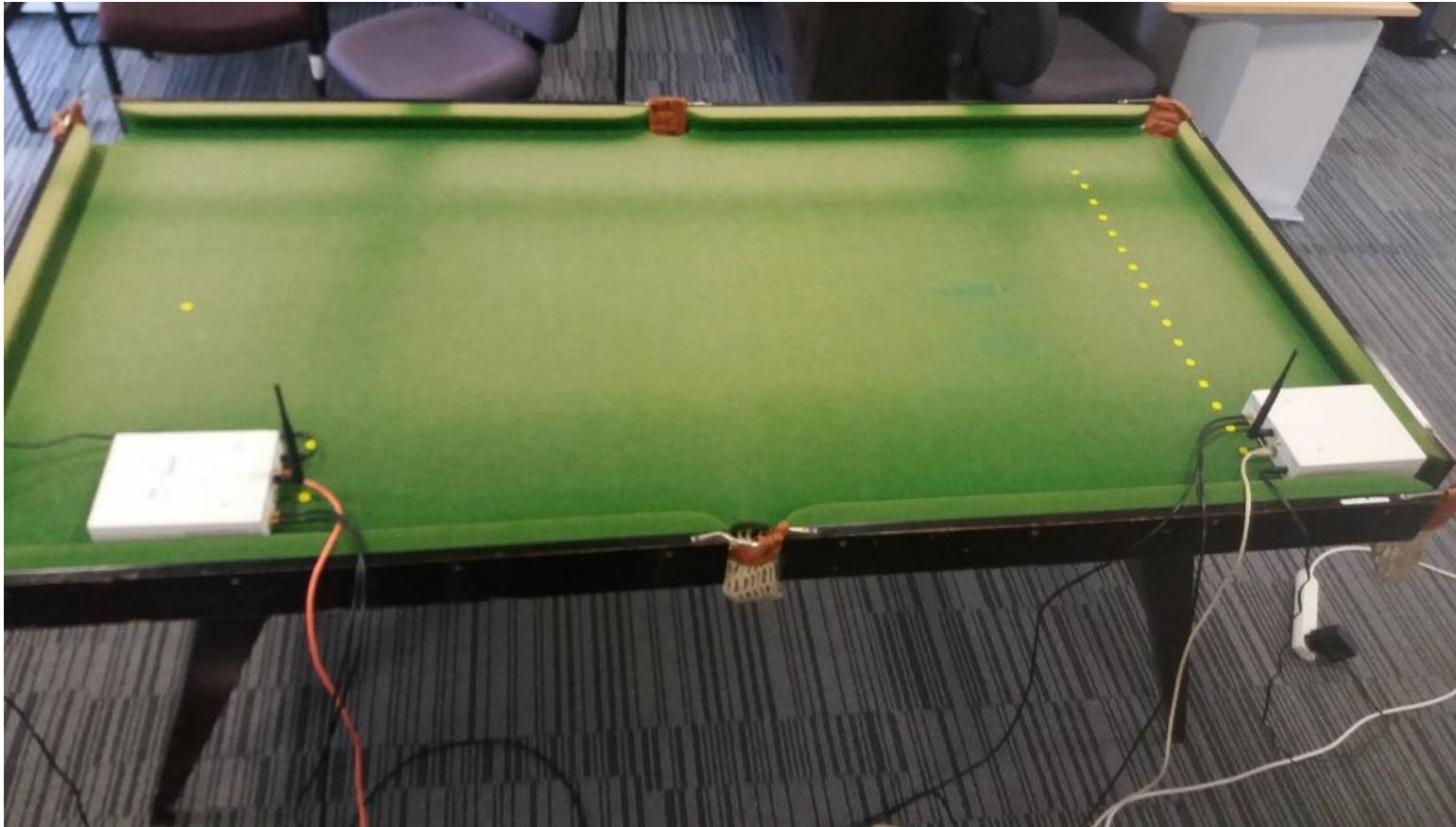


University of Bristol (England)



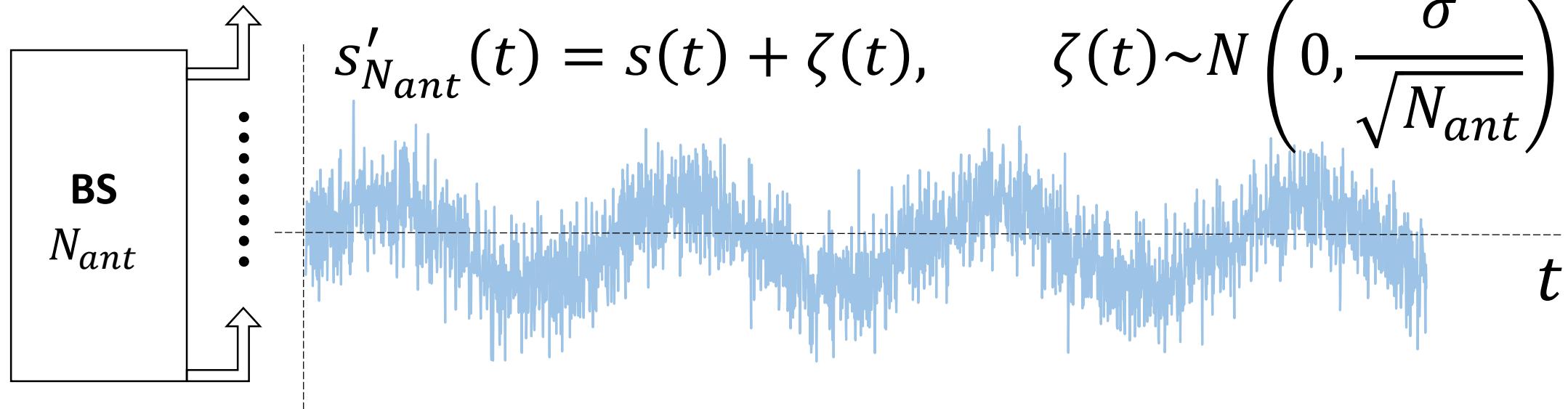
Lund University (Sweden)

# Massive MIMO prototype in Otago University

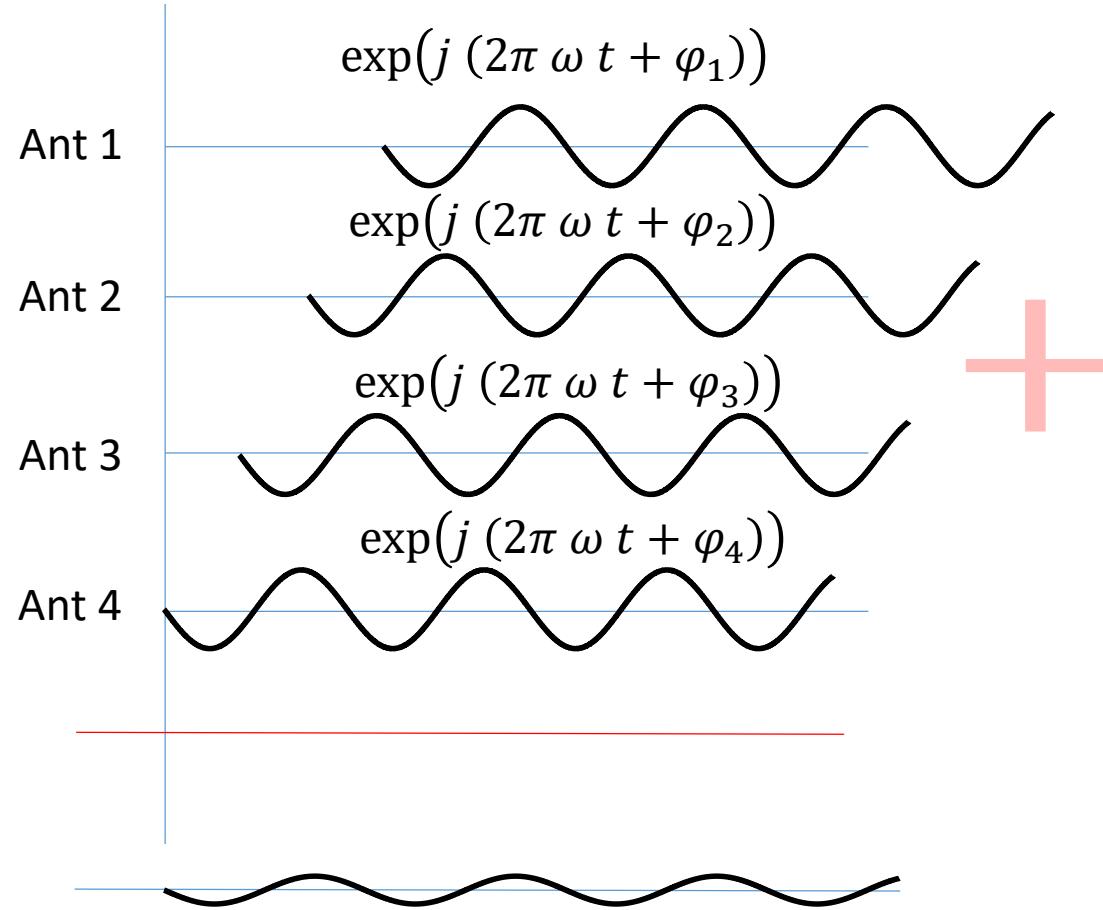


University of Otago (New Zealand)

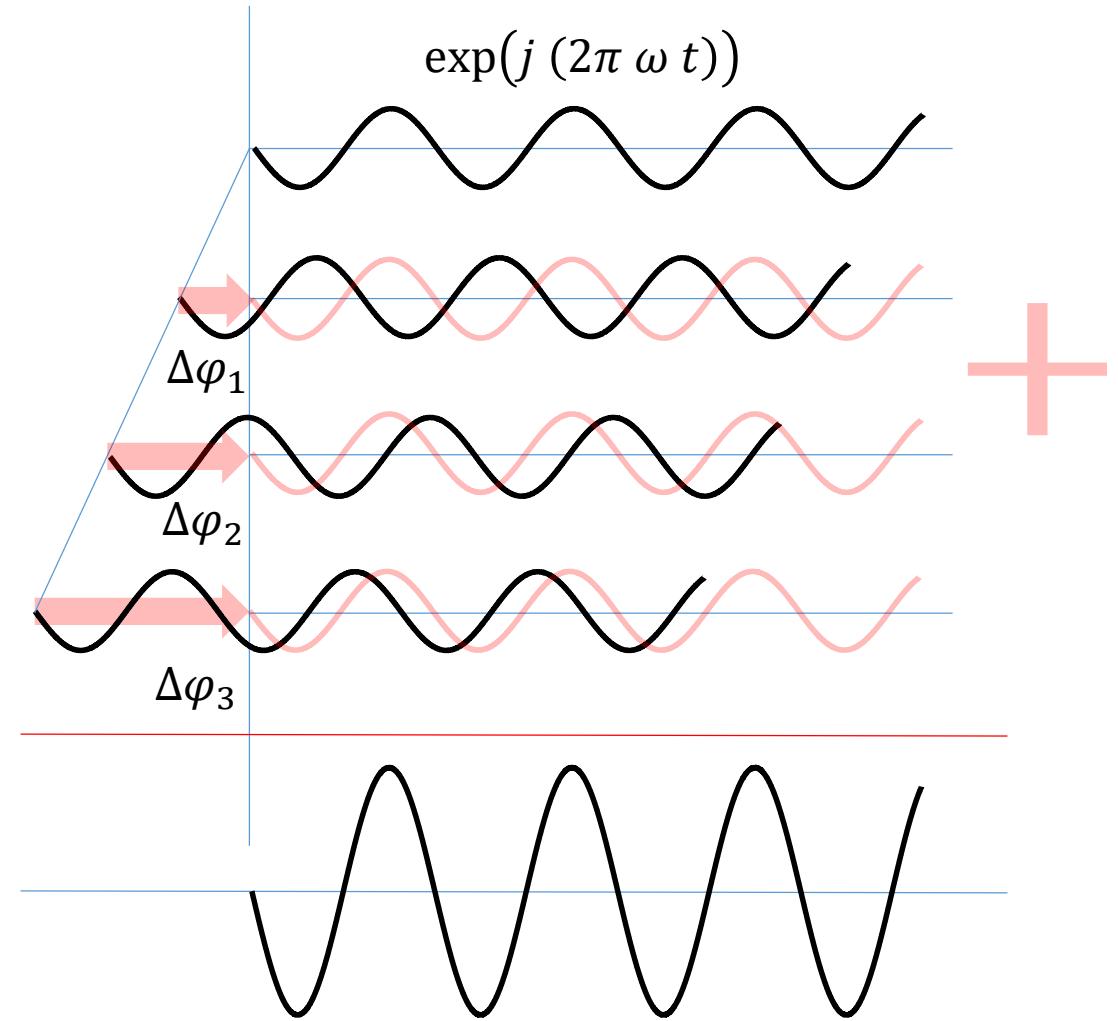
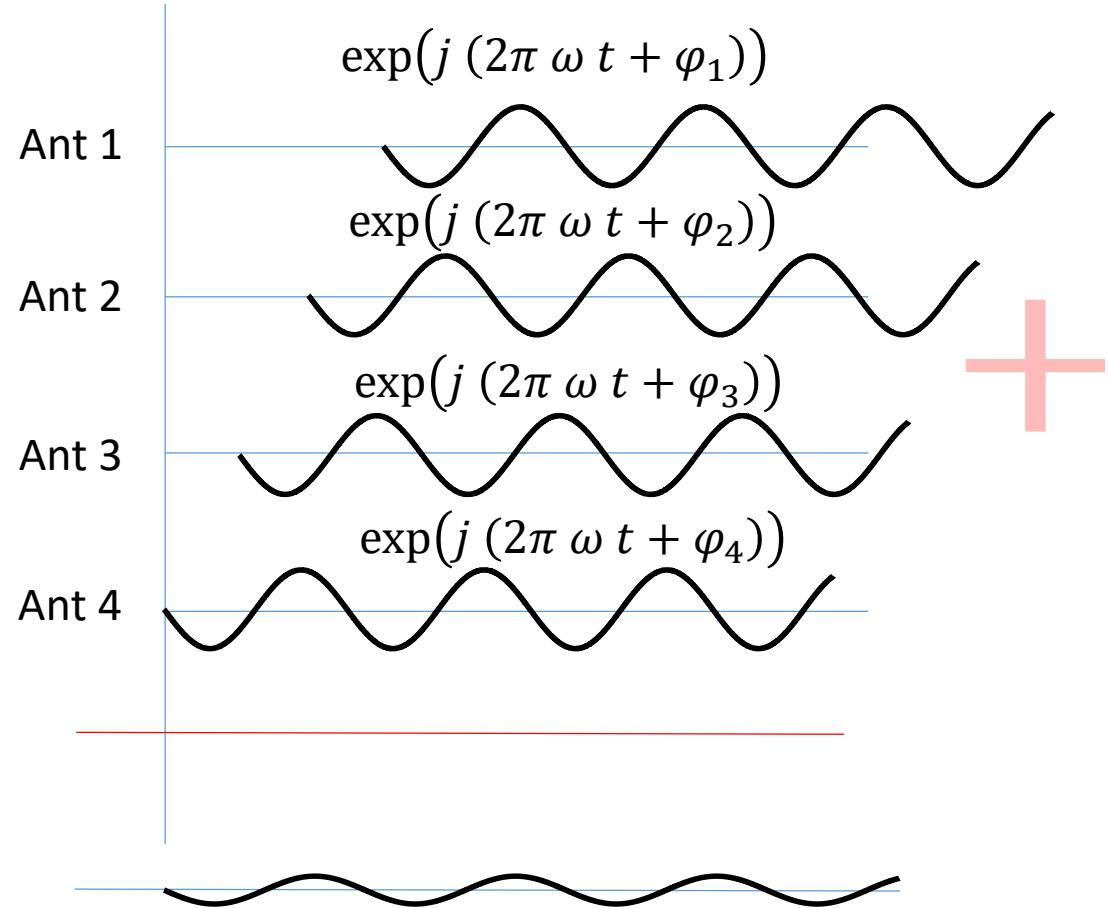
# Benefits of Massive MIMO



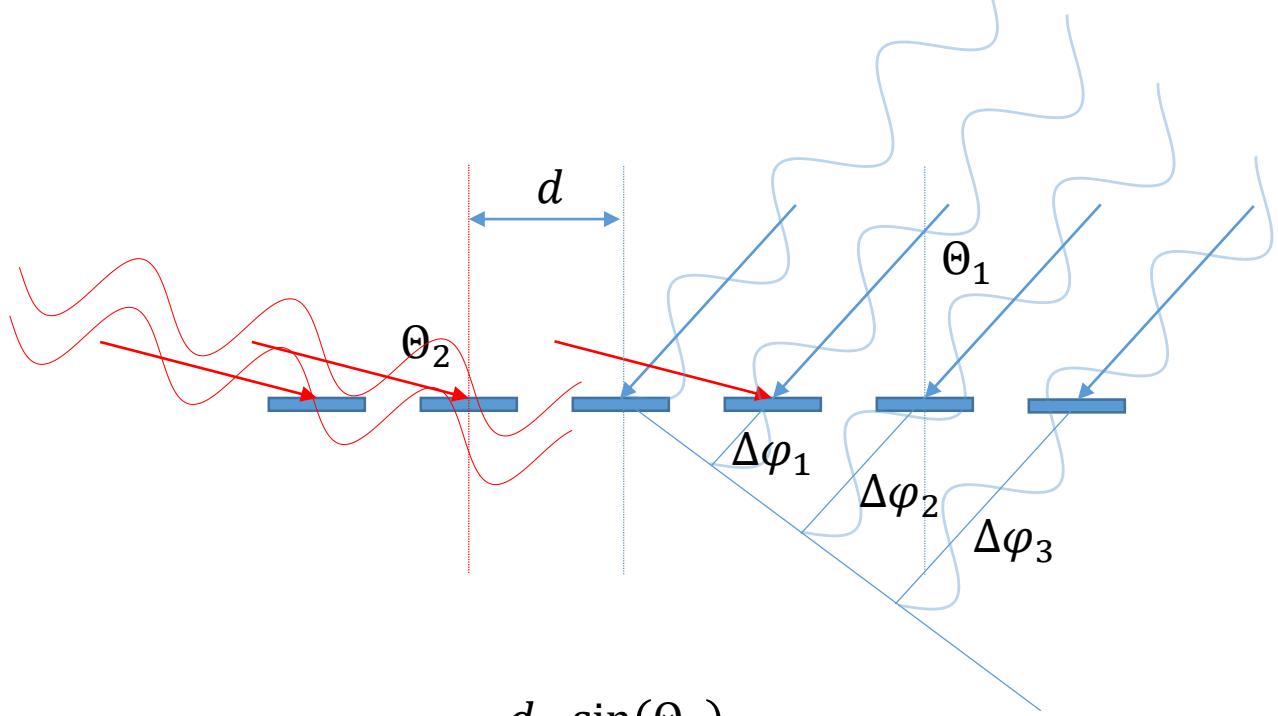
# Coherent reception by all antennas



# Coherent reception by all antennas



# Counting Angle of Arrival



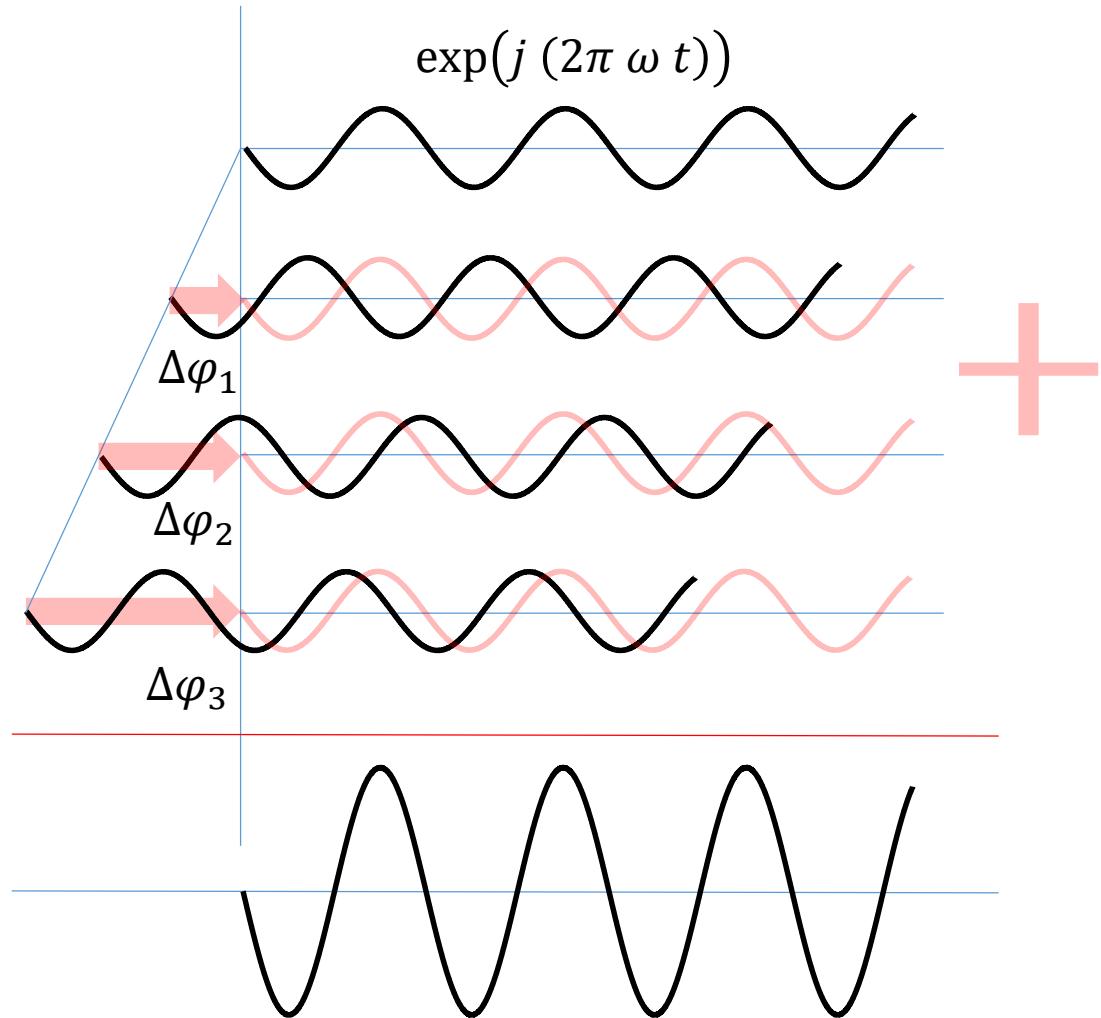
$$\Delta t_1 = \frac{d \cdot \sin(\Theta_1)}{c}$$

$$\Delta\varphi_1 = \Delta t_1 \cdot \omega$$

$$\Delta\varphi_2 = 2 \Delta\varphi_1$$

$\vdots$

$$\Delta\varphi_N = (N - 1) \Delta\varphi_1$$



# Outline

- History of mobile communication
- Physical aspects of radio signals
- Introduction to LTE/4G
- Massive MIMO approach
- **What we do**

# What we do

We increase throughput and quality of connection

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We increase throughput and quality of connection

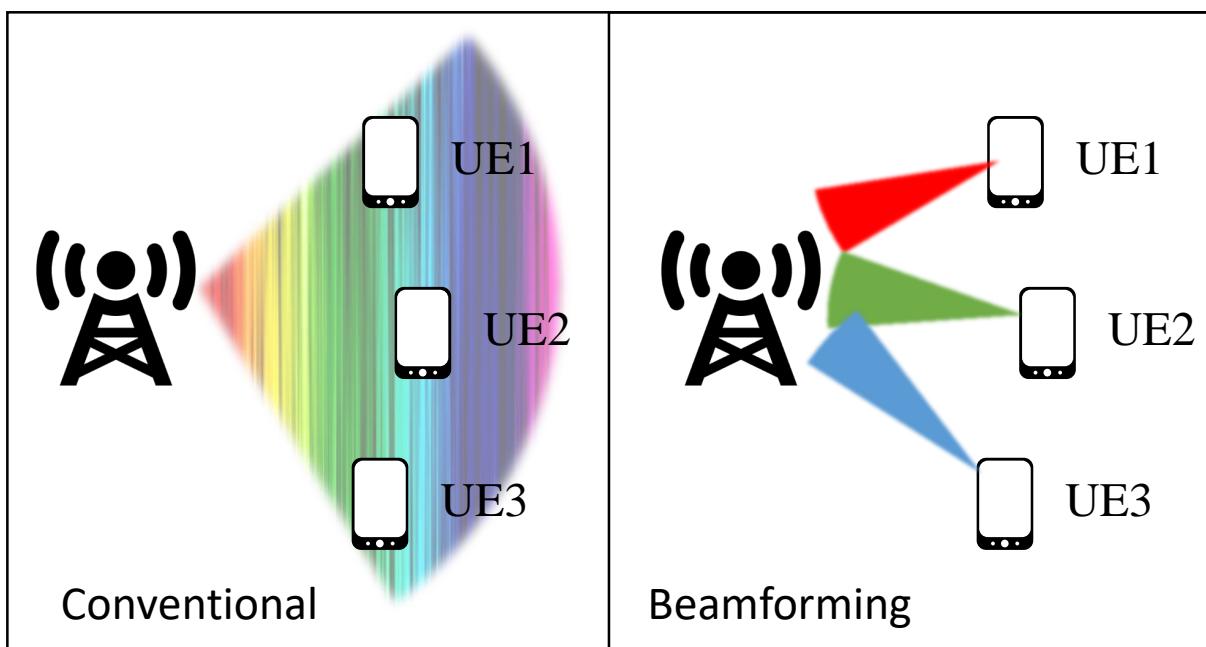


Beamforming

# What we do

We increase throughput and quality of connection

→ Beamforming



Advantages:

1. Increase the signal's power
2. Reduce users interference
3. Radio resource reuse

# What we do

We increase throughput and quality of connection



→ Beamforming



→ Localization

# What we do

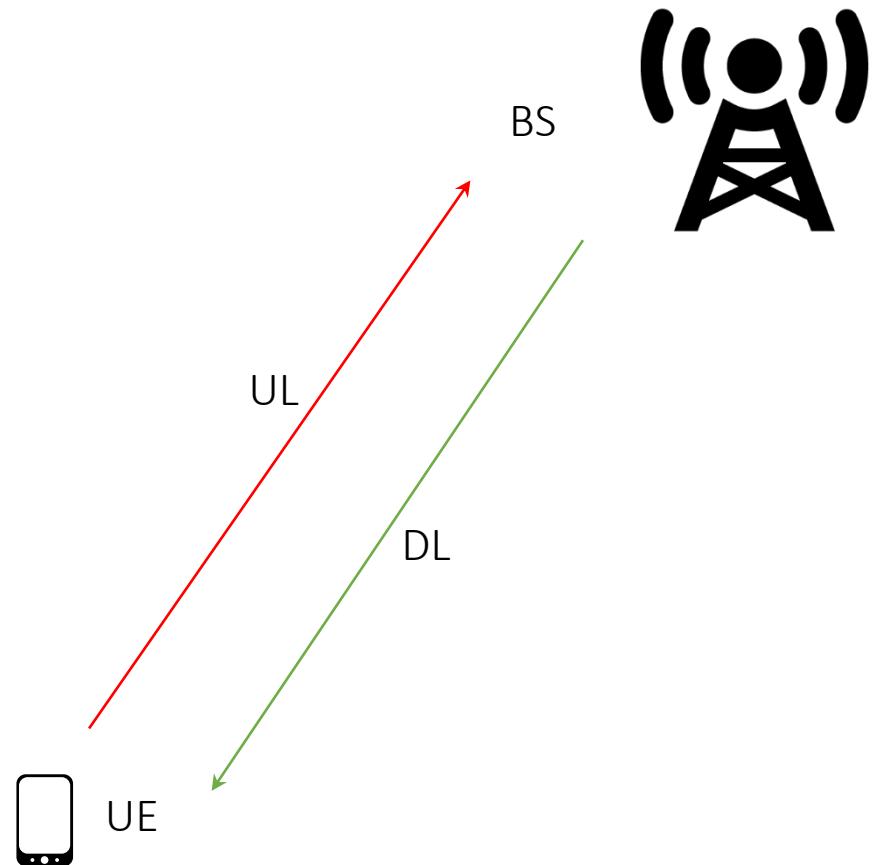
We increase throughput and quality of connection

→ Beamforming

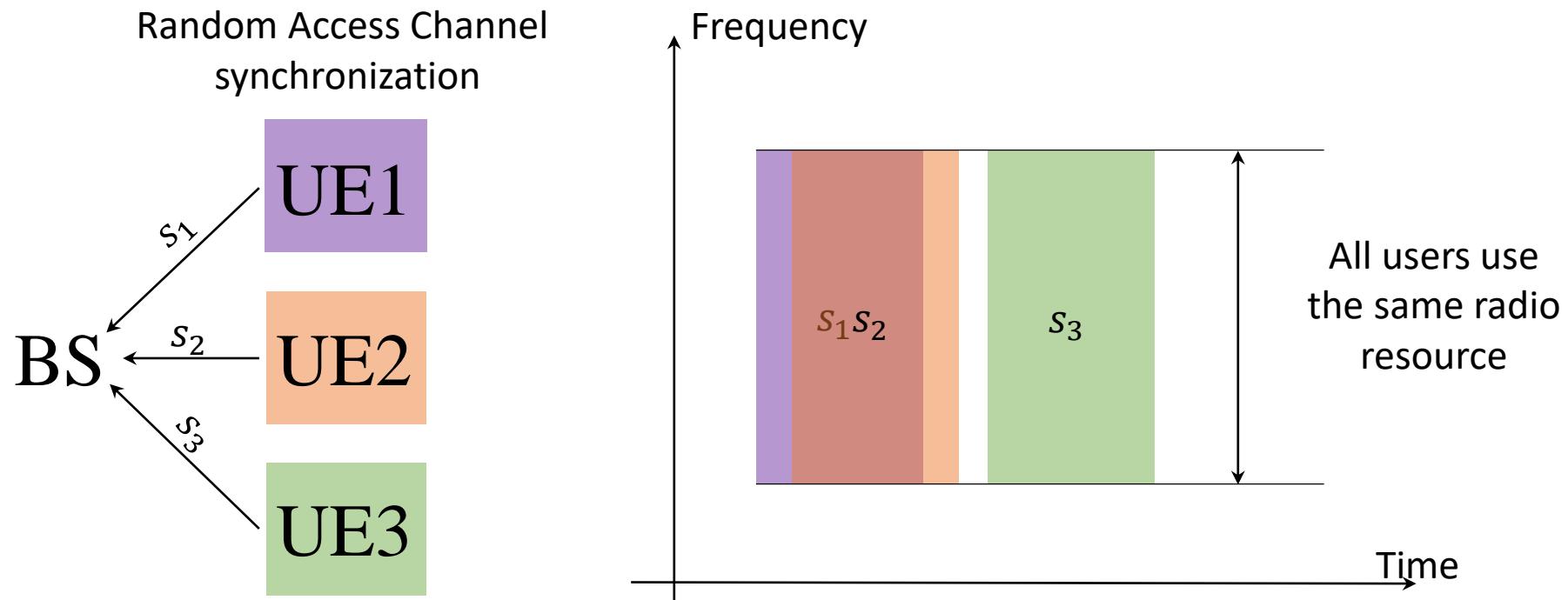
→ Localization

It is challenging task in radio spectrum,  
while obvious in visible light spectrum

# Theory behind Users localization



# Connection to a network

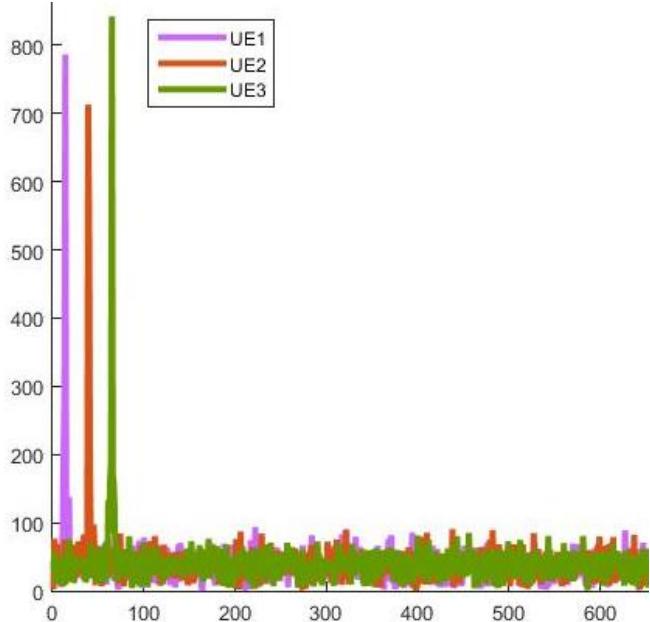


We want to localize users during the connection setup phase as this is going to be used for beam generation.

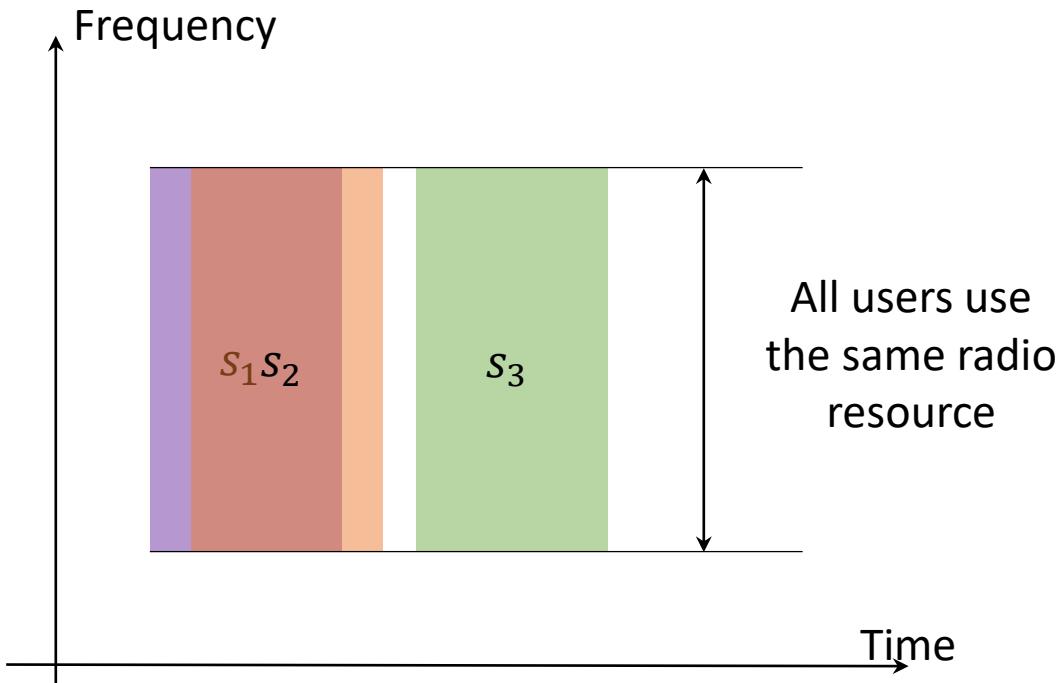
$$s_{BS} = s_1 + s_2 + s_3 + \text{noise}$$

# Distinguishing of the users

The BS perception



Frequency



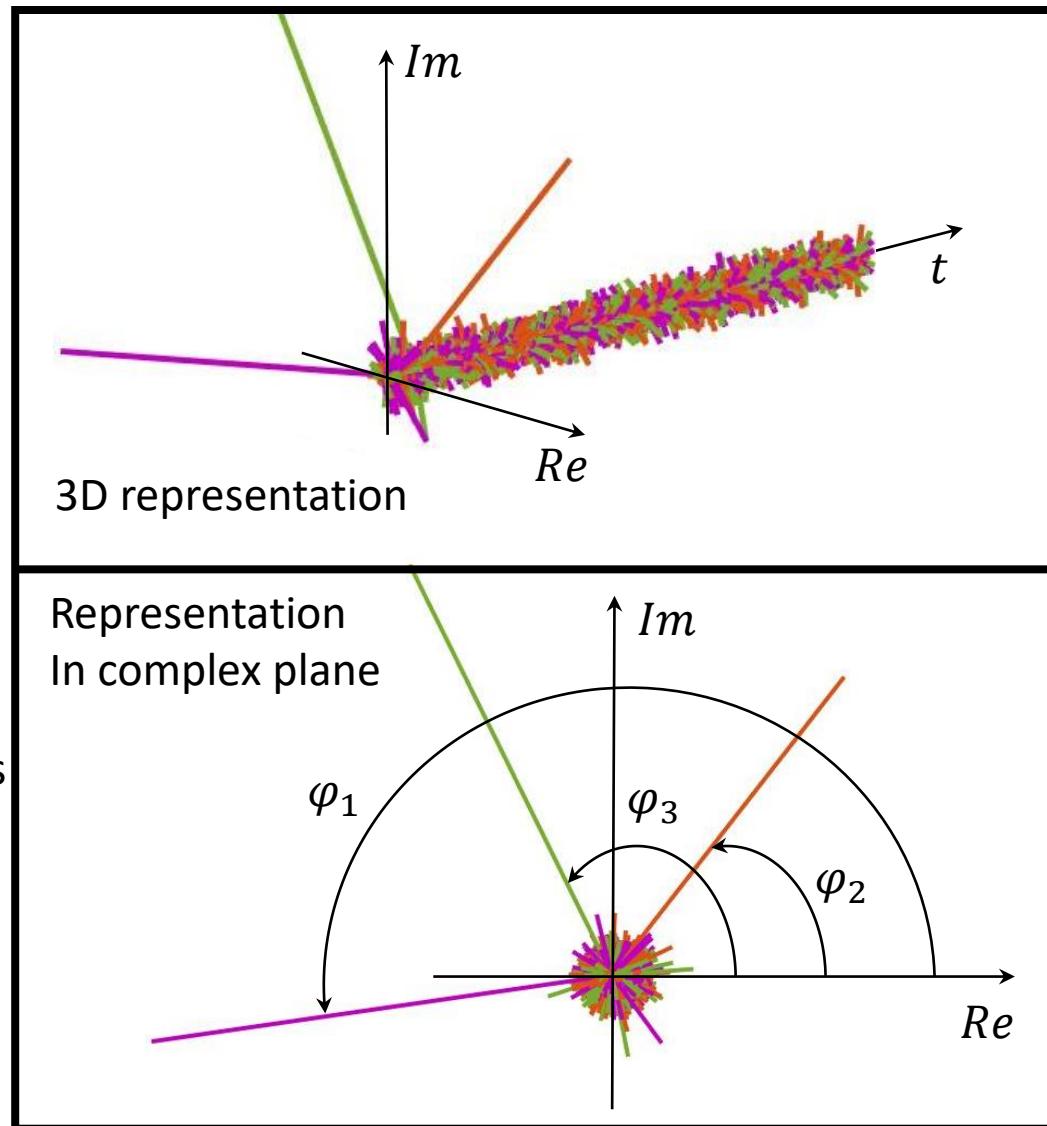
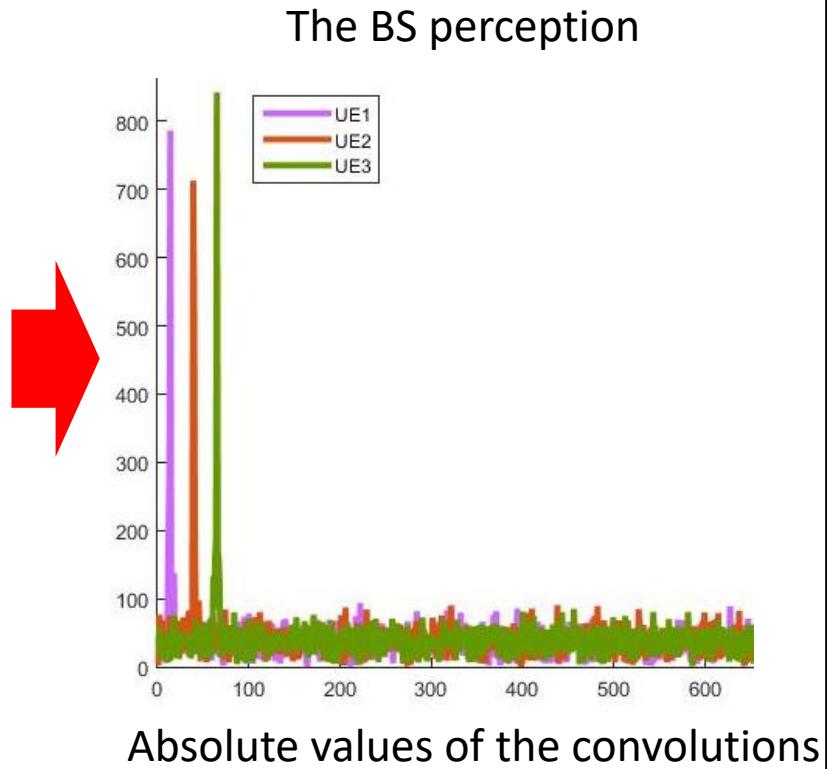
Absolute values of the convolutions

$$s_1 * s_{BS} = s_1 * s_1 + 0 + 0 + r_1$$

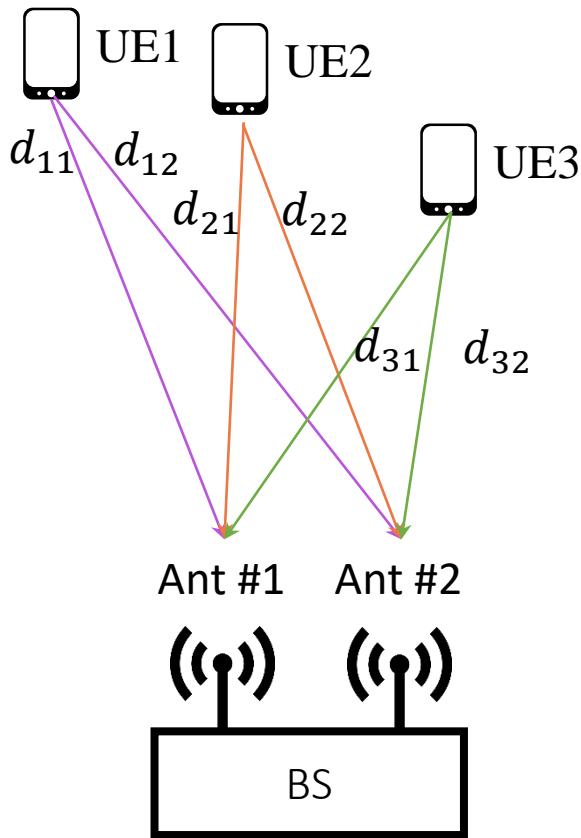
$$s_2 * s_{BS} = 0 + s_2 * s_2 + 0 + r_2$$

$$s_3 * s_{BS} = 0 + 0 + s_3 * s_3 + r_3$$

# Convolution in the complex plane

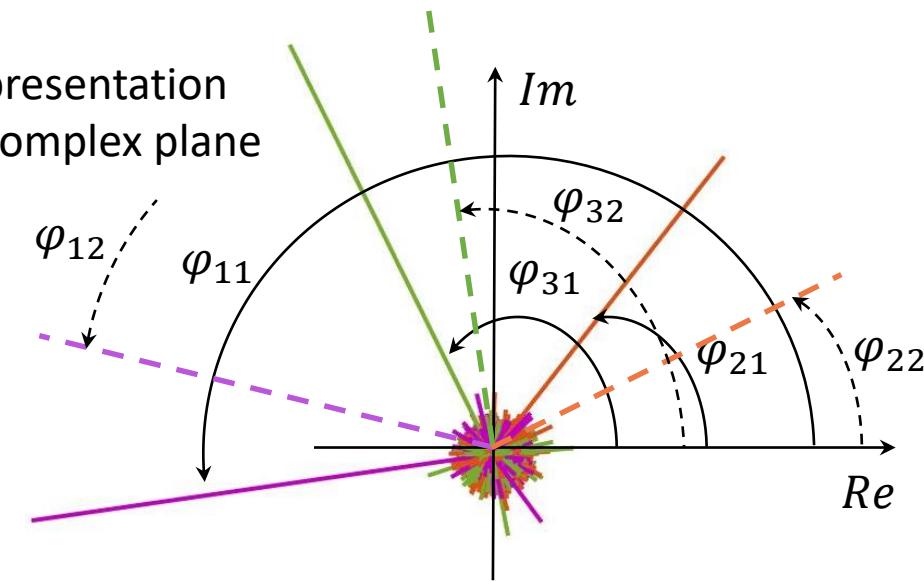


# Convolutions' spike for neighboring antennas



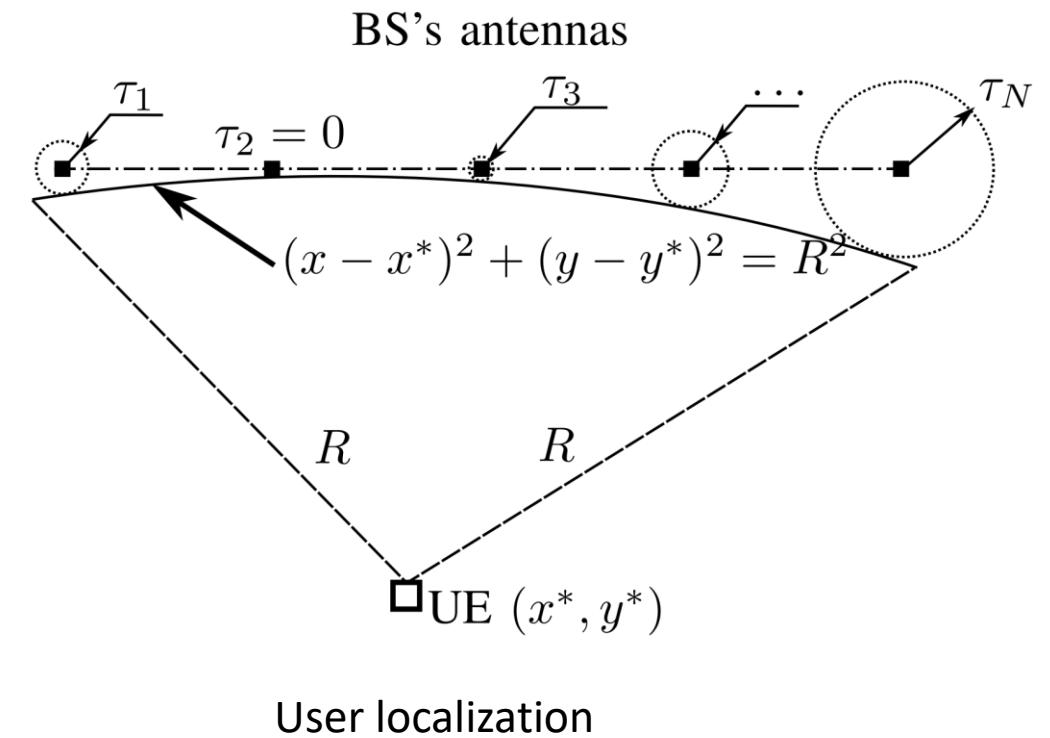
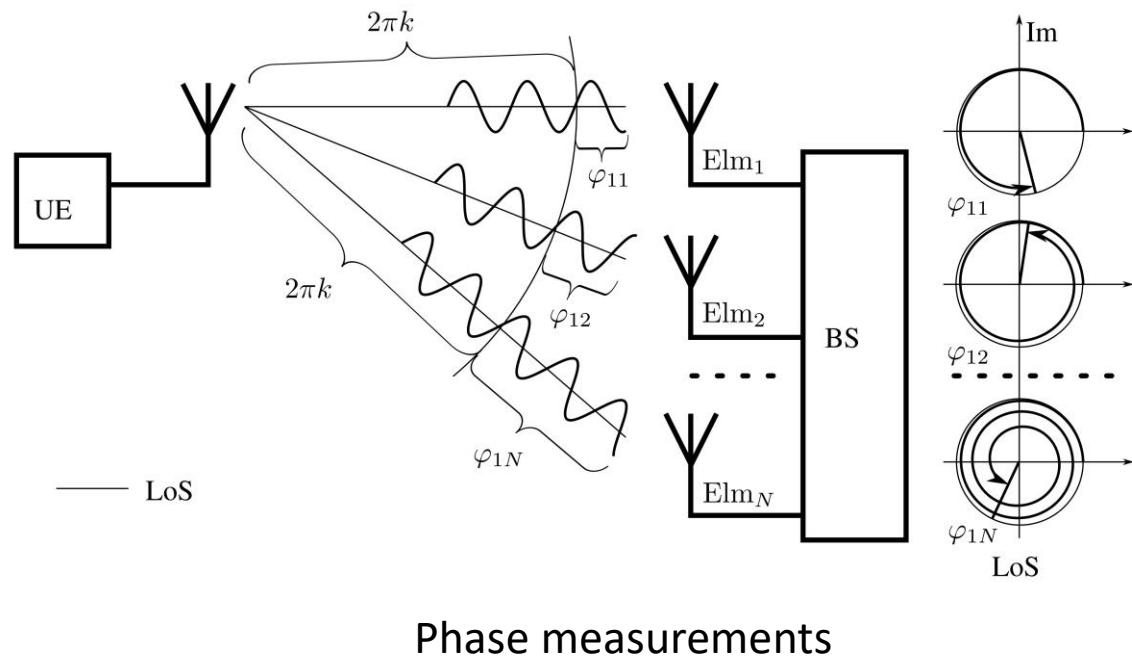
The distance between antennas less  
than the half of wavelength  $\lambda/2$

Representation  
In complex plane

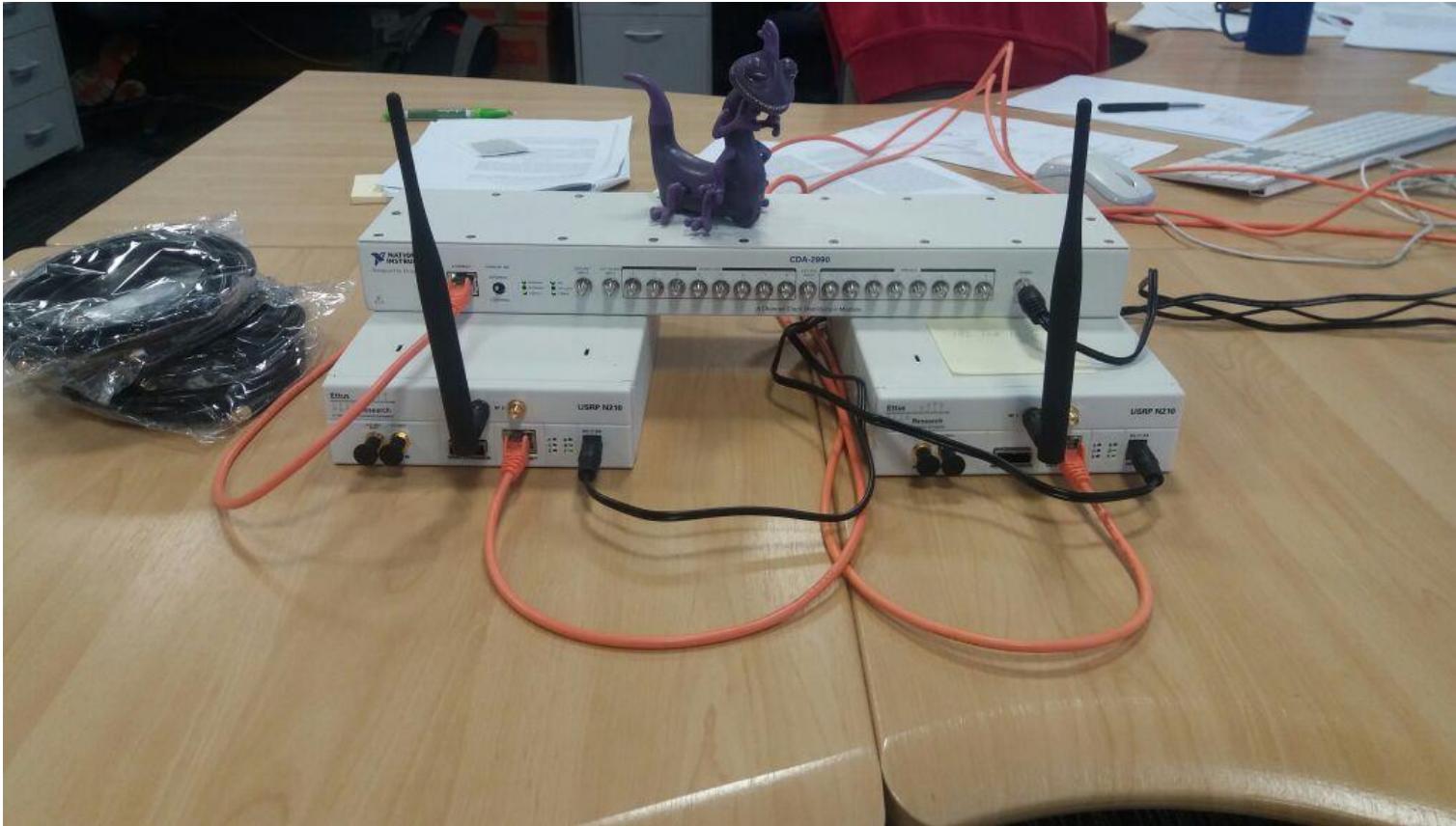


$$\varphi_{ij} = f(\omega, d_{ij})$$

# Implementation of the idea



# 10 kNZD experiment hardware



Two USRPs N210, one Octoclock, two antennas and 2 SMA cables

Having only one antenna,  
how to increase the number of antenna  
elements in the receiving side?

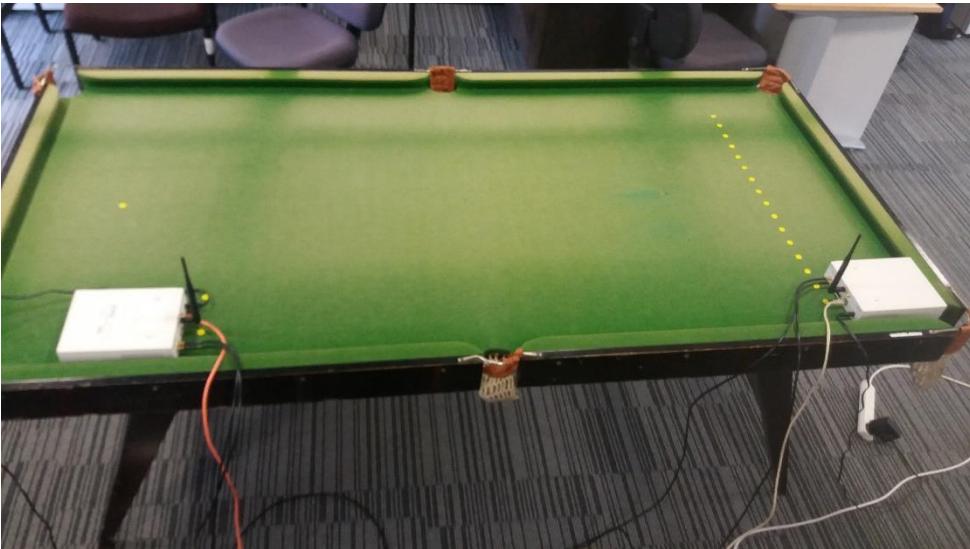
Having only one antenna,  
how to increase the number of antenna  
elements in the receiving side?

**Realize timing is the key (BMW)**

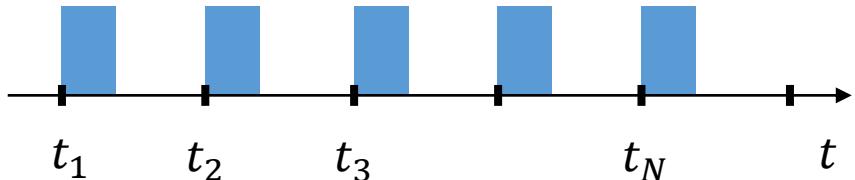


**Realize timing is the key (BMW)**

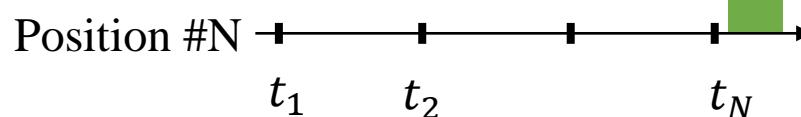
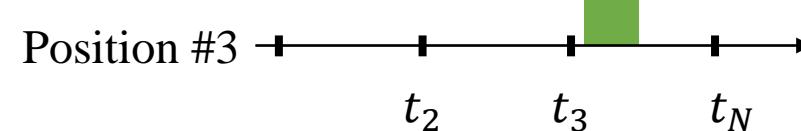
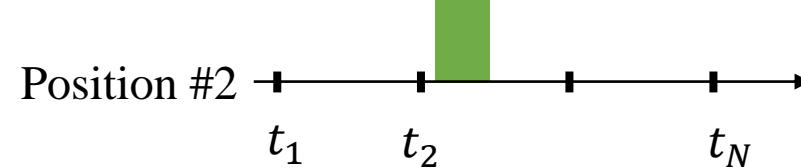
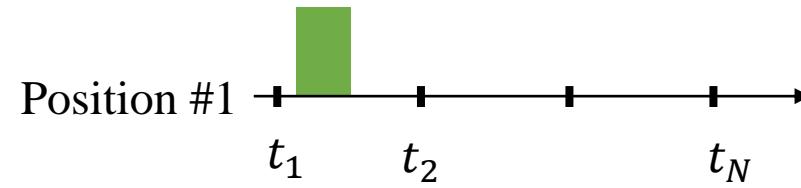
# Time alignment



Transmitter is periodically sending a signal

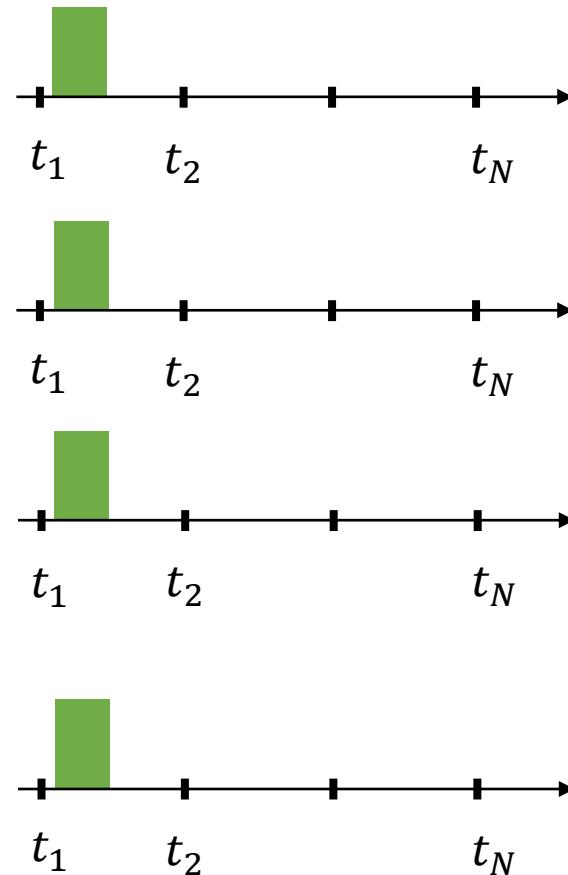
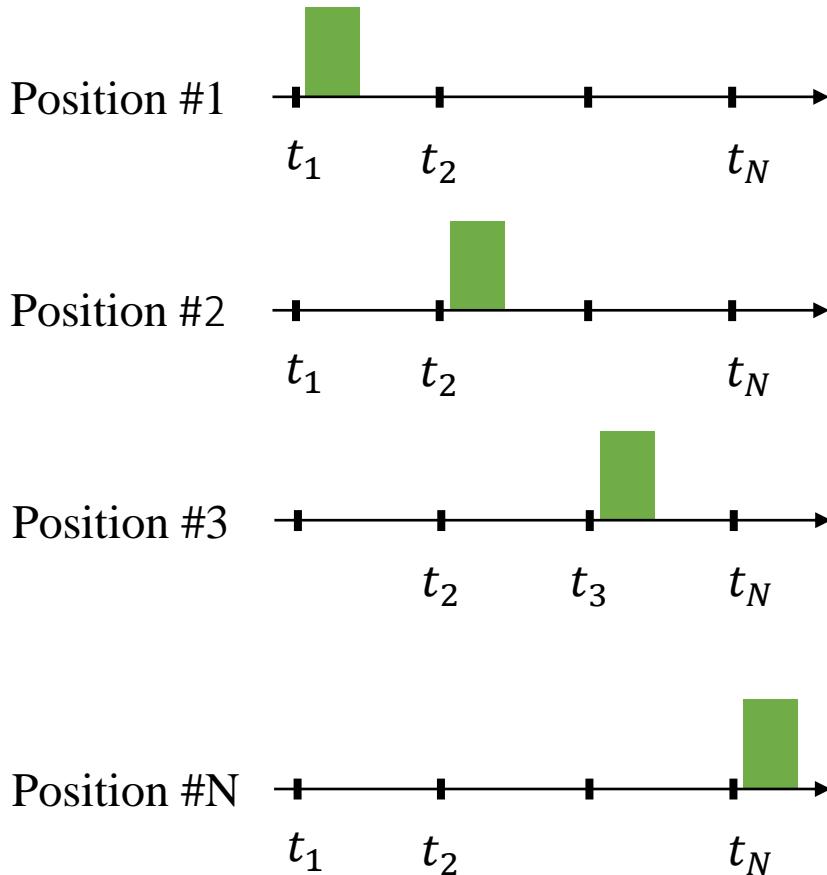


Receiver is recording at exact time



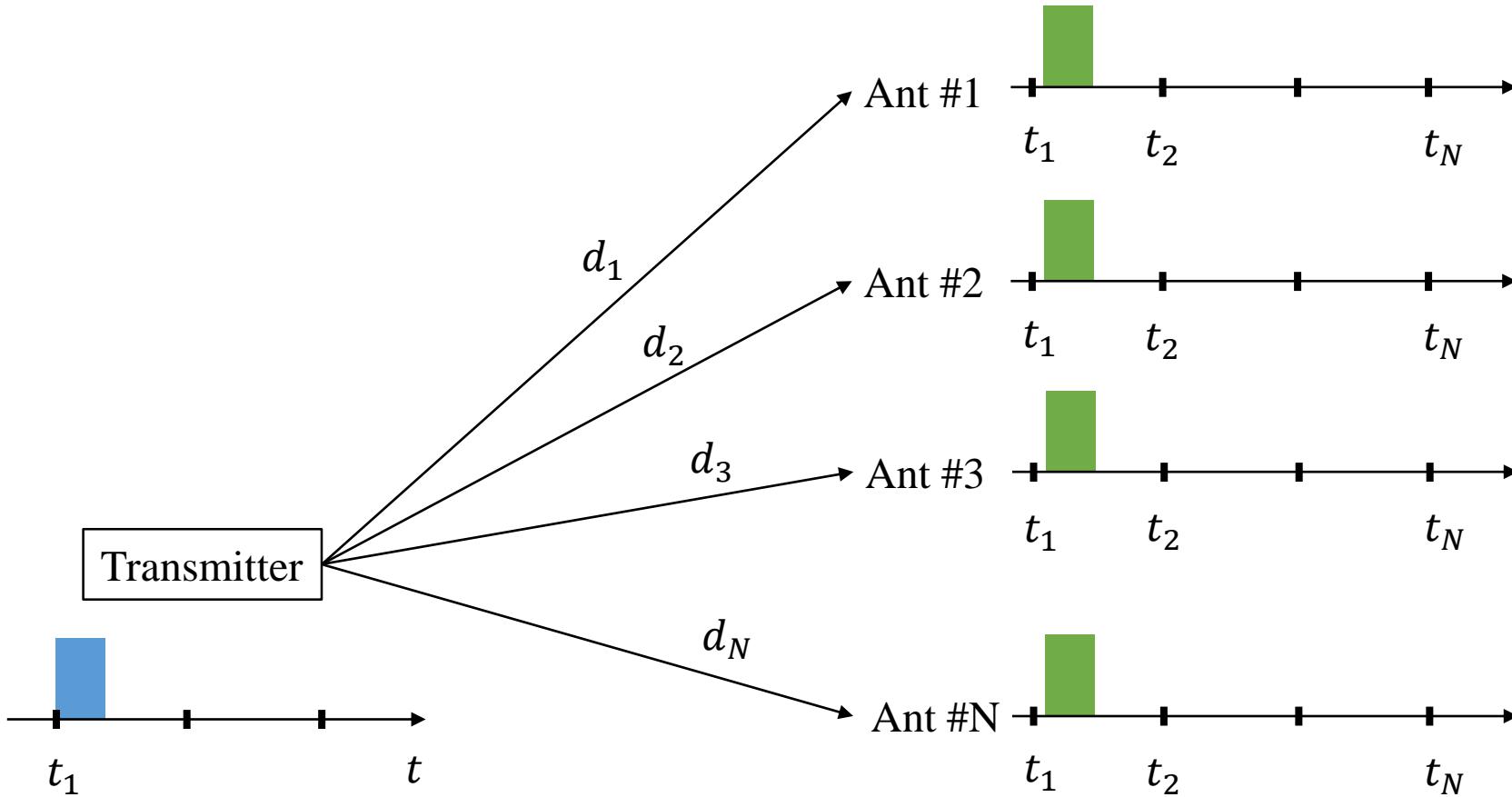
# Time alignment

The precise knowledge of time allows us to align the received signals to the start point

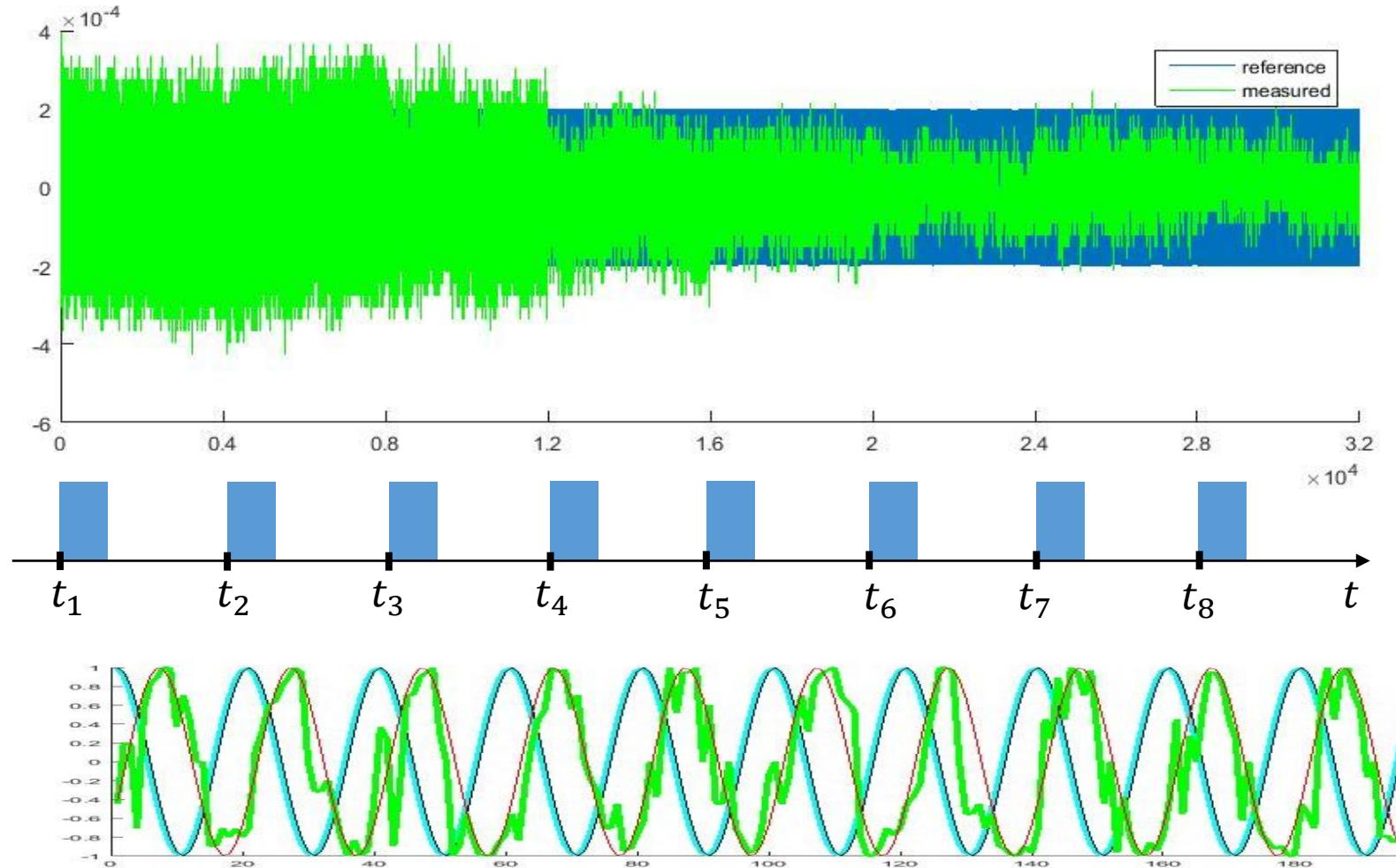


# Time alignment

The precise knowledge of time allows us to align the received signals to the start point



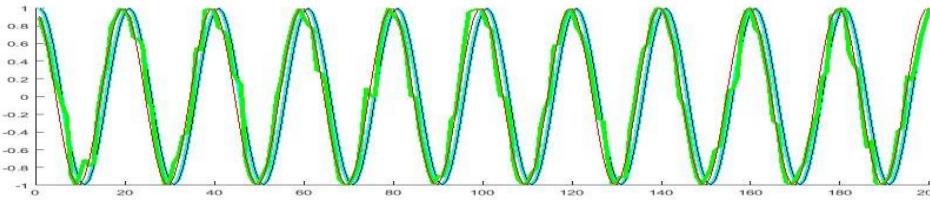
# Real experiments using 1 antenna



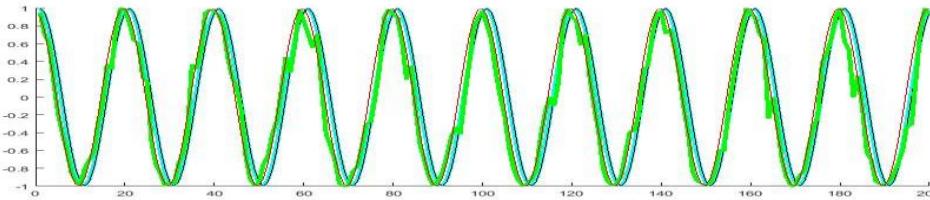
Digital cosine function, which is sent at the exact moments

# Real experiments using 1 antenna

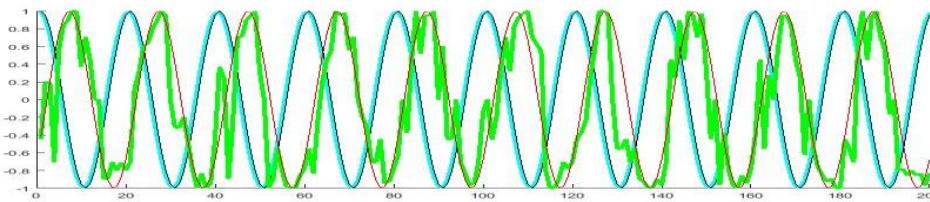
Ant #1



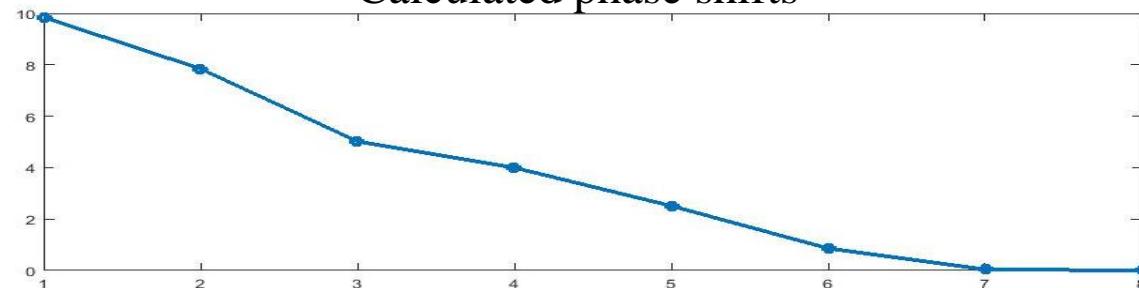
Ant #2



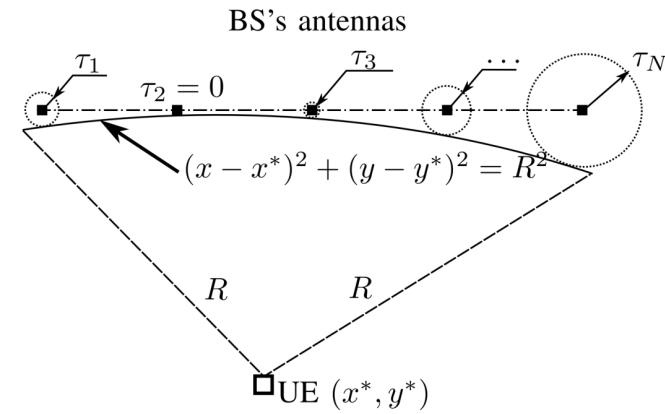
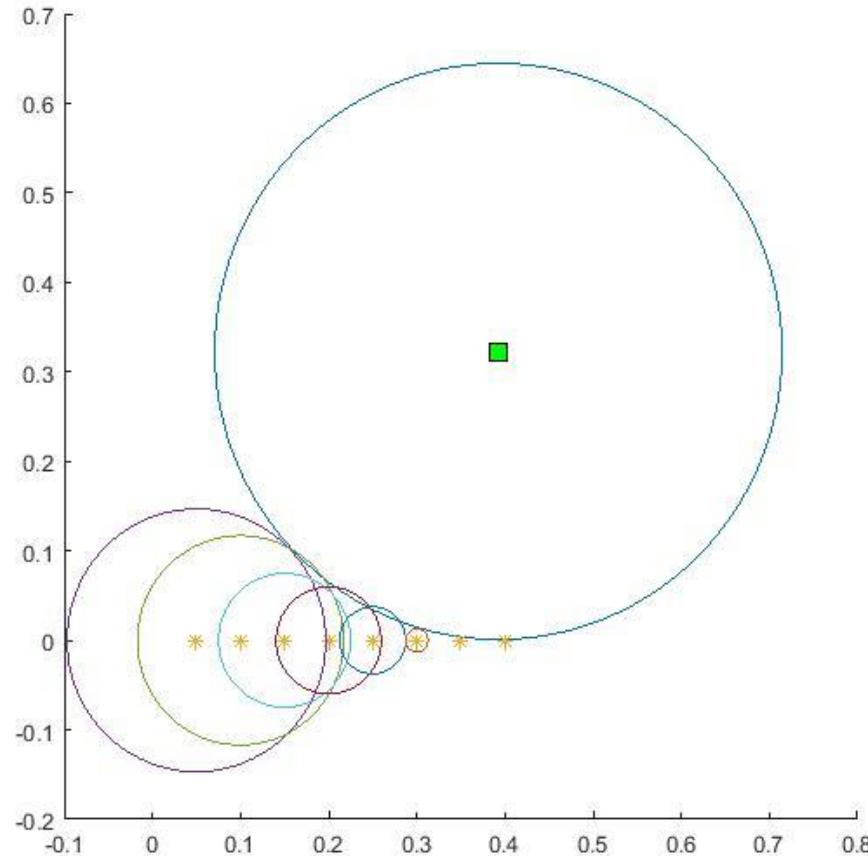
Ant #3



Calculated phase shifts



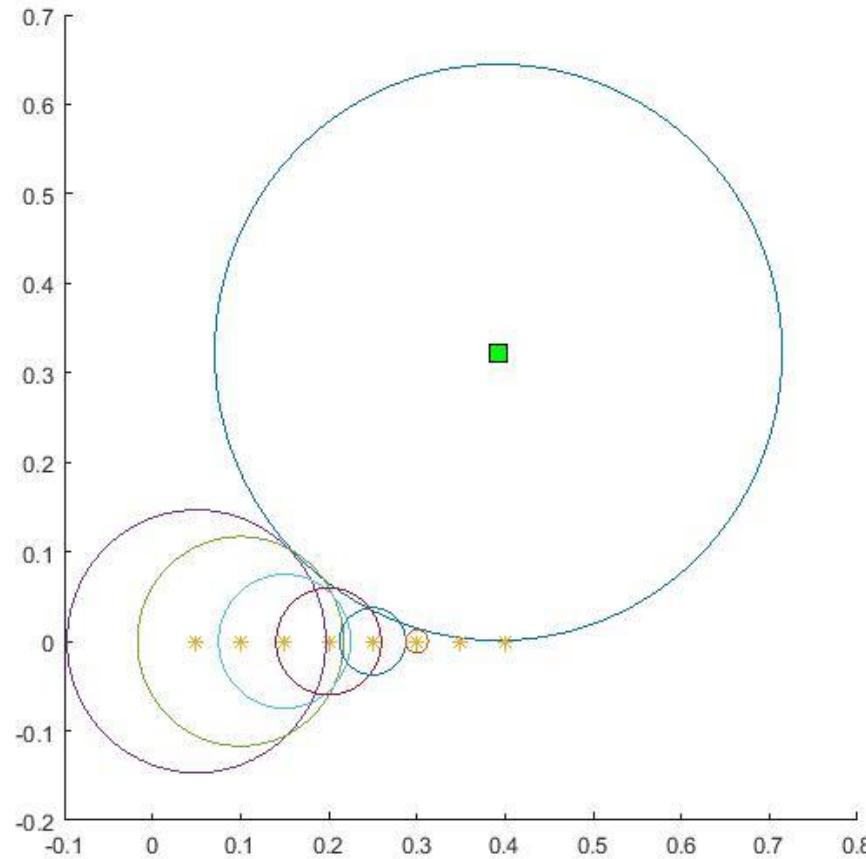
# Localization in a real environments



The same algorithm as for simulation.

For single user mode,  
the accuracy around 7 cm  
without calibration and  
implementing advanced  
signal processing algorithms.

# Localization in a real environments



Thank you