

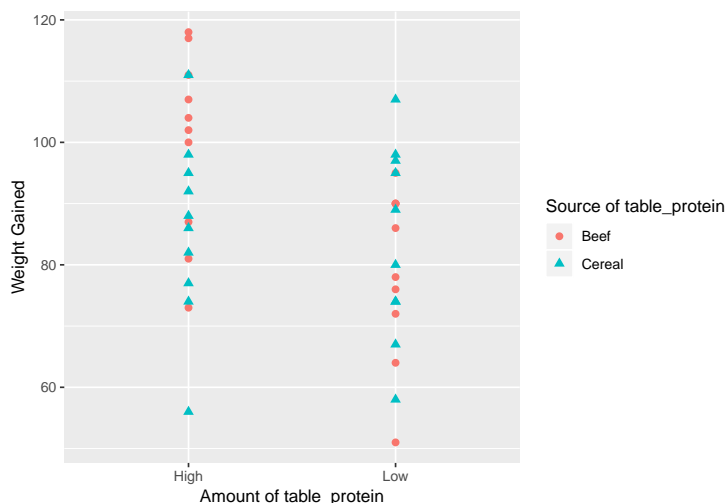
Lab 5 Two factor Factorial 1

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An experiment was designed to study weight gain of rats fed four different diets, where there were two levels of protein (high or low) and two sources of protein (beef or cereal). This gives 2 x 2 treatment combinations: high/beef (HB), high/cereal (HC), low/beef (LB), low/cereal (LC). Ten rats were in each of the four treatment groups. Use $\alpha=0.01$

- (a) Plot the data and report the plot here (A plot with data and means of treatment combinations). Do not report code here. Describe the observed relationship between two factors.

```
## Observations: 40
## Variables: 5
## $ Source <chr> "Beef", "Beef", "Beef", "Beef", "Beef", "Beef", "Beef", ...
## $ Amount <chr> "Low", "Low", "Low", "Low", "Low", "Low", "Low", "Low", ...
## $ Gain <dbl> 90, 76, 90, 64, 86, 51, 72, 90, 95, 78, 73, 102, 118, 1...
## $ Trt1 <fct> Beef, Beef, Beef, Beef, Beef, Beef, Beef, Beef, Beef, B...
## $ Trt2 <fct> Low, Low, Low, Low, Low, Low, Low, Low, Low, Low, High, ...
```



- (b) Obtain the numerical summary for each treatment combination and factor levels separately. Report them here in a tabular form.

```
## Source min Q1 median Q3 max mean sd n missing
## 1 Beef 51 77.5 90 102.5 118 89.6 17.71232 20 0
## 2 Cereal 56 74.0 87 95.5 111 84.9 14.99438 20 0

## Amount min Q1 median Q3 max mean sd n missing
## 1 High 56 81.75 93.5 104.75 118 92.95 16.36259 20 0
## 2 Low 51 73.50 83.0 91.25 107 81.55 14.63045 20 0

## Amount min Q1 median Q3 max mean sd n missing
## 1 Beef.High 73 90.25 103.0 110.00 118 100.00 15.13642 10 0
## 2 Cereal.High 56 78.25 87.0 94.25 111 85.90 15.02184 10 0
## 3 Beef.Low 51 73.00 82.0 90.00 95 79.20 13.88684 10 0
## 4 Cereal.Low 58 74.00 84.5 96.50 107 83.90 15.70881 10 0
## 5 High 56 81.75 93.5 104.75 118 92.95 16.36259 20 0
## 6 Low 51 73.50 83.0 91.25 107 81.55 14.63045 20 0
```

- (c) Fit the two-factor factorial model and report the complete ANOVA table here. Do not report code here. The complete ANOVA table should have a row for each of the following: main effects of each treatment, two-factor interaction effects, error and total.

```
##           Df Sum Sq Mean Sq F value Pr(>F)
## Trt1       1    221   220.9    0.988 0.3269
## Trt2       1   1300  1299.6    5.812 0.0211 *
## Trt1:Trt2   1    884   883.6    3.952 0.0545 .
## Residuals  36   8049   223.6
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

- (d) Based on the ANOVA table write your conclusion appropriately. Perform all the necessary tests and report the conclusion along with the p-value.

```
pairwise.t.test(table_protein$Gain, table_protein$Trt2, p.adj = "none")
```

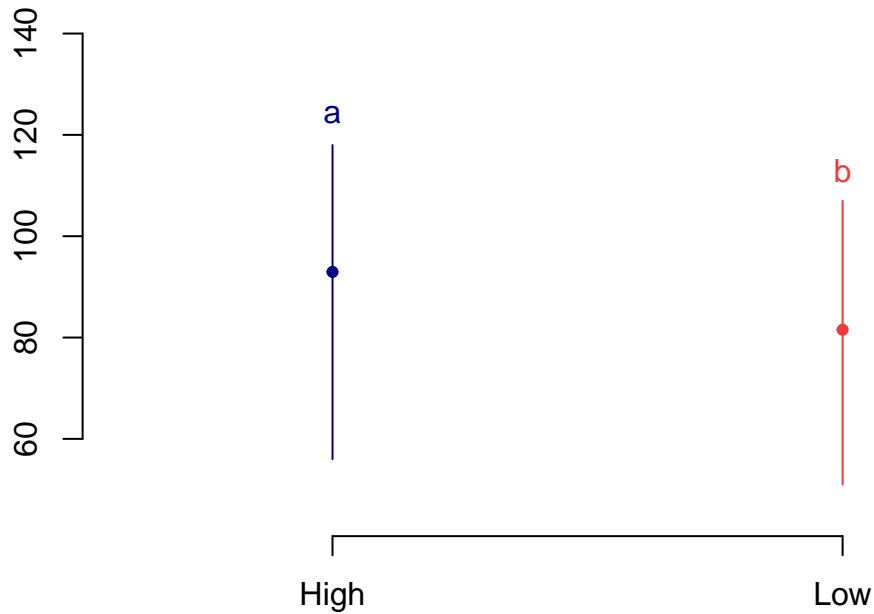
```
##
## Pairwise comparisons using t tests with pooled SD
##
## data:  table_protein$Gain and table_protein$Trt2
##
##      High
## Low 0.026
##
## P value adjustment method: none
```

```
pairwise.t.test(table_protein$Gain, table_protein$Trt2, p.adj = "bonf")
```

```
##
## Pairwise comparisons using t tests with pooled SD
##
## data:  table_protein$Gain and table_protein$Trt2
##
##      High
## Low 0.026
##
## P value adjustment method: bonferroni
```

```
plot(LSD.test(model_protein, trt = "Trt2", alpha = 0.05))
```

Groups and Range



```
(LSD.test(model_protein, trt = "Trt2", alpha = 0.05))
```

```
## $statistics
##      MSerror Df  Mean      CV t.value  LSD
##  223.5944 36 87.25 17.13819 2.028094 9.59
##
## $parameters
##      test p.adjusted name.t ntr alpha
## Fisher-LSD      none   Trt2   2  0.05
##
## $means
##      Gain      std  r      LCL      UCL Min Max  Q25  Q50  Q75
## High 92.95 16.36259 20 86.16885 99.73115  56 118 81.75 93.5 104.75
## Low  81.55 14.63045 20 74.76885 88.33115  51 107 73.50 83.0  91.25
##
## $comparison
## NULL
##
## $groups
##      Gain groups
## High 92.95      a
## Low  81.55      b
##
## attr("class")
## [1] "group"
```

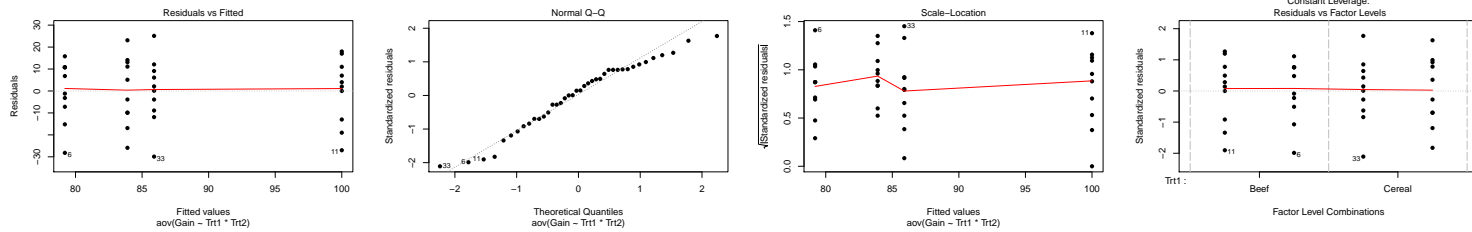
```
TukeyHSD(model_protein, conf.level = 0.95)
```

```
## Tukey multiple comparisons of means
## 95% family-wise confidence level
##
## Fit: aov(formula = Gain ~ Trt1 * Trt2, data = table_protein)
##
## $Trt1
##          diff      lwr      upr      p adj
## Cereal-Beef -4.7 -14.29  4.89 0.3268783
##
## $Trt2
##          diff      lwr      upr      p adj
## Low-High -11.4 -20.99 -1.81 0.0211449
##
## $'Trt1:Trt2'
##          diff      lwr      upr      p adj
## Cereal:High-Beef:High -14.1 -32.1102  3.910198 0.1697711
## Beef:Low-Beef:High -20.8 -38.8102 -2.789802 0.0182745
## Cereal:Low-Beef:High -16.1 -34.1102  1.910198 0.0936982
## Beef:Low-Cereal:High  -6.7 -24.7102 11.310198 0.7492577
## Cereal:Low-Cereal:High  -2.0 -20.0102 16.010198 0.9905411
## Cereal:Low-Beef:Low    4.7 -13.3102 22.710198 0.8952934
```

```
ScheffeTest(model_protein, conf.level = 0.95)
```

```
##
## Posthoc multiple comparisons of means : Scheffe Test
## 95% family-wise confidence level
##
## $Trt1
##          diff      lwr.ci      upr.ci      pval
## Cereal-Beef -4.7 -18.56594  9.165941 0.8042
##
## $Trt2
##          diff      lwr.ci      upr.ci      pval
## Low-High -11.4 -25.26594  2.465941 0.1410
##
## $'Trt1:Trt2'
##          diff      lwr.ci      upr.ci      pval
## Cereal:High-Beef:High -14.1 -33.7094  5.509402 0.2358
## Beef:Low-Beef:High -20.8 -40.4094 -1.190598 0.0338 *
## Cereal:Low-Beef:High -16.1 -35.7094  3.509402 0.1418
## Beef:Low-Cereal:High  -6.7 -26.3094 12.909402 0.8004
## Cereal:Low-Cereal:High  -2.0 -21.6094 17.609402 0.9929
## Cereal:Low-Beef:Low    4.7 -14.9094 24.309402 0.9195
##
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

(e) Provide the plots of residuals here. Do not report code here.



(f) Based on the residual plots, clearly explain whether assumptions in the model are satisfied or violated.

(g) Report the code here without output.

```
table_protein <- read_excel("Protein.xlsx")
glimpse(table_protein)

# Install and load ggplot2 package before using ggplot function #
ggplot(data = table_protein, aes(x = Amount, y = Gain, colour = Source, group = Source)) +
  geom_point(aes(shape = Source, color = Source), size = 2) + labs(y = "Weight Gained",
    x = "Amount of table_protein", color = "Source of table_protein", shape = "Source of table_protein")

# Plots the Mean and 1SD error bars for each treatment group #
ggplot(data = table_protein, aes(x = Amount, y = Gain, colour = Source, shape = Source,
  group = Source)) + stat_summary() + labs(y = "Weight Gained", x = "Amount of table_protein",
  color = "Source", shape = "Source")

# Install and load ggpubr package before using ggline function #
ggline(data = table_protein, x = "Amount", y = "Gain", add = c("mean", "jitter"),
  shape = "Source", color = "Source", linetype = "Source", ylab = "Weight Gained",
  xlab = "Amount of table_protein")

# Load mosaic package before using faustats function#
faustats(Gain ~ Source, data = table_protein)
faustats(Gain ~ Amount, data = table_protein)
faustats(Gain ~ Source | Amount, data = table_protein)
# faustats(Gain ~ Source+Amount, data=table_protein)

# Create Categorical variables so that plot of residuals versus each
# treatment combination can be obtained using plot function with the fitted
# model later #
table_protein$Trt1 = as.factor(table_protein$Source)
table_protein$Trt2 = as.factor(table_protein$Amount)

model_protein <- aov(Gain ~ Trt1 * Trt2, data = table_protein)
summary(model_protein)
plot(model_protein, pch = 16)

# Pairwise comparisons using t tests with pooled Standard Deviation # The
# output gives a matrix of p values for each pair of treatments #
pairwise.t.test(table_protein$Gain, table_protein$Trt2, p.adj = "none")

# Pairwise comparisons using t tests with pooled Standard Deviation and
# Bonferroni adjustment # The output gives a matrix of p values for each
# pair of treatments #
```

```
pairwise.t.test(table_protein$Gain, table_protein$Trt2, p.adj = "bonf")

# Install and load the agricolae package before running the LSD.test
# function below # p.adj option in the LSD.test function can be used to
# apply different adjustments to control error rates#
plot(LSD.test(model_protein, trt = "Trt2", alpha = 0.05))
# The treatments sharing the same letter on the plot are not different#

(LSD.test(model_protein, trt = "Trt2", alpha = 0.05)) # Using outer parentheses prints the output#

# Tukey's test to get observed difference in means, CI and p value#
TukeyHSD(model_protein, conf.level = 0.95)

# Scheffe's test to get observed difference in means, CI and p value #
# Install and load the DescTools package before using the ScheffeTest
# function #
ScheffeTest(model_protein, conf.level = 0.95)
```