$U \sim Geom(p=\frac{1}{2}), u=1,2...$ the number of trials needed to get the first head.

 $V \sim NBin(p=\frac{1}{2},r=2), v=2,3..$ the number of trials needed to get two heads in repeated tosses of a fair coin.

the distribution of (U,V) is $\{(u,v): u = 1, 2, ...; v = u + 1, u + 2, ...\}$ is not a cross-product set. U and V are not independent.

Conditional expectations and variances

$$f(x_{2}|x_{1}) = \frac{f(x_{1},x_{2})}{f_{1}(x_{1})}; p(x_{2}|x_{1}) = \frac{p(x_{1},x_{2})}{p_{1}(x_{1})}$$

$$4.2.1 \ f(y|x) = P(Y = y|X = x) = \frac{f(x,y)}{f_{X}(x)}$$

$$4.2.3 \ E(g(x_{2})|x_{1}) = \sum_{all \ x_{2}} g(x_{2})p(x_{2}|x_{1}), E(g(x_{2})|x_{1}) = \int_{all \ x_{2}} g(x_{2})f(x_{2}|x_{1}) dx_{2}$$

$$4.2.4 \ Var(y|x) = E(Y^{2}|x) - (E(Y|x))^{2},$$

$$V[X|Y] = E[(X - E[X|Y])^{2}|Y]$$

$$4.2.7 \ f(x,y) = g(x)h(y) \iff \text{indep}$$

$$4.2.10 \ E(g(X)h(Y)) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} g(x)h(y)f(x,y)dxdy = \int_{-\infty}^{\infty} h(y)f_{Y}(y) \left[\int_{-\infty}^{\infty} g(x)f_{X}(x)dx\right] dy = E[g(x)]E[h(y)] = (Eg(X))(Eh(Y))$$

$$F_{XY}(x,y) = P(X \le x, Y \le y)$$

Covariance and Correlation

Transformation of pairs of r.v.s

$$\begin{split} f_{Y_1,Y_2}(y_1,y_2) &= \sum_{i=1}^k f_{X_1,X_2}(h_1(y_1,y_2),h_2(y_1,y_2))|J_i| \\ J_{1,2} &= \begin{vmatrix} \frac{\partial h_1}{\partial y_1} & \frac{\partial h_2}{\partial y_2} \\ \frac{\partial h_1}{\partial y_1} & \frac{\partial h_2}{\partial y_2} \end{vmatrix} = \frac{\partial h_1}{\partial y_1} \frac{\partial h_2}{\partial y_2} - \frac{\partial h_2}{\partial y_1} \frac{\partial h_1}{\partial y_2} \end{split}$$

Properties of \bar{X} and S^2

$$\begin{split} \bar{X}_{n+1} &= \frac{\sum_{i=1}^{n+1} X_i}{n+1} = \frac{\sum_{i=1}^{n} X_i + X_{n+1}}{n+1} = \frac{n\bar{X}_n + X_{n+1}}{n+1} \\ nS_{n+1}^2 &= (n-1)S_n^2 + (\frac{n}{n+1})(X_{n+1} - \bar{X}_n)^2 \\ \text{when } X_1, ..., X_n \text{ be iid } n(\mu, \sigma^2), \\ \frac{(n-1)S^2}{\sigma^2} &\sim \chi_{n-1}^2, Var\chi_{n-1}^2 = 2(n-1) \\ Var[\frac{(n-1)S^2}{\sigma^2}] &= \frac{(n-1)^2}{\sigma^4} Var[S^2] = 2(n-1) \implies Var[S^2] = \frac{2\sigma^4}{n-1} \end{split}$$

Connection between N, χ^2, t, F

W Normal	$\bar{X} \sim N(\mu, \frac{\sigma^2}{n})$	\bar{X}, S^2 indep	$\frac{(n-1)S^2}{\sigma^2} \sim \chi_{n-1}^2$
W/o Normal	$E[\bar{X}] = \mu$	$V[\bar{X}] = \frac{\sigma^2}{n}$	$E[S^2] = \sigma^2$

5.2.8 Distribution of the mean: $\bar{X} \sim gamma(n\alpha, \beta/n)$ 5.2.9 Convolution formula Z = X + Y $f_Z(z) = \int_{-\infty}^{\infty} f_X(w) f_Y(z-w) dw$

 $5.3.2 \ Z \sim n(0,1), Z^2 \sim \chi_1^2, \ X_1...X_n \ \text{indep}$ $X_i \sim \chi_{p_i}^2, X_1 = \dots = X_n \sim \chi_{p_1 + \dots p_n}^2$

 $\chi_p^2 \sim gamma(p/2,2)$

5.3.4 T

5.3.5 $X_1..X_n,Y_1..Y_m$ indep.

 $X_i \sim n(\mu_X, \sigma_X^2) Y_j \sim n(\mu_Y, \sigma_Y^2), \frac{S_X^2}{\sigma^2} \sim \chi^2 \text{F: } \frac{S_X^2/\sigma_X^2}{S^2/\sigma^2}$

Order statistics

$$\begin{array}{ll} 5.4.6 \; f_{X(i)}, \chi_{(j)}(u,v) = \\ \frac{n!}{(i-1)!(j-1-i)!(n-j)!} f_X(u) f_X(v) [F_X(u)]^{i-1} [F_X(v) - F_X(u)]^{j-1-i} [1 - F_X(v)]^{n-j} \\ f_{X_{(1)}, \dots, X_{(n)}}(x_1, \dots, x_n) = \\ \begin{cases} n! f_X(x_1) \cdot \dots \cdot f_X(x_n) & -\infty < x_1 < \dots < x_n < \infty \\ 0 & \text{otherwise} \end{cases}$$

Conditional/Baye's: $P(A|B) = \frac{P(A \cap B)}{P(B)} = \frac{P(B|A)P(A)}{P(B)}$;disjoint

 $P(B) = P(B|A_1)P(A_1) + ...P(B|A_k)P(A_k) = \sum_{i=1}^{k} P(B|A_i)P(A_i)$ 3 $1 \left| \frac{de^{-Y/2}}{du} \right| = \frac{1}{2}e^{-Y/2}, 0 < y < \infty$ Independence:

 $P(A \cap B) = P(A)P(B) \quad | \quad P(X \le x, Y \le y) = P(X \le x)P(Y \le y) \quad 4 \quad 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 | \frac{d\sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 |$ $F_{X,Y}(x,y) = F_X(x)F_Y(y)$ E(XY) = E(X)E(Y) $V(X \pm Y) = VX + VY$ $f_{X,Y}(s,t) = f_X(s)f_Y(t)$

pdf/pmf

CDF:
$$F(x) = P(X \le x) = \sum_{y:y \le x} p(y) = \int_{-\infty}^{x} f(y) dy$$
 probabilities: $a \le b$:

PMF: $p(x) = P(X = x) = P(\forall w \in \mathcal{W} : X(w) = x)$
 $P(a \le X \le b) = F(b) - F(a^-)$; $P(a < X \le b) = F(b) - F(a)$; $P(a \le X \le a) = p(a)$; $P(a < X < b) = F(b^-) - F(a)$; (where a^- is the largest possible X value strictly less than a); Taking $a = b$ yields $P(X = a) = F(a) - F(a - 1)$ as desired.

PDF: $P(\forall w \in \mathcal{W} : a \le X(w) \le b) = \int_a^b f(x) dx$
 $P(a \le X \le b) = P(a < X \le b) = P(a < X < b)$;

P(X > a) = 1 - F(a); P(a < X < b) = F(b) - F(a)

CDF

Condition:
$$f(x) \ge 0 \forall x \text{ pmf } \sum_{x} f_X(x) = 1, pdf \int_{-\infty}^{\infty} f(x) dx = 1$$

$$c \sin x \ge 0, 0 < x < \pi/2 \qquad \int_{0}^{\frac{\pi}{2}} c \sin x dx = 1 \qquad c = 1$$

$$ce^{-|x|} \ge 0, -\infty < x < \infty \qquad c \int_{-\infty}^{\infty} e^x dx + c \int_{0}^{\infty} e^{-x} dx = 1 \qquad c = \frac{1}{2}$$

mean/variance

$$\begin{split} E[g(x)] &= \mu = \sum_{x \in D} h(x) p(x) = \int_{-\infty}^{\infty} g(x) f(x) dx \\ E[(X - \mu)^n] &= \mu_n = \sum (x - \mu)^n p(x) = \int (x - \mu)^n f(x) dx \\ E(aX + b) &= aE(X) + b & E(X) = \int_{-\infty}^{0} F_X(t) dt + \int_{0}^{\infty} F_X(t) dt \\ V(aX + b) &= a^2 \sigma^2 & V(X \pm Y) = VX + VY \pm 2Cov(X, Y) \\ \sigma_{ax + b} &= |a| \cdot \sigma_x & Cov(x, y) = E(XY) - E(X)E(Y) \\ V(X) &= \sigma_x^2 = E(X^2) - [E(X)]^2 & E(X^2) - E(X^2) \end{split}$$

$f_X(x)$	EX	EX^2	V(X)
$\frac{1}{n}$	$\sum_{1}^{n} x \frac{1}{n}$	$\sum_{1}^{n} x^{2} \frac{1}{n}$	
16	$\frac{1}{n}\frac{n(n+1)}{2}$	$\frac{1}{n} \frac{n(n+1)(2n+1)}{6}$	$\frac{n^2-1}{12}$
ax^{a-1}	$\int_0^1 x a x^{a-1} dx$	$\int_0^1 x^2 a x^{a-1} dx$	$\frac{\frac{a}{a+2} - \left(\frac{a}{a+1}\right)}{a+2}$
	$\frac{a}{a+1}x^{a+1} _0^1$	$\frac{a}{a+2}x^{a+2} _0^1$	$\frac{a}{(a+2)(a+1)^2}$
$\frac{3}{2}(x-1)^2$	$\int_0^2 x \frac{3}{2} (x-1)^2 dx$	$\int_0^2 x^2 \frac{3}{2} (x-1)^2 dx$	$\frac{8}{5} - 1^2$
	$\frac{3}{2}(\frac{x^4}{4} _0^2)$	$\frac{3}{2}(\frac{x^5}{5} _0^2)$	3 5

transform

$$\begin{array}{l} g(x) \uparrow & F_{Y}(y) = F_{X}(g^{-1}(y)) \\ g(x) \downarrow & F_{Y}(y) = 1 - F_{X}(g^{-1}(y)) \\ \text{not monotone} : X \leq 0 \text{ is } \emptyset : P(X \leq -\sqrt{y}) = 0 \\ F_{Y}(y) = P(Y \leq y) = P(X^{2} \leq y) = P(-\sqrt{y} \leq X \leq \sqrt{y}) = P(X \leq \sqrt{y}) - P(X \leq -\sqrt{y}) = F_{X}(\sqrt{y}) = \sqrt{y}, \ 0 < \sqrt{y} < 1 \\ Y & X & f_{X}(x) & F_{Y}(y) & f_{Y}(y) = \frac{dF_{Y}(y)}{dy} \\ X^{2} & \sqrt{Y} & \frac{e^{-x^{2}/2}}{\sqrt{2\pi}} & F_{X}(\sqrt{y}) - F_{X}(-\sqrt{y}) & \frac{e^{-y/2}}{2\sqrt{2\pi y}}, y > 0 \end{array}$$

monotone:
$$f_Y(y) = f_X(g^{-1}(y)) |\frac{d(g^{-1}(y))}{dy}|$$

$$\begin{vmatrix} Y & X & ay \\ 1 & -\log X & e^{-Y} & x^n(1-x)^m, 0 < x < 1 \\ 2 & e^X & \ln Y & \frac{1}{\sigma^2}xe^{-(x/\sigma)^2/2}, 0 < x < \infty \\ 3 & -2lnX & e^{-Y/2} & 1, 0 < x < 1 \\ 4 & X^2 & \sqrt{Y} & 1, 0 < x < 1 \\ 5 & d\tan X & \arctan \frac{Y}{d} & \frac{1}{b-a} = \frac{2}{\pi} \\ 1 & (e^{-y})^n(1-e^{-y})^m|\frac{d(e^{-y})}{dy}| = e^{-(n+1)y}(1-e^{-y})^m, \ 0 < y < \infty$$

$$2 \frac{1}{\sigma^2} \ln y e^{-(\ln y/\sigma)^2/2} \left| \frac{d(\ln y)}{dy} \right| = \frac{\ln(y)}{\sigma^2 y} e^{-(\ln(y)/\sigma)^2/2}, 1 < y < \infty$$
$$3 1 \left| \frac{de^{-Y/2}}{dy} \right| = \frac{1}{2} e^{-Y/2}, 0 < y < \infty$$

$$\begin{array}{l} 4 \ 1 | \frac{d \sqrt{y}}{dy} | = \frac{1}{2\sqrt{y}}, 0 < y < 1 \\ 5 \ \frac{2}{\pi} | \frac{d(\arctan \frac{y}{d})}{dy} | = \frac{2}{\pi} \frac{d(\frac{y}{d})}{[(\frac{y}{d})^2 + 1]} = \frac{2}{\pi d[(\frac{y}{d})^2 + 1]} 0 < y < \infty \end{array}$$

find mean/variance by mgf

$$\begin{array}{l} E(e^{tx}) = \int e^{tx} f(x) dx = \sum e^{tx} f(x); \ M_{aX+b}(t) = e^{tb} M_{aX}(t) \\ M_X(t) = E(e^{tx}) & M_X(0) = 1 \\ M_X'(t) = E(xe^{tx}) & M_X'(0) = E(X) \\ M_X'(t) = E(x^2 e^{tx}) & M_X'(0) = E(X^2) \\ M_X'(t) = E(x^n e^{tx}) & M_X'(0) = E(X^n) \end{array}$$

- 1	series				
	Finite	Binomial			
	$\sum_{k=1}^{n} k = \frac{n(n+1)}{2}$ $\sum_{k=1}^{n} (2k-1) = n^2$	$\sum_{k=0}^{n} \binom{n}{k} = 2^n$ $\sum_{k=0}^{n} \binom{r+k}{k} = \binom{r+n+1}{n}$			
	$\sum_{k=1}^{n} k^2 = \frac{n(n+1)(2n+1)}{6}$	$\sum_{k=0}^{n} \binom{k}{m} = \binom{n+1}{m+1}$			
	$\sum_{k=1}^{n} k^3 = (\frac{n(n+1)}{2})^2$	$\sum_{k=0}^{r} {m \choose k} {n \choose r-k} = {m+n \choose r}$			
	$\sum_{k=0}^{n} c^k = \frac{c^{n+1} - 1}{c - 1}$	$\sum_{k=0}^{n} \binom{n}{k} a^{n-k} b^k = (a+b)^n$			
L	Infinite $ p < 1$ $\sum_{k=0}^{\infty}$	$_{0} kp^{k-1} = \frac{d}{dp} \left(\sum_{k=0}^{\infty} p^{k} \right) = \frac{1}{(1-p)^{2}}$			
2	$\sum_{k=0}^{\infty} p^k = \frac{1}{1-p} \sum_{k=0}^{\infty}$	$\binom{r+k-1}{k}x^k = (1-x)^{-r}r \in \mathbb{N}^+$			
	$\sum_{k=1}^{\infty} p^k = \frac{p}{1-p} \mid \sum_{k=1}^{\infty}$	$\binom{\alpha}{k}p^k = (1+p)^{\alpha} p < 1, \ \alpha \in \mathbb{C}$			
	$\Gamma(n) = (n-1)!$	$\sum_{n=0}^{\infty} \frac{x^n}{n!} = e^x$			
		$\sum_{n=0}^{\infty} ar^n = \frac{a}{1-r}, r < 1$			
		$\sum_{k=0}^{n-1} ar^n = \frac{a(1-r^n)}{1-r}$			
	$\Gamma(0) = \Gamma(-1) = \infty$	$\int_0^1 x^{a-1} (1-x)^{b-1}, dx = \frac{\Gamma(a)\Gamma(b)}{\Gamma(a+b)}$			
	$\Gamma(-1/2) = -2\Gamma(1/2)$	$\int_0^\infty x^{t-1}e^{-x}dx = \Gamma(t)$			

Integrals+c
$$\int kdx = kx$$

$$\int e^{u}du = e^{u}$$

$$\int \int \ln udu = u \ln(u) - u$$

$$\int \ln udu = u \ln(u) - u$$

$$\int \int \frac{1}{a^{2} + u^{2}} du = \frac{1}{a} \tan^{-1}(\frac{u}{a})$$

$$\int \ln aa^{x} = a^{x}$$

Substitution

Integreation by parts

$$\begin{array}{c|c|c} u & du & dv & v \\ x & dx & e^{-x} & -e^{-x} & \int_a^b u dv \\ lnx & \frac{1}{x} dx & dx & x & \int_3^5 x lnx dx \\ & = uv|_a^b - \int_a^b v du \\ & = -xe^{-x} + \int xe^{-x} dx = -xe^{-x} - e^{-x} + c \\ & = x lnx|_3^5 - \int_3^5 dx = (x lnx - x)|_3^5 = 5 ln5 - 3 ln3 - 2 \\ \int_a^b f(x) dx = F(b) - F(a) = - \int_b^a f(x) dx = \int_a^c f(x) dx + \int_c^b f(x) dx; \\ \frac{d}{dx} \int_{v(x)}^{u(x)} f(t) dt = u'(x) f[u(x)] - v'(x) f[v(x)] \end{array}$$

Derivatives

Distribution	\mathbf{CDF}	P(X=x),f(x)	μ	EX^2	Var	MGF	M'(t)	M" (t)	$M^n(t)$
Bern(p)		$p^x q^{1-x}, x \in \{1, 0\}$	p	p	pq	$pe^t + q$			
$\operatorname{Bin}(n,p)$	$I_{1-p}(n-x,x+1)$	$\binom{n}{x} p^x q^{n-x}; x \in \{0, 1n\}$	np	$\mu(\mu+q)$	$q\mu$	$(pe^t + q)^n$			
Geom(p)	$1 - q^x$	$pq^{x-1}, x \in 1, 2, \dots$	$\frac{1}{p}$	$\frac{p+2q}{p^2}$ $\frac{q^2+q}{p^2}$	$\frac{q}{p^2}$	$\frac{pe^t}{1-qe^t}, t < -\ln q$	4	_	
	$1 - q^{x+1}$	$pq^x, x \in 0, 1, \dots$	$\frac{q}{p}$	$\frac{q^2+q}{p^2}$	$\frac{q}{p^2}$	$\frac{p}{1-qe^t}, qe^t < 1$	$\frac{pqe^t}{(1-qe^t)^2}$	$\frac{2pqe^t}{(1-qe^t)^3} - M'(t)$	
$\operatorname{NBin}(r,p)$		$\binom{x-1}{r-1} p^r q^{x-r}, x \in r, r+1$	$\frac{r}{p}$		$\frac{rq}{p^2}$ $\frac{rq}{p^2}$	$(\frac{pe^t}{1-qe^t})^r$			
		$\binom{x+r-1}{r-1} p^r q^x, x \in 0, 1$	$\frac{rq}{p}$		$\frac{rq}{p^2}$	$(\frac{\vec{p}}{1 - qe^t})^r, qe^t < 1$			
$\mathrm{HGeom}(N,m,k)$		$\frac{\binom{m}{x}\binom{N-m}{k-x}}{\binom{N}{k}}$	$\frac{km}{N}$		$\mu \tfrac{(N-m)(N-k)}{N(N-1)}$				
$\mathrm{HGeom}(w,b,k)$		$\frac{\binom{w}{x}\binom{\acute{b}}{k-x}}{\binom{w+b}{k}}$	$\frac{kw}{w+b}$		$\mu_{\frac{b(w+b-k)}{(w+b)(w+b-1)}}$				
$Pois(\mu)$	$e^{-\mu} \sum_{i=0}^{x} \frac{\mu^i}{i!}$	$\frac{\mu^x}{x!}e^{-\mu}, x \in 0, 1$	μ	$\mu^2 + \mu$	μ	$e^{\mu(e^t-1)}$	$\mu e^t M(t)$	$\mu e^t (1 + \mu e^t) M(t)$	
Unif(n)		$\frac{1}{n}, x \in 1, 2n$	$\frac{n+1}{2}$	$\frac{(n+1)(2n+1)}{6}$	$\frac{(n^2-1)}{12}$	$\frac{\sum_{i=1}^{n} e^{ti}}{n}$			
$\mathrm{Unif}(a,b)$	$\frac{x-a}{b-a}$	$\frac{1}{b-a}, x \in (a,b)$	$\frac{a+b}{2}$		$\frac{(b-a)^2}{12}$	$\frac{e^{tb} - e^{ta}}{t(b-a)}$			
$\mathcal{N}(\mu,\sigma^2)$		$\frac{1}{\sigma\sqrt{2\pi}}e^{-\frac{(x-\mu)^2}{2\sigma^2}}$	μ	$\mu^2 + \sigma^2$	σ^2	$e^{\mu t + \frac{\sigma^2 t^2}{2}}$	$(\mu+\sigma^2t)M(t)$	$[(\mu+\sigma^2t)^2+\sigma^2]M(t)$	
$\mathcal{N}(0,1)$		$\frac{1}{e^{-\frac{x^{2}}{2}}}$	0	1	1	$e^{\frac{t^2}{2}}$			
$\mathcal{LN}(\mu, \sigma^2)$		$\frac{1}{\frac{1}{x\sigma\sqrt{2\pi}}e^{\frac{-(\ln x - \mu)^2}{2\sigma^2}}}$	$e^{\mu + \frac{\sigma^2}{2}}$	$e^{2\mu+2\sigma^2}$	$\theta^2(e^{\sigma^2}-1)$	×			
$Cauchy(\theta, \sigma^2)$		$\pi \sigma \frac{1+(\frac{x-\theta}{2})^2}{1+(\frac{x-\theta}{2})^2}$	×	×	×				
D Expo (μ, σ^2)		$\frac{1}{2\pi\sigma}e^{-\left \frac{x-\mu}{\sigma}\right }$	μ	$\mu^2 + 2\sigma^2$	$2\sigma^2$	$\frac{e^{\mu t}}{1 - \sigma^2 t^2}$			
$\text{Expo}(\lambda)$	$1 - e^{-\lambda x}$	$\lambda e^{-\lambda x}, x \in (0, \infty)$	$\frac{1}{\lambda}$		$\frac{1}{\lambda^2}$	$\frac{\lambda}{\lambda - t}, t < \lambda$			
$\operatorname{Expo}(\beta)$		$\frac{1}{\beta}e^{-\frac{x}{\beta}}$	β		β^2	$\frac{1}{1-\beta t}$	$\beta(1-\beta t)^{-2}$	$2\beta^2(1-\beta t)^{-3}$	
$\operatorname{Gamma}(a,\lambda)$		$\frac{\lambda^a}{\Gamma(a)} x^{a-1} e^{-\lambda x}, x \in (0, \infty)$	$\frac{a}{\lambda}$	$\frac{a}{\lambda^2}$	$\left(\frac{\lambda}{\lambda - t}\right)^a, t < \lambda$				
$\operatorname{Gamma}(\alpha,\beta)$		$\frac{1}{\Gamma(a)\beta^{\alpha}}x^{a-1}e^{-x/\beta}$	lphaeta	$\alpha \beta^2$	$\left(\frac{1}{1-\beta t}\right)^a, t < \frac{1}{\beta}$				
Beta(a,b)		$\frac{\Gamma(a+b)}{\Gamma(a)\Gamma(b)}x^{a-1}(1-x)^{b-1}$	$\frac{a}{a+b}$		$\frac{\mu(1-\mu)}{(a+b+1)}$				$\frac{\Gamma(\alpha+n)\Gamma(\alpha+\beta)}{\Gamma(\alpha+\beta+n)\Gamma(\alpha)}$
$B(\alpha, \beta) =$		$\Gamma(\alpha)\Gamma(\beta)$ $\sigma \in (0, 1)$		$\frac{a(a+1)}{(a+b)(a+b+1)}$	$\frac{ab}{(a+b)^2(a+b+1)}$				
χ_p^2		$\frac{1}{2^{p/2}\Gamma(p/2)} x^{p/2-1} e^{-x/2}$	p	$2p + p^2$	2p	$(1-2t)^{-p/2}, t < \frac{1}{2}$			
t_n		$\frac{\Gamma(\frac{n+1}{2})}{\sqrt{n\pi}\Gamma(\frac{n}{2})} \left(1 + \frac{x^2}{n}\right)^{-\frac{n+1}{2}}$	0, n > 1		$\frac{n}{n-2}, n > 2$	×			