# A Documentary History of the Nock Combinator Calculus

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#### Abstract

Nock is a family of computational languages derived from the SKI combinator calculus. It serves as the ISA specification layer for the Urbit and NockApp systems. This article outlines the extant historical versions of the Nock combinator calculus and reconstructs the motivation for the changes made at each kelvin decrement. It begins with an exposition of Nock as a tool of computation, outlines the history of Nock's decrements, and speculates on motivations for possible future developments.

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# 1 Introduction

Nock is a combinator calculus which serves as the computational specification layer for the Urbit and Nockchain/Nock-35 App systems. It is a hyper-RISC instruction set architecture 36 (ISA) intended for execution by a virtual machine (but see Mopfel2025 37 (Mopfel2025), pp. XX–XX herein). Nock's simplicity and unity 38 of expression make it amenable to proof-based reasoning and 30 guarantees of correctness. Its Lisp-like nature surfaces the abil-40 ity to introspect on the code itself, a property which higher-41 level languages compiling to it can exploit. Yet for all this, Nock 42 was not born from a purely mathematical approach, but found 43 its roots in practical systems engineering. 11

Nock permits itself a finite number of specification changes, called "decrements" or "kelvins", which allow it to converge on a balance of expressiveness and efficacy. This article outlines the extant historical versions of the Nock combinator calculus and reconstructs the motivation for the changes made at each kelvin decrement. It begins with an exposition of Nock as a tool of computation, outlines the history of Nock's decrements, and speculates on motivations for possible future developments.

# 2 Nock as a Combinator Calculus

Fundamental computer science research has identified a family of universal computers which may be instantiated in a variety of ways, such as the Turing machine, the lambda calculus,

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and the combinator calculus. Equivalence theorems such as the Church–Turing thesis show that these systems are equivalent in their computational power, and that they can be used to compute any computable function. The combinator calculus is a family of systems which use a small set of combinators to express computation. The most well-known member of this family is the ski combinator calculus, which uses only three combinators: s, k, and i. Other members of this family include the BCKW combinator calculus and the H combinator calculus. These systems are all equivalent in their computational power, but they differ in their syntax and semantics. The Nock combinator calculus is an extension of the ski combinator calculus which adds a few axiomatic rules to navigate and manipulate binary trees, carry out a very primitive arithmetic, and provide for side effects.

Q/I

Perhaps better put, Nock is a family of combinator calculi that sequentially converge on an "optimal" expressiveness for certain design desiderata. This includes an economy of expression (thus several macro opcodes) and consideration of how a higher-level language would invoke stored procedural expressions. Furthermore an opcode exists which produces and then ignores a computation, intended to signal to a runtime layer that a side effect may be desired by the caller.

Nock bears the following characteristics:

- Turing-complete. Put formally, Turing completeness (and thus the ability to evaluate anything we would call a computation) is exemplified by the μ-recursive functions. In practice, these amount to operations for constant, increment, variable access, program concatenation, and looping (Reitzig, 2012). Nock supports these directly through its primitive opcodes.
- Functional (as in language). Nock is a pure function
  of its arguments. In practice, the Urbit operating system provides a simulated global scope for userspace applications, but this virtualized environment reduces to
  garden-variety Nock. (See Davis2025b (Davis2025b),
  pp. XX–XX in this volume, for details of a Nock virtualized interpreter.)

- Subject-oriented. Nock evaluation consists of a formula as a noun to be evaluated against a subject as a noun. Taken together, these constitute the entire set of inputs to a pure function.
  - Some Nock opcodes alter the subject (for instance a variable declaration) by producing a new subject which is utilized for subsequent axis lookups.
- Homoiconic. Nock unifies code and data under a single representation. A Nock atom is a natural number, and a Nock cell is a pair of nouns. Every Nock noun is acyclic, and every Nock expression is a binary tree. For example, Nock expressions intended to be evaluated as code are often pinned as data by the constant opcode until they are retrieved by evaluating the constant opcode at that axis.
- Untyped. Nock is untyped, meaning that it does not impose any type system on the expressions it evaluates.
  Nock "knows" about the natural numbers in two senses: such are used for addressing axes in the binary tree of a noun, and such are manipulated and compared using the increment and equality opcodes.
- Solid-state. A Nock interpreter is a solid-state machine, meaning that it operates from a state to a new state strictly according to inputs as a pure lifecycle function. The Nock interpreter must commit the results of a successful computation as the new state before subsequent computations, or events, can be evaluated. Transient evaluations (uncompleted events) and crashes (invalid evaluations) may be lost without consequence, and the Nock interpreter layer persists the underlying state of the machine.

We have asserted without demonstration thus far that Nock is a combinator calculus. We now show that this is the case, with reference to Nock 4K, the latest specification. The simplest combinator calculus consists of only three combinators: s,  $\kappa$ , and t (Wolfram, 2021). These combinators are:

1. s substitution. sxyz = xz(yz), returns the first argument applied to the third, then applies this to the result of the second argument applied to the third. This corresponds to Nock 4K's opcode 2, which substitutes the second argument into the first argument at the third argument's axis. (There are some subtle differences to Nock's expression of s as opcode 2 that we will elide as being fundamentally similar, but perhaps worthy of its own monograph.)

- 2. K constant.  $\kappa xy = x$ , consumes its argument and returns a constant in all cases. This corresponds to Nock 4K's opcode 1, which yields its argument as a constant noun.
- 3. I identity. Ix = x, returns its argument. This corresponds to a special case of Nock 4K's opcode o, a generalized axis lookup operator, which can trivially retrieve the current subject or expression as well as any children.

While Nock introduces a few more primitive operations as a practicality, the above identities establish its bona fides as a combinator calculus capable of general computation. Similar to Haskell Curry's BCKW system, which can be written in forms isomorphic to SKI, Nock provides a set of primitive rules and a set of economic extended rules for convenience in writing a compiler.<sup>1</sup>

In an early document, Yarvin explained two of his design criteria in producing Nock as a practical ISA target (~sorreg-namtyv, 2010):

- Natural conversion of source to code without other inputs.
- Metacircularity without deep stacks; i.e., the ability to extend Nock semantics without altering the underlying substrate.

<sup>&</sup>lt;sup>1</sup>See **Galebach2025** (**Galebach2025**), pp. 1–45 in this volume, for exposition on how to evaluate a Nock expression by hand or by interpreter.

This latter idea he particularly connected to the concept of what came to be called a "scry namespace": "dereferencing Urbit paths is as natural (and stateless) a function as increment or equals" (ibid.). Indeed, Urbit's current userspace utilizes such an affordance to replicate a global scope environment for accessing system and remote resources. (See **Davis2025b** (**Davis2025b**), pp. XX–XX in this volume, for a discussion of the Nock virtualized interpreter.)

# 3 Nock's Decrements

The Nock family survives in a trail of breadcrumbs, with each version of the specification being a decrement of the previous version.<sup>2</sup> Early versions were produced exclusively by Curtis Yarvin, eventually involving the input of other developers after the 2013 founding of Tlon Corporation. In this section, we present each extant version of the Nock specification and comment on the changes and their motivations. Only the layouts have been changed for print. Dates for Nock specifications were derived from dated public posts (U, 9K), internal dating (13K, 12K, 11K, 10K), or from Git commit history data (8K, 7K, 6K, 5K).<sup>3</sup> No version of 14K survives publicly, nor does any primordial version prior to U (15K) appear to exist.

Yarvin's background as a systems engineer with systems like Xaos Tools (for sgi Irix), Geoworks (on DoCoMo's iMode), and Unwired Planet (on the Wireless Application Protocol, WAP) inclined him towards a formal break with Unix-era computing (~sorreg-namtyv, 2025). He sought to produce a system enabling server-like behavior rather than a network of clients dependent on centralized servers for a functional Internet. This required a deep first-principles rederivation of computing; the foundational layer was a combinator calculus which became Nock. Nock was intended from the beginning to become less provisional over time, encoding a kelvin decrement which forced

<sup>&</sup>lt;sup>2</sup>This system, called "kelvin decrementing", draws on analogy with absolute zero as the lowest possible temperature—and thus most stable state.

<sup>&</sup>lt;sup>3</sup>In at least one case (7K), Yarvin claims to have finished the proposal a month earlier but to not have posted it until this date.

the specification to converge on a sufficiently good set of opcodes. Many downstream consequences of Urbit and NockApp as systems derive directly from the affordances encoded into Nock.

### 3.1 U

I have not really worked with combinator models, but my general impression is that it takes essentially an infinite amount of syntactic sugar to turn them into a programming language. U certainly takes some sweetener, but not, I think, as much. (~sorreq-namtyv4, 2006)

The earliest extant Nock is U, a proto-Nock posted to the Lambda the Ultimate blog in 2006 (~sorreg-namtyv (2006); ~sorreg-namtyv (2006)).<sup>5</sup> The draft is versioned 0.15; subsequent evidence indicates that this is a downward-counting kelvin-versioned document already. The full specification is reproduced in Listing 1.

Extensive commentary on the operators is provided. Rightwards grouping of tuple expressions has already been introduced. Extension of the language is summarily ruled out.<sup>6</sup> Data are conceived of as Unix-like byte streams; details of parsing and lexing are considered. Terms (the ancestor of nouns) include a NULL-like "foo" type ~ distinguishable by value rather than structure. ASCII is built in as numeric codes, similar to Gödel numbering.

As commenter Mario B. pointed out, the U specification permits SKI operators with the simple expressions,

221	[name]	[pattern]	[definition]								
222	(I)	(I \$a)	\$a								
223	(K)	(K \$a \$b)	<b>\$</b> b								
224	(S)	(S \$a \$b \$c)	(\$a \$c (\$b \$c))								

<sup>&</sup>lt;sup>4</sup>Avant la lettre.

 $<sup>^5</sup>$ Curtis Yarvin was consulted for elements of this history. Unfortunately many elements of the original prehistory of Nock appear to be lost to the sands of time on unrecoverable hard drives.

<sup>&</sup>lt;sup>6</sup>Compare Ax and Conk, pp. XX-XX herein.

While early work (1940s-50s) had been carried out on "minimal instruction set computers" (MISCS), it is more likely that Yarvin was influenced by contemporaneous work on "reduced instruction set computers" (RISCS) in the 1980s and 90s. Language proposals like that of Madore's Unlambda and Burger's Pico Lisp may have influenced Yarvin's design choices throughout this era.

The U specification is in some ways the single most interesting historical document of our series. Yarvin particularly identified a desire to avoid baking abstractions like variables and functions into the U cake, and an emphasis on client–server semantics. The scry namespace appears *avant la lettre* as a referentially transparent immutable distributed namespace. U expresses a very ambitious hyper-Turing operator, acknowledging that its own instantiation from the specification is impossible and approximate. Yarvin grapples in U with the halting problem (via his follow operator) and with the tension between a specification and an implementation (a gulf he highlighted as a human problem in his 2025 LambdaConf keynote address). Furthermore, asides on issues like the memory arena prefigure implementation details of Vere as a runtime.

Listing 1: U, 31 January 2006. The earliest extant patriarch of the Nock family.

```
246
    U: Definition
247
248
    1 Purpose
249
         This document defines the U function and its data
250
251
252
    2 License
253
         U is in the public domain.
254
255
    3 Status
256
         This text is a DRAFT (version 0.15).
257
258
    4 Data
259
         A value in U is called a "term."
                                                There are three
260
         kinds of term: "number," "pair," and "foo."
261
262
```

```
A number is any natural number (ie, nonnegative
263
         integer).
264
265
         A pair is an ordered pair of any two terms.
266
267
         There is only one foo.
268
269
270
    5 Syntax
         U is a computational model, not a programming
272
         language.
273
         But a trivial ASCII syntax for terms is useful.
275
    5.1 Trivial syntax: briefly
236
        Numbers are in decimal. Pairs are in parentheses
         that nest to the right. Foo is "~".
278
279
         Whitespace is space or newline.
                                             Line comments
280
         use "#".
281
282
283
    5.2 Trivial syntax: exactly
         term
                  : number
284
                  | 40 ?white pair ?white 41
285
                  | foo
286
287
         number
                 : 48
288
                  | [49-57] *[48-57]
289
290
         pair
                  : term white term
291
                  | term white pair
292
293
        foo
                 : 126
294
295
                 : *(32 | 10 | (35 *[32-126] 10))
296
207
    6 Semantics
298
         U is a pure function from term to term.
299
300
         This document completely defines U. There is no
30,1
         compatible way to extend or revise U.
302
303
    6.1 Rules
304
```

```
[definition]
         [name]
                  [pattern]
305
306
                   ($a 0 $b)
         (a)
                                               $b
307
                   ($a 1 $b $c)
         (b)
                                               1
308
         (c)
                   ($a 1 $b)
                                               0
309
         (d)
                   ($a 2 0 $b $c)
                                               $b
310
                   ($a 2 %n $b $c)
         (e)
                                               $c
314
                   ($a 3 $b $c)
         (f)
                                               =($b $c)
312
                   ($a 4 %n)
         (g)
                                               +%n
313
314
                   ($a 5 (~ ~ $b) $c)
         (h)
                                               $b
315
                   ($a 5 (~ $b $c) $d)
                                               *($a $b $c $d)
         (i)
31/6
                   ($a 5 (~ ~) $b)
         (j)
317
         (k)
                   ($a 5 (~ $b) $c)
                                               *($a $b $c)
318
                   ($a 5 ($b $c) $d)
         (1)
                                    (*(\$a \$b \$d) *(\$a \$c \$d))
320
                   ($a 5 $b $c)
                                               $b
         (m)
321
322
         (n)
                   (\$a 6 \$b \$c) * (\$a * (\$a 5 \$b \$c))
323
                   ($a 7 $b)
                                               *($a 5 $a $a $b)
324
         (0)
                   ($a 8 $b $c $d)
                                               >($b $c $d)
325
         (p)
326
         (p)
                   ($a $b $c)
                                    *(\$a 5 *(\$a 7 \$b) \$c)
                   ($a $b)
                                               *($a $b)
         (r)
328
                                               *$a
         (s)
                   $a
329
330
        The rule notation is a pseudocode, only used in
331
        this file. Its definition follows.
332
333
    6.2 Rule pseudocode: briefly
334
         Each line is a pattern match. "%" means
         "number." Match in order. See operators below.
336
337
    6.3 Rule pseudocode: exactly
338
         Both pattern and definition use the same
339
         evaluation language, an extension of the trivial
340
         syntax.
341
342
        An evaluation is a tree in which each node is a
343
        term, a term-valued variable, or a unary
344
        operation.
345
346
```

```
Variables are symbols marked with a constraint.
347
        A variable "$name" matches any term.
348
        matches any number.
349
350
        There are four unary prefix operators, each of
351
        which is a pure function from term to term: "=",
352
        "+", "*", and ">". Their semantics follow.
353
354
    6.4 Evaluation semantics
355
        For any term $term, to compute U($term):
356
357
             - find the first pattern, in order, that
358
               matches $term.
359
             - substitute its variable matches into its
360
               definition.
361
             - compute the substituted definition.
362
363
        Iff this sequence of steps terminates, U($term)
364
        "completes." Otherwise it "chokes."
365
366
        Evaluation is strict: incorrect completion is a
367
               Choking is U's only error or exception
368
        bug.
        mechanism.
369
370
    6.5 Simple operators: equal, increment, evaluate
371
         =($a $b) is 0 if $a and $b are equal; 1 if they
372
        are not.
373
374
        +%n is %n plus 1.
375
376
        *$a is U($a).
377
378
    6.6 The follow operator
379
        >($a $b $c) is always 0. But it does not always
380
        complete.
381
382
        We say "$c follows $b in $a" iff, for every $term:
383
384
             if \star($a 5 $b $term) chokes:
385
                 \star(\$a 5 \$c \$term) chokes.
386
387
             if *(\$a 5 \$b \$term) completes:
388
```

```
either:
389
                     \star($a 5 $c $term) completes, and
390
                     *($a 5 $c $term) equals
393
                       *($a 5 $b $term)
392
                or:
393
                     *($a 5 $c $term) chokes.
394
395
        396
397
398
        If this statement cannot be shown (ie, if there
        exists any $term that falsifies it, generates an
399
        infinitely recursive series of follow tests, or is
400
        inversely self-dependent, ie, exhibits Russell's
401
        paradox), >($a $b $c) chokes.
402
403
    7 Implementation issues
404
        This section is not normative.
405
    7.1 The follow operator
407
        Of course, no algorithm can completely implement
408
        the follow operator. So no program can completely
409
        implement U.
410
451
        But this does not stop us from stating the
412
        correctness of a partial implementation - for
413
        example, one that assumes a hardcoded set of
414
        follow cases, and fails when it would otherwise
415
        have to compute a follow case outside this set.
416
417
        U calls this a "trust failure." One way to
418
        standardize trust failures would be to standardize
        a fixed set of follow cases as part of the
420
        definition of U.
                          However, this is equivalent to
423
        standardizing a fixed trusted code base.
422
        problems with this approach are well-known.
423
424
        A better design for U implementations is to
425
        depend on a voluntary, unstandardized failure
426
                    Because all computers have bounded
        mechanism.
427
        memory, and it is impractical to standardize a
428
        fixed memory size and allocation strategy, every
429
        real computing environment has such a mechanism.
430
```

```
431
        For example, packet loss in an unreliable packet
432
        protocol, such as UDP, is a voluntary failure
433
        mechanism.
434
435
        If the packet transfer function of a stateful UDP
436
        server is defined in terms of U. failure to
                                           If the server
        compute means dropping a packet.
438
        has no other I/O, its semantics are completely
        defined by its initial state and packet function.
440
441
    7.2 Other unstandardized implementation details
442
        A practical implementation of U will detect and
443
        log common cases of choking.
                                        It will also need a
444
        timeout or some other unspecified mechanism to
        abort undetected infinite loops.
446
448
        (Although trust failure, allocation failure or
448
        timeout, and choke detection all depend on what
449
        is presumably a single voluntary failure
450
        mechanism, they are orthogonal and should not be
451
        confused.)
452
453
        Also, because U is so abstract, differences in
454
        implementation strategy can result in performance
455
        disparities which are almost arbitrarily extreme.
456
        The difficulty of standardizing performance is
458
        well-known
458
459
        No magic bullet can stop these unstandardized
460
        issues from becoming practical causes of lock-in
461
        and incompatibility. Systems which depend on U
462
        must manage them at every layer.
463
```

## 3.2 Nock 13K

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At some point between January 2006 and March 2008, Nock acquired its cognomen.

Source: ~sorreg-namtyv (2006)

The only compound opcode is opcode 6, the conditional branch opcode.

## Axiomatic operator \* tar7 is identified as a GOTO.8

# Listing 2: Nock 13K, 8 March 2008.

```
472
    Author: Curtis Yarvin (curtis.yarvin@gmail.com)
473
    Date: 3/8/2008
474
    Version: 0.13
475
    1. Manifest
47%
178
        This file defines one Turing-complete function,
        "nock."
480
481
        nock is in the public domain.
                                           So far as I know,
482
        it is neither patentable nor patented. Use it at
483
        your own risk.
484
485
    2. Data
486
483
        Both the domain and range of nock are "nouns."
488
489
        A "noun" is either an "atom" or a "cell."
490
        "atom" is an unsigned integer of any size.
491
        "cell" is an ordered pair of any two nouns, the
492
        "head" and "tail."
493
494
    3. Pseudocode
495
496
        nock is defined in a pattern-matching pseudocode.
497
498
        Match precedence is top-down.
                                           Operators are
400
        prefix.
                 Parens denote cells, and group right:
500
         (a b c) is (a (b c)).
501
502
    4. Definition
503
504
```

505

<sup>4.1</sup> Transformations

<sup>&</sup>lt;sup>7</sup>We refer to Nock axiomatic operators via their modern aural ASCII pronunciations. While these evolved over time (to wit, ^ "hat" became "ket"), to attempt to synchronize pronunciation with the era of a Nock release is a fool's errand.

 $<sup>^8\</sup>mbox{One}$  can see the influence of this version's naming scheme on Atman's Ax, pp. XX–XX herein.

```
506
            *(a 0 b c)
                           => *(*(a b) c)
503
            *(a 0 b)
                            => /(b a)
508
            *(a 1 b)
                            = > (b)
509
            *(a 2 b)
                            => **(a b)
510
            *(a 3 b)
                            => &*(a b)
511
51/2
            \star (a 4 b)
                            => ^*(a b)
513
            *(a 5 b)
                            => =*(a b)
            \star(a 6 b c d) => \star(a 2 (0 1)
514
                                       2 (1 c d) (1 0)
515
                                       2 (1 2 3) (1 0) 4 4 b)
516
            *(a b c)
                            => (*(a b) *(a c))
543
            *(a)
                            => *(a)
518
519
     4.2 Operators
520
521
     4.2.1 Goto (*)
532
523
            *(a)
                                -> nock(a)
524
525
     4.2.2 Deep (&)
526
523
            &(a b)
                                 -> 0
528
            &(a)
529
530
     4.2.3 Bump (^)
531
532
            ^(a b)
                                 -> ^(a b)
533
            ^(a)
                                 \rightarrow a + 1
534
535
     4.2.4 Same (=)
536
537
                                 -> 0
538
            = (a a)
                                 - > 1
            = (a b)
539
            = (a)
                                 -> = (a)
540
541
     4.2.5 Snip (/)
542
543
            /(1 \ a)
544
            /(2 a b)
                                 - > a
545
            /(3 \ a \ b)
                                 - > b
546
            /((a + a) b)
                                 -> /(2 /(a b))
543
```

```
548 /((a + a + 1) b) -> /(3 /(a b))

549 /(a) -> /(a)
```

### 3.3 Nock 12K

551

552

Opcodes were reordered slightly. Compound opcodes were introduced, such as a conditional branch and a static hint opcode.

# Listing 3: Nock 12K, 2008.

```
555
    Author: Curtis Yarvin (curtis.yarvin@gmail.com)
556
    Date: 3/28/2008
557
    Version: 0.12
558
559
    1. Introduction
560
561
        This file defines one function, "nock."
562
         nock is in the public domain.
564
565
    2. Data
566
567
        A "noun" is either an "atom" or a "cell." An
568
         "atom" is an unsigned integer of any size.
569
         "cell" is an ordered pair of any two nouns,
578
        the "head" and "tail."
571
572
    3. Semantics
573
574
         nock maps one noun to another. It doesn't
575
         always terminate.
576
577
    4. Pseudocode
578
579
         nock is defined in a pattern-matching
588
         pseudocode, below.
581
582
         Parentheses enclose cells. (a b c) is
583
         (a (b c)).
584
585
    5. Definition
586
```

```
587
     5.1 Transformations
588
589
            *(a (b c) d) => (*(a b c) *(a d))
599
            *(a 0 b)
                            => /(b a)
591
            *(a 1 b)
                            => (b)
592
593
            *(a 2 b c)
                            => *(*(a b) c)
594
            *(a 3 b)
                            => **(a b)
            \star(a 4 b)
                            => &*(a b)
595
            \star(a 5 b)
                            => **(a b)
596
            *(a 6 b)
                            => =*(a b)
597
598
           *(a 7 b c d) \Rightarrow *(a 3 (0 1) 3 (1 c d) (1 0)
599
                                     3 (1 2 3) (1 0) 5 5 b)
60,9
                            \Rightarrow *(a 2 (((1 0) b) c) 0 3)
            *(a 8 b c)
            *(a 9 b c)
                            => *(a c)
602
603
            *(a)
                            => *(a)
604
695
     5.2 Operators
606
607
     5.2.1 Goto (*)
608
609
                                 -> nock(a)
            *(a)
610
611
612
     5.2.2 Deep (&)
613
            &(a b)
                                 -> 0
614
            &(a)
                                 -> 1
616
616
     5.2.4 Bump (^)
617
618
            ^(a b)
619
                                 -> ^(a b)
            ^(a)
                                 \rightarrow a + 1
629
621
     5.2.5 \text{ Same (=)}
622
623
            =(a a)
                                 -> 0
624
            =(a b)
                                 - > 1
625
            = (a)
                                 -> = (a)
626
627
    5.2.6 Snip (/)
```

## 3.4 Nock 11K

637

638

639

640

641

642

Opcodes were reordered slightly. The conditional branch was moved to 2. Composition, formerly at 2, was removed.

The kelvin versioning system here became explicit (rather than implicitly decreasing minor versions).

## Listing 4: Nock 11K, 25 May 2008.

```
643
    Author: Mencius Moldbug (moldbug@gmail.com)
644
    Date: 5/25/2008
645
    Version: 11K
646
    1. Introduction
648
649
        This file defines one function. "nock."
650
651
        nock is in the public domain.
652
653
    2. Data
654
655
        A "noun" is either an "atom" or a "cell." An
656
        "atom" is an unsigned integer of any size. A
657
        "cell" is an ordered pair of any two nouns, the
658
        "head" and "tail."
659
660
    3. Semantics
661
662
668
        nock maps one noun to another. It doesn't always
        terminate.
664
665
    4. Pseudocode
666
667
```

```
nock is defined in a pattern-matching pseudocode,
668
         below.
669
670
         Parentheses enclose cells. (a b c) is (a (b c)).
671
672
    5. Definition
633
674
    5.1 Transformations
675
676
           *(a (b c) d) => (*(a b c) *(a d))
677
           *(a 0 b)
                          => /(b a)
678
           *(a 1 b)
                           => (b)
679
           *(a 2 b c d) => *(a 3 (0 1) 3 (1 c d) (1 0)
680
                                   3 (1 2 3) (1 0) 5 5 b)
681
           *(a 3 b)
                           => **(a b)
682
           *(a 4 b)
                          => &*(a b)
683
           *(a 5 b)
                          => * (a b)
684
           *(a 6 b)
                           \Rightarrow = *(a b)
685
686
                          => *(a 3 (((1 0) b) c) 1 0 3)
687
           *(a 7 b c)
           *(a 8 b c)
                          => *(a c)
688
689
           *(a)
                          => *(a)
690
691
    5.2 Operators
692
693
    5.2.1 Goto (*)
694
695
           *(a)
                               -> nock(a)
696
697
    5.2.2 Deep (&)
698
699
           &(a b)
                               -> 0
700
           &(a)
                               -> 1
701
702
    5.2.4 Bump (^)
768
704
           ^(a b)
                               -> ^(a b)
705
           ^(a)
                               \rightarrow a + 1
706
707
    5.2.5 Same (=)
708
709
```

```
=(a a)
                                       -> 0
710
              =(a b)
                                       -> 1
711
              = (a)
                                       \rightarrow = (a)
712
71/3
     5.2.6 Snip (/)
714
715
716
              /(1 \ a)
              /(2 \ a \ b)
                                       - > a
717
              /(3 \ a \ b)
                                       \rightarrow /(2 /(a b))
719
              /((a + a) b)
              /((a + a + 1) b) \rightarrow /(3 /(a b))
720
                                       -> /(a)
              /(a)
733
```

## 3.5 Nock 10K

723

725

726

727

729

Parentheses were replaced by brackets. Opcodes were reordered slightly. Hint syntax was removed. Functionally, 11K and 10K appear very similar, particularly if the Watt (proto-Hoon) compiler is set up to produce variable declarations and compositions as the compound opcodes had them.

Listing 5: Nock 10K, 15 September 2008.

```
730
    Author: Mencius Moldbug [moldbug@gmail.com]
731
    Date: 9/15/2008
732
    Version: 10K
733
734
    1. Introduction
735
736
         This file defines one function, "nock."
737
738
        nock is in the public domain.
739
740
    2. Data
741
742
        A "noun" is either an "atom" or a "cell."
         "atom" is an unsigned integer of any size.
744
         "cell" is an ordered pair of any two nouns, the
745
         "head" and "tail."
746
747
```

```
3. Semantics
748
749
        nock maps one noun to another. It doesn't always
750
        terminate.
751
752
    4. Pseudocode
753
        nock is defined in a pattern-matching pseudocode,
755
        below.
756
757
        Brackets enclose cells. [a b c] is [a [b c]].
758
759
    5. Definition
760
761
    5.1 Transformations
763
          *[a [b c] d] => [*[a b c] *[a d]]
764
          *[a 0 b]
                      => /[b a]
765
          *[a 1 b]
                       => [b]
766
          *[a 2 b c d] => *[a 3 [0 1] 3 [1 c d]
767
                                [1 0] 3 [1 2 3] [1 0] 5 5 b]
768
                         => **[a b]
          *[a 3 b]
769
          *[a 4 b]
                        => &*[a b]
770
          *[a 5 b]
                         => ^*[a b]
771
                        => =*[a b]
          *[a 6 b]
772
          *[a]
                         => *[a]
773
774
    5.2 Operators
7745
776
    5.2.1 Goto [*]
777
778
          *[a]
                            -> nock[a]
779
780
    5.2.2 Deep [&]
781
782
          &[a b]
                             -> 0
783
          &[a]
                              -> 1
784
785
    5.2.4 Bump [^]
786
787
           ^[a b]
                             -> ^[a b]
788
          ^[a]
                             -> (a + 1)
789
```

```
790
    5.2.5 Like [=]
791
792
            =[a a]
                                  -> 0
793
            =[a b]
794
            = [a]
                                  -> = [a]
795
796
    5.2.6 Snip [/]
797
798
799
            /[1 a]
            /[2 a b]
800
            /[3 a b]
801
            /[(a + a) b]
                                  -> /[2 /[a b]]
802
            /[(a + a + 1) b] -> /[3 /[a b]]
803
                                  -> /[a]
            /[a]
804
```

### 3.6 Nock 9K

806

0N7

808

809

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825

The cell detection axiomatic operator underlying opcode 4 (cell detection) was changed from & pam to? wut. Versus 10K, 9K elides operator names in favor of definitions. Other differences are likewise primarily terminological, such as the replacement of Deep & pam with? wut.

This version of Nock was published on the Moron Lab blog in 2010 (~sorreg-namtyv, 2010) as "Maxwell's equations of software". Yarvin emphasized that Nock was intended to serve as "foundational system software rather than foundational metamathematics" (ibid.). Yarvin also publicly expounded on the practicality of building a higher-level language on top of Nock at this point (ibid.):

To define a language with Nock, construct two nouns, q and r, such that \*[q r] equals r, and \*[s \*[p r]] is a useful functional language. In this description,

- p is the function source;
- q is your language definition, as source;

- r is your language definition, as data;
- s is the input data.

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More concretely, Watt (the predecessor to Hoon) is defined as:

This remains the essential pattern followed to this day by higher-level languages targeting Nock as an ISA.

Yarvin had prepared to virtualize Nock interpretation to expose a broader namespace for interaction with values than the "strict" subject of a formula (~sorreg-namtyv, 2010).

Listing 6: Nock 9K, terminus ad quem 7 January 2010.

```
840
    1 Context
841
842
         This spec defines one function, Nock.
843
844
    2 Structures
845
846
         A noun is an atom or a cell. An atom is any
847
848
         unsigned integer.
                                A cell is an ordered pair of
         any two nouns.
840
    3 Pseudocode
851
852
                                       [a b c] is [a [b c]].
         Brackets enclose cells.
853
854
         *a is Nock(a). Reductions match top-down.
855
856
    4 Reductions
857
858
         ?[a b]
859
         ? a
                              = > 1
866
861
         ^[a b]
                              => ^[a b]
862
          ^ a
                              \Rightarrow (a + 1)
863
864
         =[a a]
                              = > 0
865
```

```
=[a b]
                              = > 1
866
867
868
         /[1 a]
869
         /[2 a b]
870
         /[3 a b]
871
         /[(a + a) b]
                              => /[2 /[a b]]
         /[(a + a + 1) b] => /[3 /[a b]]
873
         / a
                              => /a
874
875
                              => /[b a]
         *[a 0 b]
876
         *[a 1 b]
                              = > b
877
         *[a 2 b c d]
                              => *[a 3 [0 1] 3 [1 c d] [1 0]
878
                                      3 [1 2 3] [1 0] 5 5 b]
879
         *[a 3 b]
                              => **[a b]
880
         *[a 4 b]
                              => ?*[a b]
881
         *[a 5 b]
                              => ^*[a b]
882
         *[a 6 b]
                              => =*[a b]
883
         *[a [b c] d]
                              => [*[a b c] *[a d]]
884
                              = > * a
885
```

#### 3.7 Nock 8K

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900

The compound opcodes reappeared. Opcode 6 defined a conditional branch. Opcode 7 was described as a function composition operator. Opcode 8 served to define variables. Opcode 9 defined a calling convention. The remaining opcodes are hints, but each serving a different purpose:

- 11. consolidate for reference equality.
- <sub>895</sub> 12. yield an arbitrary, unspecified hint.
  - 13. label for acceleration (jet).

Nock 8K received an uncharacteristic amount of commentary, given a preprint document prepared for presentation at the 42nd ISCIE International Symposium on Stochastic Systems Theory and Its Applications (SSS'10) (~SOTTEG-namtyv, 2010).

Lambda was highlighted as a design pattern (a "gate" or stored procedure call) enabled by the "core" convention. Notably, [[sample context] battery] occurred in a different order than has been conventional since 2013 (emphasizing that the ubiquitous core pattern is a convention rather than a requirement). Watt was revealed to have a different ASCII pronunciation convention than Nock at this stage.

901

902

903

904

905

907

Listing 7: Nock 8K, 25 July 2010.

```
908
    1 Structures
909
910
         A noun is an atom or a cell. An atom is any
911
         unsigned integer. A cell is an ordered pair of
         nouns.
913
914
    2 Pseudocode
915
916
         [a b c] is [a [b c]]; *a is nock(a). Reductions
917
         match top-down.
918
919
    3 Reductions
921
         ?[a b]
                               0
922
         ? a
                               1
923
         ^ a
                               (a + 1)
924
         =[a a]
                               0
925
         =[a b]
926
927
         /[1 a]
928
         /[2 a b]
                               а
929
         /[3 \ a \ b]
                               b
930
         /[(a + a) b]
                              /[2 /[a b]]
931
         /[(a + a + 1) b]
                               /[3 /[a b]]
932
933
         *[a [b c] d]
                               [*[a b c] *[a d]]
934
         *[a 0 b]
                               /[b a]
935
         *[a 1 b]
936
         *[a 2 b c]
                               *[*[a b] *[a c]]
937
         *[a 3 b]
                               ?*[a b]
938
         *[a 4 b]
                               ^*[a b]
939
         *[a 5 b]
                               =*[a b]
940
```

```
941
         *[a 6 b c d]
                              *[a 2 [0 1] 2 [1 c d] [1 0]
942
                                   2 [1 2 3] [1 0] 4 4 b]
943
         *[a 7 b c]
                              *[a 2 b 1 c]
944
                              *[a 7 [7 b [0 1]] c]
         *[a 8 b c]
945
         *[a 9 b c]
                              *[a 8 b 2 [[7 [0 3] d] [0 5]]
946
                                                              0 51
947
                              *[a 8 b 8 [7 [0 3] c] 0 2]
         *[a 10 b c]
948
         *[a 11 b c]
                              *[a 8 b 7 [0 3] c]
949
         *[a 12 b c]
                              *[a [1 0] 1 c]
950
951
         ^[a b]
                              ^[a b]
952
953
         = a
                              = a
         / a
                              / a
954
955
```

### 3.8 Nock 7K

957

958

959

960

961

962

During this era, substantial development took place on the early Urbit operating system. Nock began to be battle-tested in a way it had not previously been stressed. Several decrements occurred in short order.

The three hint opcodes were refactored into two, a static and a dynamic hint, both at 10.

Listing 8: Nock 7K, terminus ad quem 14 November 2010.

```
965
    1 Structures
966
967
       A noun is an atom or a cell. An atom is any
968
       natural number. A cell is any ordered pair of
969
       nouns.
970
971
    2 Pseudocode
972
973
974
       [a b c]
                             [a [b c]]
       nock(a)
975
                             * a
976
       ?[a b]
                             0
977
       ? a
                             1
078
```

```
^ a
                             1 + a
979
        =[a a]
                             0
989
        =[a b]
                             1
981
982
        /[1 a]
983
                             а
        /[2 a b]
                             а
984
        /[3 a b]
985
        /[(a + a) b]
                             /[2 /[a b]]
986
        /[(a + a + 1) b]
                             /[3 /[a b]]
987
988
       *[a [b c] d]
                             [*[a b c] *[a d]]
989
990
       *[a 0 b]
                             /[b a]
991
       *[a 1 b]
992
       *[a 2 b c]
                             *[*[a b] *[a c]]
       *[a 3 b]
                             ?*[a b]
994
       *[a 4 b]
                             ^*[a b]
995
       *[a 5 b]
                             =*[a b]
996
997
       *[a 6 b c d]
                             *[a 2 [0 1] 2 [1 c d] [1 0]
998
                                  2 [1 2 3] [1 0] 4 4 b]
aga
       *[a 7 b c]
                             *[a 2 b 1 c]
1000
       *[a 8 b c]
                             *[a 7 [[7 [0 1] b] 0 1] c]
1001
       *[a 9 b c]
                             *[a 7 c 0 b]
1002
       *[a 10 b c]
                             *[a c]
1003
       *[a 10 [b c] d]
                             *[a 8 c 7 [0 3] d]
1004
1005
        ^[a b]
                             ^[a b]
1006
        = a
                             = a
1007
        / a
                             / a
1008
        * a
                             * a
1898
```

# 3.9 Nock 6K

1011

1012

The axiomatic operator for increment was changed from \* ket to + lus. Compound opcode syntax was reworked slightly.

```
Listing 9: Nock 6K, 6 July 2011.
```

```
1015
1016 1 Structures
```

Source: ~sorreg-namtyv (2010)

```
A noun is an atom or a cell.
                                            An atom is any
1018
       natural number. A cell is an ordered pair of
1019
       nouns.
1020
1021
     2 Reductions
1022
1023
1024
       nock(a)
                              * a
        [a b c]
                              [a [b c]]
1025
1026
       ?[a b]
                              0
1027
        ? a
                              1
1028
                              1 + a
1029
        + a
        =[a a]
                              0
1030
        =[a b]
                              1
1031
1032
        /[1 a]
                              а
1033
        /[2 a b]
                              а
1034
        /[3 a b]
1035
        /[(a + a) b]
                              /[2 /[a b]]
1036
1037
       /[(a + a + 1) b]
                             /[3 /[a b]]
1038
       *[a [b c] d]
                             [*[a b c] *[a d]]
1039
1049
       *[a 0 b]
                              /[b a]
1041
       *[a 1 b]
1042
       *[a 2 b c]
                              *[*[a b] *[a c]]
1043
       *[a 3 b]
                             ?*[a b]
1044
                             +*[a b]
       *[a 4 b]
1045
       *[a 5 b]
                             =*[a b]
1046
1047
       *[a 6 b c d]
                              *[a 2 [0 1] 2 [1 c d] [1 0]
1048
                                            2 [1 2 3] [1 0] 4 4 b]
1049
       *[a 7 b c]
                              *[a 2 b 1 c]
1059
       *[a 8 b c]
                              *[a 7 [[0 1] b] c]
1051
       *[a 9 b c]
                              *[a 7 c 0 b]
1052
       *[a 10 b c]
                             *[a c]
1053
       *[a 10 [b c] d]
                             *[a 8 c 7 [0 2] d]
1054
1055
       +[a b]
                              +[a b]
1056
        = a
                              = a
1057
        / a
1058
                              / a
        * a
                              * a
1858
```

```
Source: ~sorreg-namtyv (2011)
```

## 3.10 Nock 5K

1061

1062

1063

1064

1065

1066

1067

1068

Compound opcode syntax was reworked slightly. All trivial reductions of axiomatic operators were removed to the preface of the specification.

(For instance, a trivial "cosmetic" change was made to 5K's specification after it was publicly posted in order to synchronize it with the VM's behavior (dd779c1).)

Listing 10: Nock 5K, 24 September 2012.

```
1069
     1 Structures
1070
1071
        A noun is an atom or a cell.
                                               An atom is any natural
1072
                   A cell is an ordered pair of nouns.
1073
1074
     2 Reductions
1075
1076
        nock(a)
1077
        [a b c]
                               [a [b c]]
1078
1079
        ?[a b]
                               0
1080
1081
        ? a
        +[a b]
                               +[a b]
1082
        + a
1083
                               1
        =[a a]
1084
        =[a b]
                               1
1085
1086
        = a
                               = a
1087
        /[1 a]
                               а
1088
        /[2 a b]
1089
        /[3 a b]
1090
        /[(a + a) b]
                               /[2 /[a b]]
1091
        /[(a + a + 1) b]
                               /[3 /[a b]]
1092
1093
        / a
                               / a
1094
        *[a [b c] d]
                               [*[a b c] *[a d]]
1095
1096
        *[a 0 b]
                               /[b a]
1097
        *[a 1 b]
1098
```

```
*[*[a b] *[a c]]
       *[a 2 b c]
1099
       *[a 3 b]
                            ?*[a b]
1100
       *[a 4 b]
                            +*[a b]
1101
       *[a 5 b]
                            =*[a b]
1102
1103
       *[a 6 b c d]
                            *[a 2 [0 1] 2 [1 c d] [1 0] 2
1104
1105
                                             [1 2 3] [1 0] 4 4 b]
       *[a 7 b c]
                            *[a 2 b 1 c]
1106
       *[a 8 b c]
                            *[a 7 [[7 [0 1] b] 0 1] c]
1107
       *[a 9 b c]
                            *[a 7 c 2 [0 1] 0 b]
1108
       *[a 10 [b c] d]
                            *[a 8 c 7 [0 3] d]
1109
       *[a 10 b c]
                            *[a c]
1111
       * a
                             * a
1113
```

#### 3.11 Nock 4K

1114

1116

1116

1117

1118

1119

1120

1121

1122

1125

1126

1127

1128

The primary change motivating 5K to 4K was the introduction of an edit operator # hax, which ameliorated the proliferation of cells in the Nock runtime's memory. The edit operator is an optimization which makes modifications to a Nock data structure more efficient. It's a notable example of a change motivated by the pragmatics of the runtime rather than theoretical or higher-level language concerns. To

Opcode 5 (equality) was rewritten to more explicit with application of the cell distribution rule. Opcodes 6–9 were rewritten to utilize the \* tar operator rather than routing via opcode 2. Opcode 11 (formerly opcode 10) was likewise massaged. In general, preferring to express rules using \* tar proved to be slightly more terse than utilizing opcode 2.

Listing 11: Nock 4K, terminus ad quem 27 September 2018.

```
1129 Nock 4K
1131
1132 A noun is an atom or a cell. An atom is a natural
```

<sup>&</sup>lt;sup>9</sup>The date must be earlier than 27 September 2018; cf. urbit/urbit #1027. <sup>10</sup>See ~niblyx-malnus, pp. XX–XX, this volume, for a verbose derivation of the edit operator and opcode 10 from the primitive opcodes.

```
number. A cell is an ordered pair of nouns.
1133
1134
     Reduce by the first matching pattern; variables match
1135
1136
     any noun.
1137
     nock(a)
1138
                            * a
1139
     [a b c]
                            [a [b c]]
1140
1141
     ?[a b]
                            0
     ? a
                            1
1142
                            +[a b]
1143
     +[a b]
                            1 + a
1144
     + a
     =[a a]
                            0
1145
     =[a b]
                            1
1146
1147
1148
     /[1 \ a]
                            а
     /[2 a b]
                            а
1149
     /[3 a b]
1150
     /[(a + a) b]
                            /[2 /[a b]]
1151
1152
     /[(a + a + 1) b]
                            /[3 /[a b]]
1153
     / a
                            / a
1154
     #[1 a b]
1155
     \#[(a + a) b c]
                            \#[a [b / [(a + a + 1) c]] c]
1156
     \#[(a + a + 1) b c] \#[a [/[(a + a) c] b] c]
1157
     #a
                            #a
1158
1159
                            [*[a b c] *[a d]]
     *[a [b c] d]
1160
1161
     *[a 0 b]
                            /[b a]
1162
     *[a 1 b]
1163
     *[a 2 b c]
                            *[*[a b] *[a c]]
1164
1165
     *[a 3 b]
                            ?*[a b]
     *[a 4 b]
1166
                            +*[a b]
     *[a 5 b c]
                            =[*[a b] *[a c]]
1167
1168
                         *[a *[[c d] 0 *[[2 3] 0 *[a 4 4 b]]]]
     *[a 6 b c d]
1169
     *[a 7 b c]
                            *[*[a b] c]
1170
     *[a 8 b c]
                            *[[*[a b] a] c]
1171
     *[a 9 b c]
                            *[*[a c] 2 [0 1] 0 b]
1172
                           #[b *[a c] *[a d]]
     *[a 10 [b c] d]
1173
1174
```

```
1175 *[a 11 [b c] d] *[[*[a c] *[a d]] 0 3]

1176 *[a 11 b c] *[a c]

1177

*a *a *a
```

Source: ~sorreg-namtyv (2018-09-27)

# 4 The Future of Nock

While deviations from the trunk line of the Nock family have been proposed at various points, 11 Nock itself has remained the definitional substrate of Urbit since its inception. It has also been adopted as the primary ISA of Nockchain and the NockApp ecosystem.

Why, then, do we contemplate further changes? The skew proposal by ~siprel and ~little-ponnys argued that Nock 4K represented an undesirable saddle point in the design space of possible Nocks, itself a "ball of mud" (~siprel and ~littel-ponnys, 2020). While skew itself was not adopted, it inspired the development of Plunder and PLAN as a solid-state computing architecture sharing some ambitions with Urbit and Nock (~siprel and ~littel-ponnys, 2023). A rigorously æsthetic argument can thus be sustained that Nock is not yet "close enough" to its final, diamond-perfect form to be a viable candidate.

While some have found this argument compelling, Urbit's core developers have elected to maintain work in the "main line" of traditional Nock as the system's target ISA. The Nock 4K specification is a good candidate, in this sense, for a "final" version of Nock, as it has been successfully used in production for several years. It seems more likely that subsequent changes to Nock will derive not from alternative representations but from either dramatically more elegant expressions (e.g., of opcode 6 or a combinator refactor) or from an implicit underspecification in the current Nock 4K which should be made explicit.

 $<sup>^{11}\</sup>mbox{Notably},$  Ax (see pp. XX–XX, this volume), skew, and plan (see pp. XX–XX, this volume).

## 5 Conclusion

123/

A13: If you don't completely understand your code and the semantics of all the code it depends on, your code is wrong.

A21: Prefer mechanical simplicity to mathematical simplicity. Often mechanical simplicity and mathematical simplicity go together.

F1: If it's not deterministic, it isn't real.

(~wicdev-wisryt, Urbit Precepts (2020))

Nock began life as a hyper-Turing machine language, a theoretical construct for the purpose of defining higher-level programming languages with appropriate affordances and semantics. While its opcodes and syntax have gradually evolved over the course of two decades, the ambition to uproot the Unix "ball of mud" and replace it with a simple operating function amenable to reason has remained the north star of Urbit and Nock. The history of Nock serves as an index of refinement as Yarvin and contributors sought to balance conciseness, efficiency, and practicality.

The most recent version, Nock 4K, appears to provide all of the opcodes necessary for correct and efficient<sup>12</sup> evaluation. It is likely that future versions of Nock will be based genetically on Nock 4K, but with some changes to improve its performance and usability. The road to zero kelvin is likely very long still, given an abundance of caution, but it also appears to be straight.

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<sup>&</sup>lt;sup>12</sup>Modulo the vagaries of the von Neumann architecture, etc.

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