# **Classification using Logistc Regression**

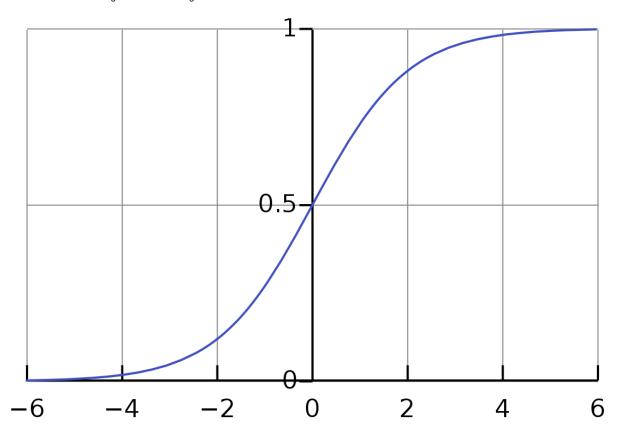
Let X1, X2, ..., Xn be n number of features.

Z = b0 + b1 X1 + ... + bn Xn

 $f(Z) = e^{Z}/(1 + e^{Z}) ....(f(Z))$  always less than 1), (e<sup>Z</sup> always greater than 0)

Therefore, f(Z) lies in between 0 and 1 for every value of Z

Such a function is called the logistic function or Sigmoid function.



f(Z) is the probability

If 0 < f(Z) < 0.5 then Z ==> belongs to the class 0

If 0.5 < F(z) < 1 then Z ==> belongs to the class 1

$$f(Z) = \frac{e^Z}{1 + e^Z}$$

# **Logistic Regression for German Credit platform**

# Sourcing the data

```
In [1]: import numpy as np import pandas as pd import matplotlib.pyplot as plt import seaborn as sns
```

```
In [2]: # Dataset
        gc = pd.read_csv("https://online.stat.psu.edu/onlinecourses/sites/stat508/files/german_credit.csv")
Out[2]:
                                           Payment
                                                                                                                   Duration
                                                                                                                               Most
                                  Duration
                                             Status
                                                                                     Length of
                                                                                                          Sex &
                                                              Credit
                          Account
                                                                             Value
                                                                                               Instalment
                                                                                                                            valuable
                                                                                                                                       Age
                                                                                                                                            Concurrent
              Creditability
                                                    Purpose
                                  of Credit
                                                of
                                                                                       current
                                                                                                         Marital
                          Balance
                                                            Amount
                                                                    Savings/Stocks
                                                                                                per cent
                                                                                                                    Current
                                                                                                                            available
                                                                                                                                                Credits
                                   (month)
                                                                                   employment
                                                                                                         Status
                                                                                                                    address
                                                                                                                               asset
                                             Credit
           0
                                       18
                                                               1049
                                                                                            2
                                                                                                             2
                                                                                                                                        21
                                                                                                                                                     3
           1
                                        9
                                                                                                      2
                                                                                                             3
                                                                                                                         2
                       1
                                1
                                                 4
                                                          0
                                                               2799
                                                                                1
                                                                                            3
                                                                                                                                        36
                                                                                                                                                     3
           2
                               2
                                       12
                                                 2
                                                          9
                                                                841
                                                                                2
                                                                                            4
                                                                                                      2
                                                                                                             2 ...
                                                                                                                         4
                                                                                                                                        23
                                                                                                                                                     3
                                                                                                             3 ...
                                                 4
                                                                                                                         2
           3
                       1
                                1
                                       12
                                                          0
                                                               2122
                                                                                            3
                                                                                                      3
                                                                                                                                  1
                                                                                                                                        39
                                                                                                                                                     3
                                       12
                                                                                            3
                                                                                                                         4
                                                                                                                                  2
                                                                                                                                        38
                                1
                                                 4
                                                          0
                                                               2171
                                                                                1
                                                                                                             3 ...
          995
                       0
                                1
                                       24
                                                 2
                                                          3
                                                               1987
                                                                                1
                                                                                            3
                                                                                                             3 ...
                                                                                                                                  1
                                                                                                                                        21
                                                                                                                                                     3
          996
                                       24
                                                 2
                                                          0
                                                               2303
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                                                                                                              3 ...
                                                                                                                                        45
                                                                                                                                                     3
                                                                                                                                        30
          997
                                       21
                                                          0
                                                              12680
                                                                                                             3 ...
          998
                                       12
                                                          3
                                                               6468
                                                                                                              3 ...
                                                                                                                                        52
                                       30
                                                 2
                                                               6350
                                                                                            5
                                                                                                              3
                                                                                                                                        31
         1000 rows × 21 columns
In [3]: gc.info()
         <class 'pandas.core.frame.DataFrame'>
         RangeIndex: 1000 entries, 0 to 999
         Data columns (total 21 columns):
                                                    Non-Null Count Dtype
              Column
                                                     -----
          0
              Creditability
                                                    1000 non-null
                                                                      int64
              Account Balance
                                                    1000 non-null
                                                                      int64
              Duration of Credit (month)
                                                    1000 non-null
                                                                      int64
              Payment Status of Previous Credit 1000 non-null
          3
                                                                      int64
          4
              Purpose
                                                    1000 non-null
                                                                      int64
          5
              Credit Amount
                                                    1000 non-null
                                                                      int64
              Value Savings/Stocks
                                                    1000 non-null
                                                                      int64
              Length of current employment
                                                    1000 non-null
                                                                      int64
              Instalment per cent
          8
                                                    1000 non-null
                                                                      int64
          9
              Sex & Marital Status
                                                    1000 non-null
                                                                      int64
          10
              Guarantors
                                                    1000 non-null
                                                                      int64
              Duration in Current address
                                                    1000 non-null
                                                                      int64
          12
              Most valuable available asset
                                                    1000 non-null
                                                                      int64
                                                    1000 non-null
          13
              Age (years)
                                                                      int64
          14
              Concurrent Credits
                                                    1000 non-null
                                                                      int64
          15
              Type of apartment
                                                    1000 non-null
                                                                      int64
          16
              No of Credits at this Bank
                                                    1000 non-null
                                                                      int64
                                                    1000 non-null
                                                                      int64
          17
              Occupation
              No of dependents
          18
                                                    1000 non-null
                                                                      int64
          19
              Telephone
                                                    1000 non-null
                                                                      int64
                                                    1000 non-null
                                                                      int64
              Foreign Worker
         dtypes: int64(21)
         memory usage: 164.2 KB
```

# Preprocessing of the data

```
In [4]: # Target
        y = gc['Creditability']
        ٧
Out[4]: 0
               1
               1
        2
               1
        3
               1
        4
               1
        995
               0
        996
               0
        997
               0
        998
               0
        999
        Name: Creditability, Length: 1000, dtype: int64
```

```
In [5]: y.unique() # no. of unique values
 Out[5]: array([1, 0], dtype=int64)
          Only 2 classes ==> Binary Classification
 In [6]: # Features
          X = gc.drop(['Creditability'], axis = 1)
          Х
 Out[6]:
                                  Payment
                                                                                                                    Duration
                                                                                                                                Most
                        Duration
                                    Status
                                                                             Length of
                                                                                                 Sex & 
Marital
                Account
                                                     Credit
                                                                    Value
                                                                                      Instalment
                                                                                                                             valuable
                                                                                                                                        Age
                                                                                                                                             Concurrent
                                          Purpose
                                                                                                        Guarantors
                        of Credit
                                       of
                                                                              current
                Balance
                                                   Amount Savings/Stocks
                                                                                        per cent
                                                                                                                    Current
                                                                                                                            available
                                                                                                                                     (years)
                                                                                                                                                Credits
                         (month)
                                 Previous
                                                                          employment
                                                                                                                    address
                                                                                                                               asset
                                    Credit
             0
                              18
                                                2
                                                      1049
                                                                       1
                                                                                   2
                                                                                                      2
                                                                                                                                   2
                                                                                                                                         21
                                                                                                                                                     3
                               9
                                                                                   3
                                                                                              2
                                                                                                      3
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                                        4
                                                0
                                                      2799
                                                                        1
                                                                                                                                         36
             2
                      2
                              12
                                        2
                                                9
                                                       841
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                                                                                   4
                                                                                              2
                                                                                                      2
                                                                                                                 1
                                                                                                                         4
                                                                                                                                         23
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             3
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                                                      2122
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                              12
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                                                      2171
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                                                                                                                                   2
                                                                                                                                         38
                                                                                                                                                     1
           995
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                                                      1987
                                                                                              2
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                                                                                                                                                     3
                              24
                                                                                   3
                                                                                                                1
                                                                                                                                         21
           996
                              24
                                                0
                                                      2303
                                                                                                                                         45
                              21
                                                0
                                                     12680
                                                                                    5
                                                                                              4
                                                                                                      3
                                                                                                                                         30
                                                                                                                                                     3
                                                3
                                                                                                                                                     3
                                                      6468
                                                                                                                                         52
           999
                              30
                                        2
                                                2
                                                      6350
                                                                                    5
                                                                                                      3
                                                                                                                                         31
                                                                                                                                                     3
          1000 rows × 20 columns
 In [7]: X.shape
 Out[7]: (1000, 20)
 In [8]: X.columns
 Out[8]: Index(['Account Balance', 'Duration of Credit (month)',
                   'Payment Status of Previous Credit', 'Purpose',
                                                                        'Credit Amount',
                  'Value Savings/Stocks', 'Length of current employment',
'Instalment per cent', 'Sex & Marital Status', 'Guarantors'
                   'Duration in Current address', 'Most valuable available asset',
                   'Age (years)', 'Concurrent Credits', 'Type of apartment',
                   'No of Credits at this Bank', 'Occupation', 'No of dependents',
                  'Telephone', 'Foreign Worker'],
                 dtype='object')
 In [9]: category_cols = ['Account Balance', 'Payment Status of Previous Credit',
                              'Purpose', 'Value Savings/Stocks', 'Length of current employment',
                              'Instalment per cent', 'Sex & Marital Status', 'Guarantors',
                              'Duration in Current address', 'Most valuable available asset'
                             'Concurrent Credits', 'Type of apartment', 'No of Credits at this Bank',
                             'Occupation', 'No of dependents', 'Telephone', 'Foreign Worker']
          "Duration of Credit (month)','Credit Amount','Age (years)' are dropped since they are not categorical
In [10]: len(category_cols)
Out[10]: 17
In [11]: # Converting categorical features to numeric
          X_1 = pd.get_dummies(X, columns = category_cols)
In [12]: X_1.shape
Out[12]: (1000, 71)
          columns increased to 71
```

In [13]: # Adding constant import statsmodels.api as sm $X_1 = sm.add_constant(X_1)$ X\_1.shape

C:\Users\Urvi Sharma\anaconda3\lib\site-packages\statsmodels\tsa\tsatools.py:142: FutureWarning: In a future version of pandas all arguments of concat except for the argument 'objs' will be keyword-only

x = pd.concat(x[::order], 1)

Out[13]: (1000, 72)

Out[14]:

In [14]: X\_1

	const	Duration of Credit (month)	Credit Amount	Age (years)	Account Balance_1	Account Balance_2	Account Balance_3	Account Balance_4	Status of Previous	Payment Status of Previous Credit_1	 Occupation_1	Occupation_2	Occupation_3	Occu
0	1.0	18	1049	21	1	0	0	0	0	0	 0	0	1	
1	1.0	9	2799	36	1	0	0	0	0	0	 0	0	1	
2	1.0	12	841	23	0	1	0	0	0	0	 0	1	0	
3	1.0	12	2122	39	1	0	0	0	0	0	 0	1	0	
4	1.0	12	2171	38	1	0	0	0	0	0	 0	1	0	
995	1.0	24	1987	21	1	0	0	0	0	0	 0	1	0	
996	1.0	24	2303	45	1	0	0	0	0	0	 0	0	1	
997	1.0	21	12680	30	0	0	0	1	0	0	 0	0	0	
998	1.0	12	6468	52	0	1	0	0	0	0	 0	0	0	

1000 rows × 72 columns

30

6350

1.0

In [15]: X\_1.iloc[0:10, 0:20]

Out[15]:

	const	Duration of Credit (month)	Credit Amount	Age (years)		Account Balance_2	Account Balance_3		Payment Status of Previous Credit_0	Status of Previous	Status of Previous Credit_2	Status of Previous Credit_3	Status of Previous Credit_4	Purpose_0	Purpose_1 F
0	1.0	18	1049	21	1	0	0	0	0	0	0	0	1	0	0
1	1.0	9	2799	36	1	0	0	0	0	0	0	0	1	1	0
2	1.0	12	841	23	0	1	0	0	0	0	1	0	0	0	0
3	1.0	12	2122	39	1	0	0	0	0	0	0	0	1	1	0
4	1.0	12	2171	38	1	0	0	0	0	0	0	0	1	1	0
5	1.0	10	2241	48	1	0	0	0	0	0	0	0	1	1	0
6	1.0	8	3398	39	1	0	0	0	0	0	0	0	1	1	0
7	1.0	6	1361	40	1	0	0	0	0	0	0	0	1	1	0
8	1.0	18	1098	65	0	0	0	1	0	0	0	0	1	0	0
9	1.0	24	3758	23	0	1	0	0	0	0	1	0	0	0	0
4.1															

```
In [16]: X_1.iloc[0:10, 20:40]
Out[16]:
                                                                                                                                               Length of
                                                                                                                                                             Length
                                                 Value 
Savings/Stocks_1
                                                                              Value
                                                                                                Value
                                                                                                      Value 
Savings/Stocks_4
                                                                                                                                   Value
               Purpose_8 Purpose_9 Purpose_10
                                                                   Savings/Stocks_2
                                                                                     Savings/Stocks_3
                                                                                                                        Savings/Stocks_5
                                                                                                                                          employment 1
                                                                                                                                                        employment
            0
                       0
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In [17]: X_1.iloc[0:10, 40:60]
Out[17]:
                                                                                                                  Most
                                                                                                                           Most
                                                                                                                                     Most
                                                                                                                                               Most
                                                                    Duration
                                                                                          Duration
                                                                                                     Duration
                  Sex &
                                                                                                               valuable
                                                                                                                        valuable
                                                                                                                                  valuable
                                                                                                                                            valuable
                                                                                                                                                     Concurrent
                                                                                                                                                                Cor
                Marital
                        Guarantors_1 Guarantors_2 Guarantors_3
                                                                  in Current
                                                                             in Current
                                                                                        in Current
                                                                                                   in Current
                                                                                                              available
                                                                                                                        available
                                                                                                                                  available
                                                                                                                                           available
                                                                                                                                                       Credits_1
               Status_4
                                                                  address 1
                                                                             address 2
                                                                                        address 3
                                                                                                   address 4
                                                                                                               asset 1
                                                                                                                         asset 2
                                                                                                                                  asset 3
                                                                                                                                            asset 4
            0
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                     n
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In [18]: X_1.iloc[0:10, 60:]
Out[18]:
                 No of
               Credits
                       Credits
                                                                                                No of
                                                                                                              No of
                                                                                                                                                 Foreign
                                                                                                                                                           Foreign
                                Occupation_1 Occupation_2 Occupation_3 Occupation_4
                                                                                                                     Telephone_1 Telephone_2
                at this
                        at this
                                                                                        dependents_1
                                                                                                      dependents_2
                                                                                                                                               Worker_1
                                                                                                                                                         Worker_2
               Bank_3
                       Bank_4
            0
                    0
                             0
                                           0
                                                         0
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                    0
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            2
                    0
                             0
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            3
                    0
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                                                                                                                                                       1
                                                                                                                                                                 0
                                                                                                                                                                 0
           Splitting to training and testing
In [19]: from sklearn.model_selection import train_test_split
           X_train_1, X_test_1, y_train_1, y_test_1 = train_test_split(X_1, y, test_size = 0.2, random_state = 10)
           X_train_1.shape, X_test_1.shape, y_train_1.shape, y_test_1.shape
Out[19]: ((800, 72), (200, 72), (800,), (200,))
```

In [20]: X\_train\_1

```
Out[20]:
                                                                                               Payment Payment
                        Duration
                                                                                                 Status
                                                                                                           Status
                                   Credit
                                                    Account
                                                               Account
                                                                          Account
                                                                                      Account
                                             Age
                       of Credit
(month)
                                                                                                                   ... Occupation_1 Occupation_2 Occupation_3 Occu
                 const
                                                                                                     of
                                                                                                               of
                                 Amount (years) Balance_1 Balance_2 Balance_3 Balance_4
                                                                                               Previous
                                                                                                         Previous
                                                                                                Credit_0
                                                                                                         Credit_1
            188
                   1.0
                                    2273
                                               32
                                                           0
                                                                                 0
                                                                                            0
                                                                                                      0
                                                                                                                0 ...
                                                                                                                                  0
            194
                   1.0
                             12
                                    1262
                                              25
                                                          0
                                                                      0
                                                                                 0
                                                                                                      0
                                                                                                                0 ...
                                                                                                                                  0
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                                                                                                                                                              1
                                                                      0
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            225
                   1.0
                             24
                                    1516
                                               43
                                                           0
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            580
                   1.0
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                                    1546
                                              24
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            428
                   1.0
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                                    1200
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                                    1597
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            320
                   1.0
                             10
                                                                                            1
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                                                          0
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                                                                                                                                 0
            527
                   1.0
                             12
                                    2930
                                              27
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                                                                                                      0
                                                                                                                0 ...
                                                                                                                                                0
                                    2303
                                               45
                                                                      0
                                                                                 0
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            996
                   1.0
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            125
                   1.0
                             24
                                    5103
                                               47
                                                          0
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                                                                                                      0
                                                                                                                0 ...
                                                                                                                                 0
            265
                   1.0
                             22
                                    2675
                                               40
                                                                                                                0 ...
           800 rows × 72 columns
```

#### **Building the model**

```
In [21]: logR_1 = sm.Logit(y_train_1, X_train_1) #Logit function is a part of statsmodels.api
# Fit the model
logR_1 = logR_1.fit()
```

Warning: Maximum number of iterations has been exceeded.

Current function value: 0.434640

Iterations: 35

C:\Users\Urvi Sharma\anaconda3\lib\site-packages\statsmodels\base\model.py:566: ConvergenceWarning: Maximum Likelihood optimiza
tion failed to converge. Check mle\_retvals
warnings.warn("Maximum Likelihood optimization failed to "

# Diagnosing the model

In [22]:	logR_1.summary2(	)							
Out[22]:	Model:	Logit	Pseudo R-s	squared:	0.280				
	Dependent Variable:	Creditability		AIC: 8	05.4233				
	Date:	2022-10-17 12:46		BIC: 10	63.0770				
	No. Observations:	800	Log-Lik	kelihood:	-347.71				
	Df Model:	54		LL-Null:	-482.61				
	Df Residuals:	745	LLR	p-value: 1.9	042e-30				
	Converged:	0.0000		Scale:	1.0000				
	No. Iterations:	35.0000							
			Coef.	Std.Err.	z	P> z	[0.025	0.975]	
		const	-20.3529	nan	nan	nan	nan	nan	
	Duration	of Credit (month)	-0.0245	0.0108	-2.2707	0.0232	-0.0456	-0.0033	
		Credit Amount	-0.0001	0.0001	-2.7644	0.0057	-0.0002	-0.0000	

variables with p value <0.05 are important features

```
In [23]: imp_features = ['Duration of Credit (month)', 'Credit Amount', 'Age (years)']
In [24]: imp_features
```

Out[24]: ['Duration of Credit (month)', 'Credit Amount', 'Age (years)']

```
In [25]: # Update the feature set

X_2 = X_1[imp_features]
```

```
In [26]: X_2
```

Out[26]

:		Duration of Credit (month)	Credit Amount	Age (years)
	0	18	1049	21
	1	9	2799	36
	2	12	841	23
	3	12	2122	39
	4	12	2171	38
	995	24	1987	21
	996	24	2303	45
	997	21	12680	30
	998	12	6468	52
	999	30	6350	31

#### Continue with revised feature set

### **Building the model #2**

 $X_3 = X_2[imp_features_2]$ 

1000 rows × 3 columns

```
In [28]: logR_2 = sm.Logit(y_train_2, X_train_2)
          logR_2 = logR_2.fit()
          logR_2.summary2()
          Optimization terminated successfully.
                     Current function value: 0.574603
                     Iterations 5
Out[28]:
                                                                  0.048
                      Model:
                                       Logit Pseudo R-squared:
           Dependent Variable:
                                  Creditability
                                                        AIC: 925.3648
                       Date: 2022-10-17 12:46
                                                        BIC: 939.4186
             No. Observations:
                                        800
                                                Log-Likelihood:
                                                                 -459.68
                    Df Model:
                                        2
                                                      LL-Null:
                                                                 -482.61
                 Df Residuals:
                                        797
                                                  LLR p-value: 1.0992e-10
                  Converged:
                                      1.0000
                                                       Scale:
                                                                  1.0000
                No. Iterations:
                                      5.0000
                                     Coef. Std.Err.
                                                            P>|z|
                                                                   [0.025
                                                                           0.975]
           Duration of Credit (month) -0.0226 0.0078 -2.8827 0.0039
                                                                  -0.0379
                                                                          -0.0072
                     Credit Amount -0.0001
                                            0.0000 -1.8939 0.0582 -0.0001
                                                                           0.0000
                        Age (years) 0.0452 0.0044 10.2041 0.0000 0.0365 0.0539
In [29]: # Significant features
```

imp\_features\_2 = ['Duration of Credit (month)', 'Age (years)'] # features with p value < 0.05</pre>

In [30]: X\_3

Λı	4	Γ2	a	ı

	Duration of Credit (month)	Age (years)
0	18	21
1	9	36
2	12	23
3	12	39
4	12	38
995	24	21
996	24	45
997	21	30
998	12	52
999	30	31

1000 rows × 2 columns

#### Continue with revised feature set

### Building the model #3

0.044	Pseudo R-squared:	Logit	Model:
926.9100	AIC:	Creditability	Dependent Variable:
936.2792	BIC:	2022-10-17 12:46	Date:
-461.45	Log-Likelihood:	800	No. Observations:
-482.61	LL-Null:	1	Df Model:
7.7598e-11	LLR p-value:	798	Df Residuals:
1.0000	Scale:	1.0000	Converged:
		5.0000	No. Iterations:

```
        Duration of Credit (month)
        -0.0319
        0.0061
        -5.2237
        0.0000
        -0.0439
        -0.0530

        Age (years)
        0.0444
        0.0044
        10.1043
        0.0000
        0.0358
        0.0530
```

Model Building is complete (all p values are less than 0.05, 0 in the last iteration)

#### The final LR Model:

Creditability = Duration of (month) \* -0.031934 + Age (years) \* 0.044396

$$f(Z) = \frac{e^Z}{1 + e^Z}$$

#### Prediction using the model

```
In [34]: y_pred = logR_3.predict(X_test_3)
          y_pred
Out[34]: 841
                 0.690284
                 0.884680
          956
                 0.850290
          544
          173
                 0.657965
                 0.512259
          759
                 0.687278
          274
          192
                 0.385243
                 0.807991
          398
          450
                 0.927365
          520
                 0.523344
          Length: 200, dtype: float64
          These are probabilities
          Creditability of records with probability<0.5 will be 0, for others it will be 1
In [35]: y_test_3
Out[35]: 841
          956
                 0
          544
                 1
          173
                 1
          759
                 0
          274
                 1
          192
                 1
          398
                 1
          450
          520
          Name: Creditability, Length: 200, dtype: int64
In [36]: # Creating a dataframe
          pred_df = pd.DataFrame({'Actual Class':y_test_3,'Predicted Probability':y_pred})
In [37]: | pred_df
Out[37]:
               Actual Class Predicted Probability
           841
                        0
                                     0.690284
                                     0.884680
                        0
           956
           544
                        1
                                     0.850290
                                     0.657965
           173
                        1
           759
                        0
                                     0.512259
           274
                                     0.687278
           192
                                     0.385243
           398
                                     0.807991
           450
                        0
                                     0.927365
                                     0.523344
           520
          200 rows × 2 columns
```

```
In [38]: # Adding a column to the dataframe
pred_df['Predicted Class'] = pred_df['Predicted Probability'].map(lambda x: 1 if x>0.5 else 0)
pred_df
```

Out[38]: Actual Class Predicted Probability Predicted Class 0 0.690284 956 0.884680 544 1 0.850290 173 1 0.657965 759 0 0.512259 1 274 0.687278 1 192 0.385243 0 1 398 0.807991 0 0.927365 450 1 0 0.523344 1 520

200 rows × 3 columns

#### Performance measures

```
Sensitivity = P(Preditcted Class= +ve/Actual Class= +ve) = TP/(TP + FN)

Specificity = P(Preditcted Class= -ve/Actual Class= -ve) = TN/(FP + TN)

Precision = P(Actual Class= +ve/Predictive Class= +ve) = TP/(TP + FP)

F1 Score = HM(Recall, Precision)

Accuracy = (TP + TN)/N....(N -> Total number of data points)
```

This the 2nd row of confusion matrix correctly classifies

# **Confusion matrix**

#### **Classification Report**

```
In [40]: from sklearn.metrics import classification_report # performance measures not needed to be calculated manually by using the fomula
report = classification_report(pred_df['Actual Class'], pred_df['Predicted Class'])
print('The classification report:\n', report)
```

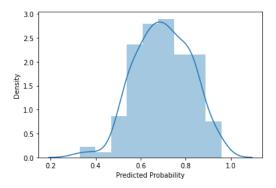
The classification	ation report:			
	precision	recall	f1-score	support
0	0.79	0.16	0.27	67
1	0.70	0.98	0.82	133
accuracy			0.70	200
macro avg	0.74	0.57	0.54	200
weighted avg	0.73	0.70	0.63	200

# Plotting the distribution of predicted probabilities

```
In [46]: # Distribution of pred prob corresponding class = 1
sns.distplot(pred_df[pred_df['Actual Class']==1]['Predicted Probability']);
```

C:\Users\Urvi Sharma\anaconda3\lib\site-packages\seaborn\distributions.py:2619: FutureWarning: `distplot` is a deprecated funct ion and will be removed in a future version. Please adapt your code to use either `displot` (a figure-level function with simil ar flexibility) or `histplot` (an axes-level function for histograms).

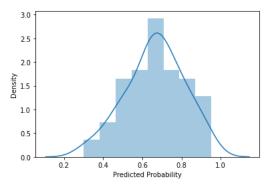
warnings.warn(msg, FutureWarning)



```
In [47]: sns.distplot(pred_df[pred_df['Actual Class']==0]['Predicted Probability']);
```

C:\Users\Urvi Sharma\anaconda3\lib\site-packages\seaborn\distributions.py:2619: FutureWarning: `distplot` is a deprecated funct ion and will be removed in a future version. Please adapt your code to use either `displot` (a figure-level function with simil ar flexibility) or `histplot` (an axes-level function for histograms).

warnings.warn(msg, FutureWarning)

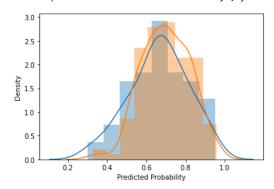


```
In [48]: sns.distplot(pred_df[pred_df['Actual Class']==0]['Predicted Probability'])
         sns.distplot(pred_df[pred_df['Actual Class']==1]['Predicted Probability'])
```

 $\verb| C:\Users\Urvi Sharma\anaconda3\lib\site-packages\seaborn\distributions.py: 2619: Future Warning: `distplot` is a deprecated function of the packages of$ ion and will be removed in a future version. Please adapt your code to use either `displot` (a figure-level function with simil ar flexibility) or `histplot` (an axes-level function for histograms). warnings.warn(msg, FutureWarning)

 $\textbf{C:} \\ \textbf{Users} \\ \textbf{Urvi Sharma} \\ \textbf{anaconda3} \\ \textbf{lib} \\ \textbf{site-packages} \\ \textbf{seaborn} \\ \textbf{distributions.py:} \\ \textbf{2619: FutureWarning: `distplot` is a deprecated functional formula for the property of the property of$ ion and will be removed in a future version. Please adapt your code to use either `displot` (a figure-level function with simil ar flexibility) or `histplot` (an axes-level function for histograms). warnings.warn(msg, FutureWarning)

Out[48]: <AxesSubplot:xlabel='Predicted Probability', ylabel='Density'>



### **ROC Curve**

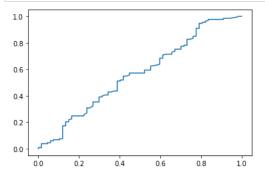
Receiver Operating Charateristics Curve

Plotted by taking:

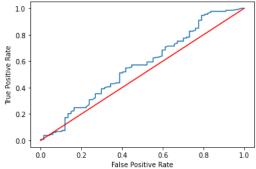
FPR(Sensitivity) ===> X-axis

TPR(1-Specificity) ===> Y-axis

```
In [49]: from sklearn.metrics import roc_curve
         fpr, tpr, threshold = roc_curve(pred_df['Actual Class'],
                                         pred_df['Predicted Probability'])
         plt.plot(fpr, tpr);
```



```
In [50]: plt.plot(fpr,tpr)
                plt.plot([0,1],[0,1],c='r')
plt.xlabel('False Positive Rate')
plt.ylabel('True Positive Rate')
                 plt.show();
```



# **ROC-AUC Curve**

```
In [51]: from sklearn.metrics import roc_auc_score
         score=roc_auc_score(pred_df['Actual Class'],
                            pred_df['Predicted Class'])
         print('The ROC-AUC-Score:',score)
```

The ROC-AUC-Score: 0.5708113567500841

# Finding the optimum classification cut-off

Many measures:

```
Youden's index : Max { Sensitivity + Specificity - 1}
                : Max { Sensitivity - (1 - Specificity)}
               : Max { FPR - TPR}, actual diff
```

```
In [53]: # Creating a new DF
         fpr_tpr = pd.DataFrame({'FPR': fpr,
                                'TPR': tpr,
                                 'Threshold':threshold})
```

In [54]: fpr\_tpr

Out[54]:

	FPR	TPR	Threshold
0	0.000000	0.000000	1.958436
1	0.000000	0.007519	0.958436
2	0.014925	0.007519	0.952478
3	0.014925	0.037594	0.928304
4	0.044776	0.037594	0.920128
102	0.910448	0.984962	0.460934
103	0.940299	0.984962	0.421208
104	0.970149	0.992481	0.385243
105	0.985075	1.000000	0.327971
106	1.000000	1.000000	0.299315

107 rows × 3 columns

```
In [55]: # creating the col of Diff
          fpr_tpr['Diff']=fpr_tpr['FPR']-fpr_tpr['TPR']
          fpr_tpr
Out[55]:
                   FPR
                            TPR Threshold
                                                Diff
             0 0.000000 0.000000
                                  1.958436
             1 0.000000 0.007519
                                  0.958436 -0.007519
             2 0.014925 0.007519
                                  0.952478
                                           0.007407
             3 0.014925 0.037594
                                  0.928304 -0.022669
             4 0.044776 0.037594
                                  0.920128 0.007182
           102 0.910448 0.984962
                                  0.460934 -0.074515
                                  0.421208 -0.044664
           103 0.940299 0.984962
           104 0.970149 0.992481
                                  0.385243 -0.022332
           105 0.985075 1.000000
                                  0.327971 -0.014925
           106 1.000000 1.000000 0.299315 0.000000
          107 rows × 4 columns
In [56]: #Sorting
          fpr_tpr.sort_values('Diff',ascending=False)
Out[56]:
                   FPR
                            TPR Threshold
            12 0.119403 0.075188
                                  0.866104 0.044215
            10 0.104478 0.067669
                                  0.877585 0.036808
            11 0.104478 0.075188
                                  0.872735 0.029290
             6 0.059701 0.045113
                                  0.895420 0.014589
             8 0.074627 0.060150
                                  0.884680 0.014476
            98 0.820896 0.962406 0.513231 -0.141510
           100 0.835821 0.977444
                                  0.504669 -0.141623
            93 0.791045 0.939850
                                  0.527421 -0.148805
            96 0.805970 0.954887
                                  0.521594 -0.148917
            94 0.791045 0.947368
                                  0.526841 -0.156324
          107 rows × 4 columns
          The threshold which provides the maximum DIFF is: 0.526841
In [59]: # Use the new cut-off
          pred_df['New Predicted Class'] = pred_df['Predicted Probability'].map(lambda x: 1 if x>0.526841 else 0)
In [60]: pred_df
Out[60]:
                Actual Class Predicted Probability Predicted Class New Predicted Class
           841
                         0
                                      0.690284
                         0
                                                           1
           956
                                      0.884680
                                                                              1
                         1
           544
                                      0.850290
           173
                         1
                                      0.657965
                                                           1
           759
                         0
                                                           1
                                                                              0
                                      0.512259
           274
                                      0.687278
                                                                              1
           192
                                      0.385243
           398
                                      0.807991
           450
                         0
                                      0.927365
           520
                                      0.523344
                                                                              0
          200 rows × 4 columns
```

```
In [64]: # New confusion matrix
        print("The new CM:\n", new_cm)
        The new CM:
[[ 14 53]
[ 8 125]]
In [66]: new_score = roc_auc_score(pred_df['Actual Class'],
                          pred_df['New Predicted Class'])
        print('The new score:', new_score)
        The new score: 0.5744024239703737
        The mode has slightly improved, not substantially
 In [ ]:
```