A diff eg of the form Mdn+Ndy = 0 is said to be non-enact Non Exact Digg Eg Now if this diff of is multiplied by affunction; then the resulting eq is Exact Dygleg. This suitable for is called Jutyrating then the resulting eq is Exact Dygleg. This suitable for is called Jutyrating Note The number of Integrating Factors may be infinite. Some Rules to Find Integrating Factors

Mdx +Ndy = 0 is not exact then find Integrating Factor using 1)  $\frac{My-Nx}{N} = p$  then  $I \cdot F = e$ where a is for & y alone 2)  $\frac{Ne^{-My}}{M} = Q$  then  $I \cdot F = e$ where xM+YN =0 3) of Mdn+Ndy=0 is Homogeneous them I.F = 2M+YN 4) of different the form y.f(xy) dn+x.g(xy) dy=0 then I.F= 1/2M-YN where xM-4N/20 Note In some cases I. F can be found only after properly regrouping the terms of a diff of and then recognising each group as an Enact differential 1) xdy+ydn=d(xy)Available at ww.mathcity.org 2) 2 dy - Ydy = d(4) ·3) Ydn - rdy = d(3) 4)  $xdu + ydy = d(x^2+y^2)$ 5) x dy + y dx = d(log(xy))2 dy - ydn = d (tan 4) ydn - ndy = d (tam 4) ·8) ndy + ydn = d(- /y)

Sulme by finding an I.F

$$0 (xy^2+y)dx - xdy = 0 - 0$$

$$M = xy^2+y \qquad N = -x$$

$$My = 2xy+1 \qquad N_x = -1$$

$$My \neq Nx \qquad Non Exact$$

$$\frac{My-Nx}{N} = \frac{2xy+1+1}{-x} \qquad Not find x alow.$$

$$\frac{Nx-My}{M} = \frac{-1-2xy-1}{-xy^2+y} = -\frac{2}{y}$$

$$\frac{(1+xy)}{M} = -\frac{2}{y} \qquad Fn gy alow$$

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j(x+4)du + Nil = C

2 + 2 = C

(3) 
$$(x^2+x-y)dx + x dy = 0$$
 $M = x^2+x-y$ 
 $N = x$ 
 $M_y = -1$ 
 $M_y = N_x$ 
 $N = -1$ 
 $N_y = N_x$ 
 $N_y = N_y$ 
 $N_y =$ 

## (43) (9) dy+(4-sinx)dn =0-0 $M = \frac{Y - Sin \cdot X}{2I} \qquad N = 1$ $M_{Y} = \frac{1}{2} - 0 \qquad N_{Z} = 0$ My + Nn: Dis Nom Exact Diglia Now M-Nx = \frac{1}{2-0} - \frac{1}{2} m8x I.F = by = lnx = M Multiplying both sides g = D by I.F=X zdy +x(4-sinx)dx =0-0 M = Y - Sim x N = x $N_x = 1$ $N_x = 1$ $M_{\gamma} = 1$ My = Nx :: 11 is Exact Diffl Eq. Indu + Items of N free from x) dy = C J(y-sinn)dn = C xy+Cosx = C @ (y4+24)dn + (xy3+2y4-4x)dy=0-0 $M = y^4 + 2y$ $N = xy^3 + 2y^4 - 4x$ $N_x = y^3 - 4$ $N_x = y^3 - 4$ My + Nx : Dis Non Exact Digleg. $\frac{N_x - M_Y}{M} = \frac{y^3 - 4 - 4y^3 - 2}{y^4 + 2y} = \frac{-3y^3 - 6}{y(y^3 + 2)} = \frac{-3}{y}$ $\frac{x^{6}y^{3}}{y^{3}}(y^{4}+2y)dx + \frac{1}{y^{3}}(xy^{3}+2y^{4}-4x)dy = 0$ (Y+==)dn+(x+2Y-4x)dy===0=1 N= x+27- 47 Now M= 4+2 $M_{\gamma} = 1 - \frac{4}{7}$ $N_{\chi} = 1 + 0 - \frac{4}{7}$

9-202000 (2xy+exy)dn-ezdy =0-0  $M = 2xy + e^{x}y$   $N = -e^{x}$   $N_{y} = 4xy + e^{x}$   $N_{x} = -e^{x}$ My + Nx : Ois Hon Exact Dylleq. My-Nx = 4xy+ex+ex Notfor 3x alone  $\frac{N_{x}-M_{y}}{M}=-\frac{e^{2}-4xy-e^{2}}{2xy^{2}+ye^{2}}=\frac{-2e^{2}-4xy}{y(2xy+e^{2})}$ = -2(ex+2xy) = -2 7(2x4+e") mgyalom  $I.F = e = e = e^{-\frac{2}{7}dY} - \frac{1}{2}lny = \frac{1}{4}ny^{2} = \frac{1}{4}$ Multiply both sides of by I.F= 1/2 +2(2xy+ey)dn - +2 edy =0  $(2x + \frac{e^7}{y})dx - \frac{e^x}{y^2}dy = 0$ N=-&1  $M = 2x + \frac{e^{x}}{y_{1}}$   $M_{y} = 0 + \left(-\frac{e^{x}}{y_{2}}\right)$   $N = -\frac{e^{x}}{y_{2}}$   $N_{x} = -\frac{e^{x}}{y_{2}}$ My = Nx = @ is Exact Digley. SMdn + S(terms of N free from x) dy = =  $\int (2x + e^{x}) dn + Nil = C$ 2+== Ams. -> · My = Nx . 1 is Exact Dypl By. [Mdn+ (terms of N free from x) dy = c  $\int \left(\gamma + \frac{2}{\gamma^2}\right) dn + \int 2\gamma d\gamma = C$ 24+2x+2y= = C  $xy+\frac{2x}{y^2}+y^2=0$ 

Si Econ 2 d Method on Page in) (8) (x+y-)dn -2xydy =0-0 1 (x2+42+2x) dn + 24 dy = 0-0 N=-2xy  $M = \chi^2 M^2$   $N = -2\chi^2$   $M_{\gamma} = 2\gamma$   $N_{\gamma} = -2\gamma$ M=2+4+2x N=24 My + Nx .: O in Non Exact Diglig My = 27 Nx=0 My + Nx : Dis Non Exact Diggleg  $\frac{N_{x}-My}{M}=\frac{-2y-2y}{x^{2}+y^{2}}$  Notingly Nx-My = 0-27 Not by 370mly  $\frac{M_{Y}-N_{X}}{N} = \frac{2Y+2Y}{-2xy} = \frac{4Y}{-2xy} = \frac{-2}{x}$  $\frac{M_1-N_2}{N}=\frac{2\gamma-0}{2\gamma}=1=\chi \ \text{for } \delta x \text{ only}$  $IF = e^{\int \frac{-2}{x} dx} -2 \ln x = \ln x^{2} = x^{2} = x^{2}$ I.F = e = e Multiply both sides of eq ( by I.F= [2] Multiply both sides of eq ( by I.F = 1 大(x++)か一年(2xy)dy=0 e'(x++++2x)du+ e'(2Y)dy =0 -1 (1+ y) dn - 24 dy= -0  $M = e^{(x^{2}+y^{2}+2x)}$   $N = e^{2}2y$   $M_{y} = e^{2}2y$   $N_{x} = e^{2}2y$  $M = \frac{2}{1+\frac{1}{2}}$   $N = -\frac{2}{2}$   $M_{y} = \frac{2}{2}$   $N_{x} = +\frac{2}{2}$   $N_{x} = +\frac{2}{2}$ My = Nx : @ is Exact DifflEq. = JMdn+ Sterms on free from x) dy = c My = Nx : 1 is Exact Diggleq. "JAdn+ Sterms of N free from re)dy = c Je.(x+y+2x)dn + Nil = C Sex dx+Jeydn+Je2x.dn =C [(1+4)dn+ Nil = C  $x-\frac{y^2}{x} = c$  Ass. z' e-jaxa du + e' j + je/xdr.=c Note 8 can be done by I.F= XM+YN Nothad. (x+y)ex =e :IF= ex = e = e = x 1. (4x+3y) du +2xy dy =0-0 Multiply both sides of Oby I.F=[x]  $M = 4x + 3y^2$  N = 2xy  $M_y = 0 + 6y$   $N_x = 2y$ (4x+3y2)dx+ (2xy)dy =0 -0  $M = 6yx^2$   $N_x = 6x^2y$   $M_y = N_x$   $Dis \in xact DigH Eq.$ My = 0+ by Ny + Nx in Non Exact Dig Eq : JMdn+ Sterms & N free from x) dy=c  $\frac{N_x - M_y}{M} = \frac{2y - 6y}{4x + 3y^2}$  not for  $\frac{9}{3}$  alone (4x+3y2x)dn + Nil = C  $\frac{M_{\gamma}-N_{\gamma}}{N}=\frac{6\gamma-2\gamma}{9\chi\gamma}=\frac{4\gamma}{2\chi\gamma}=\frac{2}{\chi}$  $4x^{\frac{4}{3}} + 37x^{\frac{3}{2}} = 0$   $x^{\frac{4}{3}} + 47x^{\frac{3}{2}} = 0$   $x^{\frac{4}{3}} + 47x^{\frac{3}{2}} = 0$ Aus

(2) (3xy + 2xy)dn + (2xy-x)dy =0-0 (9) dy = e + y-1  $dy = (e^{2\gamma} + \gamma - 1) dn$ M=3xy+2my N=2xy-x (e2x+y-1)dn-dy=0-0  $M_{y} = 12x_{y}^{2} + 2x$   $N_{x} = 6x_{y}^{2} - 2x$ M=2x+Y-1 N=-1 My + Nx :: 1) is Non Exact Digfl Eq  $M_y = 1$ My + Nx : O is Non Exact Diff &  $\frac{M_{y}-N_{x}}{N} = \frac{12x_{y}^{2}+2x_{y}-6x_{y}^{2}-2x_{y}^{2}}{2x_{y}^{3}-x_{y}^{2}-x_{y}^{2}} = \frac{6x_{y}^{2}}{x^{2}(2x_{y}^{2}-1)}$ Nx-My = a-1 Hotting  $\frac{Nz - My}{M} = \frac{6\pi y^{3} - 2x - 12\pi y^{3} - 2x}{3\pi^{2}y^{4} + 2xy} = \frac{-6\pi y^{3} - 4x}{\pi y(3\pi y^{2} + 2)}$  $\frac{M_{Y}-N_{X}}{N} = \frac{1-0}{-1} = -1 = -x^{2} \int_{0}^{\infty} b^{x}$  $= -\frac{2}{2} \frac{1}{3} \frac{3}{3} \frac{1}{4^{2}} = -\frac{2}{7} \frac{1}{7} \frac{1}{8}$   $= -\frac{2}{7} \frac{1}{3} \frac{3}{7} \frac{1}{4^{2}} = -\frac{2}{7} \frac{1}{7} \frac{1}{8}$   $= -\frac{2}{7} \frac{1}{3} \frac{1}{7} \frac{1}{4^{2}} = -\frac{2}{7} \frac{1}{7} \frac{1}{8}$ : I.F = e = [e] Multiply both sides of ego laye ex(=+4-1)dn-=xdy -0 Multiply both sides of eg (1) by I.F = fr (e+ey-e)du-edy=>-1 J. (327 + 2ny) dn + / (227 - x) dy =0  $M = e^{\chi - \chi} y^{-2\chi}$   $N = e^{-\chi}$  $(3x^{2}y^{2} + 2x)dx + (2xy - x^{2}y^{2})dy = 0 - 11$  $M_y = e^{x}$   $N_x = +e^{x}$  $M = 3x^{2}y^{2} + \frac{2x}{y}$   $N = 2x^{2}y - \frac{x}{y}$ My = Nx: 10 is Exact Diggl &y  $M_{y} = 6x^{2}y - \frac{2x}{y^{2}}$   $N_{x} = 6x^{2}y - \frac{2x}{y^{2}}$ 20 Mdn + Sterms & N gree from x) dy=c My = Nx : Dis Exact Dipley. J(e +e y-e)dn+ Nil = C :. JMdn + Sterms of N free from x)dy = C e -ey+e = c  $\int (3x^2y^2 + 2x^2y^2) dx + Nil = C$ 3xy++x = C

Easy Melhealer Panelis (1) (3xy+y)dn + (x2+xy)dy=0-0 (3) (4+x4)du-xdy = 0-0 M= 3xy+y = N= = = +xy  $M = y^2 + xy$   $N = -x^2$  $M_{y} = 3x + 2y$   $N_{x} = 2x + y$  $M_y = 2y + x$   $N_x = -2x$ My + Nx : Ois Non Exact Digol Eg My + No .: O is Non Exold Dight &  $\frac{N_{x-}My}{M} = \frac{2x+y-3x+2y}{3x+4y} = -\frac{x+3y}{y(3x+1)} \frac{N_{x+}}{y(3x+1)} \frac{N_{x+}}{$  $\frac{M_{y}-N_{x}}{N}=\frac{2y+x+lx}{-x^{l}}$  Noting x  $\frac{M_{y}-N_{x}}{N} = \frac{3x+2y-2x+y}{x^{2}+ny} = \frac{(x+y)-1}{x(x+y)} = \frac{1}{x} \log \frac{1}{x^{2}}$ Mx-My = -2x-2y-x Nitgagy J.F = e = e = X Dio Honogeneous diff og of degree 2. : XM+YN= XY+xx+(4xx) Multiply both indes of eag Dby IF = X I.F = TM+YN = Tyy-(3xxy+xy2) dn + (x3+x24) dy =0-0 Multiply both sides 30 by I.F. I.  $M = 3x^2y + xy^2$   $N = x^2 + x^2y$ 1 (y'+xy)dn - + x'dy=0  $M_{y} = 3x^{2} + 2xy$   $N_{x} = 3x^{2} + 2xy$ (+++)du - x dy = 00 My = Nn : Dis Exact Diffleq. M= ++ N=---" [Mdn + [tems of N free from n) dy = c [(3xy+xy)du+ Nil =c My = Nx : Dio Exact Diffe 3 x y + x y = c : JMdx + J (termy N free from x) dy = C 27 + 27 = c As. [( ++ ) du + Nil = C mx + 2 = e Ans. अह अह अह- अह-

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(B) ydn + (2xy-e)dy =0-0 1) (3xy+2my+y3)dn+(n+y2)dy=0-0 M=7 N=224-e M=3xy+2m+y3 N= x2m2 Nx=27  $M_{y} = 3x^{2} + 2x + 3y^{2}$   $N_{x} = 2x$ My + Nx Dis Non Exact Dys Eg My + Nx : Dis Non Exact Digg Eq.  $\frac{M_y - N_x}{N} = \frac{1 - 2\gamma}{2m_y - \epsilon^2}$  Not for gradone  $\frac{M_{4}-N_{2}}{N}=\frac{3x^{2}+3x^{2}-3x}{x^{2}+3}$  $\frac{N_{\chi}-M_{\gamma}}{M} = \frac{2\gamma-1}{\gamma} = 2-\frac{1}{\gamma} b^{-8\gamma alang}$  $= 3 \left( \frac{\chi^{2} + y^{2}}{\chi^{2} + y^{2}} \right) = 3 = 3 \chi^{2}$   $= 3 \left( \frac{\chi^{2} + y^{2}}{\chi^{2} + y^{2}} \right) = 3 = 3 \chi^{2}$   $= 3 \left( \frac{\chi^{2} + y^{2}}{\chi^{2} + y^{2}} \right) = 3 = 3 \chi^{2}$ I.F = e (2-4) 4  $= e^{2\gamma + \ln \gamma} = e^{2\gamma} \ln \left(\frac{1}{\gamma}\right) = e^{2\gamma} \frac{1}{2\gamma}$  $I.F = e = \begin{bmatrix} 3x \\ e \end{bmatrix}$ Multiply both sides of They I:F= ex Multiply Dby I.F= 24.4 2/ ydn + e' + (2m-e')dy=0 (3xye + 2xye + ye) du + (ex+ex) dy=0 M=3xyc +2xyc +ye N=ex+ey e du + (e 2x - +) dy = 0 - 1 M = 322 +2xe +3ye N=36 z+e2x+63y N=242x-1 M = 24  $M_{\gamma} = 2e^{2\gamma}$   $N_{z} = 2e^{\gamma} - 0$ My = Nx : 1 is Exact Diggl & . My = Nx : Q is Exact Diffley JMdn+Sterms of N free from x) dy = C · JMdn+ Sterms & N free from x) dj = C , Janye + 224 + yer) dn + Nil = C ,37/ 22 dn + 24/xe dn + y /e dn - C = | e dn + (-+ dy = C )34 (x e - 12x e dn) +24 (xe + y = = c => xL - ly = C => xqe -2y|xedn+2y|xe+qe=c 是 新年 新春 => xye + y<sup>3</sup> = c 

(19) edu + (e) (aty + 27 cosicy) dy = 0 -0  $M = e^{x}$   $N = e^{x}$  Cosec y M = O  $N = e^{x}$   $N = e^{x}$ My + Nx : O is Non Exact Diff  $\frac{N_{y}-N_{x}}{N} = \frac{o-e^{x}\cot y}{\sum_{c}\cot y+2y\cos cy}$  Not july x ordone Nn-My = ecoty -0 = coty by gyalone :I.F = e = e = [Simy] Multiply both sides 30 by I.F = Siny Sing edn + (Sing e City + 27 Sing Cosecy) dy = 0 Sing 2 du + (2 Cosy + 27) dy =0 M = Sinye N= @Cos y+27 M = Cosye N= e Cosy +0 My = Nx : @ is Exact Diggl 9 " JMdn + Stems of N free from n) dy = C Jesiny du + Jzydy = c. 2 Siny + 29 = c 2 Sing + 72 = c

(1) (n+2) Siny du + n (osy dy =00 M= (4+2) Siny N-2 Cosy My = (x+2) Cosy Nx = Cosy My + Nx : Dis Alon Exact  $\frac{N_x - My}{M} = \frac{Cosy - (x+2)Cosy}{(x+2)Siry} + \frac{1}{6}y$ My-Nx = (x+2)Coby-Coby =((x+2) - 1) Gody = x+1 My-Nx = 1+1 fugicalore I.F = e = e - e a Multiply by xc on both sides go xe (x+2) Sing du + xe x Cosydy = 0 M=xe(x+2) siny, N=xe Cosy M = (xex + 2xe) suy, Nx = (xex+xex) (ay My=(x2+2x2) cosy My = Nx : (1) is Exact Diff Eq. : JMdn+ S(tems & N free from x) dy = C Jorg Siny + 2xesindex + Nil = C Jze Sinydx + 2xe Sinydn = C x e Siny - 12xe siny dx +j2n 2 Sinydx x2e Siny = C

Matter or forms.

3) 
$$Y-x \frac{dy}{dx} = x+y \frac{dy}{dx}$$
 $x-y+(x+y) \frac{dy}{dx} = 0$ 
 $(x-y)dx + (x+y)dy = 0$ 
 $(x-y)dx + (x+y)dy = 0$ 
 $x=1+0$ 
 $x=1+0$ 

(49) (6) (3xy+y2) dn + (x2+ my) dy = 0  $\frac{dy}{dn} = -\frac{(3ny + y^2)}{x^2 + xy} - 0$ Put Y=Vn — (11)

dy = V+ndv — (11) Put 10 × 100 in 19  $v + x \frac{dv}{dx} = \frac{1}{3} \frac{(3 + v^2 + v^2 + v^2)}{x^2 + x^2 v}$  $x dv = -x^{2} \frac{(3v+v^{2})}{x^{2}(1+v)} - y$  $= -\frac{3 \vee - \vee^2 - \vee (1 + \vee)}{1 + \vee}$  $2 \frac{dv}{dx} = -\frac{4v-2v}{1+v}$  $\pi dv = -2\left(2\frac{V+V^{2}}{1+V}\right)$  $\left(\frac{1+v}{2v+v^2}dv\right) = -2\left(\frac{du}{2v}\right)$  separating Variables  $\frac{1}{2} \int \frac{(2+2\nu)}{2\nu+\nu^2} d\nu = -2 \frac{1}{2} \frac{1}{2\nu}$ 1 ln(2V+V2) = -2lnx + lnc ln(2V+V)= ln x2 + lnc  $\ln(2V+V) = \ln(\kappa x^2)$ 12V+V2 = C Squig  $2V+V^2 = \frac{c^2}{x^4}$  $\begin{array}{rcl} V(2 \downarrow V) & = & \frac{C^2}{X^4} \\ \frac{V}{X}(2 + \frac{V}{X}) & = & \frac{C^2}{X^4} \end{array}$  $4 y(2x+y) = c^2$ 対(2 スダナイ) = で 2 x 1 + x y = c Ans

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(49) Lary Melled and agrade 3 Y-x = x+y # x-y+(x+y) dy =0 (x-4)dn + (x+4)dy = 0 -0 M=x-4 M=0-1 N=1+0 M = 0-1  $\frac{M_y - N_x}{N} = \frac{-1 - 1}{x + y}$  Noting xalone Nx-My = 1+1. Notforg yalon : Dis Homogeneous So I.F= 1 xM+YN I.F = 1 = x(x-y)+Y(++y) = x-xy+xy+y Multiply Oby I.F = 1 x2+72  $\frac{(x-1)}{x^2+y^2}dx + \frac{(z+1)}{x^2+y^2}dy - 1$ M = (x+y)(-1) - (x-y)(2y), N = (x+y) - (x+y) - x  $(x+y)^{2}$   $(x+y)^{2}$  $M_{y} = -\frac{x^{2}+y^{2}-2xy+2y^{2}}{(x^{2}+y^{2})^{2}}, N_{x} = \frac{x^{2}+y^{2}-2x^{2}-2xy}{(x^{2}+y^{2})^{2}}$  $M_{y} = + \frac{y^{2} - x^{2} - 2xy}{(x^{2} + y^{2})^{2}}$   $N_{x} = \frac{y^{2} - x^{2} - 2xy}{(x^{2} + y^{2})^{2}}$ My=Nx : (1) is Exact Diff & · Mdn + Sterms & N free from x) dy = C  $\int \frac{(x-1)}{(x+1)} dx + Nil ; = C$ 1 2 du - 1 7 du x2+42

 $\int \frac{1}{x^{\frac{1}{4}}} \frac{1}{x^{\frac{1}{4}}} - \int \frac{1}{x^{\frac{1}{4}}} \frac{1}{x^{\frac{1}{4}}} = e \quad \left( \frac{1}{x^{\frac{1}{4}}} \frac{1}{x^{\frac{1}{4}}} - \frac{1}{x^{\frac{1}{4}}} \frac{1}{x^{\frac{1}{4}}} \right)$ 

+ lu(x++) - tan +

(5) (y+my)du-ndy =0-0  $M=y^2+xy$   $N=-x^2$ My = 27+7 My +Nx :Dionat Exact Diffley.  $\frac{My-Nx}{N} = \frac{2y+x+2x}{-x^2}$  Not for gradom  $\frac{N_{x}-M_{y}}{M}=\frac{-2x-2y-x}{y^{2}+xy}$  Not for gyalone. Dis Homogeneous diffeq of degree 5 Multiply both sides of by I.F = 1  $\frac{1}{xy^2}(y^2+xy)dn-\frac{1}{xy^2}x^2dy=0$ (+++)dn - 72 dy =0 -0  $M = \frac{1}{2} + \frac{1}{2}$   $M_{y} = -\frac{1}{2}$   $N_{z} = -\frac{1}{2}$   $N_{z} = -\frac{1}{2}$ N = -3, .. My = Nx : (1) is Exact Diff Eg. .. Judn + Sterms of N free from x) dy=C  $\int (\frac{1}{2} + \frac{1}{4}) dn + Nil = c$ 

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@9 (34+4x4) oh + (2x+2x4) dy =0-0  $M_{Y} = 3 + 8 \pi y$   $N_{X} = 2 + 6 \pi y$ My + Nx . Dio Non Exact.  $\frac{M_{Y}-N_{X}}{N}=\frac{3+8m_{Y}-2-6\pi y}{2x+3\pi^{2}y}=\frac{1+2m_{Y}}{\pi(2+3m_{Y})}$  $\frac{N_{\chi}-M_{\gamma}}{M} = \frac{2+6m_{\gamma}-3-8m_{\gamma}}{3\gamma+4m_{\gamma}} = \frac{-1-2m_{\gamma}}{\gamma(3+4m_{\gamma})}$ E, D is not Homogeneous ego is of the form y f(xy) dn+ x g(xy)dy=0 :. 1 is y (3+4xy)dn +x (2+3xy)dy=0 S. I.F = 1 xM-YN = 3xy+4xy-2xy-3xy xy+xy Multiply both sides of ego by I.F = 1 xy+xxy : (34+4xy²) dn + (2x+3x²y) dy = 0 (xy+x²y²) (xy+x²y²)  $\frac{x[3+4xy]}{x[x+x^2y]}dx + \frac{x[2+3xy]}{x[y+2y^2]}dy = 0$  $M_{\gamma} = \frac{(\chi + \chi^2 \gamma)(4\chi) - (3 + 4\chi \gamma)(\chi^2)}{(\chi + \chi^2 \gamma)^2}$  $=4x^{2}+4y^{2}y-3x^{2}-4x^{2}y^{2}+2x^{2}+2x^{2}y^{2}+2x^{2}+2x^{2}y^{2}+2x^{2}+2x^{2}+2x^{2}+2x^{2}+2x^{2}+2x^{2}+2x^{2}+2x^{2}+2x^{2}+$  $N_{x} = (1+xy^{2})(3y) - (2+3xy)(y^{2})$  $= \frac{3y^{2} + 3xy^{3} - 2y^{2} - 3xy^{3}}{(y + xy^{2})^{2}} = \frac{y^{2}}{x^{2}(1+xy^{2})}$ My=Nx: (1) is Exact Digster.

$$\int M dn + \int [terms BN free from X] dy = C$$

$$\int \left(\frac{3+4xy}{x_1+x_2y}\right) dn + \int \frac{2}{y} dy = C$$

$$\int \frac{(3+3xy+xy)}{x_1(1+xy)} dx + \int \frac{2}{y} dy = C$$

$$\int \frac{(3+3xy+xy)}{x_1(1+xy)} dx + \int \frac{2}{y} dy = C$$

$$\int \frac{(3+3xy+xy)}{x_1(1+xy)} dx + \int \frac{2}{y} dy = C$$

$$3\int \frac{d^{2}+\int \frac{1}{1+xy}}{x^{2}+x^{2}} dx + \int \frac{2}{y} dy = C$$

$$3\ln x + \ln(1+xy) + 2\ln y = C$$

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$$\ln x^{2}(1+xy)y^{2} = \ln e^{C}$$

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(5)

$$\frac{M_{y}-N_{x}}{N}=\frac{1-2\pi y-1-2\pi y^{2}}{\pi+\pi^{2}y^{2}}=\frac{-2\pi(y+y^{2})}{\pi(1+\pi y^{2})}\frac{Not fn}{8\pi}$$

$$\frac{N_2 - My}{M} = \frac{1 + 2xy^2 - 1 + 2xy}{1 - xy^2} = \frac{2xy(y+1)}{y(1-xy)} \frac{Ndy}{dy}$$

Rearranging 
$$ydn - xy^2dn + xdy + x^2y^2dy = 0$$
  
 $ydn + xdy - xy^2dn + x^2y^2dy = 0$   
 $x + x + by x$   $ydn + xdy - x^2y^2(\frac{dx}{x}) + x^2y^2dy = 0$   
 $ydn + xdy - x^2y^2(\frac{dx}{x} - dy) = 0$ 

+ by n'y mbth 
$$\frac{y dn + i dy}{x^2 y^2} - \frac{i x^2}{x^2 y^2} \left( \frac{dx}{x} - dy \right) = 0$$

$$d\left(-\frac{1}{xy}\right) - \frac{dx}{x} + dy = 0$$

$$\text{Intyrety} \quad -\frac{1}{xy} - \ln|x| + y = 0$$

from 
$$0$$
  $xdy-ydn = (x+y')dn$ 

$$\int \frac{xdy-ydn}{x^2+y^2} = \int dx$$

$$tan(x) = \cdot x+c$$

$$(x+y) = tan(x+c)$$

$$y = x tan(x+c) Ans$$

