

Merge Sort :

Algorithm MergeSort(l, h) $\leftarrow T(n)$

{

if ($l < h$)

{

mid = $(l+h)/2$; $\leftarrow 1$

MergeSort(l, mid); $\leftarrow T(n/2)$

MergeSort($mid+1, h$); $\leftarrow T(n/2)$

Merge(l, mid, h); $\leftarrow n$

}

}

$$T(n) = 2T(n/2) + n$$

$$T(n) = 2T\left(\frac{n}{2}\right) + n$$

$$a=2$$

$$b=2$$

$$k=1$$

$$p=0$$

$$a = b^k, p > -1$$

$$\Rightarrow T(n) = n^{\log_b a} \log_b^{p+1} n$$

$$= n \log n$$

$$T(n) = aT\left(\frac{n}{b}\right) + \theta(n^k \log_b^p n)$$

$$a > b^k \Rightarrow T(n) = \theta(n^{\log_b a})$$

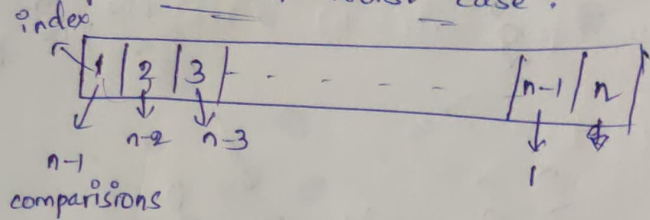
$$a = b^k \begin{cases} p > -1 \Rightarrow n^{\log_b a} \log_b^{p+1} n \\ p = -1 \Rightarrow n^{\log_b a} \log \log n \\ p < -1 \Rightarrow n^{\log_b a} \end{cases}$$

$$a < b^k \begin{cases} p > 0 \Rightarrow n^k \log_b^p n \\ p \leq 0 \Rightarrow n^k \end{cases}$$

Bubble sort:

```
for (i = 0; i < n-1; i++)  
{  
    for (j = 0; j < n-i; j++)  
    {  
        if (A[j] > A[j+1])  
        {  
            temp = A[j];  
            A[j] = A[j+1];  
            A[j+1] = temp;  
        }  
    }  
}
```

Comparisons in worst case:



$$= (n-1) + (n-2) + \dots + 2 + 1$$

$$= \frac{(n-1)(n)}{2} \Rightarrow O(n^2) \rightarrow \text{Same in avg case}$$