

1. Write a C program to implement Red black tree.

Code:`#include <stdio.h>`

`#include <stdlib.h>`

`// Define colors`

`#define RED 1`

`#define BLACK 0`

`// Structure for a node in the Red-Black Tree`

`typedef struct RBNode {`

`int data;`

`int color; // RED or BLACK`

`struct RBNode *left, *right, *parent;`

`} RBNode;`

`// Function prototypes`

`RBNode* createNode(int data);`

`void rotateLeft(RBNode** root, RBNode* node);`

```
void rotateRight(RBNode** root, RBNode* node);
```

```
void insertFixUp(RBNode** root, RBNode* node);
```

```
void insertNode(RBNode** root, int data);
```

```
void inorderTraversal(RBNode* root);
```

```
void freeTree(RBNode* root);
```

```
// Create a new node with given data
```

```
RBNode* createNode(int data) {
```

```
    RBNode* newNode = (RBNode*)malloc(sizeof(RBNode));
```

```
    newNode->data = data;
```

```
    newNode->left = newNode->right = newNode->parent = NULL;
```

```
    newNode->color = RED; // New nodes are always red
```

```
    return newNode;
```

```
}
```

```
// Left rotation
```

```
void rotateLeft(RBNode** root, RBNode* node) {
```

```
    RBNode* rightChild = node->right;
```

```
node->right = rightChild->left;
```

```
if (rightChild->left != NULL) {
```

```
    rightChild->left->parent = node;
```

```
}
```

```
rightChild->parent = node->parent;
```

```
if (node->parent == NULL) {
```

```
    *root = rightChild;
```

```
} else if (node == node->parent->left) {
```

```
    node->parent->left = rightChild;
```

```
} else {
```

```
    node->parent->right = rightChild;
```

```
}
```

```
rightChild->left = node;
```

```
node->parent = rightChild;
```

```
}
```

```
// Right rotation
```

```
void rotateRight(RBNode** root, RBNode* node) {
```

```
    RBNode* leftChild = node->left;
```

```
    node->left = leftChild->right;
```

```
    if (leftChild->right != NULL) {
```

```
        leftChild->right->parent = node;
```

```
    }
```

```
    leftChild->parent = node->parent;
```

```
    if (node->parent == NULL) {
```

```
        *root = leftChild;
```

```
    } else if (node == node->parent->right) {
```

```
        node->parent->right = leftChild;
```

```
    } else {
```

```
node->parent->left = leftChild;  
  
}
```

```
leftChild->right = node;  
  
node->parent = leftChild;  
  
}
```

// Fix the Red-Black Tree after insertion

```
void insertFixUp(RBNode** root, RBNode* node) {  
  
    while (node != *root && node->parent->color == RED) {  
  
        if (node->parent == node->parent->parent->left) {  
  
            RBNode* uncle = node->parent->parent->right;  
  
  
            if (uncle != NULL && uncle->color == RED) {  
  
                node->parent->color = BLACK;  
  
                uncle->color = BLACK;  
  
                node->parent->parent->color = RED;  
  
                node = node->parent->parent;  

```

```

} else {

    if (node == node->parent->right) {

        node = node->parent;

        rotateLeft(root, node);

    }

    node->parent->color = BLACK;

    node->parent->parent->color = RED;

    rotateRight(root, node->parent->parent);

}

} else {

    RBNode* uncle = node->parent->parent->left;

    if (uncle != NULL && uncle->color == RED) {

        node->parent->color = BLACK;

        uncle->color = BLACK;

        node->parent->parent->color = RED;

        node = node->parent->parent;

    } else {

```

```

        if (node == node->parent->left) {

            node = node->parent;

            rotateRight(root, node);

        }

        node->parent->color = BLACK;

        node->parent->parent->color = RED;

        rotateLeft(root, node->parent->parent);

    }

}

}

(*root)->color = BLACK;

}

```

// Insert a new node into the Red-Black Tree

```

void insertNode(RBNode** root, int data) {

    RBNode* newNode = createNode(data);

    RBNode* parent = NULL;

```

```
RBNode* current = *root;
```

```
while (current != NULL) {
```

```
    parent = current;
```

```
    if (data < current->data) {
```

```
        current = current->left;
```

```
    } else {
```

```
        current = current->right;
```

```
    }
```

```
}
```

```
newNode->parent = parent;
```

```
if (parent == NULL) {
```

```
    *root = newNode;
```

```
} else if (data < parent->data) {
```

```
    parent->left = newNode;
```

```
} else {
```



```

    parent->right = newNode;

}

insertFixUp(root, newNode);

}

// Inorder traversal of the Red-Black Tree

void inorderTraversal(RBNode* root) {

    if (root != NULL) {

        inorderTraversal(root->left);

        printf("%d (%s) ", root->data, root->color == RED ? "RED" :
"BLACK");

        inorderTraversal(root->right);

    }

}

// Free the memory allocated for the Red-Black Tree

void freeTree(RBNode* root) {

```

```
    if (root != NULL) {  
  
        freeTree(root->left);  
  
        freeTree(root->right);  
  
        free(root);  
  
    }  
}  
  
// Main function to demonstrate Red-Black Tree operations  
  
int main() {  
  
    RBNode* root = NULL;  
  
  
    insertNode(& root, 10);  
  
    insertNode(& root, 20);  
  
    insertNode(& root, 30);  
  
    insertNode(& root, 15);  
  
    insertNode(& root, 25);  
  
  
    printf("Inorder Traversal of Red-Black Tree:\n");
```

```
inorderTraversal(root);

printf("\n");

freeTree(root);

return 0;

}
```

Output:Inorder Traversal of Red-Black Tree:

10 (BLACK) 15 (RED) 20 (BLACK) 25 (RED) 30 (BLACK)

2 .Write a C program to implement the Splay tree.

Code:`#include <stdio.h>`

`#include <stdlib.h>`

`// Node structure for the splay tree`

`typedef struct Node {`

`int key;`

`struct Node* left;`

`struct Node* right;`

```
} Node;
```

```
// Function to create a new node
```

```
Node* createNode(int key) {
```

```
    Node* newNode = (Node*)malloc(sizeof(Node));
```

```
    newNode->key = key;
```

```
    newNode->left = NULL;
```

```
    newNode->right = NULL;
```

```
    return newNode;
```

```
}
```

```
// Function to perform right rotation
```

```
Node* rightRotate(Node* root) {
```

```
    Node* newRoot = root->left;
```

```
    root->left = newRoot->right;
```

```
    newRoot->right = root;
```

```
    return newRoot;
```

```
}
```

// Function to perform left rotation

Node* leftRotate(Node* root) {

Node* newRoot = root->right;

root->right = newRoot->left;

newRoot->left = root;

return newRoot;

}

// Splay function to bring the key to the root

Node* splay(Node* root, int key) {

if (root == NULL || root->key == key) {

return root;

}

if (key < root->key) {

if (root->left == NULL) return root;

```

// Key is in the left subtree

if (key < root->left->key) {

    // Zig-Zig (Left Left)

    root->left->left = splay(root->left->left, key);

    root = rightRotate(root);

} else if (key > root->left->key) {

    // Zig-Zag (Left Right)

    root->left->right = splay(root->left->right, key);

    if (root->left->right != NULL) {

        root->left = leftRotate(root->left);

    }

}

return (root->left == NULL) ? root : rightRotate(root);

} else {

    if (root->right == NULL) return root;

    // Key is in the right subtree

    if (key > root->right->key) {

```

```

    // Zig-Zig (Right Right)

    root->right->right = splay(root->right->right, key);

    root = leftRotate(root);

} else if (key < root->right->key) {

    // Zig-Zag (Right Left)

    root->right->left = splay(root->right->left, key);

    if (root->right->left != NULL) {

        root->right = rightRotate(root->right);

    }

}

return (root->right == NULL) ? root : leftRotate(root);

}

}

```

// Function to insert a new key

```

Node* insert(Node* root, int key) {

    if (root == NULL) return createNode(key);

```

```
root = splay(root, key);
```

```
if (root->key == key) return root;
```

```
Node* newNode = createNode(key);
```

```
if (key < root->key) {
```

```
    newNode->right = root;
```

```
    newNode->left = root->left;
```

```
    root->left = NULL;
```

```
} else {
```

```
    newNode->left = root;
```

```
    newNode->right = root->right;
```

```
    root->right = NULL;
```

```
}
```

```
return newNode;
```

```
}
```


// Function to search for a key

```
Node* search(Node* root, int key) {  
  
    return splay(root, key);  
  
}
```

// Function to find the minimum value in the splay tree

```
Node* findMin(Node* root) {  
  
    while (root->left != NULL) root = root->left;  
  
    return root;  
  
}
```

// Function to delete a key

```
Node* delete(Node* root, int key) {  
  
    if (root == NULL) return NULL;  
  
  
    root = splay(root, key);
```

```
if (key != root->key) return root;
```

```
Node* temp;
```

```
if (root->left == NULL) {
```

```
    temp = root;
```

```
    root = root->right;
```

```
} else {
```

```
    temp = root;
```

```
    Node* newRoot = splay(root->left, key);
```

```
    newRoot->right = root->right;
```

```
    root = newRoot;
```

```
}
```

```
free(temp);
```

```
return root;
```

```
}
```

```
// Function to print the tree in-order
```

```
void inorder(Node* root) {  
  
    if (root == NULL) return;  
  
    inorder(root->left);  
  
    printf("%d ", root->key);  
  
    inorder(root->right);  
  
}
```

```
// Main function for testing
```

```
int main() {  
  
    Node* root = NULL;  
  
  
    // Insert elements  
  
    root = insert(root, 10);  
  
    root = insert(root, 20);  
  
    root = insert(root, 30);  
  
    root = insert(root, 40);  
  
    root = insert(root, 50);  
  
    root = insert(root, 25);
```

```
// Print in-order traversal
```

```
printf("In-order traversal: ");
```

```
inorder(root);
```

```
printf("\n");
```

```
// Search for a key
```

```
root = search(root, 20);
```

```
printf("Root after searching for 20: %d\n", root->key);
```

```
// Delete a key
```

```
root = delete(root, 30);
```

```
printf("In-order traversal after deleting 30: ");
```

```
inorder(root);
```

```
printf("\n");
```

```
return 0;
```

$$\}$$

Output: In-order traversal: 10 20 25 30 40 50

Root after searching for 20: 20

In-order traversal after deleting 30: 10 20 25 40 50