Simulate co-transcriptional folding kinetics by genetic algorithm

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We developed a genetic algorithm based approach to simulate kinetics of co-transcriptional folding. Our method is built on two following assumptions:

- 1 All populated RNA secondary structures (SS) are linkage of locally optimal or sub-optimal structures at various folding sites;
- 2 Global structural rearrangement of a partial RNA segment is permitted only if it's folding to the optimal SS on that segment.

Formally, we denote a domain $D_{A,B}$ as a segment between base A and B that all contacts on that segment are local. For simplicity, we denote **foldon** as domains with optimal secondary structures: $D_{A,B}^{foldon} = \text{MFE}(\text{sequence}[A,B])$. Note that '.' is a trival example of foldon. Our assumption 1 can be rewritten as

$$D_{A,B} = D_{A,i_1}^{foldon} \oplus D_{i_1,i_2}^{foldon} \oplus \dots \oplus D_{i_n,B}^{foldon}$$

$$\tag{1}$$

Where \oplus represents a link operation. Note that all structural information of $D_{A,B}$ is encoded by the sequential representation $[A, i_1, ..., i_n, B]$; as a foldon is also a linkage of smaller foldons, there could be multiple way to represent $D_{A,B}$. Here we introduce **Irreducible Foldon Representation** (IFR) as sequential representations for which linkage of every adjacent foldons is not another foldon: $\forall k, D_{i_k,i_{k+1}}^{foldon} \oplus D_{i_{k+1},i_{k+2}}^{foldon} \neq D_{i_k,i_{k+2}}^{foldon}$. Then the sufficient and nessary condition for structural rearrangement is

$$\begin{split} \langle D^u_{A,\,B} | \hat{\mathbf{T}} | D^v_{A,\,B} \rangle &\neq 0 \text{ if and only if } \exists \, i, \, j \text{ satisfies} \\ i, \, j \in D^u_{A,\,B}. \text{IFR}, \, i, \, j \in D^v_{A,\,B}. \text{IFR}; \\ D^u_{A,\,i} &= D^v_{A,\,i}, \, D^u_{j,\,B} = D^v_{j,\,B}; \\ D^u_{i,\,j} &= D^{foldon}_{i,\,j} \text{ or } D^v_{i,\,j} = D^{foldon}_{i,\,j}. \end{split}$$
 Then
$$\langle D^u_{A,\,B} | \hat{\mathbf{T}} | D^v_{A,\,B} \rangle = \langle D^u_{i,\,j} | \hat{\mathbf{T}} | D^v_{i,\,j} \rangle. \end{split}$$

1 Algorithm procedure

During every elongation step, an active species pool of strands with unique SS and diffrent population is updated. New candidate strands $D_{0,L+\Delta L}^{Candidate}$ with length $L+\Delta L$ are generated by a recombination process: for every old strand $D_{0,L}^{Strand}$, all indices in its IFR is identified as possible rearrangement site, then its child strands is generated by linking partial domains $D_{0,\text{Site}}^{Strand}$ with a foldon $D_{\text{Site},L+\Delta L}^{foldon}$ that terminated at $L+\Delta L$.

We assume that elongation will not change the inital population distribution of secondary structures: child strands with the exact parental SS on [0, L] $(D_{0,L+\Delta L}^{child} = D_{0,L}^{strand} \oplus D_{L,L+\Delta L}^{foldon})$ will also inherit the population of their parents.

After structual generation the rate matrix among all candidate strands within the new active species pool is calculated. Then the population distribution of strands after elongation is computed by chemical master equation, and one iterative elongation step is finished.

Pseudocodes of the procedure are as follows:

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Algorithm 1 Co-transcriptional folding elongation procedure
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1: Initalize ActivePool
 2: while sequence length > current length do
           OldPool \leftarrow ActivePool
 3:
          renew ActivePool
 4:
           Current length \leftarrow Current length + dL
 5:
           dt \leftarrow dL / Transcription rate
 6:
           for left boundary \in \{0, dL, 2dL, ..., Current length - dL\} do
                                                                                                                  ▶ Get all new foldons
 7:
                D_{\text{left boundary, Current length}}^{foldon} \leftarrow \text{numpy.mfe}(\text{sequence}[\text{left boundary, Current length}])
 8:
 9:
          end for
           for Strand \in OldPool do
                                                                                                                         ▶ Recombination
10:
                for Site \in Strand.IFR do
11:
                      D^{Candidate}_{0,\text{Current length}} \leftarrow D^{Strand}_{0,\text{ Site}} \oplus D^{foldon}_{\text{Site, Current length}}
12:
                     if D_{0,\text{Current length}}^{Candidate} \in \text{ActivePool} then
13:
                           update D_{0,\text{Current length}}^{Candidate}.IFR
14:
                     else
15:
                           add D_{0,\text{Current length}}^{Candidate} to ActivePool
16:
                     end if
17:
                     if site = Current length -dL then
18:
                           \langle \text{ActivePool.} \mathbf{population} \, | D_{0,\text{Current length}}^{Candidate} \rangle \leftarrow \langle \text{OldPool.} \mathbf{population} \, | D_{0,\text{Site}}^{Strand} \rangle
19:
                     end if
20:
21:
                end for
           end for
22:
          \textbf{for } D^{\mathrm{u}}_{0,\mathrm{Current \ length}} \neq D^{\mathrm{v}}_{0,\mathrm{Current \ length}} \in \mathrm{ActivePool} \ \textbf{do} \qquad \triangleright \ \mathrm{Calculate \ new \ rate \ matrix}
23:
                calculate D_{\text{rearrange}}^u, D_{\text{rearrange}}^v
                                                                               ▶ Find all helices involved in rearrangement
24:
                \langle D_{\text{rearrange}}^{u} | \hat{\mathbf{T}} | D_{\text{rearrange}}^{v} \rangle \leftarrow k_0 \exp \left( -\frac{1}{RT} (\Delta G_u^{Stack} + \Delta G_v^{Loop}) \right)
25:
26:
           \langle \text{ActivePool.population} | \leftarrow \langle \text{ActivePool.population} | \exp(\hat{\mathbf{T}})
                                                                                                                       ▶ Master equation
27:
          reserve top N populated strands in ActivePool
28:
                                                                                                                                   ▶ Selection
          renormalize (ActivePool.population)
29:
30: end while
```