

Field Trip Assignment

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18EX20030

- ① We can observe that first reflecting surface is encountered by geophone placed at 40 metres.

Thus, using data for geophone at $x=40\text{m}$ and $x'=43\text{m}$, the wave time

$T=80\text{ms}$ and $T'=90\text{ms}$ respectively.

From above given equations, $T'^2 - T^2 = (x'^2 - x^2)/V^2$

$$\Rightarrow V = \sqrt{((x'^2 - x^2)/(T'^2 - T^2))}$$

$$\Rightarrow V = \sqrt{\{(43)^2 - (40)^2\} / \{(90)^2 - (80)^2\}} \text{ m/s.}$$

$$\Rightarrow V = 3827.1476 \text{ m/s}$$

Formula for 'h' is :

$$h = \sqrt{(V^2 \times T^2 - x^2)} / 2$$

$$\Rightarrow h = (\sqrt{(3827.1476)^2 (80/1000)^2 - (40)^2}) / 2$$

$$\Rightarrow h = 151.77\text{m}$$

We are given with the
shot offset $x = 34\text{m}$ and
Geophone interval $= 48\text{m}$.

Three prominent reflections are indicated
by arrows.

$$T_1 = 450\text{ms},$$

$$V_1 = (34/450/1000)\text{m/s} = 75\text{m/s}.$$

$$T_2 = 500\text{ms},$$

$$V_2 = (34/500/1000)\text{m/s} = 68\text{m/s}.$$

$$T_3 = 650\text{ms}.$$

$$V_3 = (34/650/1000)\text{m/s} = 52\text{m/s}.$$

Assuming these are the only reflections
present.

$$\text{Velocity} = \text{Displacement} / \text{Time}$$

Here distances are starting from

34, 82, 130, 178, 226, 274, 322, 370 and 418

V_{RMS} \rightarrow For multiple flat layers and
assuming the offset is small compared
with the depth, a hyperbolic moveout
equation can be derived as a
truncated power series in which V_{RMS}
is used as velocity. Root-mean-square
velocity is calculated from interval velocities

$$V_{\text{RMS}} = \sqrt{V_1^2 \cdot t_1 + V_2^2 \cdot t_2 + \dots + V_n^2 \cdot t_n} / (t_1 + t_2 + \dots + t_n)$$

$$\Rightarrow V_{\text{RMS}} = \sqrt{(75^2 \times 0.45 + 68^2 \times 0.5 + 52^2 \times 0.65) / (450 + 500 + 650)}$$

$$\Rightarrow V_{\text{RMS}} = \sqrt{(2531 + 2312 + 1757) / 1600} = 2$$

$V_{int} \rightarrow$ The constant velocity of a single layer (which can be very different) calculated from V_{rms} using Dix equation.

$$V_{int} = \left[\frac{t_2 V_{rms}^2 - t_1 V_{rms}^2}{(t_2 - t_1)} \right]$$

Where V_{int} = Interval velocity
 t_1 = travel time to first reflector
 t_2 = travel time to second reflector
 V_{rms1} = root-mean-square velocity to the first reflector

V_{rms2} = root-mean-square velocity to the second reflector

Thickness,

$$z = 0.5 \times \sqrt{(t^2 v^2 - x^2)}$$

$$z_1 = 0.5 \times \sqrt{(0.45)^2 - (34)^2} \quad \sqrt{0.45 \times (75)^2 - (34)^2}$$

$$\Rightarrow z_1 = 2 \text{ km}$$

$$z_2 = 0.5 \times 5 = 2.5 \text{ km}$$

$$z_3 = 0.5 \times 6 = 3 \text{ km}$$

From t - d curve,

$$t^2 = \frac{(x - 2j \sin \beta)^2}{v^2} + \frac{4j^2 \cos^2 \beta}{v^2}$$

$$t_{\min} = \frac{2j \cos \beta}{v}$$

~~$\Rightarrow \cos \beta = \frac{t_{\min} v}{2j}$~~

$$t_0 = \frac{2j}{v}$$

$$\Rightarrow \cos \beta = \frac{t_{\min}}{t_0}$$

$$x_{\min} = 2j \sin \beta \Rightarrow j = \frac{x_{\min}}{2j \sin \beta}$$

$$v = \frac{2j \cos \beta}{t_{\min}}$$

Selected values and computed answers

$t - zero (ms)$	51.3	$\beta (^\circ)$	-9.1
$t - min (ms)$	50.6	Thickness (m)	44.8
$x - min (m)$	14.0	velocity (m/s)	1727.5

Actual input used to produce graph values

Velocity (m/s)	1725
Thickness (m)	45
Dip ($^\circ$)	-9

⑤ We take S at $x=0$ as the source and the geophone at $x=12\text{km}$ as R . Four wave trains are observed. The slowest has an apparent velocity of about 1.4km/s , the arrival time at R is off-scale. This is the direct water wave, but its velocity is low for water perhaps because of interference with a dispersive channel is not exact. Measured data are:-

$$L: V_L = 1.7\text{km/s}, t_{RL} = 6.84\text{s}, t_{iL} = ?$$

$$M: V_M = 2.67\text{km/s}, t_{RM} = 5.38\text{s}, t_{iM} = 0.95\text{s}.$$

$$N: V_N = 5.45\text{km/s}, t_{RN} = 3.97\text{s}, t_{iN} = 1.77\text{s}.$$

if L is a head wave, the intercept time should be $(6.84 - 12/1.70) = 0.22\text{s}$. Thus we conclude that L is not a head wave from a planar refractor. it may be a dispersive water wave or part of a reflection but we have insufficient data to identify it. Disregarding L , we are left with only water layer and two refractors M and N .

(i) Assuming no-dip

Refraction M

We have following data

$$V_1 = 1.5 \text{ km/s}, \quad V_m = 2.67 \text{ km/s}, \quad t_{im} = 0.95 \text{ s.}$$

Then,

$$\sin \theta_c / 1.5 = 1/2.67$$

$$\Rightarrow \theta_c = 34.2^\circ$$

$$h_m = V_1 t_{im} / 2 \cos \theta_c = 1.50 \times 0.95 / 2 \times \cos 34.2^\circ = 0.82 \text{ km}$$

Refraction N:

$$\sin \theta_1 / 1.50 = \sin \theta_c / 2.67 = 1/5.45 \Rightarrow \theta_1 = 16^\circ, \theta_c = 29.3^\circ$$

$$1.77 = 2 \times 0.82 \cos 16^\circ / 1.50 + 2h_2 \cos 29.3^\circ / 2.67$$

$$\Rightarrow h_2 = (1.77 - 1.10) / 0.65 = 0.67 / 0.65 = 1.03 \text{ km}$$

$$Z_N = 0.83 + 1.03 = 1.86 \text{ km}$$

(ii) Assuming 5° dip to the right

In this case, the profile is in the down-dip direction, the arrival times, velocities and intercept times are all unchanged except that the velocities are now apparent velocities and the intercept time gives start depths normal to the bed.

Refraction M

We have, $V_1 = 1.5 \text{ km/s}$, $V_{am} = 2.67 \text{ km/s}$, $\theta_1 = 5^\circ$.

$$t_{im} = 0.95 \text{ s.}$$

$$\sin(\theta_c + 5^\circ) = V_1 / V_{am} = 1.50 / 2.67$$

$$\Rightarrow \theta_c + 5^\circ = 34.2^\circ \Rightarrow \theta_c = 29.2^\circ$$

$$V_m = V_1 / \sin \theta_c = 1.5 / \sin 29.2^\circ = 3.07 \text{ km/s}$$

$$h_m = V_1 t_{im} / 2 \cos \theta_c = 1.5 \times 0.95 / 2 \cos 29.2^\circ = 0.82 \text{ km}$$

Refractor N

Using Adachi's method, but given data are not in form suitable for it. Instead we shall step off the surface layer after which we have 2 parallel surface horizon - and therefore slant depth of horizon M at the source S is 0.82 km. At R, slant depth is

$$RM = 0.82 + 12 \sin 5^\circ = 1.87 \text{ km.}$$

Thus to locate horizon M we swing arc at S and R with radii 0.82 and 1.87 km respectively then draw horizon M tangent to arc.

$$\sin \alpha = V_1 (\Delta t / \Delta x) = V_1 / V_{AN} = 1.50 / 5.45$$

$$\Rightarrow \alpha = 16.0^\circ$$

$$\theta + 5^\circ = 16.0^\circ$$

$$\theta - 5^\circ = \theta^\circ$$

Total length = $SS' + RR' = (0.8 + 1.8) \text{ km}$
dividing by 1.5 gives 1.73 s to be subtracted from t_N , leaving $t_{N'} = 3.97 - 1.73$
= 2.24 s for the travel time relative to M.
Also the distance $S'R' = x' = 11.5 \text{ km}$. The intercept time for both M and N are based on the normal to the beds since the beds are parallel we can subtract time from t_N to get $t_{N'}$, the intercept time of N for virtual source S' .

$$t_{N'} = (1.77 - 0.95) \text{ s} = 0.82 \text{ s.}$$

We must correct apparent velocity

$V_{AN} = 5.45 \text{ km/s}$. We write this as $1/5.45$
 $= \Delta t / \Delta x = 2.20 / 12.03 \text{ km}$. The event N is direct
from $x=12$ to beyond $x=6 \text{ km}$ so we
write $1/5.45 = 0.110/6 \text{ s/km}$. The numerator is
difference between t_N at $x=12$ and 6 km
correction is $RT = 0.50/1.50 = 0.338$.

$\Delta t' = 1.10 - 0.33 = 0.77 \text{ s}$. Correction to Δx
is negligible so we get $V_N = 6/0.77 = 7.79 \text{ km/s}$
We can now get the depth of N below
M, we have,

$$\theta_c = \sin^{-1}(V_M - V_N) = 3.07/7.79 = 23.3^\circ$$

Because horizons M and N are parallel
we find intercept time of N relative to
M by subtracting the intercept time in
part (i) so

$$t_{iN'} = 1.77 - 0.95 = 0.82 \text{ s}$$

Thus,

$$h_{N'} = 3.07 \times 0.82 / 2 \cos 23.3^\circ = 1.37 \text{ km}$$

Since depth of M at S is 0.82 km .

$$Z_N = 0.82 + 1.37 = 2.19 \text{ km (slant depth at S')}$$

(iii) Because of shallow depth of M we check
to see where it outcrops - the horizon M
passes through the point $(x, z) = (0, 0.82 \cos 5^\circ)$
 $= (0, 0.817)$. Thus it will outcrop at

$$x = 0.817 / \tan 5^\circ = 9.34 \text{ km (in part (i) slope } \tan 5^\circ)$$

Event M exists at offset of 12 km hence
assumption of 5° dip to the left is
not consistent with given data.